1 CALIBRATING ELECTROMAGNETIC INDUCTION CONDUCTIVITIES WITH TIME-DOMAIN

2 **REFLECTOMETRY MEASUREMENTS**

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16 Abstract

17 This paper deals with the issue of monitoring the spatial distribution of bulk electrical 18 conductivity σ_{b_r} in the soil root zone by using Electromagnetic Induction (EMI) sensors under 19 different water and salinity conditions. To deduce the actual distribution of depth-specific $\sigma_{\rm b}$ 20 from EMI apparent electrical conductivity (EC_a) measurements, we inverted the data by using a 21 regularized 1D inversion procedure designed to manage nonlinear multiple EMI-depth 22 responses. The inversion technique is based on the coupling of the damped Gauss-Newton 23 method with truncated generalized singular value decomposition (TGSVD). The ill-posedness of 24 the EMI data inversion is addressed by using a sharp stabilizer term in the objective function.

25 This specific stabilizer promotes the reconstruction of blocky targets, thereby contributing to 26 enhance the spatial resolution of the EMI results in presence of sharp boundaries (otherwise 27 smeared out after the application of more standard, Occam-like regularization strategies 28 searching for smooth solutions). Time-Domain Reflectometry (TDR) data are used as ground-29 truth data for calibration of the inversion results. An experimental field was divided into four 30 transects 30 m long and 2.8 m wide, cultivated with green bean and irrigated with water at two 31 different salinity levels and using two different irrigation volumes. Clearly, this induced 32 different salinity and water contents within the soil profiles. For each transect, 26 regularly 33 spaced monitoring soundings (1 m apart) were selected for the collection of, respectively: (i) 34 Geonics EM-38 and (ii) Tektronix Reflectometer data. Despite the original discrepancies in the 35 EMI and TDR data, we found a significant correlation of the means and standard deviations of 36 the two data series, in particular, after a low-pass spatial filtering of the TDR data. Based on 37 these findings, the paper introduces a novel methodology to calibrate EMI-based electrical 38 conductivities via TDR direct measurements. This calibration strategy consists in a linear 39 mapping of the original inversion results into a new conductivity spatial distribution with the 40 coefficients of the transformation uniquely based on the statistics of the two original 41 measurement datasets (EMI and TDR conductivities).

42

43 Introduction

Soil water content and salinity vary in space both vertically and horizontally. Their distribution depends on management practices and on the complex nonlinear processes of soil water flow and solute transport, resulting in variable storages of solutes and water (Coppola et al. 2015). Monitoring the actual distribution of water and salts in the soil profile explored by roots is crucial for managing irrigation with saline water, while still maintaining an acceptable crop

49 yield. For water and salts monitoring over large areas, there are now non-invasive techniques 50 based on electromagnetic sensors which allow the bulk electrical conductivity of soils σ_b to be 51 determined (Sheets and Hendrickx 1995, Corwin and Lesch 2005, Robinson et al. 2012, 52 Doolittle and Brevik 2014, Von Hebel et al. 2014, among many others).

53 $\sigma_{\rm b}$ depends on: (i) soil water content θ ; (ii) electrical conductivity of the soil solution (salinity) 54 $\sigma_{\rm w}$; (iii) tortuosity of the soil-pore system τ ; and (iv) other factors related to the solid phase such 55 as bulk density, clay content and mineralogy.

56 Electromagnetic induction (EMI) sensors provide measurements of the depth-weighted 57 apparent electrical conductivity EC_a accordingly to the specific distribution of the bulk electrical 58 conductivity σ_b as well as the depth response function of the sensor used (McNeill 1980). Thus, 59 the dependence on $\sigma_{\rm b}$ makes EC_a sensitive to soil salinity and water distributions. In principle, 60 specific procedures for estimating salinity and water content may be developed through 61 controlled laboratory experiments where σ_b , σ_w and θ are measured simultaneously (Rhoades 62 and Corwin 1981). That said, to monitor salinity and water content, it is crucial to correctly infer 63 the depth-distribution of σ_b from profile-integrated EC_a readings. To date, this issue has been 64 tackled by applying two different strategies: The first is to use empirical calibration relations 65 relating the depth-integrated EC_a readings to the σ_b values measured by alternative methods -66 like Time-Domain Reflectometry (TDR) - within discrete depth intervals (Rhoades and Corwin 67 1981, Lesch et al. 1992, Triantafilis, Laslett, and McBratney 2000, Amezketa 2006, Yao and Yang 68 2010, Coppola et al. 2016); The second consists in the 1D inversion of the observations from 69 the EMI sensor to reconstruct the vertical conductivity profile (Borchers, Uram, and Hendrickx 70 1997, Hendrickx et al. 2002, Santos et al. 2010, Lavoué et al. 2010, Mester et al. 2011, Minsley 71 et al. 2012, Deidda, Fenu, and Rodriguez 2014, Von Hebel et al. 2014).

72 With regard to EC_a inversion, a forward model still commonly used is the cumulative response 73 model or local-sensitivity model (LSM) (McNeill 1980). McNeill's linear approach is well suited 74 to the cases characterized by an induction number B (defined as the ratio between the coil 75 distance and the skin depth) much smaller than 1. However, because of the increasing 76 computing power, improved forward modeling algorithms based on more accurate nonlinear 77 approaches are becoming increasingly common (Hendrickx et al. 2002, Deidda, Fenu, and 78 Rodriguez 2014, Deidda, Bonomi, and Manzi 2003, Lavoué et al. 2010, Santos et al. 2010). For 79 example, these more sophisticated forward modeling codes can cope with a wider range of 80 conductivities for which the assumption B<<1 is not necessarily met.

81 To obtain reliable vertical distributions of electrical conductivity, the EC_a data used for the 82 inversion should consist of multi-configuration data. Hence, data collection should be 83 performed either with the simultaneous use of different sensors or with different acquisition 84 configurations with only one sensor (different configurations may consist, e.g., in different coil 85 orientations, varying intercoil separations and/or frequencies – see, for example Díaz de Alba and Rodriguez, 2016). Multi-configuration data can be effectively used to invert for vertical 86 87 electrical conductivity profiling since the EC_a measures actually investigate different, 88 overlapping soil volumes. Devices specifically designed for the simultaneous acquisition of 89 multi-configuration data are currently available. Some of them consist of one transmitter and 90 several receivers with different coil separations and orientations (Santos et al. 2010). If, 91 instead, a sensor with single intercoil distance and frequency is available, a possible alternative 92 to having multi-configuration measurements could be to record the data at different heights 93 above the ground.

