



# Identifying, characterizing and predicting spatial patterns of lacustrine groundwater discharge

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**Abstract.** Lacustrine groundwater discharge (LGD) can play an important role for lake water balances and lake water quality. However, quantifying LGD and their spatial patterns is challenging as pronounced spatial variability is paired with a large spatial extent of the aquifer-lake interface and factors controlling LGD patterns are not well understood. We used intensive field measurements including 520 vertical temperature profiles in the near shore area, sediment temperature measurements with a fibre-optic cable along 6 transects from shoreline to shoreline and radon measurements of lake water samples to identify LGD patterns at a lake in north eastern Germany. Sediment characteristics, topographic indices and gradients of the groundwater flow field were considered as potential controls of small scale and large scale LGD patterns. The results revealed that LGD was concentrated in the near shore area with stronger rates and higher variability in the northern part of the lake. LGD generally decreased with distance to shore and offshore LGD was insignificant except for some local hotspots of LGD on steep steps towards the lake bottom. Large scale groundwater inflow patterns were correlated with topography and the groundwater flow field whereas small scale patterns correlated with grain size distributions of the lake sediment. Regression models using external controls as explanatory variables had limited power to predict LGD rates, but results encourage the use of topographic indices and sediment heterogeneities as an aid for targeted experimental designs.

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## 1 Introduction

By linking groundwater with the surface water body, lacustrine groundwater discharge (LGD) can strongly control lake water quality and lake water budgets. Hence, all processes affecting quantity and quality of groundwater could also affect lake water quantity and quality (Winter et al., 1998; Rosenberry et al., 2015). To understand the vulnerability of groundwater dominated lakes it is not only important to know the total volume of groundwater lake exchange, but also the spatial patterns of LGD (Meinikmann et al., 2013; Lewandowski et al., 2015).

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### 1.1 Spatial patterns of lacustrine groundwater discharge and their potential controls

In an isotropic homogenous aquifer, the exchange between groundwater and lake is expected to follow a distinct pattern: as sloping groundwater water tables meet the flat surface of the lake, groundwater inflow is strongest in close proximity to the shoreline and decreases exponentially with distance to shore (McBride and Pfannkuch, 1975). However, isotropic and

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homogenous conditions rarely exist and spatial distribution of groundwater inflow differs strongly from lake to lake (Rosenberry et al., 2015). Experimental studies highlighted a large variety of observed exchange patterns including decreasing seepage with distance from shoreline (McBride and Pfannkuch, 1975; Brock et al., 1982; Cherkauer & Nader, 1989; Kishel & Gerla 2002), increasing seepage with distance from shoreline (Cherkauer and Nader, 1989; Schneider et al., 2005; Vainu et al., 2015), local hotspots of off-shore seepage (Fleckenstein et al., 2009; Ono et al., 2013) and a high small scale variability in near shore zones (Kishel and Gerla, 2002; Blume et al., 2013; Neumann et al., 2013; Sebok et al., 2013). Most often complex hydrogeological settings are the reason for deviations from the theoretical pattern of LGD (Rosenberry et al., 2015). For example, it was found that off-shore LGD was forced by local connections with a deeper aquifer (Fleckenstein et al., 2009; Ono et al., 2013) or forced by a local thinning of low permeable lake sediment (Cherkauer & Nader 1989).

In general, the position of a lake in its regional groundwater flow system determines if a lake receives groundwater, loses water towards the groundwater or both (Born et al., 1974). However, the groundwater flow field is often not well known. Landscape topography can help to determine the groundwater flow field in humid regions and homogenous aquifers, where groundwater tables are likely to follow the topography (Toth, 1963).

Little is known about controls of small scale variability. LGD is driven by the hydraulic gradients between lake and aquifer and controlled by the hydraulic conductivity. So far, there is no clear picture about the role of sediment characteristics in controlling LGD patterns. For example, Kidmose et al. (2013) found that low permeable lacustrine sediments can completely prevent groundwater upwelling, whereas Vainu et al. (2015) observed LGD through low permeable lacustrine sediments. Kishel and Gerla (2002) associated small scale variabilities in LGD with small scale heterogeneities in hydraulic conductivities (Kishel & Gerla, 2002), but in contrast, Schneider et al., (2005) found no correlation between seepage rates and sediment characteristics.

## 1.2 Pattern identification

Although several methods exist to quantify groundwater-lake exchange (Rosenberry et al., 2015), measuring LGD patterns is challenging as we are faced with pronounced spatial variability across the large extent of the aquifer-lake interface. Heat as a natural tracer of groundwater-surface water interaction has received increasing attention in the last decade (Rau 2014). When groundwater and surface water temperatures differ significantly, sediment surface temperature can be used to localize groundwater inflows in lakes (Blume et al.; 2013; Sebok et al., 2013). Using a fibre optic distributed temperature sensing (FO-DTS) system for this purpose has the advantage of providing precise temperature measurements with a high spatial resolution along fibre optic cables up to a length of several kilometres (Selker et al., 2006). Although sediment surface temperatures do not allow a direct estimation of water exchange fluxes, sediment temperature anomalies can be taken as an indicator for groundwater inflows (Blume et al., 2013; Sebok et al., 2013). Another method which uses heat as a tracer and which has been used successfully to investigate exchange patterns between lakes and groundwater are vertical temperature



profiles (VTP) (Blume et al., 2013; Meinikmann et al., 2013; Neumann et al., 2013; Sebok et al., 2013). In contrast to the FO-DTS method, VTP measurements allow the calculation of exchange rates by using the analytical solution of the heat transport equation (Schmidt et al., 2006). Temperature profiles can be measured manually or continuously using profile probes. The measurement of radon activity can also help to identify groundwater inflows (Kluge et al., 2012; Ono et al., 2013; Shaw et al., 2013). Elevated radon activities in surface water indicate groundwater inflow as radon is naturally enriched in groundwater but degasses quickly in surface water.

### 1.3 Objectives

Identifying the processes and structures controlling LGD patterns is the key to reliably predicting them (Grimm 2005). The aim of this study is the characterization of inflow patterns as well as the identification of their controls. The ability to identify patterns and their controls strongly depends on the spatial resolution and the extent of the applied experimental methods. Existing lake studies have investigated LGD patterns with either a high spatial resolution (1–2 m<sup>2</sup>) but a local focus (10 m × 17 m – 25 m × 6 m) (Kishel & Gerla, 2002; Blume et al.; 2013; Sebok et al., 2013) or focused on the entire lake, but used a relatively low spatial resolution (measurements along the shoreline: every 200 m – 3 km) (Schneider et al., 2005; Meinikmann et al., 2013; Shaw et al., 2013). By taking measurements with a high spatial resolution over large parts of the lake we are closing this observational gap.

The study design aimed at answering the following research questions:

- How variable is LGD in space?
- Can we identify patterns?
- Can we link the patterns to external controls?
- Can we predict LGD patterns?

To identify LGD patterns, we measured VTPs in the near shore area and used FO-DTS measurements and radon sampling in the off-shore area. As potential controls of LGD patterns we considered a) heterogeneity of the lake sediment, such as variability in hydraulic conductivity and grain size distributions, b) topographic indices (elevation, slope) as a proxy for the flow field and c) the local groundwater flow field derived from groundwater levels measured in observation wells.

## 25 2. Methods

### 2.1 Study site

Lake Hinnensee is located in northeast Germany in the Müritz National Park. The landscape of the Müritz National Park was shaped by the last glaciation and is dominated by lakes. Lake Hinnensee was formed as a glacio-fluvial tunnel valley and is located within the outwash plain. The terminal moraine is situated north of the lake (Figure 1). Lake Hinnensee has a mean depth of 7 m with a maximum depth of 14 m and is connected to Lake Fürstenseer See in the south. The two lakes together cover an area of 2.68 km<sup>2</sup>. The lake system has no surface water inflow or outflow, apart from a two minor ditches connected



with the Lake Fürstenseer See that only become active at very high lake level. Since 2011, when first LGD measurements were conducted at Lake Hinnensee, the ditches were only active for a period of four month (maximum observed inflow:  $0.0083 \text{ m}^3 \text{ s}^{-1}$ , 22 February 2012, maximum observed outflow:  $0.0030 \text{ m}^3 \text{ s}^{-1}$ , 11 May 2012). The relief of the lake catchment is hilly in the north, with steep slopes down to the lake, and more gentle slopes and lower elevations towards the south (Figure 1). Elevations range between 63 m a.s.l. and 115 m a.s.l.. The lake is surrounded by forest. The mean annual precipitation is 610 mm and the mean annual temperature is  $8.1 \text{ }^\circ\text{C}$  (1901–2005 Neustrelitz, DWD-German Weather Service).

## 2.2 Estimating lacustrine groundwater discharge (LGD)

We applied three different methods to determine LGD patterns: VTPs in the near shore region and FO-DTS and radon in the off shore area.

### 2.2.1 Near-shore LGD derived from vertical temperature profiles (VTPs)

VTPs were used to estimate the spatial variability of LGD rates along the shoreline. Profiles were measured 50 cm away from the shoreline every 10 meters along 2.39 km of the shoreline. The dataset covers 62 % of the total shoreline (Figure 1). The VTPs were measured during five field campaigns in August 2011, June and July 2012, January and July 2013 (Table 1, Figure 1). In July 2013, sediment temperatures were additionally measured in 150 cm distance from the shoreline in order to analyse the trend of LGD with increasing distance to shore. Measurements from August 2011 and January 2013 were conducted only on a 350 m long subsection of the shoreline in the north east of the lake in order to analyse the temporal stability of the observed patterns (Figure 1).

One VTP consisted of six temperature measurements: one at the sediment–water interface and five in the saturated sediment at 5, 10, 20, 30, 40 cm depth. Temperatures were measured with a high precision digital thermometer (Greisinger GMH 3750) and a corresponding thermocouple with an accuracy of  $\pm 0.03 \text{ }^\circ\text{C}$ . The needle had a length of 45 cm and a diameter of 3 mm.

