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A look at the links between drainage density and flood statistics

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Abstract

We investigate the links between the drainage density of a river basin and selected flood statistics, namely the mean, standard deviation, coefficient of variation and coefficient of skewness of annual maximum series of peak flows. The investigation is carried out through a three-stage analysis. First, a numerical simulation is performed by using a spatially distributed hydrological model in order to highlight how flood statistics change with varying drainage density. Second, a conceptual hydrological model is used in order to analytically derive the dependence of flood statistics on drainage density. Third, the dependence between flood statistics and drainage density is analysed for 44 watersheds located in northern Italy. The three-level analysis seems to suggest that a critical value of the drainage density exists for which a minimum is attained in both the coefficient of variation and the absolute value of the skewness coefficient. Such minima in the flood statistics correspond to a minimum of the flood quantile for a given exceedance probability (i.e., recurrence interval). Therefore, the results of this study may provide useful indications for flood risk assessment in ungauged basins.

1 Introduction

Drainage density (D_d) was defined by Horton (1945) as the ratio of the total length of streams in a watershed over its contributing area. It describes the degree of drainage network development and was recognised by many authors to be significantly effective on the formation of the flood flows (see, for instance, Gardiner and Gregory, 1982). D_d is higher in arid areas with sparse vegetation cover and increases with increasing probability of heavy rainstorms (Gregory, 1976; Woodyer and Brookfield, 1966). D_d is higher in highly branched drainage basins with a relatively rapid hydrologic response (Melton, 1957).

The scientific literature proposed numerous contributions dealing with the links between D_d , geomorphological behaviors of the basin, climate and river runoff regime

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(see, for instance, Morgan, 1976; Gurnell, 1978; Rodriguez-Iturbe and Escobar, 1982). In our view, significant contributions within this respect were provided by Murphey et al. (1977) who analysed the relationship among flood hydrograph characteristics, like rise time, base time, mean peak discharge and flood volume, and basin parameters such as, among the others, contributing area and drainage density. Plaut Berger and Entekhabi (2001) and Humbert (1990) proved that drainage density is significantly related to the basin runoff coefficient. Gresillon (1997) studied 100 African catchments and concluded that D_d and watershed area are two very important variables to explain the shape of the recessing limb of the hydrograph, while in tropical regions D_d is effective on the runoff coefficient during flood events. Yildiz (2004) carried out a numerical simulation showing that streamflows simulated by a rainfall-runoff model steadily increase with increasing D_d . Recently, Grauso et al. (2008) showed that D_d is a fundamental explanatory variable in regression models for estimating the annual amount of suspended sediment yield. The explaining capability of D_d was found to be extremely relevant, therefore suggesting that a significant link exists between D_d and the river flow regime. A recent and interesting review is provided by Wharton (1994) who studied the usefulness of D_d in rainfall-runoff modelling and runoff prediction.

Nowadays, there is an increasing interest in the potential role of geomorphic parameters to effectively describe and represent some peculiar behaviours of the rainfall-runoff transformation. Such interest is motivated by the increasing attention that the hydrologic community is dedicating to the problem of prediction in ungauged basins (PUB). In fact, many researchers are involved in the activity of the PUB initiative, which was launched in 2003 by the International Association of Hydrological Sciences (Sivapalan et al., 2003). Furthermore, the continuous development of remote sensing techniques makes the estimation of a number of geomorphic parameters more accessible (Jena and Tiwari, 2006).

Within the context of PUB, it is extremely important to investigate the potential utility of geomorphic parameters in the identification and calibration of hydrological models. Such parameters can be useful “hydrological signatures”, that is, large scale markers of

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intrinsic local scale hydrological processes. While the connection between geomorphic parameters and river runoff regime has long been recognised (see the brief review presented above), expressing such link in a quantitative form is still an open problem.