94 Unfortunately, like every other physical measurement, frequency-domain electromagnetic 95 measurements are sensitive to noise that is very hard to model effectively. Moreover as

96 discussed, for example, in Lavoué et al. (2010), Mester et al. (2011), and Von Hebel et al. 97 (2014), an instrumental shift in conductivity values could be observed due to system 98 miscalibration and the influence of surrounding conditions such as temperature, solar 99 radiation, power supply conditions, the presence of the operator, zero-leveling procedures, 100 cables close to the system and/or the field setup (see, amongst others, Sudduth, Drummond, 101 and Kitchen 2001; Robinson et al. 2004; Abdu, Robinson, and Jones 2007; Gebbers et al. 2009; 102 Nüsch et al. 2010). Hence, the EC_a data from EMI measurements would generally require a 103 proper calibration. One option could be to use soil cores as ground-truth data. In this case, EC_a 104 measurements at the sampling locations can be compared against EC_a data predicted by the 105 theoretical forward response applied to the true electrical conductivity distribution measured 106 directly on the soil cores (Triantafilis, Laslett, and McBratney 2000, Moghadas et al. 2012). 107 Clearly, this strategy is extremely time- (and resource-) consuming. To avoid drilling, Lavoué et 108 al. (2010) introduced a calibration method, later also adopted by Mester et al. (2011) and Von 109 Hebel et al. (2014), using the electrical conductivity distribution obtained from Electrical 110 Resistivity Tomography (ERT) data as input for electromagnetic forward modeling. The EC_a 111 values predicted on the basis of ERT data were used to remove the observed instrumental shift 112 and correct the measured conductivity values by linear regression. However, in general, a 113 prerequisite for such an approach concerns the reliability of the inversion of the ERT result. This 114 is not only due to the quality of the original data, but also the adopted inversion procedure. 115 Indeed, ERT inversion is an ill-posed problem: its solutions are characterized by non-uniqueness 116 and instability with respect to the input data (Yu and Dougherty 2000; Zhdanov 2002; Günther 117 2011). In the Tikhonov regularization framework, ill-posedness is addressed by including the 118 available prior information. Such information can be very general. For example, it can be 119 geometrical (i.e., associated to the presence of smooth or sharp boundaries between different

lithologies). Obviously, the final result largely reflects the initial guess formalized via the chosen
regularization term (Pagliara and Vignoli 2006; Günther 2011; Vignoli, Deiana, and Cassiani
2012; Fiandaca et al. 2015).

123 When relatively shallow depths have to be explored (1-2m), direct soil sampling and ERT can be 124 effectively replaced by TDR observations. TDR devices are designed to measure the dielectric 125 properties of soils. More precisely, they measure the apparent electrical permittivity, from 126 which, not only the dielectric constant, but also the effective electrical conductivity can be 127 deduced (e.g., Dalton et al. 1984; Topp et al. 1988; Weerts et al. 2001; Noborio 2001; Jones et 128 al. 2002; Robinson et al. 2003; Lin et al. 2007; Thomsen et al. 2007; Huisman et al. 2008; Lin et 129 al. 2008; Koestel et al. 2008; Bechtold et al. 2010). In general, TDR measurements might be 130 difficult to be used to recover the electrical conductivity with the desired accuracy. However, in 131 the literature, many examples are reported in which, within the range 0.002 - 0.2 S/m 132 (compatible with the examples investigated in the present research), and by properly using the 133 TDR device (e.g., by paying attention to minimize the effects of nonparallel device rods 134 inserted into the ground), the TDR conductivity can be measured with an uncertainty level 135 lower than 5% (e.g.: Huisman et al., 2008; Bechtold et al., 2010). Besides, since the TDR 136 measurements are commonly calibrated in saline solutions just before the field data 137 acquisitions, they could potentially provide a reliable, absolute estimation of the actual ground 138 conductivity (Ferré et al., 1998a). For this reason, in some cases, TDR observations have been 139 proposed as a valid tool for ground-truthing the ERT and, possibly, as ancillary information 140 source to constraint for the ERT inversions (Koestel et al. 2008). For additional studies dealing 141 with the use of ERT data for the validation of the EMI and TDR measurements for soil 142 characterization we refer the reader to, for example, Cassiani et al. 2012 and Ursino et al. 143 2014.

144 In the present research, we focus on the use of TDR data to absolute calibrate the 145 conductivities obtained by inverting the EMI measurements. To do this, a dataset collected 146 during an experiment carried out along four transects under different salinity and water 147 content conditions (and monitored with both EMI and TDR sensors) is utilized. We first tackle 148 the problem of inferring the soil electrical conductivity distribution from multi-height EC_a 149 readings via the proper inversion strategy. Then we assess the quality of these reconstructions 150 by using TDR data as ground-truth. In this respect, in the following, we discuss how to 151 effectively compare the σ_b values generated by the EMI inversion with the associated TDR 152 values. In fact, as discussed by Coppola et al. 2016, because of their relatively smaller 153 observation volume, TDR data provide quasi-pointlike measurements and do not integrate the 154 small-scale variability (of soil water content, solute concentrations, etc.) induced by natural soil 155 heterogeneity. By contrast, EMI data necessarily overrule the small-scale heterogeneities seen 156 by TDR probes as they investigate a much larger volume. Accordingly, the paper provides a 157 methodology to calibrate EMI results by TDR readings. This procedure lies in conditioning the 158 original TDR data and in the statistical characteristics of the two EMI and TDR data series. On 159 the basis of the proposed analysis, we discuss the physical reasons for the differences between 160 EMI and TDR-based bulk electrical conductivity and identify a method to effectively migrate the 161 reliable TDR information across the larger volume investigated by EMI.

162

163 Materials and Methods

The experiment was carried out at the Mediterranean Agronomic Institute of Bari (MAIB) in south-eastern Italy. The soil was pedologically classified as Colluvic Regosol, consisting of a silty-loam layer of an average depth of 0.6 m on fractured calcarenite bedrock. The experimental set-up (Fig. 1) consisted of four transects of 30 m length and 2.8 m width,

168 equipped with a drip irrigation system with five dripper lines placed 0.35 m apart and 169 characterized by an inter-dripper distance of 0.2 m. The dripper discharge was 2 l/h. Green 170 beans were grown in each transect. The irrigation volumes were calculated according to the 171 time-dynamics of water content in the first 0.25 m measured by a TDR probe inserted vertically 172 at the soil surface. TDR readings were taken: (i) just before and (ii) two hours after every 173 irrigation. Based on the difference between the water content at field capacity and that 174 measured just before irrigation, it was easy to assess the volumes needed to bring the soil 175 water content back to the field capacity.

The four transects were irrigated with water at two different salinity levels and with two different water volumes. Transect 1: 100% of the irrigation water at 1 dSm⁻¹ (hereafter 100-1dS); Transect 2: 50% of irrigation water at 1 dSm⁻¹ (50-1dS); Transect 3: 100% of the irrigation water at 6 dSm⁻¹ (100-6dS); Transect 4: 50% of irrigation water at 6 dSm⁻¹ (50-6dS). Water salinity was induced by adding calcium chloride (CaCl₂) to tap water. Irrigation volumes were applied every two days.

EMI readings - in vertical magnetic dipoles configurations - were collected by using a Geonics EM38 device (Geonics Limited, Ontario, Canada). The EM38 operates at a frequency of 14.6 kHz with a coil spacing of 1 m, and with a nominal measurement depth of ~1.5 m (McNeill, 1980). The lateral footprint of the EM38 measurement can be considered approximately equal to the vertical one. Thus, the σ_b seen by the EMI, in a given depth-layer, necessarily differs from that seen by a TDR probe at the same depth-layer, due to the very different spatial resolutions.

