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# Ensemble modelling of nitrogen fluxes: data fusion for a Swedish meso-scale catchment

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## Abstract

Model predictions of biogeochemical fluxes at the landscape scale are highly uncertain, both with respect to stochastic (parameter) and structural uncertainty. In this study 5 different models (LASCAM, LASCAM-S, a self-developed tool, SWAT and HBV-N-D) designed to simulate hydrological fluxes as well as mobilisation and transport of one or several nitrogen species were applied to the mesoscale River Fyris catchment in mid-eastern Sweden.

Hydrological calibration against 5 years of recorded daily discharge at two stations gave highly variable results with Nash-Sutcliffe Efficiency (NSE) ranging between 0.48 and 0.83. Using the calibrated hydrological parameter sets, the parameter uncertainty linked to the nitrogen parameters was explored in order to cover the range of possible predictions of exported loads for 3 nitrogen species: nitrate ( $\text{NO}_3$ ), ammonium ( $\text{NH}_4$ ) and total nitrogen (Tot-N). For each model and each nitrogen species, predictions were ranked in two different ways according to the performance indicated by two different goodness-of-fit measures: the coefficient of determination  $R^2$  and the root mean square error RMSE. A total of 2160 deterministic Single Model Ensembles (SME) was generated using an increasing number of members (from the 2 best to the 10 best single predictions). Finally, the best SME for each model, nitrogen species and discharge station were selected and merged into 330 different Multi-Model Ensembles (MME). The evolution of changes in  $R^2$  and RMSE was used as a performance descriptor of the ensemble procedure.

In each studied case, numerous ensemble merging schemes were identified which outperformed any of their members. Improvement rates were generally higher when worse members were introduced. The highest improvements were achieved for the nitrogen SMEs compiled with multiple linear regression models with  $R^2$  selected members, which resulted in the RMSE decreasing by up to 90%.

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# 1 Introduction

## 1.1 Catchment modelling

In recent decades, anthropogenic influence on environmental systems has been demonstrated. Naturally balanced biogeochemical cycles such as the nitrogen cycles have been deeply altered (Vitousek et al., 1997; Galloway et al., 2004) since the middle of the 18th century. For about 50 years now, the increasing speed of computers allowed scientists from different fields to simulate such systems (e.g. atmosphere, hydrosphere) behaviour through different sets of mathematical equations. In hydrological sciences numerous different models were created from the 1960s onwards. For example, Boughton (2005) reviewed 13 different rainfall-runoff models developed in Australia alone in the second half of the 20th century. Numerical models are nowadays used as management tools that are able to give an approximation of the effects of different changes on a natural system (e.g. land use change, global warming).

In order to simulate both hydrology and N mobilisation and transport at the catchment scale, multiple conceptualisations, involving different degrees of complexity, were developed (e.g., see Boughton, 2005). However, as emphasised by Breuer et al. (2008), there is no single accepted theory of catchment N cycling and models simulating the effects of nitrogen on hydrological and biogeochemical ecosystem functioning are still facing a high degree of uncertainty. Differences between models can be related to the questions they are used to address, involving different descriptions of the nitrogen balance. Some are process-based (i.e. conceptual parameters determine N turnovers rates such as in LASCAM, INCA, and HBV-N), while others are more physically-based and use parameters that are directly related to measurable quantities as for example the SWAT model. However, for the sake of simplification all models neglect some part of the well described N cycle that generally consists of ammonification, nitrification, anaerobic ammonium oxidation, denitrification, and nitrogen fixation. They sometimes totally ignore one or more N-species involved into this cycle.

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Of course, due to the chaotic nature of the natural systems many simulated processes cannot be exactly described by a set of equations and this lack of knowledge involves the introduction of a certain, hardly quantifiable structural model uncertainty. Other sources of predictive uncertainty are forcing data uncertainty and parameter uncertainty, regrouped under the general term of stochastic uncertainty. It is usually difficult to assess the contribution to the total uncertainty from each of these elements. However, ensemble approaches have been proposed to investigate part of this contribution (Smith et al., 2004; Breuer et al., 2009).

## 1.2 Ensemble modelling approach

Several global methods to assess parameter uncertainty have been described, e.g. the Monte-Carlo sampling based Generalized Likelihood Uncertainty Estimation (GLUE) approach (Beven and Binley, 1992). As parameter interactions are usually a sensitive source of uncertainty, a high number of realisations is required to cover a representative number of feasible parameter combinations and corresponding model simulations. Different combinations of parameter sets for a given model, based on a random sampling of parameter values in realistic ranges (e.g., Monte-Carlo procedures or Latin-Hypercube stratified sampling, McKay et al., 1979), are a common way to compile single-model ensembles (SME), i.e. combinations of distinct predictions obtained by perturbation of parameters, input data or initial conditions. SME built from random sampling are direct descriptions of the possible range of outcomes and illustrate part of the stochastic model uncertainty.

Multi-model ensembles (MME) are based on the combination of several deterministic model outputs. They are a state-of-the-art option for considering the structural model uncertainty component of the total predictive uncertainty and have been widely used in climatic and atmospheric sciences where MMEs usually outperform individual models and SMEs. However, MMEs have received little attention in hydrology even though initial MME studies of hydrological simulation were already published in the mid 1990s.

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Still, ensembles of models have been utilised in two different ways in hydrological sciences. First, some studies considered whole sets of predictions in a probabilistic way. The evaluation of these ensembles has been carried on based on skill scores which characterise the correctness of the prediction of some selected particular events, usually exceeded thresholds, in terms of correct match and false alarm rates. Good examples of such approaches were described by Renner et al. (2009) or Georgakakos et al. (2004), the latter having been realised in the frame of the Distributed Model Intercomparison Project (DMIP; Smith et al., 2004) in which calibrated and un-calibrated models were used. Some other studies combined single predictions using different statistical post-processing methods, or data-fusion schemes, in order to produce single “best” deterministic forecasts. For instance Shamseldin et al. (1997) utilised 3 combination methods to merge the output of 5 models. The philosophy behind this approach was that each model captures certain important aspects of the information available about the system and that the strengths of some may compensate weaknesses of other models, resulting in an overall better prediction. They concluded that combining outputs of rainfall-runoff models could provide better results than the best single run even with a simple averaging method. Lately, in the frame of assessing the impact of Land Use Change on Hydrology by Ensemble Modelling (LUCHEM; Breuer and Huisman, 2009) almost 30 different merging schemes were tested with 10 different model results over the same catchment as reported by Viney et al. (2009). McIntyre et al. (2005) also used model ensembles to predict discharge in ungauged or poorly gauged basin as part of the Predictions in Ungauged Basins (PUB; Sivapalan, 2003) initiative by the International Association of Hydrological Sciences. In the light of PUB, ensemble predictions are assumed to significantly increase the credibility of predictions.

