

Reviewer 1:

1) *The method is a numerical model. The problem with the paper concerns the model. As far as I can tell, the model is not publicly available and therefore it will be difficult for the community to independently assess how varying the parameters changes the response of the system. Citation to a DRAFT version of a user manual is not sufficient. In this age of open source and online discussion of scientific papers, we as a community need to figure out how to make our models available to the greater community. This is on the one hand a comment to the entire community, but on the other hand, it is a comment to these authors. You can move us forward. At a minimum, provide a proper citation to the code and a link to where the code is described.*

The Hydrogeosphere (HGS) code is a non-commercial code developed from the University of Waterloo and Université Laval. The code is continuously under development and applied by a large research community for simulation of flow and transport in different hydrogeological media as shown by the web-site <http://hydrogeosphere.org/> (added in the manuscript now). The application of karst spring responses is still a new field. We have added further recent citations (in chapter Modeling approach) where the double continuum approach of Hydrogeosphere was applied (p. 2, line 38).

Rosenbom, A., R. Therrien, J.C. Refsgaard, K.H. Jensen, V. Ernstsen, K.E.S. Klinta, 2009. Numerical Analysis of Water and Solute Transport in Variably-Saturated Fractured Clayey Till, Journal of Contaminant Hydrology, vol 104, no 1-4, 137-152, doi:[10.1016/j.jconhyd.2008.09.001](https://doi.org/10.1016/j.jconhyd.2008.09.001).

Schwartz, F.W., Sudicky, E.A., McLaren, R.G., Park, Y.-J., Huber, M. and Apte, M., 2010. Ambiguous Hydraulic Heads and ¹⁴C Activities in Transient Regional Flow, Ground Water, 48(3), 366-379, doi:[10.1111/j.1745-6584.2009.00655.x](https://doi.org/10.1111/j.1745-6584.2009.00655.x)

2) *Specific to this paper - I would like to see the authors be more quantitative in the description of the results. There are many phrases along the lines of "steeper recession curve", "higher peak discharges"... These statements should be changed to "slope of the recession curve was 5% compared to the slope of the recession curve in the base model of 3%". These minor changes will set the standard for subsequent modeling studies.*

We agree that the descriptions can be more quantitative and have added recession coefficients for the description of recession curves (Figure 8, 10, Table 2), which describes the discharge behavior quantitatively (p. 10-11).

3) *Specific to this paper - Also, I would like better descriptions of how adding water to the bottom of the conduit was incorporated and a listing of possible effects that that might have and of the van Genuchten parameters.*

In the manuscript we already mention the adding of water: "A second specified flux boundary is set on the bottom of the whole conduit continuum to add rapid recharge in the aquifer." (p. 7, line 202-205) and why we think that this is justified.

The unsaturated conduit continuum is not affected by the rapid recharge component. Van Genuchten parameters of the conduit continuum only influence slow percolation of water, which flows from the matrix continuum into the conduit continuum. The limitation of the conduit continuum to the saturated zone is difficult to accomplish because of the variation of the water table.

4) Specific to this paper - in the discussion of Figure 7 - you claim that K_c and θ_c and θ_m control the simulated hydrograph. I see that K_c and θ_m influence the hydrograph, but I do not see that θ_c does. Please clarify.

This is correct. We clarified that θ_{sc} does only show a similar behavior regarding its influence on the discharge but does not strongly control the discharge (p.10, lines 295-298).

Simulation of saturated and unsaturated flow in karst systems at catchment scale using a double continuum approach

J. Kordilla¹, M. Sauter¹, T. Reimann², and T. Geyer¹

¹Geoscientific Centre, University of Göttingen, Göttingen, Germany

²Institute for Groundwater Management, TU Dresden, Dresden, Germany

Correspondence to: J. Kordilla (jkordil@gwdg.de)

Abstract. The objective of this work is the simulation of saturated and unsaturated flow in a karstified aquifer using a double continuum approach. The HydroGeoSphere code (Therrien et al., 2006) is employed to simulate spring discharge with the Richards equations and van Genuchten parameters to represent flow in the (1) fractured matrix and (2) conduit continuum coupled by a linear exchange term. Rapid vertical small-scale flow processes in the unsaturated conduit continuum are accounted for by applying recharge boundary conditions at the bottom of the saturated model domain. An extensive sensitivity analysis is performed on single parameters as well as parameter combinations. The transient hydraulic response of the karst spring is strongly controlled by the matrix porosity as well as the van Genuchten parameters of the unsaturated matrix, which determine the head dependent inter-continuum water transfer when the conduits are draining the matrix. Sensitivities of parameter combinations partially reveal a non-linear dependence over the parameter space. This can be observed for parameters not belonging to the same continuum as well as combinations, which involve the exchange parameter, showing that results of the double continuum model may depict a certain degree of ambiguity.

1 Introduction

Discharge dynamics in karst aquifers are determined by superposition of several effects: (1) water infiltration into soil, (2) water percolation through the unsaturated zone, (3) groundwater flow in highly conductive karst conduits and interaction with (4) groundwater flow in the low-conductive fissured and fractured rock matrix. These different effects, without even having considered the variability of precipitation and evapotranspiration, are a result of the particular properties of the individual compartments: soil-epikarstic zone, vadose zone, and phreatic zone. Each of these compartments is,

in turn, characterized by two coupled flow systems: a highly permeable one with low storage and a less permeable one with high storage. Therefore, different individual (rapid, slow) flow components with characteristic temporal distributions are induced. Accordingly, the final spring discharge is then a function of the individual flow contributions of each of these compartments (Smart and Hobbs, 1986), which makes the inverse analysis of spring discharge a major challenge, requiring elaborate modeling tools and a large spectrum of data to constrain the model. The simulation of coupled saturated and unsaturated flow is still a challenge in hydrogeology in particular in fractured (Therrien and Sudicky, 1996) and karstified systems (Reimann et al., 2011a). This is predominantly a result of the data scarcity respecting the hydraulic parameter field of real karst systems. Therefore, flow in karst systems is often simulated with lumped parameter modeling approaches, which translate precipitation signals to discharge hydrographs by applying simple transfer functions (Dreiss, 1989). Generally, this type of approach is appropriate for situations in which predicted system states are expected to range between already observed events. The simulation of natural karst systems with distributed parameter models is reported only in a few studies (e.g. Jeannin, 2001; Hill and Polyak, 2010). However, distributive modeling approaches incorporate flow laws and, therefore, are adequate for the process based simulation of karst hydraulics (e.g. Birk et al., 2006; Reimann et al., 2011b) and transport problems (e.g. Dreybrodt et al., 2005; Birk et al., 2005). Teutsch and Sauter (1991) demonstrate in how far the different mathematical model approaches are suitable for different types of problems (flow, transport, regional, local). An approach that takes into account the limited information about aquifer geometry and still allows the simulation of the dynamics of the karst system at an event basis, i.e. considers the dual flow behavior of karst systems is the double continuum approach (e.g. Teutsch and Sauter, 1991; Sauter et al., 2006). The approach was introduced by Barenblatt et al. (1960) and applied for simulation of karst hydraulics on catchment scale by Teutsch (1988) and Sauter (1992). It yields equations for simulation of slow and diffuse flow in the fissured matrix and the discrete rapid underground drainage by solution conduits in karst systems. Here, we want to assess the relative importance of individual factors and parameter combinations on the discharge behavior of a karst spring without detailed knowledge about the hydraulic parameter field of an aquifer system. This type of information is of major importance to focus characterization efforts in catchment based karst studies. Furthermore, the importance of infiltration dynamics, i.e. the temporal distribution of the rapid and the slow flow component on the discharge dynamics is to be determined. We employ the integrated saturated-unsaturated double-continuum approach HydroGeoSphere (Therrien et al., 2006) to simulate recharge and discharge dynamics in a karst aquifer with a thick unsaturated zone. Flow simulations are based on the Richards equation and respective parameters are described via the van Genuchten parametric model. The application and limitations of the approach for flow simulation in karst systems are discussed. A comprehensive parameter study was conducted in order to elucidate sensitive and important model parameters as well as parameter dependencies, and to reduce the model ambiguity to assist in focused karst characterization.

