



1 **Vegetation dynamics and climate seasonality jointly control the interannual**
2 **catchment water balance in the Loess Plateau under the Budyko framework**

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10
11 **Abstract.** Within the Budyko framework, the controlling parameter (ω in the Fu equation) is widely
12 considered to represent landscape conditions in terms of vegetation coverage (M); however, some
13 qualitative studies have concluded that climate seasonality (S) should be incorporated in ω . Here, we
14 discuss the relationship between ω , M , and S , and further develop an empirical equation so that the
15 contributions from M to actual evapotranspiration (ET) can be determined more accurately. Taking 13
16 catchments in the Loess Plateau as examples, ω was found to be well correlated with M and S . The
17 developed empirical formula for ω calculations at the annual scale performed well for estimating ET by
18 the cross-validation approach. By combining the Budyko framework with the semi-empirical formula,
19 the contributions of changes in ω to ET variations were further decomposed as those of M and S .
20 Results showed that the contributions of S to ET changes ranged from 0.1% to 65.6% (absolute values);
21 therefore, the impacts of climate seasonality on ET cannot be ignored. Otherwise, the contribution of M
22 to ET changes will be estimated with a large error. The developed empirical formula between ω , M , and
23 S provides an effective method to separate the contributions of M and S to ET changes.

24 **KEYWORDS:** Budyko framework; Controlling parameter; Vegetation dynamics; Climate seasonality;
25 Loess Plateau



27 1. Introduction

28 The water cycle has been influenced greatly by human activities and climate change since the
29 1960s, and considerable variability in hydrological processes has been observed in many basins around
30 the world; this has led to a series of problems concerning essential water resources (Stocker et al., 2014).
31 Analyses of the mechanisms of the interactions among the water balance, climate, and catchment
32 surface conditions are important for understanding these complex processes at different spatio-temporal
33 scales (Zhang et al., 2008), and such work has practical significance in regard to the improvement of
34 water resources and land management (Rodriguez-Iturbe, 2000; Xu et al., 2014).

35 Budyko (1948, 1974) postulated that precipitation (P , represents the water supply from the
36 atmosphere) and potential evapotranspiration (ET_0 , represents the demand by the atmosphere) are the
37 two dominant variables that control the long-term average water balance. The Budyko framework is
38 considered one of the most abiding frameworks linking climatic conditions to the runoff (R) and actual
39 evapotranspiration (ET) of a catchment (Donohue et al., 2007), and it has been used successfully to
40 investigate interactions between hydrological processes, climate variability, and landscape
41 characteristics (e.g. (Milly, 1994; Woods, 2003; Yokoo et al., 2008; Yang et al., 2009)). A series of
42 empirical formulas have been developed for the Budyko curve based on theoretical research and case
43 studies of regional water balance over the past 50 years. Among them, the Fu (Fu, 1981; Zhang et al.,
44 2004) and Choudhury–Yang equations (Choudhury, 1999; Yang et al., 2008) have been used widely;
45 furthermore, the controlling parameters ω (in the Fu equation) and n (in the Choudhury–Yang equation)
46 are related linearly (Yang et al., 2008).

47 Deviations from the Budyko curve have been detected in previous studies, which indicates that in
48 addition to climate conditions, other variables can also influence the variability of regional water
49 balances (Yang et al., 2007; Wang and Alimohammadi, 2012). Two kinds of factors have been identified
50 to be responsible for the deviations. The first type of factors are related to land surface conditions, and



51 these include vegetation dynamics (Donohue et al., 2007; Yang et al., 2009; Donohue et al., 2010; Li et
52 al., 2013; Zhang et al., 2016), soil properties, and topography (Yang et al., 2007; Peel et al., 2010). The
53 second type of factors include seasonal climate variability (in addition to P and ET_0), such as storm
54 depth (Shao et al., 2012; Li, 2014), frequency of daily rainfall (Milly, 1994), and differences in the
55 timing of P and ET_0 (Budyko, 1961; Potter et al., 2005). All of these factors can be encoded into the
56 controlling parameter of the Budyko equations (e.g. ω in the Fu equation and n in the Choudhury–Yang
57 equation). So far, a great deal of attention has been paid to the relationships between land surface
58 conditions and the controlling parameter. Based on satellite products of vegetation such as the
59 Normalized Difference Vegetation Index (NDVI), vegetation has been found to correlate well with the
60 controlling parameter, and some empirical relationships have been successfully developed (Yang et al.,
61 2009; Li et al., 2013). In particular, the controlling parameter can be better represented by vegetation
62 when higher spatiotemporal resolution products are used. Therefore, the impacts of dynamic changes in
63 vegetation on hydrology can be effectively quantified.

64 Many current studies attribute any effects of the controlling parameter to landscape characteristics
65 (Roderick and Farquhar, 2011; Zhou et al., 2015; Zhang et al., 2016). However, both empirical evidence
66 and modelling tests have demonstrated the important function of climate seasonality on catchment water
67 yield, and thereby, evidence exists that climate seasonality also strongly affects the controlling
68 parameter in the Budyko equations (Berghuijs and Woods, 2016). Some indices and models have thus
69 been developed to address this issue, and several potential solutions have been discussed (Milly, 1993,
70 1994; Potter et al., 2005; Yokoo et al., 2008; Feng et al., 2012; Li, 2014). So far, two notable advances
71 related to this problem have come from Yang et al. (2012) and Jiang et al. (2015). Yang et al. (2012)
72 introduced the climate seasonality index into the Budyko framework and proposed an empirical
73 equation to include its effect in the estimation of the long-term controlling parameters; however, by
74 focusing on the mean annual scale, the effects of vegetation dynamics were not considered. Jiang et al.
75 (2015) proposed an empirical formula for the parameter ω with the factors of climate (represented by



76 temperature and ET_0) and human activities, and they found that the performance was very good ($R^2 >$
77 0.9); however, as parameter ω derived from the water balance was actually a function of ET_0 , a
78 self-correlation phenomenon may exist in their formula. Therefore, how the vegetation dynamics and
79 climate seasonality jointly control the interannual variability in the controlling parameters needs further
80 interpretation.

