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Behavior analysis of convective and stratiform rain using Markovian approach over Mediterranean region from meteorological radar data

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Abstract

The aim of this study is to analyze the chronological behavior of precipitation in the north of Algeria using a Markovian approach. The probabilistic approach presented here proposes to study the evolution of the rainfall phenomenon in two distinct study areas, one located in sea and other located in ground. The data that we have used are provided by the National Office of Meteorology in Algiers (ONM). They are a series of images collected by the meteorological radar of Setif during the rainy season 2001/2002. A decision criterion is established and based on radar reflectivity in order to classify the precipitation events located in both areas. At each radar observation, a state of precipitations is classified, either convective (heavy precipitation) or stratiform (average precipitation) both for the “sea” and for the “ground”. On the whole, a time series of precipitations composed of three states; S_0 (no raining), S_1 (stratiform precipitation) and S_2 (convective precipitation), is obtained for each of the two areas. Thereby, we studied and characterized the behavior of precipitation in time by a Markov chain of order one with three states. Transition probabilities P_{ij} of state S_i to state S_j are calculated. The results show that rainfall is well described by a Markov chain of order one with three states. Indeed, the stationary probabilities, which are calculated by using the Markovian model, and the actual probabilities are almost identical.

1 Introduction

Precipitation is one of the most important variables in the global hydrological cycle, for meteorology, climate and hydrology applications. In general, precipitation can be decomposed into two types; convective and stratiform (Houze, 1993). Convective precipitation is characterized by a large vertical extent and is more intense and of shorter duration than the stratiform precipitation. Stratiform precipitation, however, usually covers large areas horizontally, and it often forms in areas adjacent to convective cells,

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which contribute to a significant portion (40–50 %) of rainfall, even for intense convective systems (Anagnostou, 2005).

The Mediterranean region has a complex orography and land-sea contrast very marked. Due to these geographical properties, the climate has unstable spatial and temporal characteristics (Lionello et al., 2006). This climate is influenced both by the tropical climate and the climate of mid-latitude systems (Trigo et al., 2006; Alpert et al., 2006; Demangeot, 1986). Mediterranean rainfall is extremely variable in this region. Storms occurring in the Mediterranean region provide high intensity and are usually associated with convective events. In Algeria in recent years, there has been a marked decrease in rainfall, with very serious consequences especially in areas where the rainfall amount and distribution were already barely adequate. From an agronomic perspective, the persistent drought during the rainy season is crucial for starting agricultural activities.

In this context, analysis of precipitation data is of great interest to interpret and to predict behavior rainfall as well as to assist in planning and management of water resources. Furthermore, a good description of the stochastic rainfall can help especially in the detection and evaluation of risk situations.

Several statistical techniques to analyze rainfall data collected by rain gauges networks have been published in the literature (e.g. Hess et al., 1989; Di Baldassarre et al., 2006; Jan Lennartsson et al., 2008; Bardossy and Pegram, 2009; Ratnasingham et al., 2009; Ćurić and Janc, 2011). The models used for this purpose can be grouped into four categories, conditional models, random cascade models, Markov chain models and nonparametric models (Hughes et al., 1999; Charles et al., 1999). The first two models require large amounts of data and thereby calculations are intensive (Mehrotra and Sharma, 2005). In contrast, parametric models, when their conditions are satisfied, they are more powerful than nonparametric models (Talagrand, 1996; Mehrotra and Sharma, 2005).

Therefore, the model, which is widely used, is the model based on Markov chains. It has been often used for analyzing of precipitations (e.g. Todorovic and Woolhier, 1975;

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Kantz, 1977; Arruda and Pinto, 1980; Hess et al., 1989; Srikanthan and McMahon, 2001; Whiting et al., 2003; Liana and Elena, 2004; Srikanthan et al., 2009). The first users of Markov chains have shown that it is adequate to describe the sequences of dry days and wet days (e.g. Gabriel and Neumann, 1962; Smith and Schreiber, 1973; Gates and Tong, 1976). The advantage of Markov chains has been highlighted by some authors (Gabriel and Neuman, 1962; Caskey, 1963; Weiss, 1964). Jimoh and Webster (1996) showed that the order one of a Markov model is sufficient to represent the chronological behavior of precipitation.

For this reason, we chose to use Markov chains due to its robustness and because it directly takes into account the influence of the nearest recent past on the next immediate. This chain is a stochastic model, iterative, which determines the probability of transition from a state to another, or a persistent state of a system.

However, many techniques have used only two states (wet, dry) to characterize the precipitation. The scale considered in the best case, was daily (e.g. Moon et al., 1994; Gomez Navaro, 1996). Indeed, no analysis took into account the variability of rainfall intensity and also no analysis have been carried out at the scale of the radar observation.

