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Assessing the impact of uncertainty on flood risk estimates with reliability analysis using 1-D and 2-D hydraulic models

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Abstract

This paper addresses the use of reliability techniques such as Rosenblueth's Point-Estimate Method (PEM) as a practical alternative to more precise Monte Carlo approaches to get estimates of the mean and variance of uncertain flood parameters

- ⁵ water depth and velocity. These parameters define the flood severity, which is a concept used for decision-making in the context of flood risk assessment. The method proposed is particularly useful when the degree of complexity of the hydraulic models makes Monte Carlo inapplicable in terms of computing time, but when a measure of the variability of these parameters is still needed. The capacity of PEM, which is a special
- ¹⁰ case of numerical quadrature based on orthogonal polynomials, to evaluate the first two moments of performance functions such as the water depth and velocity is demonstrated in the case of a single river reach using a 1-D HEC-RAS model. It is shown that in some cases, using a simple variable transformation, statistical distributions of both water depth and velocity approximate the lognormal. As this distribution is fully defined
- ¹⁵ by its mean and variance, PEM can be used to define the full probability distribution function of these flood parameters and so allowing for probability estimations of flood severity. Then, an application of the method to the same river reach using a 2-D Shallow Water Equations (SWE) model is performed. Flood maps of mean and standard deviation of water depth and velocity are obtained, and uncertainty in the extension of
 ²⁰ flooded areas with different severity levels is assessed. It is recognized, though, that
- whenever application of Monte Carlo method is practically feasible, it is a preferred approach.

1 Introduction

Flooding poses a risk to people and causes significant economic costs. In the last century floods accounted for 12% of all deaths from natural disasters (DEFRA, 2009). The number of floods registered during the period 1990–1998 was more than those in



the period 1950–1985, and the associated economic losses were seven times higher. During the period 2000 to 2006 water-related disasters killed more than 290 000 people, affecting more than 1.5 billion, and inflicting more than US\$ 422 billion of damage (UNWWAP, 2009). Though the operation of flood defence systems contribute to reduce risks, these cannot be completely eliminated and non-structural measures such as flood forecasting, warning, planning and others become even more significant on reducing flood risk. For this reason, there is a requirement for methods to estimate flood

risk (societal and economical risk) and the effect of structural and non-structural measures on risk reduction (Escuder-Bueno et al., 2011). Flood risk can be defined as the
 combination of the probability of a flood event, called hazard, with the potential adverse consequences for human health, the environment, cultural heritage and economic activity associated with a flood event (European Parliament, Directive 2007/60/EC), called vulnerability. Risk is commonly expressed by the notation

Risk = Hazards × Vulnerability

5

25

Its units are the ones used for measuring the vulnerability divided per time, for instance a monetary unit or a number of victims per year, because the hazard probability has units of time⁻¹. Flood risks can be analyzed by calculating the probability of an event occurring and the subsequent impact that it has on a receptor.

Hazard in risk models can be expressed as

20 Hazard = Load Probability × System Response

The Load corresponds to the hydrological input, usually identified by a flow discharge. The Load Probability has units of time⁻¹. The System Response, when uncertainties are incorporated into the models, is a conditional probability and has no units. The System Response is usually expressed in terms of velocity, v, water depth, y, and extension of the flooded area, A_f . These parameters are outputs of the flood model and can be considered as performance functions of the system. Vulnerability in terms of loss of lives includes the computation of population at risk and fatality rates. The fatality



(1)

(2)

rates can be calculated as a function of flood severity and warning time. Vulnerability in terms of economic losses is obtained by identifying homogeneous areas, value of assets, defining reference costs, estimating percentages of damage based on water depth in each area and flood scenario, etc.

Therefore, risk can be defined mathematically as

5

Risk = Load Probability × System Response × Vulnerability

The state of the art of this kind of analysis is a collection of raster maps of flood extent for several annual exceedance probabilities, including information on water depth and velocity. This maps are combined with a structure inventory of the flooded area that comprises structure type (residential, commercial, industrial, etc.), structure location and value, occupancy type and associated depth-percent damage functions, among other categories, that help to define the Vulnerability (USACE, 2008; Escuder-Bueno et al., 2011). Parameters commonly used to measure the severity of a flood are water depth, velocity, together with the dragging parameter, $v \cdot y$, and the sliding parameter, $v^2 \cdot y$. Due to the uncertainties that exist at several levels of the process these parameters are performance functions of basic random variables, being random variables themselves.

As it has been mentioned, the hydrological input, defined in terms of a flood hydrograph, affects the Load Probability term of the equation of Risk. Flood hydrographs are influenced by many random factors, such as rainfall pattern and amount, watershed geomorphology, ground infiltration rate, vegetation of the watershed and temperature, etc. Uncertainty on flood hydrographs has been addressed by several authors (Sarino and Serrano, 1990; Yue et al., 2002). The second term of the Risk equation is the System Response. This response is controlled by the quality of topography informa-

tion, friction coefficient and type of model used: 1-D, 2-D. Uncertainty can be taken into account by setting the model in a probabilistic framework, i.e. combining the model and a probabilistic description of the input parameters. The uncertainties are represented by random variables, therefore the response is also a random variable obtained by



(3)

the propagation of the random input through the model. Uncertainty in topography for numerical flood modelling can be reduced thanks to remote sensing techniques such as laser altimetry (Cobby et al., 2001) which allow obtaining floodplain digital elevation models, DEMs, with a high degree of accuracy. The specification of flow resistance

- is also subjected to uncertainty, with different existing laws and methods (Wohl, 1998) and a wide spectrum of values to be selected. Factors influencing the friction coefficient include bed material, bed forms both at micro- and meso-scale, and the presence of vegetation in the channel and in the floodplains (Horrit, 2006). The spatial and temporal variability of these parameters adds difficulty in the assessment of the friction coefficient (Mason et al., 2003). This is the main source of uncertainty considered in
- this paper.

Regarding analysis models, 1-D models, despite their limitations, are commonly used in engineering practice as they are simple and allow fast calculations of flood parameters. These models cannot accurately represent flood plain flows so 2-D mod-

els where the velocity vector has two components have been developed and are now common tools in flood modelling. 2-D models are solved by numerical methods and their computation even for single set of parameters can be time demanding, depending on the extent of the area and the calculation mesh density, i.e. number of points where inundation parameters are going to be calculated per unit area. (Bladé et al., 1994;
 USACE, 2002).