81 Therefore, the primary motivation behind this study was to detect the potential linkages between
82 the controlling parameter and surface condition change, as well as climate seasonality at an annual scale.
83 The specific objectives were to derive an appropriate analytic formula between parameter ω in the Fu
84 equation and the above two factors for typical catchments in the Loess Plateau, and then, quantify the
85 impacts of vegetation change and climate seasonality variability on the catchment water balance.

86 2. Methods

87 2.1. Annual water balance definition

88 The Budyko framework assumes that the long-term average water balance is in a steady state
89 (Wang and Alimohammadi, 2012), and the water storage change (ΔS) in a catchment can be negligible.
90 The interannual variability of the water balance in individual basins can also be studied by overlooking
91 the interannual variation of the catchment water storage (ΔS) (Sankarasubramanian and Vogel, 2002;
92 Yang et al., 2007; Potter and Zhang, 2009). However, water storage change can be great when analysing
93 the interannual variability of the water balance (Wang, 2012). To minimize the potential errors
94 introduced by neglecting water storage variation, the hydrological year (Sivapalan et al., 2011; Carmona
95 et al., 2014) and moving windows (Jiang et al., 2015) were introduced to the time series of annual
96 hydrological variables. Similar to Sivapalan et al. (2011) and Carmona et al. (2014), the hydrological
97 year rather than the calendar year is introduced to calculate the annual ET , and this is called the
98 “measured” ET in the subsequent discussion. Specifically, as the study area has a semiarid climate with



99 most rainfall occurring in summer and autumn (July–September), a hydrological year is defined as July
100 to June of the following year. In this way, the water input occurs mainly at the beginning of the year and
101 the water is consumed within that year.

102 2.2. Identification of factors determining parameter ω in Fu's equation

103 The Fu equation is used in this study with the following expressions:

$$\begin{aligned} 104 \quad \frac{ET}{P} &= 1 + \frac{ET_0}{P} - \left[1 + \left(\frac{ET_0}{P} \right)^\omega \right]^{1/\omega} \text{ or} \\ 105 \quad \frac{ET}{ET_0} &= 1 + \frac{P}{ET_0} - \left[1 + \left(\frac{P}{ET_0} \right)^\omega \right]^{1/\omega} \end{aligned} \quad (1)$$

106 where ω is the controlling parameter of the Budyko curve. ET_0 is calculated by using the equation of
107 Priestley and Taylor (1972).

108 The important issue regarding the parameterization of ω in Fu's equation is to choose factors with
109 physical meanings. According to the results from related studies, land surface conditions can be mainly
110 represented by vegetation, which was also true in this study. With an arid to semiarid climate, water
111 availability is the key factor that controls vegetation dynamics. Although soil properties and topography
112 also influence vegetation growth, their impacts can be ignored on an annual scale because they would
113 be expected to be almost constant over a year. Therefore, vegetation dynamics (i.e. vegetation coverage)
114 were chosen to represent the variations in surface conditions. The vegetation coverage (M) was
115 estimated by the following equation (Yang et al. (2009)):

$$116 \quad M = \frac{NDVI - NDVI_{min}}{NDVI_{max} - NDVI_{min}} \quad (2)$$

117 where $NDVI_{max}$ and $NDVI_{min}$ are the NDVI values of dense forest (0.80) and bare soil (0.05),
118 respectively.

119 Two limiting conditions were used to illustrate the effects of seasonal variations in coupled water
120 and energy on the regional water balance. If P and ET_0 are in phase, the intra-annual distribution of



121 precipitation is very symmetrical, and thus, $R \rightarrow 0$ in non-humid regions and $ET \rightarrow P$. However, if P
 122 and ET_0 are out phase, the total precipitation of one year is concentrated at a certain moment, and thus,
 123 $R \rightarrow P$ and $ET \rightarrow 0$. Therefore, the impacts of seasonal variations in coupled water and energy on the
 124 regional water balance cannot be neglected, and they can only be reflected by the controlling parameter.
 125 In this study, the climate seasonality index (S), as introduced by Milly (1994) and Woods (2003), was
 126 used to reflect the non-uniformity in the annual distribution of water and heat:

$$127 \quad S = |\delta_P - \delta_{ET_0} \phi| \quad (3)$$

128 where δ_P and δ_{ET_0} are the seasonal amplitude of precipitation and potential evapotranspiration,
 129 respectively, which can be expressed by sine functions and fitted by the monthly P and ET_0 values. ϕ
 130 is the dryness index.

131 **2.3. Evaluating the contributions of climate change and surface condition alterations to ET trends**

132 Based on the climate elasticity method, which was introduced by (Schaake and Waggoner, 1990)
 133 and improved by (Sankarasubramanian et al., 2001), the contribution of change for each climate factor
 134 to pan evaporation and/or ET_0 was defined as the product of the partial derivative and slope of the trend
 135 for the climate factor (Zheng et al., 2009). Here, we extend this method to the Budyko equation and
 136 incorporate the vegetation coverage and climate seasonality.

137 The contributions of P , ET_0 , and ω changes to the ET trends can be assessed by taking the
 138 derivative of Eq. (1) with respect to time:

$$139 \quad \frac{dET}{dt} = \frac{\partial f}{\partial P} \frac{dP}{dt} + \frac{\partial f}{\partial ET_0} \frac{dET_0}{dt} + \frac{\partial f}{\partial \omega} \frac{d\omega}{dt} \quad (4)$$

140 In order to simplify the calculation process for the partial derivative in Eq. (4), the multiple linear
 141 regression method is applied in our study by using the time series of ET , P , ET_0 , and ω for each basin,
 142 and the regression coefficients approximately replace the partial derivative. Thus, Eq. (4) can be



143 rewritten as:

$$144 \quad \frac{dET}{dt} = A * \frac{dP}{dt} + B * \frac{dET_0}{dt} + C * \frac{d\omega}{dt} \quad (5)$$

145 where A, B, and C are the regression coefficients. Alternatively, it can be expressed as:

$$146 \quad L_{(ET)} = C_{(P)} + C_{(ET_0)} + C_{(\omega)} \quad (6)$$

147 where $L_{(ET)}$ is the slope of ET , and $C_{(P)}$, $C_{(ET_0)}$, and $C_{(\omega)}$ are the respective contributions of P ,
 148 ET_0 , and ω to the ET trends.

