

1 **Towards simplification of hydrologic modeling:**
2 **identification of dominant processes**

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1 **Abstract**

2 The Precipitation-Runoff Modeling System (PRMS), a distributed-parameter hydrologic
3 model, has been applied to the conterminous United States (CONUS). Parameter sensitivity
4 analysis was used to identify: (1) the sensitive input parameters and (2) particular model
5 output variables that could be associated with dominant hydrologic process(es). Sensitivity
6 values of 35 PRMS calibration parameters were computed using the Fourier Amplitude
7 Sensitivity Test procedure on 110,000 independent hydrologically-based spatial modeling
8 units covering the CONUS and then summarized to process (snowmelt, surface runoff,
9 infiltration, soil moisture, evapotranspiration, interflow, baseflow, and runoff) and model
10 performance statistic (mean, coefficient of variation, and autoregressive lag 1). Identified
11 parameters and processes provide insight into model performance at the location of each unit
12 and allow the modeler to identify the most dominant process on the basis of which processes
13 are associated with the most sensitive parameters.

14 The results of this study indicate that: (1) the choice of performance statistic and output
15 variables have a strong influence on parameter sensitivity, (2) the apparent model complexity
16 to the modeler can be reduced by focusing on those processes that are associated with
17 sensitive parameters and disregarding those that are not, (3) different processes require
18 different numbers of parameters for simulation, and (4) some sensitive parameters influence
19 only one hydrologic process, while others may influence many.

20 **1 Introduction**

21 It has long been recognized that distributed-parameter hydrology models (DPHMs) are
22 complex because of the subtlety and diversity of the hydrologic cycle which they aim to
23 simulate (Freeze and Harlan, 1969; Amorocho and Hart, 1964). In this study, two different
24 aspects of this complexity are addressed:

25 (1) DPHMs have too many input parameters (Jakeman and Hornberger, 1993; Kirchner et al.,
26 1996; Brun et al., 2001; Perrin et al., 2001; McDonnell et al., 2007). In this article,
27 distributed parameters are defined as model inputs that remain constant through time, but can
28 vary spatially across the landscape. Those who apply these models often have difficulty in
29 the understanding of what these parameters are and how they are used in the model.
30 Regularly, there are several parameters that may have similar effect on the computations or
31 may constrain the model in unintended ways (Hrachowitz et al., 2014). Despite the

1 developer's claims that these DPHMs are more or less physically based, often there are not
2 measurements or data sources available for reliable development of all of the input
3 parameters. Duan et al. (2005) describes "a gap in our understanding of the links between
4 model parameters and the land surface characteristics." These unmeasured parameters,
5 ostensibly tangible, are really empirical coefficients when it comes to application and
6 calibration (Samaniego et al., 2010).

7 (2) The output produced by DPHMs is difficult to interpret (Schaeffli and Gupta et al., 2008;
8 Gupta et al., 2009; Gupta et al., 2012; Mayer and Butler, 1993; Ewan, 2011). Often, the
9 meaning of output variables is not always intuitive and results sometimes can seem
10 contradictory (e.g. when streamflow does not seem to correlate with climate information).
11 The result of these complex issues has led to the study of parameter interaction (Clark and
12 Vrugt, 2006) and equifinality (Beven, 2006).

13 Developing effective DPHM applications require that the modeler address these two aspects
14 of complexity at the same time (i.e. the uncertainty problem: "If I am uncertain when
15 estimating input parameters, due to either incomplete or inaccurate information, what effect
16 does it have on the output?"), and the calibration problem: "I know the output I want, which
17 parameters should I change and how much should I change them?") (Chaney et al., 2015;
18 Reusser and Zehe, 2011). While, the user of a DPHM can do nothing about the complexity of
19 the model's internal structure, the apparent complexity can be reduced by limiting the
20 parameters and the affected output under consideration (as described by Jakeman and
21 Hornberger, 1993; Hay et al., 2006).

22 Global parameter sensitivity analysis can determine the degree to which different values of
23 parameters can affect the simulation of certain model outputs (Sanadhya et al., 2013).
24 Furthermore, parameter sensitivity can be evaluated with respect to selected output variables,
25 each representing a different aspect of the hydrologic cycle (hereafter referred to as
26 *processes*). Sensitivity analysis of this form can be used to both identify the input parameters
27 that are the most sensitive (i.e. the parameters that affect the simulation the most) and the
28 dominant process(es) (i.e. those processes which are affected most, by the most sensitive
29 parameters) according to the DPHM.

30 Results of parameter sensitivity analysis can vary spatially (van Werkhoven et al., 2008).
31 Certain parameters can be more or less sensitive at different locations on the landscape. For
32 example, parameters related to simulation of snow can become more sensitive at higher

1 elevations, while parameters related to evaporation can become less sensitive at locations
2 where soil depth and the overall capacity for soil water storage decreases. Consequently, the
3 dominant process(es), as identified by parameter sensitivity analysis of the DPHM, will vary
4 across the landscape as well.

5 Any particular DPHM must necessarily be able to simulate any and all hydrological processes
6 that may occur anywhere on the landscape. However, with the application of a DPHM to a
7 specific site, it can become much less complex when the dominant hydrological process(es)
8 are identified, as not all processes are active to the same degree. The modeling problem
9 becomes less complex to the modeler when hydrological processes not relevant to the
10 modeled domain or watershed are removed from consideration (Wagener et al., 2003; Reusser
11 et al., 2011; Guse et al., 2014; Bock et al., 2015). Related to this, various methods have been
12 developed that will group similar watersheds together for purposes of study (Wolock et al.,
13 2004; Winter, 2001; Ali et al., 2012) or for parameter regionalization (He et al., 2011; Merz
14 and Blöschl, 2004, Seibert, 1999; Vogel 2005). In addition, dominant process concepts have
15 been explored as a way to classify watersheds and natural hydrologic systems for the purpose
16 of simplifying DPHMs by several researchers (Sivakumar and Singh, 2012; Sivakumar et al.,
17 2007). Some have suggested this approach for use as a possible classification framework
18 (e.g. Woods, 2002; Sivakumar, 2004). Pfannerstill et al. (2015) developed a framework for
19 identification and verification of hydrologic process in simulation models on the basis of
20 temporal sensitivity analysis. Cuntz et al. (2015) describe a method of identifying only
21 informative parameters as a screening step in order to reduce the effort required to perform
22 global sensitivity analysis on the full parameter space. McDonnell et al. (2007) discuss the
23 possibility of simplifying hydrologic modeling by identifying “fundamental laws” so that
24 overparameterized models are not needed. However, in our opinion we have not made much
25 progress on that front and DPHMs are, in many ways and for many reasons, more complex
26 than ever.

27 This article describes an approach for identification of sensitive parameters and processes for
28 a modeling application of the conterminous United States (CONUS, Fig. 1). Identification
29 and simulation of regional CONUS sub-watersheds are determined by the resolution of the
30 available information and how the DPHM responds to geophysical (e.g., topography,
31 vegetation and soils) and climatological variation. Specifically, we propose to identify the
32 sensitive parameters and dominant hydrologic process(es), thereby reducing the amount of

1 parameter input and number of output variables to consider (Chaney et al., 2015) and address
2 the two aspects of complexity as described above.

3 **2 Methods**

4 **2.1 Distributed-parameter hydrology model**

5 The U.S. Geological Survey's Precipitation-Runoff Modeling System (PRMS) is the DPHM
6 used in this study. PRMS is a modular, deterministic, distributed-parameter, physical-process
7 watershed model used to simulate and evaluate the effects of various combinations of
8 precipitation, climate, and land use on watershed response. Each hydrologic process
9 simulated by PRMS is encoded in a modular piece of source code (i.e. a "module") and is
10 represented by an algorithm that is based on a physical law (i.e. balance of energy required to
11 melt the ice in a snowpack) or empirical relation with measured or estimated characteristics
12 (i.e. a tank model used to simulate interflow). The reader is referred to Markstrom et al.
13 (2015) for a complete description of PRMS.