At the beginning of the measurement campaign, the EMI sensor was "nulled" according to the manufacturer's manual. Readings were taken just after each irrigation application at 1 m step, along the central line of each transect, for an overall total of 26 soundings per transect. Multiheight EM38 readings were acquired at heights of 0.0, 0.2, 0.4 and 0.6 m from the ground.

Taking measurements just after irrigation allowed relatively time-stable water contents to beassumed at each site throughout the monitoring phases.

194 Just after the EM38 measurements, a TDR probe was inserted vertically at the soil surface in 26 195 locations, each corresponding to the central point of an EM38 reading. A Tektronix 1502C cable 196 tester (Tektronix Inc., Baverton, OR) was used in this study. It enables simultaneous 197 measurement of water content θ and bulk electrical conductivity $\sigma_{\rm b}$ of the soil volume explored 198 by the probe (Heimovaara et al. 1995; Robinson and Friedman 2003; Coppola et al. 2011; 199 Coppola et al. 2015). The TDR transmission line consisted of an antenna cable (RG58, 50 Ω 200 characteristic impedance, 2 m long and with 0.2 Ω connector impedance) and three-wire 201 probes, 0.25 m long, 0.07 m internal distance, and 0.005 m in diameter. The TDR probe was not 202 embedded permanently at fixed depths along the soil profile to avoid any potential disturbance 203 to the EMI acquisitions. The TDR readings were taken at three different depth intervals (0.0-204 0.2, 0.2-0.4, 0.4-0.6 m). After the measurements at the surface (0.0-0.2 m), a trench was dug up 205 to 0.2 m depth. TDR probes were then inserted vertically for the additional collection of the 206 data in the interval 0.2-0.4 m, after which the trench was deepened up to 0.4 m and readings 207 were taken at 0.4-0.6 m. The $\sigma_{b,TDR}$ readings were used for the calibration of the EM38 inversion 208 results.

209

210 Data Handling

211 Multi-height EMI readings inversion

Nonlinear 1D forward modeling, which predicts multi-height EMI readings from a loop-loop device, can be obtained by suitable simplification of Maxwell's equations that takes the symmetry of the problem into account. This approach is described in detail in (Hendrickx et al. 2002), and is based on a classical approach extensively described in the literature (Wait 1982;

Ward and Hohmann 1988). The predicted data are functions of the electrical conductivity andthe magnetic permeability in a horizontally layered medium.

When the coils of the recording device are vertically oriented with respect to the ground surface, the reading at height *h* can be expressed by using the integral:

$$-\rho^{3}\int_{0}^{\infty}\lambda^{2}e^{-2h\lambda}R_{0}(\lambda)J_{0}(\rho\lambda)d\lambda,$$
(1)

220 where ρ denotes the distance between the coils, $J_0(\lambda)$ is the Bessel function of the first kind 221 of order 0, and $R_0(\lambda)$ is a complex valued function which depends upon the electromagnetic 222 properties of the ground layers. A similar expression is valid also when the coils are horizontally 223 aligned. Hence the dependence of the measured data on the electrical conductivity σ_k , of the 224 (homogeneous) j-th layer is incorporated into the function $R_0(\lambda)$. We discretize the problem 225 with n layers whose characteristic parameters σ_i (with j = 1, ..., n) are the unknowns we invert 226 for. In the present research, we neglect any dependence of the electromagnetic response on 227 magnetic permeability as we assume it is fixed and equal to the permeability of empty space. In 228 principle, it is possible to consider two measurements for each location: one for the horizontal 229 and one for the vertical configuration of the transmitting and receiving loops. In this case, the 230 data used as inputs for the inversion are 2^*m , where m is the number of heights h_1, h_2, \ldots, h_m 231 where the measurements are performed.

A least squares data fitting approach leads to the minimization of the function:

$$f(\sigma) = \frac{1}{2} \sum_{i=1}^{2m} r_i^2 (,),$$
 (2)

where $\mathbf{\sigma} = (\sigma_1, \ldots, \sigma_n)^T$, and $r_i^2 (\mathbf{P})$ is the misfit between the *i*-th measurement and the corresponding forward modeling prediction based on Eq. 1.

235 We solve the nonlinear minimization problem by the inversion procedure described in Deidda, 236 Fenu, and Rodriguez (2014). The algorithm is based on a damped regularized Gauss-Newton 237 method. The problem is linearized at each iteration by means of a first order Taylor expansion. 238 The use of the exact Jacobian (whose expression is detailed in Deidda, Fenu, and Rodriguez, 239 2014) makes the computation faster and more accurate than using a finite difference 240 approximation. The damping parameter is determined in order to ensure both the convergence 241 of the method and the positivity of the solution. The regularized solution to each linear 242 subproblem is computed by the truncated generalized singular value decomposition (TGSVD -243 Díaz de Alba and Rodriguez, 2016) employing different regularization operators. Besides the 244 classical regularization matrices based on the discretization of the first and second derivatives, 245 to further improve the spatial resolution of EMI inversion results in all the cases characterized 246 by sharp interfaces, we tested a nonlinear regularization stabilizer promoting the 247 reconstruction of blocky features (Zhdanov, Vignoli, and Ueda 2006; Ley-Cooper et al. 2015; 248 Vignoli et al. 2015; Vignoli et al. 2017). The advantage of this relatively new regularization is 249 that, when appropriate prior knowledge about the medium to reconstruct is available, it can 250 mitigate the smearing and over-smoothing effects of the more standard inversion strategies. 251 This, in turn, can make the calibration of the EMI data against the TDR data more effective. For 252 this reason, in the following, the EMI results used for our assessments are those inferred by 253 means of this sharp inversion. The differences between the "standard" smooth (based on the 254 first derivative) reconstruction and the sharp one are clearly shown in Fig.s 2 and 4. In all cases, 255 the inversions are performed with a 100-layer homogeneous discretization, down to 8 m, with 256 fix interfaces. We opted for such a parameterization to be able to: (i) control the inversion 257 results by acting merely on the regularization parameters, and (ii) remove the regularization 258 effects possibly originated by the discretization choice (e.g., the number of layers, interfaces 259 locations). In this way, it was possible to use an automatic strategy for the selection of the 260 regularization parameters. In Fig.s 2 and 4, the sharp results (upper panels) associated with the 261 cases 100-6dS and 50-6dS are compared against the corresponding smooth inversions (middle 262 panels). Even if the data misfit levels largely match (lower panels in Fig.s 2 and 4, but also Fig.s 263 3 and 5), the two inversion strategies produce reconstructions that differ significantly. This is 264 due to the inherent ill-posedness of the EMI inversion. By considering solely the geophysical 265 observations, it is impossible to decide which model is the best. In this research, based on the 266 fact that, just after the irrigation, the effect of the water is supposed to remain localized in the 267 shallowest portion of the soil section, the sharp inversion was found to provide more reliable 268 results. Moreover, to some extent, the general better agreement of the data calculated from 269 the sharp model supports the idea that the electrical properties distributions are better 270 inferred via the sharp regularization. In any case, since in this research we calibrate the EMI-271 derived models (and not the data), the final calibrated result will reflect the assumptions made 272 in the first place when the EMI data are inverted (specifically, the regularization assumptions). 273 A possible alternative way to still effectively use the TDR data to calibrate the EMI 274 measurements (and not the associated conductivity model) could consist in performing the

