Dear Editor,

as requested, we provide point-by-point response to all the comments, the revised manuscript and supplement material with track changes (attached below) and without (in separate files). In the response letter, Authors' response are identified by AR (black color) while the comments of the Reviewer are identified by RC (blue color). Page (P) and lines (L) refer to the revised manuscript in track-changes to facilitate the reading.

The manuscript has been revised based on all the general and specific comments provided by the two Reviewers. Figures and tables were also updated accordingly. Please note that Figures 4 has been also replaced by correcting the x-axis labels for the CP method.

Thank you and best regards, The Authors

Authors' Response to Reviewer 1

Specific comments

RC. Novelty: I think you should state more clearly that your study is a novel contribution in respect to both the ways of introducing uncertainty on soil properties (if I understand correctly, this is done more simple in other studies?) and that you take the temporal resolution into account in your analysis (which is not considered in Refsgaard et al. (2016), Hansen et al. (2014), He et al. (2015))

AR. We highlighted the novelty of these aspects in the introduction (P3L7-9) and in the conclusion sections (P18) of the revised manuscript.

RC. Title: I suggest changing the title to "Effects of uncertainty in soil properties on simulated hydrological state and fluxes at different spatio-temporal scales"

AR. The title has been changed.

RC. Figure 1 and Page 3, line 22: When first seeing figure 1 and reading the text, I was a bit confused about the transect depicted in the figure. After reading the rest of the article I now understand that it is a horizontal transect through a catchment and not a vertical transect (showing how the sand% change with depth). Could you maybe make this more clear in the text and also in figure 1?

AR. We specified that is a horizontal transect through a soil map in the text (P3L25) and in the caption of Figure 1. Note that Figure 1 was replaced with a new figure where x-axis of the horizontal transect is expressed in km to better identify that is a horizontal transect and not a vertical soil profile. Names of the methods were also modified to be more consistent with the acronyms used in the manuscript.

RC. Page 3, line 4: I suggest adding some extra text to this sentence, which tells the reader that you are using more sophisticated methods to describe the uncertainty, compared to the studies you mention on page 2 that use more simple assumptions. In this way you clearly indicate that your work is novel.

AR. We added some extra text to better clarify that we are presenting also a new method (P3L7-9).

RC: Page 5, line 11: I do not understand what you mean by "the vertical soil horizons are aggregated to the total soil depth of 2 m"?

AR. The text was rephrased (see P5L16-17).

RC. Page 5, line 12: How do you define the 29 soil units? Could you show the units on the maps of figure 3?

AR. We specified that the term soil units refer to polygons within the catchment (see P5L16-19).

RC. Page 6, line 21: How is the upscaling done? Is it just taking an area-weighted average of the parameters?

AR. We specified in the revised manuscript (P7L1-3) that the upscaling is done based on different average rules for each parameter (e.g. arithmetic, geometric, maximum). The rules are reported and described in details in Kumar et al. (2013) and Samaniego et al. (2010) and we referred to these studies for additional information.

RC. Page 8, line 8 + Figure 2: So are the gauging stations shown on figure 2 "artificial stations" you put in to define the subcatchments you use in analysis #3? If so, could you call them something else on figure 2 that indicates that these are not real gauging stations with actual measurements

AR: The positions represent real gauging stations. We specified in the revised manuscript (P8L22-23) that the positions of the gauging stations were used to define the subcatchments.

RC. Page 10, line 32 + page 11, line 1: Are these average CV values across the catchment (15% for Q, 11% for GWR, 3% for SM and 1% for AET) for all the perturbation methods all together (that is how I read the first part of the text) or for the RE method only i.e. the results in figure 6 left (this is how I understand the parenthesis on line 1, p.11)? Please make this more clear in the text.

AR. The text was rephrased in the revised manuscript (see P11L17-19) to clarify that average CVs estimated across the catchment are the same for each perturbation method. Differences are detected only in transition between the soil units.

RC. Page 11, line 14-15 + figure 7: So you calculated correlations coefficients for each of the 3 perturbation methods and then afterwards the average and standard deviation of these R2 (which is plotted on figure 7)? Please specify this in the text and in the figure text.

AR. We added additional text in the revised manuscript (P12L1-2) to clarify that the average and standard deviation of the 3 perturbation methods are plotted. In the capture legend of Figure 7 it was already indicated that the bars represent the mean of the correlation coefficients obtained with the three perturbation methods and the error bars the standard deviation. For this reason no changes were done there.

RC. Page 11, line 20: It looks to me as the pattern in soil moisture uncertainty is very similar to the patterns in clay%? When I visual compare the CV SM map in figure 6 (left) and clay% maps in figure 4.

AR. We checked again the correlation coefficients calculated between CVs and clay. The values are correct. From visual comparison, we see, on the one hand, that one soil unit is remarkable visible with high values in the CV SM map, i.e., one long soil unit crossing the entire catchment from south-west to north-east. On the other hand, however, other locations are not highly correlated. For these reasons, we believe that the visual comparison could be misleading for the average correlation over the entire catchment as it is quantify instead by the calculated correlation coefficient. For this reason no changes were done in the revised manuscript.

RC. Page 11, last section: When reading this I was wondering why the AET is not correlation to soil moisture. But you give the explanation on page 12 line 17-18, that AET is close to PET most of the time, and I guess that is why they are not correlated? Maybe you could also mention this explanation on page 11?

AR. In section 3.3 we discuss the correlation while in section 3.4 we provide the actual values of SM and AET. For this reason, we preferred to stick to the results presented i.e., to discuss only the correlations in section 3.3 and to extend the discussion later by reminding the correlations found (see P13L8-9).

RC. Page 12 line 29 + Page 16 line 6: I do not understand what you mean by threshold behaviour/condition?

AC. Additional text was added to clarify the threshold conditions (see P13L20-22).

RC. Page 13, line 18-26 + point 5 in conclusions: You conclude that stream flow, which is an integrated flux, is only sensitive to large spatial structures, whereas the local states and fluxes (i.e. soil moisture, AET, GWR) are sensitive to small scale variations. This makes sense to me. But I would like some more explanation (on page 13) on how you see this from the graphs in figure 9, since that is not clear to me.

AR. This conclusion is supported by comparing the results presented in both Figure 5 and Figure 9. Figure 5 presents the uncertainty introduced in the soil properties by each method. Here we show how RE method perturb long spatial structure while CP method only small scale features. Figure 9 represent the uncertainty in the model output. In this case, we can look at the uncertainty in the simulated streamflow of the entire catchment (e.g., SF CV for catchment > 60 x 60 km2) and see that this model output is strongly perturbed by the RE method, and for that, only by the long spatial structures. In the same figure we can look at the uncertainty in SM or AET at the model resolution or, eventually, as they could be measured in the field e.g., catchment < $1 \times 1 \text{ km}^2$. These model outputs are affected also by the uncertainty introduced by the CP method. For this reason, these local states and fluxes are sensitive to small scale variations. This explanation is now extended and better integrated in the revised manuscript. To this end, we rather found more convenient to first discuss the characteristic correlation lengths introduced by each perturbation method in section 3.4 and to move in section 3.5 the discussion about the implications for the specific model applications.

RC. Page 14, line 7-26: I found this section difficult to understand, please consider to rephrase so it is easier to read. Since you are talking about "representative scale" in the section, I suggest that you present the RES concept already here (you only mention it in the conclusion).

AR. The section was revised by introducing the RES concept and by rephrasing the discussion accordingly.

RC: Page 16, line 24-25: I think you should make it more clear, that you have done something new compared to the other studies using the RES approach. I suggest starting the sentence with something like "This study proposes two extensions to the RES approach..."

AR. The conclusion was rephrased to better highlight the novelty of the study (P18L3-20).

Technical comments (not listed)

Page 1, line 12: Delete "the" in front of "uncertainties" AC. Done. Page 1, line 12: Change "The methods are applied at the soil map: ::" to "The methods are applied on the soil map: :: " AR. Done. Page 1, line 21: Change to ": : :(or is not): : :" AR. Done. Page 1, line 24: Delete "the" in front of "uncertainties" and add s on "soil map" AR. Done. Page 1, line 13: Change ": : : propagated based on: : :" to ": : : propagated through: : :" AR. Done. Page 3, line2: Please add "soil" in front of "map" and change "map" to "maps" AR. Done. Page 3, line 4: Change to "In the present study, we investigate impacts of uncertainty of soil properties on hydrological states and fluxes" AR. Done. Page 3, line 4-5: change to "Uncertainty in soil properties is: ::" AR. Done. Page 3. line 5: Add comma before but AR. Done. Page 3, line 9-10: Change to "The extent of the impact is expected to decrease with increasing the aggregation area and to disappear at a specific domain size." AR. Done. Page 3-4, line 31/1: change to ": : :smaller soil units that have not been detected: : :" AR. Done. Page 4, line 27: Change "..can be also.." to ".. can also be.." AR. Done. Page 5, line 1: Change "field" to "fields" AR. Done. Page 5, line 12: Please rephrase ": : : reveals a soil prevalently clay loam..." AR. Done. Page 5, line 32: Change ": : :i.e., area smaller than: : :" to ": : :i.e., patterns smaller than: : :" AR. Done. Page 6, line 11: Change ": : : and its packages" to ": : : using add-on packages". Maybe you should write which packages you use? AR. Done. We cited the reference of the package i.e., Pebesma, E.J., 2004. Multivariable geostatistics in S: the gstat package. Comput. Geosci. 30, 683–691. doi:10.1016/j.cageo.2004.03.012 Page 6, line 23: Please rephrase the sentence. I suggest to change it to ": : :into 3 layers; the first layer is 5 cm, the second layer is 20 cm and the third has a variable thickness." AR. Changed as suggested.

Page 6, line 30: I suggest changing ", which covers around 16430 grid cells" to "resulting in 16432 grid cells"

Page 7, line 7: Delete "in" after "yield" AR. Done. Page 7, line 25: Delete "the" in front of "analysis #1" AR. Done. Page 8, line 3: Delete "the" in front of "analysis #2" AR. Done. Page 8, line 5: Add a reference to figure 2 where the location of the grid point are seen AR. Done. Page 8, line 7-8: Change "In particular, for the analysis #3" to "For use in analysis #3" AR. Done. Page 8, line 16: Change "cell" to "cells" AR. Done. Page 8, line 18: Delete "the" in front of "analysis #4" AR. Done. Page 8, line 18: Change "showed" to "shown" AR. Done. Page 9, line 9: Change "down row" to "bottom row" AR. Done. Page 9, line 17: Change to ": : :highly identifiable and the sharp changes between the units are still preserved." AR. Done. Page 9, line 22-23: Please rephrase sentence (starting with however), it is difficult to understand. AR. Done. Page 10, line 5: Change "detailed" to "described" AR. Done. Page 10, line 8: Add a comma in after magnitude AR. Done. Page 10, line 10: Change to (i.e., standard deviation > 0 for the resolution of 60 x 60 km2). Maybe the same sentence in line 13 can be shortened? AR. Line 10 changed and line 13 shortened. Page 10, line 11: Delete "the" in front of "spatial scale". AR. Done. Page 10, line 14: Add a comma in after domain AR. Done. Page 10, line 29: Change to ": : : are shown for the transect.." AR. Done. Page 10, line 32: Change ": : :over the catchment..." to ": : :across the catchment..." AR. Done. Page 11, line 5: Change "affected on" to "affected in" AR. Done. Page 12, line 23: Change "the first grid cell" to "grid cell A" and "the second grid cell" to "grid cell B" AR. Done. Page 12, line 25: Delete "the" in front of "grid cell" AR. Done. Page 14, line 11: Please rephrase "it is notable a certain spread.." AR. Done. Page 14, line 12: Add s on "catchment" AR. Done. Page 14, line 23: Change "with reducing the" to "with decreasing" AR. Done.