We were not aware of any ensemble predictions, more particularly model combinations, in hydro-biogeochemistry to date and see this methodological approach as a first step into that direction. In this study we compiled different deterministic SMEs and MMEs by merging the nitrogen outcomes of five models following different methods

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previously used in the LUCHEM project (Viney et al., 2009). The reader must keep in mind that results of the different single models were not created with the aim to produce a benchmark report on the efficiency of the models alone. We focused our evaluation on the effect of merging results rather than on the results themselves. Differences between the models led us to make some choices (i.e. studied period, number of model realisations) that one could consider arguable (see Sect. 2). However, the main aim of this study remained to apply some data-fusion methods to different sets of nutrient predictions before comparing ensembles with single models. Results should give a primary evaluation of the applicability of the ensemble-modelling concepts to the highly uncertain N predictions.

The models involved were LASCAM (Sivapalan et al., 1996a,c; Viney et al., 2000) and its modified LASCAM-S version (this paper), SWAT (Arnold et al., 1998) in its 2005 version, HBV-N-D (Lindgren et al., 2007) and a new model based on the concepts proposed in INCA (Wade et al., 2002; Whitehead et al., 1998) coupled to the soil moisture equations of the HBV model (Lindström et al., 1997). This latter tool is referred as CHIMP (Combined HBV and INCA Modified in Python) throughout the text.

This article is organised as follows. Section 2 presents the catchment and the available data for model application. The models are also described as well as the methodology we adopted to create new predictions we adopted. In Sect. 3 we present the results for the single models, SMEs and MMEs N predictions. They are discussed in Sect. 4 and possible further research directions are presented in Sect. 5 along a short summary of the main conclusions that could be drawn from this study.

## 2 Materials and methods

### 2.1 The Fyris River catchment

The Fyris catchment is located in central Sweden, 90 km north of Stockholm. The Fyris River has a catchment area of 2000 km<sup>2</sup> and flows into Lake Ekoln, a northern part of Lake Mälaren (Sweden's third largest lake) which drains into the Baltic Sea.

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It is a lowland catchment whose elevation ranges between 15 and 115 m. Streams drain from the north, east and west to the outlet at Flottsund (Fig. 1). Land use is dominated by forest (mainly coniferous) which occupies about 59% of the catchment while croplands cover 33% of the area. Other minor land-use types are wetlands (4%), urban areas (2%) and lakes (2%). Forests are mainly associated with till and croplands with clay soils (Lindgren et al., 2007).

Daily records of precipitation (8 gauges) and temperature (3 stations) collected by the Swedish Meteorological and Hydrological Institute (SMHI) were used for the 5 years study period (2000–2004). During this time mean annual precipitation was about 640 mm. The warmest and wettest months on average was July (>80 mm precipitation, +17 °C mean daily temperature) while the driest month was April (<40 mm precipitation) and the coldest months were December and January (–1 °C). Over the study period, two daily discharge series were available for two non-nested sub-catchments: Vattholma and Sävja, with contributing areas of 281 km<sup>2</sup> and 699 km<sup>2</sup>, respectively (Fig. 1). There was no gauging station available at the catchment outlet to Lake Mälaren. High flows usually occurred from late autumn to early spring. Inter-annual variability of discharge was high and thaw-refreezing events led to high temporal variability of winter discharge in some years. Mean annual runoff was 219 mm at Vattholma and 189 mm at Sävja. In-stream nitrogen input data from sewage treatment plants was also available on a daily time step for the largest plant in Uppsala, and with a biweekly or monthly resolution for four smaller ones (Fig. 1). The observed point source discharges were interpolated to a daily time step as described in Lindgren et al. (2007).

For the same period, stream chemistry data from 2 long-term measurement stations of the Swedish University of Agriculture was available for model applications. Monthly measurements of NO<sub>3</sub>+NO<sub>2</sub>, NH<sub>4</sub> and Tot-N concentrations resulted in a total of 60 measurements for each station and each nitrogen species. The water quality sampling stations Vattholma and Kuggebro were located close to the gauging stations Vattholma and Sävja, respectively (Fig. 1). The Fig. 2 illustrates the monthly average concentrations of the different N-species. More treatment plants were located upstream

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from Sävja which was surely a key factor to explain the usually higher concentrations measured at this location (Fig. 2). Concentrations were typically higher during winter months as well. More precisely at the Vattholma station, Tot-N concentrations ranged between 0.9 and 1.4 mg/l with a contribution of 26% of  $\text{NO}_3 + \text{NO}_2$  and 5% of  $\text{NH}_4$  on average. At Sävja, the Tot-N concentrations showed a higher variability as they ranged between 1.0 and 2.9 mg/l with a contribution of 54% of  $\text{NO}_3 + \text{NO}_2$  and 4% of  $\text{NH}_4$ . As shown in Fig. 2,  $\text{NO}_3 + \text{NO}_2$  concentrations were the main factor explaining the Tot-N concentrations variability as a picture of their large contribution to this global measurement.

Estimates of daily exported loads were computed for these gauging stations using concentrations measured at the sampling stations, assessing that they were representative of the mean daily concentrations. Separate sampling of the  $\text{NO}_2$  concentration indicated that it provided a negligible contribution to the  $\text{NO}_3 + \text{NO}_2$  concentration. It was therefore assumed that the  $\text{NO}_3$  concentration is approximately equivalent to the measurements of  $\text{NO}_3 + \text{NO}_2$  concentration. The combination of high concentrations and high flows during winter led to estimate large fluxes up to 700 kg and 6 tons of exported N per day at Vattholma and Sävja respectively. The water discharging from the Sävja sub-catchment had higher N concentrations as shown in Fig. 2, we therefore estimated higher specific N fluxes (about  $13.3 \text{ g/ha d}^{-1}$  on average) for this station than for Vattholma ( $6.8 \text{ g/ha d}^{-1}$ ).

## 2.2 Models

The five models used in the ensemble set up (LASCAM, LASCAM-S, CHIMP, SWAT and HBV-N-D) could simulate both runoff and the mobilisation and transport of different nitrogen species (see Table 1) at the landscape scale and at a daily time step. The models showed great variations in their smallest spatial units as well as the required input data, thus providing a good structural variability among the cohort (see Table 1).

For the semi-distributed models (i.e. all except HBV-N-D) we subdivided the Fyris River catchment into 70 sub-catchments. This spatial disaggregation assigned 9 and

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28 upstream sub-catchments for the Vattholma and Sävja stations, respectively, corresponding to mean sub-catchment areas of 31 and 25 km<sup>2</sup>. For these models we also estimated the daily potential evapotranspiration using the Hargreaves method (Hargreaves and Samani, 1985). Daily results were then aggregated to the required temporal resolution (see Table 1). The HBV-N-D evapotranspiration input was based on monthly mean evapotranspiration estimates (Lindgren et al., 2007).

