

## Author's Response

We are thankful for the critical reading, constructive comments and suggestion made by all referees. Their comments were very important to enhance our paper. Below we address all questions and comments made by each referee.

### N. Jarvis: major comments

- 5 Regarding the conclusion that proposed models are recommend, it was slightly changed after taking into consideration the Akaiki information criteria. Regarding the values of  $\lambda$  (changed to  $l_m$ ) of the proposed models, they can be greater than 1, as discussed in more detail in points 9 and 16. In applying the evaluated models in blind predictions the JMII may have more advantages over the other models as it is more physically based. This was pointed out in the conclusion. One of the reason why the models PMm and JMm perform better than JMII can be seen now in the discussion, at the end of Section 4.2.
- 10 We considered your suggestion for the title.  
Specific questions:
1. Page 2, lines 24-25 (and line 3 in the abstract): I am not so convinced of this. I would prefer to use a physics-based model even if it did have two or three more parameters, as long as they were, in principle, measurable. The limiting leaf water potential is quite well known, at least
- 15 **R.: We also would prefer using a physics-based model, but in practice it appears not to be appealing. Root water uptake (RWU) models are usually embedded in larger hydrological models, for instance the ecohydrological model SWAP (Van Dam et al., 2008), and most users are unfamiliar with plant hydraulic parameters, making them to prefer the simplicity of empirical models like the Feddes et al. (1978) model, as long as empirical parameters are available. Besides, apart from the well-known limiting leaf water potential, radial root hydraulic conductivity has a strong effect on RWU distribution as shown in the paper and it is**
- 20 **not easily available.**
2. Page 4, line 5–8: the sentence starting ... “using  $h$  seems ....” is wrong, as the authors know well enough. It is immediately contradicted by the text at lines 14-21 on the same page (and by the results shown later in the paper). This sentence should be deleted. The remaining text just says that various forms have been proposed for the  $\alpha$  function, but that making  $\alpha$  depend on M is physically the most plausible. This is quite sufficient
- 25 **R.: The sentence is in fact misleading. It was intended to say “Comparing to  $\theta$ ,  $h$  seems to be more feasible...” instead of “Using  $h$  seems”. It was corrected as such.**
3. Page 5, equation 8:  $h_0(z)$  is not defined, as far as I can see?
- R.: It is defined now**
4. Page 5, lines 20-22: yes, it would be good if you mentioned this phenomenon by its name: hydraulic lift or hydraulic re-  
30 distribution. You could also cite Jarvis (2011) here, since he discussed and clarified the relationship between water uptake compensation and hydraulic lift in some detail (see the text in relation to equations 13 to 15 in the final version of this paper, not the HESS discussion paper that you cited: see point 4. under “Presentation”)
- Agree, it is important to mention the name of the phenomena as well as cite Jarvis (2011). These changes are incorporated in the text.**
- 35 5. Page 6, lines 1-3: I know what you are trying to say here, but it is not so well expressed. You could replace i.) “... is only relevant” by “... it only needs to be explicitly addressed ...” and ii.) “... becomes less important” by “... is not necessary”. This would help, but you could also add a sentence at the end of this saying that the effects of compensation can nevertheless be explicitly discriminated and identified in physics-based models. This is demonstrated in Jarvis (2011) in the text related to equations 13 and 14 in that paper (again, in the final version).

- The text is improved accordingly. However, we don't think it is always possible to explicitly discriminate and identify the effects of compensation in physically-based models. Such relation (Jarvis (2011) eq. 13 and 14) was easily found for the De Jong van Lier et al. (2008) model comparison (Jarvis, 2011). Furthermore, adding this comment would be contrary to our general reasoning when we add that "In physical models, discriminating compensation is not necessary since in such models "compensation" follows implicitly from the RWU mechanism".
6. Page 6, lines 11-12: "In principle, any definition of  $\alpha$  is applicable...". Yes, perhaps, but it does make a difference to the results of course, as you demonstrate very well later in the paper! But what is definitely not debatable is that Jarvis (1989) used a threshold type function for  $\alpha$  based on water content (degree of saturation). The reason for adopting this approach was discussed by Jarvis (1989) in relation to the experimental evidence available at that time and no other type of function was considered. The fact that you adopt a Feddes-type function means that in the rest of the paper you cannot refer to this model as the Jarvis (1989) model. It is a modified Jarvis (1989) model, in exactly the same way that JMm is also a modified Jarvis (1989) model, where the threshold water content function is replaced by a threshold function of matric flux potential: in other words, you investigated two different modified Jarvis models and you should refer to them as such, both in table 1 and throughout the rest of the paper, including the abstract (perhaps you could call them JMm1 and JMm2?)
- 15 R. Indeed, any kind of  $\alpha$  might provide different predictions. We agree that using the Feddes reduction function in the Jarvis (1989) model is also a modification of the Jarvis (1989) model. Thus, we renamed the Jarvis (1989) model to JMf. We also moved the statement "In principle, any kind of  $\alpha$  is applicable..." to the end of the section, and then introduced the modified version JMf.
7. Page 6, line 28 to page 7, line 4: this is a little vague. You followed quite closely what Skaggs et al. (2006) wrote in this section, but since they wrote their paper ten years ago, it is now much better established exactly how the original Jarvis (1989) model departs from physicality. This was clarified in the papers by Jarvis (2010, 2011), which you also discuss in the following section. There are two aspects to this:
- i.) the choice of function for  $\alpha$ . The threshold function chosen by Jarvis (1989) doesn't make complete physical sense, as the local resistance to uptake should in principle increase continuously as the soil dries (e.g. like equation 18). Jarvis (1989) discussed this choice in terms of the overall resistance to uptake being dominated by an air gap between soil and root which might only develop after a certain critical water deficit was reached: this choice was strongly influenced by experimental studies which showed such an effect. Also, at high soil water contents, the overall resistance to uptake in the soil-plant system would be dominated by plant resistances, which may be more or less constant. Thus, a threshold function might be a good choice from an empirical point of view. In this respect, it can also be pointed out here that the authors also adopt a threshold  $\alpha$  function in the PMm model. This model is the one the authors finally recommend, because it works best, although it can certainly be criticized on the same grounds (i.e. that it "affronts the definition of  $\alpha$ ").
- ii.) Compensation under non-stressed conditions. As you point out, under non-stressed conditions the Jarvis (1989) model does give a different uptake distribution compared with the de Jong van Lier physical model. However, it is wrong to imply that the Jarvis (1989) model does not predict any compensation under non-stressed conditions (page 7, line 4). Under non-stressed conditions, water uptake is increased by a factor of  $1/\omega$  in all layers (regardless of the pressure head distribution) to maintain transpiration at the rate demanded by the atmosphere during soil drying. It is also not wrong in principle to link compensation to plant stress (page 7, line 3): the onset of stress certainly does affect the nature of compensation: this is demonstrated in Jarvis (2011) in the text following equations 13 and 14 for the physics-based model of de Jong van Lier (2008).
- 40 For the above reasons, I strongly suggest that you delete the text on page 6 line 28 to page 7, line 4 and replace it by a short sentence that simply states that the Jarvis (1989) model departs from complete physicality in some respects and that this is explained in the following section. Then at the end of the next section (i.e. after equation 21) you can briefly summarize how the Jarvis (1989) model departs from physicality, based on the comparison with the physics-based model that is represented by equation 14-21. This will be very much clearer.

This as interesting discussion regarding the expected physical behaviour of reduction functions. We agree with the arguments. Therefore, we replaced the mentioned parts by shortly referencing to Skaggs et al. (2006) and Javaux et al. (2013). Finally we discussed a bit more about Jarvis (1989) model before showing how it departs from physicality.

8. Page 7, lines 5-12. The parameter  $h_3$  does not exist in the Jarvis (1989) model (see lines 10-11 especially). I think this paragraph can be deleted (or perhaps moved to the results and discussion section). At the very least, readers should be reminded that the original Jarvis (1989) model does not use a Feddes-type  $\alpha$  function.

We rearranged this paragraph by first defining JMF, then kept this discussion regarding to JMF.

9. Page 8, line 22: you should add the limits for  $\lambda$  here. If compensation means that water uptake increases from sparsely rooted layers, then  $\lambda$  must lie between zero and 1. Also, you should replace “deeper soil layers” by “more sparsely rooted layers” to be strictly correct.

We added the limits for  $\lambda$  in the text. In fact,  $\lambda$  is not restricted to the domain between 0 and 1. This is described in the text

10. Page 9, lines 23 to 26: I wonder what it is about your modification to the Li model (the use of the matric flux potential in a threshold function) that resolves the conceptual difficulties with the original formulation that you described earlier on page 9 at lines 3 to 8. As far as I can see, the same objections should be equally valid for this modified version as for the original model. This should be clarified and the text modified accordingly.

The main objection regarding the Li et al. (2001) model is the use of  $\alpha$  in  $\zeta$  (eq. 22). Thereby, “compensation” taking place before transpiration reduction (when  $\alpha = 1$  for all soil layers) can not be computed: RWU is distributed over depth only by  $R^\lambda$ . By using  $M$  instead of  $\alpha$ , “compensation” before transpiration reduction can be computed. As  $M$  integrates both the effects of  $K$  and  $h$ , it might be a better soil hydraulic function than  $K$  or  $D$  (Molz and Remson, 1970; Selim and Iskandar, 1978) to account for the effects of soil water in partitioning RWU. Such comments are added into section 2.2.4.

11. Page 11, lines 13-28: As I understand it from table 3, you only have a maximum of two parameters to calibrate for all the models, while each parameter is constrained within known limits. This means that a “brute force” grid search for optimum parameter values would be preferable to the method you chose, since you could be sure of avoiding risks of finding local minima (although it might be slower). I am sure there is no need to repeat the calibrations, but maybe you could mention this?

R.: The “brute force” grid search is a very slow method. As there are many scenarios and some models to evaluate, we do not think it is interesting to mention it since it would not be applicable in practice (a very small grid would also be required to avoid finding relative minimum).

12. Page 13, lines 23-24: yes, this may be why a constant value of  $\omega_c$  often seems to work quite well. Maybe you could add a comment to this effect, and also refer to your equation 20 and cite Jarvis (2011), where this aspect is discussed in detail.

R.: As eq. 20 gives an expression for  $\omega_c$  derived from the De Jong van Lier et al. (2008) physics-based model (Jarvis, 2011), it indeed helps in accounting for some aspects relating RWU phenomena. A constant  $\omega_c$  might be quite robust as can be inferred by eq. 20 and from common field observations. However, adding such a comment in this part (page 13, lines 23-24) might get out of the context of the paragraph

13. Page 15, line 18: You should replace “either R or M” by “both R and M”. But this sensitivity to  $M$  is in principle also present in the empirical models that include  $M$ . Why is it more important for JMII? Is it because this model is not calibrated? Or is it because of the different type of function? I can believe that predictions of JMII are, in comparison with the empirical models, more affected by the value of  $M_{max}$ , which must be a very uncertain parameter, not least because the Mualem-van Genuchten model of soil hydraulic properties is known to have an incorrect form close to saturation (since it does not allow for a maximum size of pore in soil). These questions should be clarified.

R.: This is explained in the text, at the end of Section 4.1.2. A new graph is inserted to support the discussion.

14. Page 15, line 25: it could also be noted (perhaps by referring to equation 20) that  $\omega_c > 1$  is not physically unrealistic.

R.: Yes,  $\omega_c > 1$  is not physically unrealistic and it is implicitly stated in line 25: “by setting  $\omega_c > 1$ ”. It means JMII and JMm can predict  $T_a/T_p < 1$  for the low  $R$ -high  $T_p$  scenarios as VLM did, but we decided to not assess these results since it is not possible to compare to other empirical models.

5 15. Page 16, line 3: This is misleading. The Feddes function for  $\alpha$  is not part of the Jarvis (1989) model.

R.: The text was corrected accordingly.

16. Page 17, lines 1-2: it is confusing that different symbols are apparently used for one of the parameters in the Li-type models. In equation 25,  $\lambda$  is used, whereas in the text here and in table 5,  $l$  is used, while in table 4  $l_m$  is used. I believe they are all the same parameter?

10 If I understood it correctly, I don't see how you can write that the optimal values of  $\lambda$  follow a logical relation to  $R$  and  $T_p$  (line 1). In many cases, and especially for low root densities, values of  $l$  (i.e.  $\lambda$ ?) in table 5 are larger than 1, which implies to me that compensation is working incorrectly in these scenarios (it is decreasing uptake in the more sparsely rooted layers). Also, in table 4, it is stated that  $l_m$  (i.e.  $\lambda$ ) was constrained to take values less than or equal to 1. If I understood it correctly, the results in table 5 suggest that this was not actually the case in practice.

15 R.: All symbols refer to the same parameter and we corrected this by changing them to  $l_m$ . Regarding the  $l_m$  parameter limit values, the upper values for  $l_m$  were constrained to 3. Conceptually, there is no inconsistency in taking  $l_m > 1$ . Indeed,  $l_m = 1$  means no compensation at all and  $l_m < 1$  implies compensation. Values of  $l_m > 1$  simply indicates that the upper soil layers are more important for RWU distribution. This is now explained in section 2

17. Section 4.2, table 6: can you give the total precipitation and potential transpiration here? It's good to get a rough idea of  
20 how much stress occurred in these simulations.

The old table 6 was substituted by a figure of the time course of cumulative transpiration, precipitation and  $T_p$ . The values at the of the period are also given in the figure.

18. Page 18, lines 10-12: you did not test the Jarvis (1989) model (see earlier comments).

R.: It is corrected

25 19. Page 18, line 12: I did not get a good understanding of why the JMII model does not work so well for high  $R$ -low  $T_p$  scenarios (i.e. high compensation). I would have thought that, in principle, it should work OK. Please briefly explain what you think the reasons are for this.

R.: This is explained at the end of section 4.1.2.

20. Lines 16-18: I think this is too optimistic, as this test was not a very tough one. You had the same plants (identical roots)  
30 and the same three soils. How would it look if you had simulated different scenarios (soils, plants)? I think you would need to re-calibrate the empirical models. How useful is that?

R.: Yes, the results would be different. However, it is useful to show that the methodology used to calibrate the models is robust and can be used to assess empirical models and sensitivity of the empirical parameters in order to provide a full calibration of the empirical models in a next step.

## Anonymous Referee #2: major comments

i) Regarding the dependence of the model parameters on transpiration rate, the stress reduction function parameters are already shortly discussed on how they depend on potential transpiration. Adding a discussion about this dependence in the review section would be rather repetitive. Thus, we think is better to discuss it only in the results.

5 ii) We think the general advantages concerning the use of empirical models as compared to the De Jong van Lier et al. (2013) physical model can already be found page 2, lines 23 to 27.

iii) We included transpiration prediction in the conclusion.

10 iv) It not possible to directly retrieve root water uptake from measurements. This is one of the advantage of using physically-based models. The main purpose of this paper is to evaluate empirical models that can be sensitive to the variations of root water uptake due to different scenarios of soil and plant properties as well as climatic conditions as predicted by a physical model. By using root water uptake it is possible to strictly capture the root water patterns predicted by the models, whereas for instance if using soil water content the results can be “blinded” by the sensitivity of RWU on soil water content which vary with soil type. Using transpiration may lead to wrong predictions on root water uptake. This is addressed now in the paper, in section 4.1.5.

15 Specific questions.

1. P4: root length density  $R$ . Shouldn't that have dimension  $L L^{-3}$  ?

Yes, it is corrected.

20 2. P4: The authors propose a stress function  $\alpha$  which is a stepwise linear function of  $M$ . Since  $M$  is a function of  $h$ , the new stress function will be a function of  $h$  also. But the shape of the function will have a different shape than a piecewise linear function of  $h$ . Furthermore, the relation between the new stress function  $\alpha$  and  $h$  will depend on the hydraulic soil properties and will therefore be different in soils with a different texture. The original Feddes  $\alpha(h)$  function depends on the transpiration rate as shown in Figure 1. Figure 1 suggests that the new stress function  $\alpha(M)$  does not depend on the transpiration rate. I do not understand why the transpiration dependency of the stress function disappears when  $\alpha$  is expressed as a function of  $M$  since  $M$  does not depend on the transpiration rate.

25 This is a very important observation. In fact the new  $\alpha$  function also depends on potential transpiration rate  $T_p$ . This dependency is implicitly expressed in the critical value  $M_c$  of  $M$ . Therefore, as in the case of the Feddes  $\alpha$  function there should be two values for  $M_c$ : one for low  $T_p$  and other for high  $T_p$ . Fig. 1 is now corrected.

30 3. P5: In 15: “Because  $T_a$  and  $h_l$  are unknowns, eq. 8 and 10 cannot be solved analytically, but an efficient numerical algorithm is described in De Jong van Lier et al. (2013).” I did not understand this. I thought that either  $T_a = T_p$  is known as a boundary condition so that  $h_l$  can be calculated or  $h_l = h_w$  is known and  $T_a$  is calculated. I think that the reason why the  $h_l$  (or  $T_a$ ) cannot be derived directly is because the set of equations that needs to be solved (including also all  $h_{0,i}$ 's ) is non-linear in  $h_{0,i}$ .

As commented in the interactive discussion, the sentence is wrong. The set of equations can be solved analytically, but not in a direct way, for some special cases of Brooks and Corey (1964) soils. The sentence is now corrected.