275 calibration in the data-space (and not in the model-space). In this case, the measured TDR 276 conductivity could be used as input model to calculate the EC_a response of the EMI device 277 actually used. In turn, this calculated EC_a response can be compared against the measured EMI 278 data and used for their calibration. However, eventually, also this latter data-space calibration 279 will have to deal with the inversion issues once the calibrated EMI data need to be converted 280 into conductivities $\sigma_{\rm b}$. In this paper, we chose the model-space calibration strategy as, in 281 general, in the available EMI inversion codes, it is not always easy to decouple the forward 282 modelling routines from the overall inversion algorithm. Hence, the discussed approach could

283 be more directly applicable and beneficial for practitioners. On the other hand, it is true that 284 the data-space calibration naturally takes into account the scale-mismatch between the TDR

and the EMI measurements with no need for any statistical calculation.

286 It is worth noting that the constant magnetic permeability assumption is not always valid.

287 Inverting for the magnetic permeability is sometimes not only necessary, but it can also provide

an additional tool for soil characterization (e.g., Beard and Nyquist, 1998; Farquharson,

289 Oldenburg, and Routh, 2003; Deidda, Diaz De Alba, and Rodriguez 2017).

For the sake of clarity, hereafter, the σ_b values generated from the EMI data inversion will be identified explicitly as $\sigma_{b,\text{EMI}}$.

292

293 TDR-based water content and bulk electrical conductivity

294 The Tektronix 1502C can measure the total resistance R_t of the transmission line by:

$$\mathbf{R}_{t} = \mathbf{Z}_{c} \frac{(1+\rho_{\infty})}{(1-\rho_{\infty})} = \mathbf{R}_{s} + \mathbf{R}_{c}$$
(3)

where: R_s is the soil's contribution to total resistance and R_c accounts for the contribution of the series resistance from the cable; the connector Z_c is the characteristic impedance of the transmission line; and ρ is a reflection coefficient at a very long time, when the waveform has stabilized.

299 The σ_b value at 25°C can be calculated as (Rhoades and van Schilfgaarde 1976; Wraith et al. 300 1993):

$$\sigma_{b^{2S^{*C}}} = \frac{K_c}{Z_c} f_T$$
(4)

301 where K_c is the geometric constant of the TDR probe and f_T is a temperature correction factor 302 to be used for values recorded at temperatures other than 25°C. Both Z_c and K_c can be 303 determined by measuring R_t with the TDR probe immersed in a solution with known 304 conductivity σ_b . Hereafter, these σ_b measurements will be identified as $\sigma_{b,TDR}$.

305

306 Evaluation of Concordance between $\sigma_{b,TDR}$ measurements and $\sigma_{b,EMI}$ estimates

307 The agreement between $\sigma_{b,TDR}$ measurements and $\sigma_{b,EMI}$ estimations in the 0.0-0.6 m range was 308 evaluated by the Concordance Correlation Coefficient, ρ_L :

$$\rho_{L} = \frac{2s_{xy}}{z_{x}^{2} + z_{y}^{2} + (m_{x} - m_{y})^{2}}$$
(5)

309 where m_x , m_y , s_x , s_y , s_{xy} are means, standard deviations and covariances of the two data series 310 ($x = \sigma_{b,EMI}$; $y = \sigma_{b,TDR}$), respectively.

Scatter plots of the $\sigma_{b,EMI}$ and $\sigma_{b,TDR}$ data series (both original and filtered) were evaluated by the line of perfect concordance (1:1 line) and the reduced major axis of the data (RMA) (Freedman et al. 1991). The method combines measurements of both precision and accuracy to determine how close the two data series are to the line of perfect concordance $\sigma_{b,EMI} = \sigma_{b,TDR}$. Compared to the classical Pearson correlation coefficient, ρ_P :

$$\rho_{\rm P} = \frac{{\rm s}_{\rm xy}}{{\rm s}_{\rm x}{\rm s}_{\rm y}},\tag{6}$$

 ρ_{L} not only measures the strength of linear relationship (how close the data in the scatter plot are to a line), but also the level of agreement (how close that line is to the line of perfect agreement, the 1:1 line). In this sense, ρ_{L} may also be calculated as (Cox 2006):

$$\rho_{\rm L} = \rho_{\rm P} C_{\rm b} ,$$

$$C_{\rm b} = \frac{2}{(\mu + 1)(\mu + \mu^2)},$$
(7)

$$v_{b} = (v + 1/v + u^{2})'$$

 $v = s_{x} / s_{y}$, (7)

319 and

$$u = (m_x - m_y) / \sqrt{s_x s_y}$$
,

where C_b is the bias correction factor measuring how far the best-fit line deviates from the 1:1 line. The maximum value of $C_b = 1$ (0< C_b <1) corresponds to no deviation from the line. The smaller C_b is, the greater the deviation from the line. In other words, C_b is a measure of accuracy (how much the average estimate differs from the average measurement value, assumed to be the true value) and refers to the systematic error, whereas ρ_P is a measure of precision (measures the variability of measurements around their own average) and refers to the random error. The RMA line is given by:

$$y = (m_y - \beta m_x) + \beta x = \alpha + \beta x.$$
(8)

This line passes through the means of the x and y values and has slope given by the sign of Pearson's correlation coefficient, p_P , and the ratio of the standard deviations, s, of the two series (Freedman et al. 1991, Corwin and Lesch 2005):

$$\beta = s_y / s_x \,. \tag{9}$$

330 ρ_{L} increases in value as (i) the RMA approaches the line of perfect concordance (a matter of 331 accuracy) and (ii) the data approach the RMA (a matter of precision). In the ideal case of 332 perfect concordance, the intercept of the RMA, α , should be 0 and β should be 1. Therefore, α 333 \neq 0 or $\beta \neq$ 1 indicate additive and/or multiplicative biases (location and/or scale shifts). The 334 concordance was evaluated for the original TDR data, as well as for the filtered TDR data. For 335 the analysis described in detail later in the paper, it is worth noting that the coefficients α and β 336 depend only on the statistical characteristics (mean and standard deviation) of the two series,

337 as $\alpha = m_y - \beta m_x$ and $\beta = s_y / s_x$.

339 Fourier filtering

Because of their relatively small observation volume (~10⁻³ m³), TDR sensors provide quasipointlike measurements and are, thus, more effective in capturing small-scale variability (in water content, solute concentrations) induced by natural soil heterogeneity. Thus, the variability within a set of TDR readings is expected to originate from a combination of small and large-scale heterogeneities (high and low spatial frequency components). By contrast, the EMI measurements (because of the size and physics of the instrumentation) necessarily integrate out the small-scale variability at the TDR scale of investigation.

