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An analytical solution for tidal dynamics in the Yangtze Estuary, China

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Abstract

An analytical model for tidal dynamics has been applied to the Yangtze Estuary, a large branched estuary with three-order branches and four outlets to the sea. This study shows that the analytical model developed for a single-channel estuary can also accurately describe the tidal dynamics in a branched estuary, particularly in the downstream part. For given geometry, friction, and tidal amplitude at the mouth of every branch, the tidal damping/amplification, the phase lag, the wave celerity, and the velocity amplitude along the estuary can be computed. Within the same estuary system, the North Branch and the South Branches have a distinct tidal behavior: the former being amplified demonstrating a marine character and the latter being damped with a riverine character. The satisfactory results for the South Channel and the South Branch using both separate and combined topographies confirm that the branched estuary system functions as an entity. To further test these results, it is suggested to collect more accurate and dense bathymetric and tidal information.

1 Introduction

There exists a long tradition of analytical solutions for tidal dynamics in convergent estuaries (Dronkers, 1964; Harleman, 1966; Ippen, 1966; Prandle and Rahman, 1980; Jay, 1991; Friedrichs and Aubrey, 1994; Lanzoni and Seminara, 1998; Savenije, 1998, 2001, 2005; Prandle, 2003; Horrevoets et al., 2004; Savenije and Veling, 2005; Savenije et al., 2008; Toffolon and Savenije, 2011). These solutions were usually derived for single-channel estuaries, with different assumptions to simplify or linearise the non-linear set of equations. Most solutions use Lorentz' (1926) linearization, except Savenije (1998) who determined tidal damping by subtracting high water (HW) and low water (LW) envelopes maintaining the non-linear friction term. Whereas the linearised solution is correct for a simple M2 harmonic, Savenije's (1998) solution implicitly allows some wave deformation. This solution further assumes an exponentially converging

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estuaries where the geometry of channels cannot be described by a single exponential function, multiple reaches can be used, where i represents the reach number ($i = 1, 2, 3, \dots$, beginning from the mouth), a_i and b_i are the area and width convergence length for reach i , $x_{(i-1)}$ is the inflection point, and $A_{(i-1)}$, $B_{(i-1)}$, and $h_{(i-1)}$ are the cross-sectional area, width and depth at the inflection point.

The tidal dynamics in an alluvial estuary can be described by the following set of one-dimensional equations (Savenije et al., 2008):

$$\frac{\partial U}{\partial t} + U \frac{\partial U}{\partial x} + g \frac{\partial z}{\partial x} + g \sigma + g \frac{U|U|}{C^2 h} = 0 \quad (4)$$

$$r_s \frac{\partial z}{\partial t} + U \frac{\partial z}{\partial x} + h \frac{\partial U}{\partial x} - \frac{hU}{a} = 0 \quad (5)$$

where U is the tidal flow velocity, g is the acceleration due to gravity, z is water level fluctuation, $\sigma = \partial(z_b + \bar{h})/\partial x - h/(2\rho)\partial\rho/\partial x$ includes the free surface residual slope and the density term, z_b is bottom elevation, \bar{h} is the tidal average water level, $h = z + \bar{h}$ is water level, ρ is water density, C is Chezy's friction factor, r_s is the ratio between the storage width and the stream width, a is the area convergence length.

Equations (4) and (5) can be written in the form of four implicit analytical equations, as described by Savenije (2005) and Savenije et al. (2008):

Phase lag equation:

$$\tan \varepsilon = \frac{\omega a}{c} \left/ \left(1 - \frac{a}{\eta} \frac{d\eta}{dx} \right) \right. \quad (6)$$

Scaling equation:

$$r_s \frac{\eta}{h} = \frac{\omega}{c} \frac{1}{\sin \varepsilon} \quad (7)$$

Damping/Amplification equation:

$$\frac{1}{\eta} \frac{d\eta}{dx} \left(\frac{1 + \alpha}{\alpha} \right) = \frac{1}{a} - f \frac{\omega \sin \varepsilon}{hc} \quad (8)$$

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Celerity equation:

$$c^2 = \frac{1}{r_s} g \bar{h} / \left[1 - \frac{\sin \varepsilon \cos \varepsilon}{(1 + \alpha)} \left(\frac{c}{\omega a} - f \frac{\nu \sin \varepsilon}{\omega \bar{h}} \right) \right] = \frac{c_0^2}{1 - D} \quad (9)$$

where ε is the phase lag between high water (HW) and high water slack (HWS) (or between low water, LW, and low water slack, LWS), $\omega = 2\pi/T$ is tidal frequency, c is the actual tidal wave celerity for average depth, η is the amplitude of water level fluctuation z , ν is the amplitude of tidal velocity U , $\alpha = \nu \sin \varepsilon / (g \eta)$ is a tidal Froude number, f is dimensionless friction factor, c_0 is the classical tidal wave celerity, and D is the damping term.

Additionally, a damping number δ is defined as:

$$\delta = \frac{1}{\eta} \frac{d\eta}{dx} \frac{c_0}{\omega} \quad (10)$$

Four dimensionless parameters χ , γ , μ , and λ are introduced, which are friction number, estuary shape number, velocity number, and celerity number, respectively, as the following definitions:

$$\chi = r_s f \frac{c_0 \eta}{\omega \bar{h}^2} \quad (11)$$

$$\gamma = \frac{c_0}{\omega a} \quad (12)$$

$$\mu = \frac{1}{r_s} \frac{\nu \bar{h}}{\eta c_0} \quad (13)$$

$$\lambda = \frac{c_0}{c} \quad (14)$$

where c_0 and f can be calculated by means of the following equations:

$$c_0 = \sqrt{\frac{g \bar{h}}{r_s}} \quad (15)$$

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$$f = \frac{g}{K^2 h^{-1/3}} \left/ \left(1 - \left(\frac{1.33\eta}{h} \right)^2 \right) \right. \quad (16)$$

where $K = 1/n$ is the Manning-Strickler friction factor, n is Manning's coefficient.