Precipitation is characterized by a high variability in space, time and intensity (Virmani et al., 1992). Historically, precipitation has been observed locally by rain gauges, often only as accumulated daily amounts. The global distribution of gauges is quite variable, from relatively dense networks in the developed countries to sparsely distributed gauges in developing regions. Over oceans, gauges are almost non-existent, with only a few of them on Algeria. Furthermore, the rain gauge networks provide measurements of precipitation only where they are installed. In Algeria, these data are measured on the scale of the day, which is not sufficient for a study on an appropriate scale. However, radar data are available in real time, and collected even in remote areas where data are difficult or impossible to collect by rain gauges networks. The radar provides continuous coverage in time and space of precipitation fields. The coastal radar offers the particular advantage of being a tool to study the behavior of precipitation both on

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sea and on ground. Its measurements are widely used for hydrological purposes and in the prevention of natural disasters.

For this purpose, our contribution in this paper is to provide a better description of precipitation chronological behavior over the sea and the ground, using measurements of instantaneous weather radar. It is applied to the complex situation of the Mediterranean climate of this region. The probabilistic approach used here is a Markov chain of first order with three states.

2 Presentation of study region and data

Algeria is located on the south shore of the Mediterranean and is bordered to the east by Tunisia and Libya to the south by Niger and Mali, southwest by Mauritania and Western Sahara and the west by Morocco. The rainfall spatial distribution is characterized by a north-south gradient very marked and east-west gradient very low. The rainy season extends from October to March, with maximum rainfall occurring during November–December. In the north, the climate is Mediterranean transit, marked by seasonal oscillations. The annual rainfall average is estimated at about 600 mm. The minimum rainfall is recorded in the southern regions, it is about 50 mm, while the maximum is observed in the Djurdjura massif located in Kabylia and the massif of Edough located at east, where it exceeds 1500 mm.

The data consist of a series of 17 660 images collected by the meteorological radar of Setif (Algeria). This coastal radar located at latitude 36° N, longitude 05° E with an altitude of 1033 m, it records an image of size 512×512 pixels every fifteen minutes. Each pixel coded on four bits, it has a resolution of one km^2 . The representative physical parameter of the radar reflectivity factor is noted Z (mm^6m^{-3}). The conversion of reflectivity factor Z into rainfall intensity R (mm h^{-1}) is obtained using the Eq. (1) (Marshall and Palmer, 1948):

$$Z = 300 * R^{1.5} \quad (1)$$

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The Z can also be converted into dBZ. The technical characteristics of the radar that we have used are given in Table 1.

3 Methodology

3.1 Selection of study area

In order to describe the precipitation behavior on sea and on ground, two study areas have been selected on the space radar. One area is located over the sea and other over the ground (Fig. 1). We only set the size of the area to 15×15 km. This is to avoid high values of the variance in the area that may skew the classification. This situation can occur when a part of precipitation systems pass over the area. The values of each area are obtained by using Eq. (2) which represents the weighted average on the 15×15 pixels of the area.

3.2 Classification of rainfall into three classes

In general, rainfall can be decomposed into two types; convective and stratiform (Houze, 1993). Convective precipitation is characterized by a large vertical extension and is more intense and of shorter duration than the stratiform precipitation. Stratiform precipitation, however, usually covers large areas horizontally, and it often forms in areas adjacent to convective cells.

The radar reflectivity maps can be used to diagnose stratiform and convective precipitation fields (Steiner and Houze, 1997; Hardenberg et al., 2003; Llasat, 2001; Steiner et al., 1995; Rigo and Llasat, 2004). Convective precipitation is characterized by high reflectivity and a clearer spatial intensity gradient (Ferraris and Rebora, 2006; Steiner and Houze, 1997). Several authors propose thresholds to identify convective clouds (e.g., Johnson et al., 1998; Llasat et al., 2005). The National office of meteorology (O.N.M.) of Algiers had adopted the threshold 42 dBZ from which convective clouds are identified. The experiment conducted by the O.N.M. showed that on 422 events of

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a convective data sets references, 89% of these events are identified on the weather radar reflectivities using the threshold 42 dBZ. Below of this threshold, stratiform precipitations are detected. Therefore, in order to classify radar data, we considered that all the convective precipitation (first class), lie in the interval (≥ 42 dBZ) and all stratiform precipitation (second class) have values between 18 dBZ and 42 dBZ (42 dBZ not included). The third class is the class no raining, it is obtained for all reflectivities less than 18 dBZ.

The weighted mean representing the reflectivities of 15×15 pixels from one area, which will be compared with thresholds to determine its class, is calculated by applying Eq. (2):

$$MP = \frac{\sum_{i=1}^{15} \sum_{j=1}^{15} (C(i, j) * P(i, j))}{\sum_{i=1}^{15} \sum_{j=1}^{15} C(i, j)}. \quad (2)$$

where $P(i, j)$ is the pixel value (in dBZ) at position i and j of 15×15 pixels. $C(i, j)$ is the weighting coefficient depending on the position i and j of a pixel (Fig. 2).