2 Methods

60 2.1 Modeling approach

The application of the double-continuum approach requires two sets of flow equations, one for the matrix (primary) and one for the conduit (secondary) continuum, solved consecutively at the same node and coupled with an exchange term that defines the hydraulic interface and controls the inter-continuum exchange flow. The applied HydroGeoSphere model (Therrien et al., 2006) is a non-
 65 commercial code available to the interested user under <http://hydrogeosphere.org/>. The model has been extensively used for various studies involving dual porosities such as McLaren et al. (2000), Rosenbom et al. (2009) and Schwartz et al. (2010). The governing equation in the applied model is the Richards equation (Richards, 1931), which is slightly modified to account for inter-continuum water exchange:

$$70 \quad -\nabla w_m(q_m) + \Gamma_{ex} \pm R_m = w_m \frac{\partial}{\partial t} (\theta_{sm} S_{wm}) \quad (1)$$

$$-\nabla w_c(q_c) + \Gamma_{ex} \pm R_c = w_c \frac{\partial}{\partial t} (\theta_{sc} S_{wc}), \quad (2)$$

where w_m and w_c are the volumetric fractions of each continuum of the total porosity, such that $w_m = 1.0 - w_c$. S_{wm} and S_{wc} are the water saturations of the respective continuum and R_m and R_c denote a volumetric fluid flux per unit volume (source/sink term) for each continuum. The saturated
 75 water content of the matrix and conduit system are assumed equal to the the effective matrix porosity θ_{sm} and conduit porosity θ_{sc} and are related to the water content of the matrix θ_m and of the conduit θ_c according to

$$\theta_m = S_{wm} \theta_{sm} \quad (3)$$

$$\theta_c = S_{wc} \theta_{sc} \quad (4)$$

80 The conduit and total porosity are given as

$$\theta_{total} = \theta_{sm}(1 - w_c) + \theta_{sc} w_c = \theta_{sm}(w_m) + \theta_{sc} w_c. \quad (5)$$

i.e. the whole simulation domain consists of nodes with primary porosity θ_{sm} with a volumetric fraction of $w_m = 1.0 - w_c$ and secondary porosity θ_{sc} with a volumetric fraction of w_c . Given that the local conduit porosity is chosen to be 1.0 and that both continua cover the whole domain the
 85 overall conduit porosity can simply be evaluated as:

$$\theta_{sc} \hat{=} \theta_{sc(local)} w_c. \quad (6)$$

The fluxes q_m and q_c are obtained from

$$q_m = -K_m k_{rm} \nabla(\psi_m + z) \quad (7)$$

$$q_c = -K_c k_{rc} \nabla(\psi_c + z), \quad (8)$$

90 where K_m and K_c denote hydraulic conductivity, ψ_m and ψ_c are the pressure heads in each continuum and z is the elevation head.

In the unsaturated zone, the relative permeabilities k_{rm} , k_{rc} and k_{ri} (interface) depend on the water saturation which in turn is related to the pressure head according to van Genuchten (1980):

$$S_{wm} = S_{wrm} + (1 - S_{wrm}) \left[1 + |\alpha_m \psi_m|^{\beta_m} \right]^{-\nu_m} \quad (9)$$

$$95 \quad S_{wc} = S_{wrc} + (1 - S_{wrc}) \left[1 + |\alpha_c \psi_c|^{\beta_c} \right]^{-\nu_c} \quad (10)$$

$$S_{wi} = S_{wri} + (1 - S_{wri}) \left[1 + |\alpha_i \psi_i|^{\beta_i} \right]^{-\nu_i} \quad (11)$$

for $\psi < 0$, where S_{wrm} , S_{wrc} and S_{wri} are the residual saturations, α_m , α_c and α_i denote the inverse air-entry pressure head, β_m , β_c and β_i are the pore-size distribution indices of each continuum and the interface. Note that the evaluation of the interface relative conductivity is based on the pressure
100 head of the matrix. In the saturated zone where $\psi \geq 0$ the saturations are $S_{wm} = S_{wc} = S_{wi} = 1$. The relative permeability is given by:

$$k_{rm}(S_{wm}) = S_{em}^{(l_p)} \left[1 - \left(1 - S_{em}^{1/\nu_m} \right)^{\nu_m} \right]^2 \quad (12)$$

$$k_{rc}(S_{wc}) = S_{ec}^{(l_p)} \left[1 - \left(1 - S_{ec}^{1/\nu_c} \right)^{\nu_c} \right]^2 \quad (13)$$

$$k_{ri}(S_{wi}) = S_{ei}^{(l_p)} \left[1 - \left(1 - S_{ei}^{1/\nu_i} \right)^{\nu_i} \right]^2 \quad (14)$$

105 with l_p being the pore connectivity parameter (equals 0.5 after Mualem, 1976), S_e the effective saturation

$$S_{em} = \frac{S_{wm} - S_{wrm}}{1 - S_{wrm}} \quad (15)$$

$$S_{ec} = \frac{S_{wc} - S_{wrc}}{1 - S_{wrc}} \quad (16)$$

$$S_{ei} = \frac{S_{wi} - S_{wri}}{1 - S_{wri}} \quad (17)$$

110 and ν is defined as:

$$\nu_m = 1 - \frac{1}{\beta_m} \quad (18)$$

$$\nu_c = 1 - \frac{1}{\beta_c} \quad (19)$$

$$\nu_i = 1 - \frac{1}{\beta_i} \quad (20)$$

for $\beta > 1$. In the saturated zone the storage terms on the right-hand side of Eq. (1) and Eq. (2) are
 115 replaced by:

$$S_{wm} S_{sm} \frac{\partial \psi_m}{\partial t} + \theta_{sm} \frac{\partial S_{wm}}{\partial t} \quad (21)$$

$$S_{wc} S_{sc} \frac{\partial \psi_c}{\partial t} + \theta_{sc} \frac{\partial S_{wc}}{\partial t}, \quad (22)$$

where S_{sm} and S_{sc} are the specific storage coefficients. Water release by compaction of the porous
 medium is neglected in the unsaturated zone. The term Γ_{ex} in Eq. (1) and Eq. (2) describes the
 120 volumetric fluid exchange rate per unit volume between primary and secondary continuum and is
 given as:

$$\Gamma_{ex} = \alpha_{ex} K_i k_{ri} (\psi_c - \psi_m), \quad (23)$$

where K_i is the hydraulic conductivity of the interface (e.g. sediments) and k_{ri} the relative interface
 permeability (Barenblatt et al., 1960). The exchange parameter α_{ex} is determined by calibration and
 125 defined as (Gerke and Van Genuchten, 1993):

$$\alpha_{ex} = \frac{\beta}{\alpha^2} \gamma_w, \quad (24)$$

where β is a geometry factor (3 for rectangular matrix blocks, 15 for spheres), a is the distance
 between the center of a matrix block and the adjacent fracture or conduit and γ_w is an empirical
 coefficient usually set to 0.4. Strictly speaking, the van Genuchten approach, adopted in HydroGeo-
 130 Sphere does not apply to fractured and karstified rock materials. The highly heterogeneous flow field
 and preferential flow paths associated with such media and the consequently greater size of an REV
 compared to porous media are rendering the parameter determination by laboratory experiments im-
 practical. Still, the van Genuchten parameters reflect properties of an unsaturated porous material
 and can be considered as an adequate parameter set to describe transient infiltration processes if they
 135 are treated as calibration parameters in order to upscale from the Darcy-scale averaging volume to
 the field scale.

2.2 Sensitivity analysis

An extensive sensitivity analysis is performed to determine the influence of the calibrated parameters
 on the computed flow. The root-mean-square error (RMSE) is chosen to rate the accuracy of fit and
 140 calculate deviations from the calibrated model. The RMSE is defined as (Bamberg et al., 2007):

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (m_i - f_i)^2}, \quad (25)$$

where n is the total number of data points, m_i denotes the simulated spring discharge derived by the sensitivity analyses and f_i is the calibrated model value. For sensitivity analyses the RMSE has been evaluated using daily data and documented parameter ranges were employed if possible.

145 However, for some variables, in particular the van Genuchten parameters for the unsaturated zone of hard rocks, only few data and estimates can be found in the literature, e.g. Weiss (1987), Sauter (1992), Contractor and Jenson (2000) and Roulier et al. (2006). Consequently, the sensitivity of these parameters was determined systematically to evaluate the degree of ambiguity of the model. Depending on field observations parameter ranges were varied on linear or log-scale. Parameter spaces were assigned to cover at least the reported values from field experiments. In order to provide

150 a further quantitative comparison recession coefficients are given for one important recharge event during March 1988 (α_1) and the following recession until beginning of April 1988 (α_2). Due to the complex flow model it is likely that some parameters do not show a linear correlation and sometimes the simulated discharge curve is only influenced by specific parameter combinations. The final analysis of parameter sensitivity on an idealized example is subdivided into: (1) insensitive parameters,

155 (2) one sensitive parameter and (3) both parameters are sensitive (see Fig. 1, from left to right). In the latter case parameter A may be more sensitive for a certain range of parameter B. Given a constant parameter B_n and B_{n+dn} where n denotes the parameter value and dn a change in the parameter the parameter combination is referred to as non-linear if the change in RMSE over the whole

160 range of parameter A is different for B_n and B_{n+dn} that is if

$$f(A, B_n) \neq f(A, B_{n+dn}) \quad (26)$$

This case is particularly important if a properly calibrated model can be achieved for two different parameter combinations where at least one parameter is a pure calibration parameter, i.e. its range is difficult to estimate by field observations. Therefore, more than 1000 model runs were performed

165 and the influence of parameter combinations on the simulated discharge curve analyzed.