A common approach to solve problems where parameter uncertainty is present is the Monte Carlo Method (Aronica et al., 1998; Romanowicz and Beven, 1998). Variability of the performance functions that describe the system response is captured doing multiple realisations of the model using different sets of values of the basic random variables. These sets of values are generated according to the probability distributions of the random variables and their possible correlations (Rubinstein, 1981). The method allows considering random variables with different probability distributions and non linear performance functions. In order to get a sound approximation of the performance functions in terms of the form of their probability distributions and accuracy in



the estimation of the parameters that define the distributions it is necessary to perform a large number of simulations, assuring a dense mapping of the probability functions of the basic random variables. This is the major drawback of the method, as when there is a large number of random variables and/or the model is complex, computing time

- ⁵ can be so high that the method becomes simply inapplicable for practical purposes. To avoid this problem it is possible to use simplified models that are much less demanding in terms of computing time. An example of this is the 1-D well known HEC-RAS model, that can be used in a probabilistic framework due to its relatively short calculation time (Pappenberger et al., 2005). Another approach if 2-D models have to be used
- is the search of an approximation of the 2-D model which can be evaluated for fast explorations of its probabilistic behaviour by techniques such as spectral approximations (Liu et al., 2010). This latter approach is still in the research field and hardly used by engineers in everyday practice.
- The objective pursued in this paper is to demonstrate how practical estimates of the variability of uncertain flood parameters can be obtained with a reasonable balance between accuracy and effort. This paper addresses the use of reliability techniques such as Rosenblueth's Point-Estimate Method, PEM, as a practical alternative to more precise Monte Carlo approaches to get estimates of the mean and variance of flood parameters such as water depth and velocity. These parameters define the flood severity,
- which is a concept used for decision-making in the context of flood risk assessment. The method proposed is particularly useful when the degree of complexity of the hydraulic models makes Monte Carlo inapplicable in terms of computing time, but when still an approximate measure of the variability of these parameters can be of help for decision making.
- ²⁵ In Sect. 2 the fundamentals of the point-estimate method are shown. In Sect. 3 a case study is presented and three models of analysis are described. The first is a simple uniform flow model used to explore the transfer of variability between input random variables such as the friction coefficient and performance functions like water depth and velocity. The second model is a 1-D HEC-RAS model of the whole river



reach. The third model is a Shallow Water Equations, SWE, 2-D model, implemented in the commercial code GUAD-2D (Inclam-University of Zaragoza, 2008). In Sect. 4 point-estimate method and Monte Carlo techniques are used in combination with 1-D models to estimate the statistical properties of the performance functions and results
 ⁵ are compared. In Sect. 5 point-estimate method is used in combination with the 2-D SWE model to get estimates of flood severity in terms of mean and standard values of water depth, velocity and dragging coefficient. Section 6 gives some conclusion

2 Estimation of uncertainty

remarks.

10 2.1 Sources of uncertainty and existing methods

In engineering problems physical and probabilistic models are used as mathematical idealizations of reality. Formulation of reliability, risk and decision problems involves a set of input random variables, *X*, parameterized sub-models describing their statistical distributions and physical sub-models that describe the relationships between the random variables and the derived quantities, *Y*. In this context, the sources of uncertainty include (Der Kiureghian and Ditlevsen, 2007): inherent uncertainty in the random variables *X*; uncertain model error resulting from the selection of the form of the probabilistic sub-model; uncertainty in the estimation of the parameters of the physical sub-model; statistical uncertainty in the estimation of the parameters of the physical sub-model; uncertain errors involved in measuring of observations; and uncertainty derived from computational error parameters of an exterior derived from computational error provided error resulting of observations; and uncertainty derived from computational errors involved in measuring of observations; and uncertainty derived from computational errors involved in measuring of observations; and uncertainty derived from computational errors involved in measuring of observations; and uncertainty derived from computational errors involved in measuring of observations; and uncertainty derived from the error errors involved in measuring of observations; and uncertainty derived from computational errors involved in measuring of observations; and uncertainty derived from computational errors involved in measuring errors involved in the error error errors involved in the eror erro

- certainty derived from computational errors, numerical approximations or truncations, when computation procedures employs iterative calculations that involve convergence tolerances and truncation errors.
- To deal with at least part of the aforementioned sources of uncertainty several methods can be used (Shresta and Solomatine, 2008), including analytical methods,



approximation methods, simulation and sampling methods, Bayesian methods such as the generalized likelihood uncertainty estimation method or GLUE (Beven and Binley, 1992), statistical methods based on the analysis of model errors (Kelly and Krzysztofowicz, 1997) and methods based on fuzzy set theory (Pappenberger et al., 2007).

⁵ The approximation methods provide only the moments of the distribution of the derived parameters. Due to their simplicity and low computational demand these methods are suited for practical applications in hydrology and water resources by engineers not familiar with more complex techniques. The point-estimate method belongs to this group.

10 2.2 The point-estimate method

In this section the fundamentals of Rosenblueth's point-estimate method for approximating low-order moments of functions of random variables is presented (Rosenblueth, 1981). The mathematical problem is that of a random variable or variables, X, with probability distribution function defined by the probability density function (PDF), $f_X(x)$,

- and another variable, *Y*, which is a deterministic performance function of *X*, *Y* = g(X). The random variables are, in this paper, the three bed friction coefficients defined by Manning's roughness, n_i (i = 1, 2, 3), for the main channel and both overbanks. The performance function *Y* is the water depth and also the velocity, taking into account that these two variables are fully correlated. It is assumed that *Y* has a PDF defined by $f_Y(y)$. The problem that point-estimate faces is how to approximate the low-order
 - moments of $f_{Y}(y)$ using only the low-order moments of $f_{X}(x)$ and the function g(X).

The point-estimate method determines the first two moments of the performance function g(X) replacing the continuous random variables X by discrete random variables whose probability mass function, PMF, $p_X(x)$, has the same moments of order

 $_{25}$ *k* as does $f_X(x)$. The PMF $\rho_X(x)$ is transformed using g(X) to obtain another discrete function with a PMF denoted $\rho_Y(y)$. This latter PMF is used to calculate the moments which are assumed to approximate the moments of *Y* in the continuous case.