14 A fundamental assumption of this study is that PRMS is able to simulate and differentiate
15 hydrologic signals from all the different processes at the scale of the CONUS. Two possible
16 ways to evaluate this are: (1) an analysis of PRMS's internal structure, and (2) the history of
17 PRMS applications. A detailed analysis of PRMS's structure is beyond the scope of this
18 article (see Markstrom et al., 2015); however, PRMS is implemented in a very linear fashion.
19 Each parameter is clearly identified with an equation that is related to simulation of a specific
20 process. Equations are solved sequentially, generally in the order that is defined by water
21 moving through the hydrologic cycle, starting from the atmosphere as precipitation and
22 moving through the rivers as streamflow. The outputs of one equation may be used as inputs
23 to subsequent equations. All of the inputs for a particular equation are required before that
24 equation can be solved. This interdependency in equations can lead to parameter interaction
25 in the simulation of subsequent processes (as described by Beven, 1989; Grayson et al., 1992;
26 Yilmaz et al., 2008; Pfannerstill et al., 2015). For example, parameters related to distribution
27 of temperature and solar radiation may show correlation with each other when evaluated with
28 respect to simulation of evapotranspiration despite these parameters not being explicit terms
29 in the evapotranspiration equations. Past studies indicate that PRMS has been very useful in
30 water-resource and research studies across the CONUS (Battaglin et al., 2011; Boyle et al.,
31 2006; Hay et al., 2011; Markstrom et al., 2012) and is capable of matching measured data

1 (Bower, 1985; Cary, 1991; Dudley, 2008; Koczo et al., 2011) in a variety of geophysical and
2 climatological settings.

3 To define the spatial domain for the CONUS application of PRMS, the locations of major
4 river confluences, water bodies, and stream gages have been georeferenced. Approximately
5 56,000 stream segments are used to connect these locations. Using these stream segments,
6 the left and right bank areas that contribute runoff directly to each segment have been
7 identified, resulting in approximately 110,000 irregularly shaped hydrologic response units
8 (HRUs) of various sizes (500 m² to 14,000 km²) (Viger and Bock, 2014). These HRUs are
9 derived by their geographic and topographic location, affecting their extent and resolution.
10 The CONUS application is forced with values of daily precipitation and daily maximum and
11 minimum air temperature from the DAYMET data set (Thornton et al., 2014). The climate
12 information covers a time period from 1980-2013 on a daily time step, but a shorter period
13 (1987 – 1989 used for warmup, and 1990 – 2000 used for evaluation) was used in this study.

14 **2.2 Calibration parameters**

15 The version of PRMS used in this study has 108 input parameters. A parameter is defined as
16 an input value that does not change over the course of a simulation run. Of these parameters,
17 most would never be modified from their initial values (hereafter referred to as *non-*
18 *calibration parameters*, see Viger, 2014) because they are (1) computed directly from digital
19 data sets through the use of a geographic information system (e.g. land-surface
20 characterization parameters), (2) boundary conditions (e.g. parameters to adjust daily
21 precipitation and daily air temperature forcings), or (3) model configuration options (e.g. unit
22 conversions and model output options). This leaves 35 parameters under consideration for
23 improved model performance, hereafter referred to as *calibration parameters* (Table 1). Each
24 parameter is used within a PRMS code module that simulates a single hydrologic process in
25 PRMS. The output variables of one module may be used as input variables to other modules.
26 It is through these connections that calibration parameters associated with a PRMS module
27 may affect the results of other modules.

28 **2.3 Hydrologic processes**

29 PRMS produces more than 200 output variables that indicate the simulated hydrologic
30 response of a watershed through time (Markstrom et al., 2015, see Table 1-5). In this study,

1 eight of these output variables have been selected to represent the response of major
2 hydrologic processes at the HRU resolution. These processes are: (1) snowmelt (PRMS
3 output variable *snowmelt*) – the amount of water that has changed from ice to liquid and
4 becomes either surface runoff or infiltrates into the soil zone of the HRU; (2) surface runoff
5 (*sroff*) – water from a rainfall or snowmelt event that travels quickly over the land surface
6 from the HRU to the connected stream segment; (3) infiltration (*infil*) – the sum of rain and
7 snowmelt that passes into the soil zone of the HRU; (4) soil moisture (*soil_moist*) – the
8 storage state that represents the amount of soil water in the soil zone above wilting point and
9 below total saturation in the HRU; (5) evapotranspiration (*hru_actet*) – the total actual
10 evapotranspiration lost from canopy interception, snow sublimation, and soil and plant losses
11 from the root zone; (6) interflow (*ssres_flow*) – shallow lateral flow in the unsaturated zone to
12 the connected stream segment; (7) baseflow (*gwres_flow*) – the component of flow from the
13 saturated zone to the connected stream segment; and (8) runoff (*hru_outflow*) – the total flow
14 from the HRU contributing to streamflow in the connected stream segment. It is assumed that
15 these eight output variables are representative of the processes typically considered in
16 hydrological studies with DPHMs. Details of how these processes are simulated by PRMS
17 are described by Markstrom et al. (2015).

18 **2.4 Performance statistics**

19 For DPHMs, there are many different performance measures that have been developed for
20 different purposes (Krause et al., 2005; Gupta et al., 2008; Gupta et al., 2009; Mendoza et al.,
21 2015a; Mendoza et al., 2015b). Because this study is an analysis of model sensitivity, the
22 performance measures need only track changes in model output and do not necessarily need
23 to include observed measurements. Consequently, performance statistics can be developed
24 for processes that are not normally evaluated by performance measures. Archfield et al.
25 (2014) demonstrated that seven fundamental daily streamflow statistics (FDSS) can be used to
26 group streams by similar hydrologic response and tend to provide non-redundant information.
27 In this study, all seven FDSS were computed for each of the eight PRMS time series output
28 variables corresponding to the processes. For the purpose of illustration, this article focuses
29 on three of the FDSS: (1) mean; (2) coefficient of variation (CV); and (3) the autoregressive
30 lag-one correlation coefficient (AR-1). In an intuitive sense, these three statistics can be
31 thought to represent changes in total volume, “spikiness” or “flashiness”, and day-to-day

1 timing, respectively. These performance statistics are computed on the daily time series of
2 the process variables for the 10-year evaluation period.

3 **2.5 FAST analysis**

4 Parameter sensitivity analysis measures the variability of model output given variability of
5 calibration parameter values. This is determined by partitioning the total variability in the
6 model output or change in performance statistics to individual calibration parameters (Reusser
7 et al., 2011). The Fourier Amplitude Sensitivity Test (FAST) (Schaibly and Shuler, 1973;
8 Cukier et al., 1973; Cukier et al., 1975; Saltelli et al., 2006) was selected for this study
9 because it has been demonstrated that it can efficiently estimate non-linear hydrologic model
10 parameter sensitivity (Guse et al., 2014; Pfannerstill et al., 2015; Reusser et al., 2011). FAST
11 is a variance-based global sensitivity algorithm that estimates the first-order partial variance
12 of model output explained by each calibration parameter (hereafter referred to as *parameter*
13 *sensitivity*). Specifically, this first-order variance is the variability in the output that is directly
14 attributable to variations in any one parameter and is distinguishable from higher order
15 variances associated with parameter interactions. An important caveat is that these higher
16 order variances are not accounted for in the analysis. It is assumed that first-order partial
17 variance is sufficient to identify sensitive parameters. This same assumption, as applied to
18 process identification, may be more problematic. If there are sets of interactive sensitive
19 parameters that have not been identified, then the associated process(es) will not be identified
20 as such.

21 Selected parameters are varied within defined ranges at independent frequencies among
22 different model runs. FAST identifies the variability of parameter sensitivities and their
23 ranks, by means of their contribution to total power in the power spectrum. FAST has been
24 implemented as the ‘fast’ library in the statistical software R (Reusser et al., 2011; Reusser,
25 2013; R Core Team, 2015) in two parts. In the first part, the user identifies the calibration
26 parameters and respective value ranges for the test, then FAST generates sets of test
27 calibration parameter values (hereafter referred to as *trials*). Calibration parameter values are
28 varied across the trials according to non-harmonic fundamental frequencies. The user then
29 runs the DPHM for each trial and computes corresponding performance statistics. Then the
30 user runs the second part of the FAST package that performs a Fourier analysis of the
31 performance statistics over the trial space looking for the frequency signatures associated with
32 each calibration parameter.

1 The FAST methodology results in a simple procedure for computing parameter sensitivities
2 on an HRU basis for all the CONUS. The steps in this process are as follows:

3 1. Assign appropriate ranges for the 35 calibration parameters (Markstrom et al., 2015; as
4 in LaFontaine et al., 2013).

5 2. Run the first part of the FAST procedure (as described above) to develop over 9000
6 unique parameter sets, comprised of value combinations for the calibration
7 parameters. The total number and content of these parameter sets, and the results from
8 their simulation by PRMS are completely determined by the first part of the FAST
9 procedure in order to investigate the trial space. Each of the prescribed simulations
10 are independent of each other so they can run in parallel on a computer cluster.

11 3. Compute the FDSS based performance statistics (mean, CV, and AR-1) for each
12 process.

13 4. Run the second part of the FAST procedure (as described above) using output from
14 step 3, resulting in PRMS parameter sensitivities, at each HRU, for the 56
15 combinations of seven performance statistics and eight processes (plus totals).