The analysis presented here aims at shedding more light on the links between drainage density and streamflow regime. In fact, we believe the topology of the river network is potentially able to convey much more information than what is currently known about the formation of the river flows. In particular, the present analysis focuses on the potential interrelationships between D_d , the mean (μ), the coefficient of variation (CV) and the coefficient of skewness (k) of the annual maximum peak flow. Given that μ , CV and k summarise the frequency regime of flood flows, the possibility to derive indications about their value in ungauged basins from catchment and river network descriptors (such as D_d) is extremely important in the context of PUB.

A major problem that limits the possibility to assess the dependence of flood statistics on D_d is the scarcity of historical data that makes the estimation of the statistics themselves highly uncertain. Moreover, a lot of additional forcings, other than D_d , are effective on the rainfall-runoff transformation, like the climate, the geology of the contributing area, the presence of preferential flow and many others. Therefore, the main objective of our study, i.e. assessing the explanatory capability of D_d , is a difficult task which is complicated by the presence of a significant noise. Ideally, we would like to assess under the same climatic conditions how the flood frequency regime of a given basin changes when changing the D_d . This is clearly not possible when dealing with real world case studies, for which D_d , as well as the flood frequency regime, is a direct expression of all forcings (e.g., climatic, geological, etc.) that characterise a given catchment.

To overcome the above problem, we first focus on an ideal case study of a river basin for which we generate arbitrarily long time series of synthetic river flow data. We perform many different simulations for different values of D_d , while keeping all other forcings unchanged. This first numerical study enables us to obtain a first indication on the pattern of flood statistics depending on D_d and points out the possible existence

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of an optimal value of D_d for which the minimum CV and k are attained. To elaborate a sound physical interpretation of this result, we provide an analytical derivation of the relationship between D_d and CV . The analytical derivation is based upon a number of simplifying assumptions, but proves indeed that (1) the pattern of CV that emerges from the numerical study is feasible and (2) an optimal value of D_d exists under certain hypotheses. Finally, we assess and discuss the results obtained through the simulation study against empirical evidences for a set of river basins located in northern Italy.

We believe that recognising the pattern of the D_d – CV and D_d – k relationships is an important issue. In fact, if such a patterns were known, and the critical value for D_d was confirmed and quantified, one could estimate to what extent a river basin is prone to extreme floods on the basis of its drainage density. Our study is not conclusive in defining such a pattern in a quantitative way, but provides a first indication about its possible shape.

2 Links between the drainage density and flood statistics – a numerical simulation through a spatially distributed rainfall-runoff model

The links between the drainage density and the statistics of the annual maximum peak flows is first inspected through a numerical simulation. With reference to the Riarbero River basin, which is a right tributary to the Secchia River (Italy), we simulate many 100-year long time series of hourly river flows for varying D_d , while keeping all the other external forcings and model parameters constant. River flow simulation is carried out by using a spatially distributed rainfall-runoff model, while the meteorological input is obtained by generating synthetic rainfall and temperature series at hourly time scale.

The rainfall-runoff model applied here is AFFDEF (Moretti and Montanari, 2007). It determines the catchment hydrologic response by composing the two processes of hillslope runoff and channel propagation along the river network. A description of the structure of the model is provided in the Appendix.

AFFDEF has been calibrated for the Riarbero River basin during a previous study

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(see Moretti and Montanari, 2008). For performing the hydrological simulation, a 100-year hourly rainfall time series for the Riarbero River basin was firstly generated by using the Neyman-Scott rectangular pulses model. The model represents the total rainfall intensity at time t as the sum of the intensities given by a random sequence of rain cells active at time t . Extensive details about the model and the simulation we performed can be found in Cowpertwait (1996), Rodriguez-Iturbe et al. (1987), Burlando (1989) and Moretti and Montanari (2008).

Then, a 100-year record of hourly temperature data was generated by using a stochastic model, namely, a fractionally differenced ARIMA model (FARIMA). This kind of model has been shown in many applications to be able to well fit the autocorrelation structure of temperature series which, for increasing lag, is very often affected by a slow decay that may suggest the presence of long term persistence. FARIMA models, which are characterised by a high flexibility in their autocorrelation structure, are capable of fitting long term persistence by means of the fractional differencing operator. More details on FARIMA models and the simulation procedure herein applied for the temperature data can be found in Montanari (2003) and Montanari et al. (1997).