Based on Eqs. (6–16), the solutions for different wave types can be derived. For the mixed wave where $\lambda^2 \neq 0$, the damping number, celerity number, phase lag, and velocity number can be described by the following relations.

$$\delta = \frac{\gamma - \chi\mu^2}{2} \quad (17)$$

$$\lambda^2 = \frac{\chi^2\mu^4 - \gamma^2}{4} + 1 \quad (18)$$

$$\tan \varepsilon = \frac{\lambda}{\gamma - \delta} \quad (19)$$

$$\mu = \sqrt{\frac{1}{3\chi} \left(m - \gamma + \frac{\gamma^2 - 6}{m} \right)} \quad (20a)$$

$$m = \left[27\chi + (9 - \gamma^2)\gamma + 3\sqrt{3}\sqrt{27\chi^2 + 2(9 - \gamma^2)\gamma\chi + 8 - \gamma^2} \right]^{1/3} \quad (20b)$$

For the special case where $\lambda^2 = 0$ (the apparently standing wave), the following relations can be obtained (the subscript s represents the apparently standing wave):

$$\delta_s = \mu_s = \frac{1}{2} \left(\gamma - \sqrt{\gamma^2 - 4} \right) \quad (21)$$

$$\lambda_s = \varepsilon_s = 0 \quad (22)$$

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The critical convergence γ_c is introduced, which is the transition point between these two wave types, given by:

$$\gamma_c = \frac{1}{3\chi} \left[\frac{m_1}{2} - 1 + 2 \frac{(12\chi^2 + 1)}{m_1} \right] \quad (23a)$$

$$m_1 = \left[36\chi^2(3\chi^2 + 8) - 8 + 12\chi \sqrt{3} \sqrt{(\chi^2 - 2)^2(27\chi^2 - 4)} \right]^{1/3} \quad (23b)$$

5 If $\gamma < \gamma_c$ the solution for the mixed wave exists, while the solution for the standing wave is for the case where $\gamma > \gamma_c$.

For a longitudinal solution, the variable η needs to be determined through integration of the damping number δ . Based on Eq. (10), and using the tidal amplitude at the seaward boundary η_0 , the damping number can be integrated stepwise. The two
10 unknown parameters are: the Manning-Strickler friction factor K and the storage width ratio r_s , which can be obtained by calibrating the computed results against measurements. Thus, for a given topography the parameters of tidal propagation along the estuary can be computed by means of Eqs. (10)–(23).

3 The Yangtze Estuary

15 3.1 Overview of the Yangtze Estuary

The Yangtze Estuary is the part of the Yangtze River system downstream from Datong where the tidal limit is (Fig. 1). It has an approximate length of 630 km and a mouth which is about 90 km wide. Downstream from Xuliujing, the estuary branches into the North Branch and the South Branch forming Chongming Island. Further down, the
20 South Branch branches into the North Channel and the South Channel, forming the Changxing Island and Hengsha Island. Finally, the South Channel branches into the North Passage and the South Passage forming Jiuduansha Island. As a result, the

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estuary has three-order branches and four outlets to the sea. Among this branched part, except for the North Branch, the southern estuary system is called “the Southern Branches”. The reach upstream from the junction of the North Branch and the South Branch to Datong is called “the Upper Reach”.

The Yangtze Estuary experiences a meso-scale tide with a mean and maximum tidal range of 2.67 and 4.62 m, respectively near the mouth at Zhongjun station (Shen et al., 2003). It has an irregular semi-diurnal character. Near the mouth, the average flood and ebb duration are 5 and 7.4 h, respectively. The limit of the tidal current lies near Jiangyin (about 214 km from the estuary mouth), while the tidal limit is located near Datong, the location of which can vary with the river discharge.

The Yangtze Estuary receives a large amount of fresh water, with a mean annual discharge of $28310 \text{ m}^3 \text{ s}^{-1}$ at Datong (1950–2009), and large seasonal and annual variation. Downstream from Xuliujing, the majority of the fresh water flows into the South Branch. Because the channel of the North Branch is almost perpendicular to the main channel, the freshwater inflow of the North Branch is very small: less than 1 % and even 0.4 % of the Yangtze River discharge in recent years (Chen and Chen, 2003; Yu et al., 2003; Tan and Wang, 2004; Zhang et al., 2011). Therefore, the South Branches deliver almost all fresh water from the Yangtze River to the sea. According to the Canter-Cremers number $N(N = Q_f T / P_t, T$ is the tidal period, P_t is the tidal prism), the North Branch is a marine well-mixed channel, and the South Branches are more riverine with a partially-mixed character which becomes well-mixed situation during the dry season (Zhang et al., 2011).

3.2 Shape of the Yangtze Estuary

The shape of the Yangtze Estuary can be described by exponential functions (see Eqs. 1–3), which correspond well with observations (squares, diamonds, and triangles in Fig. 2). Good fits are obtained both for individual and combined channels. The Combined South Channel is the combination of the South Passage and North Passage (0–33 km), adding the South Channel (33–70 km). And the Combined South Branch

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is the combination of the Combined South Channel and the North Channel (0–64 km), adding the South Branch (64–113 km). Upstream from 113 km, following the South Branch, is the Upper Reach. The width and area of the combined channel are the sum of the widths and areas of corresponding separate channels. The depth of the combined channel is the ratio of combined area to combined width.

It can be seen that the combined channels such as 0–33 km of the Combined South Channel and 0–64 km of the Combined South Branch, behave similar to a single channel, connecting well with the upper reach and demonstrating a regular topography. This suggests that morphologically the estuary system functions as a unity. Comparing the North Branch to the South Branches, we see clear differences in characteristics. In the North Branch, the width and depth both decrease upstream from the mouth. However, in the South Branches the width decreases mildly and there is a slight increase of the depth. This is due to the marine character of the North Branch, which is a short estuary with a length close to the resonance length of the tide ($c_0T/4$), while the South Branches have a more riverine character, being long compared to the tidal wave length. Riverine estuaries generally have no bottom slope whereas short estuaries do (Savenije, 2005).