35 4. P5 In 17 and p 29 Figure 2: There are several things I do not understand about Figure 2. The figure caption says that the plant transpiration was set to  $1 \text{ mm d}^{-1}$ . Shouldn't for a fixed rooting depth the root water uptake or sink term  $S$  be constant and independent of the root length density  $R$  until a threshold soil water potential is reached? This threshold will depend of course on the leaf water potential and the root length density. Can it be that the curves shown in Figure 2 shown the maximal possible sink term as a function of the soil water potential for different leaf water potentials and root length densities? But, when the root water uptake goes to zero, why doesn't the soil water potential then go to the leaf water potential? Now there seems to be

a 10 m difference between them. Second, why doesn't the root water uptake for a certain soil water potential then not increase with decreasing leaf water potential. For sufficiently large (small absolute value) soil water potential, the root water uptake becomes independent of the leaf water potential. I do not understand this since the water potential difference increases with decreasing leaf water potential and therefore the root water uptake should also increase with decreasing leaf water potential.

5 These question were address in the interactive comment

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5. P7 In 21: "where  $T_{p_{max}}$  is the maximum possible transpiration rate attained when  $M_0 = 0$ ". This assumes that the minimal water potential at the soil-root interface is  $h_w$  (wilting point). But, doesn't this minimal water potential depend also on the critical leaf water potential  $h_l$ ?

10 Yes, it depends on  $h_l$ . The limiting pressure head at the soil-root interface (called  $h_{ws}$  to avoid confusion) is less negative than the limiting  $h_l$  (called  $h_{wl}$ ). Although  $h_{ws}$  depends on  $h_l$  and on plant and soil hydraulic parameters, for the sake of simplicity we considered it as constant and equal to -150 m. The  $h_{ws}$  value was the limiting value used in the empirical models that depends on  $M$  and is listed in Table 2.

6. P7 Eq. 17: Why is  $M_0$  constant with  $z$ ? The soil root interface water potential can depend on the depth, can't it?

15 We take advantage of your question and correct eq 6 to explicitly make  $M_0 = M_0(z)$ . However, De Jong van Lier et al. (2008) did assume  $M_0$  constant with depth in order to solve the problem of the two unknowns:  $T_a$  and  $M_0$ . They made a justification for that, and we refer to their paper (De Jong van Lier et al., 2008) for more detail. With this assumption it was possible later on to Jarvis (2011) make a comparison with the Jarvis (1989) model.

7. P8 In 15: "The Jarvis (1989) model predicts RWU by a weighting factor between  $\rho$  and  $M$  throughout rooting depth". This is not very clear to me. What do you mean with a weighting factor "between  $\rho$  and  $M$ "? Do you mean a weighting factor that is equal to the product of  $\rho$  and  $M$ ?

20 An interesting feature of the analogy between the Jarvis model and the De Jong van Lier et al. (2008) model is that the analogy is derived based on the assumption that stress only occurs when everywhere at the soil-root interface limiting conditions are reached. It is assumed that  $M_0$  is zero everywhere in the root zone. But, I am wondering whether the De Jong van Lier et al. (2008) only predicts stress under these conditions. Can it be that stress occurs even though  $M_0(z)$  is not zero everywhere in the root zone? If this is the case, then the analogy between the Jarvis and the De Jong van Lier et al. (2008) models is not given always when stress occurs.

30 A weighting factor was meant as equal to the product between  $\rho$  and  $M$  divided by the integral of this product over the rooting zone. As  $M_0$  in the De Jong van Lier et al. (2008) model is constant over depth, stress is assumed to occur when  $M_0 = 0$  over the root zone.

8. P 8 In 22: "The smaller  $\lambda$ , the more water is taken up in deeper soil layers" I would reword this to "... the more water is taken up from layers with a low root length density".

We improved this part and we took note of your suggestion.

9. P 9 In 1: "RWU is calculated by substituting eq. 23 into eq. 3, following the Feddes approach." This implies that you multiply Eq. 22 again by  $a(z)$ . So in the nominator, you get  $\alpha^2$ ?

Yes, and it is an alternative case to write the equation.

10. P9 In 16: Same comment as above.

No, in this case it will not happen since  $D$  or  $K$  is used to account for water availability.

11. P 9 In 18: “In drier soil layers,  $\Gamma$  is reduced, whereas in wetter soil layers  $\Gamma$  is increased, thus increasing RWU in these layers before the onset of transpiration reduction.” I do not understand this. If the soil dries out but faster in the upper layers where the root length density is higher than in the deeper layers, the deeper soil layers will not get wetter so  $\Gamma$  will not increase in the deeper soil layers, which are still wetter than the upper soil layers. But,  $\zeta(z)$  will increase in the deeper soil layers that remained wetter.

The sentence was rephrased. As you put out well, in fact  $\Gamma$  in wetter soil layers will not increase, but  $\zeta$  will do because  $\Gamma$  in these layers will be less reduced compared to  $\Gamma$  in the upper dryer layers.

12. P9: Proposed empirical model. Is in this model also the  $\alpha(z)$  factor of the Feddes model used?

General question on the used models: The Feddes stress function  $\alpha(z)$  is besides a function of the soil water potential, also a function of the potential transpiration rate. How is this considered in the different models? It should be noted that Eq. (20) suggests that  $\omega_c$  in the Jarvis model is a function of the transpiration rate but the  $\alpha(z)$  used in the Jarvis model is according to Eq. 18 not a function of the transpiration rate. Furthermore, the modified version of the Feddes model shown in Figure 1b suggests that there is no dependence of the  $\alpha_m$  function on the transpiration rate and that  $\alpha_m$  depends only on the matric flux potential. When looking at table 4, it seems that there is no transpiration rate dependence of the Feddes parameters.

15 The proposed root water uptake models are obtained by incorporating  $\zeta_m$  into eq. 23, then into eq. 3. The PM uses Feddes reduction function whereas PMm uses the proposed reduction function  $\alpha_m$  as shown in Table 1. This is described now in the text.

The dependence of the models on potential transpiration are implicitly built-in in the values of their empirical parameters that were optimized. For instance, in the Feddes reduction function there are two values for  $h_3$ : one for low  $T_p$  ( $h_{3l}$ ) and another for high  $T_p$  ( $h_{3h}$ ). The dependence of  $T_p$  in the other models are accounted for similarly. We then optimized the models for two levels of  $T_p$  (1 and 5 mm d<sup>-1</sup>), therefore the optimized parameters are derived for low and high  $T_p$ .

13. P11 In 26: “For high non-linear problems as the one in eq. 29 GLM depends on the initial values of b.” This needs to be reformulated. The GLM does not depend on the initial values of b but the optimized parameter set may depend on the initial value of b since the GLM is a local optimization algorithm that may converge in a local minimum instead of the global minimum.

We agree with your observation. It was reformulated accordingly.

14. P 12: “3.2.1 Growing season simulation”. This is not a sub section of the optimization section.

Yes, it is corrected.

15. P13 In 8: “ $h_w (= -200 \text{ m})$ ”. I am confused here because at p 10 it is written: “The value of the parameter  $h_4$  was set to -150 m.”

As discussed above in point 5, we used different abbreviations for them.

16. P15 In 30: “showed by the presence of an outlier and lower median. “→” “shown” and “median”

Thanks for noticing. It is corrected.

17. P17: Growing season simulations. It would be good to have more background about the potential transpiration and the precipitation during the considered growing season.

A new plot was inserted and Table 6 was deleted.



### Anonymous Referee #3: major comments

- i) Regarding the discussion of the empirical models, we hope it is improved with the modifications made.
- ii) Regarding fitting the models to temporal course of transpiration. We added a new subsection in which we discuss this. Instead of using a more problematic scheme, we show (for some models and scenarios) that fitting the models only to RWU can provide suitable relative transpiration predictions for the models that account for “compensation”. Therefore, it seems unnecessary to use a more problematic weigh scheme for the paper purpose. Conversely, it is shown that fitting the models to  $T_r$  leads to wrong predictions of RWU.
- iii) It is correct that those models that use matric flux potential are mathematically closer to the reference model, an advantage for the comparison. We added a comment about this at the end of Section 4.2.
- 10 iv)“ One of the critical points concerning the Feddes stress response function in combination with the Jarvis (1989) compensation approach, the authors mention, is that the models fail to predict compensation under wet conditions, where alpha is 1 for different matric potentials. The modification using martic flux potential with distinct critical point ( $M_c$ ) will perform alike. It seems it is already discussed at the end of the this paragraph: “... Conversely, the JMm was able to reproduce considerably well the VLM pattern for these scenarios due to the shape of  $\alpha_m$  as discussed above. As soon as  $M > M_c$  in the upper layers, RWU decreased at a higher rate, compensated by increasing uptake from the wetter, deeper layers”.
- 15 RWU decreased at a higher rate, compensated by increasing uptake from the wetter, deeper layers”.
- v) Regarding the fact the “Model PM mixes stress reduction described by pressure head and compensation calculation based on matric flux potential”. Conceptually the two models distributes RWU over depth by taking into account root length density and a hydraulic function to account for the effects of soil water in partitioning RWU. Any hydraulic function could be used, however the matric flux potential seems to be a good alternative since it integrates both effects of soil hydraulic conductivity and soil pressure head. This will define  $S_p$  in the model. The actual local uptake can then be obtained by applying a stress response function  $\alpha$  of any type, and for PM  $\alpha = \alpha(h)$  is used. Thus, the fact that PM mingles  $M$  and  $h$  is not conceptually unreasonable.
- 20 and soil pressure head. This will define  $S_p$  in the model. The actual local uptake can then be obtained by applying a stress response function  $\alpha$  of any type, and for PM  $\alpha = \alpha(h)$  is used. Thus, the fact that PM mingles  $M$  and  $h$  is not conceptually unreasonable.
- vi) Using variable boundary conditions would provide more information content of the “measurements”, as you comment, as compared to the used constant boundary condition. The applied scenarios included distinct hydraulic conditions, submitting the models to a wide range of conditions. This is also discussed now at the of section 4.1.4.
- 25 the models to a wide range of conditions. This is also discussed now at the of section 4.1.4.
- vii) Indeed, it is important to discuss about other existing physical models. We briefly discussed this in the introduction.
- viii) Although considering daily variation of  $T_p$  during the day would give more detail about the predictions, the simulations performed did provide important features to strictly analyse De Jong van Lier et al. (2013) model as shown in section 4.1. In most applications root water uptake models are performed with no variation of  $T_p$ .
- 30 ix) The title was changed.

Specific questions.

1)Page 1, Lines 7 to 8: “The simulated scenarios give more insight into the behaviour of the physical model, especially under wet soil conditions and high potential transpiration rate.” This statement seems not to be important for the abstract and can be omitted.

35 **OK, it is omitted**

2) Page 1, Lines 10 to 11: “...for the scenarios of low RWU “compensation”. Better: “...for the scenarios for which RWU “compensation” is expected to be low.” or “. . .for the scenarios for which the physical model predicts low RWU “compensation.”

**OK, it was will considered**



4) Page 1, Lines 13ff: When the Jarvis model is criticized it should be stated that the modifications are conceptually closer to the reference model.

It is discussed in the results.

5) Page 1, Lines 13 to 14: “Incorporating a newly proposed reduction in the Jarvis model...” Consider: “Incorporating a newly proposed reduction function in the Jarvis model...” I did not find a statement about the performance of the Jarvis (2010) model in the abstract.

Considered. A statement was added

6) Page 2, Lines 17 to 18: Models that do not account for compensation are under some circumstances (not all) less accurate, e.g. for coarse to medium textured soils and high root length density.

10 Agree, the sentence is corrected.

7) Page 5, Line 24: “non-homogeneous” consider “heterogeneous”. “For non-homogeneous conditions, RWU for lower R can be the same for higher R depending on the stress level” Consider: For heterogeneous conditions, RWU for lower R can be the same as for higher R depending on the stress level...” Maybe I am mistaken but I do not see this in Fig. 2: For a certain leaf pressure head (for example -110 m), the RWU for R=0.01 is always lower than for R=0.1 and RWU for R=0.1 is always lower than for R=1.

The sentences were corrected. It seems Fig 2 does show that for a specific  $h_l$  RWU decreases as  $R$  decreases.

8) Page 7, Line 3: Consider another word than obscure. Compensation will certainly (and shall) enhance uptake (by the factor  $\alpha_2$ ) in some depth compared to the value given by alpha. To me the specific problematic issue is that in case of homogeneous alpha smaller than 1 and  $\omega_c$  smaller than 1, these models lead to uptake greater than given by the homogeneous value of alpha or, more generally, that relative transpiration can be higher than given by the highest value for alpha in case of heterogeneous alpha distribution with depth (see e.g. Skaggs et al., 2006, Simunek and Hopmans, 2009, Peters, 2016).

This is rewritten, following also the suggestions made by N. Jarvis in RC1 comment.

9) Page 7, Lines 3 to 5: If I understand it right, this holds only for the combination of the Jarvis model with the Feddes stress function for which alpha is 1 for different pressure heads (i.e. between  $h_2$  and  $h_3$ ).

25 This was rewritten. However, it seems any type of stress reduction function can be used, as for instance Jarvis (2010) used a different reduction function. The model essentially changes how/when transpiration is reduced: a new reduction function is introduced. Locally, any stress function can be considered for RWU.

10) Page 7, Line 14: Consider “conceptually” instead of “numerically”

OK

30 11) Page 8, Lines 14-15: I cannot follow:  $\rho$  and  $M$  as defined here do not occur in the Jarvis (1989) model.

This is the result of comparing Jarvis (1989) model to De Jong van Lier et al. (2008) model. The models can be correlated for stressed conditions if  $\alpha$  and  $\beta$  are given by eq. 18 and 19, respectively. For stressed conditions, substituting these eqs into the Jarvis (1989) model leads to the same equation for  $S$  of De Jong van Lier et al. (2008) model. However, the same does not happen for unstressed condition, which leads to a different equation for  $S$ , eq. 21.

35 12) Page 10, Lines 2 to 14: Consider using subsection header such as “3.1 Applied models”

OK

13) Page 10, Lines 19 to 20: A free drainage boundary condition is usually used for the case with very deep groundwater level so that groundwater cannot influence the soil. Then the assumption is that at a reasonably deep layer below the root zone the hydraulic gradients are close to unity. This is certainly not the case at the bottom of the root zone. I would suggest to set this boundary condition at a depth of at least 1 m or 1.5 m.

- 5 This is an important point and requires a careful justification. We used free outflow close to the bottom of the root zone. Many studies of water flow in soils without roots use the unit hydraulic gradient in the entire profile as a reasonable hypothesis. Extracting roots of course change this scenario dramatically, but simulated root length densities were already very low in the bottom part of the rooted zone. Nevertheless, changing the depth of free drainage will alter the water regime, especially in the lower part of the soil profile. That may, on its turn, change the simulated uptake pattern. Other important scenario changes might also be studied, like more or different soils with distinct soil hydraulic properties. Any alteration of this kind implies in a whole new set of scenarios and simulations and a considerable job in analyzing them and possibly lead to some new discussion or insight, but will it be a crucial factor in the comparison between the RWU models? We think it will not change the conclusions and we did not make changes in this respect.

14) Page 10, Line 24: “Soil date...” should be “Soil data..”

15 OK

15) Page 10, Line 26: “These soils are identified in this text as clay, loam and sand (Table 3).” Consider “These soils are identified in this text as clay, loam and sand.”

OK

- 16) Page 11, Line 12ff: Please specify in this section at which depths and which time interval the data for  $S$  and  $S^*$  were taken and used to minimize  $\Phi$ . Consider to fit also transpiration rates and use a weighted least squares scheme instead.

OK, this was specified. We added a section in which it was discussed.

17) Page 11, Line 15: “...the objective function to be optimized...” Consider “...the objective function to be minimized...”

OK

- 18) Page 11, Line 25: For a nonlinear problem with a model error, i.e. with models that do not fit the data well, there might be several local minima. Did all fitting runs lead to the same minimum? If not I would try to use more starting points to be sure or even a global minimization scheme.

Mostly they led to the same minimum. In the case it did not happen, we compared the minimum and made the fitting runs again. It is now also added in the text.

- 19) Page 12, Lines 1 to 2: “This guaranteed that RWU predictions from SWAP corresponded to the best fit of each empirical models to the De Jong van Lier et al. (2013) model.” I do not understand this sentence and how it refers to the statement that parameter fitting was only applied for the drying out scenario.

This sentence is just to emphasize that the optimizations were performed only in the drying-out scenarios and by optimizing the parameters the best fit to De Jong van Lier et al. (2013) model was reached.

- 20) Page 12, Lines 19 to 20: “Initial pressure heads were obtained by iteratively running SWAP starting with the final pressure heads of the previous simulation until convergence.” I do not understand. What converged to which values? And why was the initial condition optimized?

The swap was run until the initial soil pressure head set values were equal to the end pressure head set values.

21) Page 13, Line 3: “The patterns for the sand and loam soil (not shown here) show very similar features.” This is not immediately clear to me since matrix flux potential ( $M$ ) for the sand is very different from  $M$  of clay. In a sand most of the water is available under very low energy densities and thus I would expect that for sand, transpiration is prolonged much longer at potential rates and the drop of  $T_a$  to be much steeper after onset of transpiration reduction. Could you discuss this briefly in 2 or 3 sentences?