16 **3 Results**

17 **3.1 Parameter sensitivity by process and performance statistic**

18 Figure 2 shows parameter sensitivity as a set of maps ordered by process and performance
19 statistic. This illustrates the spatial variability in parameter sensitivity and the importance that
20 choice of performance statistic can make in terms of evaluation of hydrologic response. In
21 these maps, the HRUs are colored according to the parameter sensitivity, which is computed
22 by summing the first-order sensitivity for all 35 parameters separately for each of the 8 output
23 variables, each corresponding to their respective process. These sums do not necessarily sum
24 to one, and then scaling each individual category of modeled process and performance
25 statistic to total sensitivity. This summed sensitivity across the parameters, by each category
26 is hereafter referred to as *cumulative parameter sensitivity*. Parameter sensitivity associated
27 with process (column labeled “Process average” in Figure 2) are averaged across all of the
28 parameter sensitivity values computed for the different performance statistics, while
29 parameter sensitivity associated with the performance statistics (last row labeled
30 “Performance statistic average” in Figure 2) are averaged across all of the parameter

1 sensitivity values computed for the different processes. These categories are indicated by
2 their position in the rows and columns in Figure 2. When looking at a single performance
3 statistic for a single process, the cumulative parameter sensitivity can vary from near 0.0
4 (white colored HRUs) to near 1.0 (black colored HRUs). Low values in these maps indicate
5 that there are no parameters that can be changed in any way to affect the performance statistic
6 (this situation is hereafter referred to as an *inferior process*). Likewise, each HRU has a
7 cumulative sensitivity value (i.e. the sum of all of the partial sensitivities for each process).
8 The process with the largest sum on an HRU is referred to as the *dominant process* for that
9 HRU.

10 An example of an inferior process is clearly seen in the case of the mean of the snowmelt
11 process in the southern CONUS HRUs. This is because the occurrence of snow in these areas
12 is very infrequent. Also, there were HRUs for which the value of some performance statistics
13 were mathematically undefined for certain processes (e.g. AR-1 and CV for the baseflow and
14 snowmelt processes). These cases occur when the output variable representing the process
15 does not change at all through time, regardless of the parameter values, and are extreme
16 examples of inferior processes. Likewise, a clear example of a dominant hydrologic process
17 is the CV of interflow in the Intermountain West region of the CONUS (Figs. 1 and 2). This
18 means that for these HRUs, there exist some calibration parameters that can be varied that
19 affect this process to a very high degree.

20 Also apparent from Figure 2 is that there are clear spatial patterns in the parameter sensitivity
21 on the basis of the geographical features of the CONUS. Generally, many of the maps show
22 a sharp break in parameter sensitivity between mountain ranges and comparatively lower
23 elevations, northern contrasted with southern latitudes, and humid versus arid climates.
24 Specific contrasts can be seen in several maps such as when examining the Humid Midwest
25 as opposed to the Great Plains regions and the Pacific Coastal areas and the Desert Southwest
26 region of the CONUS (Fig. 1). Additionally, topographic features of the landscape are
27 prominent (e.g. elevation for interflow), while in other maps, climate considerations seem to
28 dominate (e.g. snowmelt). Another specific example is that the mean of each process, which
29 indicates the ability of any parameter(s) to change the total volume of water during a
30 simulation, seems to have a low sensitivity band in the Great Plains region for all processes
31 except for snowmelt (Fig. 1). This band of low sensitivity has been noted in other modeling
32 studies (Newman et al., 2015; Bock et al., 2015).

1 **3.2 Parameter count required to parameterize each process**

2 To identify the expected count of parameters required to parameterize a particular process,
3 cumulative parameter sensitivity across all HRUs of the CONUS has been computed and
4 plotted (Fig. 3(a)—(h)). The sensitivity level accounted for by the most sensitive parameter,
5 regardless of which parameter it is, for all HRUs across the CONUS is plotted in position 1 on
6 the X axis of each of these plots (Fig. 3(a)—(h)). Then, cumulative sensitivity is plotted for
7 the parameter in rank 2, and so on, until the cumulative sensitivity of all 35 calibration
8 parameters is accounted for. The plots in Figure 3(a)—(h) show that far fewer than the full 35
9 parameters are needed to account for most of the parameter sensitivity. In fact, to account for
10 90% of the parameter sensitivity, this count varies from a low value of just over two for
11 snowmelt to an average high value of over 9 for runoff in selected HRUs.

12 The actual count of calibration parameters required to account for 90% of the parameter
13 sensitivity varies by process and region, as shown by the maps in Figure 3(i)—(p). These
14 maps were generated by counting the number of parameters required to obtain the 90%
15 cumulative sensitivity level for each HRU. For example, Figure 3(o) indicates that for the
16 baseflow process between three and nine parameters are needed to account for 90% of the
17 parameter sensitivity in the various HRUs across the CONUS, with the higher count needed
18 in mountainous, Great Lakes, and New England regions. The maps also indicate that between
19 two (Fig. 3(i)) to 13 parameters (Fig. 3(k, n, and p)) are required for parameterization of these
20 processes. This analysis indicates that more parameters are needed to simulate the
21 components of streamflow (e.g. baseflow, interflow, and surface runoff) than processes that
22 do not result directly in flow (e.g. snowmelt, evapotranspiration, and soil moisture). In
23 addition, simulated processes that are identified as being sensitive to parameters with which
24 they are not normally associated with, may indicate that these processes are a convolution of
25 other processes, consequently making parameters sensitive that are not normally sensitive.

26 Visually, these maps (Fig. 3(i)—(p)) indicate that HRU calibration parameter counts vary
27 regionally. For most processes, higher parameter counts are seen in the more mountainous
28 regions of the Cascade, Sierra Nevada, Rocky, Ozark, and Appalachian mountains, although
29 this is true to a much lesser extent for the evapotranspiration and soil moisture processes
30 (Figs. 3(m) and 3(l)). Higher values also seem prevalent in the New England and Great Lake
31 regions (Fig. 1). This result seems to indicate that, no matter which part of the hydrologic

1 cycle is simulated, more parameters are required in these regions. In contrast, low parameters
2 counts seem prevalent in the Great Plains and Desert Southwest regions.

3 Finally, Figure 3 illustrates the extent to which it is possible to decompose the parameter
4 estimation problem into a sub-set of independent problems, and hence reduce the
5 dimensionality of the inference problem and avoid the troublesome nature of parameter
6 interactions. By considering a single (or reduced set of) processes and performance statistic
7 categories at a time, the sensitive parameter space can be substantially reduced. It also
8 illustrates that there is a strong spatial component to this decomposition. In order to make the
9 information presented in Figure 3 more useful for DPHM application, the particular sensitive
10 parameters have been determined for each HRU by ranking the calibration parameters by
11 sensitivity for each category of process and performance statistic for each individual HRU
12 and is summarized by counting the occurrence of each parameter across the HRUs and
13 ranking them within their respective category of process and performance statistic (Table 2).
14 To address the issue of the spatial variability of these parameters, the percentage of the total
15 number of HRUs for which that parameter is sensitive is shown as the number in parentheses
16 after the parameter name in Table 2. Higher percentage values would indicate that the
17 corresponding parameter is sensitive across more of the CONUS. Refer to Table 1 for a
18 complete description of these parameters.

19 When looking at the categorical parameter lists of Table 2, it is expected that different
20 parameters would associate with different processes (i.e. along a column), but it is surprising
21 to see how different the parameter lists are for different performance statistics (moving across
22 a row) for the same process. An example of this is the baseflow process: the baseflow
23 coefficient (PRMS parameter *gwflow_coef*) is the most sensitive parameter for performance
24 statistics s CV and AR1, but is not even in the list of sensitive parameters for the performance
25 statistic related to the mean of the process. This implies that this parameter is influential for
26 affecting the timing of baseflow, while it does not have any effect on the total volume of
27 baseflow.

28 Further inspection of Table 2 indicates that some calibration parameters occur in many of the
29 24 categories (8 processes times 3 performance statistics), while some parameters do not
30 occur at all. A count of how many times each parameter occurs provides insight into how
31 many process/performance statistic combinations that particular parameter influences. To
32 investigate this for the CONUS application, another view of the information in Table 2 is

1 shown in Figure 4. The 25 sensitive calibration parameters from Table 2 are listed on the y-
2 axis of Figure 4, ranked by order of the number of times that they appear in the
3 process/performance statistic categories. Furthermore, each appearance is indicated by an
4 adjacent circle. Independent of the number of times a parameter occurs within a category
5 (number of circles), the color of the circle visually indicates the proportion of the CONUS
6 HRUs that are affected by that parameter. Specifically, a red circle indicates that more HRUs
7 are affected, while blue indicates that fewer HRUs are affected.