Hence, in order to make the two datasets comparable, the original spatial TDR data series need to be filtered to remove the variation from small-scale heterogeneities (recorded only by the TDR probe). In this way, only the information at a spatial scale equal to or larger than the observation volume of both sensors is preserved.

351 Thus, a simple filter based on the Fourier Transform (FT) is applied to the TDR series. 359 So, a low-pass frequency filtering is performed on the TDR data to remove all components 360 related to the small scale heterogeneities and make it comparable with the EMI measurements. 361 More specifically, for each transect, we consider the $\sigma_{b,EMI}$ reconstruction and, for each of its 1D 362 models, calculate the average conductivity value within each depth interval for which the TDR 363 data are available (namely: 0.0-0.2 m, 0.2-0.4 m, 0.4-0.6 m). Hence, for each depth interval, 364 along the entire transect, we can calculate the mean and standard deviation of the conductivity 365 values retrieved from the EMI observations. Subsequently, this standard deviation (associated 366 with the EMI data) is compared with the standard deviation of the iteratively low-pass filtered 367 TDR data for the same depth interval. In this way, an optimal cut-off frequency can be selected 368 to make the scales of the two kinds of measurements compatible. Figure 6 shows the 369 comparison between the standard deviations of the EMI and filtered TDR data, for the 50-6dS transect, at 0.2-0.4 m depth. In this specific case, the selected cut-off frequency to filter the
TDR data is 0.313 cycles/m, corresponding to a 3.2 m range. This is not surprising at this is of
the order of magnitude of the footprint of the EMI measurements.

373

374 **Results and Discussion**

Hereafter, the original and filtered data will be respectively labeled ORG and FLT. The graphs on the top panels in Fig. 7 compare $\sigma_{b,TDR}$ measured by TDR against the corresponding conductivity $\sigma_{b,EMI}$ retrieved by the EMI (sharp) inversion for the all the transects. From the left, the graphs refer respectively to the transects identified as 100-6dS, 50-6dS, 100-1dS and 50-1dS. All plots show the data for the entire investigated profile between 0.0 and 0.6 m, together with the line of perfect concordance (1:1, black line), and the main regression axis (MRA, red line).

381 The general conclusion is that, in all four transects, and for all three considered depth-layers,

 $382 \qquad \text{the } \sigma_{\text{b,EMI}} \text{ values underestimate the } \sigma_{\text{b,TDR}} \text{ measurements, such that the MRA line generally lies}$

above the 1:1 line. Not surprisingly, the EMI result seems quite insensitive to TDR variability.

Also, a considerable scatter around the MRA line may be observed for all transects.

Table 1 shows the MRA coefficients (C_b , α , β), as well as the Pearson, p_P , and the concordance correlation, p_L , for the three depth-layers and for all four transects investigated. We recall that the bias correction factor C_b , the slope β , and the intercept α should be respectively close to 1, 1 and 0, for the MRA to approximate the line of perfect concordance. For all the transects and all the depth-layers considered, the parameters confirm the relatively loose relationship between $\sigma_{b,EMI}$ and $\sigma_{b,TDR}$ already observed in the graphs, both in terms of accuracy (the distance of the MRA line from the 1:1) and precision (the data scatter around the MRA line).

392 Von Hebel et al. (2014) found a similar behavior when comparing their EMI and ERT datasets. In
 393 that case, the EC_a values measured by EMI systematically underestimated the EC_a generated by

applying EMI forward modeling to the σ_b distribution retrieved by ERT. To remove the bias, the authors performed a linear regression between measured and predicted EC_a after applying a ten-term moving average to the original data. By using the regression coefficients, all the measured EC_a values were converted to ERT-calibrated EC_a values.

398 Here, we follow a different approach to calibrate the $\sigma_{b,EMI}$ values against the $\sigma_{b,TDR}$ 399 measurements based on the MRA coefficients and, so, on the statistical parameters (mean and 400 standard deviation) of the two data series. Specifically, the present approach looks for a 401 systematic correction of the bias based on well-defined statistical sources of the discrepancies. 402 In short, the proposed method performs the calibration in the σ_b model-space, instead of the 403 EC_a data-space. Our model-space approach mostly relies on the statistical parameters of the 404 two series. Analyzing the role of these statistics in explaining the discrepancies between EMI 405 and TDR data observed in Fig. 7a may help to understand how they can be effectively used for 406 making EMI results directly comparable with the TDR values.

407 In nearly all of the graphs in the top panels in Fig. 7, the discrepancies between $\sigma_{b,EMI}$ and $\sigma_{b,TDR}$ 408 values can be decomposed in the following components:

409 1. The distance along the $\sigma_{b,EMI}$ axis of the MRA line from the 1:1 line, that is the difference 410 between the $\sigma_{b,EMI}$ and the $\sigma_{b,TDR}$ means.

411 2. The difference in the slope of the MRA and of the 1:1 lines, which stems from the different

412 variability of $\sigma_{b,EMI}$ (its standard deviation) and that of $\sigma_{b,TDR}$. We recall here that the slope of

413 the MRA is just the ratio of the two standard deviations, $\hat{\beta} = s_v / s_x$.

414 3. The scatter of the data around the MRA line, which may come from different sensors' noise

415 and the influence of surrounding conditions (e.g., temperature).

416 Below, we analyze in detail the role of all these three points with the support of the measured417 data.

418 1. The distance of the MRA from the 1:1 line is mostly due to the difference in the observed 419 means. The plot in Figure 8a compares the means for the two original series (squares-solid line 420 for TDR, circles-dashed line for EMI). Figure 8b reports the same comparison on a 1:1 plot 421 (triangles-solid regression line). The mean values confirm the general underestimation of TDR 422 by the EMI data. However, the trends are evidently similar, which is reflected in the high 423 correlation between the means of the two series, with a significantly high $R^2=0.81$. This high 424 correlation has very positive implications from an applicative point of view, since, after the 425 calibration in a specific site, it allows the EMI mean to be inferred given the mean of TDR 426 readings taken in that soil, and thus provides the possibility to migrate the more reliable TDR 427 information across the larger area that can be practically investigated during an EMI survey.