149 After obtaining the contribution of parameter ω to the ET change, the contributions of vegetation
 150 coverage (M) and climate seasonality (S) to ET change can be further decomposed as follows.

151 First, the contributions of M and S to parameter ω are calculated by using an equation similar to
 152 Eq. (4) and the partial derivatives are replaced by the regression coefficients for the relationships
 153 between ω and M as well as S . Furthermore, the individual relative contributions (RC) of M and S to
 154 ω can be calculated. Then, the contributions of M ($C_{(M)}$) and S ($C_{(S)}$) to ET trends can be obtained
 155 as follows:

$$156 \quad C_{(M)} = C_{(\omega)} \times RC_{(M)} \quad (7a)$$

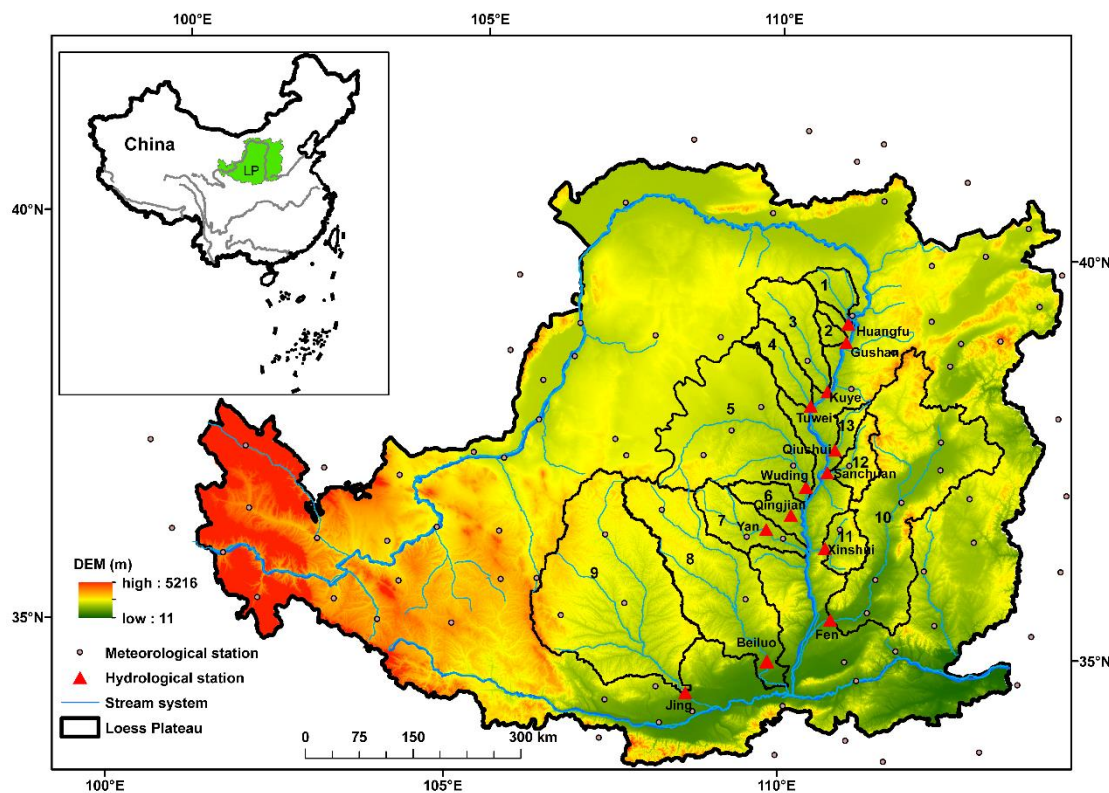
$$157 \quad C_{(S)} = C_{(\omega)} \times RC_{(S)} \quad (7b)$$

158 3. Study area and data

159 The Loess Plateau, which is located in the middle reaches of the Yellow River in China,
 160 experiences a sub-humid and semiarid continental monsoon climate (Liang et al., 2015). Frequent heavy
 161 summer storms, sparse vegetation coverage, easily erodible wind-deposited loess soil, and a long
 162 agricultural history have all contributed to severe drought and soil erosion problems in this region (Li et
 163 al., 2012). To recover and preserve the ecosystem, the Chinese government has launched numerous soil
 164 and conservation measures since the 1950s, and these include biologic measures (“Grain to Green”
 165 Project) and engineering measures (building terraces and sediment trapping dams) (Mu et al., 2007). As



166 a result, the hydrological processes of this area have undergone significant changes (Huang and Zhang,
167 2004; Zhang et al., 2008). Thirteen catchments on the Loess Plateau were selected as our study area
168 (Figure 1).



169
170

Figure 1. Locations of the study area and hydrometeorological stations.

171 Monthly runoff data for the 13 catchments were supplied by the Yellow River Conservancy
172 Commission. Detailed information about the catchment characteristics and data durations are shown in
173 Table 1. Daily meteorological data (1960–2012) comprised of precipitation, daily maximum and
174 minimum temperatures, atmospheric pressures, wind speeds, mean relative humidity values, and
175 sunshine durations, which were recorded at 96 stations, were provided by the China Meteorological
176 Administration. The new NDVI third generation (NDVI3g) dataset was used to represent the vegetation
177 characteristics of the study area, and detailed information about this dataset was presented earlier by



178 Fensholt and Proud (2012). The maximum value compositing (MVC) procedure (Holben, 1986) was
 179 applied to produce the annual NDVI values.

180 Table 1. Long-term hydrometeorological characteristics and vegetation coverage (1981–2012)^a.

ID	Basin	Data length, year	P , mm/yr	ET_0 , mm/yr	ET , mm/yr	ω	M	S
1	Huangfu	32	372	972	347	3.15	0.42	0.94
2	Gushan	25	394	975	359	2.75	0.45	0.79
3	Kuye	32	375	1018	333	2.45	0.43	0.99
4	Tuwei	32	383	1031	308	1.99	0.41	0.95
5	Wuding	32	385	1045	356	2.68	0.46	0.95
6	Qingjian	32	451	1009	417	3.00	0.60	0.60
7	Yan	32	462	984	433	3.21	0.70	0.51
8	Beiluo	28	502	960	475	3.76	0.88	0.34
9	Jing	32	529	936	497	3.74	0.59	0.51
10	Fen	29	465	982	452	4.21	0.87	0.43
11	Xinshui	32	478	992	458	3.77	0.87	0.45
12	Sanchuan	24	444	998	397	2.70	0.57	0.58
13	Qiushui	23	442	1006	418	3.33	0.67	0.60

181 ^aBecause a few runoff data points were missing for several basins, the data length in these basins was less than 32. Each item represents the mean annual value.