The largest coefficient is the central pixel, the farther away from the center, the coefficient value decreases.

We plotted curves showing the evolution of the weighted average of reflectivity factors of 15×15 pixels for each of the two areas during the study period (Fig. 3). It should be noted that these data have been acquired with a time step of fifteen minutes (temporal resolution of the radar).

3.3 Construction of time series of precipitation

To get a better representation, precipitation is classified into three states, stratiform state or convective state, and a third to represent the no raining state. These states are obtained from the following decision criteria:

- Convective state (S_2 : heavy rainfall): if $MP \geq 42$ dBZ.

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- Stratiform state (S_1 : average rainfall): if $18 \text{ dBZ} \leq \text{MP} < 42 \text{ dBZ}$.
- No raining state (S_0 : low or no rainfall): if $\text{MP} < 18 \text{ dBZ}$.

The 17 660 images that we have used in this study correspond to a period of six months, from October 2001 to March 2002. At each radar observation, a state, which is based on the weighted mean calculated by applying Eq. (2), is defined as, either high rainfall, average rainfall or no raining. Thereby, we obtain time series of precipitation, one observed over ground and other over sea. Each is composed of three states, namely “convective”, “stratiform” and “no raining”.

3.4 Markov chain

A Markov chain can be described as a set of states, $S = \{S_0, S_1, \dots, S_m\}$, where the process begins in one of these states and transits from one state to another.

If the chain is in a state S_i at time t , it switches to S_j at time $t + 1$ with a probability which is noted P_{ij} . The probabilities P_{ij} are called transition probabilities. The process may persist in a state with a probability P_{ij} . An initial probability distribution defines the state of the chain at time ($t = 0$), which specifies the initial state.

With a sequence of states in discrete time, the transition probability of the variable of state $S(t)$ at time t

depends only on its state at time $t - 1$. The general form of these probabilities is given by the following expression:

$$P_{ij} = \Pr[S(t + 1) = S_j / S(t) = S_i]. \quad (3)$$

These probabilities can be grouped into a matrix, called the transition matrix and given by the following expression (Eq. 4):

$$\mathbf{M} = \begin{bmatrix} P_{00} & \cdots & P_{0m} \\ \vdots & \ddots & \vdots \\ P_{m0} & \cdots & P_{mm} \end{bmatrix}. \quad (4)$$

They are calculated using the following equation (Eq. 5):

$$P_{ij} = \frac{N_{ij}}{N_i}. \quad (5)$$

where i and $j = 0, 1, \dots, m$. N_{ij} is the number of transitions from state S_i to state S_j , and N_i is the number of transitions from state S_i to any other state.

For a Markov chain with finite state space and transition matrix \mathbf{M} , the evolution over time of the initial probability distribution $\mathbf{Q}(0)$ is given by:

$$\mathbf{Q}(n) = \mathbf{Q}(n-1) * \mathbf{M} = \dots = \mathbf{Q}(0) * \mathbf{M}^n. \quad (6)$$

where $\mathbf{Q}(n)$ is the probability vector at time n . The probability vector is given by the following form:

$$\mathbf{Q}(t) = [P(S_0) P(S_1) \dots P(S_m)]. \quad (7)$$

where $P(S_k)$ is the probability of the state S_k with $k = 0, 1, \dots, m$.

3.5 Analysis using a Markov chain of first order with three states

To analyze the two time series of precipitation obtained in the previous sections by using Markov chains, we set the following assumptions:

- The precipitation process is described by state space $S = \{S_0, S_1, S_2\}$, this is a Markov chain with finite state space.
- The evolution of phenomenon is random: it is a stochastic process.
- The future depends only on the present; it verifies the Markov property (no memory): this is a Markov chain.
- Possible developments of the process does not depend on time, the system verifies the homogeneity property: this is a homogeneous Markov chain.

We therefore used a Markov chain of first order with a state space $S = \{S_0, S_1, S_2\}$. The time series of precipitation are modeled by the graph of the chain given in Fig. 5.

The determination of transition probabilities is an important part for the simulation of Markov processes. For this case study, nine transition probabilities are determined from the Markov chain. These probabilities are grouped into the following matrix (Eq. 8):

$$\mathbf{M} = \begin{bmatrix} P_{00} & P_{01} & P_{02} \\ P_{10} & P_{11} & P_{12} \\ P_{20} & P_{21} & P_{22} \end{bmatrix}. \quad (8)$$

4 Results

It should be noted that three states representing rainfall are considered in this study. The state of high precipitation corresponds to convective precipitation, the state of average precipitation corresponds to stratiform precipitation and the third state is no raining state. A transition matrix has been determined for each of the two study areas during the rainy season from October 2001 to March 2002. The elements of these matrices are calculated using Eq. (5). The results are given in Table 2.