The synthetic rainfall and temperature data have been subsequently routed through AFFDEF, therefore obtaining a 100-year long sequence of river flows referred to Riarbero River outlet. The simulation was performed for different values of A_0 and therefore different D_d values, while keeping any other forcing unchanged. In particular, the D_d values were computed as the ratio between the total length of the river network and the drainage area. The total length of the river networks depends on A_0 and was automatically retrieved from a Digital Elevation Model (DEM) of the catchment as described in the Appendix. Then, for each simulation (i.e., each D_d value) we extracted the annual maximum river flows and computed the sample values of the following statistics: μ , σ , CV and k .

Figure 1 shows the patterns of μ , σ , CV and k depending on D_d . The results show that μ and σ increase for increasing D_d . This outcome was expected, because D_d significantly affects the concentration time. As a matter of fact, the surface flow is much

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slower on the hillslopes than in the river network and therefore higher D_d values imply lower concentration times, which in turn imply amplified peak river flows because of the fast response of the catchment.

A more interesting result is obtained by looking at the patterns of CV and k . In fact, the simulation provided by AFFDEF supports the existence of an optimal value of D_d for which a minimum is attained for the above statistics. This outcome has a significant implication: the optimal value of D_d would correspond to a situation for which the river basin is less prone to heavy floods, while significant departures from the optimum would be signatures of a higher flood risk.

Of course the numerical simulation is affected by uncertainty and therefore its outcome may not be fully representative of what actually occurs in nature. Therefore one may wonder whether or not the patterns found for CV and k are realistic. In order to better investigate the possible physical explanations for the critical value of D_d we carried out an analytical derivation of the D_d – CV relationship, that is presented in the following Section.

3 Analytical analysis of the links between the drainage density and flood statistics – a conceptual approach

The statistics of the flood flows can be analytically computed by means of a derived distribution approach. This analysis is meaningful in order to confirm and better understand the patterns highlighted by the numerical simulation. In order to make the analytical computation possible, simplifying assumptions need to be introduced in the schematisation of the rainfall-runoff transformation.

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3.1 Conceptualisation of the processes leading to the formation of flood flows

3.1.1 Gross rainfall

We assume that the extreme mean areal gross rainfall intensity r_I is constant during the storm event and is described by a scale-invariant intensity-duration-frequency (IDF) curve of the type $r_I = a(T)d^{n-1}$, where n is fixed, $a(T)$ is a coefficient that depends on the return period T and d is the storm duration. For more details about scale invariant IDF curves see Burlando and Rosso (1996). It is also assumed that $a(T)$ is distributed accordingly to a Gumbel probability distribution (Kottegoda and Rosso, 1998) and therefore can be estimated through the relationship

$$a(T) = \mu^* - 0.453\sigma^* - \frac{\sigma^*}{1.283} \log \left[-\log \frac{T-1}{T} \right], \quad (1)$$

where μ^* and σ^* are mean and standard deviation of the annual maximum rainfall for storm duration of one hour (Burlando and Rosso, 1996).

3.1.2 Net rainfall

It is assumed that the mean areal net rainfall intensity can be estimated as

$$r = r_I - r_p \quad (2)$$

where r_p is the mean areal intensity of rainfall losses during the storm. We adopted Horton's equation for infiltration (Horton, 1933) to describe r_p , which reads

$$r_p = r_{p,c} + (r_{p,0} - r_{p,c})e^{-d/\epsilon}, \quad (3)$$

where $r_{p,c}$ and $r_{p,0}$ are the asymptotical and initial rainfall losses, respectively, and ϵ is a parameter.

