



## 1 **Regional soil erosion assessment based on sample survey and** 2 **geostatistics**

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13 **Abstract.** Soil erosion is one of the major environmental problems in China. From 2010-2012 in China, the fourth  
14 national census for soil erosion sampled 32 364 Primary Sampling Units (PSUs, micro watersheds) with the areas  
15 of 0.2-3 km<sup>2</sup>. Land use and soil erosion controlling factors including rainfall erosivity, soil erodibility, slope  
16 length, slope steepness, biological practice, engineering practice, and tillage practice for the PSUs were surveyed,  
17 and soil loss rate for each land use in the PSUs were estimated using an empirical model Chinese Soil Loss  
18 Equation (CSLE). Though the information collected from the sample units can be aggregated to estimate soil  
19 erosion conditions on a large scale, the problem of estimating soil erosion condition on a regional scale has not  
20 been well addressed. The aim of this study is to introduce a new spatial interpolation method based on Bivariate  
21 Penalized Spline over Triangulation (BPST) for the estimation of regional soil erosion. We compared five  
22 interpolation models based on BPST to generate a regional soil erosion assessment from the PSUs. Land use,  
23 rainfall erosivity, and soil erodibility at the resolution of 250×250 m pixels for the entire domain were used as the  
24 auxiliary information. Shaanxi province (3116 PSUs) in China was used to conduct the comparison and  
25 assessment as it is one of the most serious erosion areas. The results showed that three models with land use as the  
26 auxiliary information generated much lower mean squared errors (MSE) than the other two models without land  
27 use. The model assisted by the land use, rainfall erosivity factor (R), and soil erodibility factor (K) is the best one,  
28 which has MSE less than half that of the model smoothing soil loss in the PSUs directly. 56.5% of total land in  
29 Shaanxi province has annual soil loss greater than 5 t ha<sup>-1</sup> y<sup>-1</sup>. High (20-40 t ha<sup>-1</sup> y<sup>-1</sup>), severe (40-80 t ha<sup>-1</sup> y<sup>-1</sup>) and



1 extreme ( $>80 \text{ t ha}^{-1}\text{y}^{-1}$ ) erosion occupied 14.3% of the total land. The farmland, forest, shrub land and grassland in  
2 Shaanxi province had mean soil loss rates of 19.00, 3.50, 10.00,  $7.20 \text{ t ha}^{-1} \text{ y}^{-1}$ , respectively. Annual soil loss was  
3 about 198.7 Mt in Shaanxi province, with 67.8% of soil loss originating from the farmlands and grasslands in  
4 Yan'an and Yulin districts in the northern Loess Plateau region and Ankang and Hanzhong districts in the  
5 southern Qingba mountainous region. This methodology provides a more accurate regional soil erosion  
6 assessment and can help policy-makers to take effective measures to mediate soil erosion risks.

## 7 **1 Introduction**

8 With a growing population and a more vulnerable climate system, land degradation is becoming one of the  
9 biggest threats to food security and sustainable agriculture in the world. Water and wind erosion are the two  
10 primary causes of land degradation (Blanco and Lal, 2010). To improve the management of soil erosion and aid  
11 policy-makers to take suitable remediation measures and mitigation strategies, the first step is to monitor and  
12 assess the related system to obtain timely and reliable information about soil erosion conditions under present  
13 climate and land use. The risks of soil erosion under different scenarios of climate change and land use are also  
14 very important (Kirkby et al., 2008).  
15 Scale is a critical issue in soil erosion modeling and management (Renschler and Harbor, 2002). When the  
16 spatial scale is small, experimental runoff plots, soil erosion markers (e.g. Caesium 137) or river sediment  
17 concentration measurement devices (e.g. optical turbidity sensors) are useful tools. However, when the regional  
18 scale is considered, it is impractical to measure soil loss across the entire region. A number of approaches were  
19 used to assess the regional soil erosion in different countries and regions over the world, such as expert-based  
20 factorial scoring, plot-based, field-based and model-based assessments, etc.  
21 Factorial scoring was used to assess soil erosion risk when erosion rates are not required, and one only need a  
22 spatial distribution of erosion (CORINE, 1992; Guo and Li, 2009; Le Bissonnais et al., 2001). The classification  
23 or scoring of erosion factors (e.g. land use, rainfall erosivity, soil erodibility and slope) into discrete classes and  
24 the criteria used to combine the classes are based on expert experience. The resulting map depicts classes  
25 ranging from very low to very high erosion or erosion risk. Factorial scoring approach has limitations, however,  
26 due to its subjectivity and qualitative characteristics (Morgan, 1995; Grimm et al., 2002). Plot-based approach  
27 extrapolated the measurements from runoff plots to the region (Gerdan et al., 2010; Guo et al., 2015). However,  
28 Gerdan et al. (2010) discussed that the direct extrapolation may lead to poor estimation of regional erosion rates



1 if the scale issue is not carefully taken into consideration. Evan et al., (2015) recommended a field-based  
2 approach combining visual interpretations of aerial and terrestrial photos and direct field survey of farmers'  
3 fields in Britain. However, its efficiency, transparency and accuracy were questioned (Panagos et al., 2015a).  
4 The model-based approach can not only assess soil loss up to the present time, but also has the advantage of  
5 assessing future soil erosion risk under different scenarios of climate change, land use and conservation  
6 practices (Kirkby et al., 2008; Panagos et al., 2015a). USLE (Wischmeier and Smith, 1965; Wischmeier and  
7 Smith, 1978) is an empirical model based on the regression analyses of more than 10,000 plot-years of soil loss  
8 data in the USA and is designed to estimate long-term annual erosion rates on agricultural fields. (R)USLE  
9 (Wischmeier and Smith, 1978; Renard et al., 1997; Foster, 2004) and other adapted versions (for example,  
10 Chinese Soil Loss Equation, CSLE, Liu et al., 2002), are the most widely used models in the regional scale soil  
11 erosion assessment due to relative simplicity and robustness (Singh et al., 1992; Van der Knijff et al., 2000; Lu  
12 et al., 2001; Grimm et al., 2003; Liu, 2013; Bosco et al., 2015; Panagos et al., 2015b). A physically based and  
13 spatially distributed model, the Pan-European Soil Erosion Risk (PESERA) model (Kirkby et al., 2000), is  
14 recommended for use in a policy framework (DPSIR, driving-force-pressure-state-impact-response) in Europe  
15 (Gobin et al., 2004). However, Bosco et al. (2015) and Panagos et al. (2015b) argued that the input data required  
16 by the PESERA model was not always available with sufficient accuracy. Extended RUSLE (e-RUSLE) model  
17 and RUSLE2015 were used instead in the recent water erosion assessment in Europe.

18 The applications of USLE and its related models in the assessment of regional soil erosion can be generally  
19 grouped into three categories. The first category is the area sample survey approach. One representative is the  
20 National Resource Inventory (NRI) survey on U.S. non-Federal lands (Nusser and Goebel, 1997; Goebel, 1998;  
21 Breidt and Fuller, 1999). The NRI survey has been conducted at 5-year interval since 1977, and changed to the  
22 current annual supplemented panel survey design in 2000. The point level soil erosion estimate is produced  
23 based on the USLE before 2007, and RUSLE estimate is produced after 2007. Since a rigorous probability based  
24 area sampling approach is used to select the sampling sites, the design based approach is robust and reliable  
25 when it is used to estimate the soil erosion at the national and state level. However, due to sample size  
26 limitations, estimates at the sub-state level are more uncertain. The second category is based on the  
27 multiplication of seamless grids. Each factor in the (R)USLE model is a raster layer and soil loss was obtained  
28 by the multiplication of numerous factors, which was usually conducted under GIS environment (Lu et al. 2001;  
29 Bosco et al., 2015; Panagos et al., 2015b; Ganasri and Ramesh, 2015; Rao et al., 2015; Bahrawi et al., 2016).