The RWU predictions for sand soil are very close from what you inferred. A short discussion was added.

22) Page 13, Line 14: “... increases the reduction of. . .” consider “... leads to faster reduction of...”

OK

23) Page 13, Line 15: “ assumes a parsimonious relationship...” do you mean “assumes a direct relationship...”

10 We mean a simple relationship when compared to other empirical relationships, ex. Fisher et al. (1981)

24) Page 14, Line 23ff, Tab. 5 and Fig. 6: For Sand with  $T_p = 1mm/d$  and  $R = 1cm/cm^3$  using the JM:  $\omega_c = 1$ ,  $h_3 = 0$  means that transpiration must be reduced from the beginning, since  $h > 0$  from the beginning and compensation cannot take place. I cannot see this in Fig. 6, where transpiration is equal to  $T_p$  for a prolonged time: Is it due to a very small reduction of  $\alpha_f$ , so that  $T_a$  is smaller than but still close to  $T_p$ ? Please discuss briefly.

15 The discussion of Line 23ff makes it clear to me that fitting not only the uptake pattern but also actual transpiration (see major comments) would increase model performance of the conceptual models. Then compensation would be most likely predicted.

Indeed, this is due to the small reduction of  $\alpha$ . We added a subsection regarding fitting the models to  $T_r$ .

25) Page 15, Lines 5 to 6:  $h_s$  cannot be lower than  $h_4$  if only transpiration but no evaporation is considered.

Agreed. It was corrected. In fact,  $h_s$  becomes close or equal to  $h_4$ .

20 26) Page 15, Lines 16 to 20 and general: “performs better”, “overestimates RWU”, . . . Please discuss the performance of the conceptual models always with respect to the VLM since you compare models. A comparison with real data is still the best benchmark.

ok

25 27) Page 15, Lines 21ff: Here fitted models are compared by statistical measures like  $E$  and  $r^2$ . Since the fitted models use different numbers of adjustable parameters such a comparison is not justified: More free parameters mean more flexibility and thus a better “chance” to fit the data. Please consider using other measures, which account for number of fitted parameters, like AIC (Aikaike, 1974).

AIC measure was included.

30 28) Page 15, Line 25: “. . . models (except for JM and JMm by setting  $\omega_c > 1$ ) are...” This can be omitted since  $\omega_c > 1$  makes conceptually no sense.

In fact it does make sense. See point 14 of RC1 comment.

29) Page 16, Lines 16 to 17: “The optimal  $h_3$  and  $M_c$  values (Table 5) for FM and FMm, respectively, increase as  $R$  or  $T_p$  increases, contradicting their conceptual relation to  $R$  and  $T_p$  levels” I see the contradiction only with respect to increased  $R$  but not to increased  $T_p$ .

35 It was corrected.

30) Page 16, Lines 31ff: I assume that parameters  $h_3$  and  $\omega_c$  for JM are highly correlated. Can you give information about parameter correlation? Moreover, such parameter correlation might be due to model structure but also due to data used for fitting the model. Therefore, I repeat my suggestion to use not only the drying out scenario for model calibration but the scenario with changing boundary conditions. This might reduce correlations.

5 We made a brief discussion about this.

31) Page 17, Lines 1 to 2: What are  $l$ -values?  $L_m$  and lambda respectively. Please unify.

It was corrected.

32) Page 17, Line 4ff: A figure with the cumulative transpiration over time would be interesting to see if there are under-/over-estimations for specific time intervals in the complete season.

10 Figure of cumulative transpiration was added and Table 6 was deleted.

33) Page 17, Line 23: The statement that JMII is poor in performance should be discussed with more caution since it was not adjusted to the reference model. Thus, this finding can be expected. The same holds to a less extend to the models for which only one parameter was adjusted.

The use of Akaike information helped the discussion about this.

15 34) Page 17, Line 24: This is a very daring conclusion, since the reference model and the proposed models have partly a similar structure (see above).

Although the proposed models are close to the reference model, it was not guaranteed that these simple modifications would result in considerable improvements in their predictions.

35) Conclusions section: I could not find a single conclusion. This is rather a summary and not a conclusion.

20 We added more information into the conclusion, but kept the writing style

36) Page 17, Line 32: “. . . especially under wet soil conditions and high potential transpiration.” Why do the simulations yield insight especially under wet soil conditions?

For high  $T_p$  and low  $R$  under wet conditions it was shown that  $T_p$  can not be achieve and also how plant hydraulic parameters relate to this.

25 37) Page 19, Lines 21 to 22: This paper is certainly not in press.

It was corrected

38) and Figures Table 3: Although the Mualem/van Genuchten model is well known the equations should be stated in the text to make it easier to assign the parameters. What, for example, is lambda? I guess the so-called tortuosity parameter in Mualem’s model, but I am not sure. Alternatively, Tab. 3 can be completely omitted and the functional relationships of  $\theta(h)$  and  $K(h)$  might be plotted in an extra figure.

We added the equations, but we kept the table.

39) Table 4: I cannot find  $l_m$  for PM and PMm in the text. Do you mean lambda instead of  $l_m$ ?

It was corrected.

40) Table 5: In the text root length density is  $R$  here it is  $R_d$ .

It is corrected.

41) Table 6: For comparison: what was the value for potential transpiration

The old table 6 was substituted by a figure showing the time course of cumulative transpiration, precipitation and  $T_p$ . The values at the of the period was also given in figure.

- 5 42) Fig. 1: a) since  $h_1$  and  $h_2$  are set to zero in all simulations, Fig. 1,a should account for that and start with  $\alpha = 1$  at  $h = 0$ .  
b) since  $M_c$  for  $T_p=1$  mm/d is different from  $M_c$  for  $T_p = 5$  mm/d, this should be indicated in Fig. 1b using  $M_{c,l}$  and  $M_{c,h}$ , similarly to  $h_{3,l}$  and  $h_{3,h}$  in Fig 1,a.

It was corrected.

43) Fig. 3: Should only contain the three root distributions used in this study.

- 10 Because we chose to set  $b = 2$ , it would be good the graphically see how  $b$  affects the curve.

# **Determination Benchmarking test of empirical parameters for root water uptake models**

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**Abstract.** Detailed physical models describing root water uptake (RWU) are an important tool for the prediction of RWU and crop transpiration, but involved hydraulic parameters are hardly-ever available, making them less attractive for many studies. Empirical models are more readily used because of their simplicity and lower data requirements. The purpose of this study is to evaluate the capability of some empirical models to mimic the RWU distribution under varying environmental conditions predicted from numerical simulations with a detailed physical model. A review of some empirical models used as sub-models in ecohydrological models is presented, and alternative empirical RWU models are proposed. The parameters of the empirical models are determined by inverse modelling of simulated depth-dependent RWU. The ~~simulated scenarios give more insight into the behaviour of the physical model, especially under wet soil conditions and high potential transpiration rate.~~ The performance of the empirical models and their optimized empirical parameters depend on the scenario. The largely used empirical RWU model by Feddes only performs well in scenarios with low root length density  $R$ , i.e. for the scenarios of low RWU “compensation”. For medium and high  $R$ , the Feddes RWU model cannot mimic properly the root uptake dynamics as predicted by the physical model. The RWU model by Jarvis provides good predictions only for low and medium  $R$  scenarios. For high  $R$ , the Jarvis model cannot mimic the uptake patterns predicted by the physical model. Incorporating a newly proposed reduction in the Jarvis model improved RWU predictions. Regarding the ability of the models in predicting plant transpiration, all models that accounts for compensation have good performance. The AIC information indicates that JMII, which has no empirical parameters to be estimated, is the “best model”. The proposed models are more capable of predicting similar RWU patterns by the physical model. The statistical indices point them as the best alternatives to mimic RWU predictions by the physical model.

## 1 Introduction

The rate at which a crop transpires depends on atmospheric conditions, the shape and properties of the boundary between crop and atmosphere, the root system geometry, and crop and soil hydraulic properties. The study and modelling of the involved interactions is motivated by the importance of transpiration for global climate and crop growth (Chahine, 1992) as well as by the role root water uptake (RWU) plays in soil water distribution (Yu et al., 2007). The common modelling approach introduced by Gardner (1960), referred to as microscopic or mesoscopic (Raats, 2007), is not readily applicable to practical problems due to the difficulty in describing the complex geometrical and operational function of [the](#) root system and its complex interactions with soil (Passioura, 1988). However, it gives insight into the process and allows developing upscaled- physical macroscopic models (De Willigen and van Noordwijk, 1987; Heinen, 2001; Raats, 2007; De Jong van Lier et al., 2008, 2013).

In many one- and two-dimensional problems, macroscopic RWU is modelled as a sink term in the Richards equation, whose dependency on water content or pressure head is usually represented by simple empirical functions (ex. Feddes et al. (1976, 1978); Lai and Katul (2000); Li et al. (2001); Vrugt et al. (2001); Li et al. (2006)). Most of these models are derived from the Feddes et al. (1978) model, which consists of partitioning potential transpiration over depth according to root length density and applying a stress reduction function of piecewise linear shape — defined by five threshold empirical parameters — to account for local uptake reduction. Results of experimental studies (Arya et al., 1975b; Green and Clothier, 1995, 1999; Vandoorne et al., 2012) and the development of physically based-models (De Jong van Lier et al., 2008; Javaux et al., 2008) have helped in understanding the mechanism of RWU as a non-local process affected by non-uniform soil water distribution (Javaux et al., 2013). Accordingly, a plant can increase water uptake in wetter soil layers in order to compensate for uptake reductions in dryer layers to keep transpiration rate at potential rate or mitigate transpiration reduction. Several empirical approaches have been developed over the years to account for this so-called compensation mechanism (Jarvis, 1989; Li et al., 2002, 2006; Lai and Katul, 2000). These models have been incorporated into larger hydrological models and tested at site-specific environments, showing improved predictions for, e.g., soil water content and crop transpiration (ex. Braud et al. (2005); Yadav et al. (2009); Dong et al. (2010)). Comparisons with physically-based models (Jarvis, 2011; de Willigen et al., 2012) implicitly accounting for compensation showed that models that do not account for compensation, like Feddes et al. (1978), are [under some circumstances \(e.g. high root length density\)](#) less accurate with respect to crop transpiration and soil water content predictions.

Recently, De Jong van Lier et al. (2013) developed a mechanistic model for predicting water potentials along the soil-root-leaf pathway, allowing the prediction of RWU and crop transpiration. This model was incorporated in the eco-hydrological model SWAP (Van Dam et al., 2008) by employing a piece-wise function between leaf pressure head and relative transpiration, reducing the number of empirical parameters compared to other relations (ex. Fisher et al. (1981)). Besides parameters describing soil hydraulic properties and root geometry, this new model requires information about root radial hydraulic conductivity, xylem axial conductance and a limiting leaf water potential. Although conceptually interesting, the difficulty to obtain the required input parameters makes the model less attractive for routine applications.



Other physical RWU models also exist varying from the simpler Couvreur et al. (2012) model but comparable to the De Jong van Lier et al. to more complex three-dimensional models (e.g. Javaux et al. (2013) ), which accounts for the full root architecture, requiring more input parameters and a higher computational effort. Specifically, the De Jong van Lier et al. (2013) differ from the previous mentioned models on the fact the RWU is based on matric flux potential with an equation derived from the microscopic RWU approach (De Jong van Lier et al., 2008) , whereas in other models RWU is based on water pressure head. Note that De Jong van Lier et al. (2013) model does not include the gravimetric potential, as this component is considered of minor importance in dry conditions. The osmotic potential is not included in current analysis, but straightforward be included in the model (see ? ).

Empirical RWU models are more readily used because of their relative simplicity and lower data requirements. On the other hand, their empirical parameters do not have a clear physical meaning and cannot be independently measured. Their limitations under varying environmental conditions are ~~quite incomprehensible and~~ not well established. For the case of the Feddes et al. (1978) transpiration reduction function, indeed, threshold values are available in literature (Taylor and Ashcroft, 1972; Doorenbos and Kassam, 1986) for some crops and some levels of transpiration demand. Nevertheless, experimental (Denmead and Shaw, 1962; Zur et al., 1982) and theoretical (Gardner, 1960; De Jong Van Lier et al., 2006) studies indicate that these parameters do not depend only on crop type and atmospheric demand, but are also determined by root system parameters and soil hydraulic properties. Furthermore, there are only ~~very a~~ few analyses of the validity of these values, and they cannot be used for other models (ex. the Jarvis (1989) model) due to differences in model concepts. Therefore, more accurate values for crops accounting for more environmental factors are necessary in order to apply these models in ~~wider a wider range of~~ scenarios. Due to the great number of models developed over the years, it is paramount to investigate some of these models before attempting to determine their parameters.

The general purpose of this study is to evaluate the capability of some empirical models to mimic the dynamics of RWU distribution under varying environmental conditions performed in numerical experiments with a detailed physical model (De Jong van Lier et al., 2013). The detailed physical model accounts for resistances from the soil to the leaf. We first review some empirical RWU models that have been employed in ecohydrological models and suggest some alternatives. By determining the parameters of the empirical models by inverse modelling of simulated depth-dependent RWU, it becomes clear to which extent the empirical models can mimic the dynamic patterns of RWU.

## 2 Theory

RWU and crop transpiration are linked through the continuity principle for water flow in the soil-plant-atmosphere pathway:

$$T_a = \int_{z_m} S(z) dz \quad (1)$$

where  $T_a$  (L) is the crop transpiration and  $S$  ( $L^3L^{-3}T^{-1}$ ) is the root water uptake, dependent on crop properties and soil hydraulic conditions, a function of soil depth  $z$  (L), and  $z_m$  (L) the maximum rooting depth. Eq. 1 neglects the change of water storage in the plant, which is justified for daily scale predictions, assuming that plants rehydrate to the same early morning water potentials on successive days (Taylor and Klepper, 1978).

- 5 In a macroscopic modelling approach, RWU is calculated as a sink term  $S$  in the Richards equation, which for the vertical coordinate is given by:

$$\frac{\partial \theta}{\partial t} = \frac{\partial}{\partial z} \left[ K(\theta) \left( \frac{\partial h}{\partial z} + 1 \right) \right] - S \quad (2)$$

where  $\theta$  ( $L^3 L^{-3}$ ) is the soil water content,  $h$  (L) the soil water pressure head,  $K$  ( $L T^{-1}$ ) the soil hydraulic conductivity,  $t$  (T) the time and  $z$  (L) the vertical coordinate (positive upward). To apply eq. 2, an expression for  $S$  is needed. Physical equations in analogy to Ohm's law have been suggested (see the review of Molz (1981) for examples) as well as expressions derived by upscaling microscopic models (De Willigen and van Noordwijk, 1987; Feddes and Raats, 2004; De Jong van Lier et al., 2008, 2013). Alternatively, simple empirical models requiring less information about plant and soil hydraulic properties have also been proposed and are more commonly used. Most of these models use the Feddes approach (Feddes et al., 1976, 1978), formulated as:

$$15 \quad S(z) = S_p(z)\alpha(h[z]) \quad (3)$$

where  $\alpha(h)$  is the RWU reduction function, defined by Feddes et al. (1978) as a piece-wise linear function of  $h$  (Fig. 1). According to this approach, a reduction in  $S$  due to  $\alpha(h[z]) < 1$  directly implies a transpiration reduction, making  $\alpha(h)$  to be called as transpiration reduction function.  $S_p$  is the potential RWU, which is determined by partitioning potential transpiration  $T_p$  over depth. Several ways to estimate  $S_p$  have been proposed (Prasad, 1988; Li et al., 2001; Raats, 1974; Li et al., 2006), but it is most common to distribute  $T_p$  according to the fraction of root length density  $R$  ( $L^3 L^{-3}$ ):

$$S_p(z) = \frac{R(z)}{\int_{z_m} R(z) dz} T_p = \beta(z) T_p \quad (4)$$

where  $\beta$  ( $L^{-1}$ ) is the normalized root length density.

Different functions to calculate  $\alpha$  have been suggested, normally considering  $\alpha$  a function of  $\theta$  (ex. Lai and Katul (2000); Jarvis (1989)), of  $h$  (ex. Feddes et al. (1978)) or of a combination of both (Li et al., 2006). [Using Comparing to  \$\theta\$ ,  \$h\$](#)  seems to be more feasible because of its relation to soil water energy and the fact that obtained parameters of such a function would be more likely applicable to different soils. Some reduction functions, generally associated to reservoir models for soil water balance, correlates RWU to the effective saturation. Regarding the shape of the reduction curve, they can be smooth non-linear functions constrained between wilting point and saturation or piece-wise linear functions, but they all have more than one empirical parameter. The parameters of the smooth non-linear functions allow easy curve fitting, whereas in the piece-wise

functions they stand for the threshold at which RWU (or crop transpiration) is reduced due to drought stress, which has been an important parameter in crop water management.

Metselaar and De Jong van Lier (2007) showed that for a vertically homogeneous root system the shape of  $\alpha$  is linearly related nor to soil water content neither to pressure head. A linear relation to the matric flux potential, a composite soil hydraulic function defined in eq. 5, is physically more plausible and was experimentally shown by Casaroli et al. (2010). Matric flux potential is defined as

$$M = \int_{h_w}^h K(h) dh \quad (5)$$

where  $h_w$  is the soil pressure head at wilting point. Accordingly, a more suitable expression for  $\alpha$  would be a piece-wise linear function of  $M$  (Fig. 1). RWU can then be calculated by the Feddes model (eq. 3) by replacing its reduction function for water deficit by the alternative illustrated in Fig. 1.