4 Calculation of tidal dynamics for the Yangtze Estuary

4.1 Approach

Our previous research in the Yangtze Estuary demonstrated that the branched estuary system functions as an entity in terms of salt intrusion (Zhang et al., 2011). The same phenomenon was observed by Nguyen and Savenije (2006) and Nguyen et al. (2008) in the Mekong delta system. Based on this observation for salt intrusion, we expect that for tidal dynamics the branched estuary system would function as an entity as well. Hence we consider both single branches and combined channels in the system of the “South Branches”: North Branch, North Channel, North Passage, South Passage, the

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Combined South Channel and the Combined South Branch with Upper Reach. Thus, for the single branches: the North Branch, the North Channel, the North Passage, and the South Passage, computations are directly based on their individual topography and Eqs. (10)–(23). For the South Channel and the South Branch, computation continues from the junction of the North Passage and South Passage (junction 1), where the inputs of tidal amplitude and t-LW and t-HW are the weighted average of these two channels whose cross-sectional areas at the junction are taken as the weight. Similarly, at the junction of the South Channel and the North Channel (junction 2), the values are the weighted averages. At the junction of the South Branch and the North Branch, we do not consider the North Branch whose effect is considered to be small. The Upper Reach computation continues upstream directly from the South Branch.

4.2 Calibration

The tidal observations of high water level (HW), low water level (LW), and their timing (t-LW and t-HW) at 19 stations along the Yangtze Estuary on 21–22, 29–30 December 2006 (Fig. 1) have been used to calibrate the model. The Manning-Strickler friction factor K and storage width ratio r_s (Table 1) have been determined by calibrating the computed curves of longitudinal tidal damping/amplification and travel time of tidal wave against measurements. The computed results are presented in Fig. 3, with satisfactory fit to the measurements. Only the computed tidal travel time cannot nicely fit the measurements at Qinglonggang station (75 km) of the North Branch during spring tide particularly for high water (Fig. 3d). For the South Branches and Upper Reach, the computed travel time for low water is slightly higher than the observations. For better presentation of the South Branches, continuity between upper reach and lower branched channels, distances from the mouth for the South Passage, North Passage, South Channel, and North Channel in plots (b, c, f–i) are based on the topography of the Combined South Branch and Upper Reach. In the legend of these plots, the abbreviations SP, NP, SC, NC represent the South Passage, the North Passage, the South Channel, and the North Channel, respectively, and SB&UR stands for the South

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Branch (64 km–113 km) and Upper Reach. These abbreviations are used in the following figures as well.

The Manning's coefficient is an important parameter for the model. It is an index of the resistance to flow in a channel, which results from the interaction of many elements, such as particles of streambed material, bank irregularity, vegetation, channel alignment, bed forms, channel obstructions, converging or diverging streamlines, sediment load, and surface waves (Limerinos, 1969). In estuaries, the Manning's coefficient n is considered to lie between 0.033 and 0.04 for less turbid estuaries (Henderson, 1966; King and Wolanski, 1996). However, for turbid estuaries this value can be much smaller, such as the Fly River estuary in Papua New Guinea and the South Alligator River estuary in Australia with the values 0.015–0.02 (King and Wolanski, 1996), which may be due to the presence, in some areas, of fluid mud near the bottom, enabling the bulk of the flow to slip over muddy layers, thus decreasing the bottom stress (Wolanski, et al., 1992).

In the Yangtze Estuary, the n values for most channels we obtain are smaller than 0.02 with the minimum of 0.011, i.e. the Manning-Strickler friction factor K is 50–90 (Table 1), which agree with the values 0.02–0.01 used in some previous numerical-model research which usually cover the estuary downstream from Tianshenggang (162 km) or Jiangyin (214 km) (Wang, 1992; Zhou and Wu, 1994; Shi et al., 2003; Yu et al., 2007; Liu et al., 2010; Kong et al., 2010). The small n values are probably related to the turbid characteristic in the Yangtze Estuary as well. The smallest value in the North Channel (0.011) is in accordance with the previous research by Wang et al. (1987) with relatively detailed introduction about the Manning coefficient, and corresponds with the amplification in this reach. The large value for the North Passage ($n = 1/K = 0.03$) may be due to its high water depth and long convergence length, resulting from dredging and bank fixation for shipping, which leads to more damping in this channel.

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4.3 Validation

The measurements on 18–19, 24–25 February 2003 at 19 stations along the Yangtze Estuary and the observations on 1–2, 8–9 March 2002 at 18 stations excluding the North Branch, have been used to validate the model and our approach, using the parameters in Table 1. The calculated results fit the data well (Figs. 4 and 5). For the North Branch, the same deviation in the tidal travel time is obtained at Qinglonggang station (75 km) as in 2006 during spring tide particularly for high water (Figs. 4d and 3d). This may be due to the large difference in water depth between HW and LW at spring tide in this relatively shallow part of the estuary. The abnormal long travel time at Santiaogang (17 km) during neap tide in 2003 (Fig. 4e) is probably due to a data problem.

For the South Branches and Upper Reach, some computed tidal amplitudes for the upper reach particularly upstream from the location 250 km are not correct, considerably higher than observations during neap tide in 2003 and 2002 (Figs. 4c and 5b). Also a relatively bad fit of the tidal travel time occurs in this reach. These are likely due to the influence of the river discharge in this reach, or the changed topography which influences the roughness coefficient. For the South Passage, although there is only one tidal station, the computed results relate to the Nancadong station (−4.7 km) very well (Figs. 3b and 4b). For the lower reach of the North Channel, there is only one station available as well and there is no station near the mouth. However, there are three stations at sea: Sheshan, Niupijiao, and Dajishan which are at similar positions outside the mouths of the North Channel, the North Passage, and the South Passage, respectively (Fig. 1). Comparing these three stations, the tidal amplitude at Dajishan is usually slightly larger than at Niupijiao with a very small difference, whereas both are generally larger than at Sheshan (Fig. 6). These differences correspond with the differences between the three estuary mouths as presented in Figs. 3b, 4b, and 5a.