LGD was calculated from the measured VTP using the analytical solution of the 1-D heat flow equation from Bredehoeft and Papaopulos (1965). Assuming a vertical water flux along the temperature profile and steady state temperatures at the sediment–water interface, sediment temperature at a specific depth is calculated as follows:

$$T_{mod}(z) = \frac{\exp\left(\frac{qz \cdot pfcf \cdot z}{kfs} - 1\right)}{\exp\left(\frac{qz \cdot pfcf \cdot L}{kfs} - 1\right)} * (T_L - T_0) + T_0, \quad (1)$$

where  $qz$  is the vertical water flux [ $\text{m s}^{-1}$ ] (positive for groundwater gaining),  $pfcf$  is the volumetric heat capacity of the fluid [ $\text{J m}^{-3} \text{ K}^{-1}$ ],  $z$  is the depth below the upper boundary [m],  $kfs$  is the thermal conductivity of the sediment [ $\text{J s}^{-1} \text{ m}^{-1} \text{ K}^{-1}$ ],  $L$  is



the extent of the exchange zone and the depth of the lower boundary [m],  $T_L$  is the temperature of the lower and  $T_o$  of the upper boundary ( $^{\circ}\text{C}$ ). The values of  $pfcf$  of water and  $kfs$  of lake sediment were taken from Stonestrom and Constantz (2003).  $Pfcf$  of water was set to  $4.19 \times 10^6 \text{ J m}^{-3} \text{ K}^{-1}$  and  $kfs$  to  $2 \text{ J s}^{-1} \text{ m}^{-1} \text{ K}^{-1}$ , a typical value for sandy sediment, which was the dominant grain size in the upper meter of lake sediment.

5 Usually the upper boundary is the sediment-water interface (Schmidt et al. 2006; Blume et al., 2013; Meinikmann et al., 2013). But at locations with shallow water depths in lakes, temperatures in the near surface sediments can be strongly affected by daily temperature variations and thus violate the upper boundary condition of the steady state model. To avoid unreliable LGD calculations due to biased temperatures at the upper boundary, we instead used the temperatures measured at 10 cm sediment depth. A shift of the upper boundary from the sediment-water interface to a depth of 10 cm had a negligible effect on the estimation of the LGD rate assuming steady state conditions. This was validated with theoretical temperature profiles. A shift of the boundary condition to a depth of 10 cm caused a maximal deviation in the estimation of exchange rates of  $1 \text{ L m}^{-2} \text{ d}^{-1}$  and the error decreased with increasing flowrates.

For the lower boundary, we used the shallow groundwater temperature measured in close vicinity of the lake (Figure 1c). For the length of the exchange zone, we tested different values. The quality of LGD estimation increased with increasing L, but was insensitive for values larger than 3 m. Thus, L was set to 3 m.

The exchange rate was optimized by minimizing the root mean square error (RMSE) between measured and calculated sediment temperatures as described in Schmidt et al. (2006):

$$RMSE = \sqrt{\frac{1}{n} \sum (T_{meas(z)} - T_{mod(z)})^2}, \quad (2)$$

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The quality of the fit between measured and modelled sediment temperature was visually checked using plots of the measured and modelled VTPs. Fits with the RMSE greater than or equal to  $0.4 \text{ }^{\circ}\text{C}$  were not used for further analyses as differences between modelled and measured data were considered too large.

Estimated LGD values were analysed for their lateral spatial variability using VTPs measured at a distance of 50 cm from shoreline, for their trend with increasing distance from shore using VTPs measured at 50 cm and 150 cm distance from shore and for their temporal stability using VTPs measured in the different years (Table 1).

Spatial variability of LGD along the shoreline was analysed with autocorrelation plots and autocorrelation values ( $|\rho|$ ) as described in Caruso et al. (2016). High autocorrelation ( $|\rho|$ ) indicate that LGDs for given lag distances are correlated, whereas  $|\rho| < 0.2$ , indicate that LGDs are uncorrelated and strong spatial variability exists. As a second measure, we calculated the median absolute deviation (MAD) of the LGD distribution for different subsections of the lake shore.

In order to analyse the trend in LGD with increasing distance from shore line, we calculated differences between LGD rates measured at 50 cm and 150 cm distance from shore. In order to analyse the temporal stability of spatial patterns we calculated the correlation between the LGD rates measured in different surveys using the Spearman's rank correlation



coefficient ( $\rho$ ). Correlations were regarded as significant for p-values smaller than 0.05. Differences between LGD rates measured in different years were quantified with the RMSE.

### 2.2.2 Identifying hot-spots of off-shore LGD with fibre optic distributed temperatures sensing (FO-DTS)

To identify offshore groundwater inflow patterns, we measured sediment surface temperatures with a 500 m long FO-DTS cable installed permanently along 6 transects through the northern part of the lake (Figure 1c). Two divers ensured good contact of the cable to the lake sediment and also tracked the location of the cable with a differential GPS system (Topcon GR-3) installed on a buoy.

The technology of the FO-DTS is based on the detection of the Raman scattering of a laser pulse through the optical fibre (Ukil et al. 2012). For our measurements, we used a Sensornet Halo device with a sampling resolution of 2 m and a measurement precision of 0.05 °C.

We carried out two measurement campaigns, in February and in August 2014 (Table 2). In February the DTS measurements were taken between 18:49 and 19:17 CEST with a temporal resolution of 2 minutes. We used a single ended set-up with a double ended mode (four channels, two in each direction) and two calibration baths, a warm bath at one end and a cold bath at the other end.

In the second campaign from the 27–28 August 2014 measurements extended over 24 hours, from 18:43 on the 27<sup>th</sup> until 18:45 CEST the next day with a temporal resolution of 2 min. The setup was the same as in February, but additionally both cable ends were run through the cold bath.

The trend and offset in the DTS temperature data were corrected using external temperature loggers in the calibration baths (February: Greisinger GMH 3750 (accuracy:  $\pm 0.03$  °C); August: HOBO TidbiT v2 Water Temperature Data Logger (accuracy:  $\pm 0.21$  °C)).

All four channels showed the same pattern with only small differences in absolute temperature values and further analyses were based on one of the four traces. Sediment temperatures in August were strongly affected by solar radiation. Analysis of 24 hour amplitude or daily minimum temperature did not provide useful information of groundwater inflow patterns as the impact of solar radiation was too strong and spatially irregular. Sebok et al. (2013) recommended using night time data to avoid the uncertainties caused by solar radiation. However, at night shallow near shore water cooled down and it was not easy to distinguish if temperature shifts resulted from groundwater inflow or resulted from a decrease of water temperature due to decreasing air temperature. We thus chose a time window in which the temperature at the near shore shallow region and in the deeper region of the lake were very similar and groundwater inflow induced temperature shifts were easy to identify. This time window was from 18:43 to 19:11 CEST on the 27<sup>th</sup>.

Temperature depth profiles of the lake were available with 1 m spatial resolution (HOBO Water Temperature Pro v2 Data Logger, accuracy:  $\pm 0.21$  °C). In winter we had only one profile in the central part of the lake, but in August a second profile further north was available (Figure 1a, b). The groundwater temperature was measured in a piezometer (OTT Orpheus Mini, accuracy:  $\pm 0.5$  °C) close to the lake (Figure 1c) and air temperature data were available from a weather station 1.5 km away



and in August an additional air temperature data logger (of the same type as used for the water profiles) was installed directly at the lake.

During the August campaign, we additionally measured VTPs along the cable, at five measurement locations at the eastern shore and four measurement locations at the western shore.

### 5 2.2.3 Radon as indication for offshore-LGD

Radon ( $^{222}\text{Rn}$ ) is produced within the natural decay chain of uranium and has a half-life of 3.82 days. Radon occurs naturally in the aquifer matrix and as it is soluble, groundwater is enriched in radon as it passes through the aquifer matrix. However, once radon-enriched groundwater is in contact with air, radon degasses quickly. Consequently, radon activities in surface water are low. Due to the pronounced differences between groundwater and surface water concentrations, elevated radon concentrations can be used as an indicator for groundwater inflows as shown for example by Kluge et al. (2012), Ono et al. (2013) and Shaw et al. (2013). In this study, we used radon as a qualitative indicator of presence or absence of off-shore LGD. We took water samples of 1.5 L or 1.75 L from the bottom of the lake (lower end of the water column) at 19 locations (Figure 1) during three campaigns (5 June 2013, 17 September 2013 and 21 August 2014). Water samples taken at the third date (Figure 1c) were taken by divers. All other samples were taken from a boat using a peristaltic pump. Contact between water samples and air was minimized and bottles were filled without air bubbles. To test the ability of radon concentrations to identify groundwater inflow at Lake Hinnensee, we took water samples from two near-shore VTP locations where LGD rates were known and significantly different, one with strong inflow ( $153 \text{ L m}^{-2} \text{ d}^{-1}$ , located 40 m south from northern tip at the eastern shore) and one with medium inflow ( $48 \text{ L m}^{-2} \text{ d}^{-1}$ , located 60 m south from northern tip at the eastern shore). In order to estimate the radon activity of the groundwater a groundwater sample was taken in a nearby piezometer (Figure 1c). The water samples were analysed using the alpha spectrometer RAD7 (DurrIDGE Company Inc., Bedford, MA, USA) with the big bottle rad  $\text{H}_2\text{O}$  extension. Analysing time of the RAD7 was extended to 3.5 hours or longer to reduce measurement uncertainties. To remove background concentration of radon in the measurement device, the device was purged for 3.5 at least hours with fresh air between water samples. Relative humidity was kept below 8 % during measurements. Most of the samples were analysed in the first days directly after sampling. Maximum delay between sampling and analysis was one week. The data were decay corrected in dependence of the time between sampling and analysis.

### 2.3 Identifying controls of LGD patterns

In order to identify the controls of the observed LGD patterns, we characterized both the near-and the far-field conditions and correlated these characteristics with LGD rates using Spearman's rank correlation coefficient. At the local scale (near-field conditions) this includes sediment characteristics, while at the larger scale (far-field conditions) we considered topographic indices and the groundwater flow field as the most likely controls.





### 2.3.1 Sediment heterogeneity as a small scale control on LGD patterns

Hydraulic conductivity from slug tests

At 37 VTP positions (Figure 1b), slug tests were performed to estimate hydraulic conductivity ( $k_{sat}$ ) of the near-surface sediment. Slugtests were carried out in piezometers with an inner diameter of 36.4 mm. The filter placed on the lower end of the piezometer had a length of 10 cm and consisted of 4 mm diameter perforations in the PVC tube wrapped with fine mesh. The midpoint of the filter was 50 cm below the sediment surface. To minimize interference with the temperature profile measurements, the piezometers were installed at 50 cm distance. For the rising-head tests water was quickly removed out of the piezometer using a peristaltic pump. Recovery of the water table was measured with automatic pressure logger (HOBO 13-Foot Fresh Water Level Data Logger, accuracy:  $\pm 0.3$  cm) with a temporal resolution of 1 second. Recovery data were then analysed using the approach of Hvorslev (1951):

$$k_{sat} = \frac{\pi r^2}{T_0 c}, \quad (3)$$

where  $r$  is the radius of the piezometer,  $T_0$  the time needed to recover 37 % of initial water level and  $c$  a shape factor. The shape factor depends on the ratio of screen length and radius. The piezometer had a screen length radius ratio of 5.5 and thus we used a shape factor introduced by Chapuis (1989), valid for wells with ratio smaller than 8:

$$c = 4\pi r \sqrt{\frac{L}{2r} + \frac{1}{4}}, \quad (4)$$

where  $L$  is the length of the screen.

