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Interactive comment on "Technical Note: Linking soil – and stream-water chemistry based on a riparian flow-concentration integration model" by J. Seibert et al.

J. Seibert et al.

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We want here to directly respond to the error found in the equations by reviewer #3. First of all we thank reviewer #3 for making us aware of this obvious error in our equation. While this is an embarrassing error, luckily the error is rather a typographical mistake than a substantial error. The apparent error in equation 5 arises when replacing the profile depth z by the argument stated in equation 3. The actual error is not in equation 5 but in equation 3 where we transposed a and b.

Please see next pages for a detailed response including the equations.

C2303

Interactive comment on Hydrol. Earth Syst. Sci. Discuss., 6, 5603, 2009.

C2306

Fig. 2.

 $=ac_0\int_{Q_0}^{Q_0}\left(\frac{bQ}{a}\right)^{\frac{b+f}{b}}\cdot\left(bQ\right)^{-1}dQ$ Following the development above leads to (with a lot more intermediate steps): $L = ac_0 \int_{Q_0}^{Q} \left(\frac{bQ}{a}\right)^{\frac{b+f}{b}} \cdot \left(bQ\right)^{-1} dQ = ac_0 \int_{Q_0}^{Q} \left(\frac{b}{a}\right)^{\frac{b+f}{b}} \cdot Q^{\frac{b+f}{b}} \cdot \frac{1}{b} \cdot \frac{1}{Q} dQ$ $= \frac{a}{b}c_0 \cdot \left(\frac{b}{b}\right)^{\frac{b-f}{b}} \cdot \int_{c_0}^{c_0} \frac{b+f}{b} dQ = \frac{a}{b} \cdot \left(\frac{a}{b}\right)^{\frac{b-f}{b}} \cdot c_0 \cdot \int_{c_0}^{c_0} \frac{b-f}{b} dQ$ $= \left(\frac{a}{b}\right)^{1-\frac{b+f}{b}} \cdot c_0 \cdot \frac{b}{b+f} \cdot \left[\mathcal{Q}^{\frac{b}{b+f}}\right]_{Q_0}^{Q_1}$ This is the same as the last step of equation 5.

Equation 4 is found by forming the derivative of z by Q of equation 3: $\frac{dz}{dQ} = \frac{d\left[b^{-1}\ln\left(b_{a}^{\prime},Q\right)\right]}{dQ} = b^{-1} \cdot b_{a}^{\prime} \cdot \frac{1}{b / a \cdot Q} = \frac{1}{bQ} = (bQ)^{-1} \Rightarrow dz = (bQ)^{-1} dQ$ (4) Inserting (3) and (4) into (2) one can find (doing some additional rearrangement steps here) the third step as it is in the article: $L = ac_0^2 \int_{Z_0}^{Q} e^{(b+f)z} dz = ac_0^2 \int_{Q_0}^{Q} e^{(b+f)z^{-1} \ln(b/wQ)} \cdot (bQ)^{-1} dQ = ac_0^2 \left(e^{\ln(b/wQ)} \right)^{\frac{b+f}{b}} \cdot (bQ)^{-1} dQ$

 $z = b^{-1} \ln \left(\frac{b}{a} \cdot Q \right)$ (3.correct) (This is how equation 3 should have looked in the first place)

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Fig. 1.

 $Q = \int q du = \int a \cdot e^{bu} du = \frac{a}{b} \cdot e^{bz}$ Expressing z as a function of Q results in

 \boldsymbol{Q} is linked to \boldsymbol{q} and \boldsymbol{z} (with the lower integration limit being minus infinity) by

 $q = a \cdot e^{b_c}$

The water flux at a certain depth z is

We will of course correct Equation 3 and make the above change in the revised manuscript. Below is a more detailed derivation that we undertook to recheck the equations. Please see the article for explanations of the variables and for the assumptions behind the individual steps in the derivation below.

Equation 3 implies a lower integration limit of minus infinity ($Z_{a} \rightarrow -\infty$). This did not cause any error in the end because after deriving Eq. 5 the lower integration bound was set to $Z_{a} \rightarrow -\infty$ (and thus $Q_{b}=0$) anyway. However, to make the derivation presented in the manuscript consistent, this lower integration bound should be defined earlier (i.e. prior to the development of equations 3, 4 and 5).

Inserting the correct expression for z from equation 3 into equation 2 results in the sequence of steps outlined in equation 5. Equation 5 and all following equations are thus correct and it is equation 3 (and the authors) that are to blame.

The correct version of equation 3 is $z = b^{-1} \ln \left(\frac{bQ}{a} \right)$ (3.correct)

Equation 3 was erroneously written as $z = b^{-1} \ln \left(\frac{aQ}{b} \right)$ (3.erronous)

We want here to directly respond to the error found in the equations by reviewer #3. First of all we thank reviewer #3 for making us aware of this obvious error in our equation. While this is an embarrassing error, luckily the error is rather at ypographical mistake than a substantial error. The apparent error in equation 5 arises when replacing the profile depth z by the argument stated in equation 5. The actual error is not in equation 5 but in equation 5 where we transposed a and b.