## 2.1 Physically based root water uptake model

By upscaling earlier findings (De Jong Van Lier et al., 2006; Metselaar and De Jong van Lier, 2007) of water flow towards a single root in the microscopic scale disregarding plant resistance to water flow, De Jong van Lier et al. (2008) derived the following expression for  $S$ :

$$S(z) = \rho(z)(M_s(z) - M_0(z)) \quad (6)$$

where  $M_s$  is the bulk soil matric flux potential,  $M_0$  the value of  $M$  at root surface and  $\rho(z)$  ( $L^{-2}$ ) a composite parameter, depending on  $R$  and root radius  $r_0$ :

$$\rho(z) = \frac{4}{r_0^2 - a^2 r_m^2(z) + 2[r_m^2(z) + r_0^2] \ln[ar_m(z)/r_0]} \quad (7)$$

where  $r_m (= \sqrt{1/\pi R})$  (L) is the rhizosphere radius — defined as the half distance between neighbouring roots— and  $a$  the relative distance from  $r_0$  to  $r_m$  where water content equals bulk soil water content. In De Jong van Lier et al. (2013), this model is extended by taking into account the hydraulic resistances to water flow within the plant. Dividing water transport within the plant into two physical domains (from root surface to root xylem to leaf), assuming no water changes within the plant tissue and by coupling eq. 6 for water flow within the rhizosphere, they derived the following expression relating water potentials and  $T_a$ :

$$h_0(z) = h_l + \varphi(M_s(z) - M_0(z)) + \frac{T_a}{L_l} \quad (8)$$

where  $h_0$  and  $h_l$  (L) are the pressure heads at the root surface and leaf, respectively, and  $L_l$  ( $T^{-1}$ ) is the overall conductance over the root-to-leaf root xylem-to-leaf pathway. Notice that  $S$  can be calculated by eq. 6 upon solving eq. 8.  $\varphi$  ( $T L^{-1}$ ) is

defined as:

$$\varphi(z) = \frac{\rho r_m^2(z) \ln \frac{r_0}{r_x}}{2K_{root}} \quad (9)$$

where  $K_{root}$  ( $L T^{-1}$ ) is the radial root tissue conductivity (from root surface to root xylem) and  $r_x$  (L) the xylem radius.  $T_a$  is a function of  $h_l$ , which was defined piece-wisely by imposing a limiting value  $h_w$  on  $h_l$ :

$$T_r = \begin{cases} 1 & : h_l > h_{wl} \\ 0 \leq T_r \leq 1 & : h_l = h_{wl} \\ 0 & : h_l < h_{wl} \end{cases} \quad (10)$$

where  $T_r$  ( $= T_a/T_p$ ) is the relative crop transpiration. Crop water stress, a condition for which  $T_a < T_p$ , is defined at the crop level (Tardieu, 1996) and onsets when  $h_l = h_w$ . Because  $T_a$  and  $h_l$  are unknowns, eq. 8 and 10 cannot be solved analytically directly, but an efficient numerical algorithm is described in De Jong van Lier et al. (2013), along with a particular analytical solution for Brooks and Corey (1964) soils.

- 10 Fig. 2 helps to understand how RWU is distributed over depth.  $h_l$  can be regarded as a crop level measure of water deficit stress over the whole root zone: as soil gets drier,  $h_l$  is reduced, which increases the driving force for RWU (see RWU for the several values of  $h_l$  in Fig. 2). As soil pressure head  $h_s$  decreases, high uptakes are only achieved by lower  $h_l$ . For a certain  $h_l$  value, RWU is substantially reduced as  $h_s$  decreases. If  $h_l$  is not reduced as  $h_s$  gets lower,  $S$  becomes negative (negative  $S$  is not shown in Fig. 2, but it is part of an extension of each curve) and water will flow from root to soil, a phenomena called hydraulic lift or hydraulic re-distribution (Jarvis, 2011) Ref#1, point 4.
- 15 hydraulic lift or hydraulic re-distribution (Jarvis, 2011) Ref#1, point 4. This situation occurs when parts of the root zone are wetter and RWU from these parts satisfies transpiration demand, and  $h_l$  is not reduced.

- Fig. 2 also shows that RWU is sensitive to both  $R$  and  $h_s$ , and that it can be locally balanced by the  $R$  and soil water content. Under homogeneous soil water distribution, RWU is partitioned proportionally to  $R$ . For non-homogeneous-heterogeneous conditions, RWU for lower  $R$  can be the same as for higher  $R$  depending on the stress level (indicated by  $h_l$ ) and the  $h_s$  (see
- 20 Fig. 2). This is in agreement with experimental results reported by several authors (Arya et al., 1975b, a; Green and Clothier, 1995; Verma et al., 2014) who found less densely-rooted but wetter parts of the root zone to correspond to a significant portion of RWU when more densely-rooted parts of the soil are drier, allowing the crop to maintain transpiration at potential rates. Due to empirical model concepts that employ only  $R$  for predicting RWU distribution over depth (for nonstressed conditions), these results have been interpreted as due to a mechanism labelled “compensation” by which uptake is “increased” from wetter
- 25 layers to compensate the “reduction” in the drier layers (Jarvis, 1989; Šimůnek and Hopmans, 2009). Clearly, this compensation concept is based on a reference RWU distribution based on  $R$  and is only relevant it only needs to be explicitly addressed in empirical models. In physical models, discriminating compensation becomes less important is not necessary since in such models “compensation” follows implicitly from the RWU mechanism Ref#1, point 5.

In order to account for RWU pattern changes due to heterogeneous soil water distribution (the so-called “compensation”), several empirical models have been developed over the years. These models follow the general framework of the Feddes et al. (1978) model given by eq. 3. Below we review these models and present a new empirical alternative.

## 2.2 Empirical root water uptake models accounting for compensation

### 5 2.2.1 The Jarvis (1989) model

Jarvis (1989) defined a weighted-stress index  $\omega$  ( $0 \leq \omega \leq 1$ ) as

$$\omega = \int_{z_m} \alpha(z)\beta(z)dz. \quad (11)$$

where, differently from Feddes et al. (1978),  $\alpha$  was defined as a function of the effective saturation. ~~In principle, any definition of  $\alpha$  is applicable in eq. 11, and in this paper we will refer to the Feddes et al. (1978) reduction function unless mentioned~~ <sup>Ref#1, point 6</sup>.

10 Whereas Feddes et al. (1978) assume the RWU reduction directly to reflect in crop transpiration reduction, the Jarvis (1989) approach employs a so-called “whole-plant stress function” given by:

$$\frac{T_a}{T_p} = \min\left\{1, \frac{\omega}{\omega_c}\right\} \quad (12)$$

where  $\omega_c$  is a threshold value of  $\omega$  for the transpiration reduction. Substituting eq. 3 and 4 into eq. 1 (the continuity principle) and combining with eq. 12, results in:

$$15 \quad S(z) = S_p\alpha(z)\alpha_2, \text{ where } \alpha_2 = \frac{1}{\max\{\omega, \omega_c\}} \quad (13)$$

where  $\alpha_2$  is called the compensation factor of RWU, distinct from the Feddes model (eq. 3) and which can be derived by defining  $T_a$  by eq. 12. In the Jarvis (1989) model,  $\alpha$  accounts for local reduction of RWU and transpiration reduction is computed by eq. 12. When  $\omega = 1$ , there is no RWU reduction ( $\alpha = 1$  throughout the root zone) and the model prediction is equal to the Feddes model. For  $\omega_c < \omega < 1$ , uptake is reduced in some parts of the root zone (as computed by  $\alpha < 1$ ) but the plant can still achieve potential transpiration rates by increasing RWU over the whole root zone by the factor  $\alpha_2$ . When  $\omega < \omega_c$ , the uptake is still increased by the factor  $\alpha_2$  but the potential transpiration rate cannot be met. The threshold value  $\omega_c$  places a limit on the plant’s ability to deal with soil water stress. When  $\omega_c$  tends to zero, eq. 12 tends to 1, and the plant can fully compensate uptake and transpire at the potential rate provided that  $\alpha > 0$  at some position within the root zone.

~~An analogy to stomata functioning is described by~~

25 ~~In principle, any definition of  $\alpha$  is applicable in eq. 12 (Jarvis, 1989, 2011), putting this model in a more physical context. However, operational and physical limitations of this model have been raised (Skaggs et al., 2006; Javaux et al., 2013). The model introduces an additional parameter ( $\omega_c$ ), which should be determined by inverse modelling and is dependent on atmospheric~~

demand, rooting properties (usually related to root length density) and soil type. Another difficulty is the conceptual limitation raised by Skaggs et al. (2006), who showed that the model does not mimic compensation properly and affronts the definition of  $\alpha$ , as can be noticed by analysing eq. 13: RWU is reduced by  $\alpha$ , but increased by the factor  $1/\max[\omega, \omega_c]$ , making the interpretation of  $\alpha$  obscure. Another limitation is the linking of compensation to crop stress, making it to fail in predicting compensation under wet condition with a heterogeneous soil pressure head distribution (Javaux et al., 2013).

Using the piece-wise linear Feddes reduction function for  $\alpha$ , care must be taken [11](#), and usually the Feddes et al. (1978) reduction function is used instead of the original Jarvis (1989) reduction function, as it is used in HYDRUS model (Simunek et al., 2009) for instance. This modified version of Jarvis (1989) model, hereafter named JMf, will be further analysed [Ref#1, point 6](#). Nevertheless, [one should be careful](#) in setting up and interpreting the threshold parameters of [this function JMf](#) [Ref#1, point 8](#). The Feddes et al. (1978) model does not account for compensation, and the threshold pressure head value below which RWU is reduced ( $h_3$ ) also represents the value below which transpiration is reduced, making  $h_3$  values from literature usually to refer to this interpretation. [Comparing to the Jarvis model, Instead, at the JMf](#) the transpiration reduction only takes place when  $\omega < \omega_c$ , and soil pressure head in some layers is already supposed to be more negative than  $h_3$ , which means that  $h_3$  in [Jarvis \(1989\) model JMf](#) is less negative than the equivalent in the Feddes model. In that sense,  $h_3$  for the [Jarvis \(1989\) model JMf](#) is hard to determine experimentally. Inverse modelling by optimizing outcomes of soil water flow models with measured values of field experiments is an option.

[The Jarvis-type model, defined by eq. 11 to 13 with using any  \$\alpha\$ , has been well criticized \(Skaggs et al., 2006; Javaux et al., 2013\).](#) Nevertheless, [this model can to a certain extent be compared to the De Jong van Lier et al. \(2008\) physical model as shown by Jarvis \(2011\), which is shortly described below.](#)

## 20 Comparison to the De Jong van Lier et al. (2008) model

The Jarvis (1989) model was shown to be “[numerically conceptual](#)” identical to De Jong van Lier et al. (2008) physical model, but only under limiting hydraulic conditions (Jarvis, 2010, 2011). We briefly review this similarity and its implications on the empirical concept of the Jarvis (1989) model.

De Jong Van Lier et al. (2006) derived eq. 6 for describing RWU. Crop transpiration is obtained by integrating eq. 6 over  $z_m$  as defined in eq. 1, leaving two unknowns:  $M_0$  and  $T_a$ . In order to solve for these, De Jong van Lier et al. (2008) defined  $T_a$  as a piece-wise function as follows:

$$\frac{T_a}{T_p} = \min \left\{ 1, \frac{T_{p_{\max}}}{T_p} \right\} \quad (14)$$

where  $T_{p_{\max}}$  ( $L T^{-1}$ ) is the maximum possible transpiration rate attained when  $M_0 = 0$ , given by:

$$T_{p_{\max}} = \int_{z_m} \rho(z) M(z) dz. \quad (15)$$

From eq. 14 when  $T_{p_{\max}} < T_p$ , drought stress occurs and  $T_a = T_{p_{\max}}$ . Under this condition, pressure head at the root surface reaches  $h_w \rightarrow M_0 = 0$  and  $S(z)$  becomes:

$$S(z) = \rho(z)M(z). \quad (16)$$

When  $T_{p_{\max}} > T_p$ ,  $T_a = T_p$  (no drought stress) and  $M_0 (> 0)$  is given by:

$$5 \quad M_0 = \frac{\int_{z_m} \rho(z)M(z)dz - T_p}{\int_{z_m} \rho(z)dz} \quad (17)$$

Jarvis (2011) observed the similarities between eq. [14] and [12] of the models. Notice also the algebraic similarity between  $\omega$  (eq. 11) and  $T_{p_{\max}}$  (eq. 15). Thus, Jarvis (2010) showed that both models provide the same results for the stressed phase if  $\alpha$  and  $\beta(z)$  are defined as follows:

$$\alpha = \frac{M}{M_{max}} \quad (18)$$

10

$$\beta = \frac{\rho(z)}{\int_{z_m} \rho(z)dz} \quad (19)$$

where  $M_{max}$  is the maximum value of  $M$  (i.e., at  $h = 0$ ). By substituting eq. [18] and [19] into eq. 15 and comparing eq. 12 with eq. 14,  $\omega_c$  is found to be equal to:

$$\omega_c = \frac{T_p}{M_{max} \int_{z_m} \rho(z) dz} \quad (20)$$

15 Substitution of eq. [18] to [20] into eq. [12] and [11] results in eq. 16 of De Jong van Lier et al. (2008) model for stressed condition. Consequently, both models provide the same numerical results. For unstressed condition, analogous substitution results in:

$$S(z) = \rho(z)M(z) \frac{T_p}{T_{p_{max}}} = \frac{\rho(z)M(z)}{\int_{z_m} \rho(z)M(z) dz} T_p \quad (21)$$

Eq. 21 is different from eq. 6 and, therefore, the models cannot be correlated for these conditions. The Jarvis (1989) model  
20 predicts RWU by a weighting factor between  $\rho$  and  $M$  throughout rooting depth. Defining  $\alpha$  and  $\beta$  by eq. 18 and 19, respectively, allowed to correlate both models only for stressed conditions. These definitions and the resulting model will be further analysed.



### 2.2.2 The Li et al. (2001) model

Li et al. (2001) proposed to distribute potential transpiration over the root zone by a weighted stress index  $\zeta$ , being a function of both root distribution and soil water availability:

$$\zeta(z) = \frac{\alpha(z)R(z)^{l_m}}{\int_{z_m} \alpha(z)R(z)^{l_m} dz} \quad (22)$$

5 where  $\alpha(-)$  and  $R$  ( $L L^{-3}$ ) were previously defined and the exponent  $\lambda^{l_m}$  is an empirical factor that. Originally, the  $l_m$  values were based on experimental works, but in principle it modifies the shape of RWU distribution over depth. The smaller  $\lambda$ , the more water is taken up in deeper soil layers. For  $0 < l_m < 1$ , the RWU in sparsely rooted soil layers is increased in the attempt to mimic compensation. For  $l_m > 1$ , which has no maximum, the uptake in more densely rooted soil layers increases. Thus,  $S_p$  is given by:

$$10 \quad S_p = \zeta(z)T_p \quad (23)$$

and RWU is calculated by substituting eq. 23 into eq. 3, following the Feddes approach.

Defining  $S_p$  as function of root length density and soil water availability distribution is an alternative to the Jarvis (2011) model. Compensation is directly accounted for by the weighted stress index in eq. 22. However, the choice of  $\alpha$  to represent soil water availability in eq. 22 does not mimic properly the compensation mechanism. Compensation may take place before transpiration reduction. Using  $\alpha$  in eq. 22 means that compensation will only take place after the onset of transpiration reduction when  $\alpha$  in one or more layers is less than unity. The  $\lambda^{l_m}$  parameter may also be interpreted as to account for compensation under non-stressed condition. Compensation, however, and shape of RWU distribution are likely to change as soil dries. A constant  $\lambda^{l_m}$  can not account for that.

### 2.2.3 The Molz and Remson (1970) and Selim and Iskandar (1978) models

20 Decades before Li et al. (2001), Molz and Remson (1970) and Selim and Iskandar (1978) had already suggested to distribute potential transpiration over depth according to root length density and soil water availability. Instead of using  $\alpha$  to account for soil water availability, they used soil hydraulic functions. The weighted stress index was defined as

$$\zeta(z) = \frac{\Gamma(z)R(z)}{\int_{z_m} \Gamma(z)R(z)dz} \quad (24)$$

where  $\Gamma$  is a soil hydraulic function to account for water availability. Molz and Remson (1970) used soil water diffusivity  $D$  ( $L^2 T^{-1}$ ), and Selim and Iskandar (1978) used soil hydraulic conductivity  $K$  ( $L T^{-1}$ ) for  $\Gamma$  in eq. 24. RWU is then calculated by substituting eq. 24 into eq. 23 and then into eq. 3 following the Feddes approach.

These models may better represent RWU and compensation than the Li et al. (2001) model. The compensation is implicitly accounted for by means of  $\Gamma$  in  $\zeta$ . ~~In drier soil layers, Since  $\Gamma$  is reduced, whereas in wetter soil layers  $\Gamma$  is increased, thus increasing RWU in these layers~~ decreases as soil dries out, in a heterogeneous soil water distribution  $\zeta$  in wetter layers is relatively increased because the overall  $\int \Gamma R dz$  is reduced due to the reduction of  $\Gamma$  in drier, more densely rooted soil layers.