Grain size distributions from sediment cores

Sediment cores were taken from 30 selected slug test positions (Figure 1b). Sediment cores were taken with a transparent tube with an inner diameter of 32 mm. Length of cores varied between 42 cm and 145cm, with the majority of core lengths between 80 cm and 128 cm. Each core was split into samples according to their sediment profile. The samples were oven-dried at a temperature of 105 °C and sieved with a vibratory sieve shaker (Retsch AS 200). The sieving setup included the following mesh sizes: 0.063, 0.125, 0.2, 0.3, 0.5, 0.63, 2, 5, 10 mm. Grainsizes smaller than 0.063 mm were classified as silt, grainsizes larger than 0.063 mm but smaller than 0.2 mm as fine sand, larger than 0.2 mm but smaller than 0.63 mm as medium sand, larger than 0.63 mm but smaller than 2 mm as coarse sand larger than 2 mm as gravel.

For the correlation analyses between sediment characteristics and LGD, we used only samples taken from the upper 100 cm of the lake sediment. The means of each grainsize fraction was calculated for each sampling location from all single samples of the upper 100 cm in which the core was split. Additional to the correlation analyses, simple and multiple linear regression models were calculated between LGD and each grainsizes fraction. For the calculation of the multiple linear regression models, correlations between explanatory variables were checked before and variables were regarded to be independent from





each other if  $\rho$  was below 0.7. Models were regarded as significant if p-values were below 0.05. The goodness of the models were determined with the coefficient of determination ( $R^2$ ).

### 2.3.2 Topographic indices as controls on large scale LGD patterns

In order to analyse the effect of far field conditions on LGD patterns the following topographic indices were calculated using SAGA GIS: average elevation, average slope and the percentage of area with low topographic gradient in direct vicinity to the lake shore. To determine the topographic indices we used a digital elevation model (DEM) of the area with a resolution of 1 m. The topographic indices were estimated for representative areas, i.e. upslope areas for shoreline sections of 100 m length. Therefore the shoreline was split into 46 subsections of 100 m length with an overlap of 50 m. As upslope areas can only be determined for points, not for lines, we calculated upslope areas every meter along the shoreline and aggregated them to one upslope area for each subsection. The upslope areas were determined using the multiple flow direction approach. To investigate the topographical zone of influence ( $z_i$ ), four different extents of the upslope areas were considered: maximum extent of 25, 50, 100 and 200 m distance from shoreline. These zones of influence were further called:  $z_{i25m}$ ,  $z_{i50m}$ ,  $z_{i100m}$ ,  $z_{i200m}$ . The indices slope and elevation were averaged over each upslope area (arithmetic mean). The percentage of area with low topographic gradient was here defined as the percentage of the upslope area not to be higher than 50 cm above lake level in direct vicinity to the lake shore. This threshold was chosen as this was the area flooded at maximum lake levels known within the last 25 years. Indices were correlated with median LGD rates for the 100 m long subsections derived from VTPs. Each subsection included 10 VTP measurement locations. Furthermore simple and multiple linear regression models were calculated between LGDs and topographic indices derived for  $z_{i25m}$  and  $z_{i50m}$ , as in these zones correlation between LGD and far-field conditions were strongest. Correlations between explanatory variables were checked and regarded as independent from each other if  $\rho$  was below 0.7. Predictors were regarded as significant if p-values were below 0.05. The goodness of the model fits were determined with the  $R^2$ .

### 2.3.3 Groundwater flow field as control on large scale LGD patterns

The groundwater flow field was the second far-field variable assumed to affect the LGD patterns. In order to derive the groundwater flow field, measured groundwater heads from 17 observation wells located around Lake Hinnensee (Figure 1a) were spatially interpolated. 12 of the 17 bore wells were drilled in 2012, five of them in 2014. Groundwater levels were measured regularly since 2012 using an electric contact meter (SEBA Hydrometrie, electric contact meter type KLL, accuracy:  $\pm 1$  cm). To determine the groundwater flow field we used groundwater levels measured in 2014, when all wells were completed. In 2014 groundwater levels were generally lower than during the VTP measurement campaigns (2011-2013), but the spatial patterns of groundwater heads of the 12 wells already installed in 2012 remained stable. Measured groundwater levels from March 2014 had the smallest differences (mean difference 5.55 cm) to available groundwater data around the time of the VTP measurement campaigns and were chosen to derive the groundwater flow field around Lake Hinnensee. For the interpolation of the groundwater measurements, we used both ordinary kriging and regression kriging. In



regression kriging a linear regression between an external variable and a depending variable is included. This allowed us to incorporate the effect of topography on the groundwater flow field. In order to minimize the effect of small scale heterogeneities in the topography the DEM was smoothed by reducing the resolution from 1 m to 10 m and rescaled to a resolution of 1 m that results of the regression kriging still had a resolution of 1m. The groundwater gradients were calculated from the interpolated groundwater surface.

To analyse the correlation of the groundwater flow field with the LGD patterns, we averaged groundwater gradients in each subcatchments for each zone of influence (arithmetic mean) and correlated these with the median LGD rates of the subsections as described in 2.3.2. Additional to the correlation analyses, simple linear regression models were calculated between LGD and groundwater gradients. Furthermore groundwater gradients were included in multiple linear regression models calculated with topographic indices.

All analyses were carried out in the statistic software R (R Development Core Team, 2011). For the geographical analyses we used the geographical information system SAGA GIS, for some analyses applied within the R environment using the package “rsaga” (Brenning, 2008).

## 3. Results

### 3.1 Estimating lacustrine groundwater discharge (LGD)

#### 3.1.1 LGD estimations from vertical temperature profiles (VTP)

In total 520 VTPs were measured along the shoreline at Lake Hinnensee to analyse spatial patterns of near shore LGD, analyse the trend of LGD with increasing distance from shore and to analyse the temporal stability of LGD patterns. At 21 locations temperature measurements were not possible as the locations were either inaccessible or sediment was unsuitable for measuring, for example due to high stone content or a thick muddy organic material. 22 profiles (4 %) were excluded from the analyses as no satisfying fit to the heat transport equation could be achieved. The quality of all remaining LGD estimations was satisfying (mean(RMSE) = 0.09 °C, median(RMSE) = 0.06 °C, interquartile range (IQR) (RMSE) = 0.12 °C, n = 498).

#### Spatial patterns along the shore line

LGD rates determined from VTPs every 10 m along 2.39 km of the shoreline ranged from -12 L m<sup>-2</sup> d<sup>-1</sup> (lake water losses) to 169 L m<sup>-2</sup> d<sup>-1</sup> (groundwater gaining) with a median of 44 L m<sup>-2</sup> d<sup>-1</sup>. The interquartile range (IQR) was 26 L m<sup>-2</sup> d<sup>-1</sup>. Occurrence of very strong LGD rates of more than 94 L m<sup>-2</sup> d<sup>-1</sup> (positive outliers of LGD distribution), was limited to the northern most 140 m on both the western and the eastern shore of the lake (between “a” and “b” and “f” and “g” in Figure 2) and to one single spot at the western shore 470 m to the south (“i” in Figure 1&2). The northern most 140 m on both the west



and the east shore (between “a” and “b” and “f” and “g” in Figure 1&2) are in the following called “the northern part” and the adjacent region in the south (between “b” and “e” and “g” and “j” in Figure 1&2) will be called “the southern part”. Negative rates were only observed at the eastern shore, between 480 m and 530 m from the northern tip (“c” in Figure 1&2). In the northern part of the lake, LGD was stronger and spatially more variable (median =  $74 \text{ L m}^{-2} \text{ d}^{-1}$ ,  $|\rho|_{10 \text{ m}} = -0.04$ , MAD =  $21 \text{ L m}^{-2} \text{ d}^{-1}$ ) than in the southern part (median =  $41 \text{ L m}^{-2} \text{ d}^{-1}$ ,  $|\rho|_{10 \text{ m}} = 0.62$ , MAD =  $12 \text{ L m}^{-2} \text{ d}^{-1}$ ) (Figure 2, Figure 3). In the northern part LGD was statistically uncorrelated for all lag distances (Figure 3), while in the southern part it was auto correlated up to a lag distance of 50 m with  $|\rho|$  ranging between 0.62 and 0.23 (Figure 3). Autocorrelation in the southern part was stronger on the eastern than on the western shore (Figure 3).

#### 10 Spatial patterns perpendicular to the shore line

Between 660 m and 1520 m along the eastern shore and 300 m and 830 m south of the northern tip along the western shore, VTPs were measured at 50 cm and 150 cm distance from shoreline to analyse the trend of LGD with increasing distance from shore.

In more than two thirds of all cases (71 %), LGD measured at 150 cm from the shoreline was lower than the rate measured at 50 cm distance (Figure 2). The reduction of LGD rate was on average 20 % (median). However, in 29 % of all cases, LGD increased with distance to the shore (Figure 2) with an average increase of 15 % (median). The pattern of LGD along the shore line measured 50 cm and 150 cm apart from shore were very similar ( $\rho = 0.81$  (p-value  $< 2 \times 10^{-16}$ ), Figure 2).

#### Temporal stability of spatial patterns

20 The annual repetitions of LGD rates measured at 43 VTP positions (Figure 1) highlight that the observed LGD patterns were correlated between the individual measurement campaigns (Figure 4). Correlation coefficient was 0.71 (p-value =  $5 \times 10^{-6}$ ) between summer 2011 and 2012 (n = 34), 0.82 (p-value =  $10^{-3}$ ) between 2012 and summer 2013 (n = 13) 0.70 (p-value  $< 4 \times 10^{-6}$ ) between 2012 and winter 2013 (n = 34) and 0.66 (p-value  $< 3 \times 10^{-5}$ ) between 2011 with winter 2013 (n = 33). The RMSE between LGD rates measured in different years was lowest comparing rates from summer 2011 and summer 2012 ( $23 \text{ L m}^{-2} \text{ d}^{-1}$ ) and strongest comparing rates from summer 2011 and winter 2013 ( $51 \text{ L m}^{-2} \text{ d}^{-1}$ ).

