

We would first like to thank both reviewers for their profound comments and suggestions. In this rebuttal, we list the comments and suggestions raised by the reviewers and explain how we handled them in the revised manuscript. Our answers are listed in *italic*. Changes to the manuscript are given in **boldface**.

1 Specific comments of the first reviewer

1.1 Major issues

1.1.1 Seasonal effects

A copula models the dependence between two random variables X_1 , X_2 with marginal distributions F_1 and F_2 . Its parameters can be estimated from observations of these variables, $\mathbf{X}_t = (X_{1,t}, X_{2,t})$, $t = 1, \dots, T$. The usual assumption for the validity of the estimate is that the data \mathbf{X}_t are independent and identically distributed (iid). In particular, the distribution of \mathbf{X}_t should not change with t , which is usually violated by climatic variables. The authors acknowledge that by fitting multiple models, one for each month. I am afraid this may not be enough, because climatic trends also exist within months. For example: in central Europe, the end of April is on average much warmer than the beginning of April. Suppose that additionally, the average precipitation is decreasing during April. Then high temperatures will likely coincide with low levels of precipitation and vice versa. A copula fitted to this data will show negative dependence, which merely reflects the two deterministic within-month trends working in opposite directions, but not the stochastic dependence between the time series. Whether or not within-month trends exist can be easily checked visually or by formal statistical tests (e.g., Harris and Sollis, 2003, Chapter 3). If they do exist, they should be accounted for on a finer time scale. Splitting the data into weeks or even days could be a solution, but significantly decreases the number of observations available for fitting the copula model. A good alternative is to center and scale the time series by their seasonal mean and standard deviation. More specifically, if $X_{j,d,y}$ denotes variable j observed at day d of year y , set

$$\tilde{X}_{j,d,y} = (X_{j,d,y} - \mu_{j,d}) / \sigma_{j,d}, \quad (1)$$

where $\mu_{j,d}$ and $\sigma_{j,d}$ are the mean and standard deviation of $X_{j,d,y}$, $y = 1, \dots, 72$. If necessary, trends in the skewness of $\tilde{X}_{j,d,y}$ can be removed similarly using a Box-Cox transformation. This transformation is usually

sufficient to account for deterministic seasonal effects. We can now build a copula for the stochastic dependence in $\tilde{\mathbf{X}}_t = \tilde{\mathbf{X}}_{d+365(y1)}$. Simulated data from this model can be transformed to the original scale by inverting (1).

We checked the data for the existence of a within-month trend, and found that trends exists for temperature and evapotranspiration data. As advised by the referee, we standardized the data. We added a paragraph (in Section 2.1) in the revised manuscript w.r.t. standardization of the data.:

“In order to use the above-described data to fit copulas, the data should be independent and identically distributed (*iid*), indicating that the distribution of the data should not change with time. To this end, the time series is split into monthly series to which a vine copula model can be fitted. Hence, for each month a different model will be obtained. However, the data distributions can also change within the monthly series, i.e. a within-month trend may exist. Therefore, the daily distributions, each containing 72 observations were compared w.r.t. their equality within each month by means of an ANOVA test, when distributions were homoscedastic, a Welch ANOVA test (Welch, 1951) when distributions were heteroscedastic, or a Kruskal Wallis test (Kruskal and Wallis, 1952) when distributions were not-normal and heteroscedastic, at a significance level of 0.001. The results of these tests indicate that within-month trends exist for temperature and evapotranspiration, whereas no trend was found for precipitation. In order to meet the requirements of the data to be *iid*, temperature and evapotranspiration data were standardized as follows:

$$x_{s,d,y} = \frac{(x_{d,y} - \mu_d)}{\sigma_d}, \quad (2)$$

with $x_{s,d,y}$ the standardized value of temperature or evapotranspiration at day d of year y , $x_{d,y}$ the original measured value of temperature or evapotranspiration at day d of year y , μ_d and σ_d the mean value and standard deviation of x at day d .”