Page 14, line 25: Change "increasing" to "increasingly" AR. Done. Page 15, line 3: Change ": : : across the all number of grid cells: : : " to ": : : across all the grid cells: : : " AR. Done. Page 15, line 16: Change "enphasises" to "emphasises" AR. Done. Page 15, line 18: Add d on compensate AR. Done. Page 15, line 21: Add s on subcatchment AR. Done. Page 15, line 25: Please add u in "groundwater" AR. Done. Page 15, line 29: Delete "the" before "soil properties" AR. Done. Page 15, line 31: Put a ": " after "follow" AR. Done. Page 16, line 1: Delete "the" in front of uncertainty AR. Done. Page 16, line 15: Change "different" to "other" (end of line) AR. Done. Page 16, line 18: Delete "the" in front of "spatial and temporal resolution" AR. Done. Page 16, line 20: Change "This resolution is referred as: ::" to "This resolution is referred to as the: ::" AR. Done. Page 16, line 33: Please rephrase ": : : with physical sound: : : " AR. Done. Page 17, line 1: Change "soil map" to " a soil map" AR. Done. Page 17, line 7: Please change last part of line to ": : : are shown not to be.." AR. Done. Page 17, line 9: Please add "on stream flow" after "model performance" AR. Done. Page 17, line 12: Change "input factor" to "input parameters" AR. Done. Page 17, line 13: Change "soil map" to " a soil map" AR. Done. Page 17, line 17: change to ": : :(or is not): : :" AR. Done.

Authors' Response to Reviewer 2

Specific comments:

RC. Parameter maps. Currently the mentioned link between soil properties, model parameters and model fluxes is never explicitly stated within the paper. The reader is left alone with a set of references (see: p. 6, l. 25f) that lead to a detailed description of the model with all its pedotransfer functions. I believe that many readers would appreciate if the (most) relevant pedotransfer functions are explicitly mentioned (e.g. within a table). Following that reasoning, one would also like to see some maps (they should be readily available) of the change of parameters with respect to a change in

soil properties. Such maps could be made in a similar fashion as Fig. 4, where a perturbation example for percentage of clay is mapped. This would make it easier for readers to connect the information shown in Fig. 3, Fig. 4 and Fig. 7. The paper does already provide ample amounts of supplementary material, so it could at least be added there.

AR. We provided in the supplementary material the list of the pedotransfer functions integrated in the model (see Table S1), and two additional maps showing saturated water content and saturated hydraulic conductivity estimated based on these PTFs. Please note that the plots were reorganized to facilitate the comparison (See Figure S4-S5-S6). These new table and figures were also cited in the manuscript (see P7L8 and P9L24-26).

RC. P 5. l. 24. This comment might be a little nit-picky. It would be nice if the authors would elaborate a little about the mentioned bounds. One or two sentences would already suffice to make the picture clearer: Besides the 100% upper bound in the sum, the soil properties are (obviously) also bound at 0%. Furthermore there sum always results in 100%. That is (of course) the reason why the silt does not need to be perturbed directly, as it is fully defined by the other two textural classes. Now, this is all clear to readers but I think it would be good to be mentioned explicitly. Furthermore, one might expect that these bounds mess with Gaussian noise in some minor way. Intuitively one would expect that this lowers the uncertainty in some areas of the basin. This notion is dispelled in Fig. 5. It shows clearly that these theoretic influences are as good as non-existent. They are not are not visible at all! Nevertheless, there are areas in Fig. 3 (and 4) where the soil properties are exactly at these bounds – the sand is at 100% and the clay is at 0%. I think one should at least be clarify these aspects, even if they seem to be irrelevant for the resulting analysis (as shown in Fig. 6). On the other hand, it could be that I am missing something.

AR. We think the comment is relevant for a more general understanding of the perturbation methods and we added this information in the revised manuscript (see P6L17-22).

RC. P. 5, l. 21-22 and Table 1. The noise is defined by its variance. I would propose to use the standard deviation instead. This would (a) make it easier for readers to interpret (clearer units, simpler dispersion summary); (b) bring closer to the units used for the analysis (Fig. 5 shows the standard deviation (!) of the clay-ensemble); and (c) sync in a rather abstract way with the uncertainty quantification (the coefficient of variation is defined through the standard deviation).

AR. We changed the values by referring to the standard deviation in the revised version of the manuscript. Please note, however, that the variograms (e.g., exponential model used for the spatial correlated method) are usually defined by variance and correlation length. To our knowledge, it would be rather uncommon to present the variogram model in terms of standard deviation. And for this reason, the variograms depicted in the supplementary material (Figure S2 and Figure s3) are not modified.

RC. P. 13, l. 18-22. These sentences need to be reformulated somehow. The intention or setup is not clear to me. In concrete: The phrasing "streamflow at the catchment outlet" is used twice, which makes it difficult to understand.

AR. For clarity, in the revised manuscript, we decided to focus the discussion to the characteristic correlation lengths introduced by each perturbation method in section 3.4. In section 3.5 we focused the discussion to the implication for the model application by referring to Figure 10. By that, text was extensively revised.

RC. P. 17, l.5-20. The section is understandable as such, but could be rephrased to make it easier to read. As I understand it, the gist is that fine-grained soil information is important for local states and fluxes but not for integrated ones. As it stands now, one reads at first that the fine soil resolution is not important for model performance (p.17, l. 9), only to read a view later that the fine soil resolution is important for model performance (p.17, l. 14-15). Readers will infer the meaning from the context, but the phrasing seems to be needlessly difficult.

AR. The text was rephrased to make the message easier to read (see P19L1-17).

On the eEffects of the uncertainty in soil properties on the simulated hydrological state and fluxes at different spatio-temporal scales

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Abstract. Soil properties show high heterogeneity at different spatial scales and their correct characterization remains a 10 crucial challenge over large areas. The aim of the study is to quantify the impact of different types of uncertainties that arise from the unresolved soil spatial variability on simulated hydrological states and fluxes. Three perturbation methods are presented for the characterization of the-uncertainties in soil properties. The methods are applied at-on the soil map of the upper Neckar catchment (Germany), as example. The uncertainties are propagated based on through the distributed hydrological model mHM to assess the impact of the simulated state and fluxes. The model outputs are analysed by

- 15 aggregating the results at different spatial and temporal scales. These results show that the impact of the different uncertainties introduced in the original soil map is equivalent when the simulated model outputs are analysed at the model grid resolution (i.e., 500 m). However, several differences are identified by aggregating state and fluxes at different spatial scales (by subcatchments of different sizes or coarsening the grid resolution). Streamflow is only sensitive to the perturbation of long spatial structures while distributed state and fluxes (e.g., soil moisture and groundwater recharge) are only sensitive
- 20 to the local noise introduced to the original soil properties. A clear identification of the temporal and spatial scale for which finer resolution soil information is (or is not) relevant is unlikely to be universal. However, the comparison of the impacts on the different hydrological components can be used to prioritize the model improvements in specific applications, either by collecting new measurements or by calibration and data assimilation approaches. In conclusion, the study underlines the importance of a correct characterization of the uncertainty in soil properties. With that, soil maps with additional information regarding the unresolved soil spatial variability would provide a strong support to hydrological modelling applications.
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1 Introduction

The prediction of mathematical environmental models is affected by uncertainty which arises from inadequate conceptual and mathematical representations of the processes (uncertainty in model structure), inadequate and insufficient knowledge and characterization of system forcing (uncertainty in boundary conditions) and limitations in the measurements or identification of model parameters (parameter uncertainty) (Beven, 2007, 2001; Refsgaard et al., 2007; Tartakovsky et al., <u>2012)</u>(Beven, 2001, 2007; Refsgaard et al., 2007; Tartakovsky et al., 2012)</u>. The need to quantify the predictive uncertainty has led to the development of probabilistic (stochastic) frameworks in many disciplines of environmental sciences and engineering (Altarejos-García et al., 2012; Di Baldassarre et al., 2010; Dubois and Guyonnet, 2011; Savage et al., 2016; Seiller and Anctil, 2014). Nowadays rigorous quantification of uncertainty is an integral part of science-based predictions

5 and decision support systems (Beven, 2007; Farmer and Vogel, 2016; Liu and Gupta, 2007; Montanari and Koutsoyiannis, 2012).