The first moment of $f_{\chi}(x)$ about the origin is the mean, μ_{χ}

$$\mu_X = \int x \cdot f_X(x) \cdot dx$$

The higher-order central moments of $f_{\chi}(x)$ of order k are

$$\mu_{Xk} = \int (x - \mu_X)^k \cdot f_X(x) \cdot dx \tag{5}$$

⁵ The second central moment, μ_{χ_2} , is the variance, and its square root is the standard deviation, σ_{χ} . The corresponding moments of order *k* the discrete PMF $p_{\chi}(x)$ are

$$\mu_{Xk} = \sum (x - \mu_X)^k \cdot \rho_X(x)$$

Equating the moments of $f_X(x)$ and $p_X(x)$ yields

$$\int (x - \mu_X)^k \cdot f_X(x) \cdot dx = \sum (x - \mu_X)^k \cdot \rho_X(x)$$

¹⁰ An approximation to integration is done using numerical quadrature procedures. The selection of the optimal values of the coordinates at which evaluate the integrand and the corresponding weights is treated with Gaussian quadrature procedures. So it can be seen from Eq. (7) that Rosenblueth's method is an application of Gaussian quadrature procedures (Christian and Baecher, 1999). This discretization is made in a few points for each random variable (two or three points), where mass probability is concentrated in such a fashion that the sum of the probabilities assigned to each point is 1 for each random variable (Harr, 1987). The two-point method concentrates the mass probability of the random variable X_i in two points, x_{i+} and x_{i-} , each of them with a mass probability of P_{i+} and P_{i-} . Points are centred about the mean value, μ_{Xi} , at a ²⁰ distance of d_{i+} and d_{i-} times the standard deviation σ_{Xi} , respectively.

 $P_{i+} + P_{i-} = 1$

 $x_{i+} = \mu_{X_i} + d_{i+} \cdot \sigma_{X_i}$

(4)

(6)

(7)

(8)

(9)

$$x_{i-} = \mu_{X_i} - d_{i-} \cdot \sigma_{X_i}$$

Coefficients d_{i+} and d_{i-} are determined using the skew coefficient, γ_i , of the random variable X_i :

$$d_{i+} = \frac{\gamma_i}{2} + \sqrt{1 + \left(\frac{\gamma_i}{2}\right)^2} \tag{11}$$

$$d_{i-} = d_{i+} - \gamma_i$$
 (12)

Probabilities are assigned to each point according to

$$P_{i+} = \frac{d_{i-}}{d_{i+} + d_{i-}} \tag{13}$$

$$P_{i-} = 1 - P_{i+} \tag{14}$$

10

A number of 2^m values of discrete probabilities should be obtained by combination of the point probabilities of each of the *m* random variable with the other random variable's probabilities. These probabilities are $P_{(\delta_1, \delta_2, ..., \delta_m)}$, where δ_i is the sign (+/-). Their values are calculated as

$$P_{(\delta_1,\delta_2,\ldots,\delta_m)} = \prod_{i=1}^m P_{i,\delta i} + \sum_{i=1}^{m-1} \left(\sum_{j=i+1}^m \delta_j \delta_j a_{ij} \right)$$

where the coefficients a_{ii} are calculated as

15
$$a_{ij} = \frac{\frac{\rho_{ij}}{2^m}}{\sqrt{\prod_{i=1}^n \left(1 + \left(\frac{\gamma_i}{2}\right)^2\right)}}$$

Being ρ_{ij} the correlation coefficient between random variables X_i and X_j .

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(10)

(15)

(16)

The performance function g(X) has to be evaluated 2^m times, corresponding to the 2^m possible combinations of discrete probability points $P_{(\delta_1, \delta_2, ..., \delta_m)}$, obtaining $Y_{(\delta_1, \delta_2, ..., \delta_m)} = g_{*(\delta_1, \delta_2, ..., \delta_m)}$. Once this is accomplished, the expected value of the *k*th power of the probability distribution of *Y* is determined by:

$${}_{5} E\left[Y^{k}\right] \approx \sum P_{\left(\delta_{1},\delta_{2},\ldots,\delta_{m}\right)}Y^{k}_{\left(\delta_{1},\delta_{2},\ldots,\delta_{m}\right)}$$

$$(17)$$

So for k = 1 what we have is the first moment about the origin, which is the mean, μ_Y

$$E[Y] \approx \sum P_{(\delta_1, \delta_2, \dots, \delta_m)} Y_{(\delta_1, \delta_2, \dots, \delta_m)}$$
(18)

And for k = 2 the second moment about the origin is obtained

$$E\left[Y^{2}\right] \approx \sum P_{\left(\delta_{1},\delta_{2},\ldots,\delta_{m}\right)}Y_{\left(\delta_{1},\delta_{2},\ldots,\delta_{m}\right)}^{2}$$

$$\tag{19}$$

The variance of Y can be calculated from the first two moments about the origin as:

$$\sigma_{Y}^{2} = \mu_{Y2} = E\left[(Y - \mu_{Y})^{2}\right] = E\left[Y^{2}\right] - \mu_{Y}^{2}$$
(20)

So it is possible to determine the mean and the variance of the random variable Y, but the shape of the distribution remains unknown.

The method allows to handle random variables X with different symmetrical distributions. The method loses precision as nonlinearity of g(X) increases and if moments over the second are to be obtained (Harr, 1987). It does not provide a measure of the contribution of each random variable to the overall variance, so it is not an adequate method to filter the most relevant random variables. A disadvantage of the method is that the performance function has to be evaluated 2^m times, being *m* the number of random variables. If *m* is large, the method requires a considerable computational effort, above all if g(X) evaluation is not straightforward, as it is the case with 2-D SWE models.



The method performs reasonably well when g(X) can be approximated by a thirdorder or less polynomial and when the coefficient of variation of X, COV, defined as the ratio between standard deviation and mean value, is not large (Christian and Baecher, 1999).

5 3 Case study

25

In this section the river reach and the different hydraulic models used for the study are described.

3.1 Model of the Turia river reach

The modelled stream is a reach of the Turia river, located several kilometers upstream of the city of Valencia, in the eastern part of Spain. The domain modelled has a length of 1 km and an average slope of $2.3 \,\mathrm{m \, km^{-1}}$. The DEM of the terrain has a mesh size of $1 \times 1 \,\mathrm{m}$ (Fig. 1).

The bed friction coefficient used is the Manning's *n*. Three zones are defined with different bed friction values: the main channel, n_{ch} , the left overbank, n_{lob} , and the right overbank n_{ch} (see Fig. 1). The nucleus over each of the three domains are subjected

- overbank, n_{rob} (see Fig. 1). The *n* values over each of the three domains are subjected to uncertainty and therefore are defined as random variables in the model. The variables are assumed to be uncorrelated in this paper, although it is recognized that in fact some correlation may exist between the bed friction values in the defined areas. Nevertheless the methodology exposed in this paper can be applied without difficulty
- ²⁰ to correlated random variables. No spatial variability is considered inside the three defined zones, which corresponds well with the low degree of spatial heterogeneity observed in the reach analyzed.