- 5 Differently from Li et al. (2001) model, this change in RWU distribution can occur before the onset of transpiration reduction. Heinen (2014) compared different types of  $\Gamma$  in eq. 24 such as the relative hydraulic conductivity ( $K_r = K/K_{sat}$ ), relative matric flux potential ( $M_r = M/M_{max}$ ) and others. He found that using different forms of  $\Gamma$  provides very different patterns of RWU, but did not indicate a preference for a specific one.

## 2.2.4 Proposed empirical model

- 10 In describing soil water availability, the matric flux potential  $M$  may be a better choice than  $K$  or  $D$ , since it integrates  $K$  and  $h$  or  $D$  and  $\theta$  (Raats, 1974; De Jong van Lier et al., 2013). We propose a new weighted stress index, defined as:

$$\zeta_m(z) = \frac{R^{l_m} M(h)}{\int_{z_m} R^{l_m} M(h) dz} \quad (25)$$

- The exponent  ~~$\lambda$~~   $l_m$  provides additional flexibility on distribution of  $T_p$  over depth as was shown by Li et al. (2001). The proposed model differs from Li et al. (2006) only on the hydraulic property to account for soil water availability. The  $\alpha$  function used in Li et al. (2006) can not alter RWU distribution before transpiration reduction, as commented earlier. Whereas,  $M$  accounts for compensation before transpiration reduction, while it integrates ingrates the effects of both  $K$  and  $h$ .

The RWU can then be obtained by inserting eq. 25 into eq. 23 ( $S_p$ ) and multiplied by any reduction function, such as the Feddes et al. (1978) and proposed reduction functions. In other words, it follows the Feddes approach, which computes RWU by the two mentioned steps, differing only how  $S_p$  is obtained: eq. 25 (times  $T_p$ ) versus eq. 4.

- 20 **2.2.5 Relationship between plant transpiration empirical parameters**

This was suggested by the Referee#2. I have just started this and I will be brief. Although I am in doubt whether this is really necessary (See Point i).

### 3 Material and Methods

#### 3.1 Applied models

Table 1 summarizes the empirical RWU models evaluated in this study. They all follow the basic Feddes model (eq. 3), but ~~diverging~~ differing on how RWU is partitioned over rooting depth or how  $\alpha$  is defined. For each model, except for Jarvis (2010), we defined a modified version by substituting the Feddes reduction function by the proposed reduction function (Fig. 1b), and these modified versions were also evaluated. The threshold values of the Feddes et al. (1978) reduction function for anoxic conditions ( $h_1$  and  $h_2$ ) were set to zero. The value of the parameter  $h_4$  was set to  $-150$  m. The other parameters of the models were obtained by optimization as described in section 3.3.

All these models were embedded as sub-models into the ecohydrological model SWAP (Van Dam et al., 2008) in order to solve eq. 2 and to apply it for all kind of soil water flow conditions. Different scenarios of root length density, atmospheric demand and soil type (described in section 3.2) were set up in order to analyse the behaviour and sensitivity of the models. Simulation results of SWAP in combination with each of the RWU models were compared to the SWAP predictions ~~when combined to in~~ combination with the physical RWU model developed by De Jong van Lier et al. (2013).

The values of the De Jong van Lier et al. (2013) model parameters used in the simulations are listed in Table 2. The values of  $K_{root}$  and  $L_l$  are within the range reported by De Jong van Lier et al. (2013).

#### 3.2 Simulation scenarios

##### 3.2.1 Drying-out simulation

Boundary conditions for these simulations were no rain/irrigation and a constant atmospheric demand over time. The simulation continued until simulated crop transpiration by the physical RWU model approached zero. Soil evaporation was set to zero making the soil to dry out only due to RWU or drainage at the bottom. Free drainage (unit hydraulic gradient) at the maximum rooting depth was the bottom boundary condition. The soil was initially in hydrostatic equilibrium with a water table located at 1 m depth. We performed simulations for two levels of atmospheric demand given by potential transpiration  $T_p$ : 1 and 5 mm d<sup>-1</sup>. We also considered three types of soil and three levels of root length density, as described in the following.

##### 3.2.2 Soil type

Soil ~~date~~ data for three top soils from the Dutch Staring series (Wösten et al., 1999) were used. The physical properties of these soils ~~are~~ are described by the Mualem-van Genuchten functions (Mualem, 1976; Van Genuchten, 1980) for the  $K - \theta - h$

relations:

$$\Theta \approx [1 + |\alpha h|^n]^{(1/n)-1} \quad (26)$$

$$K \approx K_{sat} \Theta^\lambda [1 - (1 - \Theta^{n/(n-1)})^{1-(1/n)}]^2 \quad (27)$$

5 where  $\Theta = (\theta - \theta_r) / (\theta_s - \theta_r)$ ;  $\theta$ ,  $\theta_r$  and  $\theta_s$  are water content, residual water content and saturated water content ( $L^3 L^{-3}$ ), respectively;  $h$  is pressure head (L);  $K$  and  $K_{sat}$  are hydraulic conductivity and saturated hydraulic conductivity, respectively ( $L T^{-1}$ ); and  $\alpha$  ( $L^{-1}$ ),  $n$ , and  $\lambda$  are empirical parameters. The parameter values for the three soils are listed in Table 3. These soils are identified in this text as clay, loam and sand (Table 3).

### 3.2.3 Root length density distribution

Three levels of root length density were used, according to the range of values normally found in the literature. We considered low, medium and high root length density for average crop values equal to 0.01, 0.1 and 1.0  $cm\ cm^{-3}$ , respectively. For all cases, we set the maximum rooting depth  $z_{max}$  equal to 0.5 m. Root length density over depth  $z$  was described by the exponential function:

$$R(z_r) = R_0(1 - z_r) \exp^{-bz_r} \quad (28)$$

15 where  $R_0$  ( $L\ L^{-3}$ ) is the root length density at the soil surface,  $b$  (-) is a shape-factor parameter and  $z_r$  ( $= z/z_{max}$ ) is the relative soil root depth. The term  $(1 - z_r)$  in eq. 28 guarantees that root length density is zero at the maximum rooting depth. The parameter  $R_0$  is hardly ever determined, whereas the average root length density of crops  $R_{avg}$  is usually reported in the literature. Assuming  $R$  of such a crop given by eq. 28, it can be shown that:

$$\int_0^1 R_0(1 - z_r) \exp^{-bz_r} dz_r = R_{avg} \quad (29)$$

Solving eq. 29 for  $R_0$  and substituting into eq. 28 gives:

$$20 \quad R(z_r) = \frac{b^2 R_{avg}}{b + \exp^{-b} - 1} (1 - z_r) \exp^{-bz_r} \quad (b > 0) \quad (30)$$

Fig. 3 shows  $R(z_r)$  calculated from eq. 30 for different values of  $b$  and  $R_{avg} = 1\ cm\ cm^{-3}$ . As  $b$  approaches zero, eq. 30 tends to become linear, however it is not defined for  $b = 0$ . In our simulations  $b$  was arbitrarily set equal to 2.0.

### 3.3 Optimization

The parameters of the empirical RWU models were estimated by solving the following constrained optimization problem:

$$\begin{aligned} \text{minimize} \quad & \Phi(\mathbf{p}) = \sum_{i=1}^n \sum_{j=1}^m [S_{i,j}^* - S_{i,j}(\mathbf{p})]^2 \\ \text{subject to} \quad & \mathbf{p} \in \Omega \end{aligned} \tag{31}$$

where  $\Phi(\mathbf{p})$  is the objective function to be optimized/minimized,  $S_{i,j}^*$  is the RWU simulated by SWAP model together with the De Jong van Lier et al. (2013) model at time  $i$  (time interval of one day) and depth  $j$  (of each soil layer) and  $S_{i,j}(\mathbf{p})$  is the corresponding RWU predicted by SWAP in combination with one of the empirical models shown in Table 1.  $\mathbf{p}$  is the model parameter vector to be optimized, constrained in the domain  $\Omega$ . Both  $\mathbf{p}$  and  $\Omega$  vary depending on the empirical RWU model used. Table 4 shows the parameters of each empirical RWU model that were optimized and their respective constraints  $\Omega$ .  $m$  and  $n$  are the number of soil layers (50 soil layers of 1 cm thickness) and days of the simulation, respectively. The Jarvis (2010) model has no empirical parameters and therefore requires no optimization.

Eq. 31 was solved by using the PEST (Parameter ESTimation) tool (Doherty et al., 2005) coupled to the adapted version of SWAP. PEST is a non-linear parameter estimation program that solves eq. 31 by the Gauss-Levenberg-Marquardt (GLM) algorithm, searching for the deviation, initially along the steepest gradient of the objective function and switching gradually the search to Gauss-Newton algorithm as the minimum of the objective function is approached. Upon setting PEST parameters we made reference runs of SWAP with each empirical model using random values of  $\mathbf{p}$  and assessed the ability of PEST for retrieving  $\mathbf{p}$ . These reference runs served to set up properly PEST for our case. For high-highly non-linear problems as the one in eq. 31 GLM, the optimized parameters set depends on the initial values of  $\mathbf{b}$ . We used five random sets of initial values for  $\mathbf{p}$  in order to guarantee that GLM found the global minimum and also to check the uniqueness of the solution. Mostly these runs led to the same minimum. In the case it did not happen, we compared the minimum and made the fitting runs again.

The optimizations were performed for the drying-out simulation only. This guaranteed that RWU predictions from SWAP corresponded to the best fit of each empirical models to the De Jong van Lier et al. (2013) model. This analysis aimed to investigate the capacity of the empirical RWU models to mimic the RWU pattern predicted by the De Jong van Lier et al. (2013) model. These optimized parameters were subsequently used to evaluate the models in an independent growing season scenario.

### 3.3.1 Growing season simulation

## 3.4 Growing season simulation

The models were evaluated by simulating the transpiration of grass with weather data from the De Bilt weather station, the Netherlands (52°06' N; 5°11 'E), for the year 2006. The same root system distribution as in the drying-out simulations was used, i.e. a crop with roots exponentially distributed over depth as eq. 30 ( $b = 2.0$ ) down to 50 cm below soil surface. We also performed simulations for the same three types of soils and root length densities. In all cases the crop fully covered the soil with a leaf area index of 3.0. Daily reference evapotranspiration  $ET_0$  was calculated by SWAP using the FAO Penman-Monteith method (Allen et al., 1998). In SWAP model, a potential crop evapotranspiration  $ET_p$  is obtained by multiplying  $ET_0$  by a crop factor, which for the grass vegetation was set to 1 (Van Dam et al., 2008).  $ET_p$  was partitioned into potential evaporation  $E_p$  and  $T_p$  using parameter values for common crops given in SWAP model (see Van Dam et al. (2008) for details).

The values of the empirical parameters of each RWU model corresponding to the type of soil and root length density were taken from the optimizations performed in the drying-out experiment. Each parameter was estimated for two levels of  $T_p$  (1 and 5 mm d<sup>-1</sup>) and was linearly interpolated for intermediate levels of  $T_p$ . For  $T_p > 5$  mm d<sup>-1</sup> or  $T_p < 1$  mm d<sup>-1</sup>, the values estimated for these highest or lowest  $T_p$  values were used.

The bottom boundary condition was the same as in the drying-out simulations (free drainage). Initial pressure heads were obtained by iteratively running SWAP starting with the final pressure heads of the previous simulation until convergence.

## 4 Results and Discussion

### 4.1 Drying-out simulation

#### 4.1.1 Root water uptake pattern: De Jong van Lier et al. (2013) model

In this section we first focus on the behaviour of the De Jong van Lier et al. (2013) model in predicting RWU for the evaluated scenarios in the drying-out experiment. Fig. 4 shows the RWU patterns for the case of clay soil for the three evaluated root length densities  $R$  and the two levels of potential transpiration  $T_p$ . It can be seen how  $R$  and  $T_p$  affect RWU distribution and transpiration reduction as soil dries out. The onset and shape of transpiration reduction is affected by the RWU pattern. For low  $R$ , the low amount of roots in deeper layers is not sufficient to supply high RWU rates. When the upper layers become drier, transpiration reduction follows immediately. Under medium and high  $R$ , the RWU front moves gradually downward as water from the upper layers is depleted. For high  $R$ , the RWU front goes even deeper compared to medium  $R$ , and transpiration is sustained at potential rates for longer time (Fig. 4). Accordingly, the plant exploits the whole root zone and little water is left

when transpiration reduction onsets, causing an abrupt drop in transpiration. Regarding  $T_p$ , the RWU patterns are very similar for both evaluated rates, differing only in time scale: for high  $T_p$  the onset of transpiration reduction and the shift in RWU front occur earlier. The patterns for the sand and loam soil (not shown here) show very similar features. However, for sand soil transpiration prolonged a bit longer at potential rates and more water was extracted at deeper layers. Whereas, for loam soil, the onset of transpiration reduction started earlier.

The leaf pressure head  $h_l$  over time shown in Fig. 4 illustrates how the model adapts  $h_l$  to  $R$  and  $T_p$  levels and soil drying. Initially all scenarios have the same water content distribution and lower  $h_l$  values are required for low  $R$  or high  $T_p$  scenarios to supply potential transpiration rates. As soil becomes drier,  $h_l$  is decreased in order to increase the pressure head gradient between bulk soil and root surface and thus maintaining RWU corresponding to the potential demands. Therefore, uptake in wetter layers become more important. Transpiration reduction only onsets when  $h_l$  reaches the limiting leaf pressure head  $h_{wl}$  ( $= -200$  m), after significant changes in the RWU patterns, characterized by increased uptake in deeper layers.

For the high  $T_p$ -low  $R$  scenarios, transpiration reduction starts at the first day of simulation although the soil is relatively wet. This is a case of transpiration reduction under non-limiting soil hydraulic conditions due to high atmospheric demand (Cowan, 1965). For such conditions, the high water flow within the plant required to ~~attend~~meet the atmospheric demand cannot be supported by the root system with a low  $R$  and hydraulic parameters given in Table 2. Higher atmospheric demand (here represented by  $T_p$ ) ~~increases the~~leads to faster reduction of  $h_l$  caused by the hydraulic resistance to water flow within the plant, and the transpiration rate and RWU are a function of  $h_l$ . The physical model assumes a parsimonious relationship (eq. 10) between transpiration and  $h_l$ : transpiration rate is only reduced when  $h_l$  reaches a limiting value  $h_{wl}$ , which corresponds to a maximum possible transpiration rate  $T_{p,max}$  allowed by the plant for the current soil hydraulic and atmospheric conditions. Under non-limiting soil hydraulic conditions,  $T_{p,max}$  is a function of root system properties and plant hydraulic parameters only (Table 2). Fig. 5 shows  $T_{p,max}$  as a function of  $K_{root}$  for some values of  $L_l$  with a constant soil pressure head in the root zone of -1 m for the low  $R$  in the sandy soil. It can be seen that  $K_{root}$  is limiting the crop transpiration and that  $L_l$  becomes important only when  $K_{root}$  increases. The potential transpiration can be achieved by raising  $K_{root}$  up to about  $10^{-7}$  m d<sup>-1</sup>. This can also be achieved by decreasing  $h_{wl}$  (not shown in Fig. 5).

In the field, transpiration rate and root length density are related to each other: a high transpiration rate only occurs at high leaf area and a high leaf area implies a high root length density. Thus, even in very dry and hot weather conditions, a crop with a low  $R$  may not be able to realize high transpiration. Furthermore, crop transpiration depends on the stomatal conductance. In the De Jong van Lier et al. (2013) model, this is implicitly taken into account by the simple relationship between  $h_l$  and  $T_a$ . However, stomatal conductance is relatively complex and depends on several environmental factors such as air temperature, solar radiation and CO<sub>2</sub> concentration. Thus, high potential transpiration rate may not be achieved because of the stomatal conductance reduction due to temperature or solar radiation. These results can be enhanced by the coupling of the De Jong van Lier et al. (2013) model to stomatal conductance models, such as the Tuzet et al. (2003) model.



## 4.1.2 Root water uptake pattern predicted by the empirical models

In this section, we evaluate the empirical RWU models (models and their abbreviations are listed in Table 1) based on the comparison of RWU patterns and transpiration reduction over time with the respective predictions from the De Jong van Lier et al. (2013) model (VLM). All empirical model predictions are performed with respective optimized parameters as shown in Table 5 and are discussed in section 4.1.4, thus representing the best fit with VLM.

The RWU patterns simulated by VLM and the empirical models for the scenario of sandy soil and high  $R$  are shown in Fig. 6 and 7 for low and high  $T_p$ , respectively. Both versions of Feddes model (FM and FMm) predicted enhanced RWU from the upper soil layers. When the soil pressure head ( $h_s$ ) (for FM) or soil matric flux potential ( $M_s$ ) (for FMm) is greater than the threshold value for uptake reduction, these uptake patterns are equivalent to the vertical  $R$  distribution. For conditions drier than the threshold value (when  $\alpha_f$  and  $\alpha_m$  are less than 1), the predicted RWU patterns by the models become different (Fig. 6 and 7).