The results show that the probability of finding the same state at the next moment is stronger than that to find a different state for the two areas. The probability of transiting from convective or no raining to no raining or convective, respectively is near zero. For the two areas, these probabilities are interpreted as follows:

- If we have a no raining state, the probability to have a stratiform state at the next moment is greater than the probability to have a convective state.
- The probability of a stratiform state pass to convection state is lower than the probability to transit to no raining state.
- The probability that a convective state is followed by stratiform state is higher than the probability to be followed by no raining state.

4.1 Simulation

According to the theory of Markov stochastic process, we can use the transition probability matrix and the initial probability vector to simulate the evolution of probability distribution over time. Using Eq. (6), we calculated the probability of each state at every moment during the simulation period. The curves showing the evolution of these probabilities are given in Fig. 6.

Simulation results show that the evolution of probability distributions tends towards stationary probabilities. The probability of having a convective or stratiform state is low in sea and in ground. Note that for these two states, however, the probability is smaller in the sea area than in the ground area. In contrast, for the no raining case, the probability values are high for both areas, but more important in sea area than in ground area.

4.2 Validation

To test our model, we have compared the stationary probabilities estimated by applying Markov chains with the actual probabilities of observation series. We calculated the actual probabilities using the following equation (Eq. 9):

$$PA_i = \frac{N_i}{N}. \quad (9)$$

where N_i is the number of states S_i of observation sequence and, N is the length of the observation sequence.

The comparison is carried out using the test $X^2_{(0.05)}$ to judge the 95% significance of the results and then determine if the model is applicable or not. In the case where the calculated $X^2_{(0.05)}$ is lower than the theoretical value (0.05), the model is considered plausible. Test results have been calculated with Eq. (10) and are given in Table 3:

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$$X^2_{(0.05)} = \frac{\sum_{i=0}^2 ((PE_i - PA_i) / PE_i)}{3}. \quad (10)$$

where PE_i and PA_i are the probabilities estimated by the model and the actual probabilities of the observation series, respectively.

The values of the test $X^2_{(0.05)}$ are lower than 0.05, so they indicate that the estimated probabilities and the actual probabilities are almost identical. These results validate the Markov chain model which is used for modeling of precipitation series with three states. It is therefore possible to use the matrix of transition probabilities of the Markov chain to predict the evolution of probability distribution over study area.

4.3 Discussion

The present study attempts to explain the behavior of precipitation in the Mediterranean. However, the coexistence of convective and stratiform rain complicates their understanding. The model takes into account this complexity. Indeed, we have used a Markov chain with three states, representing a convective state, a stratiform state and a no raining state. The results show that it is the no raining state which tends to be the most persisting. Indeed, high probabilities for long sequences are found no rainy. However, they are reaching record highs in the sea area. The dynamic difference of rainfall between ground and sea has been demonstrated in this study. Indeed, the results show that rainy instant tends to favor the rain at the next time in the ground area contrary to the sea area. The climate is more unstable in the ground area than in the area sea and the memory effect more pronounced in the sea area compared with ground area. This can be explained by the fact that the temperature varies more quickly on ground than on sea. The convective precipitation is more frequent in ground than in sea. This explained by the effect of orography on precipitation in the ground of the Mediterranean region. Stratiform regime appears to be relatively similar in both areas.

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Moreover, the test result validation shows that rainfall is well described by Markov chains both in ground and in sea.

5 Conclusions

The main goal of this work was to determine the probability precipitation and to analyze their activities and to discern the difference of behavior between the ground and the sea. It permits to characterize the variability of the convective-stratiform in the Mediterranean region. The model has been validated by the results of test. All the results obtained here are important sources of information for understanding the behavior of precipitation in the region. The drought trend highlighted by Touazi and Laborde (2000) by performing the mapping of rainfall on an annual basis has been confirmed by this study. This drought is mainly due to global climate change which increased the annual average temperatures. The climate becomes increasingly dry in many countries, including Algeria.

Drought can cause considerable implications and serious consequences for the country's development. Environmental conditions responsible to maintain the ecosystem health of wetlands are degraded because the traditional water management considers only the distribution of water between economic departments and the daily lives of people, ignoring the needs in water for ecosystem functions. The quota of water consumption is unevenly distributed and there is a huge imbalance between offer and demand. Today, Algeria is more than ever called upon to take measures necessary to address this deficit. The rational use of water resources and the optimal allocation of water resources is necessary to ensure the sustainable development of areas relating to agriculture and the needs of the population.

Moreover, there are watersheds at high altitude (above 1500 m) that receive heavy rainfall. Thus, Algeria has finally important water resources, but they remain poorly exploited.

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The authorities concerned must firstly initiate projects for the construction of infrastructure (dams) to hold this water and also expand the measuring device that will allow a better understanding of water resources.