30 Note that the information for the support practices factor (P) in the USLE is not easy to be collected and was not



1 included in some assessments (Lu et al., 2001; Rao et al., 2015), in which the result maps don't reflect the  
2 condition of soil loss but the risk of soil loss. The grid resolutions of factor layers are critical and are determined  
3 by the data resolution used to derive the factor. A European water erosion assessment which introduced  
4 high-resolution (100 m) input layers reported the result that the mean soil loss rate in the European Union's  
5 erosion-prone lands was  $2.46 \text{ t ha}^{-1} \text{ y}^{-1}$  (Panagos et al., 2015b). This work is scientifically controversial mainly  
6 due to questions on these three aspects: (1) Should the assessment be based on the model simulation or the field  
7 survey? (2) Are the basic principles of the (R)USLE disregarded? and (3) Are the estimated soil loss rates  
8 realistic (Evans and Boardman, 2016; Fiener and Auerswald, 2016; Panagos et al., 2016a, b)? The third category  
9 is based on the sample survey and geostatistics. One example is the fourth census on soil erosion in China,  
10 which was conducted during 2010-2012 (Liu, 2013). The fourth census was based on a stratified unequal  
11 probability systematic sampling method (Liu et al., 2013). In total, 32 364 Primary Sampling Units (PSUs) were  
12 identified nationwide to collect factors for water erosion prediction (Liu, 2013). The Chinese Soil Loss Equation  
13 (CSLE) was used to estimate the soil loss for the PSUs, which is the multiplication of seven factors including  
14 rainfall erosivity (R factor), soil erodibility (K factor), slope length (L factor), slope steepness (S factor),  
15 biological practice (B factor), engineering practice (E factor), and tillage practice (T factor) (Liu et al., 2002).  
16 A spatial interpolation model was used to estimate the soil loss for the non-sampled sites.  
17 Remote sensing technique has unparalleled advantage and potential in the work of regional scale soil erosion  
18 assessment (Veirling, 2006; Le Roux et al., 2007; Guo and Li, 2009; Mutekanga et al., 2010; El Haj El Tahir et  
19 al., 2010). The aforementioned assessment method based on the multiplication of erosion factors under GIS  
20 interface was largely dependent on the remote sensing dataset (Panagos et al., 2015b; Ganasri and Ramesh, 2015;  
21 Bahrawi et al., 2016), which also provide important information for the field survey work. For example, NRI  
22 relied exclusively on the high resolution remote sensing images taken from fixed wing airplanes to collect land  
23 cover information. However, many characteristics of soil erosion cannot be derived from remote sensing images.  
24 Other limitations include the accuracy of remote sensing data, the resolution of remote sensing images, financial  
25 constraints and so on, which result in some important factors influencing soil erosion being not available for the  
26 entire domain. Important to note is that the validation is necessary and required to evaluate the performance of a  
27 specific regional soil erosion assessment method, although the validation process is difficult to implement in the  
28 regional scale assessment and is not well addressed in the existing literature (Gobin et al., 2004; Vrieling, 2006;  
29 Le Roux et al., 2007; Kirkby, et al., 2008).  
30 There is an important issue arising in the regional soil erosion assessment based on survey sample, which is how



1 to infer the soil erosion conditions including the extent, spatial distribution and intensity for the entire domain  
2 from the information of PSUs. NRI used primarily a design based approach to estimate domain level statistics.  
3 While robust and reliable for large domains which contain enough sample sites, such method cannot be used to  
4 compute the estimate for the small domain. In the fourth census of soil erosion in China, a simple spatial model  
5 was used to smooth the proportion of soil erosion directly. Land use is one of the critical pieces of information  
6 in the soil erosion assessment (Ganasri and Ramesh, 2015) and some of the erosion factors such as rainfall  
7 erosivity and soil erobility may be provided for the entire domain. The purpose of this study is to compare five  
8 spatial interpolation models based on bivariate penalized spline over triangulation (BPST) method to generate  
9 regional soil loss (A) assessment from the PSUs. The five models are: smoothing A directly (Model I),  
10 estimating A assisted by R and K factors (Model II), estimating A assisted by land use (Model III), estimating A  
11 assisted by R and land use (Model IV) and estimating A assisted by R, K and land use (V). There were 3116  
12 PSUs in the Shaanxi province and its surrounding areas which were used as an example to conduct the  
13 comparison and demonstrate assessment procedures.

## 14 **2 Data and Methods**

### 15 **2.1 Sample and field survey**

16 The design of the fourth census on soil erosion in China is based on a map with Gauss–Krüger projection, where  
17 the whole China was divided into 22 zones with each zone occupying three longitude degrees width (From  
18 central meridian towards west and east 1.5 degrees each). Within each zone, beginning from the central meridian  
19 and the equator, we generated grids with a size of 40 km × 40 km (Fig. 1), which are the units at the first level  
20 (County level). The second level is Township level with a size of 10 km × 10 km. The third level is the control  
21 area, with a size of 5 km × 5 km. The fourth level is the 1 km × 1 km grid located in the middle of the control  
22 area. The 1 km × 1 km grid is the PSU in the plain area, whereas in the mountainous area, a small watershed  
23 with area between 0.2-3 km<sup>2</sup> which also intersects with the fourth level 1 km × 1 km grid is randomly picked as  
24 the PSU. The area for the mountainous PSU is restricted to be between 0.2-3 km<sup>2</sup>, which is large enough for the  
25 enumerator and not too large to be feasible to conduct field work. There is a PSU within every 25 km<sup>2</sup>, which  
26 suggests the designed sample density is about 4%. In practice, due to the limitation of financial resources, the  
27 surveyed sample density is 1% for most mountainous areas. The density for the plain area is reduced to 0.25%  
28 due to the lower soil erosion risk (Li et al., 2012).



1 The field survey work for each PSU mainly included: (1) recording the latitude and longitude information for  
 2 the PSU using a GPS; (2) drawing boundaries of plots in a base map of the PSU; (3) collecting the information  
 3 of land use and soil conservation measures for each plot; and (4) taking photos of the overview of PSUs, plots  
 4 and soil and water conservation measures for future validation. A plot was defined as the continuous area with  
 5 the same land use, the same soil and water conservation measures, and the same canopy density and vegetation  
 6 fraction in the PSU (difference  $\leq 10\%$ , Fig. 2). For each plot, land use type, land use area, biological measures,  
 7 engineering measures and tillage measures were surveyed. In addition, vegetation fraction was surveyed if the  
 8 land use is a forest, shrub land or grassland. Canopy density is also surveyed if the land use is a forest.

## 9 **2.2 Database of PSUs in Shaanxi and its surrounding areas**

10 A convex hull of the boundary of Shaanxi province was generated, with a buffer area of 30 km outside of  
 11 the convex hull (Fig. 3). The raster of R factor, K factor and 1:100000 land use map with a resolution of  
 12  $250 \times 250$  m pixels for the entire area were collected. PSUs located inside the entire area were used, which  
 13 included 1775 PSUs in the Shaanxi province and 1341 PSUs from the provinces surrounding the Shaanxi  
 14 province, including Gansu (430), Henan (112), Shanxi (345), Inner Mongolia (41), Hubei (151),  
 15 Chongqing (55), Sichuan (156) and Ningxia (51). There were 3116 PSUs in total. We had the information  
 16 of longitude and latitude, land use type, land use area and factor values of R, K, L, S, B, E and T for each  
 17 plot of the PSU. The classification system of the land use for the entire area and that for the survey units  
 18 were not synonymous with each other. They were grouped into eight land use types include (1) farmland,  
 19 (2) forest, (3) shrub land, (4) grassland, (5) water body, (6) construction land, (7) bare land and (8) unused  
 20 land such as sandy land, Gebi and uncovered rock to make them corresponding to each other.

## 21 **2.3 Soil loss estimation for the plot, land use and PSU**

22 Soil loss for a plot can be estimated using CSLE equation as follows:

$$23 \quad A_{uk} = R_{uk} \cdot K_{uk} \cdot L_{uk} \cdot S_{uk} \cdot B_{uk} \cdot E_{uk} \cdot T_{uk}, \quad (1)$$

24 where  $A_{uk}$  is the soil loss for the  $k^{\text{th}}$  plot with the land use  $u$  ( $\text{t ha}^{-1} \text{y}^{-1}$ ),  $R_{uk}$  is the rainfall erosivity ( $\text{MJ mm}$   
 25  $\text{ha}^{-1} \text{h}^{-1} \text{y}^{-1}$ ),  $K_{uk}$  is the soil erodibility ( $\text{t ha h MJ}^{-1} \text{ha}^{-1} \text{mm}^{-1}$ ),  $L_{uk}$  is the slope length factor,  $S_{uk}$  is the  
 26 slope steepness factor,  $B_{uk}$  is the biological practice factor,  $E_{uk}$  is the engineering practice factor,  $T_{uk}$  is  
 27 the tillage practice factor.