### 3.2 Identification of offshore LGD

#### 3.2.1 Lake sediment temperature anomalies as indicators for LGD based on fibre optic distributed temperature sensing (FO-DTS)

We measured lake sediment temperature with a FO-DTS cable installed in 6 transects through the northern part of the lake (Figure 1c) during two measurement campaigns (20.02.2014, 27.08.2014) to identify offshore groundwater inflow.

The winter and summer measurements consisted of 15 measurements in 2 minute intervals. The repetitions resulted in very similar measurements (median range of temperature differences among repetitions in winter:  $0.19 \text{ }^\circ\text{C}$ ; maximum range in



winter: 0.44 °C, median range in summer: 0.22 °C; maximum range in summer: 0.38 °C) (Figure 5a). In winter sediment temperature ranged between 3.4 °C and 5.3 °C and in summer between 17.0 °C and 18.4 °C (Figure 5). In summer, groundwater was 7 °C cooler than lake water and in winter 3 °C warmer than the lake. The air temperature, groundwater temperatures and temperature depth profiles of the lake measured during the DTS measurements are presented in Table 2.

- 5 The spatial patterns of sediment temperature anomalies, i.e. the shifts of sediment temperatures towards groundwater temperatures, were similar in both campaigns. Strongest deviations from sediment temperatures towards the groundwater temperatures (positive in winter and negative in summer) were located near the shoreline at corners two and three (Figure 5). A slight shift towards groundwater temperatures was also observed near corner 5, but only along the DTS cable north of the corner. These hot and cold spots in winter and summer respectively were not located nearest to the shoreline, but between 2
- 10 m and 14 m offshore, where lake depth steeply increased (Figure 5b).

LGD rates estimated from VTPs measured along the fibre optic cable ranged between 109 L m<sup>-2</sup> d<sup>-1</sup> and 238 L m<sup>-2</sup> d<sup>-1</sup> at corner two and between 60 L m<sup>-2</sup> d<sup>-1</sup> and 169 L m<sup>-2</sup> d<sup>-1</sup> at corner three, which correlated with the intensities of the sediment temperature anomalies at these locations (Figure 6).

### 3.2.2 Identification of offshore LGD based on radon concentrations

- 15 To test the capability of radon as a tracer of groundwater inflow at Lake Hinnensee, we took two samples at VTP measurement locations where LGD rates were known to be significantly different. The radon activity at the sampling location with stronger LGD was significantly higher (787 Bq m<sup>-3</sup>) than the radon activity in the other sample (90 Bq m<sup>-3</sup>). The groundwater had a radon activity of 12151 Bq m<sup>-3</sup>. Radon activities in lake water samples ranged between 0 and 103 Bq m<sup>-3</sup>, with a median of 41 Bq m<sup>-3</sup> and an IQR of 30 Bq m<sup>-3</sup>. Radon activities in the uppermost quartile, (> 54 Bq m<sup>-3</sup>) were
- 20 measured in the northern part of the lake and at one sampling point in the central part of the lake 100 m east of the southern temperature logger chain. The three southernmost points had lowest radon activities (0 – 22 Bq m<sup>-3</sup>).

## 3.3 Controls of LGD patterns

### 3.3.1 Sediment heterogeneity as a small scale control

Hydraulic conductivity

- 25 The  $k_{\text{sat}}$  values estimated from the slugtests ranged between  $2.03 \times 10^{-6} \text{ m s}^{-1}$  and  $4.25 \times 10^{-5} \text{ m s}^{-1}$  with an IQR of  $1.41 \times 10^{-5} \text{ m s}^{-1}$  (Figure 7). Points with  $k_{\text{sat}}$  values lower than the 25 % quartile ( $9.20 \times 10^{-6} \text{ m s}^{-1}$ ) were mainly located at the western shoreline, while points with values higher than the 75 % quartile ( $2.33 \times 10^{-5} \text{ m s}^{-1}$ ) were located on the eastern shore. Instead of a positive correlation between  $k_{\text{sat}}$  values and LGD rates, there was a slight negative, but spastically insignificant (p-value = 0.05), correlation of -0.36 (Figure 7).

30

Grain size distributions



The sediment samples taken from 30 VTP measurement locations were dominated by sand with a small fraction of gravel and silt. The median percentages of sand, gravel and silt were 92.3 %, 6.8 % and 0.6 %, respectively. Within the sand fraction, medium sand dominated (median = 59.2 %), followed by fine sand (median = 23.3 %) and coarse sand (median = 13.7 %). No consistent layering or trends of grain sizes with depth could be identified. Only the fraction of medium sand  
5 decreased slightly with increasing sampling depth with 2 % every 10 cm, but also here the correlation was weak ( $\rho = 0.3$ ,  $p$ -value =  $6 \times 10^{-4}$ ). Along-shore textural patterns were more pronounced with the highest percentage of gravel at the western shore of the northern part. Here the percentage of gravel ranged between 20 % and 80 %, at all remaining locations percentage of gravel was below 10 %. The percentage of coarse sand was highest, between 15 % and 28 %, in samples from the northern part of the lake, but was below 10 % at the sampling locations from the southern part. Fine sand, in contrast,  
10 dominated the grainsize distribution in the south.

Relating grainsize distributions, averaged over the upper meter of the lake sediment, to the strength of LGD showed that low LGD rates occurred at locations dominated by fine sand and stronger LGD rates occurred at locations with higher fraction of larger grainsizes (Figure 8a). LGD was positively correlated with the percentage of gravel and coarse sand, but negatively correlated with the percentage of fine sand (Table 3, Figure 8 b-c), but LGD rates were uncorrelated with the grainsize  
15 fractions medium sand and silt (Table 3). The linear regression models describing these correlations can be found in Table 3. One multiple regression model considering all grainsizes was calculated. Only coarse sand and fine sand were significant variables ( $p$ -values  $< 0.05$ ). The model had a  $R^2$  of 0.54 (Table 3). The absolute residuals were on average  $21 \text{ L m}^{-2} \text{ d}^{-1}$ , with largest positive residuals (observed  $<$  calculated) at a distance of 50 m and 10 m from the northern tip at the eastern and western shore, respectively and largest positive residuals (observed  $>$  calculated) at a distance of 70 m and 90 m from the  
20 northern tip at the eastern shore (Figure 9a).

### 3.3.2 Large scale controls on LGD patterns

#### Topographic indices

Subcatchments derived from the 46 shoreline sections differed significantly in size. While subcatchments in the flatter areas of the south were larger, elevations were higher and slopes generally steeper in the north. There was no clear correlation  
25 between LGD rates and the size of the subcatchment in each topographical zones of influence (Table 4). Percentages of area with low topographic gradient in direct vicinity to the lake shore area were also not correlated with LGD rates, except for  $z_{i25m}$ , where a weak negative correlation was found (Table 4). The correlation between LGD rates and the indices elevation and slope were both positive (Table 4, Figure 10 right) and the strength of correlation was strongest considering a  $z_{i50m}$  and decreased with increasing zone of influence (Table 4).

30

#### Groundwater flow field

The interpolated groundwater table showed groundwater flow towards Lake Hinnensee from all directions (Figure 10). In general, groundwater gradients were stronger in the north than in the south. Differences between the ordinary and regression



kriging were strongest where the topography is most pronounced. The linear predictor function used for the regression kriging was  $gw = 62.5 + 0.02e$  where  $gw$  is the groundwater level in meter and  $e$  the smoothed surface elevation in meter. The topography was a significant model predictor with a p-value of  $10^{-5}$ .

The maximum deviation between interpolated and measured groundwater levels was below 1 cm for both interpolations, but in comparison to the ordinary kriging, the regression kriging resulted in significantly stronger gradients: median groundwater gradient in the  $z_{i200m}$ , for example, was  $0.24 \text{ cm m}^{-1}$  using regression kriging and  $0.09 \text{ cm m}^{-1}$  using ordinary kriging.

While the correlation between LGD and groundwater gradients derived from ordinary kriging was weak with correlation coefficients ranging between 0.28 and 0.37 (Table 2), stronger correlation was found for LGD and gradients derived from regression kriging (between 0.55 and 0.64) (Table 2).

10

Linear regression models between LGD and far-field predictors

The linear regression models describing the correlation between LGD and far-field conditions were estimated for all predictors of  $z_{i25m}$  and  $z_{i50m}$ . Significant predictors of LGD large scale patterns were elevation, slope, percentage of area with low topographic gradient, but only in  $z_{i25m}$  and groundwater gradients (Table 5). No significant linear regression model was found with the potential predictors size of subcatchment and percentage of area with low topographic gradient in  $z_{i50m}$ . The  $R^2$  of all models were not larger than 0.37 (Table 5), but for the predictors percentage of area with low topographic gradient and groundwater gradients derived from ordinary kriging below 0.12 (Table 5) and therefore not regarded for further analyses.

The calculation of multiple regression models revealed no significant relations between LDG and topographic indices in both zones of influence. Reducing stepwise the most insignificant predictor until all predictors became significant resulted in the single linear regression models as presented above and in Table 5.

Calculated large scale LGD patterns along the shoreline using the best linear regression model we found (considers groundwater gradients derived from regression kriging in  $z_{i25m}$ , Table 5), are shown in Figure 9b. The general spatial pattern was captured by the model, but absolute deviations were on average  $10.4 \text{ L m}^{-2} \text{ d}^{-1}$ . Strongest overestimations occurred at the distances 500 m at the eastern and 300 m at the western shore and strongest underestimation by the model were found at the distances 450 m and 150 m at the western shore.

## 4. Discussion

### 4.1 LGD patterns along the shoreline and potential controls

The here employed experimental design based on extensive field campaigns provided exceptionally detailed information on both small scale variabilities and large scale patterns of LGD rates along a lake shore line. This data set thus bridges the gap between the detailed local and low resolution regional investigations of previous LGD studies.