1.1.2 Inter-serial dependence

Even when the distribution of $\tilde{\mathbf{X}}_t$ is the same for each t , subsequent observations of the time series may not be independent. Such data is called stationary which is less restrictive than *iid*. Typically, stationarity is sufficient to allow for valid estimation of the marginal distributions and copula of

\tilde{X}_t . But inference tools (like confidence intervals and goodness-of-fit tests) derived under the *iid* assumption are no longer valid. Another potential issue is that inter-serial dynamics can play an important role in applications. If so, these dynamics should be modeled explicitly. In the context of hydrological discharges, this is likely the case. Large discharges often occur when extreme weather conditions have been persistent for several days, and persistence is a sign of inter-serial dependence. A simple way to check whether such dependence is present is to look at the autocorrelation of the time-series, i.e., the correlation between \tilde{X}_t and \tilde{X}_{t1} (and their squares). If the correlation is small, one can test statistically whether it is zero. If there is dependence, there are two popular ways to capture it:

1. **Copula models:** This route is taken by the authors in 2.3.3, but only for the temperature variable. Similar models for the inter-serial dependence in evapotranspiration and precipitation should be employed in addition. If $F_{j,t,t1}$ is the joint distribution of $\tilde{X}_{j,t}$ and $\tilde{X}_{j,t1}$, the between-variables dependence can be modeled by a copula for the variables

$$U_{1,t} = F_{1,t|t1}(\tilde{X}_{1,t}|\tilde{X}_{1,t1}), \quad U_{2,t} = F_{2,t|t1}(\tilde{X}_{2,t}|\tilde{X}_{2,t1}), \quad (3)$$

where $F_{j,t|t1}$ is the conditional distribution of $\tilde{X}_{j,t}$ given $\tilde{X}_{j,t1}$.

2. **Classical time series models:** Classical time series models (see, e.g., Shumway et al., 2000, Chapter 3) assume that the variable $\tilde{X}_{j,t}$ is a linear combination of the preceding values ($t' < t$) and *iid* noise. For example, the autoregressive model of order p is

$$\tilde{X}_{j,t} = \sum_{k=1}^p \phi_{j,k} \tilde{X}_{j,t-k} + \epsilon_{j,t}, \quad (4)$$

where $\phi_{j,k}$ are model parameters and $\epsilon_{j,t}$ is *iid* noise with mean zero. The sequence $\epsilon_{j,t}$ is commonly called innovation or residual series. The stochastic between-variable dependence can then be captured by a copula model for $(\epsilon_{1,t}, \epsilon_{2,t})$. More complex models are required when $\tilde{X}_{j,t}$ is autocorrelated (Harris and Sollis, 2003, Chapter 8).

We found an autocorrelation for temperature and evapotranspiration on the basis of a Ljung-Box Q-test. We took the autocorrelation into account by extending the vine V_{TPE} with E_{t-1} , i.e. including the evatranspiration of the previous time step (see Section 2.3.2 of the revised manuscript):

“In order to avoid monthly effects, the temperature and evapotranspiration data were first standardized and a different C-vine copula model is used for each month. However, subsequent observations of the time series may not be independent, meaning that values within the time series may be autocorrelated. This is accounted for by extending the vine copula V_{TPE} as used in Pham et al. (2016) with the evapotranspiration of the previous day (E_p). In this way a four-dimensional C-vine copula V_{TPE_pE} is constructed for each month. ”

1.1.3 Assessing the quality of the vine copula model

There are multiple issues with how the quality of the model is evaluated:

1. To check the models validity, the authors merely look at the density/cdf of the observed and simulated values of a single time series. This is only weakly related to the vine copula model and not a good indicator for its fit. Under this measure, just simulating from the distribution F_E (thereby assuming that E is independent of T and P) would lead to results that are at least as good as the ones from the vine copula. To adequately assess the quality of the dependence model, pair-wise comparisons should be made. For example, one can look at the scatterplots of observed and simulated pairs $(X_{1,t}, X_{2,t})$. Another alternative are contour plots of the estimated joint density of observed vs. simulated pairs. Such comparisons should be made for all variable combinations. Similarly, multivariate return periods should be considered instead of single-variable return periods (see, Salvadori et al., 2011).