In hydrological studies, several sources of uncertainty have been studied ranging from atmospheric forcing (Aguilar et al., 2010; Raleigh et al., 2015; Samain and Pauwels, 2013; Vázquez and Feyen, 2003; Zhu et al., 2013) to geology structures (Comunian et al., 2015; Hansen et al., 2014; He et al., 2015; Zech et al., 2015). Among these, the uncertainty related to the

- 10 soil properties has been widely analysed. Soil properties show in fact high heterogeneity at different spatial scales with a hierarchy of spatial structures (Burrough, 1983; Heuvelink and Webster, 2001; Vogel and Roth, 2003) and complex interactions with environmental conditions (Lin, 2010). Despite international initiatives exist to improve the current status of soil characterization (Chaney et al., 2016; Heuvelink et al., 2016; Pelletier et al., 2016; Shangguan et al., 2014), detailed information of the spatial heterogeneity of the soil properties over large areas remains a crucial challenge. For this reason, an
- 15 increasing number of hydrological modelling studies aim to integrate the uncertainty in soil properties that arise from the unresolved spatial heterogeneity for a proper quantification of the uncertainty of the model results. Since soil properties play a crucial role in the entire water cycle, this topic crosses research fields from lower atmosphere (De Lannoy et al., 2014; Garrigues et al., 2015; Guillod et al., 2013; Osborne et al., 2004; Yu et al., 2014) and surface water (Anderson et al., 2006; Geza and McCray, 2008; Li et al., 2013; Livneh et al., 2015; Salazar et al., 2008) to water and solute transport to groundwater systems (Besson et al., 2011; Hennings, 2002; Yu et al., 2014).
- Despite its relevance, however, relative simple assumptions are adopted to characterize the uncertainty in soil properties and to understand its effect on the hydrological response. In several studies the uncertainty is characterized based on relatively small number of scenarios (Baroni et al., 2010; Christiaens and Feyen, 2001; Guber et al., 2009; Herbst et al., 2006; Hohenbrink and Lischeid, 2015; Islam et al., 2006; Mirus, 2015; Moeys et al., 2012) or by a simple random noise (i.e.,
- variance) added to the original soil properties (Arnone et al., 2016; Chaney et al., 2015; Deng et al., 2009; Garrigues et al., 2015; Han et al., 2014; Loosvelt et al., 2011). Other studies explicitly integrate the complex heterogeneity of the subsurface and the uncertainty in the soil properties is characterized based on spatial correlated random fields i.e., specifying variance and correlation length (Binley et al., 1989; Fan et al., 2016; Fiori and Russo, 2007; Merz and Plate, 1997; Meyerhoff and Maxwell, 2011). Moreover, many of above-mentioned studies focused on the effect of the uncertainty in soil properties on a
- 30 selected hydrologic variable at specific temporal and spatial scale e.g., rainfall-runoff events (e.g., Arnone et al., 2016; Fan et al., 2016), simulated evapotranspiration (e.g., Garrigues et al., 2015), soil moisture distributions (e.g., Liao et al., 2014) or groundwater recharge (e.g., Moeys et al., 2012). Simultaneous assessments of different hydrological components of the water balance at different spatial and temporal scales are rare. In addition, due to the different settings used in the studies, it is not possible to draw general conclusions about the role of the uncertainty in soil properties. In some cases the refined

spatial information of soil properties does not contribute to a more accurate prediction (e.g., Li et al., 2013). In other studies the results showed to be very sensitive to the soil properties (e.g., Livneh et al., 2015). These controversial results foster the debate on the need (or not) of finer resolution <u>soil maps</u> in the different modelling applications (Baveye, 2002; Baveye and Laba, 2015; Heuvelink and Webster, 2001).

- 5 In the present study, we investigate the impacts of the uncertainty of the soil properties on hydrological states and fluxes. The uUncertainty in soil properties is characterized by three different methods that are consistent in the added noise (i.e., variance), but they differ in the perturbation of the soil spatial structure i.e., correlation length. The first two methods were previously used in other studies (e.g., Fan et al., 2016; Han et al., 2014). The third method is developed in the present study to introduce small scale soil variability while preserving the original spatial patterns. By that, We we hypothesize that local
- 10 responses of a hydrological system, like evapotranspiration and soil moisture, will be strongly impacted by the uncertainty introduced at small spatial scale. However, integrated responses like the streamflow aggregate local responses over large areas. We hypothesize that this integrated response will be less impacted by soil properties uncertainty. The extent of the impact is expected should to decrease with increasing the aggregation area and to disappear at a specific domain size. In such a condition, the system is stated to be spatially ergodic as the model output is not any more sensitive to the perturbation i.e.,
- 15 we have the equivalence between spatial and ensemble statistics (Dagan, 1989; Rubin, 2003). The paper is structured as follow. First, the perturbation methods used for the characterization of the uncertainty of the soil properties are presented. The specific case study is described presenting the catchment, the data used and the specific settings of the perturbation methods. The hydrological model is then introduced together with the uncertainty analysis conducted for the assessment of the effect of the uncertainty in soil properties on the simulated state and fluxes. The results are discussed in
- 20 section 3 focusing on the effect of the differences detected at different spatial and temporal scales. Final remarks are presented in the conclusions section.

2 Methods

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2.1 Soil perturbation methods

In this section, the three statistical methods to characterize the uncertainty in soil properties are presented. A sketch for describing the methods is provided in <u>Figure 1Figure 1</u>, where one <u>hypothetical horizontal</u> transect <u>through a soil map</u> with three soil units characterized by different percentages of sand is shown as example.

The first method (hereafter denoted as Random Error method - RE) is based on the assumption that the nominal value in each soil unit is the only source of uncertainty while the spatial patterns (i.e., soil units) are considered to be correct. To fulfil this assumption, a simple Gaussian random noise is defined with zero mean and given variance (Figure 1Figure 1, step R1). Random values are sampled from the distribution and added to the nominal value of soil properties of each soil unit (Figure

1Figure 1, step R2). This approach was commonly used in several studies with the focus of understanding the effect of the

soil properties in forward uncertainty analysis of model response (e.g., Deng et al., 2009) or for creating the forward ensemble in data assimilation tests (e.g., Han et al., 2014).

In the second method (hereafter denoted as Spatially Correlated method - SC), a similar assumption of additive random values is considered. However, it is also assumed that the uncertainty arises from the presence of smaller soil units that <u>could</u> have <u>not</u>_detected in the original soil map (Hennings, 2002). To fulfil this assumption, a spatial structure (i.e., variance and correlation length - CL) is defined (<u>Figure 1Figure 1</u>, step S1). Based on that, a spatially correlated random field with zero mean is created (<u>Figure 1Figure 1</u>, step S2) and added to the original soil map (<u>Figure 1Figure 1</u>, step S3). Random fields are used in this approach to create variability as discussed by Goovaerts (2001) with which simulated short-range components well represent the complexity of the small-scale spatial structure. Readers interested in the details of the generation of random fields are referred to Deutsch and Journel (1998), Goovaerts (1997) and Isaaks and Srivastava (1989).

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Finally, in the third approach (hereafter denoted as Conditional Points method - CP), it is assumed that the nominal value of the original soil units represents some point locations within this unit but their positions are unknown. The uncertainty arises from the spatial variability within these point locations that is not resolved in the original soil map. To fulfil this assumption, points are randomly distributed over the soil map and the soil properties are associated to each position (Figure 1Figure 1,

15 step S1). These values are used to calculate the spatial structure i.e., the empirical variogram (Figure 1 Figure 1, step S2). A variogram model is fitted and a conditional random field is created using the sampled locations as conditional points (Figure 1, step S3). It has to be noted that the CP method has some similarity with the pilot points approach used for the calibration of hydrogeological models (Carrera et al., 2005). The main difference is the use in this method of new points at each iteration i.e., the points are located in different positions for each created conditional random field.

- 20 It is noteworthy that additional statistical methods for the analysis of soil map are presented in literature (Goovaerts, 2011; Heuvelink et al., 2016; Kempen et al., 2009; Minasny and McBratney, 2016; Odgers et al., 2014). However, the aim of these methods is to downscale/disaggregate the information available in the original soil map and not to characterize its uncertainty. For this reason, these statistical methods are based on environmental covariates (i.e., environmental variables that co-vary with soil variability) known at higher resolution (i.e., digital elevation model or land use) and they require
- 25 relative well knowledge of the soil formation and the specific settings to adopt (Kerry et al., 2012; Nauman and Thompson, 2014; Subburayalu et al., 2014; Du et al., 2015). On the contrary, the three methods selected and developed in the present study represent relative simple approaches only based on the information available in the original soil map. They can be applied for the characterization of any type of soil properties (e.g., texture, saturated hydraulic conductivity, soil depth etc.) and they reflect different assumptions regarding the uncertainties in the soil properties. For this reason, they can be tuned to
- characterize uncertainty for soil maps of any scales and they can be easily used to any modelling studies (e.g., sensitivity
 analysis or data assimilation). Combinations of the methods can <u>also</u> be-<u>also</u> considered when needed i.e., soil map affected by different types of uncertainties.

2.2 Study area

The numerical experiments are conducted in the upper Neckar catchment (Figure 2Figure 2) that was extensively investigated in previous hydrological studies (Kumar et al., 2010; Samaniego et al., 2010a, 2010b; Wöhling et al., 2013b). This catchment is located in the central uplands of Germany and comprises a catchment area of approximately 4000 km².

5 The catchment has a gradient in elevation from 250 m to 1015 m a.s.l. with a mean elevation of 550 m. The catchment is prevalently characterized by cropped fields and forest but with a remarkable high degree of urbanization (11%). The longterm mean annual precipitation is around 920 mm a⁻¹.

Observed meteorological data, i.e., precipitation as well as minimum, maximum and average daily temperature, were provided by the German Meteorological Service (DWD; www.dwd.de/). These observations have been interpolated to a

- 4 x 4 km forcing dataset for the hydrological model using external drift kriging. The potential evapotranspiration is estimated 10 using the Hargreaves-Samani method (Hargreaves and Samani, 1985). Data characterizing the land surface are a digital elevation model (Federal Agency for Cartography and Geodesy), a soil map at the scale 1:1000000 (Federal Institute for Geosciences and Natural Resources - BGR), a hydrogeological map (Federal Institute for Geosciences and Natural Resources - BGR), and land cover information (CORINE, European Environmental Agency - EEA, 2009). The soil map
- used in the present study (BGR 1:1000000) contains soil texture (percentage of sand, clay and silt) and bulk density [g cm⁻³] 15 for each soil unit (i.e., polygon of the soil map) and for each soil horizon. For this study, these vertical discretization is not accounted for and the soil properties of each-vertical soil horizons are aggregated averaged to the total soil depth of 2 m (Figure 3Figure 3). The soil within the catchment map reveals a soil prevalently clay loam but with a relatively high spatial variability represented by 29 soil units (polygons) of different size within the catchment. All these data are discretized to a 20

spatial resolution of 100 x 100 m^2 . Readers interested in more details on data-set and the processing may refer to Kumar et al. (2010), Samaniego et al. (2010b) and Zink et al. (2016). The spatial distributions of cumulative rain, potential evapotranspiration, land use and the mean annual leaf area index are shown in the supplementary material (see Figure S1).

2.3 Settings of the soil perturbation methods

In this section, the specific settings of each statistical perturbation method used for the characterization of the soil properties 25 are described. The three methods are used independently to generate three different ensembles to identify the impact of the different uncertainties introduced in the original soil map on simulated state and fluxes.

Considering the random error method (see Figure 1Figure 1), a Gaussian random additive noise is used with variance standard deviation $\frac{50}{10}$ [$\%^2$] and 0.057 [g² cm⁻⁶²] for soil texture (sand and clay) and bulk density, respectively (Table 1Table 1). A correlated sampling design is used to preserve the correlation between the original soil properties (e.g., negative

30 correlation between sand and clay) and the values are forced to a realistic range i.e., not negative texture values and sum of textural fractions does not exceed 100%. These variances noises are selected to perturb the soil properties within the original soil class i.e., it is assumed that the exact values of the soil properties are unknown but the soil class (e.g., clay loam) is correct. Similar ranges were also applied in other studies (Han et al., 2014; Hennings, 2002).

