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## A study on the derivation of a mean velocity formula from Chiu's velocity formula and bottom shear stress

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### Abstract

This study proposed a new discharge estimation method using a mean velocity formula derived from Chiu's 2D velocity formula of probabilistic entropy concept and the river bed shear stress of channel. In particular, we could calculate the mean velocity, which is hardly measurable in flooding natural rivers, in consideration of several factors reflecting basic hydraulic characteristics such as river bed slope, wetted perimeter, width, and water level that are easily obtainable from rivers. In order to test the proposed method, we used highly reliable flow rate data measured in the field and published in SCI theses, estimated entropy  $M$  from the results of the mean velocity formula and, at the same time, calculated the maximum velocity. In particular, we obtained  $\phi(M)$  expressing the overall equilibrium state of river through regression analysis between the maximum velocity and the mean velocity, and estimated the flow rate from the newly proposed mean velocity formula. The relation between estimated and measured discharge was analyzed through the discrepancy ratio, and the result showed that the estimate value was quite close to the measured data.

### 1 Introduction

Korea has rainfall with large seasonal variation, and because of its east-high and west-low landform, the river slope is steep and the length of main channel is short. For these reasons, flood is discharged at once and therefore, the country is very vulnerable to water-related disasters. In order to overcome the natural environment and to achieve the national status as a world power in water control, the Korean government is promoting the Four Major Rivers Restoration Project, investing 15.4 trillion won from June 2009 as a part of the "Green New Deal" policies. This is a very important national project, and the largest river design and construction work in Korean history. Despite its scale, however, the project aims to complete weirs, reservoirs, and various linked projects within a relatively short period until 2012. Thus, it is quite important

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**Table 1.** Discharge estimation process using the proposed method.

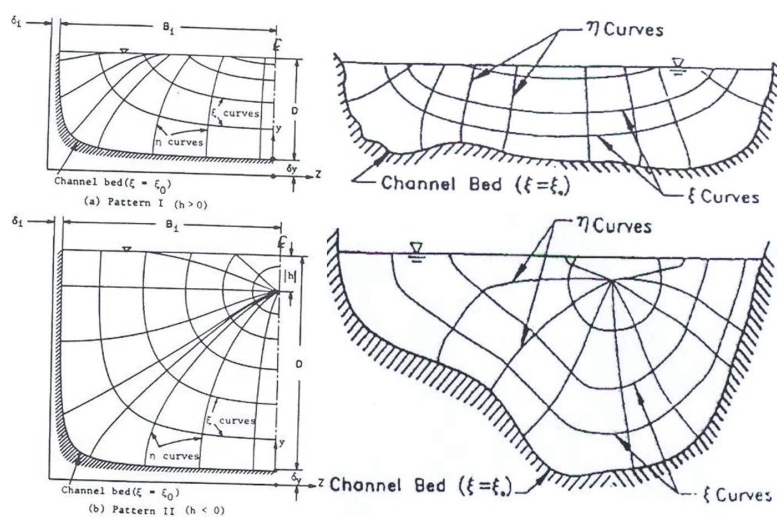
Estimate $M$ by substituting $F(M)$ , $\overline{h_{s_0}}$ , $g$ , $R$ , $l_f$ , $\nu$ for each cross-section of channel, and then estimate $\phi(M)$ .
Estimate the maximum velocity of each cross-section from Eq. (12).
From the Eq. (13), estimate overall equilibrium state $\phi(M)$ which means the gradient of the linear relation. Accurately estimate mean velocity using this $\phi(M)$ .
Test the accuracy of the flow rate based on estimated and measured flow rate using the discrepancy ratio.

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**Table 2.** Linear regression analysis between  $u_{\text{mean}}$  and  $u_{\text{max}}$ .