28 Liu et al. (2013) introduced the data and methods for calculating each factor. Here we present a brief



1 introduction. 2678 weather and hydrologic stations with erosive daily rainfall from 1981 through 2010  
 2 were collected and used to generate the R factor raster map over the entire China (Xie et al., 2016). Soil  
 3 surface attributes for 7764 soil species from the Second National Soil Survey and more than 950 soil  
 4 samples newly collected were used to generate the K factor for the country (Liu et al., 2013). R factor  
 5 raster map for the study area was clipped from the map of the country as well as the K factor raster map.  
 6 A topography contour map with a scale of 1:10000 for each PSU was collected to derive the slope length  
 7 and slope degree and to calculate the slope length factor and slope steepness factor (Fu et al., 2013). A land  
 8 use map with a scale of 1:100000 was used to determine the boundary of forest, shrub, and grass land.  
 9 For these three land use types, MODIS NDVI and HJ-1 NDVI were combined to derive vegetation  
 10 coverage. For the shrub and grass land, an assignment table was used to assign a value of the half-month B  
 11 factor based on their vegetation coverage; For the forest land, the vegetation coverage derived from the  
 12 aforementioned remote sensing data was used as the canopy density, which was combined with the  
 13 vegetation fraction under the trees collected during the field survey to estimate the half-month B factor.  
 14 The B factor for the whole year was weight-averaged by a weight of rainfall erosivity ratio for this  
 15 half-month. The engineering practice factor and tillage practice factor were assigned values based on the  
 16 field survey and assignment tables for different engineering and tillage measures, which were obtained  
 17 from published references (Guo et al., 2015).  
 18 In a PSU, there may be several plots within the same land use. Soil loss for the same land use was  
 19 weight-averaged by the area of the plot:

$$20 \quad A_{ui} = \frac{\sum_{k=1}^q (A_{uik} S_{uik})}{\sum_{k=1}^q S_{uik}}, \quad (2)$$

21 where  $A_{ui}$  is the averaged soil loss for the land use  $u$  in the sample unit  $i$ ;  $A_{uik}$  is the soil loss for the plot  $k$   
 22 with the land use  $u$ ;  $S_{uik}$  is the area for the plot  $k$  with the land use  $u$ .

23 Soil loss for the PSU was estimated by

$$24 \quad A_i = \frac{\sum_{p=1}^N (A_{ip} S_{ip})}{\sum_{p=1}^N S_{ip}}, \quad (3)$$



1 where  $A_i$  is the averaged soil loss for the sample unit  $i$  with  $N$  plots;  $A_{ip}$  is the soil loss for the plot  $p$  and  $S_{ip}$   
2 is the area for the plot  $p$ .

### 3 **2.4 Five spatial models based on BPST method**

#### 4 **2.4.1 Five spatial models**

5 Model I: Estimating  $A$  directly by spatial interpolation. Treat unit  $i$  as a point, using longitude and latitude  
6 information and  $A_i$  value of unit  $i$  to interpolate.

7 Model II: Estimating  $A$  with  $R$  and  $K$  as the auxiliary information. For any sampling unit  $i$ , let

$$8 \quad Q_i = \frac{A_i}{R_i \cdot K_i}, \quad (4)$$

9 where  $R_i$  is the rainfall erosivity value for unit  $i$ , and  $K_i$  is the soil erodibility value for unit  $i$ . By  
10 smoothing  $Q_i$ 's over the domain using longitude and latitude information, we obtain the interpolation of

11  $Q_i$ 's over the entire domain. Then for the  $j^{\text{th}}$  pixel on the domain, we estimate the soil loss  $A_j$  via

$$12 \quad \hat{A}_j = \hat{Q}_j \cdot R_j \cdot K_j, \quad (5)$$

13 where  $\hat{Q}_j$  is the estimator of  $Q_j$ .

14 Model III: Estimating  $A$  with the land use as the auxiliary information. For water body and unused area, the  
15 estimation of soil loss for the  $u^{\text{th}}$  land use and  $j^{\text{th}}$  pixel  $\hat{A}_{uj}$  was set to be zero. For the rest land use types,  $A_{ui}$   
16 for each land use was interpolated separately first and soil loss values for the entire domain  $\hat{A}_{uj}$  are the  
17 combination of estimation for all land uses.

18 Model IV: Estimating  $A$  with  $R$  and land use as the auxiliary information. For any sampling unit  $i$  in land  
19 use  $u$ , define

$$20 \quad T_{ui} = \frac{A_{ui}}{R_{ui}}, \quad (6)$$

21 where  $R_{ui}$  is the rainfall erosivity value. For land use  $u$ , we smooth  $T_{ui}$ 's using the longitude and latitude  
22 information, and obtain the interpolation over the domain. For any  $j^{\text{th}}$  pixel in land use  $u$ , we estimate the  
23 soil loss  $A_{uj}$  by





$$1 \quad \hat{A}_{uj} = \hat{T}_{uj} \cdot R_{uj}, \quad (7)$$

2 where  $\hat{T}_{uj}$  is the estimation of  $T_{uj}$  for the land use  $u$  and the pixel  $j$ .

3 Model V: Estimating  $A$  with  $R$ ,  $K$  and land use as the auxiliary information. For land use  $u$  and sampling

4 unit  $i$ , define

$$5 \quad Q_{ui} = \frac{A_{ui}}{R_{ui} \cdot K_{ui}}, \quad (8)$$

6 where  $K_{ui}$  is the soil erodibility value. For land use  $u$ , smoothing  $Q_{ui}$ 's over the domain, we obtain the

7 estimator  $\hat{Q}_{uj}$  of  $Q_{uj}$  for every pixel  $j$ . Then, for any  $j^{\text{th}}$  pixel in land use  $u$ , we can estimate the soil loss  $A_{uj}$

8 by

$$9 \quad \hat{A}_{uj} = \hat{Q}_{uj} \cdot R_{uj} \cdot K_{uj}, \quad (9)$$

#### 10 **2.4.2 Bivariate penalized spline over triangulation method**

11 Let  $(x_i, y_i) \in \Omega$  be the latitude and longitude of unit  $i$  for  $i = 1, 2, \dots, n$ . Suppose we observe  $z_i$  at

12 locations  $(x_i, y_i)$  and  $\{(x_i, y_i, z_i)\}_{i=1}^n$  satisfy

$$13 \quad z_i = f(x_i, y_i) + \varepsilon_i, i = 1, 2, \dots, n, \quad (10)$$

14 where  $\varepsilon_i$ 's are random variables with mean zero, and  $f(\cdot)$  is some smooth but unknown function. To

15 estimate  $f$ , we adopt the bivariate penalized splines on triangulations to handle irregular domains. In the

16 following we discuss how to construct basis functions using bivariate splines on a triangulation of the

17 domain  $\Omega$ . Details of various facts about bivariate splines stated in this section can be found in Lai and

18 Schumaker (2007). See also Guillas and Lai (2010) and Lai and Wang (2013) for statistical applications of

19 bivariate splines on triangulations.

20 A triangulation of  $\Omega$  is a collection of triangles  $\Delta = \{\tau_1, \tau_2, \dots, \tau_N\}$  whose union covers  $\Omega$ . In addition, if

21 a pair of triangles in  $\Delta$  intersects, then their intersection is either a common vertex or a common edge. For a

22 given triangulation  $\Delta$ , we can construct Bernstein basis polynomials of degree  $p$  separately on each

23 triangle, and the collection of all such polynomials form a basis. In the following, let  $S_r^p(\Delta)$  be a spline

24 space of degree  $p$  and smoothness  $r$  over triangulation  $\Delta$ . Bivariate B-splines on the triangulation are

25 piecewise polynomials of degree  $p$  (polynomials on each triangle) that are smoothly connected across

26 common edges, in which the connection of polynomials on two adjacent triangles is considered smooth if



1 directional derivatives up to the  $r^{\text{th}}$  degree are continuous across the common edge.