For the spatially correlated method (see Figure 1Figure 1), the parameters for the variogram and co-variogram models are selected to be consistent with the perturbation introduced in the random error method (Table 1Table 1). In particular, exponential variogram models are prescribed with the same effective variances noises used in the random error method (i.e., standard deviation 50-7 [$\%^2$] and 0.057 [g^2 cm⁻⁶³] for texture and bulk density, respectively) and preserving the correlation between the original soil properties. The correlation length of 3 km is selected to represent relative small spatial patterns that were not captured by the original soil map i.e., area-patterns smaller than most of the soil units (Figure 3Figure 3). The variogram and co-variograms models selected are shown as supplementary material (see Figure S2).

- Finally, considering the conditional points method (see Figure 1Figure 1), tests are conducted to identify the density of the conditional points within the soil map. One sample at every 3 x 3 km² is found to introduce the same variance-noise prescribed by the other two methods (Table 1Table 1). A stratified spatial random sample is used to distribute the points within each soil units. Based on these, two nested exponential variogram and co-variogram models are fitted to the experimental variograms based on ordinary least-squares residuals (Pebesma, 2004). These variogram models are used to
- 15 create the conditional random fields. The experimental variograms and the fitted models for one realization (i.e., one random field) are shown, exemplarily, in the supplementary material (Figure S3).
 In each method, the perturbed values are forced to a realistic range i.e., texture values between 0% and 100% and the sum of textural fractions equal 100%. By that, it has to be noted that these constraints (i) could modify the Gaussian noise introduced and (ii) could lower the uncertainty in areas of the basin where the actual values are close to the bounds. These constrains did
- 20 <u>not affect the spatial patterns of the generated soil maps of the present study due to the relative small perturbation introduced</u> and the presence of limited areas with extreme texture conditions. However, attention has to be paid in cases where these features are more relevant.

For each method, an ensemble of 100 realizations is created to characterize the uncertainty in soil properties. The analysis is conducted with the statistical software R 3.2.x (R Core Team, 2013) <u>using add-on and its</u>-packages (Pebesma, 2004). The multi-variate conditional random fields were generated with GCOSIM3D code (Gómez-Hernández and Journel, 1993).

2.4 The hydrological model mHM

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The effect of the uncertainty in soil properties as characterized by the three perturbation methods on hydrological states and fluxes is analysed using the hydrological model mHM. The mesoscale Hydrological Model mHM (Kumar et al., 2013; Samaniego et al., 2010b) is an open source, spatially distributed hydrologic model (www.ufz.de/mhm). It considers

30 interception, snow accumulation and melting, soil water retention, evapotranspiration, percolation, and runoff generation as main hydrologic processes. The Multiscale Parameter Regionalization (MPR) embedded in mHM allows for the application of the model at various locations and scales (Kumar et al., 2013; Rakovec et al., 2016). MPR accounts for sub-grid variabilities by estimating model parameters at the scale of the morphological input, e.g. 100 x 100 m². Subsequently, these

parameters are upscaled to the model resolution <u>based on different average rules (e.g., harmonic mean, arithmetic mean etc.)</u>. For a detailed model description and the <u>regionalization_MPR</u> scheme interested readers may refer to Samaniego et al. (2010b) and Kumar et al. (2013). For this study, the soil within mHM is discretized into 3 layers, <u>ending in 5 cm, 25 cm, and a variable depth below ground the first layer is 5 cm, the second layer is 25 cm and the third has a variable thickness</u>. The

- 5 depth of latter is based on the information provided by the soil map (2 m). Based on the soil textural properties, mHM estimates effective parameters for porosity, hydraulic conductivity, field capacity and permanent wilting point using a set of pedotransfer functions (Cosby et al., 1984; Twarakavi et al., 2009; van Genuchten, 1980; Zacharias and Wessolek, 2007)(e.g., Zacharias and Wessolek, 2007). The list of the functions is reported in Table S1 in the supplementary material.
- The model was calibrated and validated in previous studies showing very good capability to match streamflow measurements at catchment of different sizes (Kumar et al., 2010, 2013; Samaniego et al., 2010b; Wöhling et al., 2013b). The same parameterization is used for the present study. We establish the mHM over the Upper Neckar catchment at 500 m spatial resolution <u>resulting in which covers around 164320</u> grid cells. The model run is conducted at an hourly time scale. All simulations are conducted with a five year model spin up time (1985 - 1989) to minimize the effect of inappropriate initial conditions. The implications of uncertain soil properties are evaluated showing the uncertainty in simulated routed
- streamflow (*SF*), generated runoff at every grid cell (*Q*), actual evapotranspiration (*AET*), volumetric soil moisture (*SM*) in the upper 30 cm and groundwater recharge (*GWR*). For each perturbation method 100 simulations were performed which yield in-a total of 300 simulations. The results obtained during one year of forward simulation (1990) are shown, as example. This year is selected to represent average climate condition of the area (i.e., two rain seasons concentrated in spring and fall and a relatively dry summer season) but with a relatively high variability within the catchment (see Figure S1 in supplementary material).

2.5 Uncertainty analysis at different spatio-temporal scales

The uncertainty in simulated states and fluxes is quantified based on the coefficient of variation (CV [%]) to allow comparability between the results obtained in the different model outputs. Assuming a generic variable v representing simulated state or fluxes, CV is calculated as follow:

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$$CV_{i,t}^m = \frac{\sigma_{i,t}^m}{\mu_{i,t}^m} \, 100 \tag{1}$$

where σ is the standard deviation of the variable *v* at each cell *i* and time *t* calculated based on each perturbation method *m* (i.e., random error method, spatially correlated method or conditional points method) as follow:

$$\sigma_{i,t}^{m} = \sqrt{\frac{1}{N_{ens}} \sum_{j=1}^{Nens} \left(v_{i,t}^{m,j} - \mu_{i,t}^{m} \right)^2}$$
(2)

with N_{ens} the number of ensemble members (i.e., 100), *j* one single ensemble member and μ representing the mean of the ensemble at each cell *i* and time *t* calculated as follow:

5
$$\mu_{i,t}^m = \frac{1}{N_{ens}} \sum_{j=1}^{Nens} v_{i,t}^{m,j}$$
 (3)

The values obtained with the three perturbation methods are compared by aggregating the simulated states and fluxes at different spatial and temporal resolutions. In particular, four analyses are conducted (<u>Table 2</u><u>Table 2</u>).

In the analysis #1, the spatial variability of the uncertainty of the simulated state and fluxes is presented i.e., depending on the geographical location within the catchment. In this case the average *CV* calculated for the entire simulation period (i.e., one year) in each grid cell is quantified as follow:

$$\overline{CV}_i^m = \frac{1}{T} \sum_{t=1}^T CV_{i,t}^m \tag{4}$$

15 where T is the number of simulations time steps (i.e., 365 days). This value is used to represent and discuss the average uncertainty obtained in the specific cell *i* and its spatial variability within the catchment.

In the analysis #2 (Table 2Table 2), the daily temporal dynamic of the uncertainty obtained at each grid cell is discussed. For this reason the $CV_{i,t}^m$ calculated at the daily time step (Eq. 1) is directly compared for two representative grid cells selected within the catchment (see Figure 2, point A and B).

The uncertainty on simulated states and fluxes is further compared by aggregating the model outputs at different resolution to identify the effect of the spatial scale on the performance of the model as discussed by Refsgaard et al. (2016). In particular, for the use in analysis #3 (Table 2Table 2), subcatchments of different sizes are defined based on 36 gauging stations located within the catchment (see Figure 2Figure 2), and tThe effect of the uncertainty in soil properties to the streamflow routed to the outlet (SF) of each subcatchment is then compared. For the other simulated model outputs (i.e., evapotranspiration, soil moisture and groundwater recharge), the values of each grid cell within the subcatchment are aggregated calculating the average of simulated model output *v* obtained at the finer resolution as follow:

$$\bar{v}_{sc,t}^{m,j} = \frac{1}{N_{sc}} \sum_{i=1}^{N_{sc}} v_{i,t}^{m,j}$$
(5)

where N_{sc} is the number of grid cells within the subcatchment *sc*. The value $\bar{v}_{sc,t}^{m,j}$ is used in Eq. (1 - 4) to calculate and compare the coefficient of variation of the mean simulated state and fluxes for the subcatchments of different sizes.

Finally, in the analysis #4 (<u>Table 2</u>Table 2), the effect of the aggregation of states and fluxes at different resolutions is further analysed based on the approach showed shown by Hansen et al. (2014) and Rasmussen et al. (2012). In this case, the generic model output *v* is averaged coarsening the model grid at different resolutions r_d (i.e., $r_2 = 2$ km, $r_4 = 4$ km, $r_8 = 8$ km, $r_{16} = 16$ km, $r_{32} = 32$ km). These values are substituted in Eq. (1 - 3) to calculate the coefficient of variation in each new coarsened grid cell *i*. In this analysis the average of the *CV* across the entire domain and over the entire simulation period

(i.e., 365 days) is calculated as a summary statistic as follow:

$$\overline{CV^{m,r_d}} = \frac{1}{T} \sum_{t=1}^{T} \frac{1}{N_r} \sum_{i=1}^{N_r} CV_{i,t}^{m,r_d}$$
(6)

10 with N_r representing the number of cell *i* within the coarsened domain r_d .

In addition to the spatial dimension, in this study, the same procedure is also repeated for each spatial aggregation r_d considering a time aggregation t_d . In particular, all the simulated model outputs *v* obtained at daily time step are averaged at $t_{10} = 10$ days, $t_{30} = 30$ days, $t_{60} = 60$ days, $t_{120} = 120$ days and $t_{180} = 180$ days, respectively. These values are substituted in Eq. (1-4) to calculate the coefficient of variation in each temporal aggregation t_d and they are considered to represent the uncertainty in the simulated state and fluxes in case the averaged values are used in the assessment of the performance of the model.

The four analyses described above are conducted based on the results of 100 simulations obtained with the distributed hydrological model for each perturbation methods. A total of 300 simulations, analysed in 12 cases, are discussed in the results section (Table 2Table 2).