In addition to these factors, the lack of available scientific research has complicated the understanding of water cycle. For these reasons, the plan Orsec has been declared and the rationalization of water distribution has been respected. This work here is part of this logic for the development of methods for assessing water resources and evaluating drought risk in Algeria.

Perspective, further analysis of rainfall in this region deserves to be carried out with dynamic climate models. Indeed, the Markov assumptions used in this article do not represent the all activity rainfall. The rainfall intensity depends on the season and it is linked to the situation day or night. It would be interesting to test this technique over long periods of observation and use of non-homogeneous Markov chains by increasing the order.

References

- Alpert, P., Baldi, M., Ilani, R., Krichak, S., Price, C., Rodó, X., Saaroni, H., Ziv, B., Kishcha, P., Barkan, J., Mariotti, A., and Xoplaki, E.: Relations between climate variability in the Mediterranean region and the tropics: ENSO, South Asian and African monsoons, hurricanes and Saharan dust, *Mediterranean Climate Variability*, Elsevier B. V., 149–177, 2006.
- Anagnostou, E. N.: A convective/stratiform precipitation classification algorithm for volume scanning weather radar observations, *Meteorol. Appl.*, 11, 291–300, 2005.
- Arruda, H. V. and Pinto, H. S.: An alternative model for dry-spell probability analysis, *Mon. Weather Rev.*, 108, 823–825, 1980.
- Bárdossy, A. and Pegram, G. G. S.: Copula based multisite model for daily precipitation simulation, *Hydrol. Earth Syst. Sci.*, 13, 2299–2314, doi:10.5194/hess-13-2299-2009, 2009.
- Caskey, J. E.: Markov Chain Model for the probability of precipitation occurrence in intervals of various length, *Mon. Weather Rev.*, 91, 298–301, 1963.

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Ćurić, M. and Janc, D.: Analysis of predicted and observed accumulated convective precipitation in the area with frequent split storms, *Hydrol. Earth Syst. Sci.*, 15, 3651–3658, doi:10.5194/hess-15-3651-2011, 2011.

Gabriel, K. R. and Neumann, J.: A Markov chain model for daily rainfall occurrence at Tel Aviv, *Q. J. Roy. Meteorol. Soc.*, 88, 90–95, 1962.

Gómez Narvaro, L.: Calcul par les chaînes de Markov des probabilités de durée des séquences sèches et pluvieuses en Espagne, *Publ. Assoc. Int. Climatol.* 9, 203–209, 1996.

Hess, G. D., Leslie, L. M., Guymer, A. E., and Fraedrich, K.: Application of a Markov technique to the operational, short-term forecasting of rainfall, *Aust. Meteorol. Mag.*, 37, 83–91, 1989.

Houze Jr., R. A.: *Cloud dynamics*, Academic Press, 573 pp., 1993.

Hughes, J. P., Guttorp, P., and Charles, S.: A non-homogeneous hidden Markov model for precipitation occurrence, *Appl. Statist.*, 48, 15–30, 1999.

Dernangeot, J.: *Les milieux “naturels” du globe*, 2nd Edn., Masson, Paris, 1986.

Di Baldassarre, G., Castellarin, A., and Brath, A.: Relationships between statistics of rainfall extremes and mean annual precipitation: an application for design-storm estimation in northern central Italy, *Hydrol. Earth Syst. Sci.*, 10, 589–601, doi:10.5194/hess-10-589-2006, 2006.

Johnson, J. T., MacKeen, P. L., Witt, A., Mitchell, E. D., Stumpf, G. J., Eilts, M. D., and Thomas, K. W.: The Storm Cell Identification and Tracking (SCIT) algorithm: An enhanced WSR-88D algorithm, *Weather Forecast.*, 13, 263–276, 1998.

Katz, R. W.: Precipitation as a chain-dependent process, *J. Appl. Meteorol.*, 16, 671–676, 1977.

Lennartsson, J., Anastassia, B., and Deliang, C.: Modelling precipitation in Sweden using multiple step markov chains and a composite model, *J. Hydrol.*, 363, 42–59, 2008.

Llasat, M. C.: An objective classification of rainfall events on the basis of their convective features, Application to rainfall intensity in the North-East of Spain, *Int. J. Climatol.*, 21, 1385–1400, 2001.

Llasat, M. C., Rigo, T., Ceperuelo, M., and Barrera, A.: Estimation of the convective precipitation: the meteorological radar versus an automatic raingauge network, *Adv. Geosci.*, 2, 103–109, 2005, <http://www.adv-geosci.net/2/103/2005/>.