We examined the values of Kendall’s tau to check whether or not the dependence between the generated variables is maintained. By examining scatter plots between observed and simulated pairs, as the referee suggests, one would rather investigate whether the simulated values approximate the observed values, as in a prediction model. In this study, however, it is not the aim to match the observed values for each time step t as closely as possible, but rather mimic the behaviour of the observed time series w.r.t. statistics and extremes. We therefore did not include scatterplots in the revised manuscript.

2. Figures 6 and 9 use empirical cumulative distribution functions (ECDF) instead of densities for no obvious reason. I advise against using

ECDFs because they suggest a misleading sense of closeness between distributions. Since ECDFs are necessarily monotone functions with boundary values 0 and 1, their shape is quite restricted. For example, the left panels of Figure 9(d) show that the distributions are different, but the ECDFs still look somewhat similar. But the corresponding densities would show almost no overlap and more clearly communicate the dissimilarity.

We changed the figures and used densities instead of the ECDFs.

3. In Section 4, the uncertainty in the simulation model is assessed for various degrees of data availability. From the spread of estimated densities in Figures 11-15, the authors conclude that uncertainty increases when a variable is not observed and needs to be simulated. This is likely true, but can not be inferred from these figures. The density plots for cases 1-3 are based on a different number of observations. The spread seen on 125000 simulations will naturally be larger than the spread on 50 observations even when the actual distribution is the same. Hence, the spreads should only be compared when they are based on the same number of simulations.

In the revised manuscript, we kept our original approach in cases 1-3, as in this way we also take the stochasticity of the MBL and the temperature model into account. However, we also compared the extremes obtained for the different cases when one would use the same number of simulations, i.e. for each simulated time series of temperature, only one corresponding time series of evapotranspiration is generated in case 2, and for each simulated time series of precipitation, only one corresponding time series of temperature and one of evapotranspiration are generated. The spread obtained for this approach has been added to Figure 15 in the revised manuscript, and some explanatory text has been included in the manuscript:

“ However, it should also be noted that the results for cases 2 and 3 are obtained on the basis of a wider ensemble of time series as compared to case 1 (2500 for case 2, and 125000 for case 3). In order to also compare the variations obtained on the basis of an equal number of time series within the ensemble (i.e. 50 time series), for each time series of observed (case 2) or simulated (case 3) precipitation, one corresponding time series of temperature and one corresponding time

series of evapotranspiration are generated. The bottom panel of Fig.15 illustrates the extremes obtained on the basis of this ensemble of 50 time series of discharge. These results also show that most of the variation obtained in case 3 is due to the stochastic generation of precipitation.”

1.2 Minor issues

1. Since vine copulas are the essential ingredient in your model, I suggest to indicate this in the abstract.

This has been indicated in the abstract:

“In this paper, stochastically generated rainfall and coinciding evapotranspiration time series, generated by means of vine copulas, are used to force a simple conceptual hydrological model.”

2. p. 4, p. 165: If unconditional bivariate copulas are used (as is common), a vine copula is not a decomposition, but a construction. A decomposition is called non-simplified vine copula and involves conditional bivariate copulas (see, e.g., Stöber et al., 2013). I suggest to rephrase this sentence.

We rephrased this sentence:

A flexible construction method for high-dimensional copulas, known as the vine copula construction, has been introduced in the work of Bedford and Cooke (2001, 2002), in which multivariate copulas, and hence the multivariate densities, are constructed as a product of bivariate copula densities.

3. p. 4, l. 167: I suggest to change all types of dependence to a wide range of dependence structures. All types can only be modeled by a non-simplified vine copula.

This has been changed in the manuscript.

4. p. 5, l. 179: What do you mean by C-vine copulas are easier to construct than D-vine copulas? In fact, any three-dimensional vine is both a C- and D-vine, which can be easily verified by re-arranging the vertices of the vine graph

This sentence has been removed from the manuscript.

5. p. 6, l. 203 ff.: I am afraid a reader without prior knowledge of vine copulas will not understand your paragraph on how the model is estimated. Instead of your explanation, it should suffice to refer the reader to Aas et al. (2009).