3 Case study

3.1 Description of the field site

The HydroGeoSphere model is employed to simulate flow in the catchment area of the Gallusquelle spring from February 1988 to January 1990. The Gallusquelle spring is situated in Southwest Germany on the Swabian Alb, a northeast-southwest striking Jurassic carbonate plateau. The catchment

170 area has been studied extensively by several authors including aquifer characterization (Birk et al., 2005; Sauter, 1992), speleology (Abel et al., 2002; Gwinner, 1976), and flow processes (Geyer et al., 2008). The size of the catchment is about 45 km². It is delineated by a water divide in the northwest and the River Fehla in the northeast (see Fig. 2). In the south the catchment is bounded by

175 the northeastern fault zone of the Hohenzollerngraben, which was found to be impermeable by tun-

neling works in the 1960's. After Sauter (1992) the base of the aquifer is formed by Kimmeridge marls (ki1). With a 70 m to 90 m thickness, this unit is rather consistent in the northwestern parts of the project area and consists of calcareous marls and occasional limestone intercalations. In the southeastern area no borehole information about the lower boundary of the unit are available. The uppermost catchment is made up of a sequence of Kimmeridgian limestones (ki2-5) from which the majority is developed as algal-sponge facies and, therefore, belongs to the Unterer Massenkalk or Oberer Massenkalk. The largest part of the catchment comprises limestones belonging to the Unterer Massenkalk (ki2 and ki3). The whole Jurassic sequence dips southeast at an angle of 1.2 degrees.

3.2 Geometry of the flow model

Based on the geological model, a vertical two-dimensional model domain of the catchment area was set up. The length of the domain is 10 km with a vertical thickness of 225 m. It reflects a cross section parallel to the direction of flow in the Gallusquelle catchment (see Fig. 2, lower figure). The model domain is represented by two continua reflecting flow in the low permeability fissured matrix (*matrix continuum*) and the highly permeable conduits (*conduit continuum*). The top of the model domain is set to 775 m a.s.l., which is an average elevation between ca. 910 m a.s.l. in the north-western part of the catchment and ca. 640 m a.s.l. in the south-eastern catchment and higher than the maximum groundwater head in the catchment. Every continuum is spatially discretized into 50 columns with a length of 200 m and a width of 1 m and 44 layers with a thickness of 5 m.

3.3 Boundary conditions

The lateral sides of the matrix continuum and of the conduit continuum, as well as the top of the conduit continuum are defined as no flow boundaries (see Fig. 3). A constant head boundary is applied to the right side of the conduit continuum at 634 m a.s.l. to represent the spring and allow discharge. A specified flux boundary is set at the top of the matrix continuum to account for diffuse recharge. Daily data of total recharge was estimated by Geyer (2008) for the simulation period on the Gallusquelle catchment. The applied water balance approach accounts for canopy storage, snow storage and soil-moisture storage before water entering the bedrock. A second specified flux boundary is set on the bottom of the whole conduit continuum to add rapid recharge in the aquifer. The location of the boundary condition considers that the transit time of the rapid recharge component through the unsaturated zone is below one day (Geyer et al., 2008) and, therefore, negligible with regard to the daily time steps. The simulation of rapid water percolation from the top of the conduit continuum to the groundwater surface is physically not possible with the van Genuchten approach, because it does not consider gravity driven flow processes like film and droplet flow. The initial head distribution for transient discharge simulations is computed with a steady state simulation. The applied total recharge for the simulation is 1.5 mm/d, which corresponds to the average recharge across the catchment area during the year 1988. Ten percent of the total recharge is employed as

rapid recharge component at the bottom of the conduit continuum. The amount is in the range of the rapid recharge component estimated by Sauter (1997) from event analysis using oxygen isotopes in precipitation and Gallusquelle spring water to differentiate between different flow components.

3.4 Parameterization

215 For the model calibration, known parameters are only varied within reasonable ranges that agree with actual field observations (Tab. 1). Unknown model parameters are investigated by an extensive sensitivity analysis. The specific storage coefficients for matrix and conduits are negligible since the aquifer is unconfined; hence, water released due to compaction in the saturated zone is irrelevant. As there are no documented values for the hydraulic properties of the interface available, the van
220 Genuchten parameters α_i , β_i , S_{wri} and the interface hydraulic conductivity K_i were set to values equal to the surrounding fissured matrix. Accordingly, inter-continuum water exchange is solely controlled by adjusting the exchange parameter α_{ex} . Model calibration is accomplished by fitting the observed and simulated discharge curves. Finally, the flow model contains 21 adjustable parameters for the fissured matrix and the conduit continuum.

225 4 Results and discussion

4.1 Model calibration

The calibrated model shows a good fit with most of the specific characteristics of the discharge hydrograph during the period between Feb./16th/1988 and Jan./20th/1990 (see Fig. 4). Please note that the discharge has been normalized to catchment area (45 km²). Calibrated values for all
230 varied parameters are comparable to values documented in the literature (Tab. 1). The observed discharge curve shows less sharp peaks and is smoother than the simulated curve. Sauter (1992) did get a comparable fit with a double continuum model for the saturated zone. The author did apply a function for the transfer of water from the soil zone to the groundwater surface, which is not necessary for our model.

235 During the time period investigated, two strong discharge events occurred, caused by major snowmelts which are referred to as first and second peak (see Fig. 4). The discharged water volume agrees well with the simulated data during the time period of the first peak. During the second discharge event (second peak) the simulated peak height is overestimated. It is not possible to change the relative peak height difference between the first and second peak with the available calibration
240 parameters. The recession curve slopes after discharge events show a good fit, except during low flow conditions between July and October 1989. This behavior could be attributed to the simplified geometry of the numerical model, which does not include the documented slightly inclined aquifer base and the geometry of different karstified zones in the karst system. The hydraulic heads in the matrix continuum and the conduit continuum are nearly identical during the simulation period with

245 a difference of a few centimeters. Above the water table the matrix saturation drops to 0.35 near
the surface (see Fig. 5). Flow paths in the unsaturated matrix continuum and conduit continuum
are slightly inclined towards the spring, whereas flow in the saturated zone is laterally oriented to-
wards the outlet, i.e. the karst spring. The flow paths of the unsaturated matrix continuum, which
would be expected to be vertical for such a large scale porous medium, are caused by the strong
250 influence of the conduit continuum which imposes a strong hydraulic gradient all over the matrix
continuum. This behavior cannot be prevented unless the secondary continuum would be restricted
to cover only the saturated zone. However, this is not an adequate solution considering the transient
behavior of the system, i.e. the variation of water levels within both continua. The saturation in
the conduit continuum is close to zero and has a very sharp transition along the water table. In this
255 model, unsaturated flow in the conduits is also calibrated by the k_{rminc} parameter (minimum relative
permeability of the conduits). Without this parameter, the relative permeability of the conduit con-
tinuum is a function of the residual saturation, i.e. setting of k_{rminc} simply overrides Eq. (13). This
is the case for most of the unsaturated conduit continuum, where saturation declines very quickly
(below 0.05) above the water table for the given van Genuchten parameters. Therefore, with the ap-
260 plied van Genuchten parameters only, water flow in the unsaturated conduit continuum is extremely
small such that exchange from the matrix into the conduit system is nearly completely prevented
and a proper model calibration is impossible due to numerical insufficiencies. However, Tokunaga
and Wan (1997) showed that gravity driven film flow processes occur on unsaturated fracture walls,
which contribute to water percolation along surfaces and may act as an interface from the conduit
265 system to the matrix system, thus giving a physical meaning to the k_{rminc} parameter. As the original
van Genuchten model relies on a uni-modal distribution of the pore space the hydraulic response of
such flow processes cannot be expected to be fully resolved by the model. Attempts to refine the
original van Genuchten approach and include hydraulic features of fractures into a continuum model
have been made for example by Ross and Smettem (1993), Durner (1994) and Brouyère (2006) by
270 constructing a continuous bi-modal retention curve.

An important role for the water exchange in the double continuum approach plays the exchange
parameter α_{ex} . It determines the ability of water to move in and out of the conduit continuum and
lumps geometrical and hydraulic properties of the karst matrix system. The surface-volume ratio,
for example, is higher for a dendritic system than for a single conduit with the same conduit volume.
275 The exchange parameter in the calibrated model is set to a high value such that it does not act as an
additional barrier for water transfer between both continua and water transfer is mainly controlled
by the hydraulic properties of the two continua.