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5 Discussion

5.1 Tidal damping and amplification

Seeing from Figs. 3a–c and 4a–c, in the Yangtze Estuary there are two clear differences between the North Branch and the South Branches. One is tidal damping or amplification. In the North Branch, the tidal wave is first amplified and then damped, while it is essentially damped along the South Branches, which agree with the common perception (Shen et al., 1988, 2003; Yang et al., 2001; Liu et al., 2006). However, among the South Branches there are some differences as well. In the South Passage, the tidal damping is less strong in the second half of the reach than in the first half. In the North Passage the damping is the strongest. In the South Channel and the North Channel, slight amplification occurs before the inflection point and after the inflection point, respectively.

The other difference between the North Branch and the South Branches is that the tidal amplitude in the North Branch is larger than in the South Branches (Figs. 3a,b and 4a,b). Among the South Branches, the tidal amplitude is the highest near the mouth of the South Passage and the lowest near the mouth of the North Channel. One reason for this is the amplification in the North Branch and the damping in the South Branches. The other reason may be the largely different freshwater discharge into the channels, which also causes a difference in the salinity distribution between these channels (Zhang et al., 2011). Further upstream, between the South Channel and the North Channel, the tidal amplitudes in the two channels is equal at the intersection point, the location of Wusong in the South Channel and Baozhen in the North Channel. Before the intersection point the tidal amplitude is larger in the South Channel, and after which it is the reverse, which result from their tidal damping and amplification, respectively (Figs. 1, 3b, 4b, and 5a).

The tidal damping or amplification is the result of the imbalance between the topographic convergence and friction. If convergence is stronger than friction the wave is amplified, if friction is stronger than convergence the wave is damped (Langbein, 1963;

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Dyer, 1973; Jay, 1991; Savenije, 1998, 2005). The amplification in the North Branch agrees with strong convergence. The amplification before the inflection point in the South Channel results from the funneling effect at the junction of the North Passage and the South Passage, where the tidal energy from two channels is combined. This effect was demonstrated as well in the Fly River estuary in Papua New Guinea (King and Wolanski, 1996). Because there is no observation available in this reach, further work is required to confirm this effect. At the junction of the North Channel and the South Channel, this effect is not clear, which may be due to the parallel channels. If we continue the computation for the South Branch using separate topography of the North Channel and the South Channel after their junction, the computed results fit the measurements well before a point about 90 km from the mouth, particularly when the fit is nice at the intersection point of the North Channel and the South Channel (Fig. 7). The Nanmengang station (81 km) is located at the north bank of the South Branch following the North Channel, and the Yanglin station (89 km) is situated at the south bank following the South Channel (Figs. 1 and 7). Probably the parallel channels of the North Channel and the South Channel and the similar width after their junction until 90 km (Fig. 1), permit the tidal dynamics of the two channels to function separately, which results in the relatively high tidal amplitude at the north bank and lower value at the south bank in this reach following the amplification in the North Channel and the damping in the South Channel.

5.2 Tidal propagation

The tidal wave celerity also depends on the imbalance between convergence and friction, with a close relation to tidal damping or amplification (Savenije, 2005). For the North Branch, the tidal wave travels much faster in the lower reach than the upper reach, corresponding with amplification and damping, respectively. Particularly in the lower reach near the mouth, the tidal travel time is almost zero indicating an apparently standing wave. This is in accordance with the tidal amplification and strong convergence, which can lead to a near standing wave in short estuaries (Savenije, 2005).

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For the South Branches near the mouth, the tidal wave travels faster in the North Passage, which agrees with its small storage width ratio r_s and higher water depth resulting from bank fixation and dredging of the deep-water shipping channel. Furthermore, the higher celerity in the upper reach of the North Channel than in the South Channel is due to the large Manning-Strickler friction factor K and small storage width ratio r_s in the North Channel, corresponding with its slight amplification. At the two junctions, junction 1 and junction 2, the tidal wave in the North Passage and the North Channel seems to “wait” for the wave in the South Passage and the South Channel, respectively, taking time to fill the storage before the joint wave proceeds.

5.3 Phase lag, estuary shape, and friction

The phase lag ε is a crucial parameter in tidal hydraulics, which can be used to classify the type of tidal wave, and the estuary shape number γ is the main indicator for estuary shape. Figure 8 presents the diagram for the phase lag ε in different channels, as a function of the estuary shape number γ and friction number χ , from which the characteristics of channels can be identified. The lower reach of the North Branch has the largest estuary shape number and a very small phase lag, indicating its marine character with strong convergence. The upper reaches of the South Channel and the North Channel, the South Branch and Upper Reach, all have a very small estuary shape number γ and high phase lag, which suggest their riverine character with long convergence length. The South Passage, the North Passage, the lower reaches of the South Channel and North Channel, and the upper reach of the North Branch all lie in between with a moderate estuary shape number and phase lag, which imply that they receive moderate influence both from the sea and river. Of these, the South Passage, the North Passage, the lower reach of the South Channel, and the upper part of the North Branch are all situated around the transition point $\gamma = 1.5$ where the lines for different values of χ cross, the phase lag is insensitive to friction. For $\gamma < 1.5$ the phase lag decreases with friction, while for $\gamma > 1.5$ it increases with friction. The lower reach of the North Branch apart from the first reach 0–5 km, belongs to the latter situation,

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whereas other channels belong to the former situation. In the first reach of the North Branch 0–5 km, the estuary shape number is very large around 5 and $\varepsilon = 0$ which suggests the apparently standing wave without dependence on friction. In other channels and reaches, $0 < \varepsilon < \frac{\pi}{2}$ indicates a mixed tidal wave (Savenije, 2005). In the reach upstream from 5 km in the North Branch with an estuary shape number larger than 2, which is critical convergence, the very small ε indicates an approximately standing wave.