Below an overview of the various models is given, for a more detailed description of the water and nitrogen simulations the reader is referred to the original publication of the models. A short, general overview of nitrogen processes considered in these models was also provided by Breuer et al. (2008).

### 2.2.1 LASCAM and LASCAM-S

The semi-distributed LASCAM model was first developed for applications in arid or semi-arid regions in order to simulate water and salt balance at larger scales (Sivapalan et al., 1996a,b,c). Later new routines were integrated to simulate sediments (Viney et al., 1999) and nutrients (e.g., Total-N, NO<sub>3</sub> and NH<sub>4</sub>; Viney et al., 2000) mobilisation and transport. Each sub-catchment corresponds to an idealised hill slope in which 3 water and 2 nitrogen stores are interconnected. As the LASCAM model was designed to simulate dry and warm environments, the original version did not integrate any snow routine. We therefore developed the extended LASCAM-S version by implementing the degree-day approach used in the original HBV model to allow simulation of snow accumulation and melt at the sub-catchment scale. This routine is based on air temperature and a water-holding capacity of the snowpack. Depending on a threshold temperature (usually 0°C) the snow pack melts and the water equivalent is added to the water input to the soil (Lindström et al., 1997).

The same parameter set is applied to each sub-catchment in combination with interpolated precipitation and temperature data (only for LASCAM-S). The daily potential evapotranspiration is calculated for each sub-catchment by multiplying the mean annual potential evapotranspiration by a scaling factor derived from a sinusoidal function

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of time. Evaporation demand is fulfilled by the 3 water stores depending on their respective levels. Nitrogen cycling at the sub-catchment scale is simulated by the following processes for both models: residue decay, plant harvest, mineralisation, volatilisation, plant uptake, nitrification, denitrification and fixation.

Water and nutrients are routed downstream. While dissolved nitrogen is not affected by any further in-stream biological or chemical reactions, water can evaporate and re-infiltrate and particulate nitrogen is affected by the erosion and sediments dynamics.

### 2.2.2 CHIMP

The semi-distributed INCA model requires daily effective rainfall (i.e. after canopy interception) and daily soil moisture deficit input data (Whitehead et al., 1998) which are usually difficult to assess. These variables were derived by feeding the flow generation and nitrogen routines of INCA with the output of the snow and soil moisture routines of HBV (Lindström et al., 1997). The INCA nitrogen module only outputs predictions of inorganic nitrogen species (i.e.  $\text{NO}_3$  and  $\text{NH}_4$ ) balance. All the equations were adapted from literature references (Whitehead et al., 1998; Lindström et al., 1997) and the two models were regrouped under the name CHIMP.

Each sub-catchment is disaggregated into up to 5 different land-use classes which all have their own parameter sets for water and nutrients balance. They are not spatially identified within the sub-catchment and their outputs are weighted by their respective areas to contribute to the stream flow.

The HBV snow routine is also based on the empirical degree-day approach. Evapotranspiration is calculated as a function of the input potential evapotranspiration and the HBV soil store. Below a chosen threshold of soil moisture the actual daily evaporation is computed as a linear function of the daily potential evapotranspiration. Above this threshold the total evaporation demand is fulfilled (Lindström et al., 1997). The soil routine of HBV provides the hydrological effective rainfall (e.g. water available for runoff) which is routed to the 2 INCA flow generation boxes. The soil moisture deficit

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required by INCA is computed as the difference between this soil storage content and the maximum value.

In both flow generation boxes different nitrogen turnover processes are simulated: plant uptake, nitrification, denitrification, fixation, mineralisation and immobilisation.

5 The organic N store is considered as infinite so that the mineralisation rate does not depend on its magnitude. Each process is characterised by a kinetic equation which is based on turnover rates (user input) as well as a temperature and a soil moisture deficit index. Water,  $\text{NO}_3$  and  $\text{NH}_4$  concentrations discharge into the sub-catchment stream. There is no re-infiltration but nitrification and denitrification can still occur. Sewage  
10 treatment plant effluents are directly added to the stream  $\text{NO}_3$  and  $\text{NH}_4$  contents.

### 2.2.3 SWAT

The SWAT model (Arnold et al., 1998) is a semi-distributed, physically-based model (Gassman et al., 2007). It is able to simulate the long term water and nutrients balance (e.g.  $\text{NO}_3$ ,  $\text{NO}_2$ ,  $\text{NH}_4$  and Organic-N, see Table 1). We used the SWAT model in its  
15 2005 version.

Each SWAT sub-basin is divided into Hydrological Response Units (HRU). Each HRU corresponds to a single combination of a land-use class and a soil-type that can be parameterised individually. HRUs are not spatially identified within their sub-catchment. SWAT simulates snowpack and snowmelt processes at the HRU scale based on the  
20 empirical degree-day approach with a daily update of the melting rate between user defined maximum and minimum values. At the HRU scale, SWAT incorporates a simplified dynamic crop growth module. The corresponding canopy intercepts a part of the precipitation which is a function of its Leaf Area Index. Evaporation demand is first fulfilled by the canopy and eventual higher demand is partly fulfilled by the soils. In-stream  
25 discharge of each HRU is composed of several elements: surface runoff, lateral flow and baseflow. Therefore, the idealised hill slope is composed of interconnected multi-layer soil storages and a double groundwater system. Different nitrogen processes are simulated within each HRU soil layer: plant uptake, residue decay, mineralisation,

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nitrification, volatilisation, denitrification, fixation and leaching. Turnover rates depend on temperature and moisture, or soil water content.

In-stream water and corresponding nutrient content routing is based on a variable storage method (Williams, 1969). Re-infiltration and biochemical nitrogen reactions are allowed: algal respiration and uptake, hydrolysis and oxidation. Turnover rates are temperature-dependent.

The SWAT setup was realised with the support of the ArcSWAT 2.1.4 for ArcGIS 9.2 extension (Olivera et al., 2006). Within 70 sub-catchments for the whole Fyris River watershed, a total of 622 HRUs was delineated by combining 5 land-use classes with 7 soil types. This corresponds to a total of 108 and 232 HRU for Vattholma and Sävja sub-basins, respectively with corresponding mean area of 2.60 and 2.48 km<sup>2</sup>, respectively. ArcSWAT automatically assigns the climatic records of the nearest station to each sub-catchment.