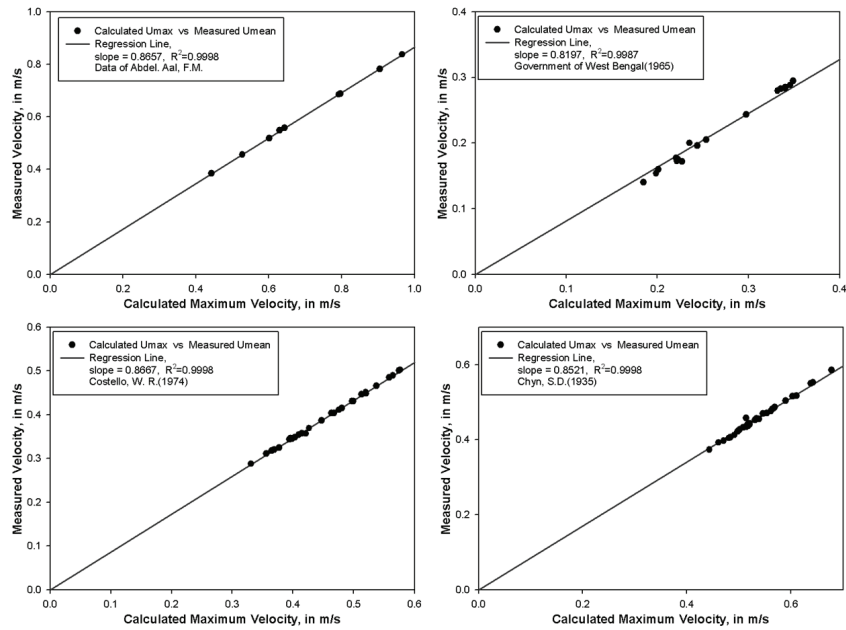
Data		$u_{\text{mean}} = \phi(M)u_{\text{max}}(y = ax)$	$\phi(M)$	$R^2$
In the lab	Abdel-Aal (1969)	$u_{\text{mean}} = 0.8657u_{\text{max}}$	0.8657	0.9998
	Govt. of W. Bengal (1965)	$u_{\text{mean}} = 0.8197u_{\text{max}}$	0.8197	0.9987
	Chyn (1935)	$u_{\text{mean}} = 0.8521u_{\text{max}}$	0.8521	0.9998
	Costello (1974)	$u_{\text{mean}} = 0.8667u_{\text{max}}$	0.8667	0.9998
In the river	Acop Canal data of Mahmood et al. (1979)	$u_{\text{mean}} = 0.9110u_{\text{max}}$	0.9110	0.9999
	Hii River data of Shinohara and Tsubaki (1959)	$u_{\text{mean}} = 0.8824u_{\text{max}}$	0.8824	0.9992
	Leo-River data of Leopold (1969)	$u_{\text{mean}} = 0.9146u_{\text{max}}$	0.9146	0.9999

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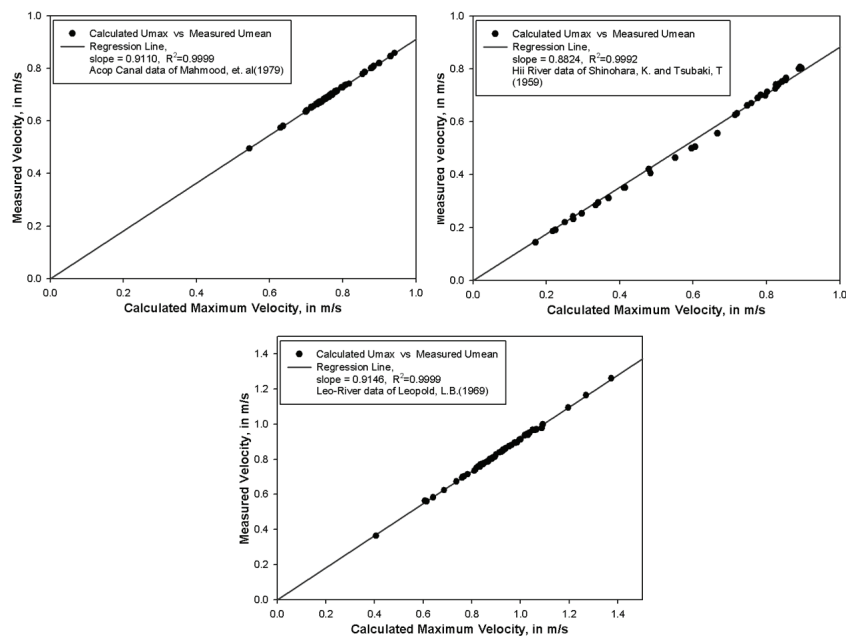
**Fig. 1.**  $\xi - \eta$  coordinates in open-channel sections (Chiu, 1988, 1989).