Lionello, P., Malanotte-Rizzoli, P., Boscolo, R., Alpert, P., Artale, V., Li, L., Luterbacher, J., May, W., Trigo, R., Tsimplis, M., Ulbrich, U., and Xoplaki, E.: The Mediterranean Climate: An overview of the main characteristics and issues, *Mediterranean Climate Variability*, Elsevier B. V., 1–26, 2006.

- Marshall, J. S. and Palmer, W. M.: The distribution of raindrops with size, *J. Meteorol.*, 5, 165–166, 1948.
- Mehrotra, R. and Sharma, A.: A non-parametric non-homogeneous hidden Markov model for downscaling of multi-site daily rainfall occurrences, *J. Geophys. Res.*, 110, D16108, doi:10.1029/2004JD005677, 2005.
- Mehrotra, R., Srikanthan, R., and Sharma, A.: A comparison of three stochastic multi-site precipitation occurrence generators, *J. Hydrol.*, 331, 280–292, 2006.
- Moon, S. E., Ryoo, S. B., and Known, J. G.: A Markov chain model for daily precipitation occurrence in South Korea, *Int. J. Climatol.*, 14, 1009–1016, 1994.
- Ratnasingham, S., Geoffrey, G., and Pegram, S.: A nested multisite daily rainfall stochastic generation model, *J. Hydrol.*, 371, 142–153, 2009.
- Rigo, T. and Llasat, M. C.: A methodology for the classification of convective structures using meteorological radar: Application to heavy rainfall events on the Mediterranean coast of the Iberian Peninsula, *Nat. Hazards Earth Syst. Sci.*, 4, 59–68, doi:10.5194/nhess-4-59-2004, 2004.
- Srikanthan, R. and McMahon, T. A.: Stochastic generation of annual, monthly and daily climate data: A review, *Hydrol. Earth Syst. Sci.*, 5, 653–670, doi:10.5194/hess-5-653-2001, 2001.
- Steiner, M. and Houze Jr., R. A.: Sensitivity of estimated monthly convective rain fraction to the choice of Z-R relation, *J Appl. Meteorol.*, 36, 452–462, 1997
- Talagrand, M.: The Glivenko-Cantelli Problem, Ten Years Later, *J. Theor. Probab.*, 9, 371–384, doi:10.1007/BF02214655, 1996.
- Todorovic, P. and Woolhiser, D. A.: A stochastic model of n-day precipitation, *J. Appl. Prob.*, 12, 488–497, 1975.
- Touazi, M. and Laborde, J. P.: Cartographie des pluies annuelles en Algérie du nord, *Association Internationale de Climatologie*, 13, 192–198, 2000.
- Trigo, R. M., Xoplaki, E., Lüterbacher, J., Krichak, S. O., Alpert, P., Jacobeit, J., Sáenz, J., Fernández, J., and González-Rouco, J. F.: Relationship between variability in the Mediterranean region and mid-latitude variability, *Mediterranean Climate Variability*, Elsevier, B. V., 179–226, 2006.
- Virmani, S. M., Sivakumar, M. V. K., and Reddy, S. J.: Rainfall probability for selected locations of semi-srid india, *Research bulletin no. 1, 2nd Edn.-ICRISAT, Patancheru, India*, 1992.
- Von Hardenberg, J., Ferraris, L., and Provenzale, A.: The shape of convective rain cells, *Geophys. Res. Lett.*, 30, 2280, doi:10.1029/2003GL018539, 2003.

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Weiss, L. L.: Sequences of wet or dry days described by a Markov chain probability model, Mon. Weather Rev., 92, 169–176, 1964.

Whiting, J. P., Lambert, M. F., and Metcalfe, A. V.: Modelling persistence in annual Australia point rainfall, Hydrol. Earth Syst. Sci., 7, 197–211, doi:10.5194/hess-7-197-2003, 2003.

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9, 6225–6250, 2012

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Table 2. Results of Transition probabilities matrix.

Study area	Ground			Sea		
	S_0	S_1	S_2	S_0	S_1	S_2
S_0	0.83	0.25	0.07	0.88	0.22	0.06
S_1	0.14	0.61	0.41	0.11	0.67	0.37
S_2	0.03	0.14	0.52	0.01	0.11	0.57

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Table 3. Estimated probabilities and actual probabilities.