#### 4.1.1 Large scale patterns

The observed large scale patterns of LGD at Lake Hinnensee could only partially be explained by predictors derived from topography or the groundwater flow field. However, correlation between LGD and surface elevation, slope or groundwater gradients derived from regression kriging indicate a linkage between topography, groundwater movement and patterns of LGD. A similar link had previously been observed in groundwater river interactions (Caruso 2016). As correlation was stronger between LGD and groundwater gradients derived from regression kriging than between LGD and groundwater gradients derived from ordinary kriging, we assume that the groundwater surface was more realistically interpolated using regression kriging. This indicates again a link between topography and groundwater movement, which is in consistent with the theory of topography–controlled groundwater flow introduced by Toth (1963).

In contrast to observations of streamflow generation in mountain catchments (Jencso et al., 2009, 2010), no positive correlation was found between the size of the subcatchment and LGD rates (Table 4) indicating that surface catchments derived for lake subsections were not a good estimator for the amount of subsurface water flowing into the corresponding lake sections. We assume our result indicates that subsurface catchments differ from surface catchments which is not unusual in low land areas. The weak negative correlation between LGD and the topographic index percentage of area with low topographic gradient in direct vicinity to the lake shore in  $z_{i25m}$  indicated that low topographic gradients at the shoreline could buffer groundwater flow towards the lake.

Even though the interpolated groundwater surface showed groundwater flow towards Lake Hinnensee from all directions (Figure 10), we measured negative LGD rates at one small subsection of the lake (Figure 2). Reasons for this flow reversal are unclear, however, a local inversion in the groundwater – lake gradients might be the result of a near shore depression in groundwater levels caused by transpiration (Winter et al., 1998).

#### 4.1.2 Small scale patterns

Our measurements revealed strong small scale spatial variability in LGD along the shoreline (Figure 2). Absolute amounts and spatial variability of LGD were within the range of previous studies (Rosenberry et al., 2015; Blume et al.; 2013; Neumann et al., 2013). Measuring VTPs with a high measurement resolution along large parts of the shoreline highlighted furthermore that the strength of small scale variability also varies along the shoreline. This type of information is likely to be overlooked in studies focusing either on entire lake systems but using a low spatial resolution (Schneider et al., 2005; Meinikmann et al., 2013; Shaw et al., 2013) or using a high spatial resolution but only on a very local scale (Kishel & Gerla, 2002; Blume et al.; 2013; Sebok et al., 2013). The repetitions of VTP measurements revealed that the observed patterns were stable in time and are thus likely controlled by static characteristics. Differences in LGD rates measured in different years might result from climate driven processes.

Surprisingly no positive correlation was found between LGD rates and  $ksat$  values derived from slugtest at Lake Hinnensee. The relationship between  $ksat$  and LGD could be confounded as a result of strong differences in hydraulic gradients.





However, even when only adjacent measurement locations with similar gradients were taken into account no clear positive correlations appeared (Figure 7). Slug test were found to be the most accurate method to determine  $k_{sat}$  values of sandy stream beds (Landon et al., 2001), but estimation of hydraulic conductivity is always characterised by high uncertainties (Landon et al., 2001; Kalbus et al., 2006). Even though the slug tests were carried out carefully, we cannot exclude that pore structure, was altered during the piezometer installation and thus the  $k_{sat}$  values of lake sediments were changed. In contrast to  $k_{sat}$  values, LGD rates clearly correlated with both the finest and the coarsest grain size fractions. Grain sizes give no direct information of the hydraulic conductivity, but coarse sand and gravel is associated with higher hydraulic conductivity values than well sorted fine sand (Bear, 1972). As LGD rates correlated positively with percentages of gravel and coarse sand and negatively with the percentage of fine sand, this corroborates the assumption that sediment heterogeneities do at least partially control small scale variability in LGD.

#### 4.2 LGD patterns with increasing distance to shore and its potential controls

To identify LGD patterns with increasing distance to shore, we analysed VTP profiles measured in 50 cm and 150 cm distance from the shoreline in the southern part. Results showed a prevailing decrease of LGD with distance to shore. This observation corresponds to the theoretical pattern of LGD found by McBride and Pfannkuch (1975) and other experimental studies (Brock et al., 1982; Cherkauer & Nader 1989, Kishel & Gerla 2002; Blume et al.; 2013). The study from Blume et al. (2013), conducted in the northern part of Lake Hinnensee, indicated that the strongest decrease of LGD occurred in the first 1.5 m distance from shore. However, in 29 % of the locations, LGD increased with increasing distance from shore. The locations with anomalously increasing LGDs did not show any obvious anomalies with respect to local bathymetry, density of vegetation or organic top layers, which could have been used to explain the observed patterns. The hypothesis that differences in sediment characteristics cause these anomalies could unfortunately not be tested as no information on sediment characteristics is available for distances from shore larger than 50cm.

#### 4.3 Offshore LGD patterns and potential controls

We investigated the presence and absence of offshore LGD with two methods: radon and heat (sediment temperature measurements with FO-DTS) as natural tracers. Measured radon activities of lake samples indicate groundwater inflow, but activities were low. Sampling locations were mainly located in the epilimnion, where lake levels were too shallow to allow for a thermocline. In the epilimnion, the lake water is assumed to be well mixed (Kluge et al., 2012). Therefore it is possible that the homogeneous and very low radon activity in the deeper parts of the lake result from groundwater inflow from the near shore area instead from the deep sampling locations itself. As also FO-DTS showed no shifts in sediment temperatures towards the groundwater temperature in the flatter and deeper parts of the lake (Figure 5b), we assume that groundwater inflow is insignificant here. Insignificant groundwater inflow in the flatter and deeper part of the lake is in correspondence with the theory of exponentially decreasing groundwater inflow with distance from the shore introduced by McBride & Pfannkuch (1975). Furthermore we know from observations by divers that the lake bottom was covered with fine-grained



organic sediments, which typically accumulates in the deep, flat parts, where wave action cannot re-suspend the fine sediments (Rosenberry et al., 2015). A layer of fine-grained sediment could significantly decrease hydraulic conductivity of the lake bed sediment and can even totally prevent groundwater lake exchange (Kidmose et al., 2013).

The radon activity of the sample taken few meters apart from the shoreline close to corner 3 (Figure 5b) had the strongest  
5 radon activity of the lake water samples, and also FO-DTS measurement showed a clear groundwater signal at this location. FO-DTS showed local hotspots of groundwater inflow at three locations, all on steep steps between the near shore part and the flatter central basin. We only had detailed information of sediment temperatures at the steep steps close to corner 1, 2, 3 and 5. At the other corners fallen trees made it impossible to lay out the FO-DTS cable closer to the shoreline. However, locations with sediment temperature anomalies coincided with high near shore LGD rates (estimated with VTPs), while  
10 corners where no temperature anomalies were found, coincided with low near shore LGD rates (Figure 5b). As hotspots in near shore LGD occurred locally and mainly in the northern part of the lake, we assume that the occurrence of hotspots of LGD at steep steps is also a local phenomenon limited to the northern part. As the occurrence of the local sediment temperature anomalies is temporally stable (Figure 5a), we assume that static characteristics are responsible – at this  
15 locations, where near shore LGD was already strong, the morphology of steep steps might force a local offshore increase of LGD again: at steep slopes fine sediment is prone to be re-disturbed by turbidity current activities (Håkanson, 1977), locally increasing hydraulic conductivity and thus also LGD.

#### 4.4 Prediction of LGD patterns

Using linear regression models based on topographic characteristics or the groundwater flow field to predict large scale patterns of LGD at Lake Hinnensee roughly reproduced the observed patterns, but locally strongly over- or underestimated  
20 the observed LGD rates (Figure 9b). However, regression models considering sediment heterogeneities were able to explain more than 50 % of the observed small scale variability in LGD ( $R^2 = 0.55$ ). We calculated linear regression models separately for topographic indices and sediment heterogeneities, because sediment cores were only taken from a fraction of the lake covering not more than one lake subsection used for far field analysis. But as LGD is driven by both, the hydraulic gradients between lake and aquifer and by the hydraulic conductivity, combining the information would likely explain more  
25 of the observed variability. Another possible explanatory variable is heterogeneity within the adjoining aquifer (Winter 1999; Cherkauer & Nader, 1989; Fleckenstein et al., 2009). Based on the analysis of cores from the bore holes of the observation wells and also on geophysical measurements around Lake Hinnensee, the presence of till lenses in the aquifer seems likely (H. Wilke, pers. comm. 2016). Small scale structures, such as these may influence the groundwater flow paths and cause variability in LGD.



## 5. Conclusion

While LGD is known to be strongly spatial variable across the entire aquifer-lake interface it is also not easily measured, especially not with an extent and spatial resolution that allows for the characterisation of LGD patterns. Furthermore, structures controlling these patterns are not well understood. Our aim was the characterization of LGD patterns at Lake Hinnensee based on intensive experimental investigations. As experimental investigations of this calibre are rarely feasible, we furthermore wanted to identify the controls behind these patterns, in the hope of pattern predictability via external (and easily measurable) controls. By using VTPs in the near shore area and FO-DTS measurements and radon sampling in the off-shore area, we identified the following pattern in LGD for Lake Hinnensee: LGD was concentrated in the near shore area and generally decreased with distance to shore; some local hotspots of LGD were identified in locations of steep steps towards the lake bottom; overall, LGD was insignificant in the central part of the lake. LGD was generally stronger and more variable in the northern part than in the southern part of the lake. Repetitions of LGD measurements indicated that the observed patterns in LGD remained stable in time. We identified the following links between LGD patterns and external factors at Lake Hinnensee: Large scale LGD patterns at Lake Hinnensee were linked to the local topographic gradient and also groundwater gradients derived from regression kriging. The explanatory power of these indices was strongest when derived locally up to a distance of 50 m from shoreline, but decreased with increasing distance. Small scale LGD patterns in the north were linked to sediment heterogeneities: LGD patterns correlated positively with percentages of gravel and coarse sand and negatively with the percentage of fine sand. However, LGD patterns did not correlate with  $k_{\text{sat}}$  values derived from slug tests.

Our results furthermore showed that predictions of LGD rates using regression models derived from correlation of external controls and LGD were associated with high uncertainties, but nevertheless allowed a rough estimation of LGD patterns. Topographic indices, such as elevation or slope, are often readily available. Analysing grainsize distributions of lake sediment is labour intensive, but sediment cores taken with transparent cores can be easily analysed at least qualitatively. This information combined with information of topographic gradients can then be used to develop an effective and efficient measurement design for more a detailed characterisation of spatial patterns of LGD that goes beyond the rough estimate that the linear regression models can provide.