After a period of reduced RWU, the length of which depends on  $R$ ,  $T_p$  and  $h_3$ , RWU from the upper soil layers predicted by FM rapidly decreases to zero. This zero-uptake zone expands downward as soil dries out. On the other hand, the uptake predicted by FMm is substantially reduced right after the onset of transpiration reduction, proceeding at lower rates and a much longer time until approaching zero. These features become evident by comparing the shape of both reduction functions (Fig. 8).  $\alpha_m$  is linear with  $M$  after  $M > M_c$ , but it is concavely-shaped as a function of  $h$  — as also shown by Metselaar and De Jong van Lier (2007) and De Jong van Lier et al. (2009). Thus,  $\alpha_m$  is abruptly reduced for  $M > M_c$ , causing substantial reduction in RWU even when  $h$  is slightly below the threshold value. Therefore, RWU proceeds at low rates for longer time. Conversely, due to the linear shape of  $\alpha_f$ , RWU predicted by FM remains higher for a longer time after  $h < h_3$ . No abrupt change in RWU patterns is predicted by this model, especially when  $T_p$  is low (Fig. 6). When  $h$  comes close to  $h_4$ ,  $\alpha_f$  is still relatively high and RWU continues, making  $h$  to rapidly approach  $h_4$ . Another diverging feature between  $\alpha_f$  and  $\alpha_m$ , also shown in Fig. 8, is that the shape of  $\alpha_m$  varies with soil type (regardless the value of its threshold parameter  $M_c$ ), whereas  $\alpha_f$  does not. These different features of the reduction functions also affect the matching values of the parameters as discussed below. The choice of the reduction function, however, affects transpiration curve over time only slightly, but RWU patterns are strongly affected (Fig. 6 and 7).

The RWU patterns predicted by ~~JM~~-JMf and JMm models can be very different, as shown by Fig. 6 for the high  $R$ -low  $T_p$  scenario. In fact, the ~~JM~~-JMf model did not predict any compensation at all because the optimal  $\omega_c$  was equal to unity (Table 5) — thus becoming identical to FM — and the optimal  $h_3$  for ~~JM~~-JMf and FM were similar. In Fig. 6, although  $h_3$  values for FM and JMf ( $\omega_c = 1$ ) are close to zero, the plant transpiration is close to  $T_p$  for a prolonged time due to a small reduction of  $\alpha$ . These high  $R$ -low  $T_p$  scenarios with a high  $R$  in deep soil layers allow RWU at higher rates when surface soil layers becomes drier (as predicted by VLM). Then, reducing  $\omega_c$  in an attempt to predict compensation with ~~JM~~-JMf makes RWU pattern to deviate even more from the VLM pattern. This is illustrated in Fig. 6 and by the optimal  $h_3$  and  $\omega_c$  values shown in

Table 5. In order to mimic the VLM uptake patterns, the value of  $h_3$  for all soil types in this scenario was equal or close to zero. Decreasing  $h_3$  or  $\omega_c$  in order to simulate compensation makes JM-JMf predicting higher uptake from upper layers, increasing the discrepancy between the models. The optimal  $\omega_c$  for all soil types was equal to 1 (in other words: no compensation). RWU in the upper layers predicted by VLM is substantially reduced within a few days, whereas reducing  $\omega_c$  in JM-JMf model to  
5 predict compensation causes also an increase of uptake in upper layers. The model, therefore, cannot mimic the scenarios with compensation evaluated here. Conversely, the JMm was able to reproduce considerably well the VLM pattern for these scenarios due to the shape of  $\alpha_m$  as discussed above. As soon as  $M > M_c$  in the upper layers, RWU decreased at a higher rate, compensated by increasing uptake from the wetter, deeper layers. This agrees more closely to VLM predictions.

For high  $T_p$  (Fig. 7), the JM-JMf model can predict compensation ( $\omega_c < 1$ ), however its predicted RWU pattern is very different  
10 from JMm and VLM. JM-JMf predicts a higher RWU near the soil surface for a longer period than the other models that account for compensation. This makes soil water depletion to be more intense and RWU from these layers will cease sooner when  $h_s$  becomes lower than  $h_4$ . At this point,  $T_a$  is predicted to continue equal to  $T_p$  because of the low optimal  $\omega_c$  (= 0.19), which increases RWU from the deeper layers where  ~~$h > h_4$~~   $h$  is close or equal to  $h_4$ . JMm behaved very differently with uptake over the first few days (when  $M_s > M_c$ ) in accordance with  $R$  distribution. After  $M < M_c$  in upper soil layers, the RWU pattern  
15 started to change gradually and RWU increased at lower depths.

The proposed models (PM and PMm) are capable of predicting similar RWU patterns as VLM. For the low  $T_p$ -high  $R$  scenario (Fig. 6), RWU is more uniformly distributed over depth than in the VLM model for the first days and uptake from upper layers is lower than that predicted by VLM model. For high  $T_p$  (Fig. 7), these models better represent RWU patterns and, in general, there is not much difference in predictions of RWU between the proposed models. The shape of the transpiration reduction  
20 over time however, is smoother than the VLM model. Concerning the relative transpiration curve, the proposed models appear to be less precise than the other models that account for RWU compensation.

JMII does not mimic well the RWU pattern predicted by VLM for the high  $R$ -low  $T_p$  scenarios. It overestimates uptake from surface layers for the first days. Before the onset of transpiration reduction, uptake from upper layers becomes zero, but is compensated by a higher uptake from deeper layers. The model is very sensitive to either both  $R$  or  $M$ . For the high  
25  $R$ -high  $T_p$  scenarios JMII provides better uptake pattern predictions (Fig. 7). However, the model does not perform well in the other scenarios of low and medium  $R$  (data not shown here), ~~which will be discussed in section 4.1.3.~~

Comparing RWU predictions from JMf and JMII it is clear that the Jarvis-type models are affected by the definition of  $\alpha$ . This becomes more evident by analysing Fig. 9 which shows  $\alpha$  of JMII (eq. 18) as a function of  $h_s$  and  $\omega_c$  (eq. 20) for different soil types, expressed by  $M_{max}$ . Focussing first on the  $\alpha$  function, it can be seen that despite the fact that the soil resistance should increase continuously as soil dries, defining  $\alpha$  by eq. 18 does not seem very realistic. In this case  $\alpha$  is suddenly reduced even  
30 when the soil is near saturation. When  $h_s = 1$  m, for instance,  $\alpha$  is much lower than 0.5. Such a behaviour is not expected for the  $\alpha$  concept. The  $\omega_c$  values are also extremely low. The low  $\alpha$  values are, however, balanced by high  $\alpha_2$  values (due to low  $\omega$  and  $\omega_c$  values), leading to suitable values of RWU in a given soil layer. Nevertheless, the magnitude of  $\alpha$  and  $\omega_c$  are conceptually

questionable. Therefore, we conclude that: i) the  $\omega_c$  value in Jarvis-type models, which sets the compensation level, depends on the  $\alpha$  definition. For instance, for the original Jarvis (1989) model,  $\omega_c = 0.5$  corresponds to a moderate level of compensation. Surely, it does not hold if  $\alpha$  is defined by eq. 18; ii) Comparing Jarvis (1989) to De Jong van Lier et al. (2008) model led to a rather unrealistic  $\alpha$  function, and its behaviour does not properly represent the  $\alpha$  concept. This behaviour might be due to the fact that the De Jong van Lier et al. (2008) model does not take into consideration the plant hydraulic resistances. This might explain the rapid decline of  $\alpha$  near saturation. The threshold type functions like the other ones evaluated in this paper seems to be more feasible.

The fact that JMII is more sensitive to both  $R$  and  $M$ , as stated above, when compared to the other  $M$ -based models is attributed to the  $\alpha$  function and the derived equations to express their parameters (eq. 19 and 20). It can be seen from Fig. 9(c) that  $\beta$  defined by eq. 19 ( $\beta$  of JMII) tends to be higher when  $R$  increases and lower when  $R$  decreases compared to  $\beta$  of JMf and JMm. Thereby, for the first days of simulations when the soil hydraulic conditions tend to be rather uniform over depth, JMII overestimates RWU compared to VLM predictions. This becomes more important for the high  $R$ -low  $T_p$  scenarios. For such conditions, the RWU over depth predicted by the VLM tends to be more uniform, which is reasonable since the low transpiration demand can be met by any small  $R$  that can be found in deeper soil depths. After some period of time, the discrepancies between VLM and JMII tend to increase, since the higher RWU in the upper layers reduces  $h$ ; thus, because of  $\alpha$  shape of JMII RWU in the upper layers are suddenly reduced towards zero. These are the main reasons why JMII does not predict well in the high  $R$ -low  $T_p$  scenarios.

### 4.1.3 Statistical indices

The performance of the empirical models was analysed by the coefficient of determination  $r^2$  and the model efficiency coefficient  $E$  (Nash and Sutcliffe, 1970) calculated by comparing to the RWU and relative transpiration predicted by VLM. For the low  $R$ -high  $T_p$  scenarios, the VLM predicts water stress ( $T_a < T_p$ ) since the beginning of the simulation as discussed in section 4.1.1. The empirical models (except for JM-JMf and JMm by setting  $\omega_c > 1$ ) are not able to reproduce these results, thus these scenarios are not taken into account ~~on~~-when analysing the performance of the models.

These statistical indices for the evaluated scenarios of each model are concisely shown by the boxplots in Fig. 10. The width of whiskers indicates the range of the statistical indices for each model used in the evaluated scenarios. The outliers indicate whether a model had different performance at some scenarios than its overall performance. Focusing first on RWU, it can be easily seen the better performance of the proposed models. The performance of PM was just a bit poorer than PMm's, showed shown by the presence of an outlier and lower ~~medium~~median. JMm performed as good as the proposed models, and only in two scenarios it had a bad performance as shown by the outliers in Fig. 10. The wider whiskers and presence of outliers of the others models confirm their poorer performances.

Among the models that account for RWU compensation, JM-JMf and JMII had the poorest performances. These models had very low performances in the high  $R$ -low  $T_p$  scenarios and in general their performances were poorer for medium  $R$  scenarios, especially for low  $T_p$ . Thus, the use of  $\alpha_m$  to replace Feddes original reduction function  $\alpha_f$  in Jarvis (1989) model in Jarvis-type models promotes substantial improvements, especially from medium to high  $R$  scenarios. For low  $R$  scenarios all models performed well and the highest values of the boxes in Fig. 10 usually refer to this scenario.

On predicting transpiration all models accounting for compensation performed well, except JM-JMf. It can be noticed that JMII performed much better on predicting transpiration than RWU. Similarly as for the RWU predictions, all models had their poorest performance in the high  $R$  scenarios.

As the evaluated models differ regarding the number of empirical parameters (from 0 to 2), it is important to use a statistical measure that penalizes the models with more parameters. The Akaike's information criteria (AIC) is a suitable measure for such a model comparison. The selection of the "best" model is determined by an AIC score, defined as (Burnham and Anderson, 2002):

$$AIC = 2K - \log(\mathcal{L}(\hat{\theta}|y)) \quad (32)$$

where  $K$  is the number of fitting parameters and  $\mathcal{L}(\hat{\theta}|y)$  is the log-likelihood at its maximum point. The "best" model is the one with the lowest AIC score. Table 6 lists the best models for every scenario based on AIC score. Overall, the AIC supports the above descriptive statistical analyses, indicating that the proposed models are the best models in predicting RWU estimated by VLM, specially from medium-high  $R$  scenarios. For the low  $R$  scenarios JMm is the best model. On predicting  $T_r$  by VLM, the above analyses indicated that in general most models had similar performance. The AIC indicated similar results, but overall JMm was the best model. The proposed models (PM or PMm) were the best models for high  $R$ -low  $T_p$  scenarios.

#### 4.1.4 Relation of the optimal empirical parameters to $R$ and $T_p$ levels

The optimal values of the empirical parameters of all models (except for JMII that has no empirical parameters) for all scenarios (except for the high  $T_p$ -low  $R$  scenario) are shown in Table 5. The threshold reduction transpiration parameters  $h_3$  and  $M_c$  (for FM and FMm, respectively) stands for the soil hydraulic conditions from which the crop cannot meet its potential transpiration rate. Conceptually, the more the roots, the lower is  $h_3$  or  $M_c$  due to the larger root surface area for RWU, i.e. the crop can extract water in drier soil conditions. Similarly, lower  $h_3$  and  $M_c$  are expected for low  $T_p$ . This can also be deduced from Fig. 6 and 7 by means of the predictions of relative transpiration and RWU by VLM.

The optimal  $h_3$  and  $M_c$  values (Table 5) for FM and FMm, respectively, increase as  $R$  or  $T_p$  increases, contradicting their conceptual relation to  $R$  and  $T_p$ . For  $T_p$  levels, there is no specific relationship for these parameters: whether they increase or decrease with  $T_p$  depends on the value of  $R$ . In drying-out scenarios, soil water from top layers depletes rapidly due to the higher initial uptake. As a result, uptake from these layer starts to decrease whereas RWU in deeper, wetter layers increases.

The higher the  $R$ , the more intense is this process as seen by the VLM predictions in section 4.1.1. Because FM and FMm do not account for this mechanism, decreasing  $h_3$  or  $M_c$  in search for conceptually meaningful values would make these models to predict higher RWU at upper layers (in accordance with  $R$  distribution) for a longer period, increasing the discrepancy with VLM predictions. Therefore, their best fitted values are physically without meaning due to the model assumptions.

- 5 In order to interpret the parameters in Table 5 for **JMJMf**, one should first recall that  $\alpha$  in **JMJMf** stands for the local RWU reduction due to soil resistance. Thus, its  $h_3$  parameter refers to the local soil pressure at which RWU starts to reduce. It may be argued that RWU reduction occurs in drier soil conditions as  $R$  increases, that is  $h_3$  is more negative for higher  $R$  (similarly as for FM and FMm). However, since **JMJMf** accounts for compensation, RWU is interpreted as a non-local process, i.e. uptake in one layer depends on water status and root properties from other layers (Javaux et al., 2013). Thus, JM's  $h_3$  parameter is
- 10 affected by other parts of the root zone. Predictions by VLM show that RWU reduction from the upper layers starts at less negative soil pressure head as  $R$  increases. Therefore,  $h_3$  in **JMJMf** should increase as  $R$  increases. The values of  $h_3$  for **JMJMf** shown in Table 5 agrees to this conceptual meaning. The JMm's  $M_c$  parameter can be interpreted likewise.

The **JMJMf**'s  $\omega_c$  parameter values for the high  $R$ -low  $T_p$  scenarios equal 1, thus contradicting its conceptual meaning: as in these scenarios the compensation mechanism is more intense,  $\omega_c$  should be less than one for the medium and high  $R$  scenarios.

- 15 The reason for  $\omega_c = 1$  was discussed in section 4.1.2. Conversely,  $\omega_c$  values for JMm follow the conceptual meaning.

The optimal parameters of the proposed models follow the logical relation to  $R$  and  $T_p$ . The  $h_{rw}$  values for both models are very close. The optimal  $h_{rw}$  values are less sensitive to soil types and more sensitive to  $R$ .

High correlation parameters might result in uncertainties and nonunique solution of the optimization problem. In general, the correlation parameter coefficients were low, except in some scenarios in which high correlation coefficients between  $\omega_c$  and  $h_3$  (or  $M_c$ ) were found. These high correlations might be due to model structure rather than to the data used for fitting the models, since the correlation for PM and PMm parameters were considerably low (absolute correlation coefficient below 0.53).

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#### 4.1.5 Optimization using $T_r$

In order to evaluate the empirical models and find their empirical parameters, the empirical models were only fitted to RWU, since we are primarily interested on the capability of the models in predicting the RWU patterns under different scenarios. This is a great advantage of using physical RWU models, since RWU is not easily obtained in real conditions. Nevertheless, plant transpiration is one of the main outputs in RWU models and it is more easily obtained. Thus, one might consider to fit the models to the temporal course of (relative) plant transpiration or to fit the models simultaneously to both plant transpiration and RWU, at which a rather complicated optimization scheme is required.

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We addressed this issue by fitting the models to the course of relative transpiration for some scenarios. The procedure was the same as explained in Section 3.3, but substituting  $S_{i,j}$  in eq 31 by  $T_{r,i}$ . The results for some models in two contrasting scenarios

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of  $R$  is shown in Fig 11. It can be seen that the models who account for “compensation” can predict  $T_r$  quite reasonably even when fitted to RWU only. The models who do not account for “compensation” can not mimic well  $T_r$  course for the high  $R$  scenario predicted by VLM, even when they are fitted to  $T_r$ , and the predictions worsen when fitted to RWU. The most important aspect shown in Fig 11 is that fitting the models to  $T_r$  can improve  $T_r$  predictions but impairing considerably their RWU predictions, specially for high  $R$ . Conversely, if a model can fit well to RWU, they can provide suitable transpiration predictions. This can also be seen by the analysis of Section 4.1.3, when the proposed models and JMm had good performance in predicting  $T_r$  as well.

## 4.2 Growing season simulation

By evaluating the RWU models under real weather conditions during a relatively dry year and considering the same soil types and crop characteristics as for the drying-out experiment, it was possible to use the respective soil type and root length density specific calibrated parameters. We did not evaluate the models for the low  $R$  scenario because the empirical models (except JM-JMf and JMm) were not able to mimic those conditions for high  $T_p$  (section 4.1.1). This evaluation is also important to analyse whether calibration of an empirical model with a single drying-out experiment type results in consistent behaviour in other circumstances.