5 Sensitivity analysis

5.1 Single variation of hydraulic parameters for saturated flow conditions

280 Tab. (2) gives an overview of the recession coefficients and RMSE values obtained for the sensitive parameters. A parameter has been discarded as insensitive if the maximum RMSE is below 0.05 mm/d. The recession coefficients have been measured at the first strong recharge event beginning of March 1988 (α_1) and during the low flow recession beginning of April 1988 (α_2). The calibrated values are $\alpha_1 = 0.23$ and $\alpha_2 = 0.03$ which is close to what has been reported by Sauter (1989) for a conduit dominated recession ($\alpha = 0.25$) for the same recharge event. Figure 6 (upper two graphs) shows the computed spring discharge for several model runs with varying hydraulic conductivity K_c and porosity θ_c in the conduit continuum. These parameters strongly influence the simulated spring discharge. Figure 7 (upper two graphs) additionally shows the respective recession coefficients. An increased conduit conductivity K_c results in higher α_1 recession coefficients and lower base flow levels indicated by the strong decrease of α_2 . A decreased conduit conductivity K_c favors a slow recession and decreases α_1 to 0.06 which according to Sauter (1989) already indicates a mixed system (fractured matrix + conduits) response. Discharge peaks are broadened and the base flow is higher. In case the conduit drains the matrix system an increase of K_c enhances the exchange process between matrix and conduits by decreasing the hydraulic gradient in the conduit continuum and consequently increasing the hydraulic gradient between matrix and conduits. The conduit porosity θ_{sc} follows a similar pattern, i.e. an increase will enhance the exchange process, however, the impact on the discharge curves is far less pronounced within the given ranges and both recession coefficients are all in the same order of magnitude indicating a conduit dominated recession. A contrasting behavior is observed by a variation in matrix porosity θ_{sm} . With an increase in the parameter the water transfer between the continua during recharge events is decreased because of the lower head difference between conduit and matrix and the discharge curve is smoothed accordingly (see Fig. 6). The recession coefficient α_1 and α_2 are consequently slightly lower while for a very low matrix porosity of 1.2% it is apparent that recessions coefficients represent a strongly conduit dominated system $\alpha_1 = 0.33$ and $\alpha_2 = 0.066$. K_m displays a low sensitivity within the given parameter range which can be attributed to the high exchange parameter of the calibrated model of $\alpha_{ex} = 1.0$. The high value leads to an immediate equalization of heads between conduit and matrix such that water will not be restrained within the matrix system when total heads are slightly higher than within the conduit system. The matrix system always depends on the hydraulic state of the conduit continuum, which discharges water rapidly to the spring. However, in a three-dimensional karst system, flow velocities within the matrix will be little influenced by the conduit system with increasing distance to the conduit. The exchange parameter α_{ex} is sensitive only for strong reductions on the order of three to four magnitudes. A reduction to 0.001 lowers the peak height of both main peaks while decreasing recession curve slopes α_1 to 0.06 and slightly increasing base levels. Further reduction to

0.0001 drastically decreases peak heights and increases the base levels. The resulting α_2 coefficients
315 are very low (0.002) and recharge events show no more pronounced peaks. An exchange reduction
to 0.1 or 0.01 has no significant influence on the discharge curves which indicates a sensitive interval
between 0.001 and 0.0001.

5.2 Single variation of unsaturated zone parameters

Variations of the sensitive van Genuchten parameters for the vadose zone are shown in Fig. (8) and
320 the corresponding recession coefficients in Fig. (9). The decrease of α_m and β_m results in a strong
rise of peak heights and increase of recession slopes ($\alpha_1 = 0.36$ and 0.26 respectively). The influence
of the van Genuchten α_m parameter on the discharge curve is connected to the inter-continuum water
exchange process. Lowering the parameter increases the capillary rise, i.e. the matrix has higher
saturation (and relative permeability) above the water table. Consequently the increased permeability
325 leads to a stronger and earlier exchange of water from the matrix into the conduit continuum, such
that recharge events affect spring discharge a lot earlier (pronounced event peaks). The opposite
can be observed for a value of 0.365 where the saturation fringe declines very quickly with lower
saturations above the water table. This reduces the main exchange interface to a smaller area above
the water table. Thus during high recharge events, peak heights are reduced since water will remain
330 longer in the matrix continuum and the α_2 recession coefficient becomes slightly lower (0.025)
reflecting the delayed discharge via the conduit system. The van Genuchten parameter β_m can be
considered insensitive compared to α_m . The conduit van Genuchten parameters α_c and β_c are as well
insensitive for the shown simulations. In the range of chosen values, the conduits do not produce a
strong capillary rise, i.e. the unsaturated zone above the conduit water table always displays a sharp
335 transition from saturated to strongly unsaturated. As mentioned earlier the application of the van
Genuchten parameters to a highly conductive and discrete flow system such as a conduit implies
a general abstraction of the physically based van Genuchten parameter set in order to create an
upscaled continuum system with a characteristic infiltration behavior and travel time distribution
as well as an exchange interface in the unsaturated zone. In this work the exchange process in
340 the unsaturated zone can be controlled by the α_c parameter in order to increase the capillary rise
in the conduit continuum and enhance inter-continuum water transfer. However, such an approach
also introduces a spatial information (i.e. the thickness of the conduit capillary fringe in vertical
direction) which is not known in real karst systems. As described before the k_{rminc} parameter is used
instead to maintain a constant water exchange in the unsaturated zone independent of the hydraulic
345 state of the conduit system if saturations are too low. The residual water saturation of the matrix
 S_{wrm} and the minimum relative permeability of the conduits k_{rminc} both show a similar behavior
regarding parameter variations. Increasing the parameters yields an enhanced exchange from the
matrix to the conduit continuum due to a higher relative conductivity. Consequently recharge events
are transmitted faster to the model outlet, i.e. the spring.

350 5.3 Combined parameter variations

The above presented sensitivity analyses imply only one single parameter varied at a time. However, a further important observation is that certain parameter combinations may show non-linear behavior with respect to their sensitivity, i.e. the influence of one parameter on the RMSE is not linear over the whole range of a second parameter. Tab. (3) shows maximum RMSE obtained for each parameter combination and if a non-linear relationship can be observed (bold RMSE values). For example, 355 the simultaneous variation of the matrix van Genuchten parameter α_m and the conduit conductivity K_c displays a pronounced sensitivity for low α_m values (Fig. 10). While for the calibrated α_m value of 0.0365 m^{-1} the conduit conductivity K_c is almost insensitive in the range of 1-10 m/s a lower α_m value of 0.00365 m^{-1} yields a high RMSE of 1.6 mm/d already at a K_c value of 360 10 m/s, i.e. $\partial \text{RMSE}(\alpha_m = 0.00365) / \partial K_c$ is much higher. A similar behavior can be shown for a combination of matrix porosity θ_{sm} and the conduit conductivity where lower porosities yield higher RMSE values with an increase in conduit conductivity to 100 m/s whereas for rather high matrix porosities of 0.102 the increase in RMSE is less pronounced. The conduit conductivity K_c exhibits a higher sensitivity for the calibrated exchange parameter $\alpha_{ex} = 1.0$ (see Fig. 10) such that a high 365 conductivity value (100 m/s) results in RMSE values of ca. 1.4 mm/d while for a lower exchange parameter the same conductivity yields a deviation of only 0.4 mm/d. The exchange parameter has a higher sensitivity for high conductivity values of the conduit system while it is nearly insensitive for low values (1 m/s). In sum, the variation of the exchange parameter influences the discharge curve depending on the combination with other parameters. This behavior can also be observed for 370 the combination of matrix porosity θ_{sm} and exchange parameter α_{ex} . Here the exchange parameter has a higher sensitivity for matrix porosities between 0.032 and 0.102 while at the lower limit (0.012 - 0.022) this sensitivity vanishes.

6 Conclusions

The applied two-dimensional double continuum approach lumps the horizontal flow components of 375 a karst system but accounts physically-based for the dual flow in the subsurface. The advantage of the approach is that only limited informations about the geometry of the aquifer system and recharge area are necessary. Due to their large volume, vertical conduits in a karst unsaturated system would act as flow barriers if simulated by the Richards equation. However, flow in vertical shafts is not controlled by matrix potential and capillary forces but rather flow processes dominated by gravita- 380 tional forces such as film flow (Tokunaga and Wan, 1997; Tokunaga et al., 2000), turbulent film flow (Ghezzehei, 2004), droplet flow (Doe, 2001; Dragila and Weisbrod, 2004) and rivulet flow (Su et al., 2001; Dragila et al., 2004; Su et al., 2004). In order to be able to use a consistent modeling approach, boundary conditions were modified and conduit recharge was directly injected at the bottom of the saturated conduit system. This procedure allows the simulation of rapid recharge with the given