182 4. Results

183 4.1. Interannual variability of parameter ω

184 The Budyko framework is usually used for analyses of long-term average data on catchment-scale
 185 water balances; however, in this study, it was employed for the interpretation of the interannual
 186 variability of the water balances by using the hydrological year approach described earlier. To validate
 187 the feasibility of using Fu's equation for interannual variability, the evapotranspiration ratio (ET/P) and
 188 dryness index (ET_0/P) on an annual scale for 13 basins are presented in the supporting information
 189 (Figure S1), and it can be seen that almost all points are focused on Fu's curves in each basin. Therefore,
 190 Fu's equation was considered adequate for the analysis of the interannual variability of the water



191 balance.

192 If the controlling parameter ω on an annual scale can reflect the combined impacts of vegetation
193 change and climate seasonality, it should also exhibit interannual variability with the seasonal variation
194 in vegetation and climate, especially in those catchments affected significantly by climate change and
195 human activities. Obviously, this is true for basins in Loess Plateau (Figure 2). During 1961–2012, ω
196 values in all 13 basins had an upward trend. Along with such a changing trend in ω , ET should
197 increased for the same levels of P and ET_0 . Before the 1980s, the variation in ω for each basin was
198 relatively gentle; however, since that time, it has increased dramatically.

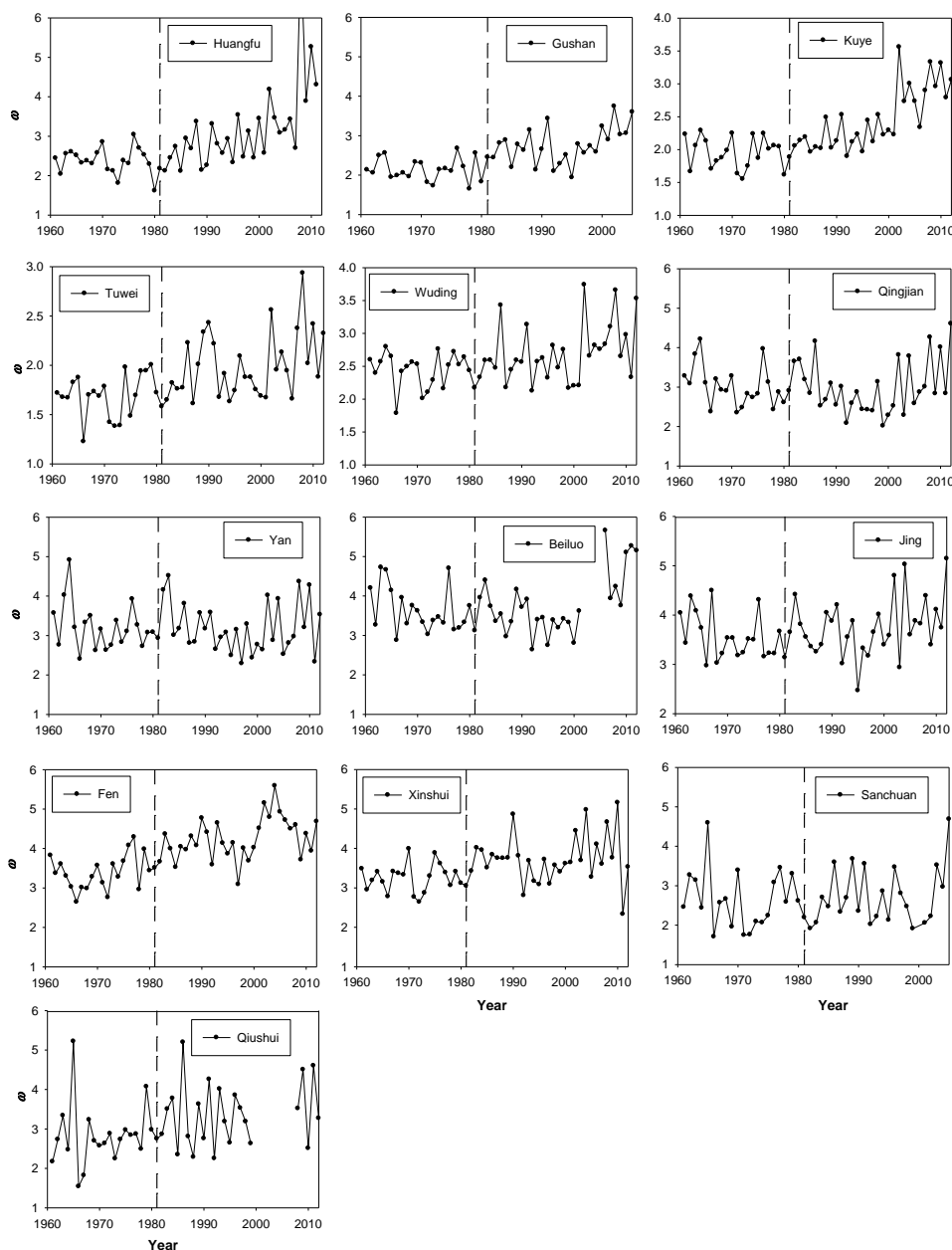


Figure 2. Interannual variability of parameter ω for 13 basins during 1961 to 2012.

4.2. Development of the semi-empirical formula for parameter ω

The relationships between the annual parameter ω and vegetation coverage M as well as the



203 climate seasonality index S were first explored in each study basin during the period 1981–2012, and
204 the results are shown in Figures 3 and 4. We can see that the parameter ω generally had a positive
205 correlation with M , which implies that evapotranspiration increased with improvements in the
206 vegetation conditions. However, ω was correlated negatively with S , which means that larger seasonal
207 variations of coupled water and energy resulted in less evapotranspiration in this area. The relationships
208 between ω and M as well as S imply that the annual variation in parameter ω can be estimated by the
209 changes in vegetation dynamics and climate seasonality.