20 3. Results and discussion

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3.1 Perturbation of the soil properties

Three methods are used to perturb the values of the original soil map i.e., sand [%], clay [%] and bulk density [g cm⁻³]. This section discusses the results obtained on clay percentage exemplarily. Similar results are obtained for the other soil properties (see supplementary material, Figure S4 - S7) and for the related soil hydraulic parameters (see supplementary

- 25 <u>material, Figure S4 S6</u>). For each method, <u>Figure 4Figure 4</u> (top row) shows one realization of the perturbed clay percentage. In addition (<u>Figure 4Figure 4</u>, <u>bottomdown</u> row), one transect along the catchment is selected and the clay percentage of the original soil map, of one realization and of the ensemble spread (95% confidence interval) are shown. The longitudinal transect was selected to capture the strong variability in the soil units detected along this direction (see Figure 3).
- 30 The random error method (RE) preserves the shapes of the soil units and perturbs just the nominal values. The results therefore show how the contrasts between the soil units are modified and in some cases are exaggerated. For this reason, it is

noteworthy to observe that this method could create non-realistic spatial patterns since soil properties usually show smother changes in space. The results obtained based on the spatially correlated method (SC) show that the shapes of the soil units are still highly identifiable and, with that, still the sharp changes between the units are <u>still</u> preserved. With this method, however, the random fields superimposed to the original soil map were selected with a correlation length of 3 km (see

- 5 section 2.3). For this reason, smaller spatial structures than the original soil units are introduced and the sharp changes in the soil properties are not uniformly distributed all over the soil unit. Finally, considering the results obtained with the conditional points method (CP), the results show that the soil units are visible but the contrasts are completely smoothed eliminating the artefact of the original soil map. However, a wider spread in the ensemble in comparison to the perturbation obtained within the unit is visible in this transition between the soil units. the spread (gray area) in this transition between
- 10 soil units (polygons) is wider than the spread detected within each soil unit. The effect is due to the combination of the uncertainty introduced to the nominal value of the soil property and to the exact position of the transition between the soil units.

The spread of the realizations is quantitatively evaluated based on the standard deviation of the ensemble. In particular, <u>Figure 5</u>-a represents the probability distribution of the standard deviation of the clay percentage calculated at every

- 15 grid cell within the catchment (i.e., 16432 grid cells) for each method. Results obtained based on the three methods, on average, exhibit a high consistency in representing the uncertainty over the catchment (i.e., average standard deviation is for all the methods 7%). However, some differences are detected in the distributions. The random error method (RE) shows a normal distribution with a relatively low variability (i.e., the coefficient of variation of the distribution is 6%). This is the consequence of the fact that the soil properties within the catchment are perturbed with almost the same magnitude.
- 20 Similarly, the spatially correlated method (SC) shows also a normal distribution but with a slightly wider variability (i.e., *CV* = 8%). In contrast, the results obtained with the conditional points (CP) method show a very different distribution that is skewed with a tail to high extreme values. These high spreads in the soil realizations are located in the transition between the soil units, in particular if the transition is sharp (see Figure 4Figure 4).

Finally, the standard deviation of the values is calculated by aggregating the map for different subcatchments (Figure

- 25 <u>5</u>Figure 5b) and at different grid resolution (Figure 5Figure 5c) based on the analysis detailed described in section 2.5. The spreads of the realizations obtained with the three perturbation methods are of similar magnitude considering the finer resolution (e.g., resolution $< 1 \times 1 \text{ km}^2$). The differences between the perturbation methods become more relevant by aggregating to a coarser resolution. In other words, this means that the introduced uncertainty is in the same order of magnitude, but the spatial patterns are different. In the random error method (RE), the spread is relatively high at all scales
- 30

and even the mean value of the soil properties of the entire catchment is perturbed (i.e., standard deviation > 0 for the resolution of 60 x 60 km²). The spread obtained with the spatially correlated method (SC) decreases more rapidly with increasing the spatial scale. This is consistent with the correlation length prescribed to the random fields used in this method (i.e., 3 km). However, it is noteworthy to observe how also the average mean value of the soil properties over the entire catchment is still perturbed also with this method (i.e., standard deviation > 0 also for the resolution of 60 x 60 km²). This is

explained by the fact that the random fields superimposed to the original soil map have zero mean over a rectangular domain, but the average can be different when masked to the catchment. The behaviour is exaggerated when a relatively long correlation length in comparison to the size of the domain is used. Finally, the results of the conditional points method (CP) show how just the small scale is perturbed and the spread of the ensemble drops already at the resolution of 5 km to

5 disappear completely when the average over the catchment is considered. This behaviour is consistent with the density of the samples used to constrain the random fields (i.e., one sample every $3 \times 3 \text{ km}^2$).

3.2 Spatial variability of the uncertainty of state and fluxes

increases close to the catchment outlet (see Figure 2Figure 2).

In this section, the spatial variability of the uncertainty of the simulated state and fluxes is presented. In this analysis (see section 2.5, Table 2Table 2, uncertainty analysis #1), the mean coefficient of variation over time (i.e., 1 year) is calculated for each grid cell (i.e., 16432 grid cells) and the spatial distributions obtained with the three perturbation methods are

- 10
- compared (Figure 6Figure 6).

The uncertainties of all hydrological states and fluxes obtained with each perturbation methods provide nearly the same magnitude and the same spatial variability, with correlation coefficients calculated between the results obtained by each method higher than 0.8. For this reason, only the spatial distribution of the coefficient of variations (CVs) of the model

- outputs over the entire catchment obtained with the random error method (RE) is shown as example (Figure 6, left). 15 The results obtained with all the three perturbation methods are shown only for the same transect depicted in Figure 4Figure 4 (Figure 6, right) to facilitate the visualization of the relatively small differences (Figure 6, right).
- In general, the results obtained based on all the three perturbation methods show that, independently from the perturbation method used, the uncertainty in the total runoff (O) and groundwater recharge (GWR) are highest, with an average CV20 estimated over across the catchment of 115% and 4415%, respectively. Soil moisture (SM) and actual evapotranspiration (AET) appear to be less sensitive to the soil variability with an average CV of 3% and 1%, respectively (Figure 6, left). The relatively small differences detected based on the use of different perturbation methods are located in the transition between the soil units (Figure 6Figure 6, right) and they are attributed to the higher uncertainty in the soil properties introduced in those areas (see Figure 5Figure 5a). Overall, a strong spatial variability in the uncertainty in the model outputs 25 is detected with some differences depending on the considered model output. The uncertainty in runoff is more pronounced in the north-west areas, actual evapotranspiration appears to be more affected on-in the central-north areas. High uncertainty in simulated soil moisture is distributed across the catchment and the uncertainty in simulated groundwater recharge

For a further interpretation, the spatial variability of the uncertainty in the simulated model outputs is compared to different boundary conditions and input properties. In particular, the correlation coefficients between the spatial distribution of the 30 CVs of each model outputs and the spatial distribution of clay [%], the mean leaf area index (LAI $[m^2 m^{-2}]$) and the annual sum of the potential evapotranspiration (PET [mm]) calculated over the simulation period (i.e., one year) are calculated. These three factors are selected to represent soil, vegetation and atmospheric conditions, respectively. The spatial distributions of these factors are shown in the supplementary material (see Figure S1). Correlation coefficients for each perturbation method are calculated and average and standard deviation based on the three methods are depicted in Figure 7. The results obtained with the three different methods are consistent between each other also in this comparison (i.e., as represented by the small error bars) showing different correlations for each model output (Figure 7). The uncertainty in the

- 5 runoff is stronger correlated to the actual value of the soil property. This correlation can be visually identified comparing the spatial variability detected in Figure 6Figure 6 (right) and the spatial variability of the soil property shown in Figure 4Figure 4 for the same transect. The uncertainty in the actual evapotranspiration is strongly correlated to the atmospheric conditions and, to less extend, to the soil properties. Finally, the uncertainties of the soil moisture and groundwater recharge are correlated to the vegetation characteristics, with a relatively lower effect of soil properties.
- 10 To further evaluate the different correlations found for each simulated model output, the correlation matrix between the uncertainty (CV) detected in each model output is calculated (Table 3Table 3). On the one hand, the results show that the uncertainties in the fluxes are positively correlated (correlation coefficient > 0.2). This means that when the uncertainty in one specific flux is relatively high, also other fluxes to some degree are uncertain. On the other hand, it is interesting to note that the uncertainty in soil moisture is highly correlated to the groundwater recharge (correlation coefficient = 0.7) while the
- 15 correlations to the other model outputs are negligible (correlation coefficient < 0.2). This means that the model could have relatively low uncertainty in soil moisture but high uncertainty in evapotranspiration or runoff and vice-versa. These results are consistent among all the three perturbation methods and they support the use of both state and fluxes for a proper assessment of the performance of hydrological models as it was underlined in several other studies (Ahmadi et al., 2014; Baroni et al., 2010; Conradt et al., 2013; Delsman et al., 2016; McCabe et al., 2005; Rakovec et al., 2016; Silvestro et al., 20 2015; Wöhling et al., 2013a; Zink et al., 2016).

3.3 Temporal variability of the uncertainty of state and fluxes

The daily temporal variability of the uncertainty on the simulated state and fluxes obtained at the model resolution (i.e., 500 m) is presented in this section. In this analysis (see section 2.5, Table 2Table 2, analysis #2), the coefficient of variation at daily time step for each perturbation method obtained in two grid cells selected within the catchment are compared for an illustrative purpose. The two locations A and B are depicted in Figure 2 Figure 2. The two grid cells are characterized by (see 25 also supplementary material, figure S1) a remarkable difference in the rain (i.e., almost 1600 mm a⁻¹ and 1000 mm a⁻¹, respectively), by different land use (i.e., crop field and deciduous forest, respectively) but they have almost the same soil properties (i.e., 19% sand and 59% clay for grid cell A; 19% sand and 66% clay for grid cell B). The grid cells are selected to represent different uncertainties of the model outputs (see Figure 6Figure 6). In particular, grid cell A shows relatively high uncertainty in simulated soil moisture ($CV \sim 4\%$) while grid cell B show relatively low uncertainty ($CV \sim 2\%$). The

values of simulated state and fluxes for comparison (i.e., mean value and 95% confidence interval of the ensemble simulations obtained with the random error method).

The results show how the uncertainty of the total runoff is relatively high during the entire simulation period with a tendency of increasing the uncertainty during high flow period. The behaviour is particularly evident in the grid cell B (i.e., correlation

- 5 coefficient between *CV* and simulated runoff is 0.6). In contrast, the actual evapotranspiration is close to the potential rate for most of the simulation period and, for this reason, it is not sensitive to changes in soil properties. As expected, the uncertainty is only detected during summer time when soil moisture is relatively low and the actual evapotranspiration rate decreases in comparison to the potential evapotranspiration. This result also explains the low correlation detected between the uncertainty in soil moisture and evapotranspiration (sees Table 3). The temporal variability obtained for the uncertainty
- 10 in soil moisture shows a more complex behaviour depending on the grid cell considered. In grid cell A, the *CV* increases with the increasing of soil moisture while it decreases in grid cell B. The different behaviours are explained comparing the actual soil moisture values. In the first-grid cell <u>A</u>, the soil moisture values are relatively low (0.25 m³ m⁻³) while, in the secondgrid cell <u>B</u>, the values are close to saturation (0.4 m³ m⁻³). Finally, groundwater recharge shows also a strong temporal dynamic with a tendency of higher uncertainty with increasing groundwater recharge in the-grid cell A (correlation 15 coefficient = 0.2) while the correlation is negligible in grid cell B (correlation ~ 0).
- Overall, it is noteworthy to observe how the uncertainty in soil moisture is relatively constant in time while the uncertainty in the fluxes shows much stronger temporal variability. This different behaviour can be explained considering two main characteristics. On the one hand, the presence of non-linear relations between state and fluxes generates threshold behaviour for which the uncertainty in soil moisture could be limited to ranges where the fluxes are not affected. This is for instance the
- 20 case with-when the uncertainty inhigh soil moisture is limited to relative wet conditions (i.e., above plant stress) and for this reason it does not affect the and evapotranspiration-. Similarly, the uncertainty in or low soil moisture could be limited in relative dry conditions and the runoff could be generation affected. On the other hand, there is a tendency of compensation in the uncertainty in the model outputs for which an overestimation of the actual evapotranspiration could be related to an underestimation of the groundwater recharge (or vice-versa). In these conditions the soil moisture could be still
- 25 well defined without providing any indication of the degradation of the model performance. As a result, the low uncertainty in soil moisture does not represent the overall uncertainty in the model. Overall, this analysis underlines the role of the different hydrological conditions (e.g., dry or wet) for understanding the effect of the uncertainty in soil properties on the model response. Similar conclusions are supported by the use of temporal sensitivity and identifiability analysis to better capture the role of the different uncertainties in the parameters analysed (Ghasemizade et al., 2017; Guse et al., 2015; Pianosi
- 30 and Wagener, 2016; Wagener et al., 2003).