## 2.2.4 HBV-N-D

HBV-N-D is a fully distributed version of the original HBV model routines combined with the conservative solute transport model concepts of the TAC<sup>D</sup> model (Wissmeier and Uhlenbrook, 2007). The model used a grid representation of the catchment (here 250 x 250 m<sup>2</sup> grid cells) and is implemented in the PCRaster modelling environment (Karssenberg et al., 2001). HBV-N-D requires daily precipitation and temperature data input and weighs resulting flow and storage amounts per fractions of land-use class in each grid cell. Snow is simulated using an empirical degree-day approach at the land-use scale. Within a grid cell, HBV soil moisture and flow generation boxes can be parameterised individually for each land-use class (Lindström et al., 1997). The actual evaporation is calculated in accordance with the HBV equations following the same process described in Sect. 2.2.2. Water entering a response function is assigned a Tot-N leakage concentration. HBV-N-D is based on a single flow direction algorithm (O'Callaghan and Mark, 1984) for lateral cell to cell connection, so that water or Tot-N output from any runoff generation box is diverted into the corresponding box of

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the neighbouring downstream cell. When a grid cell is identified as a stream cell, a simple distribution function is applied to route the water and corresponding Tot-N content downstream. Nitrogen retention is modelled as a net effect of various biogeochemical processes such as uptake, sedimentation and denitrification. It is a function of the Tot-N concentration, the average temperature of the 10 last days and a free parameter and retention occurs in each response function box as well as in lakes or in-stream.

The HBV-N-D model application in this study is based on the identical model setup utilised in an earlier model comparison for nitrogen source apportionment (Lindgren et al., 2007). The running time of the model was a limiting factor for our study which explains the choice of a relatively short 5 years evaluation period and discrepancies in the hydrological calibration and ensemble generation procedures (Sect. 2.3).

## 2.3 Ensembles construction and assessment

A global overview of the methodological approach used in this study is presented in the Fig. 3. This flow chart summarises the different steps which followed to create the different types of ensembles. A more detailed chronological description of the adopted methodology is presented in the next paragraphs.

### 2.3.1 Hydrological calibration

Water transports particulate and dissolved chemical species through a catchment. A certain part of the stochastic uncertainty of the nutrient fluxes is then logically linked to the variations of the hydrologic parameters. In a calibration context, numerous studies were based on a two-step approach. First, modellers determined the optimal parameter sets for hydrology only. Then, they calibrated the nutrient component only while keeping this optimal water balance description (e.g., Andersson et al., 2005; Viney and Sivapalan, 2001; Wade et al., 2002).

Subsequently, in this study we calibrated the hydrological components of the models against the two available discharge records (i.e. Vattholma and Sävja) in order to

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obtain the best water balance simulation for the whole catchment over the study period from 1 January 2000–31 December 2004. For all models except the computationally expensive HBV-N-D model, the Parameter Solution method (ParaSol, van Griensven et al., 2002) which is based on the Shuffled Complex Evolution algorithm (SCE-UA, Duan et al., 1992) was used for parameter optimisation. The ParaSol method requires the daily sum of the squared errors (SSE, Eq. 1).

$$SSE = \sum_{i=1}^N (O_i - S_i)^2 \quad (1)$$

In the Eq. (1),  $O_i$  and  $S_i$  are observed and simulated runoff at time step  $i$ . Their squared difference is summed for each of the  $N$  considered time steps. ParaSol automatically aggregates SSE values for each considered flux in a global objective criterion which is reduced by the SCE-UA algorithm. The Parameter Estimator (PEST; Doherty, 2005) was chosen to calibrate the computationally expensive HBV-N-D model as it usually requires fewer model realisations. The objective function was a weighted SSE with weights set as the inverse of the standard deviation of the corresponding observations.

In order to compare the goodness-of-fit resulting from the calibration efforts at each station, the results were expressed as the Nash-Sutcliffe efficiency for daily flows (NSE, Nash and Sutcliffe, 1970) which is a common standardisation of the SSE normalised by the variance of the observations (Eq. 2).

$$NSE = 1 - \frac{\sum_{i=1}^N (O_i - S_i)^2}{\sum_{i=1}^N (O_i - \bar{O})^2} \quad (2)$$

In the Eq. (2),  $O_i$  and  $S_i$  corresponds to notations in the Eq. (1) while  $\bar{O}$  is the mean observed runoff over the  $N$  considered time steps. No differences in model performance rankings are to be expected after this transformation. NSE values range between  $-\infty$  and 1, the latter being achieved for a perfect fit between observations and predictions. NSE values tend to be not very sensitive to the volume error but are biased in favour

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of peak flows (Legates and McCabe, 1999; Krause et al., 2005) which are dominant in this catchment in response to the spring snow melt. In such conditions, good NSE values could be achieved with somewhat biased predictions. To cope with this, we also evaluated our models by using the total bias to assess the performance of the models to estimate the total runoff.

### 2.3.2 Nitrogen ensembles construction

In order to focus the study on the stochastic uncertainty linked to the nitrogen algorithms only, a large number of model runs were realised by keeping the previously calibrated water balance parameters and altering the parameters only governing the N mobilisation and transport. A Monte-Carlo procedure was used for LASCAM, LASCAM-S, CHIMP and SWAT, providing 40 000; 40 000; 60 000 and 20 000 realisations corresponding to 16; 16; 28 and 7 altered parameters, respectively. A Latin-Hypercube stratified sampling procedure (McKay et al., 1979) was chosen for the computationally expensive HBV-N-D model, leading to overall 280 model runs for only 4 altered parameters. We are conscious that one would argue that the number of model realisations was not sufficient to explore the whole uncertainty. However, our aim was to create large sets of model realisations before testing the effect of our different data-fusion methods. Moreover optimal parameter sets may actually not exist according to the equifinality theory (Beven and Freer, 2001) or may differ for the different considered N species and stations as well. We still allocated more runs to the more parameterised models, taking into account that more parameter interactions would occur.

The large number of realisations for each model allowed us to compile several SMEs for each model, N species and measurement station independently. Each realisation was evaluated with two goodness-of-fit indicators: the coefficient of determination  $R^2$  and the Root Mean Squared Error (RMSE; Eq. 3).

$$\text{RMSE} = \sqrt{\frac{\sum_{i=1}^N (O_i - S_i)^2}{N}} \quad (3)$$

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In Eq. (3) notations correspond to those used in the Eqs. (1) and (2). The coefficient of determination and the RMSE were computed by comparing the estimated exported loads with the predictions of the corresponding time step. The difference between the two criteria is that  $R^2$  requires only the dynamics, or relative differences, to be simulated correctly, while RMSE evaluates differences between observed and simulated values (Legates and McCabe, 1999). While  $R^2$  is not a suitable criterion alone, because the best achievable value of 1.0 does not imply a perfect fit. However, it provides in the case of N concentrations the useful information of whether at least the dynamics are correct. The lower the RMSE, the better the results, and by evaluating the error this last criterion is partly influenced by the bias of prediction. For each case (i.e. each N species, station and model), SMEs were compiled by using the five merging schemes in Table 2 applied to the 2 to 10 best model runs regarding each criterion, respectively (i.e.  $R^2$  and RMSE). This resulted in a total of 90 SMEs per model, station and nitrogen species, and 2160 SMEs overall (CHIMP being not able to simulate Tot-N, and HBV-N-D not being able to simulate  $\text{NO}_3$  and  $\text{NH}_4$ ). The coefficients obtained by unconstrained multiple linear regression (UR) and constrained multiple linear regression (CR) with monthly measurements were applied to the whole time series (i.e. the daily predictions over 5 years). Due to the occasional occurrence of negative coefficients, some negative predictions may occur and the corresponding SMEs were discarded.