Table ?? shows the Fig 12 shows the time course of cumulative actual transpiration simulated by SWAP using all the RWU models. Actual cumulative transpiration, together with rain and  $T_p$  throughout the growing season period. It can be seen that right after the first dry spell,  $T_{ac}$  by FM and FMm, who do not account for “compensation”, starts to be lower than that by other models. Two or three more dry spells occur in the evaluated period. The magnitude of this underestimation, however, varies with soil type and  $R$ . For the medium  $R$ -loam soil scenario, for instance, the  $T_{ac}$  for all models are quite similar. The  $T_{ac}$  at the end of the evaluated period predicted by VLM for low  $R$  (not shown in Fig. 12) was much lower and approximately equal for the three soil types (40.45, 40.05 and 40.08 cm for clay, loam and sand soil, respectively). In fact, a higher  $R$  resulted in an increasing difference of cumulative transpiration between soil types. Most water is extracted from the clay soil, followed by sand and loam. Little difference of cumulative transpiration is found between medium and high  $R$ : for sand and clay soil, the cumulative transpiration was slightly higher for high  $R$  and practically identical for the loam soil.

Comparing cumulative  $T_a$  predicted by the empirical models with VLM predictions shows that the models that do not account for compensation underestimate cumulative  $T_a$  from 2.0 % (medium  $R$  –sand soil scenario) to 13.9 % (high  $R$ –clay soil scenario). Overall, the highest underestimates occurred for high  $R$ . All other models predict similar values. Therefore, for total actual transpiration any of the evaluated models accounting for compensation might be suitable after calibration.

An overall analysis of the models performance is shown in Fig. 13 and a list of the “best” model for each scenario based on AIC is shown in Table 7. The best performances are from the models that account for compensation. An improvement of JM-JMf by using the proposed reduction function can be observed. Among the models that account for compensation, JM-JMf had

the worst performance. JMII also was poor in predicting RWU, but showed good performance in estimating plant transpiration. Overall, the best performances were also obtained by the proposed models (PM and PMm) and by the modified Jarvis (1989) model (JMm) in predicting RWU. These results also indicate that the strategy of designing a single drying-out experiment to calibrate an empirical model in a single drying-out experiment is successful.

5 The selection of the best models based on AIC also indicates PM, PMm and JMm as the best models in predicting RWU. Regarding  $T_r$  predictions, Fig. 13 shows considerably high statistical indices ( $E$  and  $r^2$ ) for all models that account for “compensation”. However, the AIC, which penalizes the models with more parameters, indicates that JMII was the “best” model for most of the scenarios.

In general, the proposed models as well as JMm showed better performance than the other empirical models. It should be noted, however, that these models are based on  $M$ , making them closer to the physical De Jong van Lier et al. (2013) model. In this regard, it is important to separately compare JMf and JMm and PM and PMm. The only difference between JMf and JMm is the  $\alpha$  reduction, which resulted in considerable improvements as already discussed. In the proposed models,  $M$  is included in  $S_p(z)$  to distribute  $T_p$  over depth. In PMm  $\alpha_m$  is used instead of the Feddes reduction function (used by PM). These simple modifications were sufficient to make these empirical models mimic the predictions made by the more complex physical model when fitted.

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## 5 Conclusions

Several simple RWU models have been developed over the years and here we outlined some of these models and also proposed alternatives. Some of these models were embedded as sub-models into the eco-hydrological model SWAP (Van Dam et al., 2008) and their evaluation was based on the comparison of with RWU predictions performed by the physical De Jong van Lier et al. (2013) model (also embedded into the SWAP model) for two numerical experiments with several scenarios of soil type, root length density and potential transpiration. The parameters of the empirical models were determined by inverse modelling of simulated RWU. The simulated scenarios also allowed insight into the behaviour of the De Jong van Lier et al. (2013) model, especially under wet soil conditions and high potential transpiration. We found that for the low  $R$ -high  $T_p$  scenarios the De Jong van Lier et al. (2013) model predicts crop transpiration reduction in wet soil conditions. For such cases, the maximum crop transpiration rate is dependent on crop hydraulic parameters, especially the radial root hydraulic conductivity. More insight into these results may be obtained by coupling the De Jong van Lier et al. (2013) physical model with stomatal conductance models. Regarding the performance of the empirical models we conclude:

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- The widely-used Feddes et al. (1978) empirical RWU model performs well only under circumstances of low root length density  $R$ , that is for the scenarios of low root water “compensation”. From medium to high  $R$ , the model cannot mimic properly the RWU dynamics as predicted by the De Jong van Lier et al. (2013) model, resulting in very poor predictions.
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Besides, the optimized  $h_3$  values are counterintuitive when interpreting their conceptual meaning. Using our proposed RWU reduction function (the FMm model) does not improve performance either.

- The [Jarvis \(1989\)-JMf](#) model provides good predictions only for low and medium  $R$  scenarios. For high  $R$ , the model cannot mimic the RWU patterns predicted by the De Jong van Lier et al. (2013) model. Using our proposed reduction function (the JMm model) helps to improve RWU predictions. Similarly, the JMII model does not perform well for high  $R$ -low  $T_p$  scenarios, [as explained in Section 4.1.2.](#)
  - The proposed models are capable of predicting RWU [patters-patterns](#) similar to those obtained by the De Jong van Lier et al. (2013) model. The statistical indices point them as the best alternatives to mimic RWU predictions by the De Jong van Lier et al. (2013) model.
- 10 • [Regarding the ability of the models in predicting plant transpiration, all models that accounts for compensation have good performance. The AIC information indicates that JMII, which has no empirical parameters to be estimated, is the “best model”. This model is also more suitable for blind predictions.](#)
- The simulations for a growing season experiment confirmed these findings, suggesting that a single experiment of soil drying-out is sufficient to analyse the performance of RWU models and retrieve their empirical parameters by defining the objective
- 15 function in terms of RWU.

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## List of tables

**Table 1.** Summary of empirical models used.  $\alpha_f$  and  $\alpha_m$  are the Feddes et al. (1978) (Fig. 1a) and proposed reduction functions (Fig. 1b),  $S_p$  (eq. 4) is the potential root water uptake,  $\omega$  (eq. 11) and  $\omega_c$  are the weighted stress index and threshold value in Jarvis (1989) model and  $\zeta_m$  (eq. 25) is the weighted stress index in the proposed models.

Model	Acronym	Equation
Feddes et al. (1978) model	FM	$S(z) = S_p \alpha_f$
Modified Feddes et al. (1978) model	FMm	$S(z) = S_p \alpha_m$
Jarvis (1989) model	<del>JM</del> JMf	$S(z) = S_p \frac{\alpha_f}{\max\{\omega, \omega_c\}}$
Modified Jarvis (1989) model	JMm	$S(z) = S_p \frac{\alpha_m}{\max\{\omega, \omega_c\}}$
Jarvis (2010) model	JMII	Eqs. 11 to 13 with parameters given by eqs. 18 to 20
proposed model I	PM	$S(z) = \zeta_m T_p \alpha_f$
proposed model II	PMm	$S(z) = \zeta_m T_p \alpha_m$

**Table 2.** Values of the parameters of De Jong van Lier et al. (2013) model used in the simulations.

Parameter	Value	Unit
$r_0$	0.5	mm
$r_x$	0.2	mm
$K_{root}$	$3.5 \cdot 10^{-8}$	$\text{m d}^{-1}$
$L_l$	$1 \cdot 10^{-6}$	$\text{d}^{-1}$
$\overline{h_w} - \underline{h_{w\varepsilon}}$	<u>-150</u>	<u>m</u>
$\underline{h_{wl}}$	-200	m

**Table 3.** Mualem-van Genuchten parameters for three soils of the Dutch Staring series (Wösten et al., 1999) used in simulations.  $\theta_s$  and  $\theta_r$  are the saturated and residual water content, respectively;  $K_s$  is saturated hydraulic conductivity and  $\alpha$ ,  $\lambda$  and  $n$  are fitting parameters.

Staring soil ID	Textural class	Reference in this paper	$\theta_r$	$\theta_r$	$K_s$	$\alpha$	$\lambda$	$n$
			$\text{m m}^{-3}$	$\text{m m}^{-3}$	$\text{m d}^{-1}$	$\text{m}^{-1}$	-	-
B3	Loamy sand	Sand	0.02	0.46	0.1542	1.44	-0.215	1.534
B11	Heavy Clay	Clay	0.01	0.59	0.0453	1.95	-5.901	1.109
B13	Sand Loam	Loam	0.01	0.42	0.1298	0.84	-1.497	1.441



**Table 4.** Parameters of the root water uptake models estimated by optimization and their respective constraints  $\Omega$ .

Model	Parameter	$\Omega$	Unit
FM	$h_3$	$-150 < h_3 < 0$	m
FMm	$M_c$	$0 < M_c < M_{max}$	$\text{m}^2 \text{d}^{-1}$
<del>JM</del> <u>JMf</u>	$h_3$	$-150 < h_3 < 0$	m
	$\omega_c$	$0 < \omega_c \leq 1$	-
JMm	$M_c$	$0 < M_c < M_{max}$	$\text{m}^2 \text{d}^{-1}$
	$\omega_c$	$0 < \omega_c \leq 1$	-
PM	$h_3$	$-150 < h_3 < 0$	m
	$l_m$	$\theta < l_m \leq 1$ $0 < l_m \leq 3$	-
PMm	$M_c$	$0 < M_c < M_{max}$	$\text{m}^2 \text{d}^{-1}$
	$l_m$	$\theta < l_m \leq 1$ $0 < l_m \leq 3$	-

**Table 5.** Optimal parameters of each empirical model for all scenarios in the drying-out experiment

Soil	Tp	$R\bar{D}-R$	FM	FMm	JMf	JMm	PM		PMm			
			$h_3$	$M_c$	$h_3$	$\omega_c$	$M_c$	$\omega_c$	$h_3$	$H_m$	$M_c$	$H_m$
	mm d <sup>-1</sup>	cm cm <sup>-3</sup>	cm	cm <sup>2</sup> d <sup>-1</sup>	cm	-	cm <sup>2</sup> d <sup>-1</sup>	-	cm	-	cm <sup>2</sup> d <sup>-1</sup>	-
clay	1	0.01	-1968.7	0.213	-284.5	0.711	0.366	0.494	-1615.7	1.322	0.227	1.290
clay	1	0.10	-1211.0	0.329	-132.4	0.196	0.944	0.024	-7579.9	0.869	0.076	0.884
clay	1	1.00	-1.7	0.950	-0.0	1.000	5.971	0.004	-10673.7	0.354	0.022	0.342
loam	1	0.01	-7588.1	0.334	-5.0	0.457	22.483	0.016	-6927.6	1.086	0.408	1.084
loam	1	0.10	-6085.6	0.487	-93.9	0.126	25.721	0.002	-11795.6	0.911	0.113	0.917
loam	1	1.00	-17.0	5.014	-48.0	1.000	106.223	0.000	-10878.8	0.561	0.058	0.553
sand	1	0.01	-1014.0	0.146	-291.6	0.942	0.288	0.436	-621.2	1.262	0.149	1.252
sand	1	0.10	-1122.6	0.115	-113.6	0.407	1.925	0.005	-2351.3	1.179	0.024	1.159
sand	1	1.00	-3.9	0.338	-0.0	1.000	25.887	0.000	-3158.0	0.717	0.005	0.706
clay	5	0.10	-1397.7	0.334	-218.4	0.325	0.395	0.271	-5537.2	1.512	0.196	1.449
clay	5	1.00	-260.6	0.792	-135.3	0.148	1.212	0.013	-6745.0	0.672	0.088	0.687
loam	5	0.10	-5236.5	0.784	-0.0	0.277	2.306	0.100	-8322.9	1.165	0.488	1.157
loam	5	1.00	-1249.5	2.563	-292.9	0.161	28.143	0.001	-8630.0	0.833	0.224	0.838
sand	5	0.10	-918.0	0.190	-556.2	0.432	4.154	0.018	-1273.9	1.612	0.083	1.510
sand	5	1.00	-582.3	0.533	-342.5	0.193	4.888	0.001	-3582.3	1.272	0.012	1.240

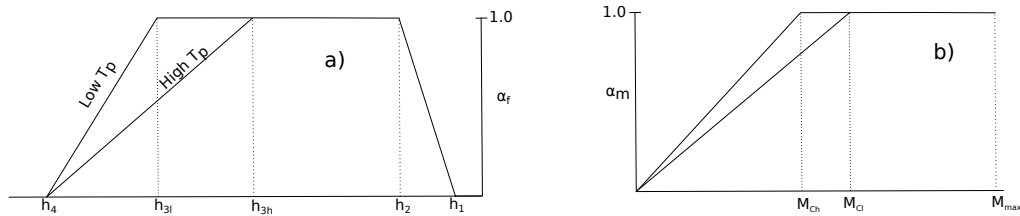
**Table 6.** Best models for the evaluated scenarios (root length density  $R$ , soil type and potential transpiration  $T_p$ ) based on Akaike's information criteria AIC through comparison of root water uptake (RWU) and relative transpiration ( $T_r$ ) predicted by De Jong van Lier et al. (2013) physical model in the drying-out experiment.

		Low $T_p$			High $T_p$			
		<u><math>R</math></u>	<u>Clay</u>	<u>Loam</u>	<u>Sand</u>	<u>Clay</u>	<u>Loam</u>	<u>Sand</u>
RWU	<u>Low</u>	<u>JMm</u>	<u>JMf</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>
	<u>Medium</u>	<u>PMm</u>	<u>PMm</u>	<u>JMII</u>	<u>JMm</u>	<u>PM</u>	<u>PMm</u>	<u>PMm</u>
	<u>High</u>	<u>PMm</u>	<u>PMm</u>	<u>PM</u>	<u>PM</u>	<u>PMm</u>	<u>PM</u>	<u>PM</u>
$T_r$	<u>Low</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>
	<u>Medium</u>	<u>JMm</u>	<u>JMm</u>	<u>JMII</u>	<u>JMm</u>	<u>PM</u>	<u>JMf</u>	<u>JMf</u>
	<u>High</u>	<u>PMm</u>	<u>PMm</u>	<u>PMm</u>	<u>JMII</u>	<u>JMm</u>	<u>JMm</u>	<u>JMm</u>

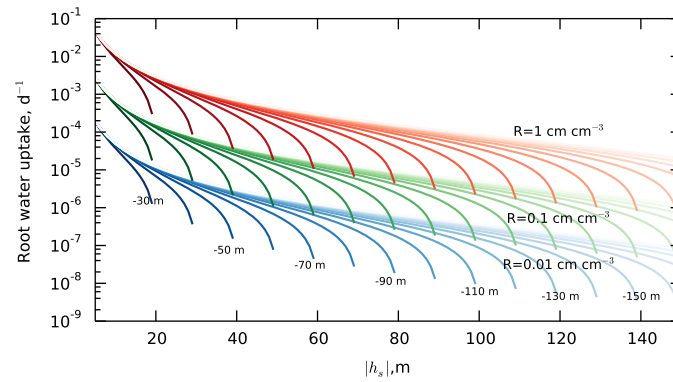
**Table 7.** Best models for the evaluated scenarios (root length density  $R$  and soil type) based on Akaike's information criteria AIC through comparison of root water uptake (RWU) and relative transpiration ( $T_r$ ) predicted by De Jong van Lier et al. (2013) physical model in the growing season experiment.

	Clay		Loam		Sand	
	<u>Medium R</u>	<u>High R</u>	<u>Medium R</u>	<u>High R</u>	<u>Medium R</u>	<u>High R</u>
<u>RWU</u>	<u>JMm</u>	<u>PM</u>	<u>PM</u>	<u>PMm</u>	<u>JMm</u>	<u>JMm</u>
<u><math>T_r</math></u>	<u>JMII</u>	<u>JMII</u>	<u>JMf</u>	<u>JMm</u>	<u>JMII</u>	<u>JMII</u>

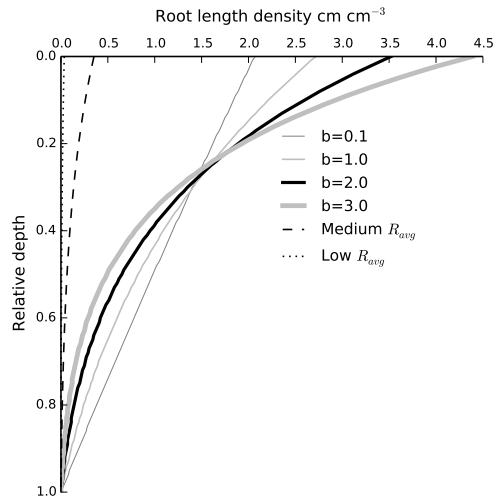
## List of figures



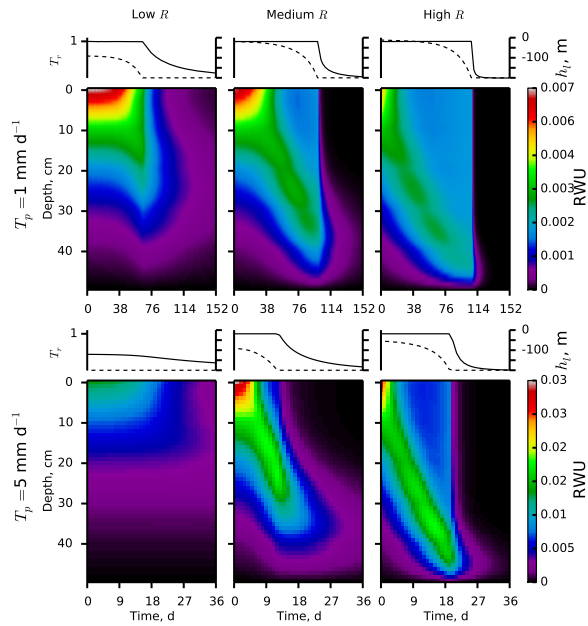
**Figure 1.** a) Feddes et al. (1978) root water uptake reduction function.  $h_2$  and  $h_3$  are the threshold parameters for reduction in root water uptake due to oxygen deficit and water deficit, respectively. The subscripts  $l$  and  $h$  stands for low and high potential transpiration  $T_p$ .  $h_1$  and  $h_4$  are the soil pressure head values above and below which root water uptake is zero due to oxygen and water deficit, respectively. b) Root water uptake reduction function  $\alpha_m$  as a function of matric flux potential  $M$ ;  $M_c$  is  $M_{ch}$  and  $M_{cl}$  are the critical value-values of  $M$  for high and low  $T_p$ , respectively, from which the uptake is reduced and  $M_{max}$  is the maximum value of  $M$ , dependent on soil type.