3.1.3 Rainfall-runoff

We assume that the rainfall-runoff transformation can be schematised by using a unit hydrograph rainfall-runoff model. Accordingly, under the assumption of constant rainfall introduced above, the flood hydrograph can be estimated through the linear relationship

$$Q(t) = rA \int_{t_0}^t h(t - \tau) d\tau \quad (4)$$

where t_0 is the initial time of the hydrograph, A is the drainage area and $h(t - \tau)$ is the travel time distribution of the catchment, which is supposed to be a stationary function of time. Let us denote with t_c the concentration time of the catchment. We assume that the travel time distribution can be written in the form

$$h(t) = \begin{cases} 0 & \text{if } t < t_0 \\ c & \text{if } t_0 < t < t_c \\ 0 & \text{if } t > t_c \end{cases} \quad (5)$$

where c is a constant parameter.

3.1.4 Computation of the annual maximum flood statistics

Finally, we assume that the annual maximum flow Q_j , for the year j , is induced by a rainstorm event with return period T_j , duration $d = t_c$ and rainfall intensity r_j . Under the assumptions introduced in Sects. 3.1.1, 3.1.2 and 3.1.3, the annual maximum peak flow Q_j can be written in the form

$$Q_j = A \left[a(T_j) t_c^{n-1} - r_{p,c} - (r_{p,0} - r_{p,c}) e^{-t_c/\epsilon} \right], \quad (6)$$

while μ , σ and CV can be written as:

$$\begin{aligned}\mu &= A \left[\mu^* t_c^{n-1} - r_{p,c} - (r_{p,0} - r_{p,c}) e^{-t_c/\epsilon} \right] \\ \sigma &= A t_c^{n-1} \sigma^* \\ CV &= \frac{\sigma^* t_c^{n-1}}{\mu^* t_c^{n-1} - r_{p,c} - (r_{p,0} - r_{p,c}) e^{-t_c/\epsilon}}\end{aligned}\quad (7)$$

3.1.5 Link between the annual maximum flood statistics and the drainage density

We suppose that the main impact of D_d on the frequency regime of annual maximum flood, summarised by the statistics computed in Sect. 3.1.4, is due to its monotonically decreasing relationship with the concentration time t_c of the catchment. We assume this relationship to be linear and expressed by

$$D_d = \frac{M}{A t_c}, \quad (8)$$

where M is constant.

3.2 Results of the analytical computation

For the sake of providing an example of the analytically derived relationships $D_d - \mu$, $D_d - \sigma$ and $D_d - CV$, let us assign the following values to the parameters of the conceptual model introduced above:

- $\mu^* = 30$ mm;
- $\sigma^* = 10$ mm;
- $A = 10$ km²;
- $M = 40$ km s;
- $r_{p,0} = 20$ mm/h;

- $r_{p,c} = 3 \text{ mm/h}$;
- $\epsilon = 0.8 \text{ s}$;
- $n = 0.6$;
- $t_c = [1, 10] \text{ h}$.

5 Figure 2 shows the patterns of μ , σ and CV depending on D_d that were derived through the conceptual approach. The results show that the patterns obtained through the hydrological simulation are confirmed. In particular, the analytical derivation confirms the presence of an optimal value for D_d with regard to CV .

10 Of course, the outcome of the conceptual approach is strongly affected by the underlying assumptions. In particular, it is worth noting that a non-linear relationship between D_d and t_c (Eq. 8) would affect the patterns in Fig. 2. Nevertheless, the monotonically decreasing relationship between D_d and t_c assures the existence of an optimal D_d regardless the assumption of linearity. Therefore, the hypothesis of a linear relationship between D_d and t_c could be relaxed and still an optimal D_d could be found under the
15 adopted assumptions.

Furthermore, it is interesting to note that the simple conceptual model that was used to perform the analytical derivation, with the parameters given above, would have provided a constant value of $CV=0.333$ over an arbitrary range of drainage densities if the rainfall losses were neglected. The adoption of Horton's equation for explaining
20 the losses along with the other simplifying assumptions mentioned above result in the presence of the optimal value of D_d .