For each model, N species and station, the best SME considering RMSE was selected for inclusion in the MMEs. Again following the merging schemes outlined in Table 2 applied to each possible combination of 2 to 4 selected SMEs, we obtained 55 different MME predictions for each N species. We evaluated the evolution of both criteria for every generated MME and SME by also quantifying the improvement rate for RMSE.

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3 Results

3.1 Hydrology

A summary of calibration results for the water balance components of the models is presented in Table 3. A high variability across models is observed between the different NSE and bias values. The models perform alternatively better at Vattholma (LASCAM-S, SWAT) or at Sävja (LASCAM, CHIMP, HBV-N-D). Considering the bias, which was not used for the automatic calibration procedure, results are worse for Sävja than for Vattholma, except for CHIMP. Over-predicting models at Vattholma under-predict at Sävja and vice-versa. While SWAT shows the best NSEs for each station it also presents the highest absolute biases in each case.

3.2 Nitrogen

3.2.1 Single runs overview

A summary of the best simulations for each model and each criterion ( $R^2$  and RMSE) is given in Table 4 together with the results of the SMEs. As expected models that were presenting the best  $R^2$  value for each N species do not necessarily have the best RMSE performance. SWAT performed the best for  $\text{NO}_3$  simulations for both criteria. For  $\text{NH}_4$ , the best  $R^2$  and RMSE were provided by CHIMP at Vattholma and LASCAM-S at Sävja. For Tot-N, the best  $R^2$  values were obtained with SWAT and the best RMSE with LASCAM-S, SWAT presenting the worst RMSE values in those cases. While LASCAM-S presented better results than the original LASCAM for the hydrological predictions (Table 3), it did not always give significantly better results for nitrogen predictions, being even outperformed for Tot-N at Vattholma.

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### 3.2.2 Single-model ensembles

SMEs decreased the RMSE in all cases (Table 4 and Fig. 4). The selected SMEs presented in the Table 4 were the ones representing the best compromise between  $R^2$  and RMSE explaining why in four cases we obtained a lower  $R^2$  for the selected SMEs than for the best single member (i.e. Tot-N at Vattholma and for LASCAM-S, NO<sub>3</sub> for LASCAM-S, CHIMP and SWAT at Sävja).

Improvement of RMSE could be quantified in terms of error reduction which can also be visualised in the Fig. 3. Corresponding decreases in RMSE ranged between 9 and 92% for NO<sub>3</sub> at Sävja with LASCAM and NH<sub>4</sub> at Vattholma for SWAT, respectively. The RMSE was reduced by more than 30% in 16 cases out of 24.

On the other hand the evolution of  $R^2$  mainly showed weak improvements but still the best MMEs present a better agreement between estimated and predicted loads as illustrated in the scatter plots of the Fig. 5. More than 80% of UR ensembles had to be discarded due to the occurrence of some negative regression coefficients providing negative predictions when applied to the whole simulated time series. We used CR ensembles to circumvent this problem. The MD ensemble never increased both criteria and only rare and weak improvements were achieved by using the ME and WM ensemble models. The best SME results were always obtained by UR ensembles compiled with  $R^2$  selected members. As was the case for single predictions LASCAM-S SMEs did not always obtain better criterion values than the original LASCAM model.

### 3.2.3 Multi-model ensembles

About 27% of the ME MMEs decreased RMSE values in comparison to their best member (i.e. selected SME), and 38% of the weighted average MMEs compared to the best SMEs. Similarly to SMEs, the feasibility of each MME prediction was checked prior to further model evaluation. Once again, a high number (49%) of regression schemes was discarded. However all the available UR and CR ensembles presented an improvement of both criteria compared to the predictions of the best SME. The

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best results were obtained by including the maximum number of ensemble members (4 for nitrogen if not dismissed due to negative unrealistic negative predictions) in UR ensembles. The best MMEs are illustrated for each N-species and station in the scatter plots of the Fig. 4 beside the best SME predictions. It showed the better agreement between observations and predictions achieved with the MME. It is interesting to notice that the improvement in RMSE of MMEs was stronger if members that were combined in a MME originally presented weaker SME results for  $R^2$  values (e.g. an improvement in RMSE of 27% for  $\text{NH}_4$  at Vattholma) as compared to members of MMEs that already performed well (e.g. an improvement in RMSE of 6% for Tot-N at Vattholma).

#### 4 Discussion

At each discharge and nitrogen station, the quality of the predictions was extremely variable across models even though homogeneous input datasets were used. This behaviour has been reported by many others in hydrological modelling notably (Breuer et al., 2009; Reed et al., 2004; Refsgaard et al., 1996) but also for nutrient predictions at different scales (Diekkrüger et al., 1995; Kronvang et al., 2009b). This variability was also defined as the starting point for any ensemble prediction (Georgakakos et al., 2004; Shamseldin et al., 1997; Viney et al., 2009) with the idea to compensate weaknesses of some models with strengths of the others to improve the global prediction.

A preliminary step of this study constituted in an inter-comparison between the different N models. Heterogeneous results for water and nutrient balance description were obtained. The models which provided the best hydrological predictions did not always give the best N prediction results and no global best model was to be found in our particular case study justifying in some way the need to use different models. A first effort to intercompare a variety of models that have been set up to predict nitrogen flows in different agricultural systems has been published by Diekkrüger et al. (1995). Like in our study the models were set up using a common dataset, guaranteeing that eventual prediction differences depended only on the models or applied concepts themselves.

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Results showed a very high variability between predictions for different N turnover processes. Here we did not quantify process rates, considering our models as black boxes and only analysing the net export of the considered N species through the two outlets. This may be considered as an empirical approach but some big differences in terms of RMSE between the single models (Table 4 and Fig. 3) intrinsically imply high differences in the total N balance description and thus in the involved processes. Recently Kronvang et al. (2009b) provided the first comprehensive results of a model intercomparison project on nutrient load predictions at the mesoscale. This study included 8 nitrogen models (Kronvang et al., 2009a) and concluded that no single nutrient model could be recommended to simulate catchment scale nutrient losses. Accordingly our results (Table 4 and Fig. 4) show that the best single performers (i.e. model) vary between catchments and N species.