**Figure 2.** Root water uptake  $S$  as a function of soil pressure head  $h_s$  for three values of root length density ( $0.01$ ,  $0.1$  and  $1.0 \text{ cm cm}^{-3}$ ) and leaf pressure head values ranging from  $-30$  to  $-200$  m by  $-10$  m interval shown by colors gradient (lighter colors indicate lower values and some values are also indicated in the plot). These results were obtained by the analytical solution of eq. 8 given by De Jong van Lier et al. (2013) for a special case of Brooks and Corey (1964) soil. Plant transpiration was set to  $1 \text{ mm d}^{-1}$ , rooting depth to  $0.5$  m, and the soil and plant hydraulic parameters were taken from De Jong van Lier et al. (2013).

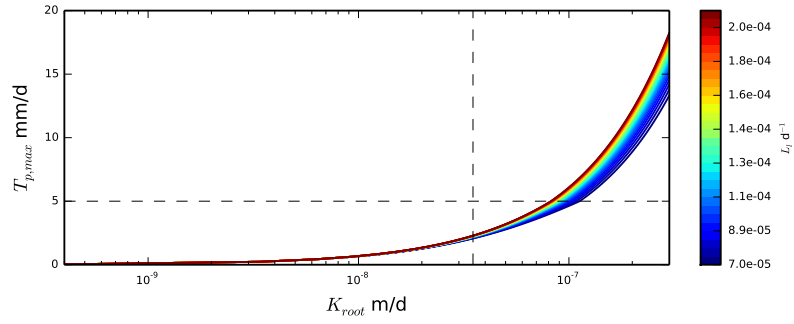


**Figure 3.** Root length density distribution over depth calculated by eq. 30 for several values of  $b$  and  $R_{avg} = 1.0 \text{ cm cm}^{-3}$  and for low and medium  $R_{avg}$  with  $b = 2$ .

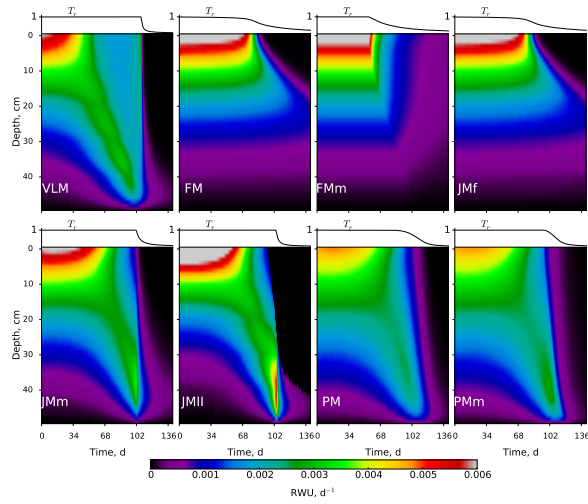


**Figure 4.** Time-depth root water uptake (RWU,  $\text{d}^{-1}$ ) pattern, leaf pressure head ( $h_l$ , dashed line) and relative transpiration ( $T_r$ , continuous line) simulated by SWAP model together with the De Jong van Lier et al. (2013) model for clay soil, two levels of potential transpiration  $T_p$ : 1 and 5  $\text{mm d}^{-1}$  (first and second line of plots, respectively) and three levels of root length density  $R$ : low, medium and high (indicated at the top of the figure).

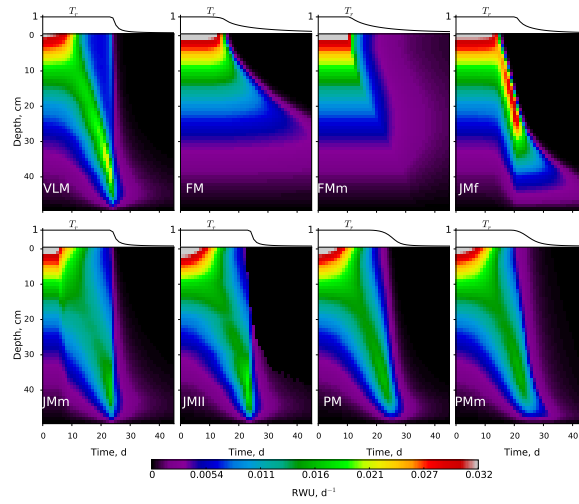




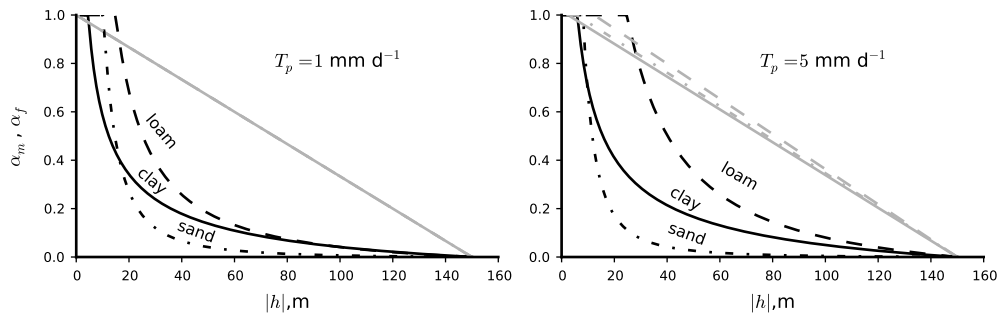
**Figure 5.** Maximum possible transpiration  $T_{p,max}$  as a function of root hydraulic conductivity  $K_{root}$  for some values of the overall conductance over the root-to-leaf pathway  $L_l$  computed by De Jong van Lier et al. (2013) model for rooting depth of 0.5 m, low root length density and constant soil pressure head over depth equals to -1 m for sandy soil. The dashed vertical line highlights the value of  $K_{root} = 3.5 \cdot 10^{-8} \text{ m d}^{-1}$  that was used in our simulations. Horizontal dashed line highlights the value of potential transpiration.



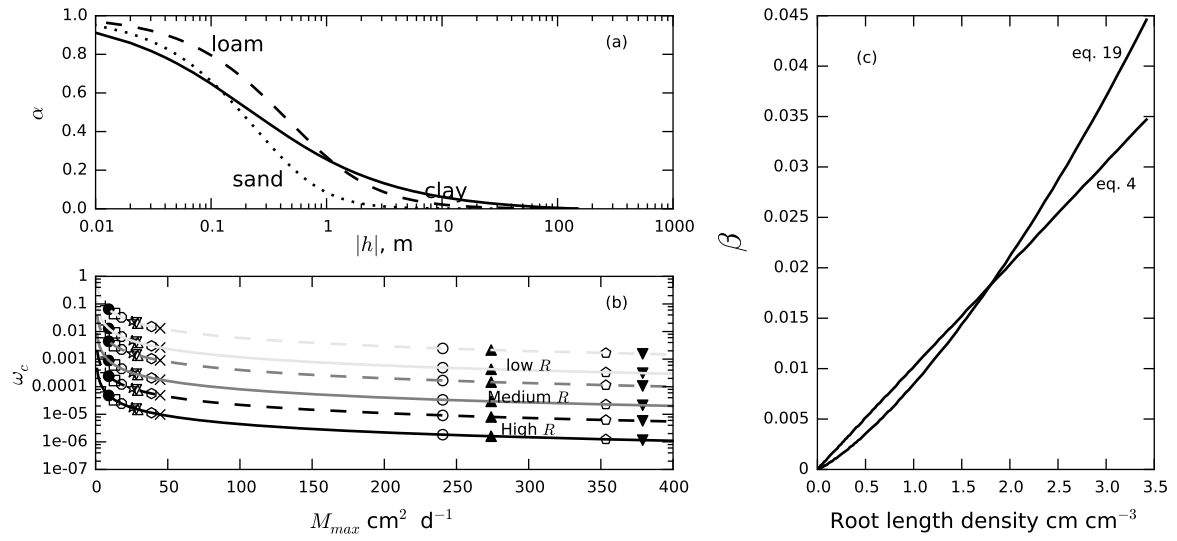
**Figure 6.** Time-depth root water uptake (RWU) pattern and relative transpiration ( $T_r$ ) simulated by SWAP model together with De Jong van Lier et al. (2013) sink and the others empirical models for sandy sand soil texture, high root length density and  $T_p = 1 \text{ mm d}^{-1}$ .



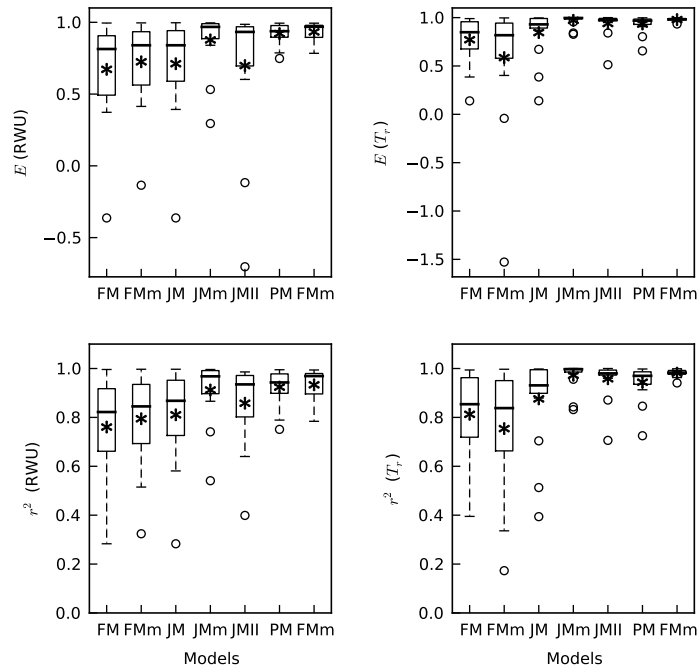
**Figure 7.** Time-depth root water uptake (RWU) pattern and relative transpiration ( $T_r$ ) simulated by SWAP model together with De Jong van Lier et al. (2013) sink and the others empirical models for sandy soil texture, high root length density and  $T_p = 5 \text{ mm d}^{-1}$ .



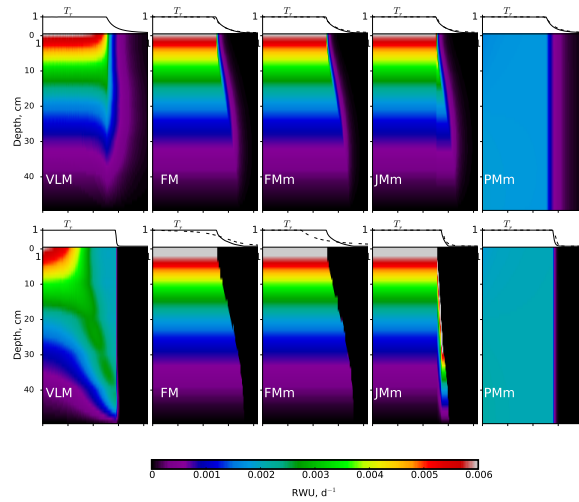
**Figure 8.** Feddes et al. (1978) ( $\alpha_f$ , gray lines) and proposed ( $\alpha_m$ , black lines) water uptake reduction functions as a function of soil pressure head  $h$  using their respective optimized parameters for the scenario of high root length density, three types of soil and two potential transpiration levels.



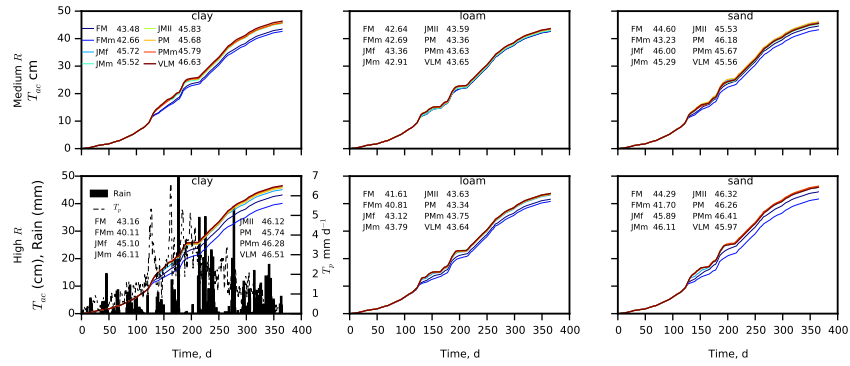
**Figure 9.** (a)  $\alpha$  of JMII model (eq. 18) as function of soil pressure head  $h_s$ , (b)  $\omega_c$  parameter (eq. 20) for different soil types (the three soil types used in the simulations and more soils from Wösten et al. (1999) ), expressed by  $M_{max}$  and (c) the normalized root length density  $\beta$  computed by the eqs. 4 (JMf) and 19 (JMII) as function of root length density  $R$ , with  $R$  over depth given by eq. 30 with  $R_{avg}$  and  $b$  equal to  $1.0 \text{ cm cm}^{-3}$  and 2, respectively.



**Figure 10.** Box plot of the coefficient of determination  $r^2$  and model efficiency coefficient  $E$  for the comparison of root water uptake (RWU) and actual transpiration ( $T_a$ ) predicted by each empirical model with the De Jong van Lier et al. (2013) model predictions for the drying-out simulations for three levels of root length density and three types of soil and two potential transpiration levels. The symbols \* and o represent the average and outliers, respectively.

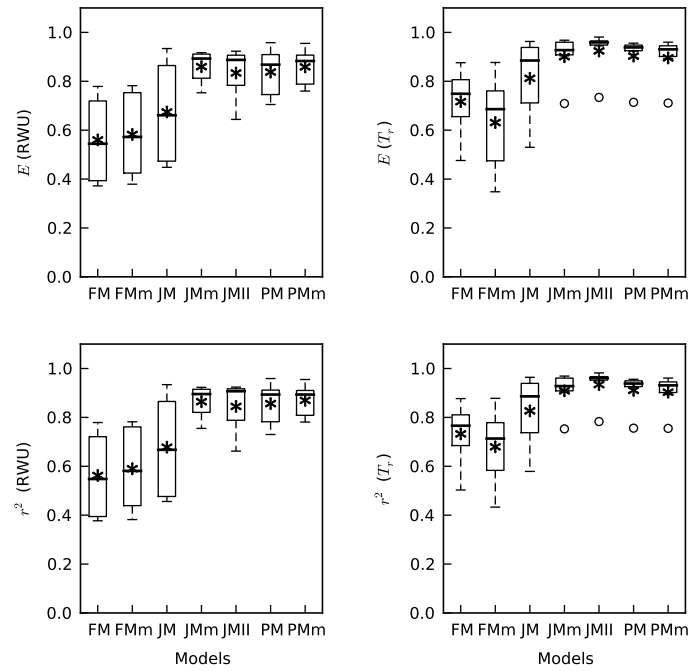


**Figure 11.** Time-depth root water uptake (RWU) pattern and relative transpiration ( $T_r$ ) simulated by SWAP model together with De Jong van Lier et al. (2013) sink and some empirical models when optimization was performed with  $T_r$  instead of RWU for loam soil texture, low (first line of plots) and high (second line of plots) root length density and  $T_p = 1 \text{ mm d}^{-1}$ . The dashed lines indicate  $T_r$  when the models were optimized with RWU.



**Figure 12.** Time course of actual cumulative plant transpiration  $T_{ac}$  predicted by the De Jong van Lier et al. (2013) and all the empirical models for the three types of soil (clay, loam and sand) and two levels of root length density (medium and high), rain and potential transpiration  $T_p$  for the growing season experiment. The total  $T_{ac}$  values predicted by each model for the whole period are shown in the plot aside the model names.





**Figure 13.** Box plot of the coefficient of determination  $r^2$  and model efficiency coefficient  $E$  for the comparison of root water uptake (RWU) and actual transpiration ( $T_a$ ) predicted by each empirical model with De Jong van Lier et al. (2013) model for the growing season experiment for two levels of root length density and three types of soil. The symbols \* and o represent the average and outliers, respectively.