We believe that the reader should get some insight in how the vine is constructed and therefore, we revised this paragraph and added a reference to Aas et al. (2009):

“The construction of V_{TPE_pE} is given as follows. First, values $(u_{T,j}, u_{P,j}, u_{E_p,j}, u_{E,j})$ of U_T , U_P , U_{E_p} and U_E are derived from the marginal distributions of respectively T , P , E_p and E ($j = 1, \dots, n$ and n is the number of data points), and are used to select and fit the bivariate copulas C_{TP} , C_{TE_p} and C_{TE} . These bivariate copulas are conditioned on U_T through partial differentiation as given in Eq. (5), resulting in the conditional cumulative distribution functions $F_{P|T}$, $F_{E_p|T}$ and $F_{E|T}$.

$$\begin{aligned}
 F_{P|T}(u_P|u_T) &= \frac{\partial}{\partial u_T} \mathbf{C}_{TP}(u_T, u_P) \\
 F_{E_p|T}(u_{E_p}|u_T) &= \frac{\partial}{\partial u_T} \mathbf{C}_{TE_p}(u_T, u_{E_p}) \\
 F_{E|T}(u_E|u_T) &= \frac{\partial}{\partial u_T} \mathbf{C}_{TE}(u_T, u_E).
 \end{aligned} \tag{5}$$

Using these three conditional distributions, the conditional probabilities are calculated for all data points $(u_{T,j}, u_{P,j}, u_{E_p,j}, u_{E,j})$. To these conditional probabilities, which are also uniformly distributed on $[0,1]$, two bivariate copulas $C_{PE_p|T}(F_{P|T}, F_{E_p|T})$ and $C_{PE|T}(F_{P|T}, F_{E|T})$ are fitted, of which the partial derivatives to $F_{P|T}$ can be computed to obtain $F_{E_p|TP}$ and $F_{E|TP}$. Again, using these two conditional distributions, a bivariate copula $C_{E_pE|TP}(F_{E_p|TP}, F_{E|TP})$ is fitted, which can also be conditioned by calculating the partial derivative. For more detailed information about the construction of vine copulas, we refer to (Aas et al., 2009).”

6. How are marginal distributions modeled/estimated?

We added in the manuscript that empirical distributions are employed as marginal distributions.

7. Figures 4, 12–17 should use a larger smoothing parameter to decrease variability of the density estimates. A large proportion of the observed

variability is due to the density estimation technique. This is not the kind of variability you want to assess.

We changed the smoothing parameter to reduce this variability.

8. Figure 22: What is i ?

i is the cumulative relative frequency at which the RMSD between the simulated and the reference discharge is calculated. See also the explanation of Eq. (6):

$$\text{RMSD}(i) = \sqrt{\frac{1}{n} \sum_{s=1}^n (Q_{m,s}(i) - Q_o(i))^2}, \quad (6)$$

where $Q_m(i)$ and $Q_o(i)$ are respectively the modelled and reference discharge value at a cumulative relative frequency $i \in [0, 1]$, and n is the number of the members in the ensemble considered.

2 Comments of the second reviewer

This is a nice study that uses copula-based approaches to stochastically generate mutually dependent rainfall and evapotranspiration forcing for rainfall runoff models. This could be used for design purposes where observation is sparse or missing. However, this approach does not seem to be working properly for the extreme events (which are needed for design purposes). Acknowledging this fact, the study is valuable for the areas with no observation. Overall, paper is well written and well structured. I have some comments (most of them major) that could potentially improve the quality of this paper.

1. Line 46: Authors use stochastic process models to generate precipitation series. My question is:

How do stochastic process models handle changing characteristics of precipitation? Several studies have shown, for parts of the world, that rainfall events are shrinking in time and expanding in amplitude. Also there is a temporal shift in rainfall events in some parts of the world, let alone the changes in the distribution of rainfall/snow. Addressing these issues could be helpful.

We addressed this in the introduction:

“The BL model will be employed on a monthly basis such that temporal changes in precipitation characteristics due to the annual cycle can be underpinned. Long-term changes, e.g. due to climate change, however, cannot be accounted for in this model set-up.”