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**Fig. 2.** The relationship between measured mean velocity and caculated maximum velocity in the lab. channels.

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**Fig. 3.** The relationship between measured mean velocity and caculated maximum velocity in the natural open channels.

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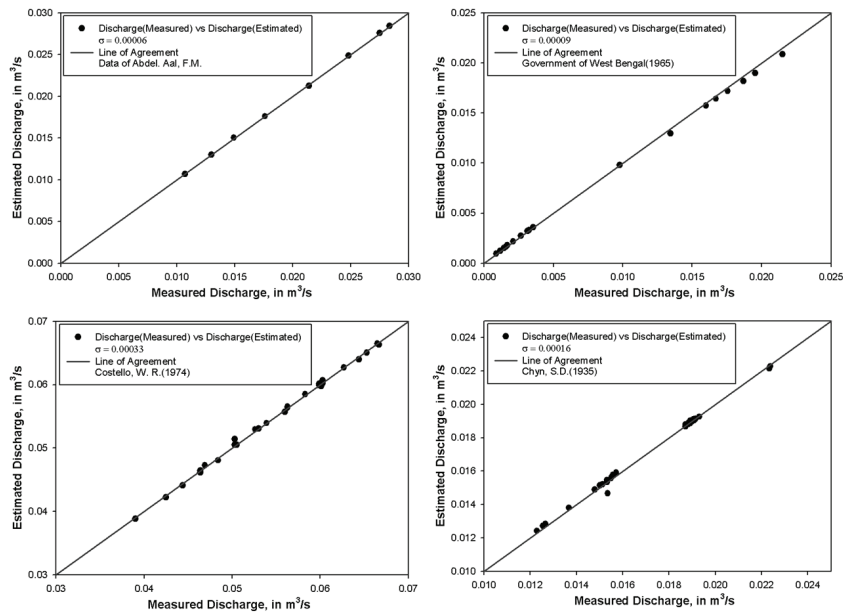


Fig. 4. Analysis results by using proposed mean velocity equation in the lab. channels.