Additionally, most reaches of the channels in the Yangtze Estuary lie close to the line of an ideal estuary (the line with dots) where friction and convergence cancel out, with not much damping or amplification. Here, we can also distinguish the amplified channels below the line of the ideal estuary for high γ (or marine channels) such as the lower reach of the North Branch, and above the line for small γ (or riverine channels) such as the upper reach of the North Channel. It is the reverse for the damped channels.

5.4 “Entity” behavior of the branched estuary

Based on the assumption that the branched estuary system functions as an entity, the computations for the South Channel and the South Branch can be carried out by means of a combined approach (approach 2). Computations begin from the mouth using the combined topographies. The input of tidal amplitude at the mouth η_0 is the weighted average of the corresponding separate channels, whose cross-sectional areas at the mouth are taken as the weight. For the South Channel, topography of the Combined South Channel is used, and the tidal amplitude at the mouth η_0 is the weighted average of the North Passage and the South Passage. For the South Branch, topography of the Combined South Branch is used, and the tidal amplitude at the mouth η_0 is the weighted average of the Combined South Channel and the North Channel, or the weighted average of the South Passage, the North Passage, and the North Channel.

The computed tidal amplitude and travel time for two junctions by means of the two approaches are presented in Table 2. The approach introduced in Sect. 4.1 is called

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approach 1. For junction 1 between the North Passage and the South Passage, the computed values using approach 2 are all very close to approach 1. For junction 2 between the North Channel and the South Channel, the computed tidal amplitudes using the two approaches are almost the same as well. However, the computed tidal travel time using approach 2 is larger than approach 1 by 23 min at low water and 12 min at high water on average, which is probably due to the error of determination of the combined topography. These underline the assumption that the branched estuary system functions as an entity for the tidal dynamics, similar to what was concluded for salt intrusion by Nguyen and Savenije (2006), Nguyen et al. (2008), and Zhang et al. (2011).

The Manning-Strickler friction factor K and storage width ratio r_s are key calibration parameters of the model. It can be seen from Table 1 that the values K and r_s of the combined channels are basically the weighted average of the corresponding separate channels, using the cross-sectional areas as the weights. For example, 0–33 km of the Combined South Channel corresponds with the North Passage and the South Passage, and 34–64 km of the Combined South Branch corresponds with 40–70 km of the South Channel and 18–53 km of the North Channel. This behavior also suggests that the branched estuary system functions as an entity.

5.5 Uncertainty and limitation of the model

In this study, the model performs well for the Yangtze Estuary, which indicates that this simple analytical model for single-channel alluvial estuary can describe the tidal dynamics in a branched estuary as well. However, there are several uncertainties and limitations of parameters of the model.

Firstly, the Manning-Strickler friction factor K and storage width ratio r_s are usually obtained by calibration. Because they are related to many factors, there is uncertainty in determination of them, particularly the friction factor K . Additionally, there is a limit to the accuracy that can be obtained for the depth near the estuary mouth. Therefore,

although the values we obtain accord with the values in previous research, they require more measurements and more accurate topography to be improved.

Secondly, there are uncertainties about the tidal average cross-sectional depth \bar{h} . On the one hand, there is uncertainty in the determination of the average depth over the cross-section, particularly when there is a shallow part or deep part. Longitudinally if there is a long reach with a curve fitted depth much lower or higher than the measurements, it is better to modify the depth in the model using the measurements. In this study, we modify the depths between 130 and 250 km where the curve fitted values are much higher than the data (Fig. 2f), then as a result, the model results are better. For the combined channels used in approach 2, the uncertainty may be larger because the lengths of the corresponding separate channels are different, which probably causes the larger tidal travel time at junction 2. On the other hand, the \bar{h} in Savenije's model is the average depth at mean sea level, whereas in this study it is the tidal average depth for different tidal ranges (the tidal average depth varies with the tidal amplitude). In this analysis we take account of this difference. We find that the results are much better if we use the actual tidal average depth for different tidal ranges, particularly when the tidal range is very high or low. This procedure requires further confirmation based on more observations and more accurate bathymetry.

Thirdly, one assumption of the model is the partially to well mixing characteristic of the estuary. The North Branch of the Yangtze Estuary is a marine well-mixed channel. The South Branches are the more riverine partially-mixed channels in which well-mixed situations also occur during the dry season (Zhang et al., 2011). During the flood season the influence from river discharge undoubtedly is larger, which likely induces higher computed values than the actual ones. Because we have no data during the flood season, further work is required, and it is better if river discharge can be included in the model.

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In this study, an analytical model for tidal dynamics has been applied for the first time to the Yangtze Estuary, a large and branched estuary. The results indicate that this simple model originally derived for single-channel alluvial estuary can very well describe the tidal dynamics in the branched estuary as well, particularly for the lower part. The satisfactory computed results for the South Channel and the South Branch using both the individual topographies and the combined topographies, and the obtained Manning-Strickler friction factor K and storage width ratio r_s for the combined channels which are basically the weighted average of the corresponding separate channels, confirm that a branched estuary system functions as an entity. However, the model requires more measurements and more accurate bathymetry to improve and confirm the parameters used.

Acknowledgements. This study was supported by the National Natural Science Foundation of China (Grant No. 40701182). Authors acknowledge the Bureau of Hydrological and Water Resources Survey of the Yangtze Estuary, Shanghai Hydrological Administration, and Marine Safety Administration of Shanghai for kindly providing the tidal measurements data.