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**Table 1: Dates, information and use of vertical temperature profile surveys.**

<i>Date</i>	<i>Groundwater temperature [°C]</i>	<i>Lake water temperature [°C]</i>	<i>Data analysis</i>
24–25 August 2011	10.7	22.7	Temporal stability of LGD patterns
12–14 June 2012	8.9	18.2	Spatial patterns of LGD along the shoreline
16–17 July 2012	10.1	20.1	Spatial patterns of LGD along the shoreline
21–23 January 2013	7.0	0.0	Spatial patterns of LGD along the shoreline
17–25 July 2013	10.1-10.3	23.2	Spatial patterns of LGD along the shoreline and LGD patterns with increasing distance from shore

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**Table 2: Groundwater temperatures and lake water temperatures depth profile measured during FO-DTS campaigns. \*<sup>1</sup> measured at the nearby weather station, \*<sup>2</sup> measured close to the lake**

<i>Date</i>	<i>Air temperature [°C]</i>	<i>Groundwater temperature [°C]</i>	<i>Temperature depth profile [°C]</i>
20 February 2014	6.8* <sup>1</sup>	6.3	0m: 1.8 -1m: 3.4 -2m: 3.4 -3m: 3.4 -4m: 3.4 -5m: 3.4
27 August 2014	19.4* <sup>1</sup> 16.1* <sup>2</sup>	11.6	0m: 18.9 -1m: 18.7 -2m: 18.7 -3m: 18.5 -4m: 18.4 -5m: 18.4

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**Table 3: Correlation coefficients ( $\rho$ ), linear models describing the correlation between LGD and predictors and the coefficient of determination ( $R^2$ ).  $\rho$  coloured in black indicate significant correlation ( $p$ -value  $< 0.05$ ), light red indicate insignificant correlations ( $p$ -value  $> 0.05$ )**

Predictor (x)	$\rho$	Models (LGD = ...)	$R^2$
gravel	0.61	$49.84 + 1.78x$	0.25
coarse sand	0.62	$14.03 + 5.27x$	0.46
medium sand	0.01	-	-
fine sand	-0.7	$127 - 2.12x$	0.48
Silt	0.01	-	-
Coarse + fine sand		$72.72 + 3.06x_1 - 1.35x_2$	0.54

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**Table 4: Correlation coefficients ( $\rho$ ) between LGD and far field predictors calculated for upslope areas in certain topographical zones of influence (zi).  $\rho$  coloured in light red indicate insignificant coefficients ( $p$ -value  $> 0.05$ ).  $\rho$  coloured in grey to black in dependence of the strength of correlation indicate significant coefficients ( $p$ -value  $< 0.05$ ). gg is the abbreviation for groundwater gradients and ltg the abbreviation for low topographic gradient in direct vicinity to the lake shore.**

zi/ Predictors	Size	Mean elevation	Mean slope	Percentage of ltg	Mean gg -ordinary kriging-	Mean gg -regression kriging-
<b>25 m</b>	<b>0.15</b>	<b>0.61</b>	<b>0.58</b>	<b>-0.44</b>	<b>0.33</b>	<b>0.64</b>
<b>50 m</b>	<b>0.03</b>	<b>0.62</b>	<b>0.64</b>	<b>-0.30</b>	<b>0.36</b>	<b>0.65</b>
<b>100 m</b>	<b>-0.19</b>	<b>0.45</b>	<b>0.58</b>	<b>0.00</b>	<b>0.32</b>	<b>0.59</b>
<b>200 m</b>	<b>-0.31</b>	<b>0.23</b>	<b>0.54</b>	<b>-0.02</b>	<b>0.33</b>	<b>0.55</b>

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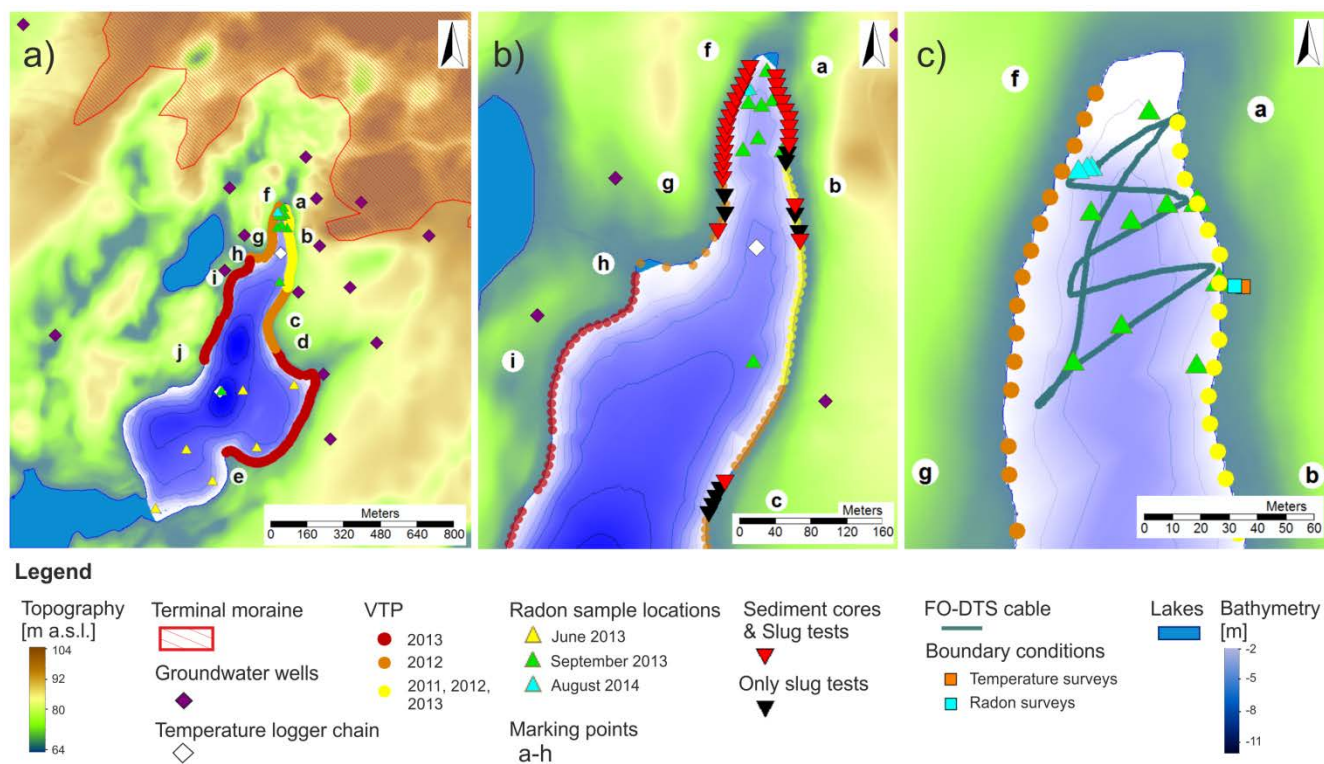


**Table 5: Linear regression models describing the correlation between LGD and far-field predictors and the coefficient of determination ( $R^2$ ). gg is the abbreviation for groundwater gradients and ltg the abbreviation for low topographic gradient in direct vicinity to the lake shore.**

Predictor (x)	$z_{i25m}$		$z_{i50m}$	
	Models (LGD = ...)	$R^2$	Models (LGD = ...)	$R^2$
Elevation	$-591.62 + 9.65x$	0.35	$-273.14 + 4.65$	0.34
Slope	$21.66 + 2.04x$	0.33	$20.74 + 2.2x$	0.32
Percentage of ltg	$52.61 - 1.29x$	0.11	-	-
gg -ordinary kriging-	$30.12 + 141.11x$	0.09	$27.18 + 167.90x$	0.12
gg -regression kriging-	$21.16 + 62.30x$	0.37	$21.08 + 64.36x$	0.36

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**Figure 1: Study site and experimental infrastructure. (a) Overview of the study site with VTP measurement and radon sampling locations and locations of groundwater wells and temperature logger chains (b) Slug test and sediment core sampling locations, (c) FO-DTS installation and radon sample location in the northern part of the lake.**

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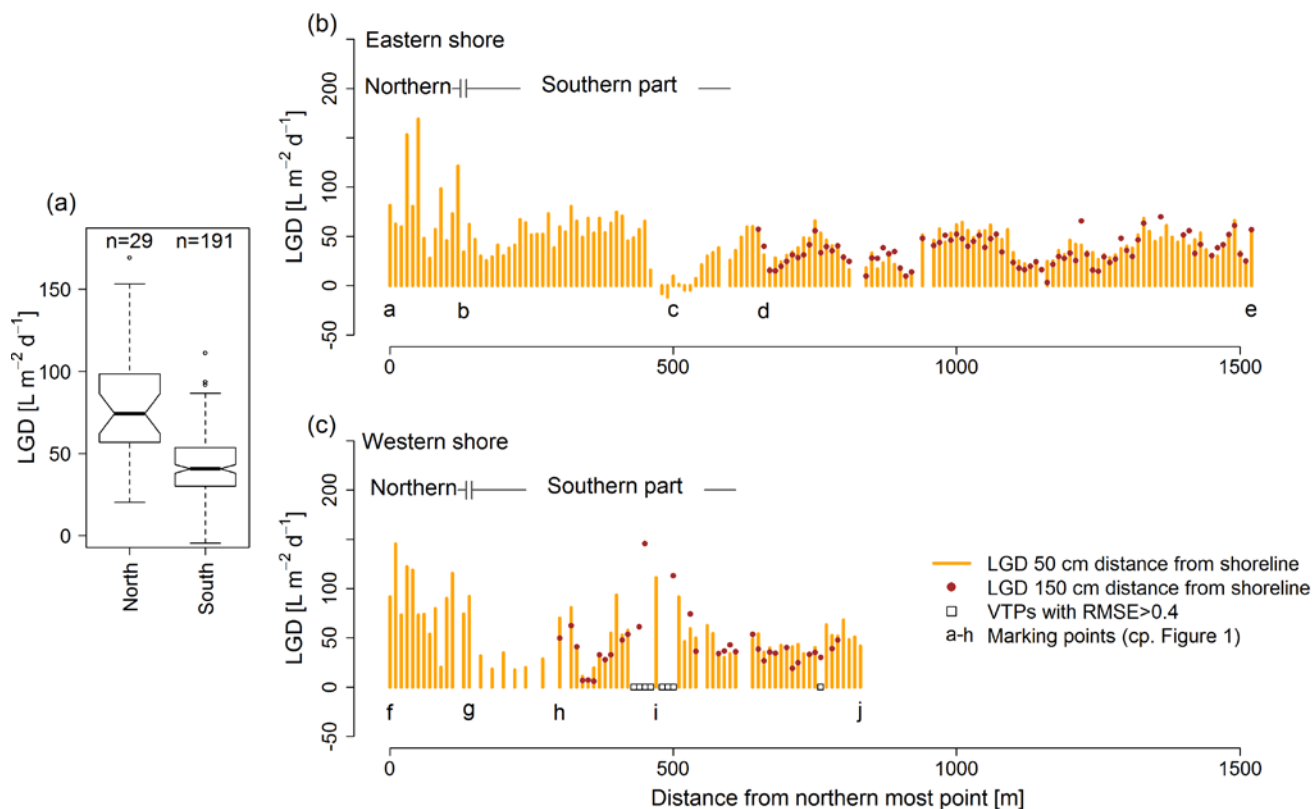
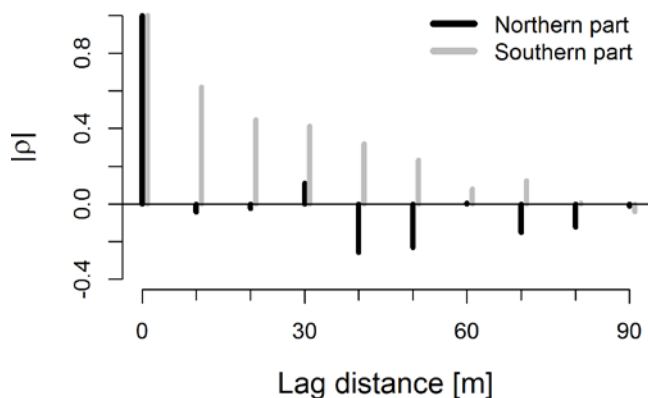