3.4 Spatial uncertainty of state and fluxes at subcatchments

The uncertainties (CV) of simulated state and fluxes are also compared by aggregating the results over subcatchments of different sizes (see section 2.5, Table 2Table 2, analysis #3). The results obtained with the three perturbation methods are shown against the catchment size in Figure 9Figure 9.

- 5 As presented by Refsgaard et al. (2016), the uncertainty in all the model output reduces with increasing catchment area. Assuming an arbitrary threshold (i.e., CV) acceptable for a specific model application, this analysis identifies, on the one hand, the spatial limit of model predictive capability for the specific application. On the other hand, it identifies the resolution below which it might become important to have a better understanding of the soil spatial variability. This resolution is referred to as the Representative Elementary Scale (RES) by Refsgaard et al. (2014) and it provides a clear and
- 10 simple framework for the assessment of the performance of distributed models. However, it is interesting to note that the three perturbation methods generated very different results and, assuming the same arbitrary threshold for each method, different RESs are identified. The random error method (RE) creates higher uncertainty in all the subcatchments and even the mean of states and fluxes over the entire catchment is uncertain (i.e., $60 \times 60 \text{ km}^2$). The spatial correlated method (SC) shows a similar pattern but the uncertainty is lower in all the subcatchments. Finally, the uncertainty based on the condition
- points method (CP) decreases already at small catchment sizes of e.g., 2 x 2 km². 15 The different results obtained with the three perturbation methods have important implication when considering the specific model application. For instance, it is notable how the streamflow at the catchment outlet, that was used for calibration of the model in previous studies (Kumar et al., 2013; Samaniego et al., 2010b), is sensitive only to the perturbation of long soil spatial structures introduced with the random error method. In contrast, the streamflow at the catchment outlet is not
- 20 sensitive to the perturbations introduced at small scale (e.g., conditional points method). On the one hand, this means that small soil variabilities are not relevant when the model application focuses on the streamflow prediction. On the other hand, this results underlines that it is not possible to infer (e.g., calibrate) these small spatial soil patterns based on the streamflow observations. The contrary behaviour is noted for the distributed hydrological states and fluxes (evapotranspiration and groundwater recharge). These distributed model output represent in fact local conditions. For this reason, they show to be sensitive to all type of perturbation introduced. This means that these localized state and fluxes can be used to infer local 25 properties but it is not possible to use this type of observations to calibrate the values for larger areas. For this reason, the use
 - of e.g., remote sensing products as total water storage anomalies and evapotranspiration is an effective approach for constraining and improving model parameterization (e.g., Rakovec et al., 2016).

The different results in the uncertainty in the model outputs obtained by the use of the different perturbation methods are

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consistent with the different uncertainties introduced in the soil properties (Figure 5Figure 5b). This result supports the conclusion that the differences-different RESs identified are related to the underlying correlation length scale (CL) used in each perturbation method (Refsgaard et al., 2016). The random error method perturbs the value of the entire soil units and it does not generate spatially ergodic soil parameters fields i.e., aggregated hydrological responses still show a non-vanishing uncertainty at large catchment. The spatial correlated method introduced correlation length of 3 km and the effect on the uncertainty in the aggregated model output reached a remarkable reduction (e.g., > 90% of the uncertainty in all the simulated state and fluxes is reduced) when the entire catchment is considered. Finally, the conditional points method introduces uncertainty only at small spatial scales while the longer spatial patterns are preserved. For this reason the domain is ergodic already at relatively low catchment size (i.e., 20 x 20 km²).

- These characteristic lengths (<u>Representative Elementary Scale catchment dimension DRES</u> *vs.* correlation length CL) identified by the use of the three different soil perturbation methods are in agreement with previous studies conducted in surface hydrology (Binley et al., 1989; Fan et al., 2016; Herbst et al., 2006; Merz and Plate, 1997) and in stochastic subsurface hydrology (Dagan, 1989; Fiori and Russo, 2007; Rubin, 2003), where a suitable value for defining ergodic
- 10 system (or representative scale) was found to be ~ DRES/CL > 20. For this reason, it is notable the equivalence of the ergodic concept introduced in subsurface hydrology (Dagan, 1989; Rubin, 2003) and the RES concept in the case the arbitrary threshold (i.e., *CV*) is set to zero. However, two important characteristics can be further underlined. First, it is notable how a certain spread in the uncertainty of catchments with similar size provide different degrees of uncertainties in the model output. This behaviour is in agreement with the results discussed in section 3.2 showing different sensitivity on the
- 15 soil perturbation depending on the different boundary conditions and model set-up (i.e., depending on the location within the catchment). For this reason, the results support the difficulties to find a universal representative scale<u>RES</u> that is not affected by the uncertainty in the soil properties for the entire catchment. Despite th<u>e RES concept is scale</u>-has some differences with the Representative Elementary Area concept (REA) introduced in past literature (see Refsgaard et al. (2016) for further discussion about the differences), it is noteworthy how this result is in agreement with the difficulties for finding a universal
- 20 REA discussed also in those studies (e.g., Fan and Bras, 1995; Wood et al., 1988). Secondly, different sensitivities arise depending on the model output considered. Soil moisture is more sensitive to the perturbation of soil properties since the relative change between the three different methods is highest among the four hydrological variables under investigation. This behaviour is particularly evident when considering the results obtained with the random error method. In this case, a relatively small perturbation introduced in the mean of the entire catchment (60 x 60 km²) explains already most of the
- 25 uncertainty in the simulated soil moisture. The uncertainty slightly increases with reducing decreasing the catchment size. In comparison, all the fluxes are much less affected by the small perturbations introduced for the entire catchment but they become increasingly pronounced with a decreasing catchment size. For this reason, the representative scale<u>RES</u> is also different depending on the model output considered.

3.5 Uncertainty of state and fluxes at different spatio-temporal scales

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30 A similar scaling analysis is also conducted averaging state and fluxes by coarsening the grid resolution and by aggregating at different temporal scales (see section 2.5, <u>Table 2</u>Table 2, analysis #4). The results obtained with the three perturbation methods are presented in <u>Figure 10</u>Figure 10. The spatial aggregation of the model output, as represented in the x-axis of Figure 10Figure 10, shows the same effect obtained by aggregating the model output based on catchment of different sizes (Figure 9Figure 9). For this reason, the two analyses (aggregating by catchment vs. coarsening the grid resolution) can be considered equivalent in the identification of the effect of the spatial resolution on the uncertainty in the model outputs. However, the results described in the previous

5 sections showed also a strong variability in space and in time. For this reason, the use of the mean coefficient of variation calculated over time and across the all number of the grid cells to represent the model performance (Eq. 6) can be misleading e.g., underestimating the actual uncertainty in the model output. Instead, the use of the maximum CV calculated over the catchment and over the simulated period could be used to better represent the model performance. In addition, the extension of the analysis to the temporal scale (y-axis in Figure 10Figure 10) emphasizes the clear trade-off of the performance of the

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model between the spatial resolution and the temporal resolution. In particular, assuming an arbitrary threshold (i.e., CV) as a limit of model predictive capability for the specific model application (Refsgaard et al., 2016), the spatial and temporal analysis shows how the simulated state and fluxes should be aggregated in time to maintain acceptable performance when decreasing the space resolution.

- On the one hand, this analysis can support the use of the model results for specific model applications. On the other hand, it 15 would be possible to identify when it might become important to have a better representation of the soil spatial variability for the improvement of the performance of the model. Overall, also for this spatio-temporal analysis,
 - Finally, it is noteworthy how these conclusions are supported by the results obtained with all the three perturbation methods are very different and - However, the RES (here defined as the spatial and temporal actual scale at which it might become important - (or not) - to have a better understanding of the soil spatial variability) strongly depends on the perturbation
- 20 methods used. Since the three perturbation methods reflect different uncertainties introduced in the original soil map, the analysis enphasises emphasises the importance to identify the correct approach to characterize the uncertainty for each model application and for further model improvements. For the specific case study presented here, it is notable how the streamflow at the catchment outlet (i.e., spatial resolution > 32 km), that was used for calibration of the model in previous studies (Kumar et al., 2013; Samaniego et al., 2010b), is sensitive only to the perturbation of long soil spatial structures introduced
- 25 with the random error method. For this reason, it could be assumed that the uncertainty in soil properties indrouced with the RE method that affects the simulated streamflow at the catchment outlet is well compensated by the calibration (Kumar et al., 2013; Samaniego et al., 2010b). For this reason, and the random error RE method could not represent the actual uncertainty in the specific model application as it shows to strongly effect also the simulated streamflow. The same could be considered for the results obtained with the spatially correlated method, as soon as subcatchments of different sizes are used
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- conditional points method). On the one hand, this means that small soil variabilities are not relevant when the model application focuses on the streamflow prediction. On the other hand, this results underlines that it is not possible to infer (e.g., calibrate) these small spatial soil patterns based on the streamflow observations. For this reasonOn the contrary, the conditional points method appear to be a simple and effective method to preserve the general spatial pattern of the original

soil map while introducing uncertainty due to the unresolved spatial heterogenity within the soil units. This type of uncertainty affects the streamflow only for small subcatchments (size $< 1 \text{ x}_1 \text{ km}^2$) while introducing relavant effects on the local hydrological states (i.e., soil moisture) and fluxes (e.g., groundwater recharge). This method therefore could be considered as a valuable choice to account for the uncertainty of soil properties for this type of model applications i.e., when well calibrated hydrological models based on streamflow measurements are used.