385 modeling code. Slow percolation of water through the unsaturated zone was simulated with the
van Genuchten parametric model. The approach is successfully employed to simulate the discharge
curve of the karst system Gallusquelle for a period of two years with hydraulic parameter ranges
reported in literature. Because of the high amount of model parameters of the saturated-unsaturated
flow model, a comprehensive sensitivity analysis was performed. The analysis shows that the simu-
390 lated discharge curve displays high sensitivity to a variation of a number of model parameters. The
sensitivity study demonstrates that the simulation of karst hydraulics requires a-priori knowledge
about parameter ranges of model variables to reduce ambiguity of the model. However, especially
for unsaturated zone parameters in double continuum karst systems, only little information about the
parameter ranges is documented and further research is needed. Furthermore, the analysis shows that
395 the sensitivity of a parameter depends to a large degree on the other calibrated model parameters.
Therefore, sensitivity analyses should simultaneously take into account parameters of both continua
in order to detect deviations from a linear behavior if both parameters are sensitive. It also means
that conclusions about parameter sensitivity change from model to model and are not simply trans-
ferable. The fissured matrix porosity as well as van Genuchten parameters of the matrix continuum
400 are the most important parameters for an appropriate flow simulation. The conduit system drains the
fissured matrix and can, due to its high hydraulic conductivity, effectively discharge varying quan-
tities of water transferred from the matrix continuum. It should be noted that the double-continuum
approach assumes Darcian flow for the matrix as well as the conduits. Considering the high flow
velocities in the conduits it is apparent that strictly Darcian flow will underestimate the heads (no
405 energy loss due to friction) and consequently the exchange from matrix to conduits when the con-
duit continuum is draining the matrix system. More realistic results may be obtained by evaluating
these influences for example by applying turbulent flow in the conduit continuum (Shoemaker, 2008;
Reimann et al., 2011b). The van Genuchten parameters of the matrix are the most crucial property
in terms of sensitivity, uncertainty and model limitations. The exchange process between matrix
410 and conduit continuum is mainly controlled by differences in hydraulic properties. The α_{ex} pa-
rameter was set to a rather high value during the calibration, i.e. exchange is not limited by a too
low exchange coefficient. According to Gerke and Van Genuchten (1993) the parameter is defined
to express the interface connectivity on a rather small scale, e.g. between a porous medium and
macropores. On catchment scale it might implicitly correspond to the type of conduit system (i.e.
415 dendritic vs. large single conduits). If the parameter is used to calibrate the model by limiting water
transfer between continua, attention should be paid to the non-linear behavior of certain parameter
combinations and their resulting sensitivities. The application of van Genuchten parameters to frac-
tured aquifer systems treats them as upscaled calibration parameters. Local scale flow processes, e.g.
film and droplet flow along fracture surfaces, are not physically represented. Additionally, the dual-
420 continuum approach lumps the geometrical features of the conduit system and the fissured matrix
blocks, respectively, in the saturated and unsaturated zone.

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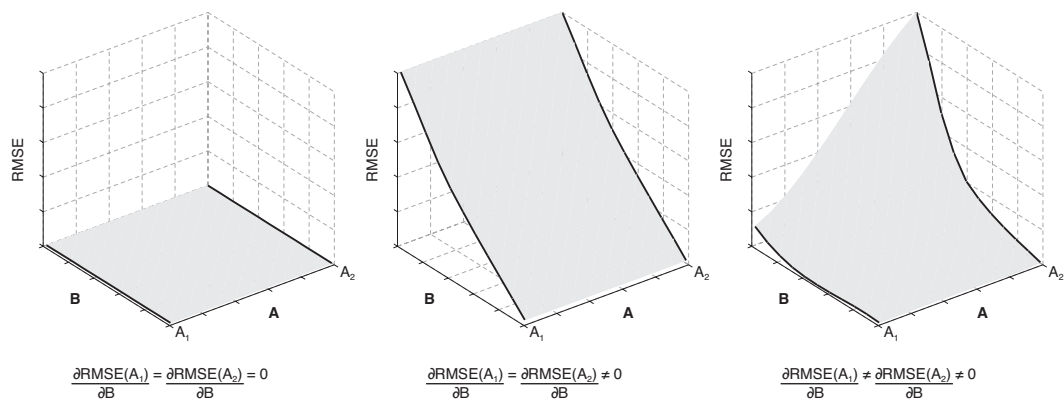


Fig. 1. Examples for inter-parameter dependencies. From left to right: (1) both parameters insensitive, (2) both parameters sensitive with linear dependency, (3) both parameters sensitive but non-linear dependency.

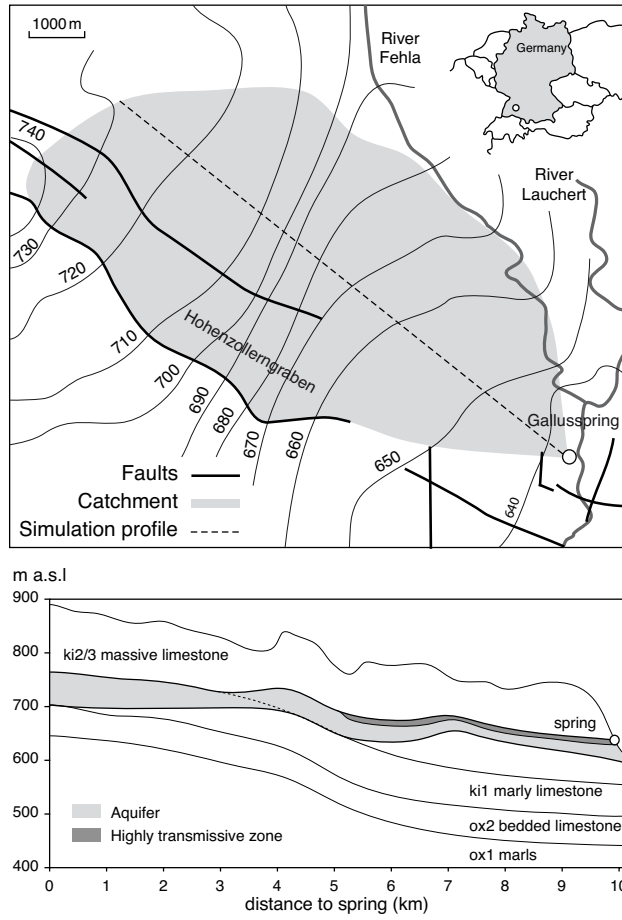


Fig. 2. Gallusquelle catchment and crosssection used for the simulation.

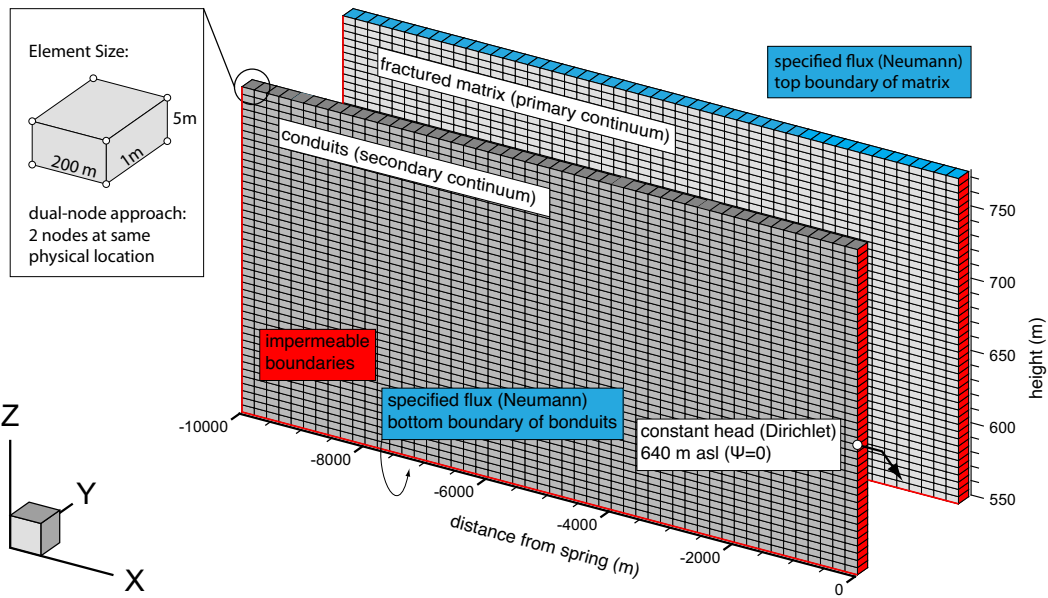


Fig. 3. Model grid of the two-dimensional model. A constant head boundary is applied at 640 m in the second continuum. Recharge is applied along the top boundary in both continua. Every node in the primary continuum has its counterpart in the secondary continuum at the same physical location.