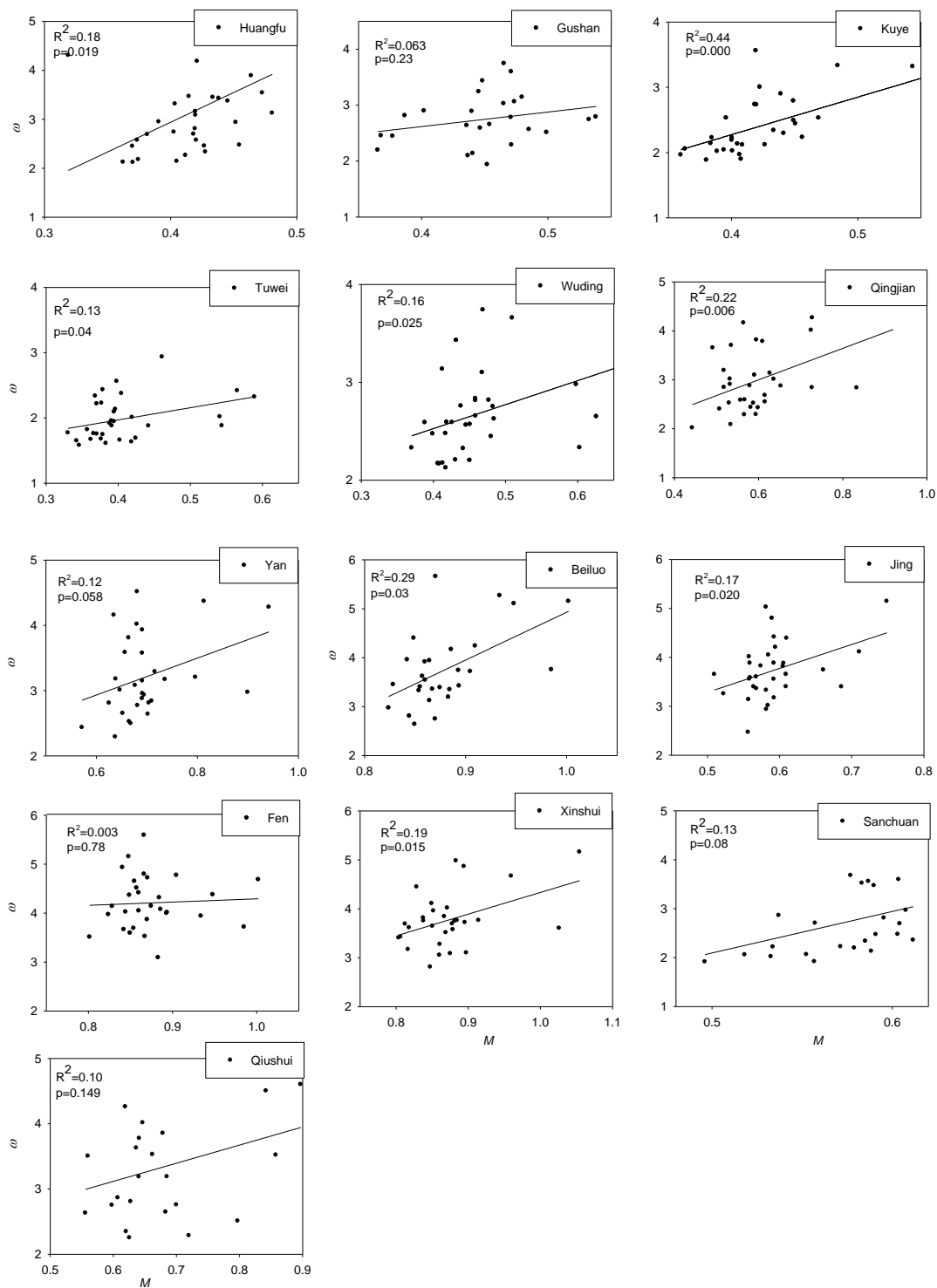


Figure 3. Relationships between the annual ω and vegetation coverage for each basin.

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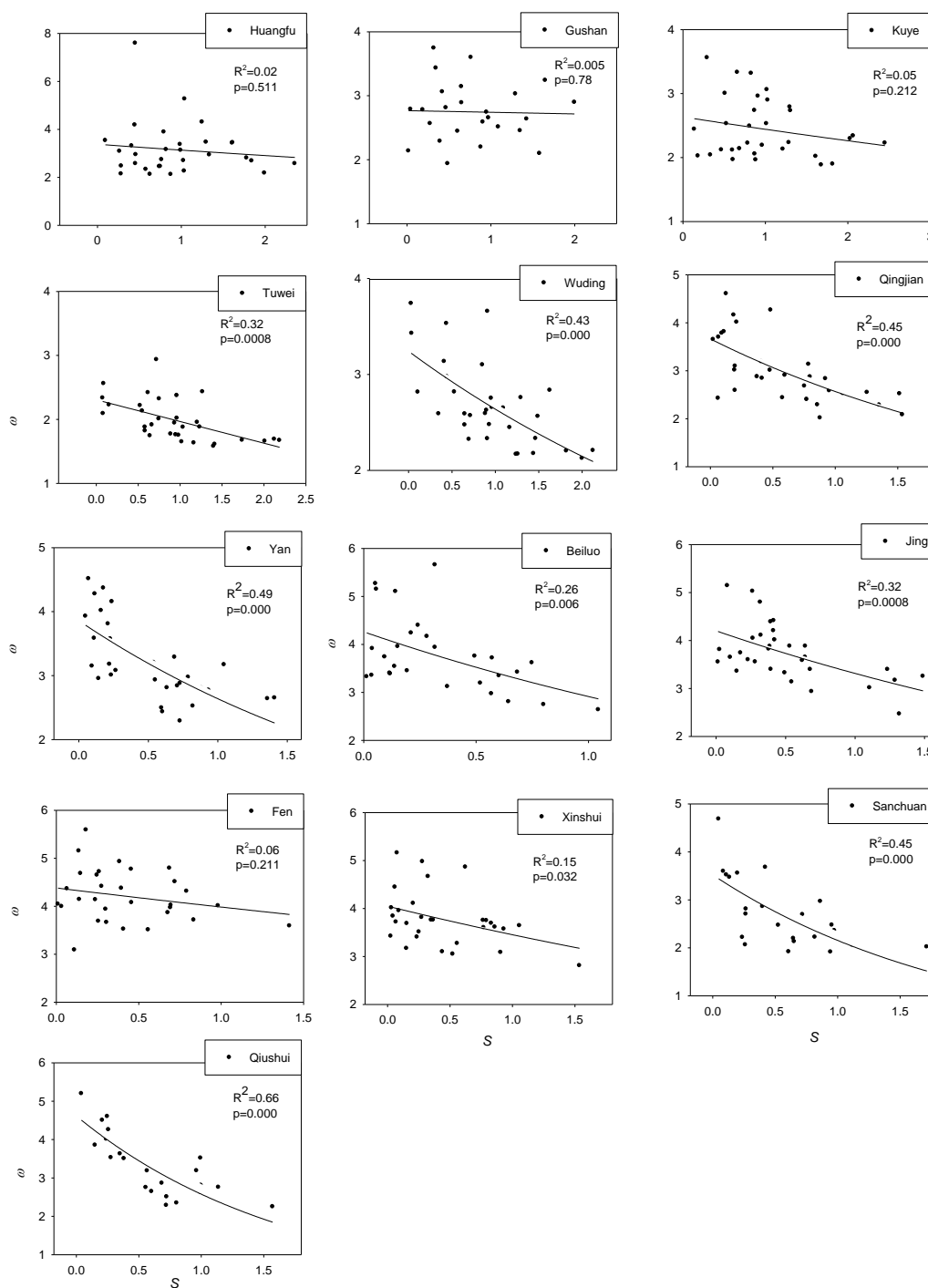