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**Table 1.** Calibrated parameters K and r_s of the Yangtze Estuary.

Parameter	North branch		North channel		North passage	South passage	Combined south channel		0–34 km	Combined south branch and upper reach			
	0–5 km	5–85 km	0–18 km	18–53 km			0–40 km	40–70 km		34–90 km	90–130 km	130–250 km	250–626 km
K	50	50	55	90	33	50	45	50	50	71	60	55	30
r_s	Spring tide	3	1	2	1	1.1	2.1	1.72	1	1.85	1	1	1
	Neap tide	3	1	2	1	1.1	2.1	1.72	1.7	1.9	1.45	1.1	1

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Table 2. Difference of the computed tidal amplitude and travel time at two junctions between two approaches.

Date	Junction 1 (north passage and south passage)						Junction 2 (north channel and south channel)					
	A-1	A-2	tLW-1	tHW-1	tLW-2	tHW-2	A-1	A-2	tLW-1	tHW-1	tLW-2	tHW-2
21–22 Dec 2006	1.58	1.59	119.62	71.87	119.15	71.41	1.45	1.44	171.34	108.34	191.14	117.97
21–22 Dec 2006	1.22	1.22	109.40	73.64	109.12	73.33	1.05	1.06	174.14	118.80	198.53	131.54
29–30 Dec 2006	1.09	1.08	102.02	72.69	102.05	72.62	0.94	0.94	166.43	119.03	192.29	133.27
29–30 Dec 2006	0.93	0.93	94.29	71.44	94.66	71.62	0.81	0.82	158.84	119.33	183.54	133.97
18–19 Feb 2003	1.92	1.92	126.91	69.82	126.62	69.28	1.72	1.72	179.68	105.11	200.77	114.27
18–19 Feb 2003	1.62	1.63	120.45	71.65	119.99	71.18	1.47	1.47	172.16	108.00	192.19	117.60
24–25 Feb 2003	1.02	1.02	98.60	72.13	98.80	72.21	0.90	0.89	163.73	119.07	189.21	133.69
24–25 Feb 2003	0.88	0.88	92.11	70.94	92.40	71.25	0.76	0.77	156.25	119.46	180.40	134.37

Note: A – tidal amplitude, tLW – tidal travel time at low water, tHW – tidal travel time at high water; 1 indicating approach 1, 2 indicating approach 2.

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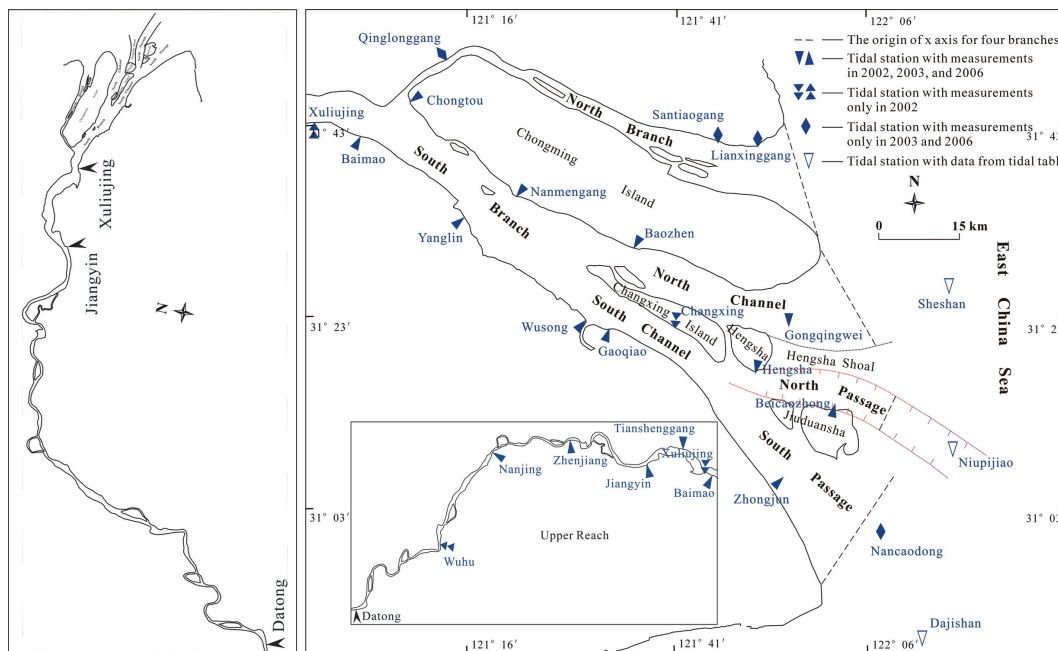


Fig. 1. The Yangtze Estuary.

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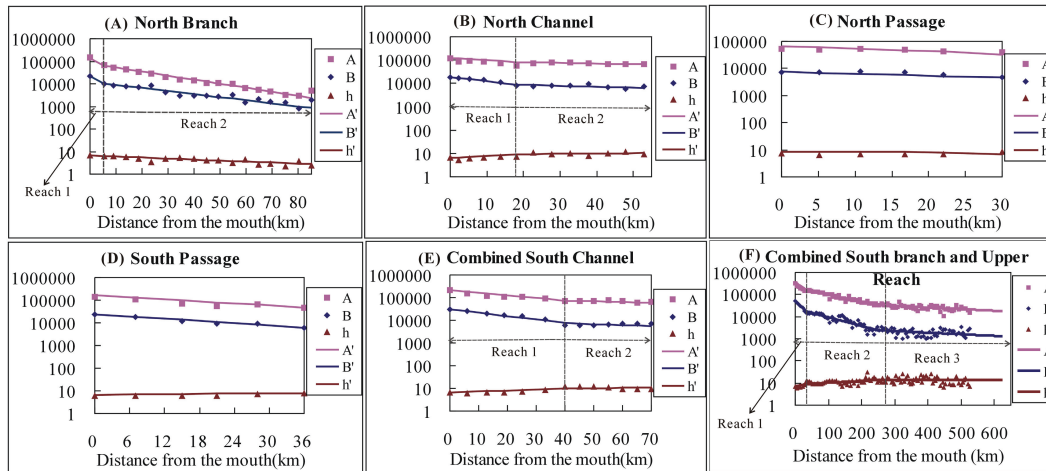


Fig. 2. Geometry of the Yangtze Estuary (Reach 1, 2, 3 represent the reaches of multi-reach channels, 1, 2, 3 are the reach number i in Eqs. 1–3).