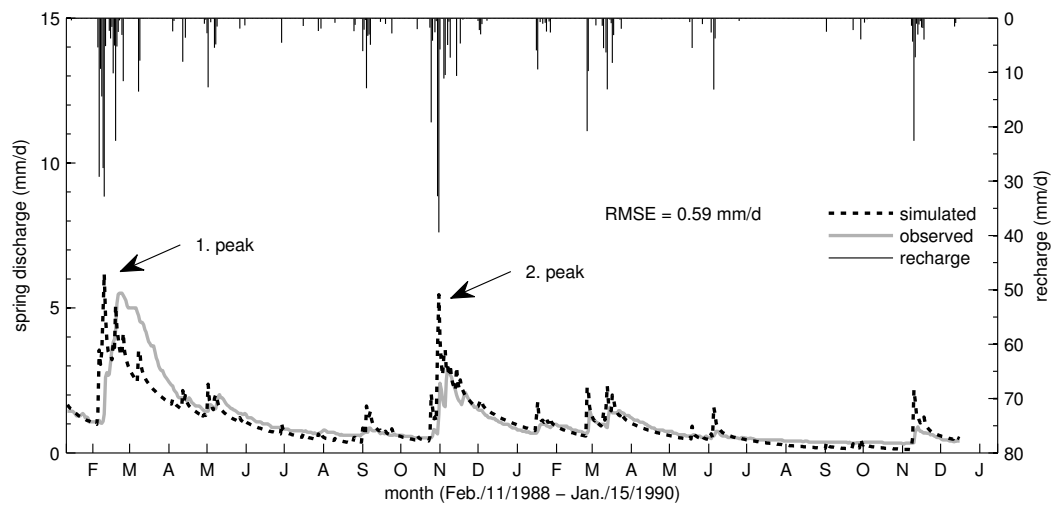


Fig. 4. The calibrated curve shows an acceptable fit. The secondary peak height is overestimated by the model. The first recharge event (first peak) reaches the spring too early. Recession curve slopes show a good overall correlation.

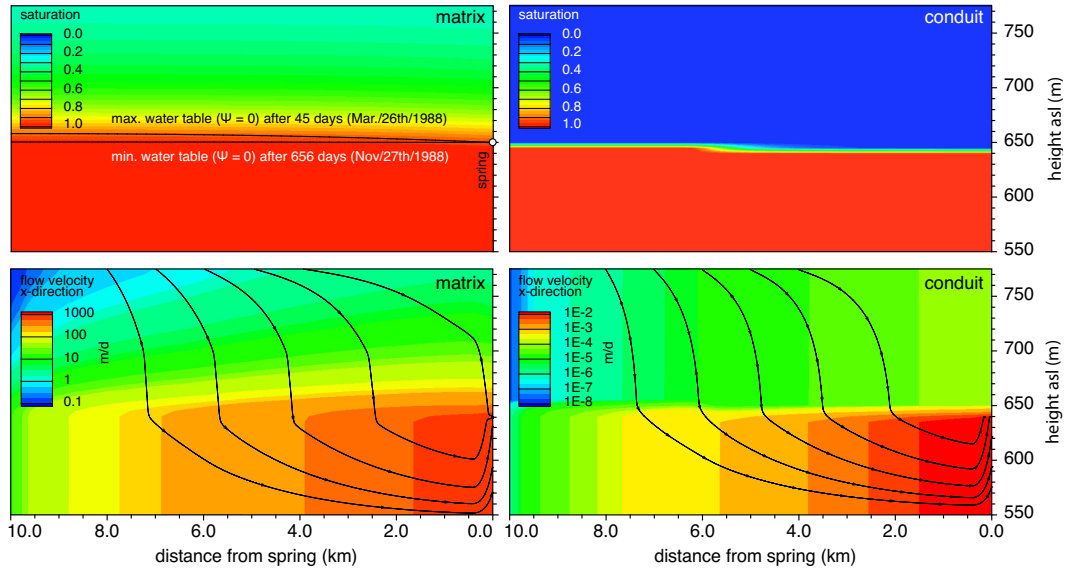


Fig. 5. Results of the transient flow model (Mar./26th/1988). Shown water tables apply for both continua as the height is nearly equal and differs 1 cm at most. The van Genuchten parameter α_m leads to a strong difference between the continua. The capillary rise is more pronounced in the matrix system, where saturation is ca. 0.35 near the surface. Saturation in the conduit system is lower than 0.1 above the water table and below 0.0001 near the surface. Flow velocities (only x-direction vector, note the different scaling for matrix and conduits) are apparently higher in the conduit continuum.

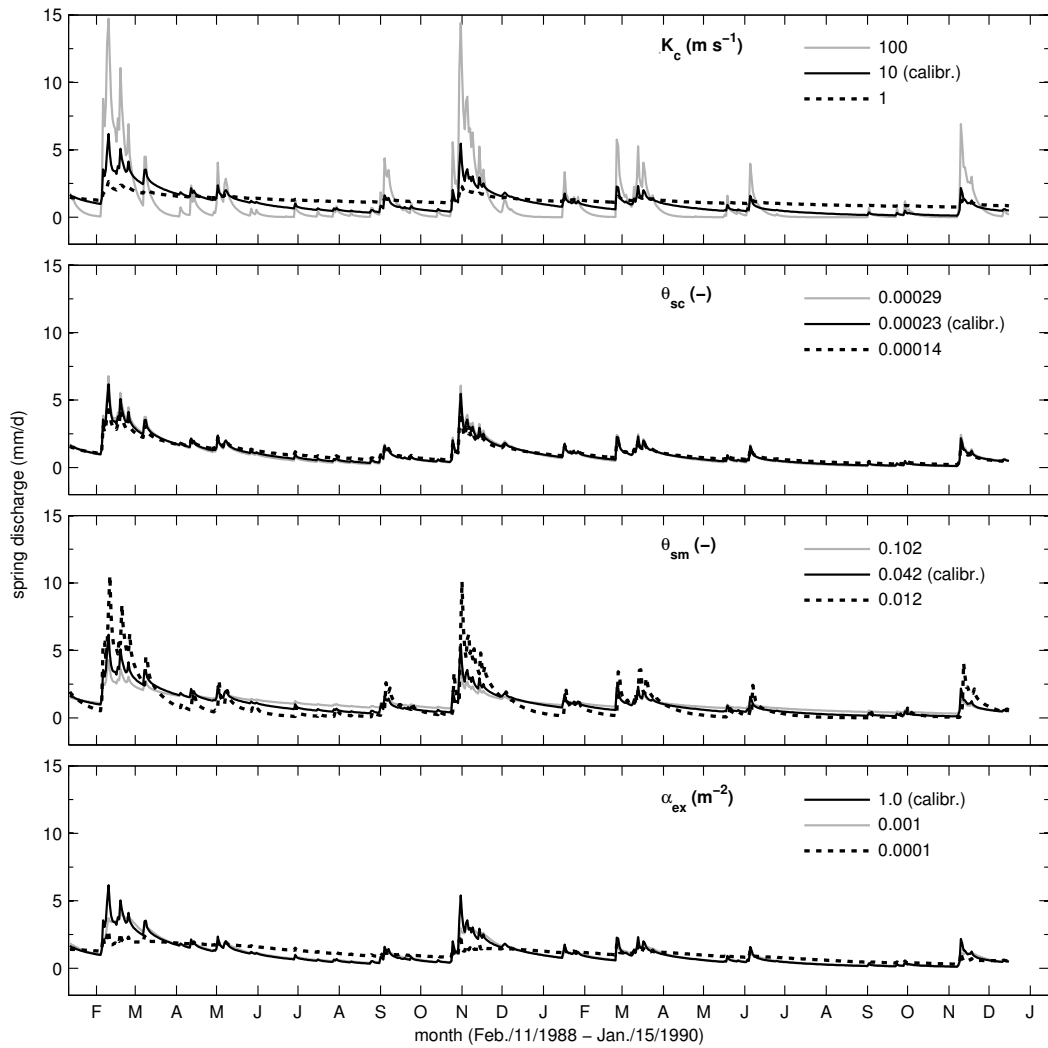


Fig. 6. Variation of hydraulic parameters (K_c , θ_{sc} , θ_{sm}) and the exchange parameter (α_{ex}).