Considering the hydrological calibration results (Table 3) the implementation of a snow module into the LASCAM model significantly improved the water balance description, whereas very similar results for the different nitrogen species were obtained. As illustrated on Fig. 3 the SWAT model always presented the worst RMSE for N except for  $\text{NO}_3$  while it presented the best calibration results for hydrology (Table 3). The same behaviour is observed with HBV-N-D which gave an equivalent calibration result for hydrology at Sävja while not presenting the best Tot-N prediction for this station.

These results show that improved water description, even applied with the same N balance description (e.g. LASCAM and LASCAM-S), does not necessarily provide better nutrient export predictions. This means that in the models utilised the N components would be more or less independent from the water routines even though water is the driving force for the movement of any dissolved nutrients in the catchment.

Moreover, high discrepancies between criteria values of each of our “best” nitrogen models (Fig. 4) indicated heterogeneous prediction qualities. The large number of runs realised previously to the SMEs data-fusion procedure guaranteed us that the mismatches of the predictions with the observations could not only be attributed to the sole parameter uncertainty. As suggested by Vrugt et al. (2007) uncertainty of predictions

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also depends on the inadequate or incomplete representation of processes which could be illustrated by the differences in nitrogen cycling conceptualisations (see Breuer et al., 2008). Moreover we demonstrated that more complex tools based on a more detailed description of processes (e.g. SWAT in comparison of LASCAM and LASCAM-S) were not necessarily better as already highlighted by Abrahart et al. (2002) in the frame of another data-fusion comparison project.

A good match of observed and simulated N loads is not necessarily required to achieve good  $R^2$  values. Selecting the best single runs regarding this criterion is therefore probably source of a large predictive uncertainty. Abrahart et al. (2002) demonstrated that the most efficient data fusion scheme depended on the application case. Here and as already depicted by Viney et al. (2009) and for our hydrological results, UR and CR regression ensembles created in a calibration context gave the best results for our SMEs and MMEs. However, this was only true when merging the predictions showing the highest values for the  $R^2$  criterion even while the RMSE values were very high. Different well trended realisations were weighted in an optimal way to adjust the predicted absolute values as illustrated by some strong decrease of the RMSE values (e.g. around 90% for  $\text{NH}_4$  and Tot-N with SWAT at Vattholma; Table 4). The risk of unrealistic values when extrapolating the coefficients obtained with monthly measurements remained very high. The ME, WM and MD schemes still gave worse predictions (usually around the RMSE value of the best single run). Viney et al. (2009) also demonstrated that that in the LUCHEM project the multiple linear regression predictions quality was significantly reduced between calibration and validation periods contrary to most of the utilised schemes (including the simplest mean ones).

MME results always showed the best overall model performances for both criteria. This confirmed the benefits of exploring different model structures as already suggested by Butts et al. (2004) for hydrological predictions. The different scatter plots of the Fig. 5 showed that the predictions of the best MME were always surrounded by the predictions of the introduced SMEs. For instance the predictions corresponding to the highest estimated N load export always showed a great deviation from the line

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symbolising the perfect fit for the different SMEs, especially for Tot-N at Savja. In this latter case, the best MME gave a good prediction for the extreme value. It is a confirmation of the advantage of combining the different model structures and getting a part of the information about the system into each of these conceptualisations. Nevertheless the improvements were not very high compared to those of the SMEs. This could be mainly attributable to the already good performances of the best selected SMEs, as there was only limited space for further improvement of the overall model performance. Moreover, as measurements and the method to estimate the loads were already sources of uncertainty, it would not be reasonable to trust a perfect fit as well.

Constructing MMEs from the best single runs, or from calibrated runs, rather than the SME could have been another way to take the global prediction uncertainty linked to the full set of considered models into account while introducing worse predictors and probably a higher uncertainty. Other methods could also have been applied like Bayesian model averaging and Kalman filtering techniques which provided more accurate results and allowed a more reliable treatment of conceptual errors in some other hydrological and climatic studies (Raftery et al., 2005; Vrugt et al., 2006; Vrugt and Robinson, 2007).

## 5 Conclusions

A total of 2490 ensembles (SMEs and MMEs) were compiled. In every studied situation numerous combination schemes showed improvements compared to the performance of their single members. For all the studied fluxes, regression schemes were the most efficient combinations but need, as well as the adopted weighted average, comparison with observed data. This could not be applicable in ungauged conditions for instance. Data-fusion procedures have been demonstrated to greatly improve the prediction of different N fluxes at the mesoscale.

This first step in multi-model nutrient predictions let us see further research direction in this domain. Of course more data-fusion schemes should be used but we could

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also analyse ensembles directly in a probabilistic way to assess the risk of occurrence of certain particular events (e.g. concentration thresholds). However, even if lots of rainfall-runoff models exist, only are able to simulate N mobilisation and transport. Diversity in the considered N species is also a limiting factor and we cannot make definitive statements on the effect of ensemble modelling in that case.

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**Table 1.** Model characteristics.

Model	Smallest spatial unit	Climate forcings	Outputs	N forcings
LASCAM	Sub-catchment	Daily $P$ and annual PET	$\text{NO}_3$ , $\text{NH}_4$ , Tot-N	Rainfall concentration, fertilizer application
LASCAM-S	Sub-catchment	Daily $P$ and $T$ , annual PET	$\text{NO}_3$ , $\text{NH}_4$ , Tot-N	Rainfall concentration, fertilizer application
CHIMP	Land-Use	Daily $P$ , $T$ and PET	$\text{NO}_3$ , $\text{NH}_4$	Wet and dry deposition, fertilizer application, STP effluents
SWAT	HRU	Daily $P$ , maximal and minimal daily $T$	$\text{NO}_3$ , $\text{NO}_2$ , $\text{NH}_4$ , Organic-N	Rainfall concentration, fertilizer application, STP effluents
HBV-N-D	Grid cell	Daily $P$ and $T$ , monthly PET	Tot-N	Rainfall concentration, leaching coefficients, STP effluents

HRU: Hydrological Response Unit, Unique combination of a land-use with a soil type,  $P$ : Precipitation,  $T$ : Temperature, PET: Potential Evapotranspiration, STP: Sewage Treatment Plant.

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**Table 2.** Overview of the adopted merging schemes for ensemble generation.

Merging scheme	Description	Abbreviation
Mean	Daily mean of the predictions	ME
Weighted mean	Daily weighted mean of the predictions. <sup>a</sup>	WM
Median	Daily median value of the prediction	MD
Unconstrained multiple linear regression	Observations are used as dependent variables while predictions are used as independent ones.	UR
Constrained multiple linear regression	Same as above with an interception constrained through the origin	CR

<sup>a</sup> Weights are set at the objective function value for  $R^2$ , but its inverse for RMSE.

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**Table 3.** Goodness-of-fit indicators of calibrated models runs for daily runoff prediction (best achieved values are highlighted in bold).