Different probability distributions have been used by different authors to statistically characterise the friction coefficient, such as the normal (Cesare, 1991; Mays and Tung, 1992; Horrit, 2006), triangular (Yeh and Tung, 1993), lognormal (USACE, 1986; Liu,



2010) and uniform distributions (Johnson, 1996; Pappenberger et al., 2005). In this paper the uniform distribution is selected to examine how point-estimate method performs when distributions have such a high variability. To check the impact of the type of probability distribution of the bed friction on water depth and velocity estimates, also

- ⁵ triangular symmetrical and normal distributions have been tested with the 1-D uniform flow model. In the case of the triangular symmetrical distribution the minimum and maximum values are the same as those of the uniform distribution. In the case of the normal distribution a different truncation has been adopted so the variable is confined exactly between the range $[\mu_n - 2\sigma_n, \mu_n + 2\sigma_n]$, with μ_n and σ_n the mean and standard deviation of *n*. The probability distributions adopted for *n* are summarized in Table 1.
- The study has been undertaken with three different imposed flows at the upstream end of 200, 300 and 500 m³ s⁻¹.

3.2 Numerical flood models

In this section the three hydraulic models used in the study are described.

15 3.2.1 Uniform flow model

The first model used is a uniform flow model that is applied to a simplified geometry (Fig. 2) of the river station RS 768 of the 1-D HEC-RAS model that is described in Sect. 3.2.2. The model assumes an infinite reach length with constant geometry in terms of cross section and slope. The slope of this ideal reach is 2.1 m km⁻¹. This model has been prepared to explore the transfer of variability from bed friction coefficient to water depth and velocity functions under ideal conditions, without non-linear perturbations of flow due to changes in geometry. The implicit equation to be solved is the well-known uniform flow formula

$$Q \cdot S^{-0.5} = \sum_{i} n_i^{-1} A_i(y) [R_i(y)]^{0.67}$$



(21)

where *Q* is the flow $(m^3 s^{-1})$, *S* is the slope of the channel $(m m^{-1})$, n_i is the random roughness coefficient in the *i*th-zone in which the section is divided, A_i is the flow area of the *i*-zone (m^2) , R_i is the hydraulic radius (m) of the *i*th-zone and *y* is the water depth (m). In this case three zones have been defined (i = 3): main channel and the left and right overbanks. The simplification of the geometry allows using algebraic expressions for $A_i(y)$ and $R_i(y)$. The model is implemented in a spreadsheet.

3.2.2 1-D HEC-RAS model

5

A 1-D HEC-RAS gradually varied flow model of the reach has been prepared. This model is defined by 12 cross sections located along the reach and numbered according to their position in terms of distance in meters to the downstream end (0; 219; 353; 454; 558; 591; 640; 694; 737; 768; 773 and 987). Position of the bank stations that define the main channel and the overbanks is consistent with the extent of the zones defined in Fig. 2. At the downstream boundary a normal depth condition is imposed assuming a friction slope of 1.9 m km⁻¹ according to the average river slope further downstream. In this model the geometry varies between cross sections. The real cross section at RS 768 compared to the simplified section and the ground profile of the model can be seen in Fig. 2.

3.2.3 2-D Shallow Water Equations model

A 2-D Shallow Water Equations (SWE) flow model has been used to evaluate the system response in terms of water depth and velocities in the domain under analysis. The model solves the well-known 2-D finite volume shallow water equations

$$\frac{\partial h}{\partial t} + \frac{\partial (hu)}{\partial x} + \frac{\partial (hv)}{\partial y} = 0$$

(22)



$$\frac{\partial(hu)}{\partial t} + \frac{\partial(hu^2)}{\partial x} + \frac{\partial(huv)}{\partial y} = -gh\frac{\partial(h+z)}{\partial x} + \frac{n^2u\left(u^2 + v^2\right)^{0.5}}{h^{4/3}} + hv_{\rm T}\nabla^2 u \tag{23}$$

$$\frac{\partial(hv)}{\partial t} + \frac{\partial(huv)}{\partial x} + \frac{\partial(hv^2)}{\partial y} = -gh\frac{\partial(h+z)}{\partial y} + \frac{n^2v\left(u^2 + v^2\right)^{0.5}}{h^{4/3}} + hv_{\rm T}\nabla^2 v \tag{24}$$

where *h* is the flow depth, *u* and *v* the components of the depth averaged flow velocity vector, *z* the bed elevation, *g* the acceleration due to gravity, *n* the Manning's coefficient of roughness and v_T the turbulent viscosity. The upstream boundary condition is an imposed inflow and the downstream boundary condition is a stage-discharge relation. This model is implemented in the commercial code GUAD 2D (Inclam and University of Zaragoza, 2008).

The continuous fields h, u and v are discretized over a mesh of elements that in this case are squares, but that can have other shapes such as triangles. The governing equations are integrated over each element. The finite volume method combines the main advantages of finite element methods, such as its great geometrical flexibility, with the main advantages of finite difference methods, such as its flexibility in the definition of discrete flow variables.

The finite volume method has some disadvantages in the representation of high order derivatives, so they should be used when the viscosity terms can be ignored. The problem is solved over time in GUAD 2D using the Roe approximation based on the local linearization of each Riemann problem between adjacent cells. The time step should be selected small enough to assure stability.

20 4 Application of the method

In this section the point-estimate method is used to calculate flood parameters. Results obtained using PEM in combination with uniform flow and 1-D HEC-RAS models are compared with those obtained using the Monte Carlo approach.



4.1 Uniform flow model – Monte Carlo solutions

The first model used has been the uniform flow model described in previous section. The number of random variables is three which correspond to Manning's *n* values in main channel and both overbanks. Three flow values are considered, 200, 300 and $500 \text{ m}^3 \text{ s}^{-1}$. Three different probability distributions have been used for n_i according to Table 1, uniform, triangular and normal. The problem has been solved initially with Monte Carlo simulation with 1000 model runs. From these simulations the mean and standard deviation of water depth and velocity at the section have been estimated, and an adaptation of several probability distributions has been attempted, using the statistical tool @RISK (Palisade, 2005).