Figure 4. Relationships between the annual ω and climate seasonality index for each basin.

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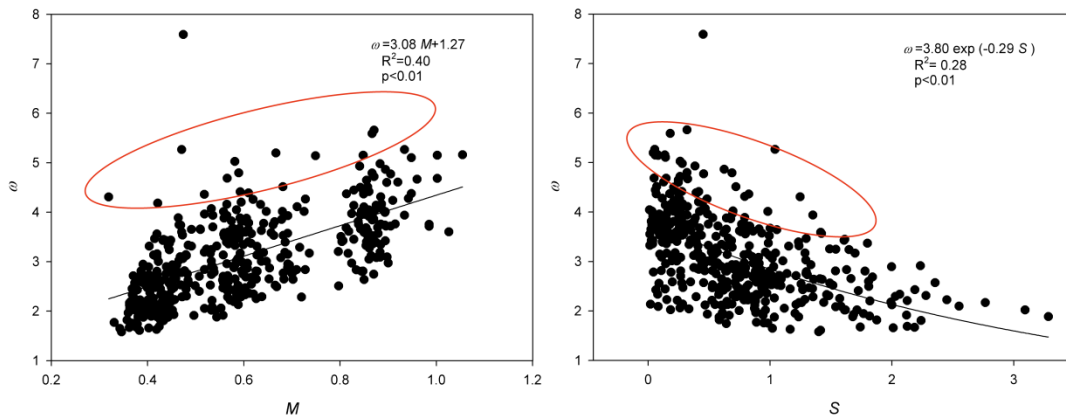
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To expand the sample size and span a wider range of climate conditions, as well as to make the



215 derived semi-empirical formula of parameter ω more representative, relationships were then developed
 216 based on the combined dataset from the 13 basins (Figure 5). These results also indicate a good
 217 relationship between ω and M ($R^2 = 0.40$, $p < 0.01$) as well as S ($R^2 = 0.28$, $p < 0.01$).



218
 219 Figure 5. Relationships between the (a) annual ω and vegetation coverage (M) and (b) ω and climate seasonality
 220 index (S) based on the combined dataset from 13 basins.

221 To develop the semi-empirical formula of parameter ω , the limiting conditions of the two
 222 variables were considered as follows:

- 223 (1) If $M \rightarrow 0$, i.e. the land surface was bare, which indicates that the climate was extremely dry,
 224 $P \rightarrow 0$, $ET \rightarrow 0$, and thus, $\omega \rightarrow 1$;
- 225 (2) If $S \rightarrow \infty$, i.e. P and ET_0 were completely out of phase, which means the total precipitation
 226 within a year was all concentrated within a particular point of time, $R \rightarrow P$, $ET \rightarrow 0$, and
 227 $\omega \rightarrow 1$.

228 Considering the relationships shown in Figure 5 and given the above limiting conditions, the
 229 general form of parameter ω can be expressed as follows:

$$230 \quad \omega = 1 + a \times M^b \times \exp(cS) \quad (8)$$

231 where a , b , and c are constants. Using the least linear square regression method, the semi-empirical



232 formula of parameter ω is derived as follows:

$$233 \quad \omega = 1 + 3.525 \times M^{0.783} \times \exp(-0.218 S) \quad (9)$$

234 The coefficient of determination R^2 and the statistics for the F test of the modelled ω were 0.51 and
 235 218.94, respectively. Thus, incorporation of the climate seasonality index into the semi-empirical
 236 formula of parameter ω improved the estimation of parameter ω by advancing the determining
 237 coefficient (R^2) from 0.45 to 0.51 as compared to the formula that only considered the vegetation
 238 information (see Table 2).

239 Table 2. Analysis of factors affecting parameter ω , as determined by the stepwise regression method.

Variables	R^2	F	Model coefficients		
			Ln a	b	c
<i>M</i>	0.45	336.57	3.32	0.979	
<i>M,S</i>	0.51	218.94	3.525	0.783	-0.218

240 A cross-validation approach was chosen to calibrate and test the above semi-empirical formula for
 241 parameter ω . Specifically, the dataset for the 13 basins in our study was separated into two groups. One
 242 was applied to build the semi-empirical formula, and it consisted of 12 basins for each time; the other
 243 was used for testing the performance of the semi-empirical formula, and it consisted of the remaining 1
 244 basin. In total, the cross-validation process was conducted 13 times. After building the semi-empirical
 245 formula by using the vegetation coverage data and climate seasonality index data for the 12 basins, the
 246 parameter ω for the validated basin was modelled by using this fitted formula, and the annual *ET* for
 247 the validated basin was evaluated with the modelled ω , which is referred to as the “modelled” *ET*. Then,
 248 the “modelled” *ET* was compared with the “measured” *ET*.