8 Figure 4 shows that three specific parameters affect 18 or more process/performance statistic
9 categories; seven parameters affect seven to 14 categories, and 15 specific parameters affect
10 one to five categories. Finally, of the 35 parameters studied, 10 are never used for any
11 combination of process and performance statistic (Table 2 and Fig. 4). It is apparent from
12 Figure 4, that for the CONUS application of PRMS, the parameters affecting the most process
13 categories are *soil_moist_max* (maximum available water holding capacity), *jh_coef* (Jensen-
14 Haise air temperature coefficient), and *dday_intcp* (intercept in degree-day solar radiation
15 equation). Because these parameters affect so many categories, modelers would be wise to
16 invest their resources in developing the best values possible for these parameters to avoid
17 unintended parameter interaction during calibration. Ideally, these parameters could be
18 estimated from reliable external data and set for the model and not calibrated. The parameters
19 that affect the least number of process categories (aside from the parameters that are never
20 sensitive) are *cecn_coef* (convection condensation energy coefficient), *ssr2gw_exp*
21 (coefficient in equation used to route water from the soil to the groundwater reservoir),
22 *emis_noppt* (emissivity of air on days without precipitation), *potet_sublim* (fraction of
23 potential evapotranspiration that is sublimated), and *slowcoef_lin* (slow interflow routing
24 coefficient). Ideally, these parameters could be set to default values since there is limited
25 value in calibrating them.

26 Also apparent from Figure 4 is that there are many parameters between these two extreme
27 groups. Parameters like *smidx_coef* (soil moisture index for contributing area calculation) can
28 appear in several process categories, without any high rankings, while there are other
29 parameters like *slowcoef_sq* (slow interflow routing coefficient) that appear in relatively few
30 process categories, but have high rankings. This behavior may be due to the vertical routing
31 order (i.e. processes that occur nearer to the surface happen before the deeper ones) of the
32 associated processes (Yilmaz et al., 2008; Pfannerstill et al., 2015). In PRMS, the process of

1 partitioning of precipitation into either direct surface runoff or infiltration (controlled directly
2 by parameter *smidx_coef*) is “faster” and occurs in the vertical routing order before the
3 process of interflow generation (controlled directly by parameter *slowcoef_sq*). These
4 parameters may be the best candidates for calibration because they are sensitive, while at the
5 same time interaction across processes is perhaps limited.

6 **3.3 Identification of dominant and inferior processes by HRU**

7 To identify the dominant and inferior process(es) by geographic area, the following procedure
8 is done for each HRU:

- 9 1. The parameter sensitivity scores are summed for each parameter, resulting in a score
10 for each parameter for each time series output variable and performance statistic.
- 11 2. The parameter scores are averaged by performance statistics, resulting in a score for
12 each process.
- 13 3. The process scores are ranked for each HRU.
- 14 4. The top (and bottom) ranked process determines the most dominant (and most
15 inferior) single process for each HRU as shown in Figure 5.

16 Generally, Figure 5(a) shows that evapotranspiration is the most prevalent dominant process
17 for the CONUS. This is probably because it is a major component of the hydrologic cycle
18 and sensitive parameters are available to affect it in every HRU. However, this is not
19 universal, and the dominant process varies by geographic region, with snowmelt being the
20 dominant process in the northern Great Plains and northern Rocky Mountains, total runoff
21 being the most important in the Pacific Northwest, and with interflow important in bands
22 across the Intermountain West (Fig. 1). Each process is dominant somewhere depending on
23 local conditions. Equally informative are the locations of the most inferior processes (Fig.
24 5(b)). This clearly shows that PRMS snowmelt parameters are not sensitive across the
25 Central Valley of California, and in the Deep South and the Southwestern United States (Fig.
26 1). Areas where runoff is more dominant than evapotranspiration, as in the Cascade
27 Mountains and coastal areas of the Pacific Northwest, are locations where the runoff is a
28 substantially greater part of the water budget. Interestingly, infiltration and baseflow appear
29 to be equally inferior across most of CONUS, with pockets of HRUs that are insensitive to

1 soil moisture, surface runoff, and interflow, depending on local conditions. There are no
2 HRUs that rank evapotranspiration as the most inferior process.

3 Dominant and inferior processes can be identified for HRUs at the watershed scale as well.
4 Figure 5(c) shows the most dominant process by HRU for the Apalachicola – Chattahoochee–
5 Flint River watershed in the Southeastern United States. This watershed has been the subject
6 of previous PRMS modeling studies (LaFontaine et al. 2013). When using this information at
7 a finer resolution, it shows that evapotranspiration is the most dominant process watershed
8 wide, but with pockets of HRUs in the northern part of the watershed where runoff is the most
9 dominant and a pocket in the southern part of the watershed where infiltration is most
10 dominant. Likewise, the most inferior process for each HRU is identified in Figure 5(d). This
11 clearly indicates that parameters and performance statistics related to snowmelt, and to a
12 lesser degree baseflow do not need to be considered when modeling this watershed. Figure
13 5(d) also indicates, that in the northern part of the watershed, infiltration and runoff are
14 inferior processes as well, which could in part be due to impervious conditions around the
15 Atlanta metropolitan area.

16 **4 Discussion**

17 **4.1 Causes of parameter sensitivity**

18 There are regions where parameter sensitivity is typically high for a particular performance
19 statistic (e.g. New England region [Fig. 1] for performance statistic based on mean of
20 processes) or typically low (e.g. Great Plains region [Fig. 1] for mean of processes) regardless
21 of the process (Fig. 2). Why do the HRUs of some regions exhibit parameter sensitivity to
22 almost all processes, while others exhibit parameter sensitivity to almost none? All other
23 things being equal, there can only be two sources of these spatial patterns:

- 24 1. The physiography that is used to define the non-calibration parameters (e.g. elevation,
25 vegetation type, soil type) renders all calibration parameters insensitive. A theoretical
26 example of this could be if an HRU is characterized as entirely impervious, resulting
27 in the non-existence of any simulated soil water.
- 28 2. Patterns in the climate data used to drive the model (e.g. daily temperature and
29 precipitation) could control model response. A theoretical example of this could be an
30 HRU that receives no precipitation. The hydrologic response of the HRUs in either
31 case would always remain unchanged, regardless of changes in any parameter value.

1 In either case, these sources of information are independent of the DPHM and could lead to
2 the conclusion that the dominant processes identified by the methods outlined in this article
3 could correspond to perceptible dominant processes in the physical world (i.e. how the “real
4 world” works).

5 The number of unique calibration parameters for each process in Table 2 (i.e. counting the
6 parameters across each row) may provide some insight into the complexity of each process as
7 represented in the model structure of PRMS. In theory, more “complicated” hydrologic
8 processes would require more parameters for parameterization than the “simpler” ones.
9 According to this view, runoff (16 calibration parameters), infiltration (12 calibration
10 parameters), and interflow (12 calibration parameters) are the most complex processes to
11 simulate, with soil moisture (4) being the simplest. Baseflow (11 calibration parameters),
12 snowmelt (11 calibration parameters), surface runoff (10 calibration parameters), and
13 evapotranspiration (8 calibration parameters) are in between. This reflects the fact that in
14 PRMS, runoff is a much more complicated calculation with many of the other processes
15 directly contributing information. Also apparent is that more parameters are needed to
16 simulate the components of streamflow (e.g. baseflow, interflow, and surface runoff) than
17 processes that do not result directly in flow (e.g. snowmelt, evapotranspiration, and soil
18 moisture). The only process that does not follow this pattern is infiltration. Storm-event
19 based infiltration is typically simulated with sub-daily time steps to account for the
20 time/intensity variability of this process. It is possible that PRMS must compensate for this
21 shortcoming in structure with a more complex parameterization of the process.

22 Table 2 indicates that there are 10 calibration parameters that are never sensitive regardless of
23 the process or performance statistic. This indicates that these parameters should always be set
24 to the default value, with minimal resources used to estimate them, and never be calibrated.
25 Additional modeling studies could reveal situations where these parameters actually do
26 exhibit some sensitivity, perhaps in situations with smaller geographical domains or over
27 different time periods. It is also possible that these parameters are never sensitive, indicating
28 some structural problem or unwarranted complexity in the DPHM and the removal of some
29 algorithms from the source code of the DPHM is advised. Additional study is required of
30 these 10 non-sensitive calibration parameters and upon further review of the PRMS source
31 code, a structural problem (e.g. unintended constraint, non-differentiable behavior, or
32 software bug) might be revealed. Alternatively, the problem could be related to invalid

1 parameter ranges in the FAST analysis or problems with the climate data used to drive the
2 model. Finally, it could be that alternative or improved performance statistics could resolve
3 this issue.