- A different behaviour is noted for the distributed hydrological states and fluxes (evapotranspiration and groundwater recharge). These variables represent in fact local conditions (i.e., spatial resolution < 1 km) and they show the same degree of uncertainty independently from the perturbation method used. This means that these localized state and fluxes can be used to infer local properties but it is not possible to use this type of observations to calibrate the values for larger areas. For this
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reason, the use of e.g., remote sensing products as total water storage anomalies and evapotranspiration is an effective approach for constraining and improving local model parameterization.

4. Conclusions

In the present study, the uncertainty in soil properties is characterized based on three statistical perturbations methods. This uncertainty is propagated applying the distributed hydrological model mHM. The uncertainty in the simulated states and fluxes are analysed at different spatial and temporal scales. The main conclusions are summarized as follow:

- 1. The effect of the-uncertainty in soil properties depends on the hydrological model output. In particular, the uncertainty in the fluxes are relatively positive correlated i.e., if the uncertainty in one of the simulated flux is high, also the other fluxes show, to some degrees, uncertainties. On the contrary, the uncertainty in the simulated soil moisture shows a more complex relation as its uncertainty does not always represent the overall uncertainty in the simulated fluxes. This behaviour is explained by the non-linear relation between state and fluxes and the occurrence of threshold conditions in the model response. For this reason, these results support the need of multi-variable (e.g., soil moisture and streamflow) for a proper assessment of the overall performance of hydrological models (Rakovec et al., 2016; Zink et al., 2016)-and the use of temporal diagnostic tools for a better understanding of the input output space (Ghasemizade et al., 2017; Guse et al., 2015; Pianosi and Wagener, 2016; Wagener et al., 2003).
- The uncertainty in state and fluxes depends on the specific locations and on the boundary conditions. In particular, the uncertainty in the model results shows strong temporal and spatial variability over the catchment with complex interactions to local environmental conditions (i.e., atmosphere, vegetation and soil). These results highlight the role of specific model settings (i.e., parameters and boundary conditions) for a proper characterization of the model response and the difficulty to generalize the result for other applications (i.e., different study areas and weather conditions). Similar conclusions were obtained based on sensitivity analysis conducted using hydrological models in different other catchments (e.g., Shin et al., 2013; van Griensven et al., 2006) and they support the use of spatial

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and temporal diagnostic tools for a better understanding of the input-output space (Ghasemizade et al., 2017; Guse et al., 2015; Pianosi and Wagener, 2016; Wagener et al., 2003).

- The uncertainty in state and fluxes depends on the spatio-temporal resolution used for the analysis. In particular, the 3. uncertainty in all the model outputs decreases with increasing the spatial and temporal resolution. Assuming an arbitrary threshold (e.g., CV) acceptable for a specific model application as proposed by Refsgaard et al. (2016), this scaling analysis identifies the so-called Representative Elementary Scale (RES,). on-On the one hand, the spatial and temporal this scale resolution represents the resolution at which the model output produces acceptable limits of predictive capabilityeould be used. This resolution is referred as Representative Elementary Scale (RES) by Refsgaard et al. (2016) and it provides a clear and simple framework for the assessment of the performance of distributed models. On the other hand, this Representative Elementary Scale it identifies the resolution below which it might become important to have a better understanding of the soil spatial variability. For this reason, this analysis shows to be a simple and practical approach for the assessment of spatially distributed models. However, in the present study it was underlined the difficulties to identify a universal RES since it depends on locations, time and model output. For these reasons, the present study proposes Two three possible possible extensions of the RES approach-as proposed by Refsgaard et al. (2016): are the use of the maximum CV, and the temporal aggregation and the assessment of multi-variables. The former-first extension should better capture the model performance due to the strong spatial and temporal variability that could be present in the uncertainty within the catchment. The latter second extension could be used to emphasize the trade-off between temporal and spatial resolution of the model application. Finally, the third extensions should provide a better assessment of the overall performance of the model.
- 4. The assumptions and the methods used for the characterizations of the uncertainty in the-soil properties plays a crucial role. In particular, the above conclusions are supported by the results obtained with all the three soil perturbation methods used in this study. However, the absolute value of the uncertainty detected in state and fluxes at different spatial and temporal scales strongly depends on the perturbation methods. For this reason, the results underline the importance to properly characterize the specific sources of uncertainty to transform a pure numerical exercise to specific results with physical sound-that are able to better support the model applications. The three methods developed and used in the present study represent three relatively simple approaches that can be considered to account for different types of uncertainty in the-a soil map. In particular, this study proposes a new perturbation method (here called Conditional points method) able to introduce small scale soil variability while preserving the original spatial patterns. In this context, however, the availability of soil map with additional information regarding not only the actual mean value within the soil units but also information representing the unresolved variability (variance and correlation length of the subdominant soil units) would provide a strong support to hydrological modelling applications.

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5. Finally, the analysis conducted in the present study identifies important information to be used for possible model improvement, either by collecting additional data regarding the soil properties or for inverse modelling and data assimilation frameworks. In particular, integrated fluxes like river discharge of large catchments are shown not to be not-impacted by small scales soil variabilities (i.e., variancestandard deviation) but only by long spatial structures (i.e., long correlation lengths). For this reason, additional details in the soil map do not improve the model performance on streamflow but rather other sources of uncertainties should be considered for that (e.g., vegetation properties). For the same reason, this integrated observation cannot be used to infer local parameters (i.e., parameter of finer resolutions) but only mean characteristics of the input factor parameters (e.g., average soil properties over the soil units). On the contrary, local state and fluxes show to be very sensitive to local variation in the soil properties (i.e., variancestandard deviation). For this reason, a soil map with finer resolution data is found to be an important factor for decreasing the uncertainty in these local model outputs further improvement of the performance of the model. For the same reason, these simulated outputs can be used to infer local soil parameters in calibration or data assimilation. Despite the transition between these two extreme conditions for which the uncertainty in soil properties is (or is not) important is quite smooth, it depends on the output considered and on the boundary conditions, this analysis provides a strong support to prioritize the model improvements in specific model applications. For this reason, similar studies can be considered for comparing statistical methods to characterize other sources of uncertainty relevant in catchment hydrology (e.g., precipitation, vegetation parameters).

Acknowledgment. The study was supported by the Deutsche Forschungsgemeinschaft (DFG) under CI 26/13-1 in the 20 framework of the research unit FOR 2131 "Data Assimilation for Improved Characterization of Fluxes across Compartmental Interfaces" and by the Helmholtz Alliance - Remote Sensing and Earth System Dynamics (HGF-EDA). <u>The</u> <u>comments provided by the two anonymous Reviewers were highly appreciated.</u>

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Figure 1. Soil perturbation methods (Random <u>Error Method RE</u>, Spatially <u>Correlated method SC</u> and <u>Conditional Points methods CP</u>). The panel on the left shows the fraction of sand of <u>a hypothetical horizontal transect trough</u> the original soil map as orange line. Within the transect three different soil units are observed, which leads to three different sand contents. Each row of the right panels depicts the steps

5 for setting the perturbation methods. The blue line depicts one realization of the respective perturbation method. The detailed description of these methods can be found in section 2.1. Abbreviations: var – variance, CL – correlation length.



Figure 2. Location of the upper Neckar catchment within Germany. The positions of the 36 gauging stations (red points) used for defining the subcatchments, the transect (dashed black line) and the two grid cells analysed (green points A and B) are depicted on the map.



Figure 3. Soil maps of sand [%], clay [%] and bulk density [g cm⁻³] and area [km²] of the soil units within the catchment.





Figure 4. Soil realizations obtained for the percentage of clay based on the Random Error method (RE, left column), Spatially Correlated method (SC, middle) and Conditional Points method (CP, right column). The top row shows one realization for each method and the transect (dashed black line). The bottom row depicts the spread of the 100 realizations by using the 5th and 95th percentile for the selected transect (gray area). The red line depicts one realization, whereas the black line shows the percentage of clay by the original soil map.



Figure 5. (a) Probability distribution of the standard deviation of the clay percentage based on 100 realizations of the soil map calculated for all grid cells and each method (RE = Random Error method; SC = Spatially Correlated method; CP = Conditional Points method). The mean and coefficient of variation of the distribution are indicated in parenthesis. (b) Standard deviation calculated by aggregating the clay

5 percentage at subcatchments with different size. (c) Standard deviation calculated by aggregating the clay percentage at different grid resolutions.



Figure 6. Spatial variability of the uncertainty (*CV*) in the simulated model outputs (Q = generated runoff; *AET* = evapotranspiration; *SM* = soil moisture; *GWR* = groundwater recharge). On the left column, the results obtained based on the Random Error method (RE) over the entire catchment are depicted together with the position of the transect (dashed black line) and the two grid cells (blue points). On the right column, the *CVs* along the transect within the catchment based on the three perturbation methods (Random Error RE; Spatially

5 right column, the *CVs* along the transect within the catchment based on the three perturbation methods (Random Error RE; Spatially Correlated SC; Conditional Points CP) are plotted. Vertical dashed gray lines indicate the position of the grid cells A and B within the transect. Please note that all the plots have individual limits for the y-axis.



Figure 7. Correlation coefficient calculated between the spatial distributions of the uncertainty (*CV*) of the simulated model outputs (Q = runoff; *AET* = actual evapotranspiration; *SM* = soil moisture; *GWR* = groundwater recharge) and local environmental conditions (the clay [%] is used to represent the soil; annual mean leaf area index *LAI* [m² m⁻²] is used to represent the vegetation; cumulative potential evapotranspiration *PET* [mm a⁻¹] is used to represent the atmospheric water demand). The bars represent the mean of the correlation coefficients obtained with the three perturbation methods and the error bars the standard deviation.



Figure 8. Daily temporal variability of the uncertainty in state and fluxes (Q = runoff, AET = evapotranspiration, SM = soil moisture, GWR = groundwater recharge) obtained in two grid cells within the catchment obtained based on the random error method (RE). The mean (black) and the 95% confidence interval (gray) of the ensemble is depicted together with the coefficient of variation (CV) calculated at daily time step (red). Note the log y-axis for Q and GWR. Location of grid cell A and B is shown in Figure 2 and Figure 6.

Figure 9. Uncertainty, i.e., coefficient of variation (*CV*), of hydrological state and fluxes at catchments with different sizes (SF = streamflow, AET = evapotranspiration, SM = soil moisture, GWR = groundwater recharge). Exponential curves are fitted to the data. Please not that all figures have individual limits for the y-axis.

Figure 10. Spatio-temporal uncertainty analysis by aggregating the model results at different spatial and temporal resolutions. The three columns refer to the results obtained by (left) Random Error Method - RE, (middle) Spatially Correlated method - SC and (right) Conditional Points method - CP. The rows refers to the different model outputs (i.e., Q = runoff, AET = actual evapotranspiration, SM = soil moisture; GWR = groundwater recharge). Note that a smooth approximation is depicted to facilitate the visualization of the actual CVs values.