Study area state	Ground		Sea	
	estimated values (PE_i)	actual values (PA_i)	estimated values (PE_i)	actual values (PA_i)
Convective	0.1496	0.1482	0.0882	0.0862
Stratiform	0.3434	0.3501	0.5070	0.5017
No-raining	0.2879	0.2930	0.6239	0.6208
Test: $\chi^2_{(0.05)}$	0.0131		0.0151	



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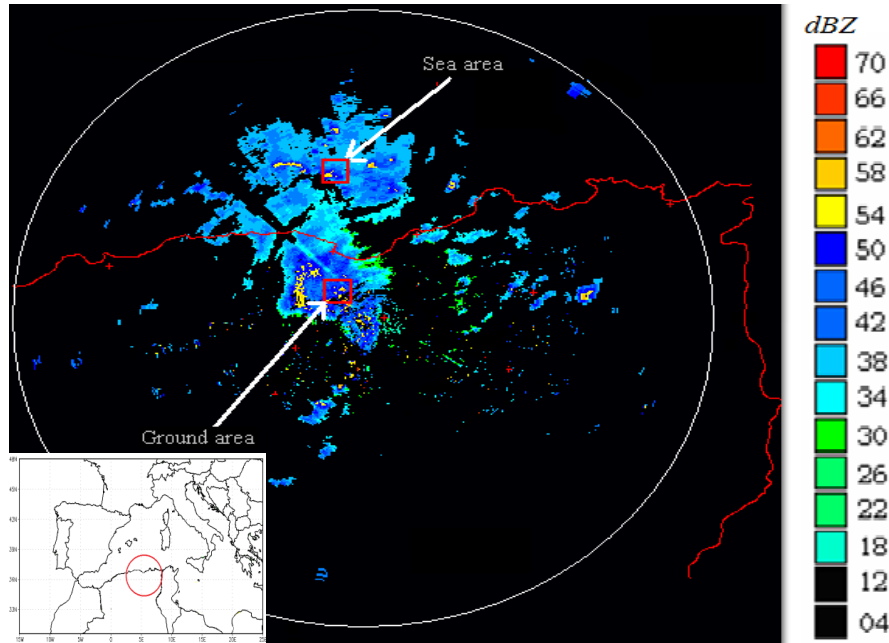


Fig. 1. Location of study areas.

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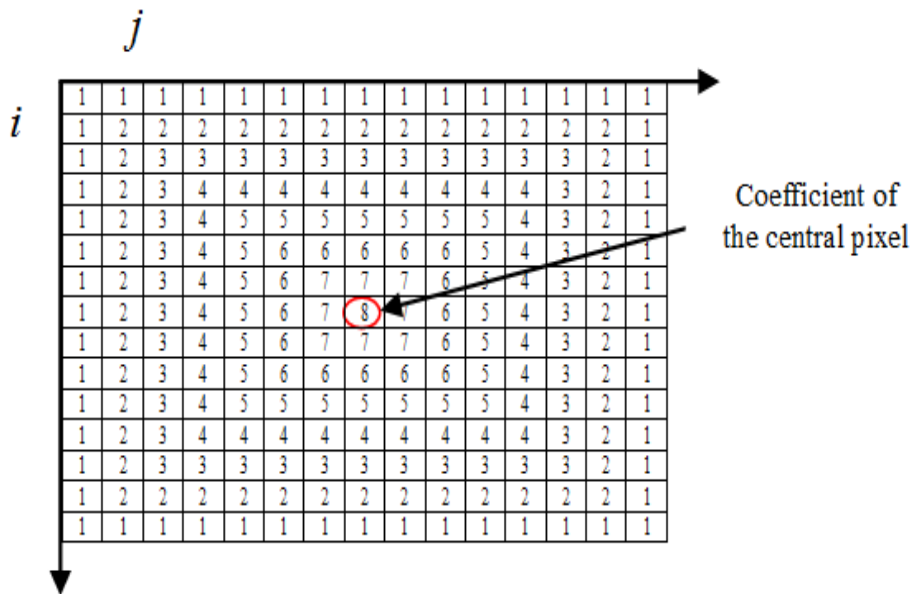


Fig. 2. Weighting coefficients of the area.

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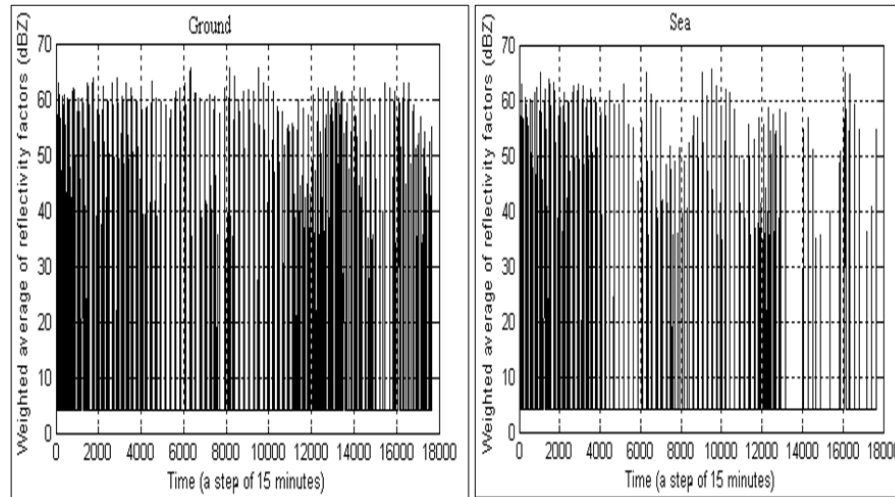


Fig. 3. The evolution of weighted mean of radar reflectivities over time.