4 **4.2 Choice of performance statistic**

5 The maps of Figure 2 clearly illustrate the importance that choice of performance statistic can
6 make in terms of evaluation of hydrologic response. When the maps of performance statistics
7 within a single hydrologic process are compared (i.e. the maps across a single row), the
8 spatial patterns and magnitude of the parameter sensitivity can be very different. This could
9 indicate that the performance statistics based on the FDSS truly are non-redundant and are
10 accounting for different aspects of the processes.

11 Table 2 indicates that the baseflow coefficient (PRMS parameter *gwflow_coef*, Markstrom et
12 al., 2015) is the most sensitive parameter for performance statistics CV and AR1, but not
13 sensitive to the mean of the baseflow process performance statistics. This points to the fact
14 that despite having knowledge of a parameter being associated with the computation of a
15 certain process, sensitivity analysis can reveal that the response of the simulation is
16 completely different when the performance statistic changes. It also indicates that sensitivity
17 analysis might be an important step in selection of an appropriate performance statistic and
18 that uncritical application of performance statistics may be misleading.

19 **4.3 Spatial aspects of dominant and inferior processes**

20 When the dominant and inferior processes are determined for an HRU (Fig. 5), it is possible
21 that certain parameters are included in both the most dominant dominate and most inferior
22 processes at the same time. This apparent contradiction is not necessarily a conflict but
23 indicates that the calibration parameters must work in concert with the evaluation method.
24 For example, there exist HRUs where the evapotranspiration process is dominant and at the
25 same time the runoff or infiltration processes are inferior (Fig. 5(a) and 5(b)). The parameter
26 *soil_moist_max* is indicated as being sensitive for all three of these processes (Table 2). This
27 parameter would demonstrate equifinality if evaluated within the context of the inferior
28 processes (i.e. those output variables and performance statistics associated with the inferior
29 process) but would be a very effective calibration parameter resulting in optimal values when
30 viewed within the context of parameters and variables of the dominant process.

1 This method of identification of inferior and dominant processes for a specific geographical
2 location (i.e. HRU, watershed, or region), determined by sensitivity analysis, is defined within
3 the context of the application of the DPHM and may not necessarily have the same meaning
4 within a different context. However, this methodology does have the ability to spatially
5 classify watersheds and identify dominant processes. This classification scheme depends not
6 only on the physiographic nature of the watershed, but also on the scale, resolution, and
7 purpose that were considered by the modeler when the application was developed.

8 **4.4 Further study**

9 Providing modelers with reduced lists of calibration parameters on an HRU-by-HRU,
10 watershed-by-watershed, or region-by-region basis is the first step in the path of this research.
11 Subsequent steps to this approach could be developed into more sophisticated methods where
12 orthogonal output variables and performance statistics could provide much more insight into
13 methods of effective model calibration. Other advancements in this approach may identify
14 groups of parameters that effectively behave together, thus reducing the number of parameters
15 and making specific model output respond more directly to a single or a few parameters,
16 reducing parameter interaction. This suggests that model parameterization and calibration
17 might benefit from a step-by-step strategy, using as much information as possible to set non-
18 interactive parameters and remove them from consideration before the more interactive
19 parameters are calibrated, reducing the dimensionality of the problem (Hay et al., 2006; Hay
20 and Umemoto, 2006).

21 Another question for future research is: Does the classification of dominant hydrologic
22 processes, both geographical and categorical, as described in this study, apply in other
23 contexts? Comparable findings from other modeling studies, such as those by Newman et al.
24 (2015) and Bock et al. (2015), might indicate that there could be a connection. These other
25 studies use the same input information (i.e. being driven with the same climate data and using
26 the same sources of information for parameter estimation), and thus simulation results and
27 model sensitivity to this information might be similar. Also, can real world watersheds be
28 classified by sensitivity analysis using DPHMs? Based on the findings of the work presented
29 so far, the answer is inconclusive. Clearly there are some results that indicate that it might be
30 possible. For example, the methods described here effectively identify “snowmelt
31 watersheds” in the mountainous and northern latitudes, but, is all of this necessary to

1 accomplish this? Might simpler methods (e.g. an isohyetal snowfall map) identify snowmelt
2 watersheds just as effectively?

3 Questions remain about using parameter sensitivity for identification of structural
4 inadequacies within the CONUS application and specifically the PRMS model itself. A full
5 analysis of these parameters and how they relate to their respective process(es) is beyond the
6 scope of this article, but it could relate information about the structure of PRMS. In this
7 study, certain hydrologic processes (e.g. depression storage, streamflow routing, flow through
8 lakes, and strong groundwater/surface-water interaction) were not considered because of
9 additional data requirements and parameterization complexity. The PRMS model also allows
10 for selection of alternative methods for many of the module types. Each of these modules
11 uses different equations and calibration parameters. Future work might be to determine the
12 effect of using different modules or maybe even to determine the selection of the PRMS
13 modules through sensitivity analysis. Just as the spatial and temporal scope of any modeling
14 project must be defined, the scope of the hydrologic processes, and the detail to which these
15 processes are simulated, must be likewise defined. Also, alternative ways of defining HRUs
16 (e.g. larger or smaller, or even based on dominant process instead of geographic location)
17 could affect the analysis. Model development and application could perhaps proceed by first
18 accounting for those factors that have the most effect.

19 **5 Conclusion**

20 Watersheds in the real world clearly exhibit hydrologic behavior determined by dominant
21 processes based on geographic location (i.e. land surface conditions and climate forcings). A
22 methodology has been developed to identify regions, watersheds, and HRUs according to
23 dominant process(es) on the basis of parameter sensitivity response with respect to a
24 distributed-parameter hydrology model. The parameters in this model were divided into two
25 groups – those that are used for model calibration and those that were not. A global
26 parameter sensitivity analysis was performed on the calibration parameters for all HRUs
27 derived for the conterminous United States. Categories of parameter sensitivity were
28 developed in various ways, on the basis of geographic location, hydrologic process, and
29 model response. Visualization of these categories provides insight into model performance,
30 and useful information about how to structure the modeling application should take advantage
31 of as much local information as possible.

1 By definition, an insensitive parameter is one that does not affect the output. Ideally, a
2 distributed-parameter hydrology model would have just a few calibration parameters, all of
3 them meaningful, each controlling the algorithms related to the corresponding process. This
4 would result in low parameter interaction and a clear correspondence between input and
5 output. However, this is not always the case, and despite the fact that parameter interaction is
6 unavoidable in these types of models, this behavior is also seen in the real world. For
7 instance, in watersheds where evaporation is very high, antecedent soil moisture is affected,
8 which has a direct influence on infiltration. The real world process of evaporation has an
9 effect on infiltration, just as evaporation parameters have an effect on simulation of
10 infiltration in watershed hydrology models. Application of distributed-parameter hydrologic
11 modeling application require that the uncertainty problem and the calibration problem be
12 addressed at the same time. While, the user of a DPHM can do nothing about the complexity
13 of the model's internal structure, the apparent complexity can be reduced by limiting the
14 parameters and the affected output under consideration.

15 Results of this study indicate that it is possible to identify the influence of different hydrologic
16 processes when simulating with a distributed-parameter hydrology model on the basis of
17 parameter sensitivity analysis. Factors influencing this analysis include geographic area,
18 topography, land cover, soil, geology, climate, and other unidentified physical effects.
19 Identification of these processes allows the modeler to focus on the more important aspects of
20 the model input and output, which can simplify all facets of the hydrologic modeling
21 application.

22

1 **Data availability**

2 The Precipitation-Runoff Modeling System software used in this study is developed,
3 documented, and distributed by the U.S. Geological Survey. It is in the public domain and
4 freely available from their web site (<http://wwwbrr.cr.usgs.gov/prms>). Data analysis and
5 plotting is done with the R software package (<http://www.r-project.org>), which is freely
6 available, subject to the GNU General Public License.

7 The climate forcing data set used in this study came from the U.S. Geological Survey Geo
8 Data Portal (<http://cida.usgs.gov/climate/gdp>). The HRU delineation and default
9 parameterization came from the U.S. Geological Survey GeoSpatial Fabric
10 (http://wwwbrr.cr.usgs.gov/projects/SW_MoWS/GeospatialFabric.html). Finally, the
11 parameter sensitivity output values that were used to make the maps and tables in this article
12 are available at <ftp://brrftp.cr.usgs.gov/pub/markstro/hess>.

