

Dear Editor and Reviewers.

We appreciate your constructive comments and thank you for the time spent on reviewing our work. Your comments and suggestions have certainly improved the scope and focus of the manuscript. Please find below our detailed answers to the reviewer comments.

The paper by Jadoon et al. addresses the estimation of parameter error for inversion of electromagnetic induction measurements, using a Bayesian framework. Overall the inversion approach and the Bayesian procedure for parameter error estimation have valid scientific merit. Nevertheless, I have some concerns on the experimental dataset that was used. The structure of the paper needs moderate revisions.

1.1: Specific comments Title. The paper never attempts to calibrate the EC<sub>a</sub> readings to actual salinity estimations. Therefore the title is not reflecting the contents of the paper. EC<sub>a</sub> does not equal to salinity. The interpretation of EC<sub>a</sub> is much more complex. The experimental data of the paper deals with a highly conductive medium (wet & saline soil) and a non-conductive one (dry soil). The results should be therefore discussed in this light.

Reply 1.1:

Indeed, in this paper a relationship was not developed to calibrate the EC<sub>a</sub> readings to actual salinity. In the revised manuscript a relationship that estimates soil salinity from EC<sub>a</sub>, which was previously established in Jadoon et al. WRR (2015) for the same site, is included. The interpretation of EC<sub>a</sub> is complex. Nevertheless, in the saline soil the EC<sub>a</sub> measurement is generally dominated by the soil salinity. A figure related to the soil salinity is included in the revised manuscript (see Figure 9 below) and results are discussed in the context of EC<sub>a</sub> and later soil salinity. For example:

*"Figure 9 shows the spatial distribution of soil salinity estimated from EMI measurement using Bayesian MCMC simulations. Soil salinity EC<sub>e</sub> is related to bulk electrical conductivity  $\sigma_b$  via a linear relationship ( $EC_e = 13.74 \sigma_b + 0.001$ ) established by Jadoon et al. (2015) for the same site. Infiltration front and high soil salinity ranges from 0.01 to 0.5 m at three locations where Acacia trees are irrigated with brackish water. Results show that the Bayesian inversion of multi-configuration EMI measurement permits the estimation of soil salinity caused by the brackish water infiltration. In the field, Acacia roots were concentrated in the top 70 cm of soil and the low soil salinity below 30 cm shows that Acacia are capable of extracting salt solutions and reduce subsoil salinity."*

1.2: L67-78. This is a summary of what's done in the paper. I would rewrite this section featuring what the objectives of the paper are. (If you want to guide the reader through the paper by explaining the workflow, then do it at the beginning of the Materials and methods section.

Reply 1.2:

The final paragraph of the introduction is rewritten as below:

*"Conventional estimation of a single best-fit model with linear uncertainty usually does not trace ambiguity in the models, and may lead to a misguiding or imprecise interpretation. In this work,*

*an adaptive Bayesian MCMC algorithm was used for multi-orientation and multi-offset EMI measurements, in which the parameters posterior distribution represents the complete solution of the Bayesian inversion problem, including prediction of optimal parameters value and the associated uncertainty. Synthetic scenarios were analyzed for a three-layered earth model to evaluate the estimated parameter and uncertainty for saline and non-saline soil using the characteristics of the CMD-Mini Explorer EMI system. Furthermore, field measurements of the CMD-Mini explorer were used to estimate parameter uncertainty in the three-layered earth model and soil salinity distributions in an agricultural field irrigated with drip irrigation system."*

1.3: L79. Start the Materials and methods section by describing the synthetic and experimental data. Currently such descriptions are in the Results and Discussion session: they do not belong there. L98-99

**Reply 1.3:**

Following the suggestion, in the revised manuscript the setup of synthetic and field measurements is incorporated in the Material and Methods section with the subtitle: "Synthetic and Field measurements"

1.4: L99-101- "The electromagnetic forward model, which is based on high induction number assumption, returned more reliable apparent electrical conductivity values than the standard sensitivity curves of McNeill (1980)." This should be moved up (L 82?) and rephrased as: "preliminary analyses indicated that:" L103-108 "Lavoue et al. (2010) and Moghadas et al. (2012) : : : to be a homogeneous half-space." These lines seem a little out of place here. Maybe you should move them to the section where the experimental data is described.

**Reply 1.4:**

The sentence is moved and rephrased as suggested.

1.5: L118 I think you should explain Eq (5) in words so to warrant faster understanding.

**Reply 1.5:**

Following text is incorporated in the revised manuscript:

The equation (5) refers to Bayes law which describes the probability of an event, based on conditions that might be related to the event. One of the many applications of Bayes theorem is Bayesian inference.

1.6: L134 "Here, an informative uniform prior for all five (three conductivities and two thickness) parameters" Describe the parameters earlier on. L135. Awkward wording: maybe a verb is missing? L136. "The problem now reduces to simulate (sample) this posterior." Awkward phrasing: reword the sentence.