2 To estimate  $f$ , we minimize the following penalized least square problem:

$$3 \min_{f \in S^p(\Delta)} (z_i - f(x_i, y_i))^2 + \lambda \text{PEN}(f), \quad (11)$$

4 Where  $\lambda$  is the roughness penalty parameter, and  $\text{PEN}(f)$  is the penalty given below:

$$5 \text{PEN}(f) = \int_{\tau \in \Delta} \left( \frac{\partial^2 f(x,y)}{\partial x^2} \right)^2 + \left( \frac{\partial^2 f(x,y)}{\partial x \partial y} \right)^2 + \left( \frac{\partial^2 f(x,y)}{\partial y^2} \right)^2 dx dy, \quad (12)$$

6 For Models I-V defined in Section 2.4.1, we consider the above minimization to fit the model, and obtain

7 the smoothed surface using the measurements of A (Models I and III) or Q (Models II and V) or T (Model

8 IV) and their corresponding location information.

## 9 2.5 Assessment methods

10 To compare different models, we estimate the out-of-sample prediction errors of each method using the 10-fold

11 cross validation. We randomly split all the observations over the entire domain (with the buffer zone) into ten

12 roughly equal-sized parts. For each  $k = 1, 2, \dots, 10$ , we leave out part  $k$ , fit the model to the other nine parts

13 (combined) inside the boundary with the buffer zone, and then obtain predictions for the left-out  $k^{\text{th}}$  part inside

14 the boundary of Shaanxi Province. In the Model I and Model II,  $\text{MSE}_{\text{overall}}$  is calculated as follows:

$$15 \text{MSE}_{\text{overall}} = \frac{\sum_{k=1}^{10} \text{SSE}_k}{n}, \quad (13)$$

16 In Models III, IV and V, we consider land use as one covariate. Therefore, the overall mean squared prediction

17 error ( $\text{MSE}_{\text{overall}}$ ) is calculated by the average of the sum of the product of individual MSE and the

18 corresponding sample size. The overall  $\text{MSE}_{\text{overall}}$  was calculated as follows: we first calculated the MSE of land

19 each use  $u$ ,  $u = 1, 2, \dots, 8$ , similar as for Model I and Model II,

$$20 \text{MSE}_u = \frac{\sum_{k=1}^{10} \text{SSE}_k}{n}, \quad (14)$$

21 Then, the overall MSE can be calculated using

$$22 \text{MSE}_{\text{overall}} = \frac{\sum_{u=1}^8 \text{MSE}_u \cdot C_u}{\sum_{u=1}^8 C_u}, \quad (15)$$

23 where  $C_u$  is the sample size for the land use  $u$ .

24 Six soil erosion intensity levels were divided according to the soil loss rate, which were mild (less than 5 t

25  $\text{ha}^{-1}\text{y}^{-1}$ ), slight (5-10 t  $\text{ha}^{-1}\text{y}^{-1}$ ), moderate (10-20 t  $\text{ha}^{-1}\text{y}^{-1}$ ), high (20-40 t  $\text{ha}^{-1}\text{y}^{-1}$ ), severe (40-80 t  $\text{ha}^{-1}\text{y}^{-1}$ ), and

26 extreme (greater than 80 t  $\text{ha}^{-1}\text{y}^{-1}$ ), respectively. Each pixel in the entire domain was classified as an intensity

27 level according to  $A_j$  or  $A_{uj}$ . The proportion of intensity levels, soil loss rates for different land uses and the



1 spatial distribution of soil erosion intensity levels were based on the soil erosion conditions of pixels located  
2 inside of the Shaanxi boundary.

### 3 **3 Results**

#### 4 **3.1 Estimation for four models**

5 Table 1 summarized the MSEs of the soil loss estimation based on different methods. Model V generated the  
6 least overall MSE values and the best result. Model II performed better than Model I, and Models IV and V  
7 performed better than Model III, which suggested R and K factors contributed some information. Models III, IV  
8 and V were much better than Model I and Model II, which suggested that land use is the key auxiliary  
9 information for the spatial model, which contributed much more information than R and K factors did.

#### 10 **3.2 Soil erosion intensity levels**

11 These five models can be divided into two groups in the proportion pattern of soil erosion intensity levels (Fig.  
12 4). The first group is two models without the land use as the auxiliary information (Model I and II) and the  
13 second group is three models assisted with the land use (Model III, IV and V). The first group generated no  
14 severe and extreme erosion levels and had a higher proportion of slight and moderate erosion levels than the  
15 second group. The second group generated a higher proportion of mild, severe and extreme erosion levels than  
16 the first group. Most severe and extreme erosion mainly occurred in the farmland and bare land (Fig. 5). The  
17 first group mainly underestimated the erosion degrees for the farmland and bare land and overestimated those  
18 for the forest, grassland and construction land.

19 The result of Model V with BPST method showed that the highest percentage is the mild erosion (43.5%),  
20 followed by the slight (21.3%), moderate (20.9%) and high erosion (10.1%). The severe and extreme erosion  
21 occupied 3.9% and 0.3%, respectively (Fig. 4). When it came to land use (Fig. 5), the largest percentage for the  
22 farmland was the high erosion, which occupied 26.6% of the total farmland. The severe and extreme erosion for  
23 the farmland were 11.3% and 0.9% of the total farmland, respectively. Most forest land and grassland had mild  
24 erosion (75.4% and 42.5%, respectively). Each of mild, slight and moderate erosion degrees occupied about 30%  
25 of the total shrub land.



### 1    **3.3 Soil loss rates for different land uses**

2    Fig.6 showed soil loss rates for different land use generated from five models. Similar to the estimation of soil  
3    erosion intensity levels, the first group mainly underestimated the soil loss rates for the farmland and bare land  
4    and overestimated those for the forest, grassland and construction land. The standard deviations of the farmland  
5    and bare land for the second group were much higher than those for the first group, which suggested the  
6    variation of soil loss rates for farmland and bare land pixels for the second group were greater than for the first  
7    group.

8    The soil loss rate for four main land uses (farmland, forest, shrub land and grassland) by Model V was reported  
9    in Table 2.

### 10    **3.4 Spatial distribution of soil erosion intensity**

11    Five models simulated generally similar spatial patterns of soil erosion intensity (Fig. 7 (a)-(e)). Three models  
12    assisted with the land use (Model III, IV and V) showed more reasonable details (Fig. 7). Fig. 7(e) showed that  
13    severe and extreme soil erosion mainly occurred in the farmlands in the southern Qingba mountainous area.

14    Fig 7(f) demonstrated the difference between Model V and Model I, which suggested Model I overestimated the  
15    erosion intensity levels for most forests and grasslands, whereas it underestimated the intensity of farmlands.

16    The estimation from Model V showed that annual soil loss from Shaanxi province was about 198.7 Mt, 49.8%  
17    of which came from farmlands and 35.0% from grasslands (Table 3). The soil loss rate in Yan'an and Yulin in  
18    the northern part was 15.3 and 11.9 t ha<sup>-1</sup> y<sup>-1</sup> and ranked the highest among ten prefecture cities. About half of  
19    the soil loss for the entire province was from these two districts (Table 3). Ankang and Hanzhong in the  
20    southern part also had a severe soil loss rate and contributed about one quarter of soil loss for the entire  
21    province.

## 22    **4 Discussion**

23    Guo et al. (2015) analyzed 2823 plot-year runoff and soil loss data from runoff plots across five water erosion  
24    regions in China and compared the results with previous research across the world. The results showed that  
25    there were no significant differences for the soil loss rates of forest, shrub land and grassland worldwide,  
26    whereas the soil loss rates of farmland with conventional tillage in northwest and southwest China were much  
27    higher than those in most other countries. Shaanxi province is located in the Northwest region. Soil loss rates for