The results for water depth are shown in Tables 2 to 4. In a first step the probability distributions to be fitted have been filtered so only those with lower and upper bounds have been considered, as distributions of n_i are bounded as well. The distributions that best fit the data according to the χ^2 test are the 4-parameter beta distribution (Beta General) and the 3-parameter triangular distribution. In a second step and for comparison purposes the normal distribution has been selected for fitting. The comparison of the 4-parameter beta distributions that best fit water depth for case flow $500 \text{ m}^3 \text{ s}^{-1}$ when n_i has different probability distributions is shown in Fig. 3. Graphical comparison of probability density functions suggest that better fitting is obtained when

- n_i are triangular or normal distributed. The best approximation according to χ^2 test is obtained when n_i have triangular distributions. From Fig. 3 it can be seen that the probability distribution of the water depth is not symmetrical, showing some negative skewness. This indicates that symmetrical distributions such as the normal are not a good choice when attempting to describe water depth in a probabilistic way.
- ²⁵ A similar analysis has been performed for velocity of flow. The procedure followed has been the same as for water depth. The bounded distributions that best fit the data according to the χ^2 test are the 4-parameter beta distribution (Beta General) and the triangular distribution. Again, the normal distribution has been selected for comparison



purposes. The results for velocity are shown in Tables 5 to 7. The high values of the χ^2 statistic indicates poor fitting in all cases. The comparison of the 4-parameter beta distributions that best fit velocities for flow case 500 m³ s⁻¹ when n_i has different probability distributions is shown in Fig. 3. The graphic comparison confirms the bad fitting seen in the χ^2 goodness of fit test. It can be seen that the probability distribution 5 of the velocity is strongly asymmetrical, showing positive skewness. The values of the χ^2 statistic for a significance levels of $\alpha = 0.05$ and $\alpha = 0.01$ are shown in Table 8. It can be seen that none of the distributions adapted to water depth and velocity pass the test for a the selected significance levels, thus showing poor fitting, even for this simple hydraulic model.

Given that bed friction coefficients n_i are defined as random variables with bounded distributions, the water depth y derived from the model is another random variable with a bounded distribution, with range $[y_{MIN}, y_{MAX}]$. These limiting values can be calculated straightforwardly from the model. A transformation of the water depth random variable. v, into another random variable, w, is proposed according to

 $W = Y_{MAX} - Y$

10

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Now w is a bounded random variable, with positive skewness and confined in the range $[0, y_{MAX} - y_{MIN}]$. The 1000 realisations of y obtained with Monte Carlo have been transformed according to Eq. (25) and new adaptations have been performed. Candidate probability distributions have been filtered relaxing the upper bound restriction to let upper unbounded distributions such as the lognormal to be fitted. The results obtained show an improvement in the fitting, particularly when n_i friction values are normally distributed. In Fig. 4 a comparison of lognormal distributions fitted to calculated values is shown. The lognormal distributions fitted do not pass the χ^2 goodness of fit test.

mainly due to the inaccuracy in the adaptation of the upper tail. This was somehow 25 expected as the lognormal is an upper unbounded distribution while w is a bounded random variable. Still, it is interesting to see from the graphs in Fig. 4 that the lognormal distribution fits reasonably well for low w values, which correspond to high y values. An advantage of the lognormal distribution is that it is completely defined by only two



(25)

parameters, its mean and standard deviation. The importance of these feature will be addressed later.

The convergence of results of mean and standard deviation values for water depth and velocity obtained with Monte Carlo simulation is shown in Fig. 5 for the case of n_i uniformly distributed and case flow 500 m³ s⁻¹. Similar results have been obtained for the rest of the cases of n_i distributions and flow values, so they have not been included here.

4.2 Uniform flow model – point-estimate method approximation

To apply the point-estimate method the first step has been to identify the 2^m points where the performance function has to be evaluated, being *m* the number of random variables, which is three in this case. The different probability distributions of the bed friction coefficient considered are symmetrical and roughness values in the three zones defined are assumed to be uncorrelated, although correlation can be easily included as shown in Sect. 2. Applying Eqs. (9) to (12) it can be seen that the two points per variable are located one standard deviation above or below the mean. In this case m = 3 and we 15 had $2^3 = 8$ points where the performance function had to be evaluated (n_{1+}, n_{2+}, n_{3+}) , $(n_{1+}, n_{2+}, n_{3-}), (n_{1+}, n_{2-}, n_{3+}), (n_{1+}, n_{2-}, n_{3-}), (n_{1-}, n_{2+}, n_{3+}), (n_{1-}, n_{2+}, n_{3-}), (n_{1-}, n$ n_{2-} , n_{3+}), (n_{1-}, n_{2-}, n_{3-}) . According to Eqs. (13) and (14) the probability or weight of each point is $P_i = 0.125$. In Table 9 the corresponding values of n_{i+} and n_{i-} for each zone and distribution are summarized. The mean and variance of the water depth y20 and velocity v have been calculated with Eqs. (17) to (20), solving the model at the 8 points defined.

The comparison of the results obtained with the three probability distributions of the bed friction coefficient considered is shown in Fig. 6. Each dot on the chart correspond to a different flow case. It can be observed that point-estimate gives almost exact estimates of the mean water depth values and provides a good approximation of velocities. The standard deviations show some scatter but still a reasonably good



estimation is obtained. In summary, point-estimate provides a good approach for mean and standard deviation values of water depth and velocity with a very limited calculation effort.

4.3 1-D HEC-RAS model

- A similar procedure has been followed using the 1-D HEC RAS model of the river reach. A difference from the previous case is that in this case only uniform probability distributions for bed friction coefficients have been considered. The hydraulic model comprises the whole river reach, allowing for changes in section and slope, and so adding non linear effects to the problem with respect to the uniform flow model. Values
- of water depth and velocity are obtained at the 12 river stations defined in the model. The Monte Carlo analysis has been limited to 100 simulations, which are sufficient to get a good estimation of the mean and standard deviation values of water depth and velocity, as can be seen by the convergence curves shown in Fig. 7 for cross section at river station RS 768 and flow case 500 m³ s⁻¹. In this case the estimated mean
- water depth is y = 4.37 m, and the 95% confidence interval that corresponds to 100 simulations is [4.33; 4.41]. The length of the interval is 0.08 m, which is considered enough accuracy for the purpose of this paper. As a reference, interval lengths of 0.20 and 0.02 m would be expected for 10 and 1000 simulations, respectively. Similar results have been obtained for the other cross sections and flow cases so they are not shown here.

The point-estimate method needed only 8 calculations of the hydraulic model for each flow case. The comparison of results obtained with Monte Carlo and point-estimate method is shown in Figs. 8 to 10 for the three flow cases considered. Each dot on the chart corresponds to a different river cross section. It can be seen that the mean depth is well approximated by point-estimate for almost all cross sections. For flow cases of 300 and 500 m³ s⁻¹ the mean depth is slightly underestimated by point-estimate method. For example, at RS 768 the point-estimate method gives a mean water depth *y* = 4.34 m. This fact shows the appearance of non linear effects



and the influence of the whole reach in the flow characteristics of different sections of the model. The standard deviation of the water depth is reasonably well estimated, showing some scatter for different flow rates and different cross sections. For example, at RS 768 the standard deviation of water depth estimated with Monte Carlo has a

- ⁵ value of 0.1954 m while point-estimate gives a value of 0.1986 m. The mean velocity is slightly overestimated by point-estimate method though values fit reasonably well with those obtained with Monte Carlo. The standard deviation for velocity shows good performance. A comparison of mean and standard deviation of flow profiles for flow case $500 \text{ m}^3 \text{ s}^{-1}$ is shown in Fig. 11.
- Flood uncertainty can be depicted by raster maps of mean and standard deviation 10 of water level values. In Fig. 12 flood inundation maps of the analysed river reach with mean water depths for the three flow cases are shown. In Fig. 13 the raster map of standard deviation of water levels is shown, where the 1-D mathematical structure of the model is highlighted by the alignment of the standard deviation bands parallel to the

cross section definition in HEC-RAS model. The pattern reproduced is that of Fig. 11. 15

5 Application to 2-D model

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In this section the application of the point-estimate method in combination with a 2-D shallow water equations model is presented. Only uniform probability distributions have been considered for the roughness values of channel and overbanks, in a similar fashion as with 1-D HEC-RAS model.