13

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1 Tables

2 Table 1. Precipitation Runoff Modeling System (PRMS) calibration parameters used in this
 3 study. The values in the column labeled “PRMS module” identify the module type equation(s)
 4 from the PRMS source code (see Markstrom et al., 2015).

Parameter name	Description	PRMS module	Range
adjmix_rain	Factor to adjust rain proportion in a mixed rain/snow event	climate	0.6—1.4
tmax_allrain	Maximum air temperature above which precipitation is rain	climate	-8.0—60.0
tmax_allsnow	Maximum air temperature below which precipitation is snow	climate	-10.0—40.0
dday_intcp	Intercept in degree-day equation	solar radiation	-60.0—10.0
dday_slope	Slope in degree-day equation	solar radiation	0.2—0.9
ppt_rad_adj	Solar radiation adjustment threshold for precipitation days	solar radiation	0.0—0.5
radj_sppt	Solar radiation adjustment on summer precipitation days	solar radiation	0.0—1.0
radj_wppt	Solar radiation adjustment on winter precipitation days	solar radiation	0.0—1.0
radmax	Maximum solar radiation due to atmospheric effects	solar radiation	0.1—1.0
tmax_index	Temperature to determine precipitation adjustments to solar radiation	solar radiation	-10.0—110.0
jh_coef	Coefficient used in Jensen-Haise potential ET computations	Potential ET	0.005—0.06
jh_coef_hru	Coefficient used in Jensen-Haise potential ET computations	Potential ET	5.0—25.0
srain_intcp	Summer rain interception storage capacity	interception	0.0—1.0
wrain_intcp	Winter rain interception storage capacity	interception	0.0—1.0
cecn_coef	Convection condensation energy coefficient	snow	2.0—10.0
emis_noppt	Average emissivity of air on days without precipitation	snow	0.757—1.0
freeh2o_cap	Free-water holding capacity of snowpack	snow	0.01—0.2
potet_sublim	Snow sublimation fraction of potential ET	snow	0.1—0.75
carea_max	Maximum area contributing to surface runoff	surface runoff	0.0—1.0
smidx_coef	Non-linear contributing area coefficient	surface runoff	0.001—0.06
smidx_exp	Exponent in non-linear contributing area coefficient	surface runoff	0.1—0.5
fastcoef_lin	Linear coefficient in equation to route preferential-flow	soil-zone	0.001—0.8
fastcoef_sq	Non-linear coefficient in equation to route preferential-flow	soil-zone	0.001—1.0
pref_flow_den	Fraction of the soil zone in which preferential flow occurs	soil-zone	0.0—0.1
sat_threshold	Water capacity between field capacity and total saturation	soil-zone	1.0—999.0
slowcoef_lin	Linear coefficient for interflow routing	soil-zone	0.001—0.5
slowcoef_sq	Non-linear coefficient for interflow routing	soil-zone	0.001—1.0
soil2gw_max	Maximum soil water excess that is routed directly to groundwater	soil-zone	0.0—0.5
soil_moist_max	Maximum available water holding capacity of soil-zone	soil-zone	0.001—10.0

soil_rechr_max	Maximum available water holding capacity of recharge zone	soil-zone	0.001—5.0
ssr2gw_exp	Non-linear coefficient in equation used to route soil-zone water to groundwater	soil-zone	0.0—3.0
ssr2gw_rate	Linear coefficient in equation used to route soil-zone water to groundwater	soil-zone	0.05—0.8
transp_tmax	Temperature that determines start of the transpiration period	soil-zone	0.0—1000.0
gwflow_coef	Linear groundwater discharge coefficient	groundwater	0.001—0.5

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1 Table 2. Ordered list of most sensitive Precipitation-Runoff Modeling System calibration
2 parameters by process and performance statistic. The parameters listed in each cell of the
3 table are those that are required to account for 90 percent of the cumulative sensitivity across
4 all hydrologic response units (HRUs). The number in parentheses following the parameter
5 name is the proportion of the CONUS HRUs, in percent, in which that parameter is part of the
6 set that accounts for 90 percent of the cumulated sensitivity on an HRU-by-HRU basis. These
7 parameters are described in Table 1.

Process	Performance Statistic		
	Mean	CV	AR 1
Snowmelt	tmax_allsnow(96), tmax_allrain(92)	tmax_allsnow(39), tmax_allrain(38), rad_trncf(9), freeh2o_cap(8), dday_intcp(7)	tmax_allsnow(34), dday_intcp(29), rad_trncf(28), radmax(24), tmax_allrain(17), jh_coef(15), freeh2o_cap(14), cecn_coef(14), emis_noppt(13), jh_coef_hru(13), potet_sublim(10)
Surface runoff	smidx_exp(98), carea_max(98), soil_moist_max(98), smidx_coef(96), jh_coef(90), dday_intcp(33)	carea_max(93), smidx_exp(82), jh_coef(64), tmax_allsnow(55), smidx_coef(52), srain_intcp(33), soil_moist_max(23), tmax_allrain(22)	soil_moist_max(92), carea_max(83), jh_coef(65), smidx_exp(64), smidx_coef(42), tmax_allsnow(39), dday_intcp(25), srain_intcp(23), tmax_allrain(16), radmax(15)
Infiltration	smidx_exp(99), soil_moist_max(99), carea_max(99), smidx_coef(95), jh_coef(64), srain_intcp(50)	carea_max(80), tmax_allsnow(69), jh_coef(63), smidx_exp(62), srain_intcp(54), smidx_coef(54), tmax_allrain(48), radmax(37), freeh2o_cap(36), soil_moist_max(35), dday_intcp(31), rad_trncf(18)	carea_max(72), soil_moist_max(64), smidx_exp(61), tmax_allsnow(60), srain_intcp(60), tmax_allrain(42), jh_coef(35), smidx_coef(24), freeh2o_cap(16), dday_intcp(16)
Soil moisture	soil_moist_max(100), jh_coef(99),	jh_coef(98), radmax(98), soil_moist_max(97),	soil_moist_max(99), jh_coef(98),

	dday_intcp(94), radmax(82)	dday_intcp(94)	dday_intcp(89), radmax(35)
Evapo- transpiration	jh_coef (100), soil_moist_max (96), dday_intcp (96), radmax (92), jh_coef_hru (62), smidx_coef (37), dday_slope (25)	radmax(100), jh_coef (100), soil_moist_max (95), dday_intcp (73), dday_slope (67), soil_rechr_max (34)	jh_coef(100), radmax(100), dday_slope(75), soil_moist_max(74), dday_intcp(67), soil_rechr_max(49)
Interflow	soil_moist_max(99), soil2gw_max(94), pref_flow_den(90), jh_coef(84), carea_max(65), smidx_exp(45), dday_intcp(31), smidx_coef(19)	fastcoef_lin(100), soil_moist_max(87), pref_flow_den(71), jh_coef(61), carea_max(49), soil2gw_max(29), smidx_exp(25), tmax_allsnow(17), dday_intcp(16)	soil_moist_max(96), fastcoef_lin(89), slowcoef_sq(83), carea_max(72), jh_coef(61), pref_flow_den(47), smidx_exp(47), ssr2gw_exp(40), soil2gw_max(26), dday_intcp(18), tmax_allsnow(16)
Baseflow	jh_coef (100), soil_moist_max (91), dday_intcp (81), soil2gw_max (74), radmax (64), carea_max (37), jh_coef_hru (36)	gwflow_coef (48), soil_moist_max (40), jh_coef (28), soil2gw_max (28), smidx_coef(20), carea_max(16), tmax_allsnow(13), dday_intcp(12), smidx_exp (8)	gwflow_coef (48), soil_moist_max (44), soil2gw_max (22), carea_max (18)
Runoff	jh_coef(100), dday_intcp(96), soil_moist_max(96), radmax(93), jh_coef_hru(62), smidx_coef(37), dday_slope(26)	gwflow_coef(97), soil_moist_max(81), fastcoef_lin(76), pref_flow_den(71), carea_max(58), jh_coef(54), smidx_exp(49), smidx_coef(42), soil2gw_max(36), tmax_allsnow(15)	slowcoef_sq(90), soil2gw_max(90), gwflow_coef(82), carea_max(81), soil_moist_max(78), smidx_exp(72), smidx_coef(60), fastcoef_lin(36), pref_flow_den(35), jh_coef(30), slowcoef_lin(22)
Parameters not sensitive	adjmix_rain, fastcoef_sq, ppt_rad_adj, radj_sppt, radj_wppt, sat_threshold, ssr2gw_rate, tmax_index, transp_tmax, wrain_intcp		