1 the farmland, forest, shrub land and grassland based on the plot data for the NW region in Guo et al. (2015)  
2 were extracted and presented in Table 2 for comparison. Soil loss rate for the farmland based on the plot data  
3 varied greatly with the management and conservation practices and the result in this study was within the range  
4 (Table 2). The soil loss rate for the shrub land is similar with that reported in Guo et al. (2015). The soil loss rate  
5 for the forest in this study was  $3.50 \text{ t ha}^{-1}\text{y}^{-1}$ , which is much higher than  $0.10 \text{ t ha}^{-1}\text{y}^{-1}$  reported in Guo et al. (2015,  
6 Table 2). The reason may be due to the steeper slope degree and longer slope length for the forest in Shaanxi  
7 province than the plots in Guo et al. (2015). The forest plots in Guo et al. (2015) were with an averaged slope  
8 degree of  $25.9^\circ$  and slope length of 21.1 m, whereas 74.0% of forest lands were with a slope degree greater than  
9  $25^\circ$  and 97.2% of them with a slope length longer than 20 m based on the survey result of PSUs in this study.  
10 The soil loss rate for the grassland in this study was  $7.20 \text{ t ha}^{-1}\text{y}^{-1}$ , which was smaller than  $11.57 \text{ t ha}^{-1}\text{y}^{-1}$   
11 reported in Guo et al. (2015). The reason may be due to the lower slope degree for the grassland in Shaanxi  
12 province. The mean value of the slope degree for grassland plots was  $30.7^\circ$  in Guo et al. (2015), whereas 68.6%  
13 of the grass lands were with a slope degree smaller than  $30^\circ$  from the survey in this study.  
14 Remarkable spatial heterogeneity of soil erosion intensity was observed in the Shaanxi province. The Loess  
15 Plateau region is one of the most severe soil erosion regions in the world due to seasonally concentrated and  
16 high intensity rainfall, high erodibility of loess soil, highly dissected landscape, and long-term intensive human  
17 activities (Zheng and Wang, 2014). Most of the sediment load in the Yellow River is originated and transported  
18 from the Loess Plateau. Recently, the sediment load of the Yellow River declined to about 0.3 billion tons per  
19 year from 1.6 billion tons per year in the 1970s, which benefited from the soil and water conservation practices  
20 taken in the Loess Plateau region (He, 2016). However, more efforts on controlling human accelerated soil  
21 erosion in the farmlands and grasslands are still needed. Soil erosion in southern Qingba mountainous region is  
22 also very serious, which may be due to the intensive rainfall, farming in the steep slopes and deforestation (Xi et  
23 al., 1997). According to the survey in Shaanxi province, 11.1% of the farmlands with a slope degree ranging  
24  $15\text{-}25^\circ$  and 6.3% of them greater than  $25^\circ$  were without any conservation practices. Mountainous areas with a  
25 slope steeper than  $25^\circ$  need to be sealed off for afforestation (grass) without the disturbance of the human and  
26 livestock. For those farmlands with a slope degree lower than  $25^\circ$ , terracing and tillage practices are suggested  
27 which can greatly reduce the soil loss rate (Guo et al., 2015, Table 2).  
28 The survey result showed that there were 26.5% of grasslands with a slope degree of  $15\text{-}25^\circ$  and 57.6% of them  
29 steeper than  $25^\circ$  without any conservation practices. Enclosure and grazing prohibition are suggested on the  
30 grasslands with steep slope and low vegetation coverage.



1 Note that CSLE, as well as USLE-based models, simulate sheet and rill erosion, so erosion from gullies is not  
2 taken into consideration in this study. Erosion from gullies is also very serious in the Loess Plateau area and  
3 there were more than 140,000 gullies with length longer than 500 m in Shaanxi province (Liu, 2013).

#### 4 **5 Conclusions**

5 The regional soil erosion assessment focused on the extent, intensity, and distribution of soil erosion on a  
6 regional scale and it provides valuable information to take proper conservation measures in erosion areas.  
7 Shaanxi province is one of the most severe soil erosion regions in China. A field survey in 3116 PSUs in the  
8 Shaanxi province and its surrounding areas were conducted, and the soil loss rates for each land use in the PSU  
9 were estimated from an empirical model (CSLE). Five spatial interpolation models based on BPST method were  
10 compared in generating regional soil erosion assessment from the PSUs.

11 The model assisted by the rainfall erosivity factor (R), soil erodibility factor (K) and land use (Model V)  
12 generated the best result, with the minimum mean squared error (MSE). R and K factors provided some useful  
13 information, and land use was the key auxiliary information for the spatial geostatistical models in the regional  
14 soil erosion assessment. Three models that included land use generated more reasonable assessment results in  
15 terms of the proportion of soil erosion intensity levels, soil loss rates for different land use and spatial  
16 distribution of soil erosion intensity.

17 Results showed that 56.5% of total land had annual soil loss rate greater than  $5 \text{ t ha}^{-1} \text{ y}^{-1}$  and total annual soil  
18 loss amount was about 198.7 Mt in Shaanxi province. Most soil loss originated from the farmlands and grass  
19 lands in Yan'an and Yulin districts in the northern Loess Plateau region and Ankang and Hanzhong districts in  
20 the southern Qingba mountainous region. Special attention should be given to the 0.11 million  $\text{km}^2$  of lands with  
21 soil loss rate greater than  $5 \text{ t ha}^{-1} \text{ y}^{-1}$ , especially 0.03 million  $\text{km}^2$  of farmlands with severe erosion (greater than  
22  $20 \text{ t ha}^{-1} \text{ y}^{-1}$ ).

23 The sample survey and geostatistics based regional assessment methodology was valuable to identify the soil  
24 erosion area and location. The information collected in the survey and the generated soil erosion degree map  
25 (such as Fig. 7e) can help policy-makers to take suitable erosion control measures in the severely affected areas.  
26 Moreover, climate and management scenarios could be developed based on the database collected in the survey  
27 process to help policy-makers in decision making for managing soil erosion risks.



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## 4 References

- 5 Bahrawi, J. A., Elhag, M., Aldhebani, A. Y., Galal, H. K., Hegazy, A. K., and Alghailani, E.: Soil erosion  
6 estimation using remote sensing techniques in Wadi Yalamlam Basin, Saudi Arabia, *Adv Mater Sci Eng*, in  
7 press, <http://dx.doi.org/10.1155/2016/9585962>, 2016.
- 8 Blanco, H., and Lal, R.: *Principles of Soil Conservation and Management*. Springer, New York, 2010.
- 9 Bosco, C., de Rigo, D., Dewitte, O., Poesen, J., and Panagos, P.: Modelling soil erosion at European scale  
10 towards harmonization, *Nat Hazards Earth Syst Sci*, 15, 225–245, 2015.
- 11 Breidt, F. J., and Fuller, W. A.: Design of supplemented panel surveys with application to the National  
12 Resources Inventory. *J Agr Biol Envir St*, 4, 391–403, 1999.
- 13 Cerdan, O., Govers, G., Le Bissonais, Y., Van Oost, K., Poesen, J., Saby, N., Gobin, A., Vacca, A., Quinton, J.,  
14 Auerswald, K., Klik, A., Kwaad, F. J. P. M., Raclot, D., Ionita, I., Rejman, J., Rousseva, S., Muxart, T.,  
15 Roxo, M. J., and Dostal, T.: Rates and spatial variations of soil erosion in Europe: a study based on erosion  
16 plot data. *Geomorphology*, 122, 167–177, 2002.
- 17 CORINE: Soil Erosion Risk and Important Land Resources in the Southern Regions of the European  
18 Community. European Commission, EUR 13233 EN, Luxembourg, 1992.
- 19 El Haj El Tahir, M., K ääb, A., and Xu, C. Y.: Identification and mapping of soil erosion areas in the Blue Nile,  
20 Eastern Sudan using multispectral ASTER and MODIS satellite data and the SRTM elevation model.  
21 *Hydrol Earth Syst Sci*, 14, 1167–1178, 2010.
- 22 Evans, R., Collins, A. L., Foster, I. D. L., Rickson, R. J., Anthony, S. G., Brewer, T., Deeks, L., Newell-Price, J.  
23 P., Truckell, I. G., and Zhang, Y.: Extent, frequency and rate of water erosion of arable land in  
24 Britain—benefits and challenges for modelling. *Soil Use Manage*, in press, 2015.
- 25 Fiener, P., and Auerswald, K.: Comment on “The new assessment of soil loss by water erosion in Europe” by  
26 Panagos et al. (*Environmental Science & Policy* 54 (2015) 438–447). *Environ Sci Policy*, 57, 140–142,  
27 2016.
- 28 Foster, G. R.: *User’s Reference Guide: Revised Universal Soil Loss Equation (RUSLE2)*. U.S. Department of  
29 Agriculture, Agricultural Research Service, Washington DC, 2004.
- 30 Fu, S. H., Wu, Z. P., Liu, B. Y., and Cao, L. X.: Comparison of the effects of the different methods for  
31 computing the slope length factor at a watershed scale. *Int Soil Water Conserv Res*, 1(2), 64–71, 2013.
- 32 Ganasri, B. P., and Ramesh, H.: Assessment of soil erosion by RUSLE model using remote sensing and GIS - A  
33 case study of Nethravathi Basin. *Geoscience Frontiers*, in press, doi:10.1016/j.gsf.2015.10.007, 2015.
- 34 Gobin, A., Jones, R., Kirkby, M. J., Campling, P., Govers, G., Kosmas, C., and Gentile, A. R.: Indicators for  
35 pan-European assessment and monitoring of soil erosion by water. *Environ Sci Policy*, 7, 25–38, 2004.