The 2-D hydraulic model had to been run 8 times, according to the 8 combinations of the three random variables point values adopted, for each of the 3 flow cases, so initially 24 runs were needed. To optimize the process a hydrograph with three steps with constant flow rates of 200, 300 and 500 m³ s⁻¹ has been prepared, reducing the number of model runs from 24 to 8. The duration of each constant flow step has been set

25 to allow the model to reach a steady state flow in the whole domain. Results are then retrieved and the calculations proceed to the next flow value. The time of calculation



with the 2-D model implemented in the commercial code GUAD-2D is considerably longer that with 1-D models. Each run of the HEC-RAS model takes less than 1 s while each run of the GUAD-2D model has had an average time duration of 5 h, which makes flood uncertainty analysis with Monte Carlo unfeasible from a practical point of view in engineering. Still, an approximate uncertainty analysis can be performed with the help

- of the point-estimate method. The first step has been to perform the calculations with the 2-D hydraulic model at
- the 8 points where the performance functions have to be evaluated. In this case the performance functions are the water depth and the total velocity at every 1×1 m cell of the model. In this case the total velocity value has been selected though the analysis can be done separately for its components (v_X , v_Y). Series of raster maps with the results of water depths and velocities evaluated for the 8 combinations of roughness coefficients are stored in a GIS framework. The mathematical operations defined in Eqs. (18) to (20) have been performed within the GIS using the generated layers with
- GUAD 2D. The first two moments about the origin of the performance functions are calculated at every point of the grid, and from those the expected value and the standard deviation are derived. The flood map with expected values of water depth for the three flow cases is shown in Fig. 14. The standard deviations of water depth can be seen in Fig. 15, where the 2-D mathematical structure of the model becomes clear when compared with equivalent map obtained with HEC-RAS model. The map of mean and
- standard deviation of velocities of flow is shown in Figs. 16 and 17, respectively.

Results from 2-D models can be used to assess the extension of flooded areas with different severity levels. The flood severity levels are defined in terms of flood depth, velocity and dragging coefficient, which is defined as the product of the water depth

times the velocity. An example of a chart for flood severity levels is shown in Fig. 18 (Gracia et al., 2010). In this case 5 severity levels are defined as low (1), moderate (2), high (3), very high (4) and extremely high (5), according to Table 10. Flood severity levels are used to estimate fatalities and/or economic losses.



For each flow case, every point of the flooded area has been evaluated in terms of water depth, velocity and dragging coefficient for the 8 runs of the 2-D model. With the help of GIS tools, the corresponding severity level has been derived for each 1 m² cell using the criteria defined in Fig. 18. The total area for every flood severity level was ⁵ computed, obtaining 8 different values for each level. Following the procedure of the point-estimate method the mean and standard deviation of the extension of the flooded area for each severity level has been calculated.

The estimated mean values for each severity level and for the three flow cases are shown in Fig. 19. It can be seen that as flow rate increases the extension of flooded areas with higher severity levels is incremented. The estimated mean values and stan-

- dard deviations of the extension of the flooded areas for each severity level is shown in Fig. 20 (flow case $200 \text{ m}^3 \text{ s}^{-1}$), Fig. 21 (flow case $300 \text{ m}^3 \text{ s}^{-1}$) and Fig. 22 (flow case $500 \text{ m}^3 \text{ s}^{-1}$). It is interesting to see how the range of variation of extension of flooded areas varies for each severity level, bringing a measure of the uncertainty that can be easily transferred to consequence estimation in a risk analysis context. In the case
- flow 200 m³ s⁻¹ it can be seen that higher uncertainty derived from roughness coefficient is present for severity levels low (1) and high (3). For flow case $300 \text{ m}^3 \text{ s}^{-1}$ low, uniform uncertainty is spread over all severity levels. On the other hand, for flow case $500 \text{ m}^3 \text{ s}^{-1}$ a wider band of uncertainty is linked to severity levels high (3) and very high (4).

A normalized measure of the amount of uncertainty of a random parameter is the coefficient of variation, COV, which is defined as the ratio between the standard deviation, σ , and the mean, μ . Values of COV for each severity level for the three flow cases analyzed are depicted in Fig. 23. In engineering practice a small uncertainty would be represented by a COV = 0.05 while considerable uncertainty would be indicated by a COV = 0.25 (Hoek, 2007). It can be seen that the majority of COV values obtained in the case study lie in the range [0.05; 0.25], which means an intermediate situation where significant yet not too high uncertainty is present due to the variability assumed for the roughness coefficient.



The results in Figs. 20 to 22 show how the uncertainty in bed friction coefficient is transferred to flooded areas with different severity levels. This information is useful in the risk analysis context as flood damage is measured according to the corresponding areas on each severity level. This means that at least some of the uncertainty from the hydraulic model can be added to the estimates of flood damage in the context of risk analysis.

From the point of view of the engineer that has to build a model, information regarding the location of zones with higher variability can be useful to make decisions, such as where to direct the efforts for efficient model improvement.

10 6 Conclusions

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In the context of assessing the uncertainty in flood modelling in a river reach, the results presented have shown the practical applicability of the point-estimate method to perform uncertainty flood analysis, considering the Manning's *n* roughness coefficient as the main source of uncertainty. Reasonable estimates of mean and standard deviation values of flood parameters such as water depth and velocity have been obtained with much less effort than with Monte Carlo method using 1-D HEC RAS and a 2-D SWE model implemented in the commercial code GUAD 2D. It has been shown that with a simple variable transformation the water depth parameter can be roughly approximated by a lognormal distribution. Better fitting is observed in the lower tail of the

transformed variable which corresponds to the upper tail of the water depth distribution. As the lognormal distribution is fully defined by its mean and variance, a probabilistic characterization can be achieved using PEM.

