

## ***Interactive comment on “Extended power-law scaling of air permeabilities measured on a block of tuff” by M. Siena et al.***

### **Anonymous Referee #1**

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#### General comments

This paper represents a substantial contribution to the understanding of the often-observed power-law scaling of porous media (soil, aquifers, . . .) properties and specifically hydrogeologic variables such as permeability and porosity. The authors used the methods of moments and of the so called extended power-law scaling to identify power law scaling of log air permeability data collected (using four measurement support scales) on the faces of a laboratory-scale cube of tuff and published by Tidwell and Wilson in 1999. The methodology used for analyzing the data are presented in a clear-cut manner and the discussion/conclusions are original bringing a new insights into the derivation and significance of these power-law scaling (and range of occurrence)

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observation. The explanation of the advantage of ESS for analyzing the power-law scaling is particularly interesting.

### Specific comments

Although the paper contains sufficient information and original works to be published as it is there are some issues that could be discussed (or at least noted):

1) This paper focus on a structure function defined using measurement increment which supports the comparison with variogram analysis. Yet, such kind of function and moment approach (eq. 1) and the occurrence of power-law scaling have been largely applied (Bird at al., 2006, J. of Hydrology; Dathe et al., 2006; Geoderma) to the measurement itself (in this case the size of the support volume is used instead of the lag) and conclude that the nonlinear variation of the scaling exponent with  $q$  denotes multifractality. I believe it would be useful to comment on the use of measurement increment versus measurement (as well as the possible use of negative values for  $q$ ).

2) What could explain that the log permeability distribution of this rock is similar to a  $tfBm$  (and why it is not the case along direction  $z$ ).

3) Could we extend the conclusions by saying that : if the signal measured is not a  $tfBm$  distribution, then ESS should not perform better than the standard moment method ?

### Technical corrections

- The use of “ $s$ ” for denoting the lag is sometimes confusing (while the structure function is noted “ $S$ ”) and makes typos consequential such as in equation 2 ( $S \sim s^f(q)$ ).

- Why “ $N$ ” depends on “ $s$ ” (it is not always the case isn’t it) ?

- I believe that a couple of sentences (in the introduction) explaining for non-specialists what is “a signal derived from additive processes subordinated to a truncated version ( $tfBm$ ) of additive, self-affine fractional Brownian motion ( $fBm$ )” would make the paper more attractive to most of the hydrologists !

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- Line 24, page 7814 “to  $H = 0.74r_i = 1.27 \text{ cm}$ ” should be “to  $H = 0.74$  for  $r_i = 1.27 \text{ cm}$ ”
- (some of the) stationary variograms of Fig. 14 could be added in figure A1 for direct comparison.
- explain notation “!!” in A2 and A8

In conclusion, I support the publication of this paper because 1) it addresses relevant scientific questions with applications to a very large number of domains; 2) the concepts and mathematical tools are presented in details, making this paper very didactic and original; 3) substantial conclusions are reached and reopen the discussion on the significance of the observed power-law scaling in the frame of fractal and multi-fractal models.

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