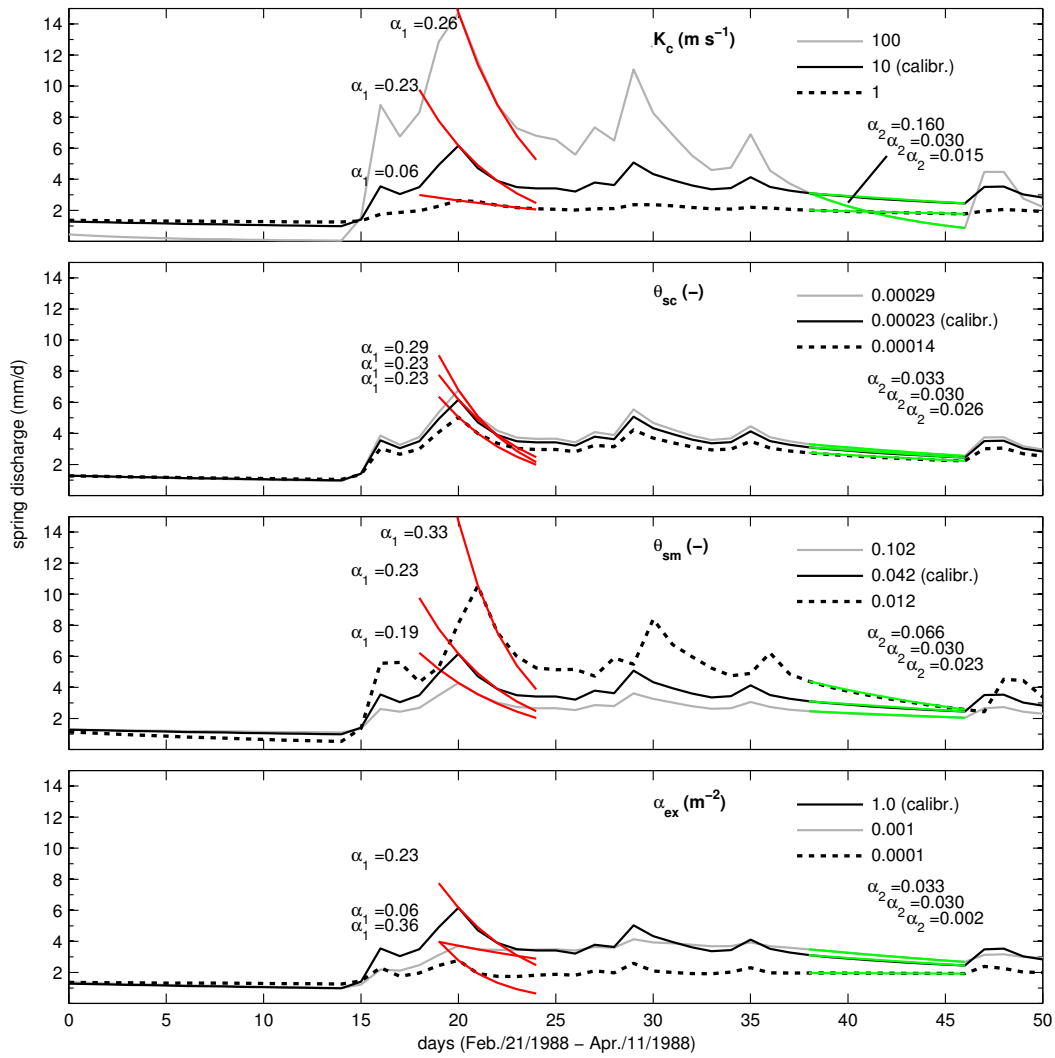


Fig. 7. Variation of hydraulic parameters (K_c , θ_{sc} , θ_{sm}) and the exchange parameter (α_{ex}).

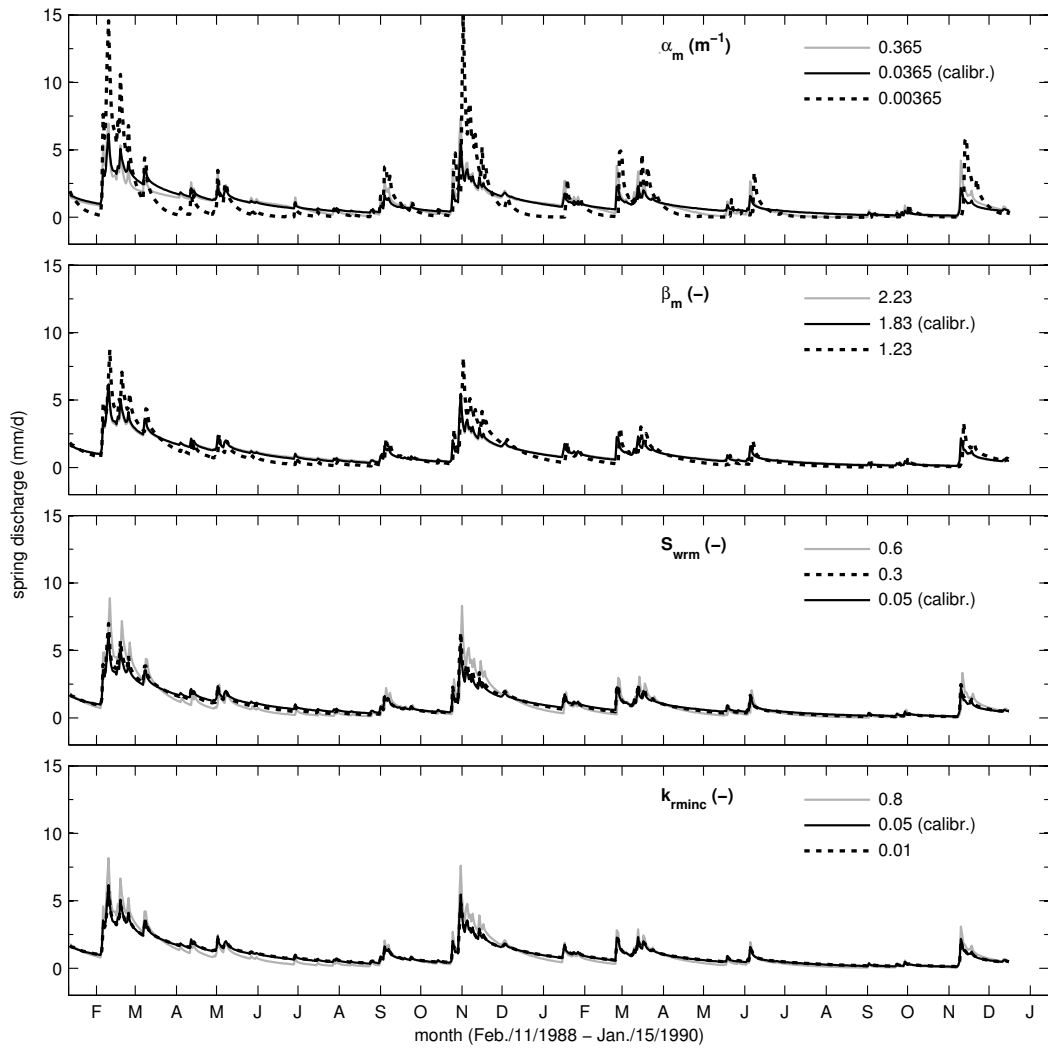


Fig. 8. Variation of the van Genuchten Parameters (α_m , β_m , S_{wrm} , k_{rminc}).

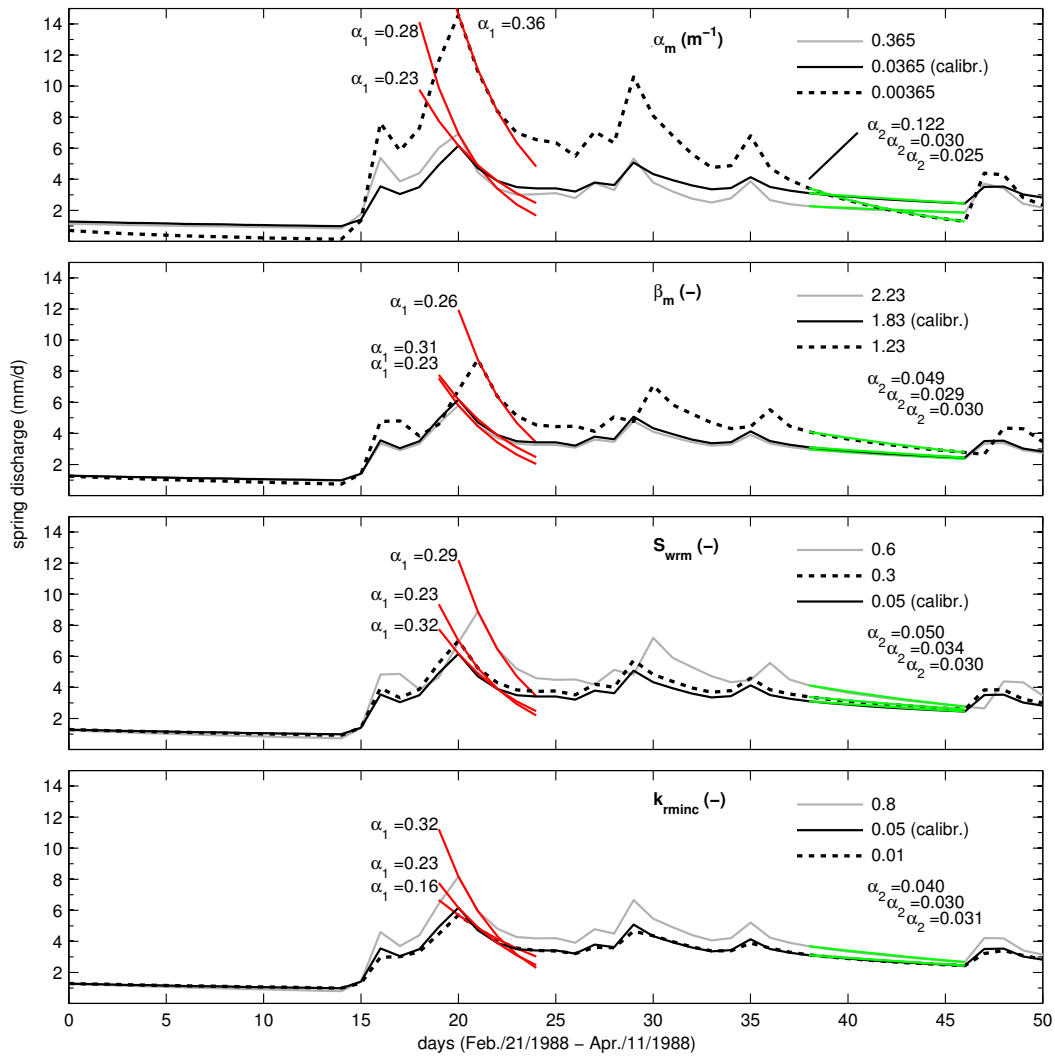


Fig. 9. Variation of the van Genuchten Parameters (α_m , β_m , S_{wrm} , k_{rminc}).