249 Table 3 shows the cross-validation results for each basin. The model coefficients of each
 250 calibration formula for parameter ω were very close with the coefficients of Eq. (9). Except for the
 251 Tuwei and Sanchuan basins, the MAE (mean absolute error) and RMSE (square root of the mean square
 252 error) values for each cross-validation process were relative low, with mean values of 13.5 mm and 16.8



253 mm, respectively. The NSE coefficient (Nash–Sutcliffe coefficient of efficiency) for each process was
 254 greater than 0.8, thus suggesting that vegetation changes and climate seasonality can well explain the
 255 interannual variation in the controlling parameter of the catchment water balance.

256 Table 3. Cross-validation results for each basin.

ID	Validated basin	Model coefficients			ET estimation accuracy		
		a	b	c	MAE	RMS	NSE
1	Huangfu	3.597	0.868	-0.228	22.3	23.8	0.88
2	Gushan	3.525	0.787	-0.231	16.3	21.3	0.90
3	Kuye	3.490	0.743	-0.233	17.4	22.7	0.88
4	Tuwei	3.350	0.627	-0.224	33.4	37.5	0.84
5	Wuding	3.525	0.803	-0.211	8.3	12.5	0.97
6	Qingjian	3.525	0.794	-0.206	13.9	18.1	0.96
7	Yan	3.560	0.803	-0.210	11.3	14.0	0.98
8	Beiluo	3.633	0.826	-0.213	10.2	11.9	0.97
9	Jing	3.456	0.814	-0.188	23.1	25.8	0.87
10	Fen	3.421	0.738	-0.223	6.3	8.9	0.98
11	Xinshui	3.560	0.803	-0.216	6.6	9.0	0.99
12	Sanchuan	3.561	0.782	-0.215	25.6	31.0	0.88
13	Qiushui	3.525	0.800	-0.204	12.5	16.4	0.96

257 4.3. Climate seasonality and vegetation coverage contributions to changes in *ET*

258 The impacts of vegetation changes on *ET* have been widely studied with the Budyko framework by
 259 assuming surface conditions can be represented by the controlling parameter. However, according to the
 260 developed relationships in our study, the controlling parameter is not only related to surface condition
 261 change, but also to climate seasonality. The contributions of changes in climate (P , ET_0 , and S) and
 262 vegetation (M) to the changing trend of *ET* were thus estimated by using the semi-empirical formula for
 263 parameter ω in the context of Fu's framework.

264 Trend analyses of the hydrometeorological variables and vegetation coverage were first conducted
 265 for each basin (Table S1). ET_0 , M , and S in all basins exhibited an upward trend, though the significance



266 of the trends were different. In accordance with the method described in Section 2.3, the contributions
 267 of vegetation change and climate seasonality to *ET* trends for each basin were calculated (Table 4). The
 268 changing trend in *ET* was dominated by *P* in the Qingjian, Yan, Beiluo, Jing, Fen and Qiushui River
 269 basins. However, in the Hungfu, Gushan, Kuye, Tuwei, Wuding, and Xinshui River basins, the changing
 270 trend in *ET* was mainly controlled by the improvements in vegetation. Except for the Yan River basin,
 271 improved vegetation in the basins made a positive contribution to the *ET* trend, which is consistent with
 272 the results of Feng et al. (2016). *ET* in several basins showed a downward trend even though *M* made a
 273 positive contribution to the *ET* changes; this was because of the offsetting effect of the other three
 274 factors.

275 It should be noted that the climate seasonality (represented by *S*) played an important role in the
 276 catchment *ET* variation. The contributions of *S* to *ET* changes ranged from 0.1% to 65.6% (absolute
 277 values). Besides the Gushan, Yan, Fen and Sanchuan River basins, the climate seasonality had a
 278 negative effect on *ET* variation in most of the basins, which means that larger seasonality differences
 279 between seasonal water and heat will lead to smaller amounts of evapotranspiration. Accordingly, if
 280 ω is supposed to only represent the landscape condition, the effects of landscape condition change on
 281 *ET* variation will be underestimated in the Huangfu, Kuye, Tuwei, Wuding, Yan, Jing and Xinshui River
 282 basins, while its effects will be overestimated in the other basins, and the error would be equal to the
 283 contributions of *S* to *ET* changes.

284 Table 4. Relative contributions of vegetation change and climate seasonality to *ET* trends for each basin^c.

ID	Basin	<i>ET</i> ₀ , %	<i>P</i> , %	<i>M</i> , %	<i>S</i> , %
1	Huangfu	8.7	30.3	61.0	-0.1
2	Gushan	3.7	24.0	68.8	3.4
3	Kuye	6.4	16.4	80.3	-3.2
4	Tuwei	10.3	21.7	86.5	-18.4
5	Wuding	4.3	31.3	78.7	-14.3
6	Qingjian	-3.0	72.0	-15.8	46.8
7	Yan	-6.5	101.6	9.6	-4.7



8	Beiluo	-7.5	94.0	-0.4	13.8
9	Jing	-9.4	141.9	-47.4	14.2
10	Fen	-10.2	158.6	-18.9	-29.5
11	Xinshui	22.9	-29.6	133.7	-27.0
12	Sanchuan	-2.7	4.2	32.8	65.6
13	Qiushui	-4.8	103.1	-0.1	1.7

285 ^oThe relative contribution of a certain variable to the *ET* trend ($\varphi(x)$) was calculated as follows: $\varphi(x) = (C_{-}(x)/C_{-}(\text{sum})) \times 100\%$, where $C_{-}(x)$ represents the
 286 contribution of each variable, and $C_{-}(\text{sum})$ is the sum of the contributions of the four variables.