Flood maps with expected values of water depth and velocity and their associated standard deviations have been obtained implementing the point-estimate calculations ²⁵ within a GIS framework, and flooded areas with different associated severity levels have been calculated in terms of the expected values and standard deviations of their extension. As the evaluation of consequences of a flood in terms of fatalities and/or



economic losses is achieved using rates linked to the extension of each severity level, uncertainty in the system response is transferred to the consequence evaluation.

The main limitations of point-estimate method are the loss of accuracy if the performance function cannot be approximated by third order polynomials and the fast growing

- of the number of calculations needed if the number of random variables *m* increases, rendering the method impracticable for computing time-demanding problems, such as 2-D models. Application to 2-D models, though in need of more research, is promising according to the results obtained.
- Though the method presented has some evident advantages such as its sim-¹⁰ plicity and limited effort needed to perform uncertainty analysis of floods with nonprobabilistically-oriented 2-D commercial codes, the results obtained should be taken carefully looked at. They should not be deemed as exact values and it should be kept in mind that this method is a practical alternative to more exact methods. It is acknowledged that more research is needed in order to set the limits of the applicability of ¹⁵ the method and its accuracy in the 2-D models environment, above all when strong non-linearities are present in the model.

The method presented is not always the best choice, but it may be considered by engineers as a useful tool for screening analysis before restoring to more powerful but more costly methods in terms of time and money in the risk analysis context. It is recognized, though, that whenever Monte Carlo application is practically feasible, it is a preferred approach. The underlying approach that has been presented is in line with a quote by Box (Box and Draper, 1987), in the sense that all models are wrong, and

that the practical question is how wrong do they have to be to not be useful.

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		Mean	SD	COV	Min.	Max.
PDF		μ	σ	$=\sigma/\mu$	Value	Value
Uniform	n _{lob}	0.065	0.020	0.308	0.030	0.100
	n _{ch}	0.045	0.014	0.311	0.020	0.070
	n _{rob}	0.085	0.032	0.376	0.030	0.140
Triangular	n _{lob}	0.065	0.014	0.215	0.030	0.100
	n _{ch}	0.045	0.010	0.222	0.020	0.070
	n _{rob}	0.085	0.022	0.259	0.030	0.140
Normal	n _{lob}	0.065	0.020	0.308	0.025	0.105
	n _{ch}	0.045	0.014	0.311	0.017	0.073
	n _{rob}	0.085	0.032	0.376	0.021	0.149



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Table 2. Uniform flow model. Adaptation of PDFs to water depth with uniform distributions for n_i (1000 simulations).

Flow (m ³ s ⁻¹)	Mean µ (m)	SD σ (m)	COV =σ/μ	Min. Value (m)	Max. Value (m)	PDF	χ ²
200	3.23	0.3855	0.12	2.35	3.78	Beta Gen. Triang. Normal	104.9 153.3 359.2
300	3.67	0.3856	0.11	2.83	4.28	Beta Gen. Triang. Normal	95.79 174.6 287
500	4.27	0.4071	0.10	3.39	5.03	Beta Gen. Triang. Normal	103.9 179 184.1

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	Flow (m ³ s ⁻¹)	Mean μ (m)	SD σ (m)	$COV = \sigma/\mu$	Min. Value (m)	Max. Value (m)	PDF	χ^2	sion Pa	
	200	3.25	0.2592	0.08	2.35	3.78	Beta Gen.	120.2	per	

4.28

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	Flow (m ³ c ⁻¹)	Mean	SD	COV	Min.	Max.	PDF	χ^2	ion P
	200	μ (III) 2 2 2		$=0/\mu$	value (III)	value (111)	Bota Con	97 70	ape

Flow (m ³ s ⁻¹)	Mean μ (m)	SD σ (m)	COV =σ/μ	Min. Value (m)	Max. Value (m)	PDF	χ²
200	3.22	0.3296	0.10	2.17	3.83	Beta Gen. Triang. Normal	87.79 117.5 136.8
300	3.68	0.3292	0.09	2.63	4.34	Beta Gen. Triang. Normal	71.26 71.43 146.5
500	4.30	0.3398	0.08	3.21	5.11	Beta Gen. Triang. Normal	108.8 140.5 131.1



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Table	5.	Uniform	flow	model.	Adaptatior	۱ of	PDFs	to	velocity	with	uniform	distributions	s for	n
(1000	sim	nulations).											

Flow (m ³ s ⁻¹)	Mean µ (m)	SD σ (m)	COV =σ/μ	Min. Value (m)	Max. Value (m)	PDF	χ ²
200	1.72	0.5494	0.32	1.01	3.08	Beta Gen. Triang. Normal	115.6 106.8 486.9
300	1.78	0.6580	0.37	0.97	3.36	Beta Gen. Triang. Normal	157.8 170.9 585
500	1.81	0.6442	0.36	1.04	3.68	Beta Gen. Triang. Normal	217.1 190.2 721.8



Table 6. Uniform flow model.	Adaptation of PDFs to velocity with triangular distributions for n_i
(1000 simulations).	

Flow (m ³ s ⁻¹)	Mean µ (m)	SD σ (m)	$COV = \sigma/\mu$	Min. Value (m)	Max. Value (m)	PDF	χ²
200	1.67	0.3625	0.22	1.01	3.08	Beta Gen. Triang. Normal	65.4 183.7 160.9
300	1.67	0.2033	0.12	0.97	3.36	Beta Gen. Triang. Normal	93.07 146.5 270.6
500	1.64	0.3959	0.24	1.04	3.68	Beta Gen. Triang. Normal	147.6 536.5 351.2



Table 7. Uniform flow model. Adaptation of PDFs to water depth with normal distributions for n_i (1000 simulations).

Flow (m ³ s ⁻¹)	Mean µ (m)	SD σ (m)	COV =σ/μ	Min. Value (m)	Max. Value (m)	PDF	χ ²
200	1.72	0.4730	0.27	0.96	3.47	Beta Triang. Normal	76.83 156.1 182
300	1.74	0.5670	0.33	0.93	3.83	Beta Triang. Normal	120.5 194.6 367.8
500	1.71	0.5412	0.32	1.00	4.29	Beta Triang. Normal	221.4 633 563.7



Table 8. Uniform flow model	. Values of χ^2	statistic.
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Significance level (α)	PDF fitted	Number of parameters (<i>m</i>)	Number of bins used in the test (<i>b</i>)	Degrees of freedom (<i>b</i> -1- <i>m</i>)	χ²
0.05	Beta general	4	29	24	36.42
	Triangular	3	29	25	37.65
	Normal	2	29	26	38.89
0.01	Beta general	4	29	24	42.98
	Triangular	3	29	25	44.31
	Normal	2	29	26	45.64



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Table 9. Points estimate method. Values of bed friction used to evaluate the performance function.