Model	Vattholma		Sävja	
	NSE	Bias (%)	NSE	Bias (%)
LASCAM	0.48	+10	0.53	−11
LASCAM-S	0.65	+6	0.64	−12
CHIMP	0.67	−5	0.69	+5
SWAT	<b>0.83</b>	−13	<b>0.76</b>	+18
HBV-N-D	0.65	−5	0.76	+13

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**Table 4.** Nitrogen results summary. RMSE is expressed in g/(ha d).

Models	NO <sub>3</sub>		Vattholma NH <sub>4</sub>		Tot-N		NO <sub>3</sub>		Sävja NH <sub>4</sub>		Tot-N	
	<i>R</i> <sup>2</sup>	RMSE	<i>R</i> <sup>2</sup>	RMSE	<i>R</i> <sup>2</sup>	RMSE	<i>R</i> <sup>2</sup>	RMSE	<i>R</i> <sup>2</sup>	RMSE	<i>R</i> <sup>2</sup>	RMSE
LASCAM												
Best run <sup>a</sup>	0.53	2.09	0.24	0.37	0.57	6.34	0.66	7.95	0.51	0.66	0.65	12.38
Selected SME <sup>b</sup>	0.53	1.82	0.36	0.21	0.57	3.94	0.66	7.20	0.52	0.46	0.65	10.95
LASCAM-S												
Best run <sup>a</sup>	0.67	2.04	0.19	0.36	0.69	9.00	0.77	8.08	0.57	0.62	0.77	11.13
Selected SME <sup>b</sup>	0.67	1.45	0.23	0.23	0.08	3.25	0.69	7.13	0.63	0.41	0.77	7.47
CHIMP												
Best run <sup>a</sup>	0.38	2.61	0.44	0.31			0.38	12.43	0.53	0.72		
Selected SME <sup>b</sup>	0.42	1.89	0.45	0.20			0.34	10.3	0.55	0.44		
SWAT												
Best run <sup>a</sup>	0.68	1.75	0.32	2.89	0.84	18.49	0.84	6.70	0.16	7.84	0.82	25.45
Selected SME <sup>b</sup>	0.69	1.39	0.33	0.22	0.86	2.42	0.83	5.27	0.18	0.60	0.85	6.90
HBV-N-D												
Best run <sup>a</sup>					0.38	8.12					0.62	19.63
Selected SME <sup>b</sup>					0.69	3.64					0.80	7.88
Best MME <sup>c</sup>	0.73	1.31	0.65	0.16	0.88	2.27	0.89	4.28	0.73	0.36	0.90	5.47

<sup>a</sup> Best single model runs regarding *R*<sup>2</sup> and RMSE are not necessarily obtained with the same parameter set.

<sup>b</sup> Selected SME *R*<sup>2</sup> and RMSE values are obtained with the same ensemble chosen to be merged in MMEs.

<sup>c</sup> Best MME is characterised by the both best *R*<sup>2</sup> and RMSE values.

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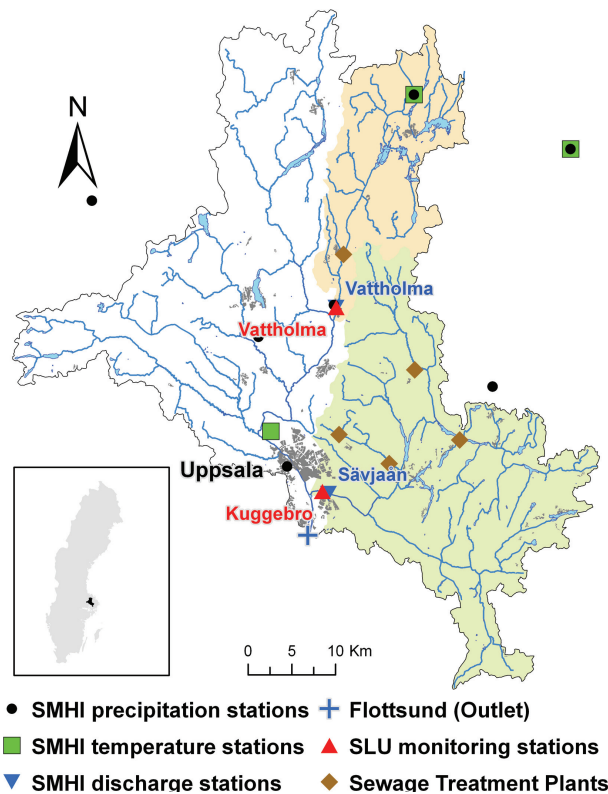
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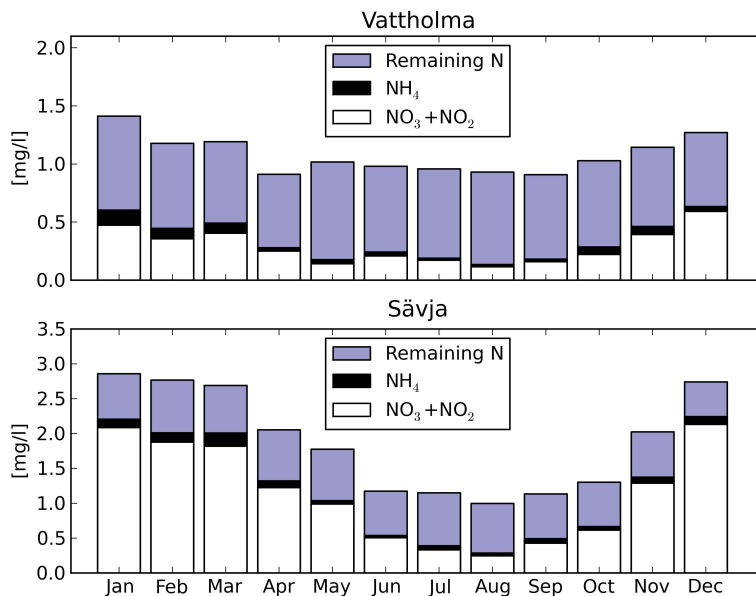
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**Fig. 1.** The River Fyris catchment (Vattholma and Sävja sub-catchments are highlighted in light-brown and light-green, respectively).