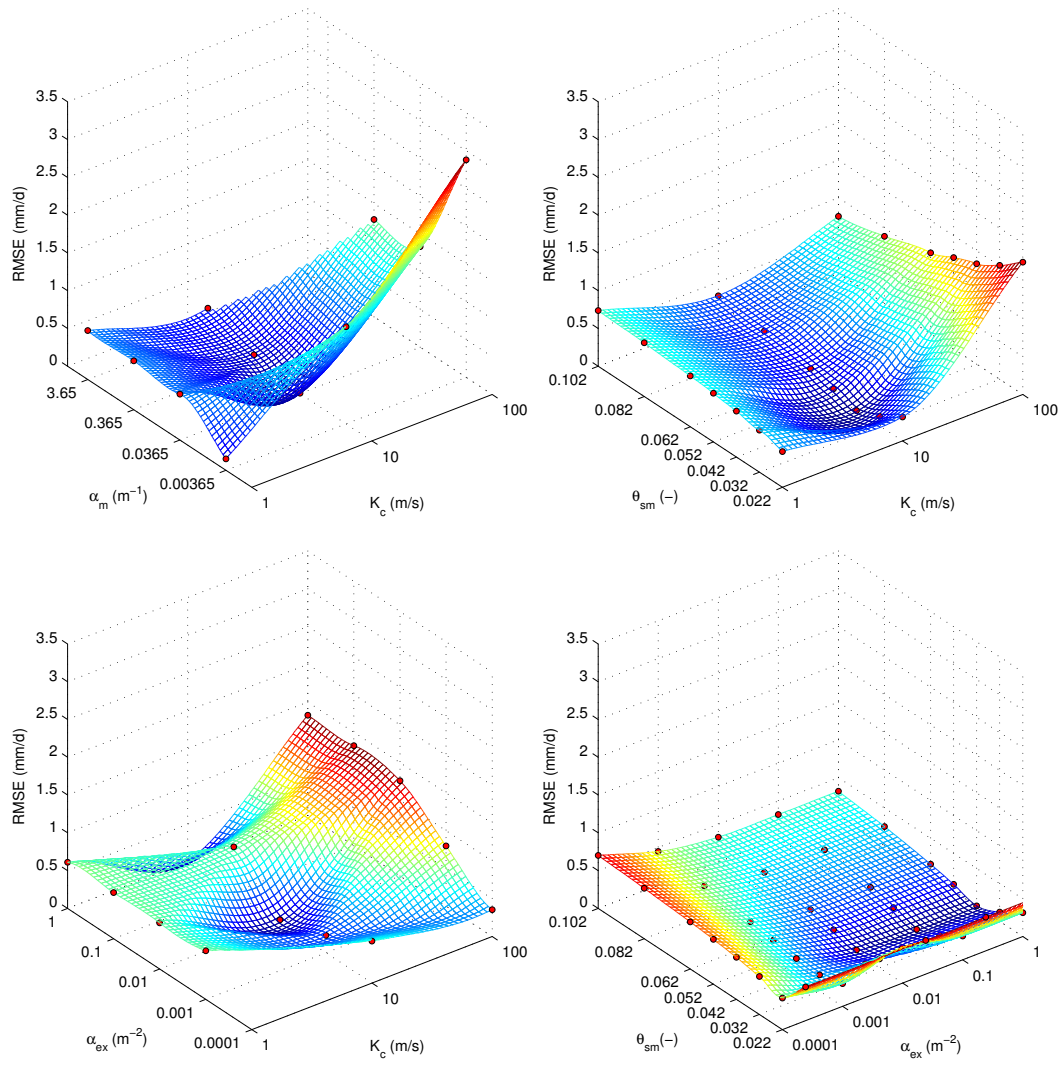


Fig. 10. Sensitivity matrices showing nonlinear inter-parameter dependencies.

Table 1. Estimated values for the flow model derived from the model calibration and value ranges reported in the literature. Subscript m and c denote the matrix resp. the conduit continuum.

Parameter	Unit	Value	Literature Values	Reference ²
K_c	(m/s)	10.0	3.0 - 10.0	1
K_m	(m/s)	2.9×10^{-6}	1.0×10^{-6} - 1.0×10^{-4}	1
θ_{sc} ¹	(-)	0.00023	0.00016 - 0.00064	1
θ_{sm}	(-)	0.042	0.007 - 0.025, >0.0 - 0.12	1,2
α_{ex}	(m ⁻²)	1.0	-	-
Q	(%)	90	-	-
α_m	(m ⁻¹)	0.0365	0.0365, 0.0328 - 0.623	3,4
β_m	(-)	1.83	1.83, 0.01 - 3.0	3,4
S_{wrm}	(-)	0.05	0.01 - 0.05	4
α_c	(-)	5.1	5.1	3
β_c	(-)	2.56	2.56	3
S_{wrc}	(-)	0.0	-	-
k_{rminc}	(-)	0.05	-	-

¹The local conduit continuum porosity is 1.0 i.e. $w_c \theta_{sc(local)} = \theta_{total} - w_m \theta_{sm}$ implicitly gives the total conduit porosity such that $\theta_{sc} \hat{=} w_c \theta_{sc(local)}$. The total porosity is $\theta_{total} = 0.0422$.

²References: 1 - Sauter (1992); 2 - Weiss (1987); 3 - Roulier et al. (2006); 4 - Contractor and Jenson (2000).

Table 2. RMSE values and recession coefficients for all sensitive parameters. Parameters with a maximum RMSE below 0.05 mm/d have been considered as insensitive. Subscript m and c denote the matrix resp. the conduit continuum. Bold numbers denote the calibrated value.

Parameter	Value	Recess. coeff. (1/d)		RMSE (mm/d)
		α_1	α_2	
K_c	100	0.26	0.160	1.329
	10	0.23	0.030	-
	1	0.06	0.015	0.645
θ_{sc}	0.00029	0.29	0.033	0.188
	0.00023	0.23	0.030	-
	0.00014	0.23	0.026	0.108
θ_{sm}	0.102	0.33	0.066	0.318
	0.042	0.23	0.030	-
	0.012	0.19	0.023	0.317
α_{ex}	1.0	0.23	0.033	-
	0.001	0.06	0.030	0.231
	0.0001	0.36	0.002	0.555
α_m	0.365	0.28	0.025	0.329
	0.0365	0.23	0.030	-
	0.00365	0.36	0.122	1.285
β_m	2.23	0.31	0.029	0.064
	1.83	0.23	0.300	-
	1.23	0.26	0.049	0.563
S_{wrm}	0.6	0.29	0.050	0.54
	0.3	0.32	0.034	0.142
	0.05	0.23	0.030	-
k_{rminc}	0.8	0.32	0.040	0.334
	0.05	0.23	0.030	-
	0.01	0.16	0.031	0.068

Table 3. Parameter combinations used for the sensitivity analyses and highest RMSE (mm/d) observed. Bold RMSE values denote a non-linear inter-parameter dependence.

	Range		K_c	K_m	θ_{sc}	θ_{sm}	α_{ex}	Q	α_m	β_m	S_{wrm}	α_c	β_c	S_{wrc}	k_{rminc}
	Low	High													
K_c	1.0	100.0	-												
K_m	2.89×10^{-7}	2.89×10^{-4}	1.34	-											
θ_{sc}	1.40×10^{-4}	2.90×10^{-4}	1.48	0.19	-										
θ_{sm}	0.022	0.102	2.23	0.83	0.89	-									
α_{ex}	1.00×10^{-4}	1.0	1.33	0.56	0.61	0.77	-								
Q	30	95	1.33	0.06	0.23	0.77	0.57	-							
α_m	0.365×10^{-3}	3.65	3.20	1.29	...	-						
β_m	1.23	2.23	0.58	...	1.58	-					
S_{wrm}	0.05	0.6	1.87	...	-				
α_c	3.1	8.1	0.56	-			
β_c	2.16	3.16	0.56	0.56	...	0.25	-		
S_{wrc}	0.0	0.4	0.56	0.01	...	-	
k_{rminc}	0.01	0.8	0.56	0.33	-