Finally, it is important to observe that the analytical model described above, in view of its linear structure, leads to obtaining $k=k^*$ for any value of D_d , where k^* is the skewness of the annual maximum rainfall corresponding to storm duration of one hour.
25 Therefore, the analytical model cannot explain the pattern simulated by AFFDEF for the third order moment. In fact, there are many possible reasons for the presence of a critical value of D_d with respect to k , that nevertheless imply relaxing some of the

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assumptions underlying the conceptual framework introduced above, with the consequence that an analytical derivation could no longer be possible. For instance, if one keeps the assumption of linear rainfall-runoff model, the variations of k depending on the drainage density could be explained by an analogous variation of k^* over different storm durations, which would imply relaxing the assumption of scale-invariant rainfall. A non-linear rainfall-runoff transformation, or the presence of a complex infiltration pattern could be other possible explanations. It is likely that in the AFFDEF simulation a combination of causes interact to induce what was detected for both CV and k .

4 Links between the drainage density and flood statistics – case studies

The patterns identified for the D_d-CV and D_d-k relationships are displayed by the outcome of mathematical models that are based on assumptions that were described in detail above. Although the models are based on reasonable conceptualisations, their output is affected by a relevant uncertainty, which is induced by many causes including input uncertainty, model structural uncertainty (also induced by the underlying assumptions) and parameter uncertainty. Therefore, there is no guarantee that the identified patterns actually correspond to what can be observed in the real world.

The analysis so far described has been performed through mathematical models in view of the aforementioned impossibility to study the dependence of the hydrological response on the drainage density for a real world watershed. However, an analysis of real world data can be carried out by considering different watersheds characterised by different drainage densities. We believe that this type of analysis is necessary in order to provide a consistent support to what has been previously found.

However, the real world analysis is affected by a relevant uncertainty as well, because different catchments have not only different drainage densities, but also different climate, geomorphology and so forth. Therefore the patterns induced by the drainage density could be masked by patterns induced by the additional forcings mentioned above. Thus, we expect that the patterns obtained through the real world analysis are

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affected by a significant scattering of the empirical data, which may make the interpretation of the results difficult and to some extent subjective. We do not expect a clear confirmation of the previous outcomes, but at least a result allowing us not to reject their plausibility. In order to limit the ambiguity induced by the additional forcings, it is important to focus on catchment with similar behaviours.

4.1 The study area and data set

We focus on 44 subcatchments of the Po River basin. The Po river flows in northern Italy, with a contributing area of about 70 000 km². The main stream is about 652 km long. The mean discharge at its mouth is around 1560 m³/s while the mean annual inflow into the Adriatic sea is around 47 billions m³. The river regime in the alpine part of the watershed is sensitive to temperature, with an important contribution by snowmelt to runoff during summer. For the tributaries from the Apennines, rainfall is the most significant contribution to river runoff. Mean annual rainfall over the Po river watershed is around 1200 mm/y, with minimum and maximum values around 600–800 mm/y and 1600–1800 mm/y, respectively. The rainfall regime is predominantly continental over the Alpine portion of the basin, with a maximum during summer and a minimum during winter. The remaining portion of the basin is mainly characterized by two rainfall maxima in Spring and Autumn (Autorità di Bacino del Fiume Po, 1986).

Annual maximum series (AMS) of river flows are available for the considered 44 catchments for the period between 1918 and 1970. These data were collected by the Italian Hydrometric Service. The series are affected by missing values, so that the sample size of the AMS ranges between 8 and 44, with an average size of 23. For each series the sample mean, standard deviation, CV and k were computed.

4.2 Computation of the drainage density

For the 44 considered catchments, D_d is calculated as the ratio between the total length of the stream network, as described by the blue lines on 1:25.000 topographic maps,

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and the drainage area of each catchment. Figure 3 shows the pattern of the computed D_d over the Po River watershed.

4.3 Results

Figure 4 shows the progression of μ , σ , CV and k depending on D_d for the considered subwatersheds of the Po River Basin. In order to aid the interpretation of the plots, a moving average (window length=9) of the statistics is also shown, along with a linear interpolation for μ and σ .