Table 1. Parameter settings for each perturbation method (Random Error, Spatially Correlated and Conditional Points). Variogram models used for the Spatially Correlated and Conditional Points methods are showed in the supplementary material (Figure S2 and Figure S3, respectively).

| Perturbation method | Parameters | Specific settings | |
|-------------------------|--|---|--|
| Random Error | VarianceStandard deviation | 50-7 [% ²] and 0.057 [g ² cm ⁻⁶³] for texture and bulk density, respectively | |
| Spatially correlated | Variograms and co-variograms models | Exponential models (see supplementary material, Figure S2) | |
| | Effective variance | 50 [% ²] and 0.05 [g ² cm ⁻⁶] for texture and bulk density, respectively. <u>These values are equivalent to the noise (i.e., standard</u> <u>deviation) introduced with the random error method.</u> | |
| | Correlation length | 3 km | |
| Conditional Points | Density of samples | 1 sample every 3 x 3 km ² | |
| | Variograms and co-variograms models | Two nested exponential models fitted to the empirical variograms and co-variograms (see supplementary material, Figure S3) | |

Table 2. Overview of the uncertainty analysis presented and discussed.

| | | Perturbation methods | | |
|----|--|--|--|--|
| n. | Uncertainty analysis | 1. Random Error | 2. Spatially Correlated | 3. Conditional Points |
| 1. | Local uncertainty: long term temporal mean of <i>CV</i> at every grid point $\mu_{i,t}^{m} = \frac{1}{N_{ens}} \sum_{j=1}^{N_{ens}} v_{i,t}^{m,j}$ $\sigma_{i,t}^{m} = \sqrt{\frac{1}{N_{ens}}} \sum_{j=1}^{N_{ens}} (v_{i,t}^{m,j} - \mu_{i,t}^{m})^{2}}$ $CV_{i,t}^{m} = \frac{\sigma_{i,t}^{m}}{\mu_{i,t}^{m}}$ $\overline{CV}_{i}^{m} = \frac{1}{T} \sum_{t=1}^{T} CV_{i,t}^{m}$ | Section 3.2 Figure 6 (left & right black line) | Section 3.2 Figure 6 (right, red line) | Section 3.2 Figure 6 (right, green line) |
| 2. | Local uncertainty: CV at every grid point $CV_{i,t}^m$ | Section 3.3 Figure 8 | Section 3.3 | Section 3.3 |
| 3. | Uncertainty by aggregating model output at catchment of different sizes $\bar{v}_{sc,t}^{m,j} = \frac{1}{N_{sc}} \sum_{i=1}^{N_{sc}} v_{i,t}^{m,j}$ $\sigma_{sc,t}^m = \sqrt{\frac{1}{N_{ens}}} \sum_{j=1}^{Nens} \left(v_{sc,t}^{m,j} - \mu_{sc,t}^m \right)^2$ $CV_{sc,t}^m = \frac{\sigma_{sc,t}^m}{\mu_{sc,t}^m}$ | Section 3.4 Figure 9 (black line) | Section 3.4 Figure 9 (red line) | Section 3.4 Figure 9 (green line) |
| 4. | Uncertainty by aggregating model output at different spatial (r_d) and temporal (t_d) resolutions $\overline{CV^{m,r_d,t_d}} = \frac{1}{T} \sum_{t=1}^{T} \frac{1}{N_r} \sum_{i=1}^{N_r} CV_{i,t}^{m,r_d,t_d}$ | Section 3.5 Figure 10 (left) | Section 3.5 Figure 10 (middle) | Section 3.5 Figure 10 (right) |

Table 3. Correlation matrix of the uncertainty (*CV*) of the model outputs (Q = generated runoff; A*ET* = actual evapotranspiration; *SM* = soil moisture; *GWR* = groundwater recharge) obtained with the three perturbation methods (Random Error, Spatially Correlated and Conditional Points).

| | | Q | AET | SM |
|-----|---------------------------|------|------|-----|
| | Random Error | 0.3 | | |
| AET | Spatially Correlated | 0.4 | | |
| | Conditional Points | 0.3 | | |
| | Random Error | -0.1 | 0.0 | |
| SM | Spatially Correlated | -0.1 | -0.1 | |
| | Conditional Points | -0.0 | 0.1 | |
| | Random Error | 0.2 | 0.2 | 0.7 |
| GWR | Spatially Correlated | 0.2 | 0.1 | 0.7 |
| | Conditional Points | 0.3 | 0.3 | 0.7 |

Supplementary Material

to paper

"On the e<u>E</u>ffect<u>s</u> of <u>the</u> uncertainty in soil properties on <u>the</u> simulated <u>hydrological</u> state and fluxes at different spatio-temporal scales<u>"</u>

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This supplementary material contains <u>seven six</u> additional figures <u>and one table</u> that support the discussion presented in the study.

Figure S1. Cumulative rainfall $[mm a^{-1}]$ and cumulative potential evapotranspiration $[mm a^{-1}]$ during the simulated year (1990); main land use within the catchment; mean leaf area index (LAI $[m^2 m^{-2}]$) over the same simulated year (1990). Transect (dashed black line) and locations of the two grid cells are also depicted.

Figure S2. Semivariograms and co-semivariograms models used in the spatially correlated method for sa = Sand [%], cl = Clay [%], bd = bulk density [g cm⁻³], respectively. Distance is in meters.

Figure S3. Experimental semivariograms and co-semivariograms (circle) and fitted models (black line) used for the conditional points method for sa=Sand [%], cl = Clay [%], bd = Bulk density [g cm⁻³], respectively. Distance is in meters.

Figure S4. From top row, As Figure 4 but for sand [%]: soil_single_realizations of sand [%], bulk density B_d [g cm⁻³], saturated water content θ_s [m³ m⁻³] and saturated hydraulic conductivity k_{sat} [cm d⁻¹] based on the Random Error method (RE, left column), Spatially Correlated method (SC, middle) and Conditional Points method (CP, right column). Please note that a log scale was used to for the saturated hydraulic conductivity (fourth row). The top row shows one realization for each method and the transect (dashed black line). The bottom row depicts the spread of the 100 realizations by using the 5th and 95th percentile for the selected transect (gray area). The red line depicts one realization, whereas the black line shows the percentage of sand by the original soil map.

Figure S5. From top row, As Figure 4 but for bulk density [g cm⁻³]: soil realizations based on the Random Error method (RE, left column), Spatially Correlated method (SC, middle) and Conditional Points method (CP, right column). The top row shows one realization for each method and the transect (dashed black line). The bottom row depicts the spread of the 100 realizations of sand [%], bulk density B_d [g cm⁻³], saturated water content θ_s [m³ m⁻³] and saturated hydraulic conductivity k_{sat} [cm d⁻¹] by using the 5th and 95th percentile (gray area) for the selected transect (gray area). The red line depicts one realization, whereas the black line shows the bulk densityvalues based on by the original soil map. Please note that a log scale was used to for the saturated hydraulic conductivity (forth row).

Figure S6. As Figure 5 but for sand [%]: (a) probability_Probability_distribution of the standard deviation (*sd*) of the sand percentagesoil properties (sand [%], bulk density B_d [g cm⁻³], and soil hydraulic parameters (saturated water content θ_s [m³ m⁻³] and saturated hydraulic conductivity k_{sat} [cm d⁻¹]) based on 100 realizations of the soil map-calculated for all grid cells and each method (RE = Random Error method; SC = Spatially Correlated method; CP = Conditional Points method). The mean and coefficient of variation of the distribution are indicated in parenthesis. (b) Standard deviation (*sd*) calculated by aggregating the

sand percentagevalues at subcatchments with different size. (c) Standard deviation (sd) calculated by aggregating the sand percentagevalues at different grid resolutions.

Figure S7. As Figure 5 but for bulk density [g cm⁻³]: : (a) probability distribution of the standard deviation of the bulk density based on 100 realizations of the soil map calculated for all grid cells and each method (RE = Random Error method; SC = Spatially Correlated method; CP = Conditional Points method). The mean and coefficient of variation of the distribution are indicated in parenthesis. (b) Standard deviation calculated by aggregating the bulk density at subcatchments with different size. (c) Standard deviation calculated by aggregating the bulk density at different grid resolutions. Table S1. Regionalization functions of the soil hydraulic parameters^a.

| Parameter | Regionalization function | Description/reference |
|------------------------------------|--|---|
| Residual water content | $	heta_r=0$ | |
| Saturated water content | $\theta_{s} = \gamma_{1} + \gamma_{2} P_{clay} + \gamma_{3} B_{d} \text{if } P_{sand} < 66.5\%$ $\theta_{s} = \gamma_{4} + \gamma_{5} P_{clay} + \gamma_{6} B_{d} \text{if } P_{sand} \ge 66.5\%$ | |
| Shape parameter | $n = \gamma_7 + \gamma_8 (P_{sand})^{\gamma_9} + \gamma_{10} (P_{clay})^{\gamma_{11}} \text{ if } P_{sand} < 66.5\%$ $n = \gamma_{12} + \gamma_{13} (P_{sand})^{\gamma_{14}} + \gamma_{15} (P_{clay})^{\gamma_{16}} \text{ if } P_{sand} \ge 66.5\%$ | Parameters of the soil retention curve (van Genuchten, 1980) estimated based on Zacharias and Wessolek (2007) |
| Shape parameter | $ln(\alpha) = \gamma_{17} + \gamma_{18}P_{sand} + \gamma_{19}P_{clay} + \gamma_{20}B_d \text{if } P_{sand} < 66.5$ $ln(\alpha) = \gamma_{21} + \gamma_{22}P_{sand} + \gamma_{23}P_{clay} + \gamma_{24}B_d \text{if } P_{sand} \ge 66.5\%$ | |
| Shape parameter | $m = 1 - \frac{1}{n}$ | |
| Soil moisture at wilting point | $\theta_{wp} = \frac{\theta_s - \theta_r}{[1 + (\alpha h)^n]^m}$ | with <i>h</i> the matric potential at -1500 [kPa] |
| Soil moisture at field capacity | $\theta_{fc} = \theta_s n^{\gamma_{25} log_{10}(q_{fc}/k_{sat})}$ | <u>Based on Twarakavi et al.</u> (2009) and assuming that the drainage flux q_{fc} is 0.01 |

| | | $[cm d^{-1}]$ |
|-------------------------------------|---|----------------------------|
| Saturated hydraulic conductivity | $log_{10}(k_{sat}) = \gamma_{26} + \gamma_{27} * P_{sand} + \gamma_{28} * P_{clay}$ | <u>Cosby et al. (1984)</u> |

^a Percentage of sand (P_{sand}), percentage of clay (P_{clay}), bulk density [g cm⁻³] (B_d). Coefficients (γ_t) used for establishing those functional relationships are regarded as calibration parameters in mHM.