428 2. The different slope of the two lines has to be ascribed to the different variability of the two 429 series. Figure 9a compares the standard deviations for the two original series (squares-solid line 430 for TDR, circles-dashed line for EMI). Figure 9b reports the same comparison on a 1:1 plot 431 (triangles-solid regression line). Conceptually, the different variability of the two series can be 432 related to the different sensor observation volumes (originated from the different spatial 433 sensitivity of the sensors - Coppola et al. 2016). For TDR probes, most of the measurement 434 sensitivity is close to the rods (Ferré et al. 1998b). Conversely, the spatial resolution of inverted 435 EMI EC_a values may be much lower as the resolution of the EMI result depends on the physics 436 of the method, the specifications (and configuration) of the recording device, and the 437 regularization strategy applied during the inversion. Thus, the EMI is generally unable to 438 capture the small-scale variability seen by the TDR. For our calibration purposes, it is important 439 to make the variability of EMI and TDR conductivities actually comparable. As discussed by

440 Coppola et al., 2016, a possible method can consist in filtering out the high frequency 441 components (at small spatial scale) of the original TDR data, while retaining the lower 442 frequency information. This corresponds to keep the information at a spatial scale larger than 443 the observation volume of the TDR sensor and attuned with the resolution of the $\sigma_{\rm b,EMI}$ 444 distribution. From a practical point of view, this makes sense, as TDR readings are often "too 445 local" to actually represent the macroscopic physical characteristics of interest for applications 446 (water content, solute concentrations). The volume explored by a TDR probe may, or may not, 447 include preferential channels (Mallants et al. 1994; Oberdörster et al. 2010), stones (Coppola et 448 al. 2011; Coppola et al. 2013), small-scale changes in the texture and structure (Coppola et al. 449 2011), which can make the interpretation of local measurements difficult for practical 450 applications. In this sense, EMI's removal of these small-scale effects may be desirable from a 451 management perspective. Consistently, the original TDR data are conditioned via a low-pass 452 filtering, as described in the Data Handling section. The filtering results, in terms of standard 453 deviations, are reported in Fig. 9a (crosses-dashed line) and Fig. 9b (squares-dashed regression 454 line). As expected, the low-pass filter makes the standard deviations much closer (almost 455 overlapping) in all transects and all considered depth-layers. The regression improved 456 significantly from 0.25 for the original data to 0.78 after the TDR data filtering.

457 3. The scatter is consistently reduced by the spatial filtering (as similarly discussed in Von Hebel458 et al., 2014).

459

460 Eventually, the calibrated $\sigma_{b,EMI}^{rg}$ distribution (superscript rg means: EMI data after regression) 461 can then be obtained from the original $\sigma_{b,EMI}$ via the linear mapping:

462
$$\sigma_{b,EMI}^{rg} = \alpha + \beta \sigma_{b,EMI}, \qquad (10)$$

463 where the coefficients α and β can be easily calculated from the means and standard 464 deviations of the EMI results and the filtered TDR data. Thus, if m_{EMI} and $m_{\text{TDR(FLT)}}$, and s_{EML} and 465 $s_{\text{TDR(FLT)}}$ are, respectively, the means and the standard deviations of the original $\sigma_{\text{b,EMI}}$ EMI data 466 and of the filtered $\sigma_{\text{b,TDR(FLT)}}$ TDR data, the MRA line coefficients can be expressed as 467 $\alpha = m_{\text{TDR(FLT)}} - \beta m_{\text{EMI}}$ and $\beta = s_{\text{TDR(FLT)}} / s_{\text{EMI}}$.

469 The bottom panels in Fig. 7 show the results of the application of the linear mapping. In 470 particular, they compare the calibrated EMI data (EMI rg) with the filtered TDR (TDR FLT) 471 measurements. The MRA parameters and the concordance coefficients in the case of filtered 472 TDR data are reported in Table 2. Clearly, considering the (calibrated) EMI and (filtered) TDR 473 standard deviations turns the MRA line to be practically matching the 1:1 line, with the 474 coefficient β approaching to 1. Moreover, from Table 2, the improvement of the bias C_b and the 475 concordance $\rho_{\rm L}$ is generally significant. On the other hand, the Pearson's correlation $\rho_{\rm P}$ is not 476 influenced by the recalibration as the proposed approach deals with the statistics of the data 477 series rather than the single data. Thus, after the application of the low-pass filter to the TDR 478 data, the coefficient β is close to 1, and the calibration turns out to be (almost) a simple shift of 479 the inverted $\sigma_{\rm b.FMI}$. The amount of this shift is equal to the difference between the mean values 480 m_{TDR(FLT)} and m_{EMI}. To summarize, the TDR filtering allows removing the outlier values generated 481 by the small scale variability and preserving the information content necessary to properly 482 calculate the shift required for the absolute calibration of the EMI inversion results.

483 Figure 10 shows, on the left, the original $\sigma_{b,EMI}$ distribution to be compared against the $\sigma_{b,EMI}^{rg}$

results (on the right) obtained through the application of the linear transformation in Eq. 10.

485 The calibrated transects preserves the spatial variability of the original EMI inversions, but are

486 now characterized by value ranges that are more realistic (as they are obviously closer to the

487 TDR measurements assumed to be more representative of the real soil conditions).

488 As already discussed, the high correlation of the means and the standard deviations of the two 489 series are central for this procedure to be of practical interest. In short, the procedure can be 490 summarized as follows: (i) An area is monitored via EMI survey and a few TDR calibration 491 measurements are collected concurrently. (ii) The availability of the two different datasets 492 allows performing the regression for the mean and the standard deviation of the original EMI 493 inversion results and the filtered TDR data, like those shown in Fig.s 8b and 9b. (iv) These 494 statistical parameters can be promptly used for the calculation of the coefficients α and β to be 495 inserted into Eq. 10. (v) The original EMI inversion results are not always reliable when 496 compared with the direct measurements obtained by using a TDR probe. Rather, they only 497 contain the low-frequency information supplied by TDR (most likely, together with some shifts 498 connected with the poor absolute calibration of the EMI system and/or the working conditions, 499 e.g., the temperature). Thus, for quantitative analyses, it may be crucial to transform the original EMI result $\sigma_{_{b,EMI}}$ into a new, calibrated section $\sigma_{_{b,EMI}}^{^{rg}}$ by means of the linear mapping 500 501 in Eq. 10.

The proposed workflow enables us to translate the original non-calibrated $\sigma_{b,EMI}$ data into the actual σ_b we would collect in ideal conditions, and which would perfectly match "lowresolution" TRD measurements. $\sigma_{b,EMI}^{rg}$ is our best possible estimation of the true electrical conductivity at the scale of investigation of the EMI survey: it is the original $\sigma_{b,EMI}$ after the application of the appropriate rescaling and shifts deduced by the more reliable and absolutely calibrated TDR measurements.

509 **Conclusions**

The objective of the paper is to infer the bulk electrical conductivity distribution in the root zone from multi-height (potentially non-calibrated) EMI readings. TDR direct measurements are used as ground-truth σ_b data to evaluate the correctness of the σ_b estimations generated by EMI inversion. For all four transects and for all three depth-layers considered in this study, the $\sigma_{b,EMI}$ values underestimate the $\sigma_{b,TDR}$ measurements, such that the MRA line generally lies above the 1:1 line. Also, a considerable scatter around the MRA line was observed for all transects.