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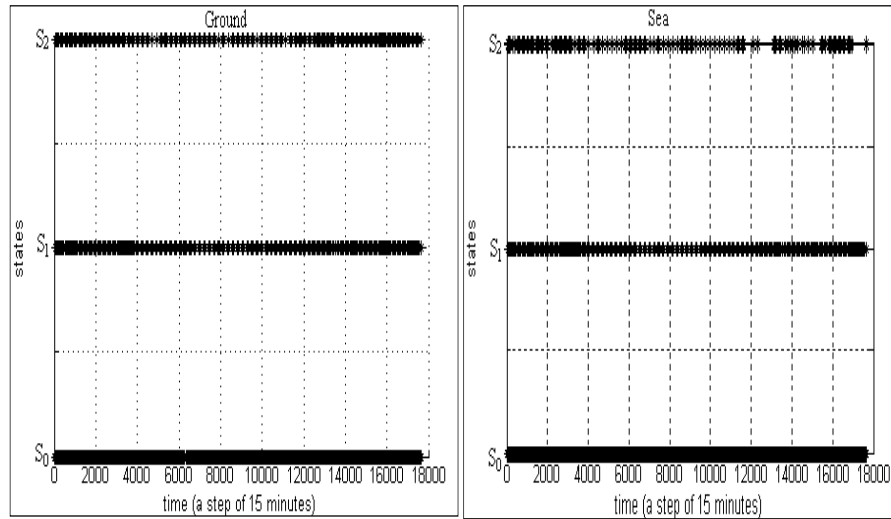
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**Fig. 4.** Observation series of precipitation with three states.

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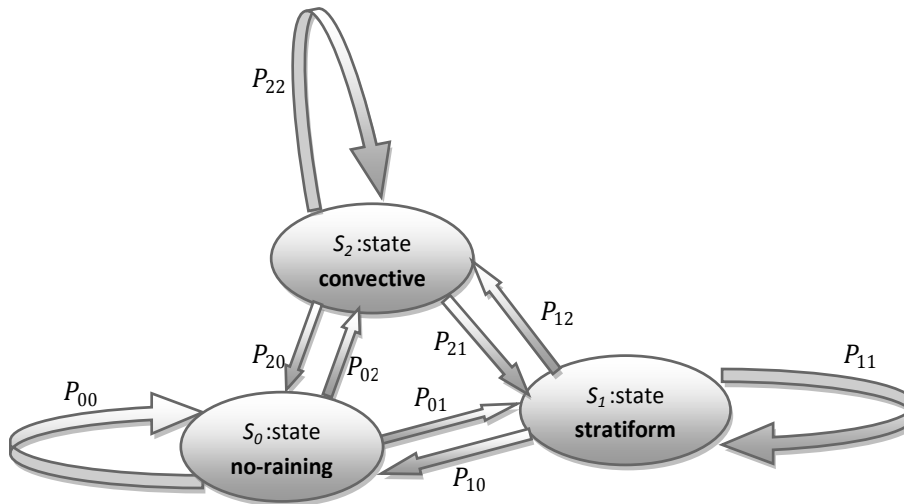
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**Fig. 5.** Graph of Markov chain of precipitation.

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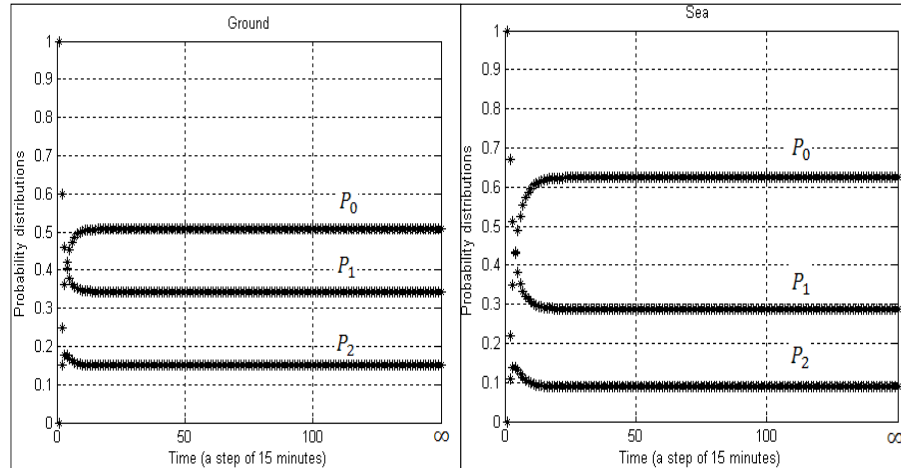


Fig. 6. The evolution of probability distributions.

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