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1 Figures

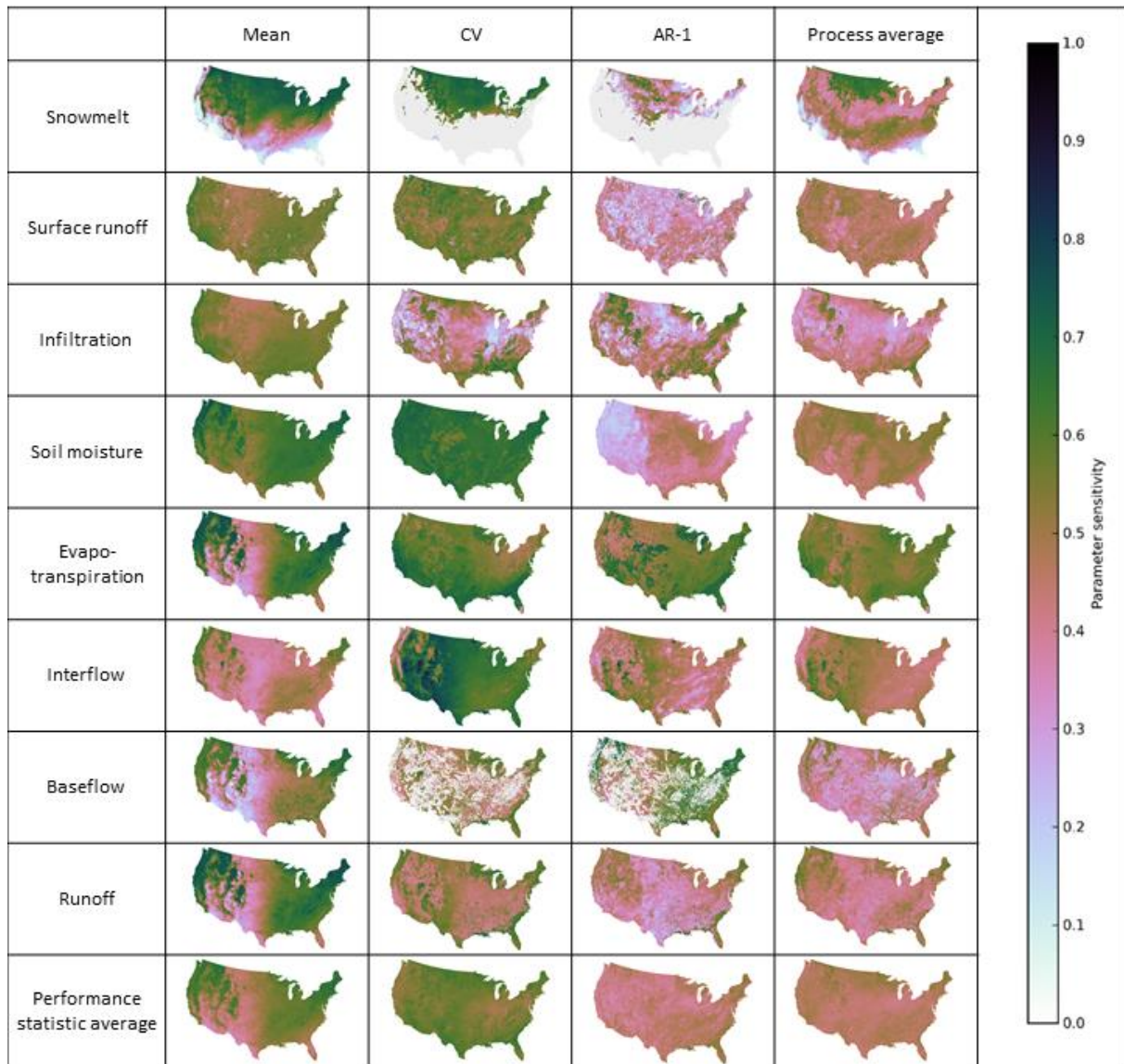


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4 Figure 1. Location Map of the conterminous United States showing the different geographic
5 regions referred to this study.

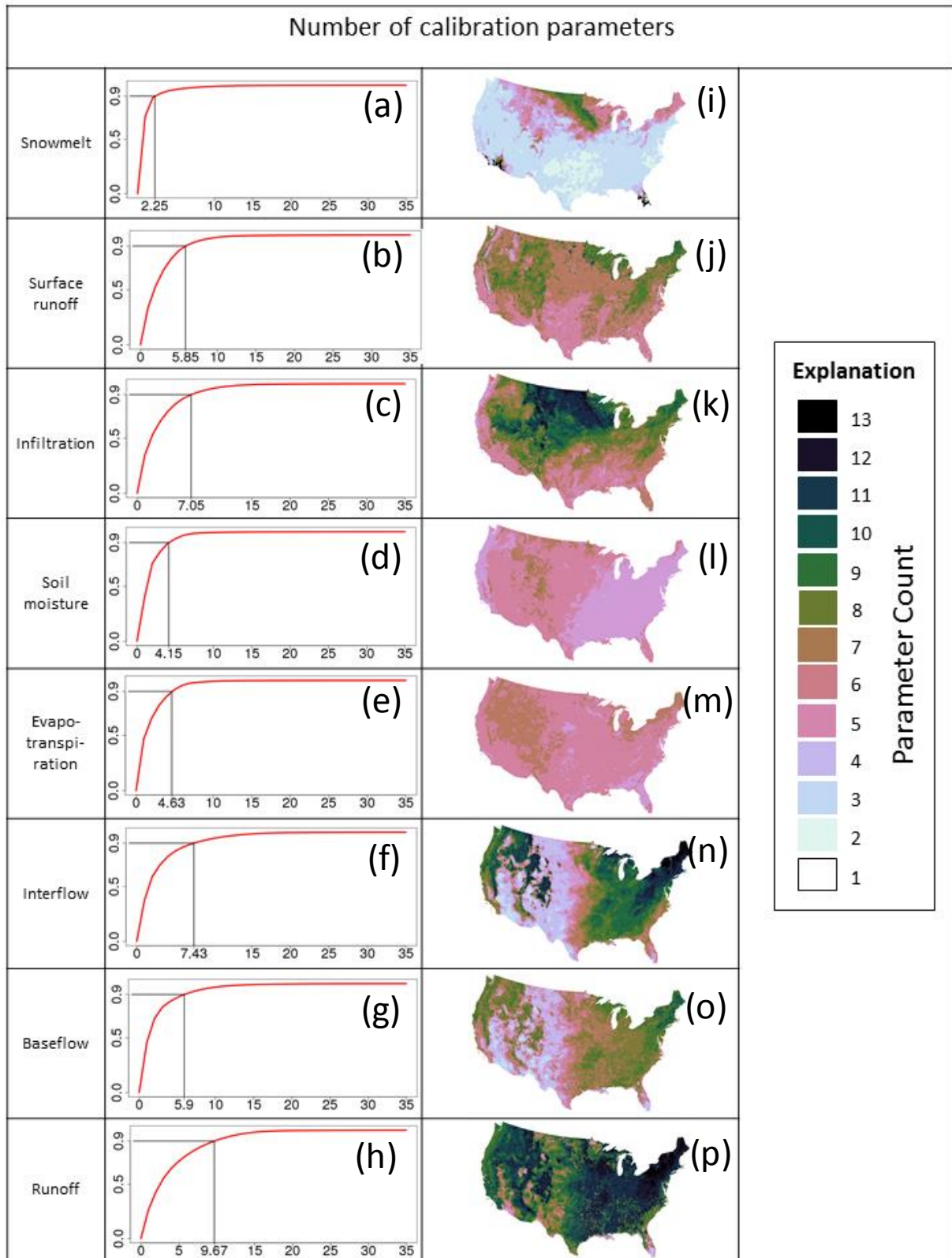
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2 Figure 2. Maps of the conterminous United States showing Precipitation-Runoff Modeling
 3 System parameter sensitivity by Hydrologic Response Unit (HRU) by process and
 4 performance statistic. The HRUs parameter sensitivity is computed by summing the first-
 5 order sensitivity for all parameters. The process average maps are made by averaging the
 6 parameter sensitivity values computed for the different performance statistics. The
 7 performance statistic maps are made averaging the parameter sensitivity values computed for
 8 the different processes.