517 The proposed analysis allows discussing the physical reasons for the differences between EMI-518 and TDR-based electrical conductivity and developing an approach to calibrate the original 519 $\sigma_{b,EMI}$ by using the $\sigma_{b,TDR}$ measurements. Our approach is based on the MRA coefficients and, 520 hence, on the statistical parameters (mean and standard deviation) of the two series. 521 Specifically, the approach looks for a systematic correction of the bias based on well-defined 522 statistical sources of the discrepancies. A low-pass filtering has been carried out on the TDR 523 data to obtain a significantly high correlation between the standard deviations of the two data 524 series. After that, a simple linear transformation can be applied to the originally inverted EMI 525 section $\sigma_{b,EMI}$ to get a calibrated σ_{b} result.

The proposed strategy lies on the assumption that TDR direct measurements supply absolutely calibrated observations of the electrical conductivity of the soil and can be effectively used to calibrate the conductivity distributions inferred from EMI data. The availability of EMI calibrated data paves the way to reliable reconstructions of the electrical conductivity distribution over large areas (typical for EMI surveys, but not for TDR campaigns) unaffected by the usual EMI miscalibrations. This, in turn, can result in the possibility of effective time-lapse surveys and/or in consistent merging of subsequent surveys.

533 On the other hand, the proposed statistical workflow for making the TDR measurement 534 comparable with the associated EMI results provides a more sophisticated approach than 535 simple smoothing to upscale the TDR data. Thus, from the opposite perspective, the approach 536 in question can be used to tackle the problems connected with handling the TDR data 537 characterized by excessively high spatial resolution.

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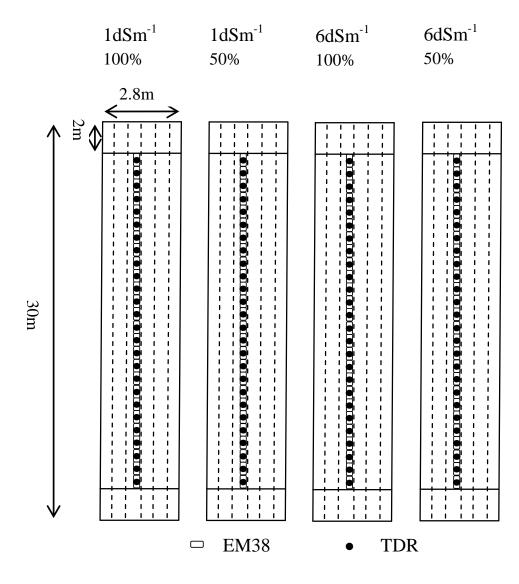
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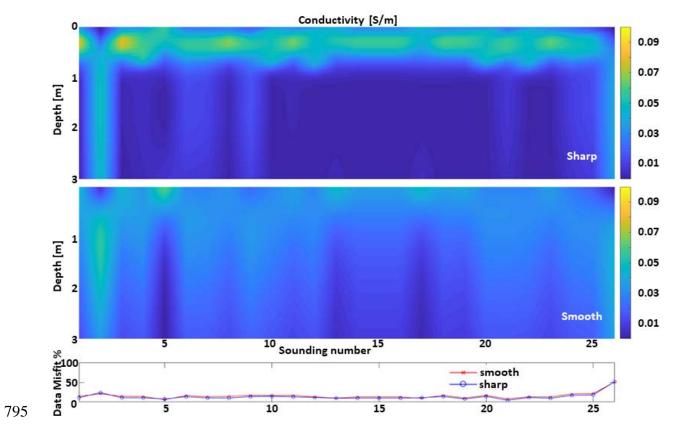
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794 Figure 1. Schematic view of the experimental field



796 Figure 2. Examples of sharp and smooth inversions applied to the dataset 100-6dS. The results

are shown together with their corresponding data misfit.

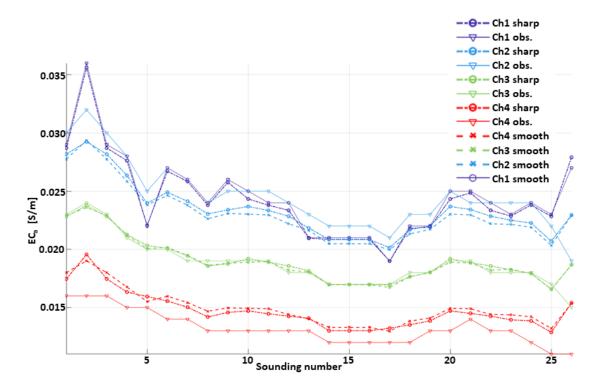
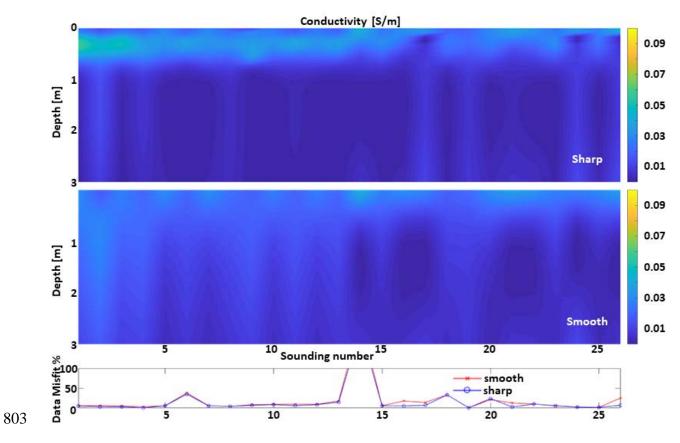


Figure 3. Comparison of the data fitting associated with the sharp and smooth inversions applied to the dataset 100-6dS (Fig. 2). The calculated data corresponding to the sharp and smooth results are shown together with the observations for each of the four measured channels (heights).



804 Figure 4. Examples of sharp and smooth inversions applied to the dataset 50-6dS. The results

805 are shown together with their corresponding data misfit.

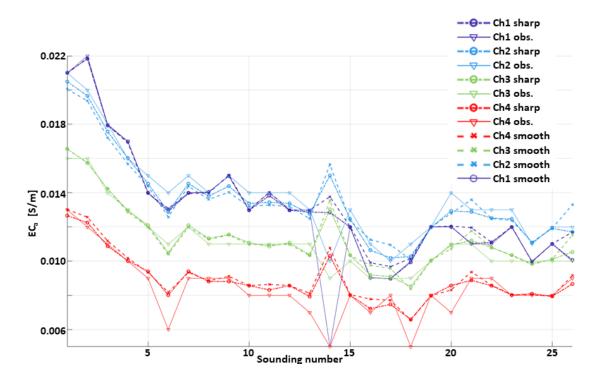


Figure 5. Comparison of the data fitting associated with the sharp and smooth inversions applied to the dataset 50-6dS (Fig. 4). The calculated data corresponding to the sharp and smooth results are shown together with the observations for each of the four measured channels (heights).