As expected, Fig. 4 shows that empirical data present a significant scattering, therefore making the interpretation of the results highly uncertain and the identification of patterns subjective. However, the linear regression and the moving average reported in the diagrams do not contradict what was inferred through the previous numerical and analytical investigations. In other words, the analysis of real world basins and their flood statistics allow us not to reject the hypothesis of the existence of a critical value of the drainage density with respect to CV and k . Although this conclusion could certainly be questioned in view of the above mentioned scatter, the practical effect of the detected critical value is evident if one looked at the progression of the dimensionless flood quantile (DFQ) depending on D_d . The DFQ is the ratio between the flood quantile and the corresponding mean value of the annual maximum peak flows. If one assumes that CV and k are given by the moving averages shown in Fig. 4, the DFQ can be easily computed by fitting a Generalised Extreme Value (GEV) distribution (Kottegoda and Rosso, 1998) to the available dimensionless flood data. The GEV distribution has been widely shown to satisfactorily reproduce the sample frequency distribution of hydrological extremes (in particular, precipitation depths and flood flows) observed in different geographical contexts around the world (see e.g., Castellarin, 2007).

Figure 5 shows the progression of the 100-year DFQ depending on the corresponding value of D_d . Indeed, it can be seen that the variation of DFQ depending on D_d is significant and certainly effective on the magnitude of the peak flows.

It is worth pointing out that one should not be surprised by the different orders of

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magnitude of the drainage density in Figs. 1, 2 and 4. In fact, D_d was estimated by using different information in each application and therefore the obtained values are not comparable.

5 Conclusions

5 Drainage density is a classical descriptor of catchment morphology which is known to control the formation of river flows. As such it may influence significantly the frequency regime of flood flows. In this study, we addressed the analysis of the relationships between drainage density and flood frequency regime by performing a numerical simulation, an analytical study based on a conceptual hydrological model and a real world investigation. We found that we cannot reject the hypothesis of the existence of a critical value of the drainage density for which a minimum is attained in the coefficient of variation and in the absolute value of the skewness coefficient for the annual maximum sequences of flood flows. This finding is relevant from a practical viewpoint. A minimum for the flood statistics mentioned above may imply a more pronounced minimum in the estimated design-flood (the flood flow associated with a given exceedance probability, or recurrence interval). Therefore drainage density could provide interesting indications about the flood risk for an ungauged river basin.

Our study is only an initial effort to understand how descriptive the drainage density is in the representation of the flood frequency regime for a given basin. For this reason we did not provide in this study any quantitative indication for identifying the critical value of the drainage density for a single ungauged basin. At this stage of our knowledge, we believe that an extended set of comparative evaluations are needed in order to gain additional insights. These further investigations should be performed for climatically and geologically homogeneous areas, at least, in order to keep unchanged the most significant forcings on the flood statistics other than the drainage density. These investigations are the subject of ongoing work.

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AFFDEF: a spatially distributed rainfall-runoff model

AFFDEF discretises the basin in square cells coinciding with the pixels of the Digital Elevation Model (DEM). The river network is automatically extracted from the DEM itself by applying the D-8 method (Band, 1986; Tarboton, 1997), which allows one to estimate the flow paths and the contributing area to each cell. In detail, the network determination is carried out by first assigning to each DEM cell a maximum slope pointer and then processing each cell in order to organise the river network. Digital pits are filled in a preprocessing step, before extracting the channel network from the DEM of the catchment. Each cell receives water from its upslope neighbours and discharges to its downslope neighbour. For cells of flow convergence, the upstream inflow hydrograph is taken as the sum of the outflow hydrographs of the neighbouring upslope cells.

Distinction between hillslope rill and network channel is based on the concept of constant critical support area (Montgomery and Foufoula-Georgiou, 1993). Accordingly, rill flow is assumed to occur in each cell where the upstream drainage area does not exceed the value of the critical support area A_0 , while channel flow occurs otherwise. The value of A_0 conditions the drainage density of the river basin. Decreasing values of A_0 induce an increase of the linear extension of the drainage network and therefore a corresponding increase of D_d .