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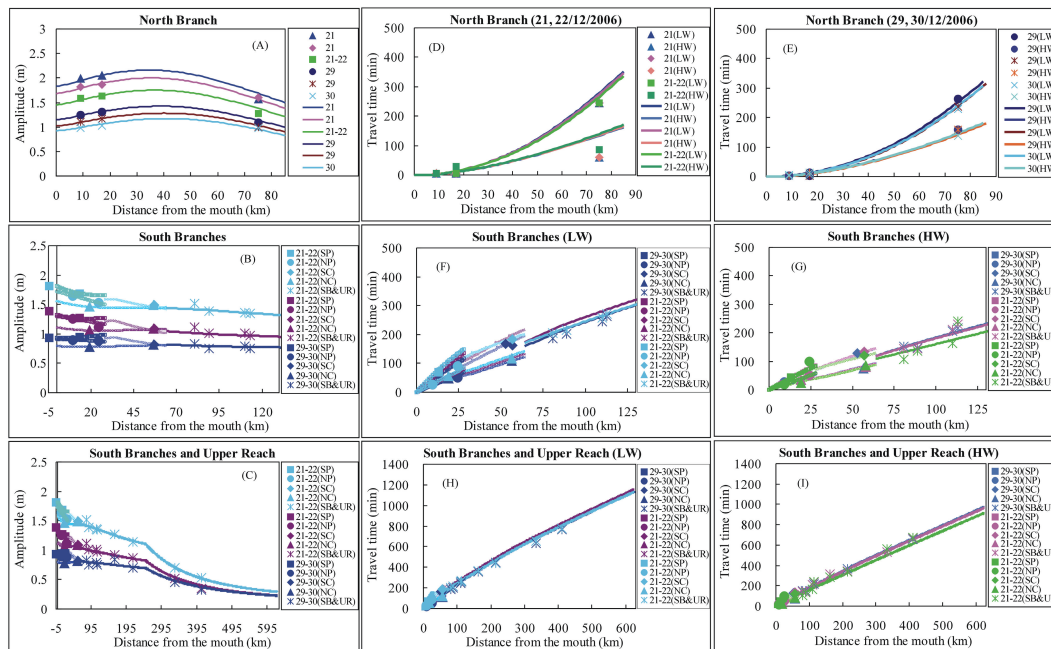


Fig. 3. Computed results (drawn lines) for the tidal amplitude (A–C) and travel time (D–I) along the Yangtze Estuary on 21–22, 29–30 December 2006, compared to measurements (symbols).

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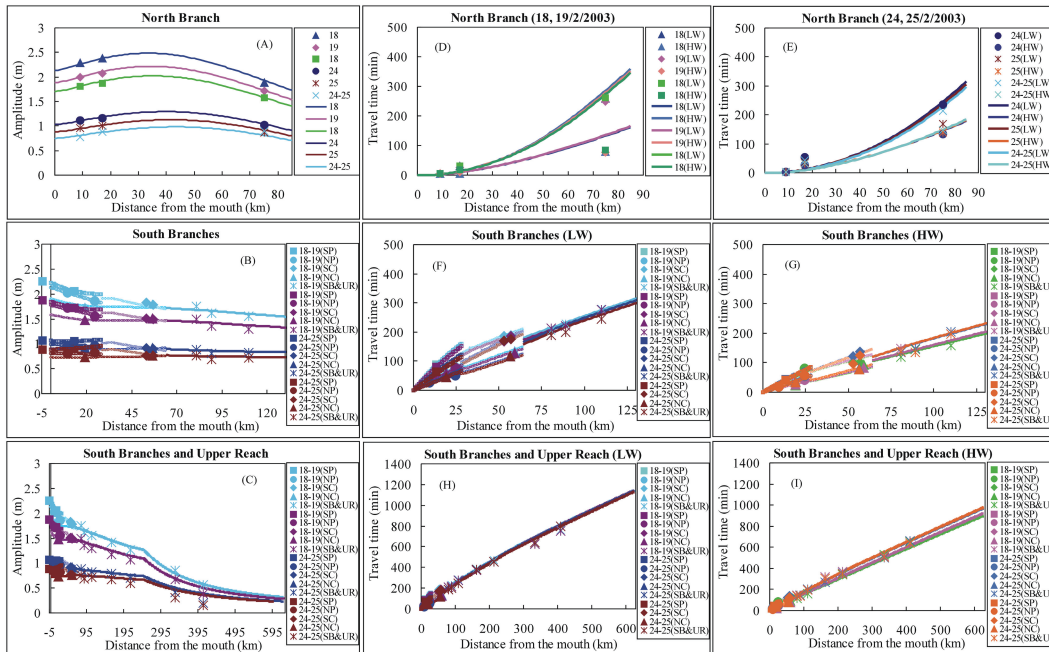


Fig. 4. Computed results (drawn lines) for the tidal amplitude (**A–C**) and travel time (**D–I**) along the Yangtze Estuary on 18–19, 24–25 February 2003, compared to observations (symbols).