PDF of n_i Zone of n_i		x_{i-} point: μ - σ	x_{i+} point: $\mu + \sigma$
Uniform Left overbank		0.045	0.085
	Channel	0.031	0.059
	Right overbank	0.053	0.117
Triangular	Left overbank	0.051	0.079
	Channel	0.035	0.055
	Right overbank	0.063	0.107
Normal	Left overbank	0.045	0.085
	Channel	0.031	0.059
	Right overbank	0.053	0.117

Table 10.	Flood severity levels.	
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Severity level	Range of water depth, y (m)	Range of velocity, $v (m s^{-1})$	Range of dragging coefficient, $y \cdot v$ (m ² s ⁻¹)
Low (1) Moderate (2) High (3) Very high (4) Extremely high (5)	$y \le 0.4 0.4 < y \le 1 1 < y \le 2 2 < y \le 4 4 < y$	$v \le 0.4 0.4 < v \le 1 1 < v \le 3.5 3.5 < v \le 6 6 < v$	$y \cdot v \le 0.08$ $0.08 < y \cdot v \le 0.5$ $0.5 < y \cdot v \le 1$ $1 < y \cdot v \le 2$ $2 < y \cdot v$





Fig. 1. Digital Elevation Model of the study river reach (left) and zones considered for different bed friction values (right).





Fig. 2. 1-D model. Geometry of the cross section at RS 768 of the HEC RAS model, with the simplified cross section for the uniform flow model showed with dashed line (top) and river reach ground profile for 1-D HEC-RAS model (bottom).





Fig. 3. Uniform flow model. Case flow $500 \text{ m}^3 \text{ s}^{-1}$. Adaptation of 4-parameter beta PDF to water depth (top) and velocity values (bottom) obtained with Monte Carlo (1000 simulations), and for different distributions of n_i : uniform (left), triangular (middle) and normal (right).





Fig. 4. Uniform flow model. Adaptation of lognormal PDF to transformed water depth variable $(w = y_{MAX} - y)$ for n_i uniformly distributed (top) and normally distributed (bottom), and for flow cases 200 m³ s⁻¹ (left side), 300 m³ s⁻¹ (middle) and 500 m³ s⁻¹ (right side).





Fig. 5. Uniform flow model. Convergence of mean and standard deviation values for water depth and velocity. Case of n_i uniformly distributed and flow case 500 m³ s⁻¹.





Fig. 6. Uniform flow model. Mean and standard deviations of water depth and velocity predicted by point-estimate method against Monte Carlo. Results for n_i distributions: uniform (squares), normal (circles) and triangular (triangles). Each point on the chart corresponds to a flow case.





Fig. 7. 1-D HEC-RAS model. Convergence of mean and standard deviation values for water depth and velocity at RS 768. Case of n_i uniformly distributed with flow case 500 m³ s⁻¹.







Fig. 8. 1-D HEC-RAS model. Mean and standard deviations of water depth and velocity predicted by point-estimate method against Monte Carlo. Results for n_i uniformly distributed and flow case 200 m³ s⁻¹. Each dot corresponds to a different RS of the model.





Fig. 9. 1-D HEC-RAS model. Mean and standard deviations of water depth and velocity predicted by point-estimate method against Monte Carlo. Results for n_i uniformly distributed and flow case 300 m³ s⁻¹. Each dot corresponds to a different RS of the model.





Fig. 10. 1-D HEC-RAS model. Mean and standard deviations of water depth and velocity predicted by point-estimate method against Monte Carlo. Results for n_i uniformly distributed and flow case 500 m³ s⁻¹. Each dot corresponds to a different RS of the model.







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Fig. 12. 1-D HEC-RAS model. Flood maps with mean values of water depth predicted by point-estimate method for flow cases of $200 \text{ m}^3 \text{ s}^{-1}$ (left), $300 \text{ m}^3 \text{ s}^{-1}$ (middle) and $500 \text{ m}^3 \text{ s}^{-1}$ (right).





Fig. 13. 1-D HEC-RAS model. Flood maps with standard deviation values of water depth predicted by point-estimate method for flow cases of $200 \text{ m}^3 \text{ s}^{-1}$ (left), $300 \text{ m}^3 \text{ s}^{-1}$ (middle) and $500 \text{ m}^3 \text{ s}^{-1}$ (right).





Fig. 14. 2-D SWE model. Flood maps with mean values of water depth predicted by pointestimate method for flow cases of $200 \text{ m}^3 \text{ s}^{-1}$ (left), $300 \text{ m}^3 \text{ s}^{-1}$ (middle) and $500 \text{ m}^3 \text{ s}^{-1}$ (right).





Fig. 15. 2-D SWE model. Flood maps with standard deviation values of water depth predicted by point-estimate method for flow cases of $200 \text{ m}^3 \text{ s}^{-1}$ (left), $300 \text{ m}^3 \text{ s}^{-1}$ (middle) and $500 \text{ m}^3 \text{ s}^{-1}$ (right).





Fig. 16. 2-D SWE model. Flood maps with mean values of velocity predicted by point-estimate method for flow cases of $200 \text{ m}^3 \text{ s}^{-1}$ (left), $300 \text{ m}^3 \text{ s}^{-1}$ (middle) and $500 \text{ m}^3 \text{ s}^{-1}$ (right).





Fig. 17. 2-D SWE model. Flood maps with standard deviation values of velocities predicted by point-estimate method for flow cases of $200 \text{ m}^3 \text{ s}^{-1}$ (left), $300 \text{ m}^3 \text{ s}^{-1}$ (middle) and $500 \text{ m}^3 \text{ s}^{-1}$ (right).





Fig. 18. Flood severity levels (adapted from Gracia et al., 2010).





Fig. 19. 2-D SWE model. Expected values of the extension of areas with different severity levels for flow cases 200, 300 and $500 \text{ m}^3 \text{ s}^{-1}$.





Fig. 20. 2-D SWE model. Expected values and standard deviations of the extension of areas with different severity levels for flow case $200 \text{ m}^3 \text{ s}^{-1}$.





Fig. 21. 2-D SWE model. Expected values and standard deviations of the extension of areas with different severity levels for flow case $300 \text{ m}^3 \text{ s}^{-1}$.





Fig. 22. 2-D SWE model. Expected values and standard deviations of the extension of areas with different severity levels for flow case $500 \text{ m}^3 \text{ s}^{-1}$.





Fig. 23. 2-D SWE model. Coefficient of variation (COV) of the extension of the area foir each severity level.