- 1 Goebel, J. J.: The National Resources Inventory and its role in U.S. agriculture. *Agricultural Statistics* 2000.
- 2 International Statistical Institute, Voorburg, 1998.
- 3 Grimm, M., Jones, R., and Montanarella, L.: Soil erosion risk in Europe. European Commission, Joint Research
- 4 Centre, EUR 19939 EN, Ispra, 2002.
- 5 Grimm, M., Jones, R., and Montanarella, L.: Soil Erosion Risk in Europe. European Commission, Joint
- 6 Research Centre, EUR 19939 EN, Ispra, 2002.
- 7 Grimm, M., Jones, R., Rusco, E. and Montanarella, L.: Soil Erosion Risk in Italy: a revised USLE approach.
- 8 European Commission, EUR 20677 EN, Luxembourg, 2003.
- 9 Guillas, S., and Lai, M. J.: Bivariate splines for spatial functional regression models. *J Nonparametr Statist*, 22,
- 10 477–497, 2010.
- 11 Guo, Q. K., Hao, Y. F., and Liu, B. Y.: Rates of soil erosion in China: A study based on runoff plot data. *Catena*,
- 12 24, 68–76, 2015.
- 13 Guo, Q. K., Liu, B. Y., Xie, Y., Liu, Y. N., and Yin, S. Q.: Estimation of USLE crop and management factor
- 14 values for crop rotation systems in China. *J Integr Agr*, 14(9), 1877–1888, 2015.
- 15 Guo, S. Y., and Li, Z. G.: Development and achievements of soil and water conservation monitoring in China.
- 16 *Science of soil and water conservation*, 7(5), 19–24, 2009 (in Chinese with English abstract).
- 17 He, C. S.: Quantifying drivers of the sediment load reduction in the Yellow River Basin. *National Sci Rev*, 00,
- 18 1–2, doi: 10.1093/nsr/nww014, 2016.
- 19 Kirkby, M. J., Irvine, B. J., Jones, R. J. A., Govers, G., Boer, M., Cerdan, O., Daroussin, J., Gobin, A., Grimm,
- 20 M., Le Bissonnais, Y., Kosmas, C., Mantel, S., Puigdefabregas, J., and van Lynden, G.: The PESERA
- 21 coarse scale erosion model for Europe. I.–Model rationale and implementation. *Eur J Soil Sci*, 59,
- 22 1293–1306, 2008.
- 23 Kirkby, M. J., Le Bissonnais, Y., Coulthard, T. J., Daroussin, J., and McMahon, M. D.: The development of land
- 24 quality indicators for soil degradation by water erosion. *Agric Ecosyst Environ*, 81, 125–136, 2000.
- 25 Lai, M. J., and Schumaker, L. L.: *Spline functions on triangulations*. Cambridge University Press, Cambridge,
- 26 2007.
- 27 Lai, M. J., and Wang, L.: Bivariate penalized splines for regression. *Statist Sinica*, 23, 1399–1417, 2013.
- 28 Le Bissonnais, Y., Montier, C., Jamagne, M., Daroussin, J., and King, D.: Mapping erosion risk for cultivated
- 29 soil in France. *Catena*, 46(2–3), 207–220, 2001.
- 30 Le Roux, J. J., Newby, T. S., and Sumner, P. D.: Monitoring soil erosion in South Africa at a regional scale:
- 31 review and recommendations. *S Afr J Sci*, 207(103), 329–335, 2007.
- 32 Li, Z. G., Fu, S. H., and Liu, B. Y.: Sampling program of water erosion inventory in the first national water
- 33 resource survey. *Sci Soil Water Conserv*, 10(1), 77–81, 2012 (in Chinese with English abstract).
- 34 Liu, B. Y., Zhang, K. L., and Xie, Y.: An empirical soil loss equation in: *Proceedings–Process of soil erosion*
- 35 *and its environment effect (Vol. II)*, 12th international soil conservation organization conference, Tsinghua
- 36 University Press, Beijing, 21–25, 2002.
- 37 Liu, B. Y., Guo, S. Y., Li, Z. G., Xie, Y., Zhang, K. L., and Liu, X. C.: Sample survey on water erosion in China.





- 1            Soil and Water Conservation in China, 10, 26–34, 2013 (in Chinese with English abstract).
- 2    Liu, Z.: The national census for soil erosion and dynamic analysis in China. *Int Soil Water Conserv Res*, 1(2),  
3            12–18, 2003.
- 4    Lu, H., Gallant, J., Prosser, I. P., Moran, C., and Priestley, G.: Prediction of sheet and rill erosion over the  
5            Australian continent, incorporating monthly soil loss distribution. CSIRO Land and Water Technical  
6            Report, Canberra, 2001.
- 7    Morgan, R. P. C.: *Soil Erosion and Conservation*, Second Edition. Longman, Essex, 1995.
- 8    Mutekanga, F. P., Visser, S. M., Stroosnijder, L.: A tool for rapid assessment of erosion risk to support  
9            decision-making and policy development at the Ngenge watershed in Uganda. *Geoderma*, 160, 165–174,  
10           2010.
- 11   Nusser, S. M., and Goebel, J. J.: The National Resources Inventory: A long-term multi-resource monitoring  
12           programme. *Environ Ecol Stat*, 4(3), 181–204, 1997.
- 13   Panagos, P., Borrelli, P., Poesen, J., Meusburger, K., Ballabio, C., Lugato, E., Montanarella, L., and Alewell, C.:  
14           Reply to “The new assessment of soil loss by water erosion in Europe, Panagos P. et al.: *Environ. Sci.*  
15           *Policy* 54, 438–447—A response” by Evans and Boardman. *Environ Sci Policy*, 58, 11–15, 2015a.
- 16   Panagos, P., Borrelli, P., Poesen, J., Ballabio, C., Lugato, E., Meusburger, K., Montanarella, L., and Alewell, C.:  
17           The new assessment of soil loss by water erosion in Europe. *Environ Sci Policy*, 54, 438–447, 2015b.
- 18   Panagos, P., Borrelli, P., Poesen, J., Meusburger, K., Ballabio, C., Lugato, E., Montanarella, L., and Alewell, C.:  
19           Reply to “The new assessment of soil loss by water erosion in Europe. Panagos P. et al., 2015 *Environ. Sci.*  
20           *Policy* 54, 438–447—A response” by Evans and Boardman [*Environ. Sci. Policy* 58, 11–15]. *Environ Sci*  
21           *Policy*, 59, 53–57, 2016a.
- 22   Panagos, P., Borrelli, P., Poesen, J., Meusburger, K., Ballabio, C., Lugato, E., Montanarella, L., and Alewell, C.:  
23           Reply to the comment on “The new assessment of soil loss by water erosion in Europe” by Fiener &  
24           Auerswald. *Environ Sci Policy*, 57, 143–150, 2016b.
- 25   Rao, E. M., Xiao, Y., Ouyang, Z. Y., and Yu, X. X.: National assessment of soil erosion and its spatial patterns  
26           in China. *Ecosystem Health and Sustainability*, 1(4), 13, doi: 10.1890/EHS14-0011.1, 2015.
- 27   Renard, K. G., Foster, G. R., Weesies, G. A., McCool, D. K., and Yoder, D. C.: Predicting soil erosion by water.  
28           U.S. Department of Agriculture, Agricultural Research Service, Agriculture Handbook 703, Washington  
29           DC, 1997.
- 30   Renschler, C. S., and Harbor, J.: Soil erosion assessment tools from point to regional scales—the role of  
31           geomorphologists in land management research and implementation. *Geomorphology*, 47, 189–209, 2002.
- 32   Singh, G., Babu, R., Narain, P., Bhushan, L. S., and Abrol, I. P.: Soil erosion rates in India. *J Soil Water Cons*,  
33           47 (1), 97–99, 1992.
- 34   Van der Knijff, J. M., Jones, R. J. A., and Montanarella, L.: Soil erosion risk assessment in Europe. European  
35           Commission, EUR 19044 EN, Luxembourg, 2000.
- 36   Vrieling, A.: Satellite remote sensing for water erosion assessment: A review. *Catena*, 65, 2–18, 2006.
- 37   Wischmeier, W. H., and Smith, D. D.: *Predicting Rainfall Erosion Losses: A Guide to Conservation Planning*.  
38           U.S. Department of Agriculture, Agricultural Research Service, Agriculture Handbook 537, Washington