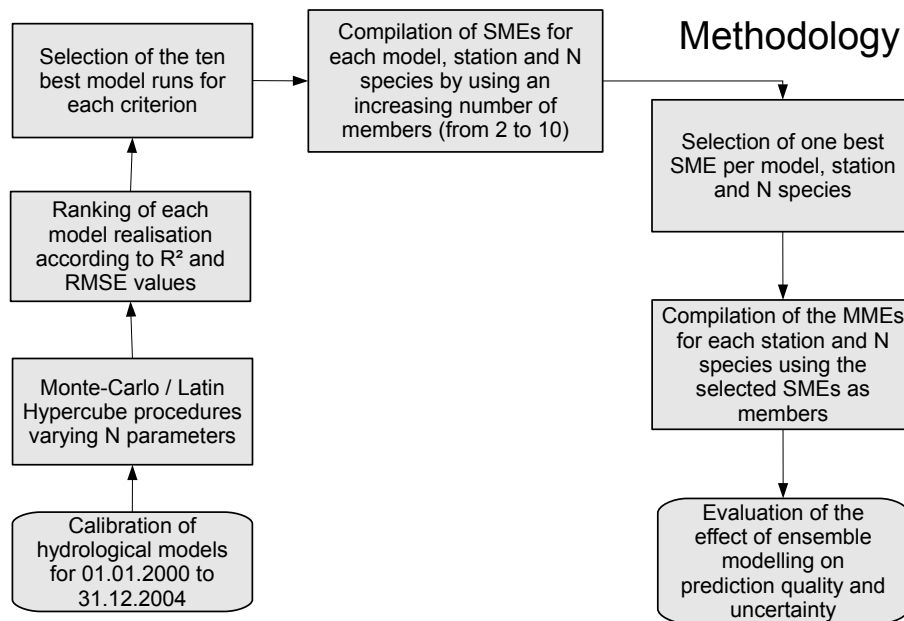
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**Fig. 2.** Average monthly concentrations of Tot-N measured at Vattholma and Sävja.

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**Fig. 3.** Methodology used in this study to compile SMEs and MMEs.

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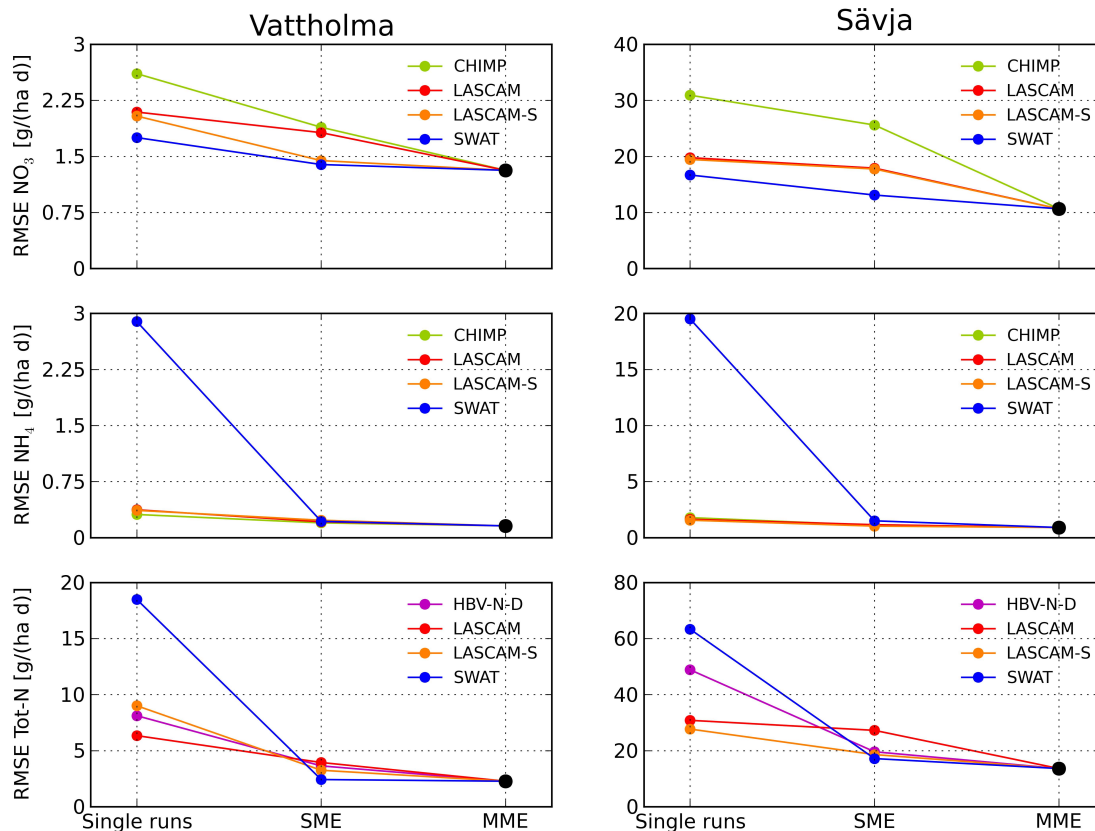
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**Fig. 4.** Evolution of the best RMSE value between single models, SMEs and MMEs (full black circle).

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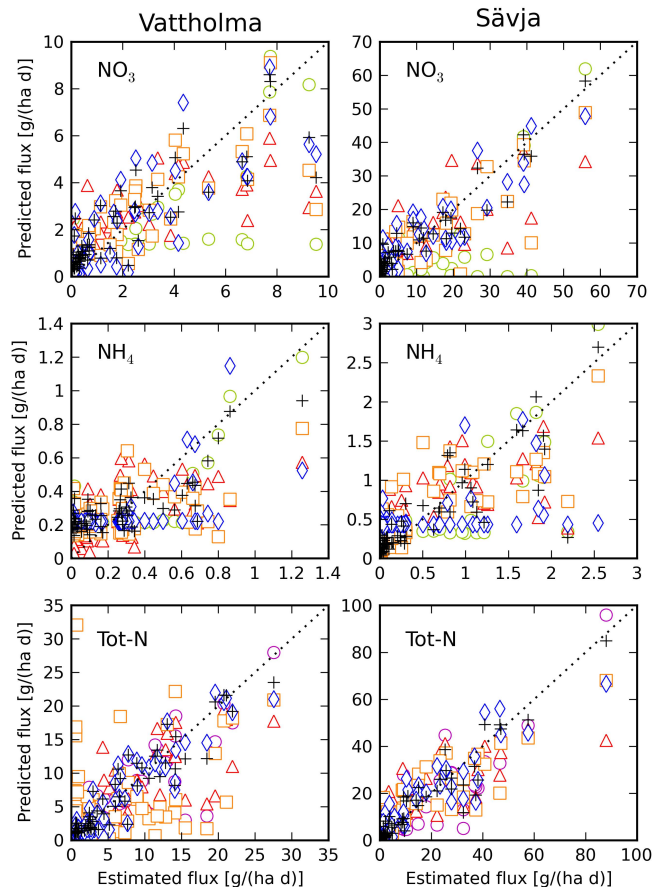
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**Fig. 5.** Estimated daily nitrogen loads (x axes, in g/(ha d)) against different prediction from the best SMEs (y axes, in g/(ha d)): CHIMP (green circles), HBV-N-D (magenta circles), LASCAM (red triangles), LASCAM-S (orange squares), SWAT (blue diamonds). Crosses represent the prediction of the best MME for each N species at each station. Corresponding criteria are summarised in Table 4.

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