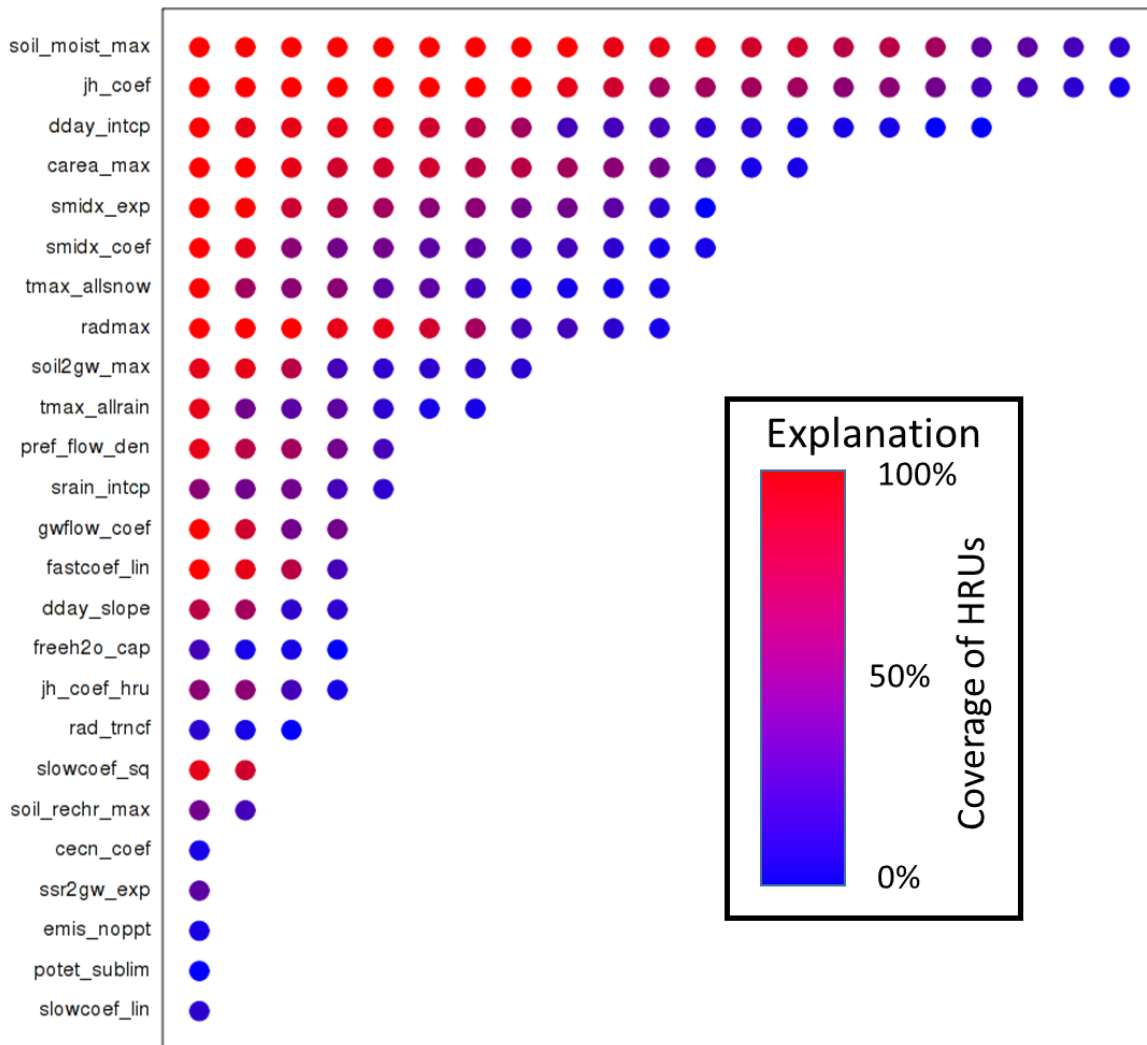
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2 Figure 3. Cumulative parameter sensitivity across all Hydrologic Response Units (HRUs) in
 3 the CONUS Precipitation-Runoff Modeling System application are shown by process. The
 4 plots (a)—(h) show the parameter count necessary to account for 90% of the cumulative

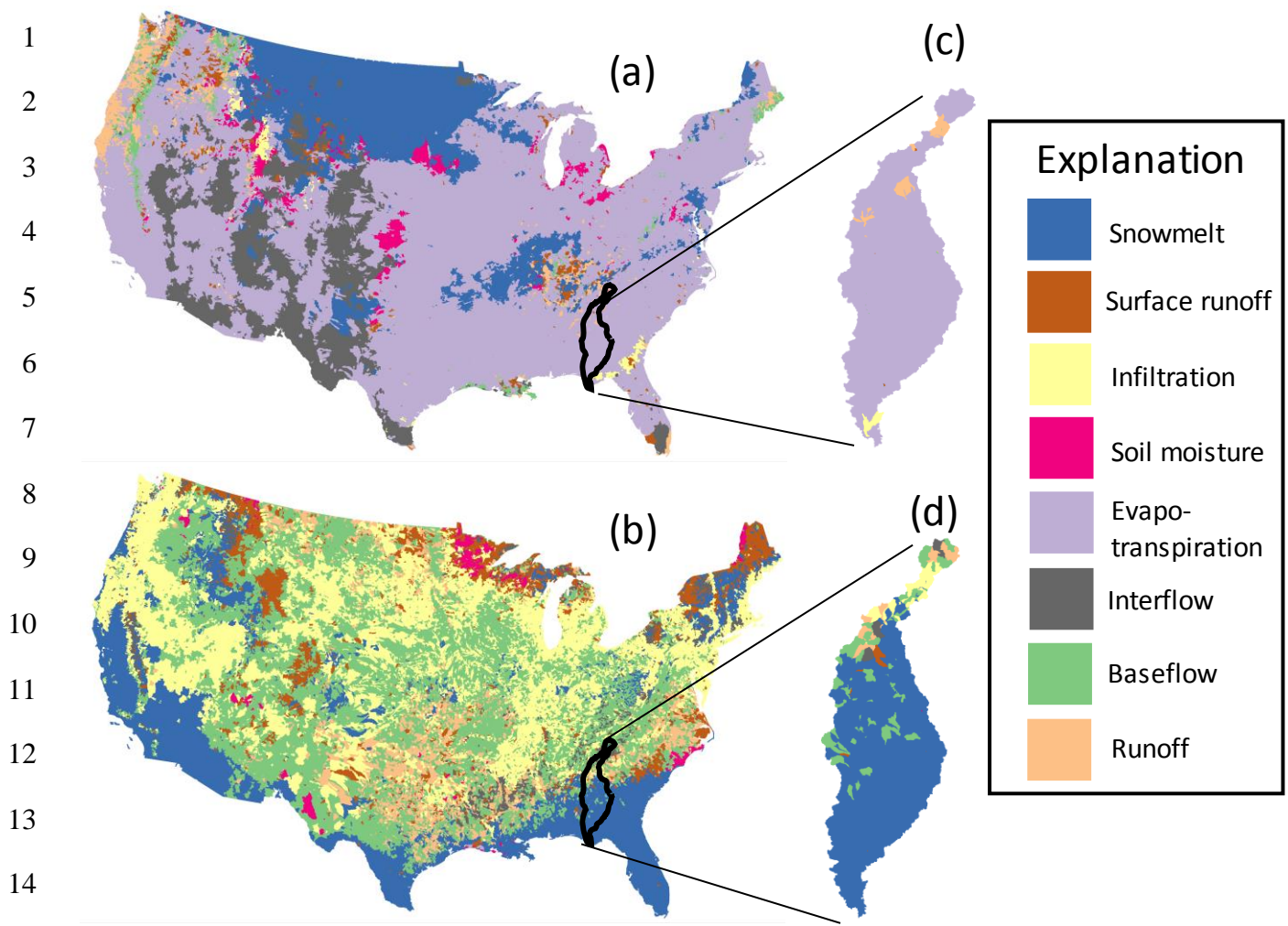
1 parameter sensitivity, summarized across all HRUs. For this count, the parameters are ranked
2 and summed until the 90% level is reached. The maps (i)—(p) show the count of ranked
3 parameters required to reach the 90% level on an HRU-by-HRU basis, by process.
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Parameter Occurrence

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Figure 4. Summarizes the frequency of occurrence of the different calibration parameters in the process/performance statistic categories of Table 2. The circles in each row adjacent to a parameter name indicate how many times the respective parameter occurs in these different categories. Parameters with more circles are affecting more process categories. The color of each circle indicates the extent of the spatial coverage of that occurrence, specifically, red circles (as opposed to blue) indicate that more Hydrologic Response Units are affected by the respective parameter.



19 Figure 5. Precipitation-Runoff Modeling System parameter sensitivity organized by process
 20 ranked for each hydrologic response unit for the entire conterminous United States (maps (a)
 21 and (b)) and for the Apalachicola – Chattahoochee – Flint River basin (maps (c) and (d)). The
 22 maps on the top ((a) and (c)) show the most dominant process, while the maps on the bottom
 23 ((b) and (d)) show the most inferior process.

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