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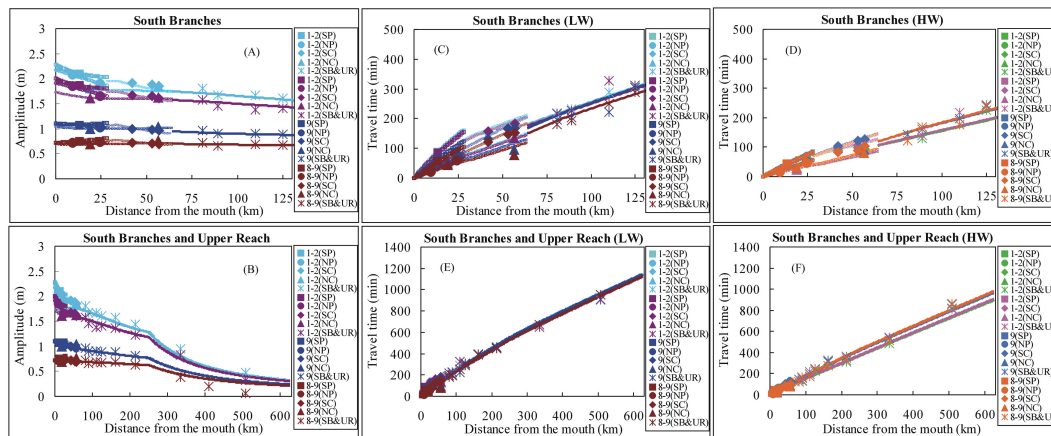


Fig. 5. Computed results (drawn lines) for the tidal amplitude (A,B) and travel time (C–F) only along the South Branches and Upper Reach on 1–2, 8–9 March 2002, compared to observations (symbols).

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Fig. 6. Tidal amplitudes from tidal table at Sheshan, Niupijiao, and Dajishan stations (outside the estuary).

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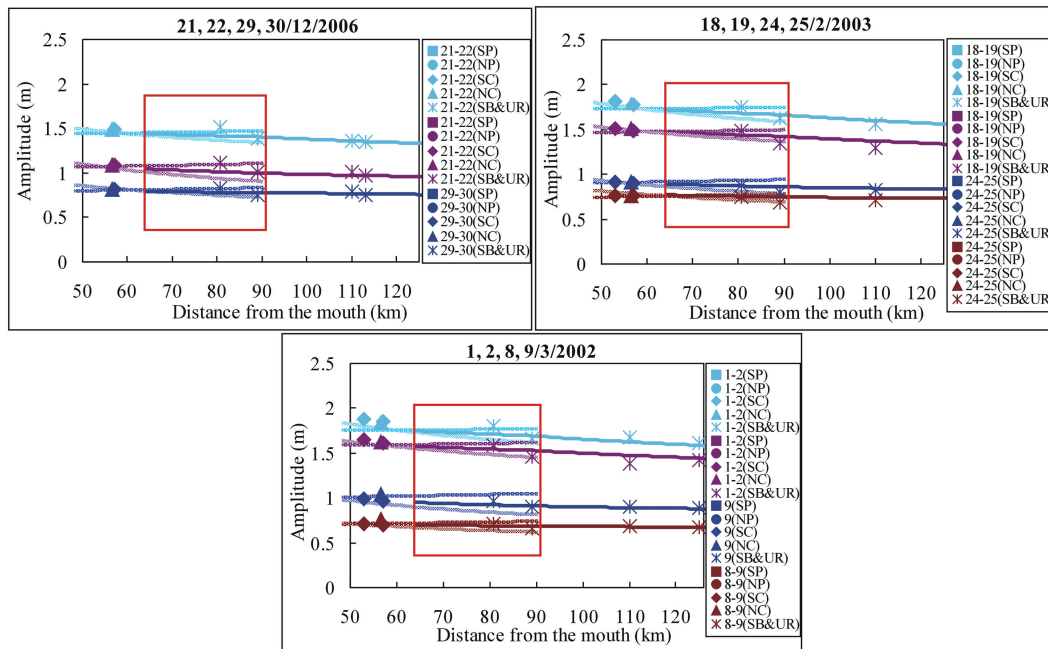


Fig. 7. Computed tidal amplitude for the South Branch after the junction of the North Channel and the South Channel (64 km) until 90 km (inside the rectangle frame), using separate topography of these two channels.

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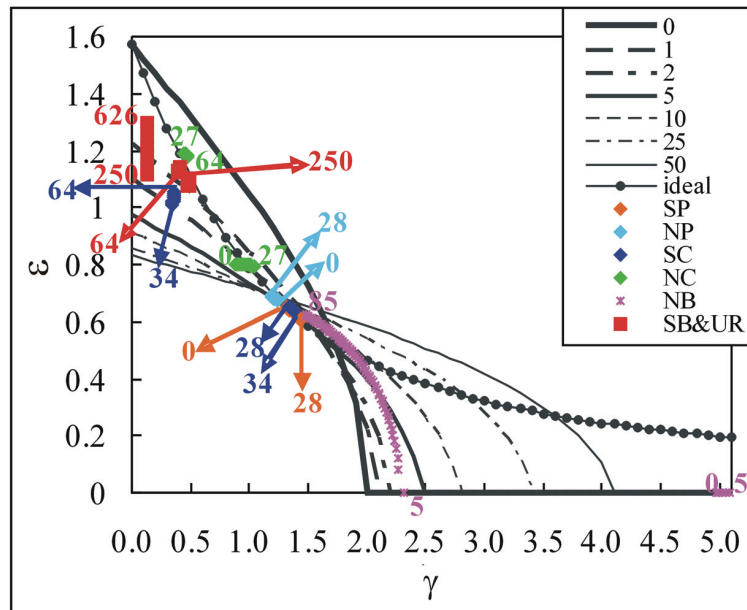


Fig. 8. Positioning of the Yangtze Estuary (NB-North Branch) in the phase lag diagram, the numbers at inflection points indicating the distance from the estuary mouth (in kilometers), the same as Figs. 3–5. The background shows lines with different values of the friction number χ . The drawn line with dots represents the ideal estuary.

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