Figure 2: LGD estimated from VTPs measured at 50 cm and 150 cm distance from shoreline, (a) LGD distribution from VTPs in the northern and southern part measured at a distance of 50 cm LGD along eastern shore (b) and LGD along western shore (c).



5 Figure 3: Autocorrelogram for the LGD series of the northern and southern part of the lake.

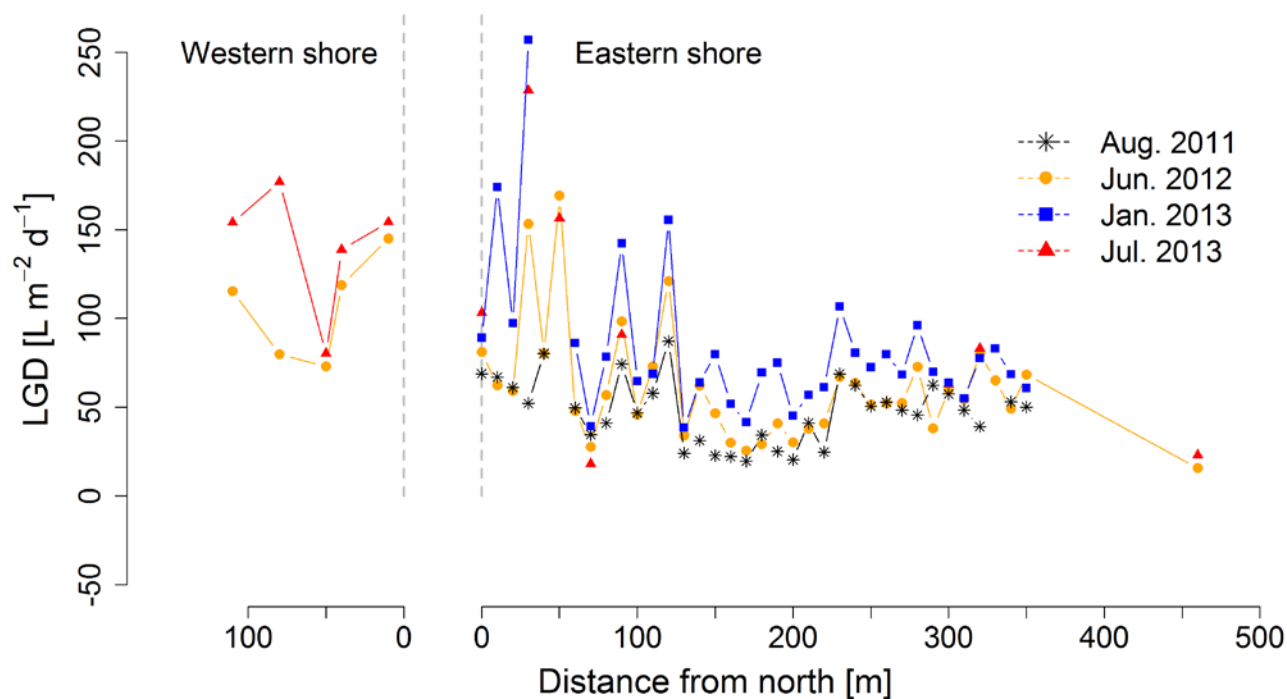
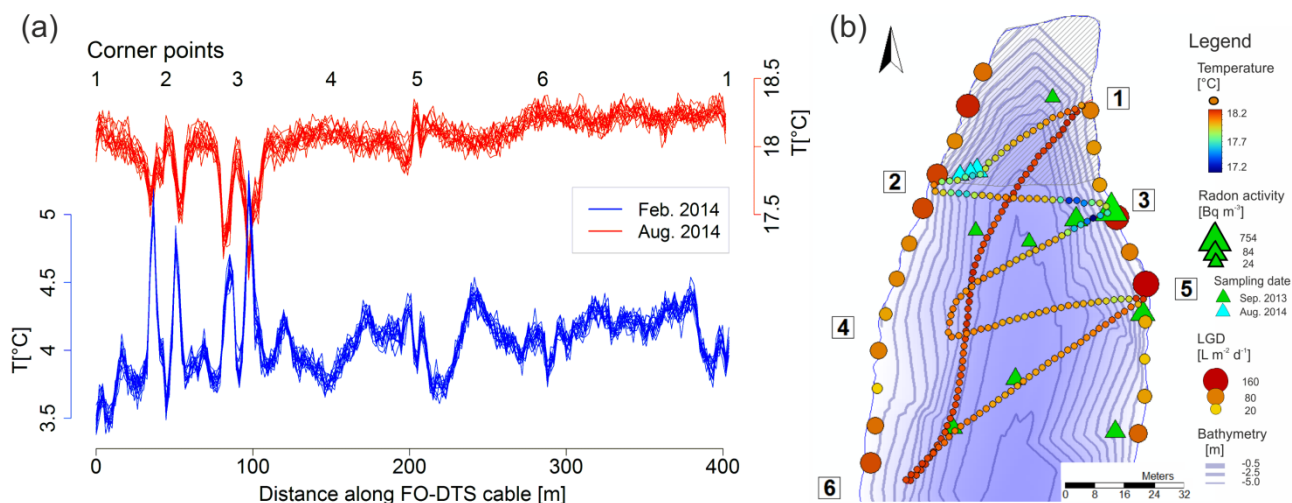


Figure 4: Calculated LGD rates from repetitions of VTP measurements in August 2011, June 2012, January 2013 and July 2013 at the northern western and eastern shore.



5 Figure 5: Lake sediment temperatures measured with the FO-DTS system. (a) Temperatures measured in February and August along the FO-DTS cable. (b) Localisation of sediment temperatures measured with the FO-DTS in August 2014 (median) and radon activities measured in September 2013 and August 2014. LGD rates along the shoreline were derived from VTPs measured in June 2012.



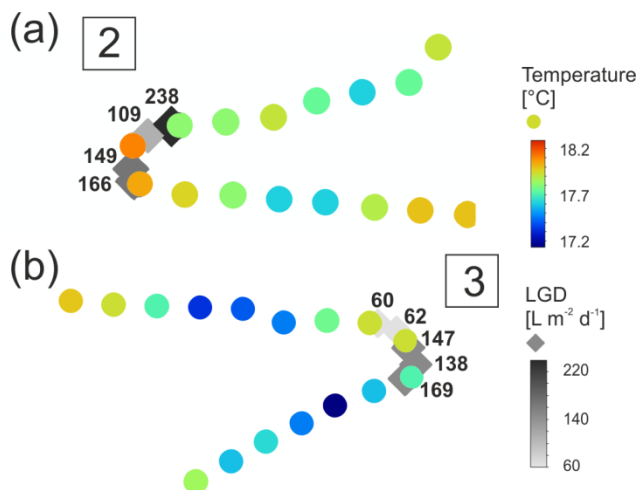
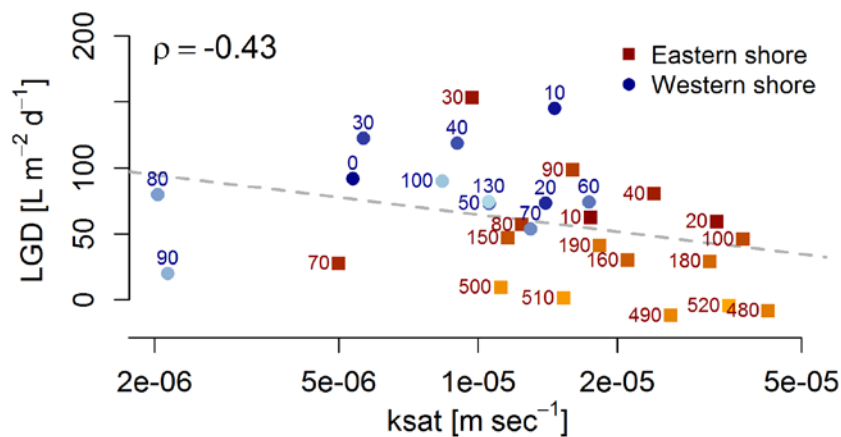


Figure 6: Sediment temperatures measured with the FO-DTS in August 2014 (median) and LGD rates derived from VTPs measured at corner two (a) and three (b). Labels of rhombuses show the measured LGD rates.



5 Figure 7: LGD plotted against  $k_f$  values determined from slug test at the western and eastern shore, the labels and the strength of colour indicates the distances of measurement locations from the northern tip of the lake.