287 5. Discussion

288 Although the controlling parameter ω showed a good relationship with the vegetation change and
 289 climate seasonality index, two groups of deviations around the regressed curves were detected (Figure
 290 5). The deviation points for the relationship between ω and M were mainly located at the top of the
 291 curve, i.e. corresponding to the same M values, where ω values were greater. We checked those points
 292 and found that precipitation and vegetation coverage in those years were normal, but runoff was very
 293 low compared to normal years. Excluding abrupt climate change, possible reasons for the extremely low
 294 runoff in those years include dam and reservoir operations, as well as irrigation diversions. A study
 295 conducted by Liang et al. (2015) on the same basins that we investigated in the Loess Plateau showed
 296 that check-dams increased continuously starting from the 1960s. By the year 2006, the numbers of dams
 297 along the Fen River and Wuding River reached up to 482 and 181, respectively. Dams can intercept
 298 stormwater runoff for a short period during flood seasons and allow more time for infiltration (Polyakov
 299 et al., 2014). A total of 21 large and 136 medium-sized reservoirs were installed along the Yellow River
 300 by 2001. Such infrastructure can also influence the runoff change by controlling the flooding, regulating
 301 the water discharge, and diverting the water to other regions (Chen et al., 2005). Agricultural production
 302 is heavily dependent on irrigation throughout the entire Yellow River basin, and it has been reported that
 303 water consumption by agricultural irrigation accounted for nearly 80.0% of the entire water consumed



304 from 1998 to 2011 (Wang et al., 2014). Thereby, water withdrawn for irrigation also plays an important
305 role in the changing trends in runoff. In this study, the deviation points around the relationship curve
306 between the annual ω and S fell in the upper left, and they were likely influenced by the low runoff.
307 However, separation of the impacts on runoff from vegetation change, climate seasonality, and
308 engineering works will have to await future work.

309 The relationships of parameter ω with vegetation dynamics and climate seasonality in some
310 single basins were not significant in this study. Similarly, Yang et al. (2014) also found a weak
311 relationship between parameter n and vegetation coverage in 201 basins in China. This implies that the
312 parameter might represent the combined effects of some other factors. For example, strong interactions
313 among vegetation, climate, and soil conditions will lead to specific hydrologic partitioning at the
314 catchment scale. In dry years, with low soil water contents, plants are trying to adapt by making use of
315 hydrological processes, e.g. ground water dynamics and plant water storage mechanisms, etc. (Renger
316 and Wessolek, 2010). Therefore, the relationship between the parameter and vegetation dynamics can be
317 influenced by climate and soil conditions. However, it is difficult to separate the climatic and soil
318 components from the vegetation change. Moreover, Zhang et al. (2001) reported that the impact of
319 different vegetation types on catchment water balance can be vastly different, and the plant-available
320 water coefficient in their function, which is similar to parameter ω in Fu's equation, is related to
321 vegetation type. Therefore, the vegetation type may also be an important variable that influences the
322 parameter ω .

323 In previous attribution analyses of water balance variation based on the climate elasticity method
324 under the Budyko framework (e.g. (Roderick and Farquhar, 2011; Xu et al., 2014; Liang et al., 2015)),
325 the study period was first divided into two periods based on the breakpoint. Then, the effect of a certain
326 variable (i.e. ET_0 , P , or ω) on the change in annual runoff (R) or ET from the first period to second
327 period was defined as the product of the elasticity coefficient (i.e. ε_P , ε_{ET_0} , or ε_ω) and the variation in



328 the variable for the two periods (i.e. ΔP , ΔET_0 , or $\Delta\omega$). This method can be successfully applied to the
329 attribution analysis of the R or ET variation when the breakpoints of annual R or ET are significant.
330 However, if such a breakpoint does not exist, or if there is more than one breakpoint for the time series
331 of annual R or ET , the uncertainty of this method will be amplified. For example, even if the elasticity
332 coefficients are constant for any sub-period, the ΔP , ΔET_0 , and $\Delta\omega$ will change with the different
333 breakpoints. As a result, the contributions of each variable to R or ET will change as well. In our study,
334 the variations in R or ET over the whole period were first distributed equally to every year, i.e. the
335 change rate of R or ET per year, and then, the attribution analysis was conducted for the average annual
336 variation in R or ET . This two-part method should yield similar results because the total increment of R
337 or ET for the whole study period in our study, i.e. the product of the change rate and study period, is
338 theoretically close to the variation from the two sub-periods in the above method. Take the Kuye River
339 in our study as an example; the relative contributions of P , ET , and parameter ω to the ET variation
340 were 7%, 7%, and 84%, respectively, by using the above previously applied method, while these values
341 with our proposed method were 16%, 6%, and 77%, respectively. The errors mainly were induced by
342 the insignificant breakpoint of the ET series. Thus, the method we used should more applicable and the
343 attribution results more stable because it will not be influenced by the choice of the breakpoint.

344 6. Conclusions

345 This study explored the concomitant effects of vegetation dynamics and climate seasonality on the
346 variation in interannual controlling parameter ω from Fu's equation within the Loess Plateau. First, to
347 reduce the impact of ignoring the water storage change on annual catchment water balance, the
348 hydrological year approach was introduced to examine the interannual variability of the controlling
349 parameter ω for the 13 basins in the Loess Plateau from 1961 to 2012. The findings showed that
350 parameter ω in all these basins presented an increasing trend, especially after the 1980s. Furthermore,



351 we checked the relationship between ω and vegetation dynamics (represented by the annual vegetation
352 coverage, M) as well as climate seasonality (represented by the climate seasonality index, S). The
353 interannual changes of parameter ω were found to be related strongly to M and S . As such, a
354 semi-empirical formula for the annual value of ω was developed based on these two parameters, and it
355 was proven superior for estimating the actual evapotranspiration (ET) by a cross-validation approach.
356 Finally, based on the proposed semi-empirical formula for parameter ω , the contributions of changes in
357 climate (P , ET_0 , and S) and vegetation (M) to ET variations were estimated. The results showed that the
358 improved vegetation conditions in all basins made a positive contribution to the ET trend, but these
359 effects were largely offset by other variables in some basins. The contribution of landscape condition
360 changes to ET variation will be estimated with a large error if the effects of climate seasonality were
361 ignored.

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