2. Lines 91-94: I don't understand how the number of stochastically generated forcing data could influence the uncertainty of the rainfall-runoff model's response. Uncertainty is a characteristic of the forcing data (let's neglect the modeling uncertainties for now), not the number of generated time series. So if you find a time series that fit your runoff extremes well, this is just a random phenomenon. This cannot be the basis for prediction, as we can't determine the best forcing for future, and need to rely on the ensemble of forcing data.

We added some text in the introduction to describe the source of uncertainty we are dealing with:

“By regarding the actual observed time series as one realisation of the meteorological process, the corresponding discharge can also be regarded as one realisation. Actually, due to chaos occurring in the climatological system, a different time series could have been observed resulting in a discharge time series different from the actual observed one. The latter will hence provide other design values than those corresponding to the actual observed time series. In order to account for this kind of uncertainty, different cases, in which the number of stochastically generated input variables to the model is increased, are investigated. For these cases, the increase of uncertainty in modelled extremes and what portion of this increase can be attributed to the different stochastic generators, is assessed.”

3. Lines 95-96: Section 2 should precede section 3!

This has been corrected.

4. I am confused about how sections 2.1 and 2.2 are connected. Historical record of climate forcing are obtained for Brussels, and RR model is calibrated for the Grote Nete catchment. How do you use a model calibrated against one watershed, to predict runoff at another watershed? Moreover, 1 year of data for evaluation is not enough. You will

need a couple of years to ensure calibrated model can capture different aspects of a catchment.

We added some text in Section 2.2. to better explain this.:

“Given the relatively small distance between Uccle and the Grote Nete catchment, and the fact that the meteorological conditions are nearly the same, one can assume that the statistics of the modelled discharge obtained with the forcing data observed near the catchment and those observed at Uccle are negligible. Furthermore, the rainfall-runoff model will not be used to make predictions, but rather to demonstrate the impact of different alternative realisations of precipitation (P), temperature (T) and evapotranspiration (E) on discharge values. Therefore, although PDM will be applied to observations from Uccle in this study, it is calibrated on the basis of a time series of more than 6 years (from 13/8/2002–31/12/2008) at an hourly time-step (precipitation, evapotranspiration and discharge) that is available for the catchment.”

5. Section 2.3: Copulas characterize dependence structure of different variables. This means there should be a dependence structure. Did you quantify the correlation between evaporation, temperature, and precip? If so, is it significant? At what temporal scale? My understanding is that you perform your analysis at daily scale, and I fear the correlation might not be significant at the daily scale.

We do not fully grasp the fear of the reviewer, but the correlation between the variables has been checked. Yet, the dependence structures, as present in the input time series, are used to build the copula models.

6. Line 150: bivariate \rightarrow It could be multivariate

True, Eq. (1) can be written with more than two dimensions. However, as Eq. (1) only concerns 2 variables, we maintain the used terminology (i.e. bivariate copula).

7. Line 152: I would reference to Joe 1997 too. Joe and Nelsen both played an important role in introducing copula to the scientific community.

We added a reference to Joe (1997).

8. Lines 171-173: I agree that vine copulas are very flexible, but it comes at a price! A model with 4 degrees of freedom is more flexible than a competitor with 2! However, usually there is not enough information to constrain all parameters. The copula literature usually does not address the parameter uncertainties, and so they neglect the identifiability of parameters. I would address this predicament here. For more info, refer to Figure 6 of: Sadegh, M., E. Ragno, and A. AghaKouchak (2017), Multivariate Copula Analysis Toolbox (MvCAT): Describing dependence and underlying uncertainty using a Bayesian framework, *Water Resour. Res.*, 53, doi:10.1002/2016WR020242.

Link: <http://onlinelibrary.wiley.com/doi/10.1002/2016WR020242/full>

We added a sentence to make the reader aware of this:

“ However, one has to be aware that the flexibility offered by vine copulas demands the estimation of a large number of parameters for which the data set should encompass sufficient information.”

9. Line 191: As a minor issue, when someone talks about a 3-dimensional model, I expect the model to have three parameters. When someone talk about trivariate model, I expect a multivariate model that associates three variables.

We prefer not to change the terminology as, in literature, the term ‘n-dimensional copula’ is commonly used for a copula that involves n variables. One wouldn’t call the Frank copula a one-dimensional copula as it only has one parameter.