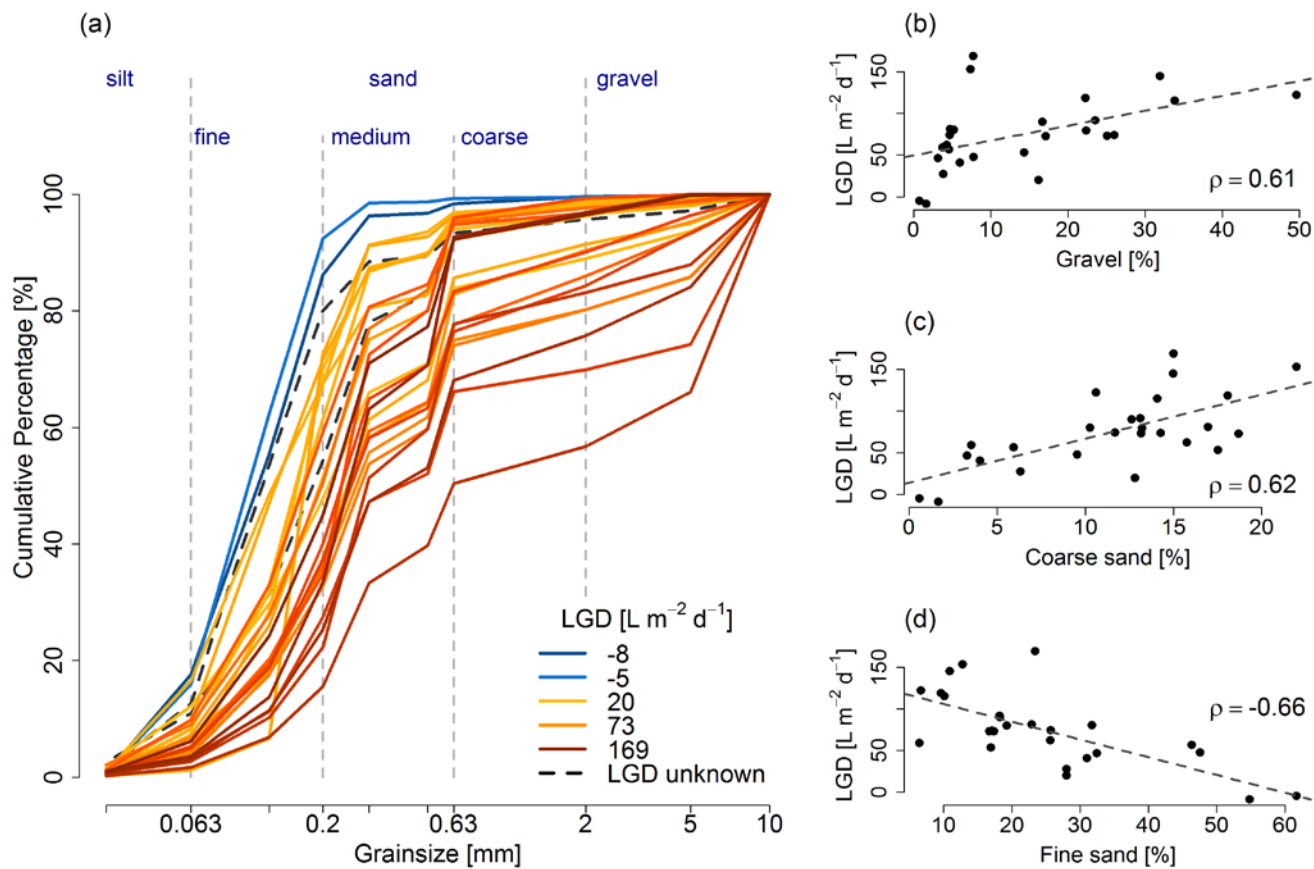
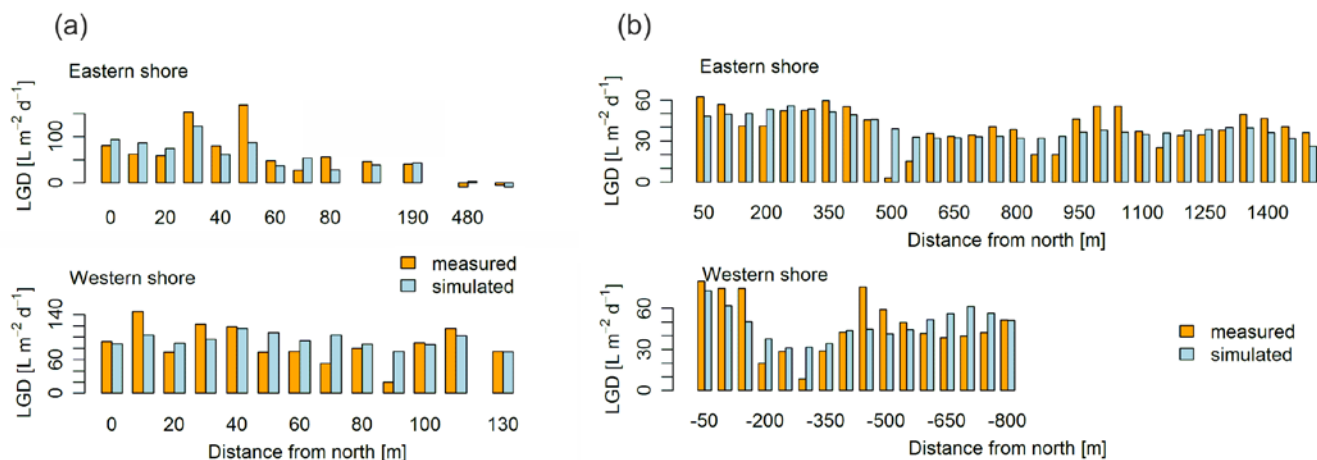


Figure 8: (a) Grain size distributions from sediment cores coloured by the strength of LGD rate; (b–d) LGD rates are plotted against the grainsizes gravel (b), coarse sand (c) and fine sand (d).



**Figure 9: Observed and calculated LGD distribution along the shore line. (a) Small scale patterns using multiple regression model with coarse sand and fine sand as predictor and (b) large scale patterns using linear model considering groundwater gradients derived from regression kriging.**

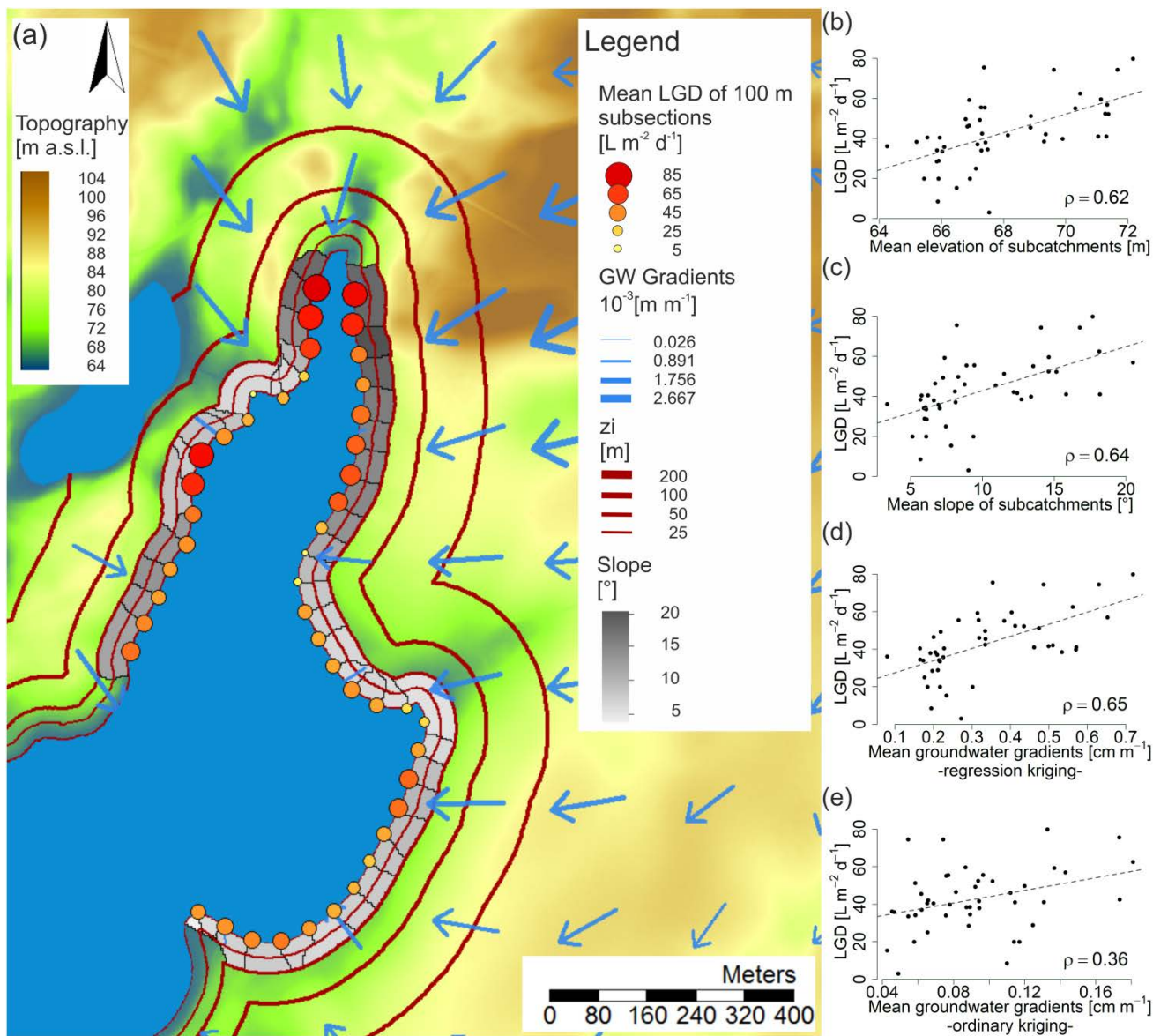


Figure 10: Correlation between far-field conditions and LGD. (a) LGD of lake subsections and mean slope of upslope areas for topographical zone of influence ( $z_i$ ) of 50 m, Groundwater gradients (GW gradients) are derived from interpolation of measured groundwater levels using regression kriging. (b–e) LGD rates of lake subsections are plotted against the far-field conditions mean elevation (b), mean slope (c) and mean groundwater gradients derived from regression (d) and ordinary kriging calculated for  $z_{i50m}$ .

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