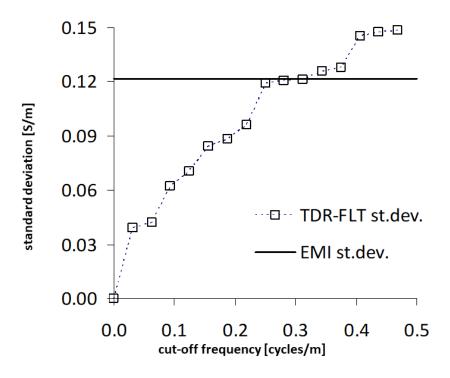


Figure 6. Standard deviation of the EMI series (horizontal black line) for the 50-6dS transect at
0.2-0.4 m depth. The squares show the corresponding standard deviations for the TDR series
for different level of filtering. The intersection of the EMI line with the TDR curve allows
identifying the optimal cut-off frequency range (~0.313 cycles/m) to make the two standard
deviations similar.

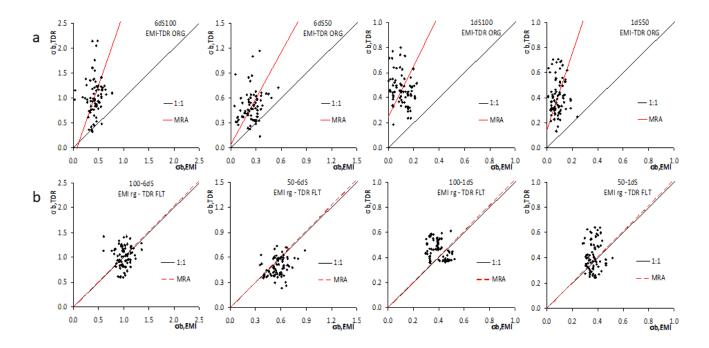


Figure 7. Comparison between $\sigma_{b,TDR}$ and $\sigma_{b,EMI}$ for all four transects for the depth range 0.0-0.6 m. The graphs in the top panels (a) show the original TDR and EMI data, while those in the bottom panels (b) the Filtered (FLT) TDR and EMI data after the regression based on MRA parameters (rg).

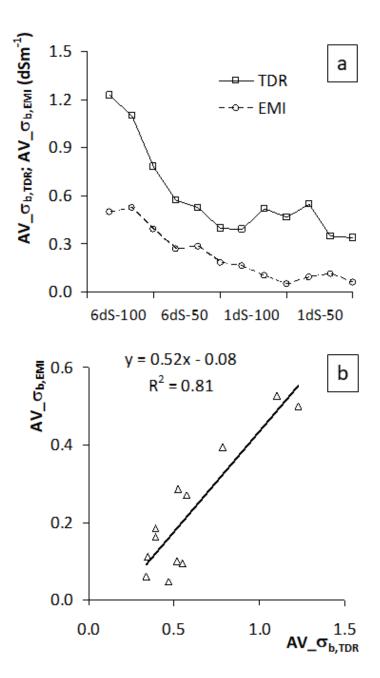


Figure 8. (a) Comparison of the means for the two original series (squares-solid line for TDR, dcircles-dashed line for EMI); (b) The same comparison on a 1:1 plot (triangles-solid regression line). In the panel (a), the four cases are shown in sequence. For each case, the three values are for the three depth intervals 0.0-0.2, 0.2-0.4, and 0.4-0.6 m.

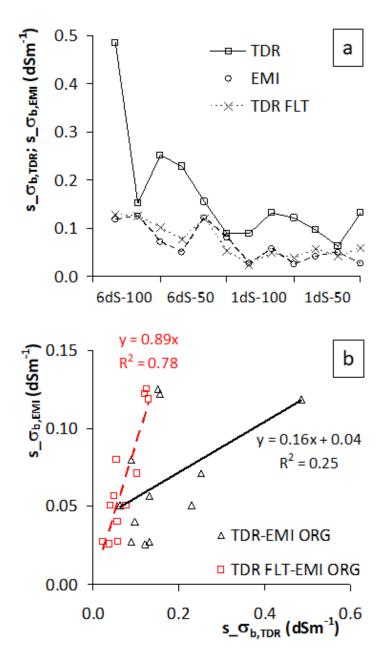


Figure 9. (a) Comparison of the standard deviations of the TDR original series (squares-solid line), of the EMI original series (circles-dashed line), and of the filtered (FLT) TDR series (crosses-dashed line); (b) The same comparison on a 1:1 plot: the original TDR and EMI data (triangles-solid regression line); filtered (FLT) TDR and original EMI data (squares-dashed regression line). In the panel (a), the four cases are shown in sequence. For each case, the three values are for the three depth intervals 0.0-0.2, 0.2-0.4, and 0.4-0.6 m.

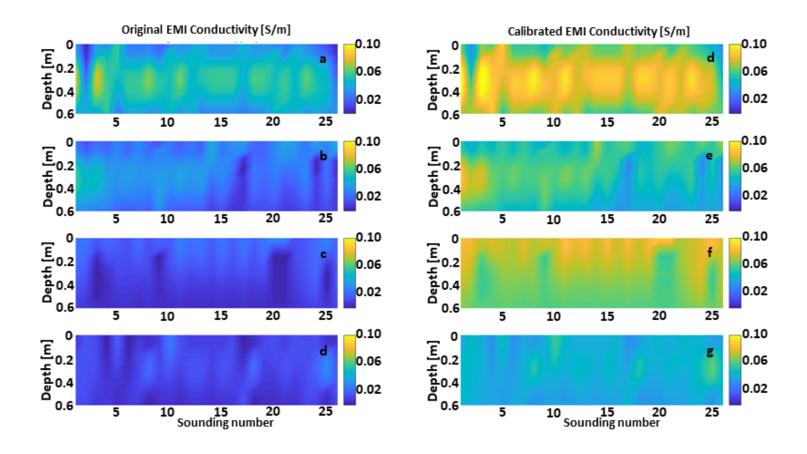


Figure 10. Maps of bulk electrical conductivity for the: (a) 100-6dS, (b) 50-6dS, (c) 100-1dS, (d) 50-1dS transects showing the original $\sigma_{b,EMI}$ resulting from the inversion of the observed EMI data. Panels (d) to (g) show instead the corresponding results after the calibration via the TDR measurements (i.e., by applying Eq. 10).

Transect	C _b	ρι	ρ	β	α
100-1dS	0.10	0.02	0.33	2.04	0.25
50-1dS	0.10	0.00	0.08	3.06	0.14
100-6dS	0.18	0.02	0.07	2.92	-0.21
50-6dS	0.34	0.08	0.32	1.84	0.04

Table 1. Concordance parameters for the four transects for the TDR_ORG and EMI_ORG data. The table reports the Concordance, ρ L, and the Pearson, ρ P, correlation, as well as parameters α and β of the MRA line. The bias factor, Cb, is also shown.

Transect	C _b	ρι	ρ	β	α
100-1dS	0.74	0.24	0.33	1.02	0.29
50-1dS	0.62	0.05	0.08	1.02	0.27
100-6dS	0.87	0.06	0.07	1.02	0.57
50-6dS	0.79	0.25	0.32	1.02	0.31

Table 2. Concordance parameters for the four transects for the TDR_FLT and EMI_ORG data. The table reports the Concordance, ρ L, and the Pearson, ρ P, correlation, as well as parameters α and β of the MRA line. The bias factor, Cb, is also shown.