10. Line 203: How did you construct the marginal distribution? Empirical? Fitted distribution?

We used the empirical distributions to construct the marginal distributions. We added this information in the manuscript.

11. Eq. 3: how did you calculate inverse of the vine copula? Analytical or numerical?

The inversions, necessary for sampling a value out of the vine copula, were performed analytically whenever possible, numerically otherwise.

12. Line 253: pvalue larger than 0.05 or smaller?!

The obtained p-values were larger than 0.05. More details about the theory and the p-values of the White test are given in Shepsmeier,

2015. We added some more information about the hypothesis of the White test in the paper:

“Further, the White goodness-of-fit test (Schepsmeier, 2015) is applied to check whether the dependence present in the data is captured by the C-vine copulas. For this test, p -values larger than the significance level indicate that the dependence structure of the data can be described by the selected copulas.”

13. Section 2.4: How did you calibrate the modified Bartlett-Lewis (MBL) model, given the stochastic nature of precipitation prediction models? With stochastic models, usually summary statistics of data and simulation are compared, rather than original time series. For this purpose, approximate Bayesian computation is a great framework.

We briefly mentioned in the paper how the model was calibrated:

“The MBL model is calibrated using the Generalised Method of Moments, i.e. the difference between the model statistics obtained by means of analytical expressions and the empirical statistics obtained from the observed time series is to be minimized. The calibration of the MBL model in this study is based on the mean, variance, lag-1 autocovariance and zero-depth probability (ZDP) at the aggregation levels of 24 h, 48 h and 72 h instead of 10 min, 1 h and 24 h that were used in Pham et al. (2013). As in Pham et al. (2013), the Shuffled Complex Evolution algorithm Duan et al. (1994) was employed to search for the optimal parameters.

14. Lines 338-344: I cannot disagree more! Forcing and model uncertainties are intertwined, and interact in a nonlinear manner. It is not as simple as you explained. You cannot simply use a RR model calibrated for one watershed to simulate runoff at another watershed! Tens (Hundreds) of papers are available on the regionalization topic, not many of them really provided a sound ground for transferring model parameters from one watershed to another! Worse is that authors assume this modeling uncertainty does not interact with the forcing uncertainty.

The comment of the reviewer is based on the misconception that the RR model is calibrated for one catchment and applied to another one. As stated before, Uccle is a city (not a catchment) where the headquarter of the Royal Meteorological Office of Belgium is located. At this place, the

meteorological data are obtained. These data, which are statistically similar to those observed in the catchment of the Grote Nete (situated less than 100 km from Uccle), are then used in the model of the Grote Nete catchment to model its discharge. The advantage of the data at Uccle is their length (72 years). Such long time series near the Grote Nete are not available. Furthermore, the simulations are made for one single catchment (i.e. that of the Grote Nete), making use of a model calibrated for it. In this sense, the exercise done in the paper allows for partly reducing the uncertainty due to the use of PDM.

15. Figure 22: 22 figures? Is that many figures really necessary when most of them don't provide any new info?

We reduced the number of figures. Figures 12–18 of the original manuscript have now been summarized in three figures.

16. Lines 476–478: I have a hard time accepting this claim. If you generate a much longer synthetic (stochastic) forcing, then lets say predictions at a 100 years return period level improves. I accept this. But I cannot accept the general comment that longer fording data reduces overall uncertainties. What if I had to estimate a 500 years return period flow?

The uncertainties that are reduced are the result of working with time series of a given length. We rephrased this sentence in the conclusion:

“With respect to extreme discharge, it was shown that the uncertainties encountered in case 3 are partly caused by the limited length of the time series used. The uncertainties on the predictions highly reduce when input time series are used that are much longer than the maximum return period aimed at. As in this particular case, all forcing data are generated, the modeller is not restricted to the length of an observed time series, and can hence generate time series of whatever length as input to the hydrological model, taking into account that the longer the time series used, the more the uncertainty reduces at the expense of increasing run-time.”

To answer to the question as what to do when a 500-year return period of discharge would be needed, then the advice should be to model discharge with forcing time series that are a multitude of the return period one aims for. In this case, one should model series of 5000 years or more.

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