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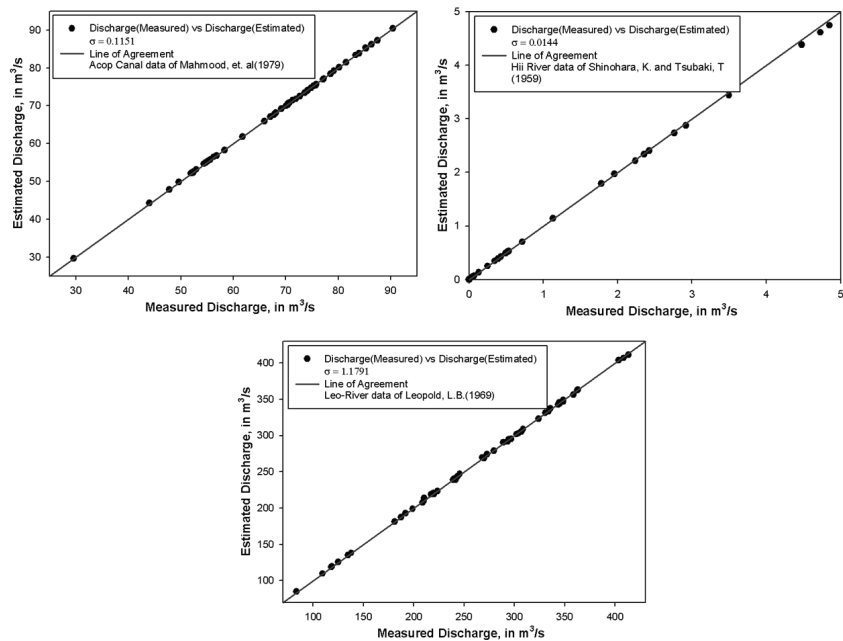
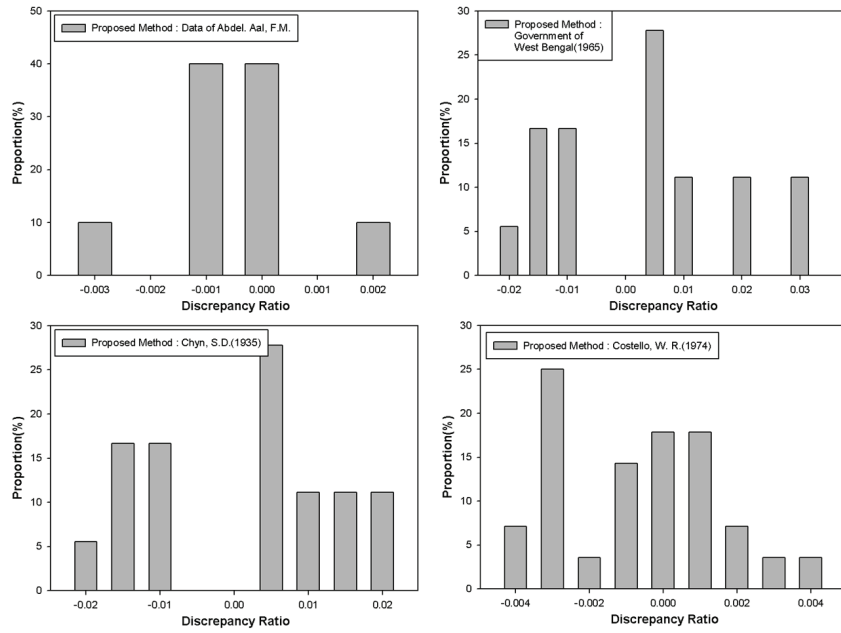


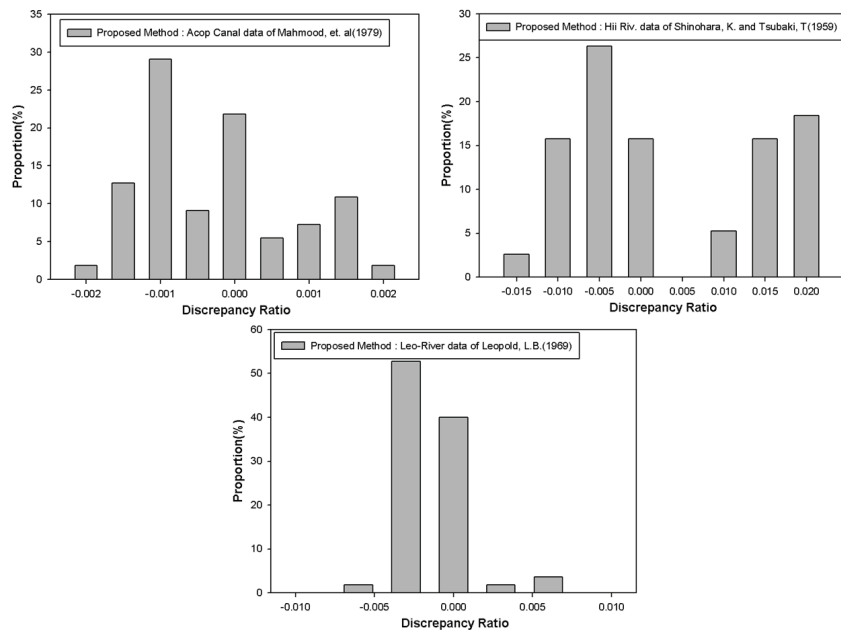
Fig. 5. Analysis results by using proposed mean velocity equation in the natural open channels.

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**Fig. 6.** Discrepancy ratio analysis between measured and estimated discharge in the lab. channels.

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**Fig. 7.** Discrepancy ratio analysis between measured and estimated discharge in the natural open channels.

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