- 1 DC, 1978.
- 2 Wischmeier, W. H., and Smith, D. D.: Predicting rainfall-erosion losses from cropland east of the Rocky  
3 Mountains. U. S. Department of Agriculture, Agricultural Research Service, Agriculture Handbook 282,  
4 Washington DC, 1965.
- 5 Xi, Z. D., Sun, H., and Li, X. L.: Characteristics of soil erosion and its space-time distributive pattern in  
6 southern mountains of Shaanxi province, Bull Soil Water Conserv, 17(2), 1–6, 1997 (in Chinese with  
7 English abstract).
- 8 Xie, Y., Yin, S. Q., Liu, B. Y., Nearing M., and Zhao, Y.: Models for estimating daily rainfall erosivity in China.  
9 J Hydrol, 535, 547–558, 2016.
- 10 Zheng, F. L., and Wang, B.: Soil Erosion in the Loess Plateau Region of China. Tsunekawa A. et al. (eds.),  
11 Restoration and Development of the Degraded Loess Plateau, China, Ecological Research Monographs.  
12 Springer, Japan, doi.10.1007/978-4-431-54481-4\_6, 2014.
- 13



1 **Tables**

2 **Table 1. Mean squared errors of soil loss (A) using bivariate penalized spline over triangulation (BPST)**

Model	Land use and sample size						Overall
	Farmland	Forest	Shrub land	Grassland	Construction land	Bare land	
	1134	1288	573	683	401	32	4111
I	—	—	—	—	—	—	352.5
II	—	—	—	—	—	—	345.5
III	399.7	25.3	45.5	20.0	165.7	4264.6	177.2
IV	404.3	25.3	45.4	19.5	164.5	3691.2	173.8
V	365.4	24.3	38.0	16.3	162.5	3555.1	152.9

3



1 **Table 2. Soil loss rates ( $t\ ha^{-1}y^{-1}$ ) for the farmland, forest, shrub land and grassland by Model V in this study and in**

2 **Northwest region of China from Guo et al. (2015).**

	Land use	Mean	Standard deviation
This study	Farmland	19.00	17.94
	Forest	3.50	2.78
	Shrub land	10.00	7.51
	Grassland	7.20	5.23
Guo et al. (2015)	Farmland (Conventional)	49.38	57.61
	Farmland (Ridge tillage)	19.27	13.35
	Farmland (Terracing)	0.12	0.28
	Forest	0.10	0.12
	Shrub land	8.06	7.47
	Grassland	11.57	12.72

3



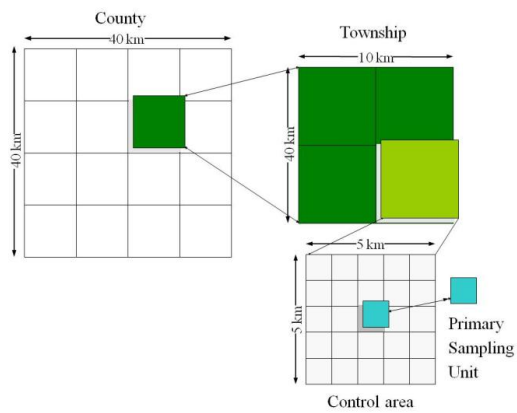
1 **Table 3. Annual soil loss amount, rate and main sources by Model V for ten prefecture cities in Shaanxi province.**

Prefecture city	Area (10 <sup>4</sup> ha)	Amount (10 <sup>6</sup> t y <sup>-1</sup> )	Rate (t ha <sup>-1</sup> y <sup>-1</sup> )	Source (%)			
				Farmland	Forest	Shrub land	Grass land
Xi'an	100.4	6.3	6.3	52.9	11.6	7.9	20.6
Ankang	230.0	26.6	11.6	42.8	10.7	2.8	42.7
Baoji	178.5	13.2	7.4	39.3	15.1	7.5	37.9
Hanzhong	266.7	21.8	8.2	42.5	12.3	3.6	40.2
Shangluo	193.0	8.5	4.4	68.0	13.1	5.9	12.9
Tongchuan	38.6	3.7	9.6	37.9	7.8	23.6	28.5
Weinan	129.5	6.4	5.0	54.4	3.9	9.5	26.7
Xianyang	101.0	5.2	5.2	44.4	8.2	8.9	35.3
Yan'an	364.9	55.9	15.3	54.5	3.1	12.1	30.0
Yulin	427.7	50.9	11.9	51.4	2.6	3.7	40.4
Overall	2030.4	198.7	9.8	49.8	6.8	7.1	35.0

2



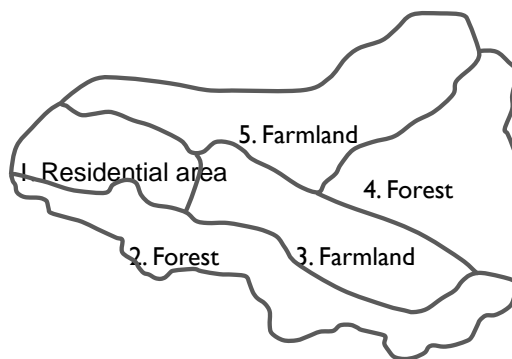
1 **Figures**



2

3 **Figure 1: Schematic of sampling strategy for the fourth census on soil erosion in China**

4



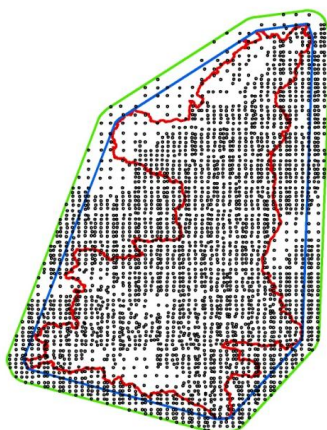
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Figure 2: An example of a PSU with five plots and three categories of land uses.

4



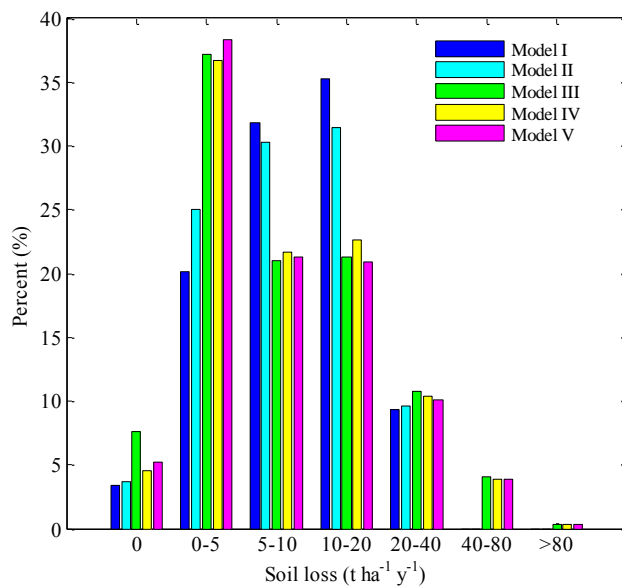
1

2 **Figure 3: Distribution of PSUs (solid dots) used in this study. The red line is the boundary of the Shaanxi province, blue**

3 **line is the convex hull of the boundary and green line is the 30 km buffer of the convex hull.**