**Reply 1.6:**

Line 136 is removed.

1.7: L142-167. This part belongs in the Materials and methods section. L185. pdf (?): define at first appearance

Reply 1.7:

Both paragraphs are moved to the Materials and methods section.

1.8: L204. Experimental data. This is the section that needs the most re-writing. Large portions of this belong in the Materials and methods section. Specific notes. –Pullman is in the state of Washington. (there are other 4 cities with the same name in the USA) - Could not understand the sentence "5TE and EMI measurements were carried out on the same day 8 hr after the drip irrigation system was stopped, so that the soil moisture concentration below the drippers be avoided, and the time be given for the reduction of soil moisture impact due to root water uptake, evaporation and infiltration (Jadoon et al., 2015)."

Reply 1.8:

The entire paragraph is moved to the Material and methods section.

The sentence is rephrased as below:

*"EMI and 5TE measurements were performed 8 h after the drip irrigation system was stopped, to avoid concentrated patterns of soil moisture below the drippers and to allow some time to for evaporative losses, root water uptake and infiltration to reduce the soil moisture impact (Jadoon et al., 2015)."*

1.9: L239 here's my only methodological issue with this paper. You use as non-conductive scenario a soil that is completely dry. (By the way, what are the salinity values measured at this site? E.g., the conductivity of the saturated paste extract?). In their protocols for use of apparent electrical conductivity measurements in agriculture, Corwin and Lesch state that the soil volumetric water content should be at least 50% of the value at field capacity (ideally between 70% and field capacity. Otherwise, the liquid pathways of electrical conductivity through the soils would be interrupted, unpredictably increasing the resistivity of the soil. This is very likely reason why your results on the non-conductive scenario are not encouraging. My criticism is the following: with one scenario where EC<sub>a</sub> is known not to be reliable, is the other scenario (highly conductive medium) enough to provide context to your data analyses? I fear not. I think this paper would make much better of a point if other scenarios (e.g., increasing water contents?) were presented. See: Corwin, D.L., and S.M. Lesch. 2013. Protocols and guidelines for field-scale measurement of soil salinity distribution with EC<sub>a</sub>-directed soil sampling.

J. Environ. Eng. Geophysics 18(1):1-25. and: Corwin, D.L., and S.M. Lesch. 2005b. Characterizing soil spatial variability with apparent soil electrical conductivity: I. Survey protocols. Comput. Electron. Agric. 46(1-3):103-134.

Reply 1.9:

We thank the reviewer for highlighting this important issue. For the same site, Jadoon et al. (2015) reported a relationship to relate bulk electrical conductivity to the soil salinity (i.e., the conductivity of the saturated paste extract). Observed soil salinity range between 3-185 dS/m). As discussed earlier (Reply 1.1), in the revised manuscript same relationship is be used to estimate the soil salinity. Text and Figure 9 is incorporated to show the soil salinity distribution.

Synthetic and field measurements were analysed to test the performance of the electromagnetic forward model in conductive and non-conductive soil, and retrieve soil salinity using Bayesian inversion. In the case of synthetic scenarios, EMI data was generated using electromagnetic forward model and Bayesian inversion was used to estimate five parameters (three layer

electrical conductivities and two layer thicknesses). Result shows that the electromagnetic forward model is not sensitive to the non-conductive soil. Similarly, Minsley (2011) used synthetic data considering the characteristics of shallow ground-based EMI system, geophex GEM-2 and reported that the electromagnetic forward model is less sensitive to the non-conductive soil. Indeed, in the agriculture field the soil electrical conductivity decreases if the soil water content is below 50% of the field capacity, which may cause the less encouraging results for the non-conductive soils. This issue is highlighted in the manuscript and the references of Corwin, D.L., and S.M. Lesch. 2005 and 2013 is incorporate.

In the synthetic scenario of non-saline soil, the increasing trend of soil moisture with depth has been analysed (Figure 1a). While certainly very interesting, undertaking time-lapse EMI measurement with varying soil moisture dynamics is beyond the scope of this current contribution.

1.10: L283-291 this section should be rephrased and moved to the conclusion L292-3006 generally, this section is not a conclusion but a summary.

**Reply 1.3:** Sentences are rephrased and conclusion is improved as suggested.

#### References:

Jadoon K. Z., Moghadas D., Jadoon A., Missimer T., Al-Mashharawi S., and McCabe M. F., 2015. Estimation of soil salinity in a drip irrigation system by using joint inversion of multi-coil electromagnetic induction measurements, Water Resources Research, volume 51, issue 5, page 3490-3504 DOI: 10.1002/2014WR016245

Minsley, B. J.: A trans-dimensional Bayesian Markov chain Monte Carlo algorithm for model assessment using frequency-domain electromagnetic data, Geophysical Journal International, 187, 252–272, 2011.