4

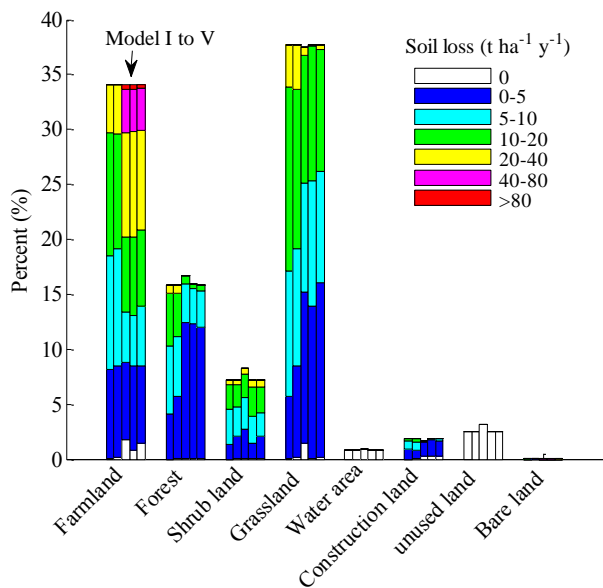




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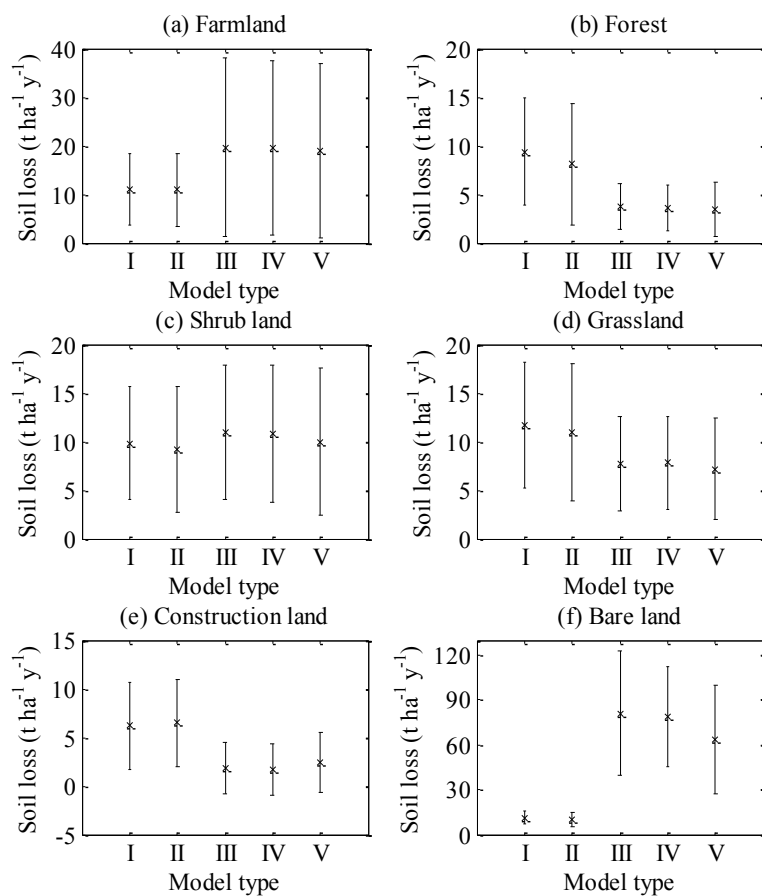
2 **Figure 4: Proportion of soil erosion intensity levels for five models.**

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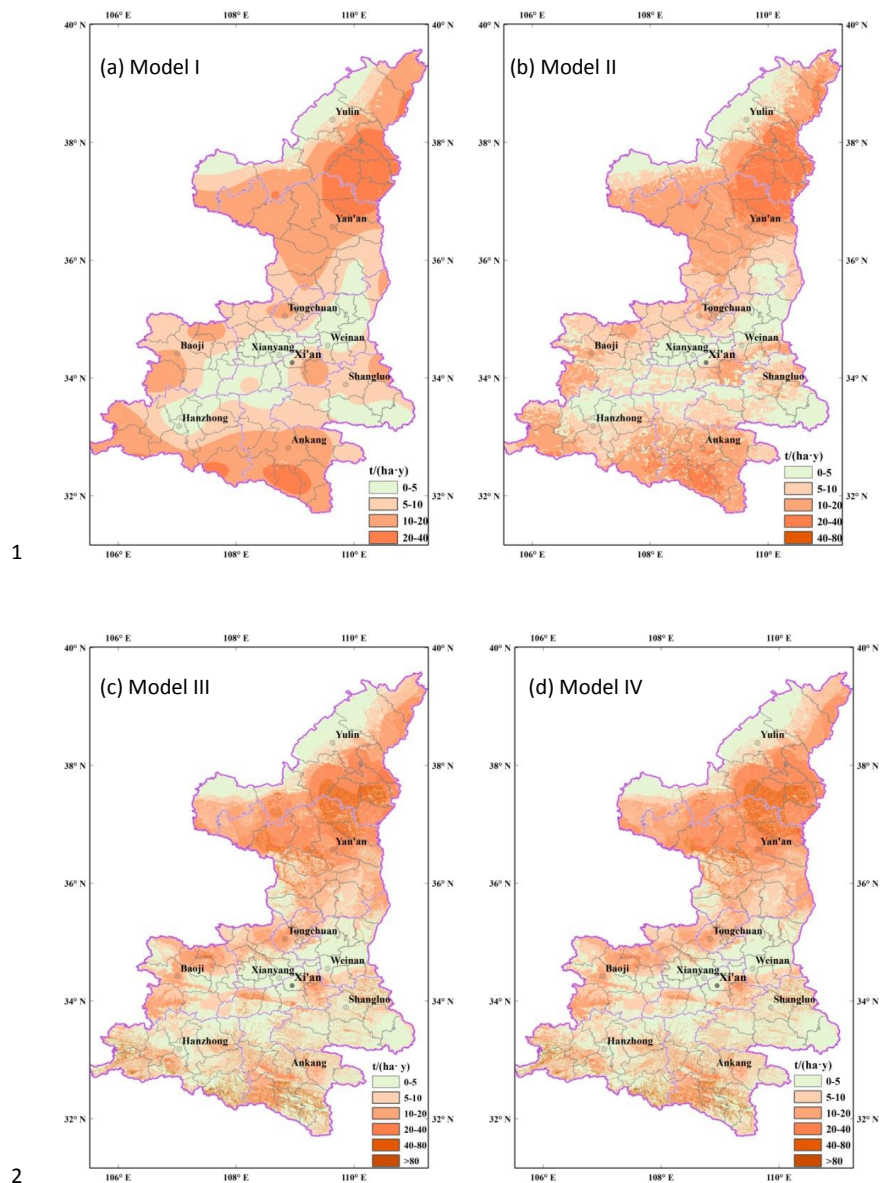
2 **Figure 5: Proportion of soil erosion intensity levels for different land use for five models.**

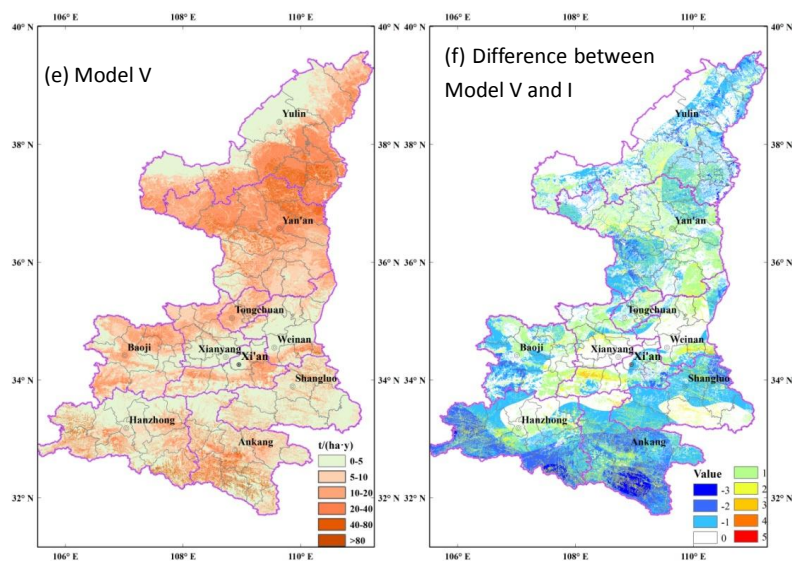


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2 **Figure 6: Error bar plot of soil loss rates for five models for different land uses: (a) Farmland; (b) Forest;**  
3 **land; (d) Grassland; (e) Construction land; (f) Bare land. The star symbols stand for the mean values and the error**  
4 **bars stand for standard deviations.**

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Figure 7: Distribution of soil erosion intensity levels for five models: (a) Model I; (b) Model II; (c) Model III; (d) Model IV; (e) Model V; (f) Difference between Model V and I. The levels of less than 5, 5-10, 10-20, 20-40, 40-80, greater than 80  $t\ ha^{-1}\ y^{-1}$  were defined as the levels 1-6, respectively and the difference was the deviation of levels for Model V from Model I.