The interaction between soil, vegetation and atmosphere is modelled by applying a conceptual approach. The model firstly computes the local gross rainfall $P_l[t, (i, j)]$, for each DEM cell of coordinates (i, j) , by interpolating the observations referred to each raingauge through an inverse distance approach. Then, for each cell a first rate of rainfall depth is accumulated in a local reservoir (interception reservoir) which simulates the interception operated by the vegetation. The capacity of such interception reservoir is equal to $C_{\text{int}}S(i, j)$, being C_{int} a parameter, constant in space and time, and $S(i, j)$

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the local storativity. The latter is computed depending on soil type and use accordingly to the Curve Number method (CN method, Soil Conservation Service, 1987; Chow et al., 1988).

Once the interception reservoir is full of water, the exceeding rainfall reaches the ground. Then, surface and subsurface flows are computed accordingly to a modified CN approach that is able to simulate the redistribution of the soil water content during interstorm periods. In detail, it is assumed that a linear reservoir (infiltration reservoir), which collects the infiltrated water, is located in correspondence of each DEM cell at the soil level. The local surface runoff and the infiltration are computed according to the relationship

$$\frac{P_n[t, (i, j)]}{P[t, (i, j)]} = \frac{F[t, (i, j)]}{H \cdot S(i, j)} \quad (A1)$$

where $P[t, (i, j)]$ is the rainfall intensity that reaches the ground at time t , $P_n[t, (i, j)]$ is the intensity of surface runoff, $F[t, (i, j)]$ is the water content at time t of the infiltration reservoir located in correspondence of the cell (i, j) , and $H \cdot S(i, j)$ is the capacity of the infiltration reservoir itself, computed by multiplying the calibration parameter H by the soil storativity previously introduced. The quantity $I[t, (i, j)] = P[t, (i, j)] - P_n[t, (i, j)]$ represents the intensity of the infiltrated water. The outflow $W[t, (i, j)]$ from the infiltration reservoir to the sub surface river network, which is assumed to coincide with the surface one, is given by the linear relationship

$$W[t, (i, j)] = \frac{F[t, (i, j)]}{H_S} \quad (A2)$$

where H_S is a calibration parameter. H and H_S are assumed to be constant with respect to both space and time.

The hourly intensity of potential evapotranspiration $E_P[t, (i, j)]$ is computed at local scale by applying the radiation method (Doorenbos et al., 1984). When some water is stored in the interception reservoir, the effective evapotranspiration $E[t, (i, j)]$ is assumed to be equal to $E_P[t, (i, j)]$ and is subtracted from the water content of the

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interception reservoir itself. When this latter is empty, or is emptied while subtracting the evapotranspiration rate, the remaining part of $E_p[t, (i, j)]$ is subtracted from the water content of the infiltration reservoir. In this case, it is assumed that $E[t, (i, j)]$ is varying linearly from 0 when $F[t, (i, j)] = 0$, to $E_p[t, (i, j)]$ when $F[t, (i, j)] = H \cdot S(i, j)$.

Evapotranspiration is the only source of water losses in the model, which primarily depends on the capacity of the interception reservoir and hence on the parameter C_{int} . Therefore a first estimation of C_{int} can be obtained by comparing observed and simulated runoff coefficients. Figure A1 shows the scheme of the interaction among soil, vegetation and atmosphere operated by the model.

The continuity equation applied to the infiltration reservoir can be written as:

$$I[t, (i, j)] - W[t, (i, j)] = \frac{dF[t, (i, j)]}{dt}. \quad (A3)$$

By combining Eqs. (A1), (A2) and (A3) and taking the effective evapotranspiration into account, the mass balance equation for the infiltration reservoir can be derived and written in the form

$$\frac{dF[t, (i, j)]}{dt} = -\frac{F[t, (i, j)]}{H_S} - E[t, (i, j)] + P[t, (i, j)] \left\{ 1 - \frac{F[t, (i, j)]}{H \cdot S(i, j)} \right\}. \quad (A4)$$

Surface and sub surface flows are propagated towards the basin outlet by applying the variable parameters Muskingum-Cunge model. Extensive details can be found in Cunge (1969) and Orlandini et al. (1999) for surface and sub surface propagation, respectively. For the surface flow, the kinematic celerity is computed by considering rectangular river cross section with fixed width/height ratio. The latter parameter and the channel roughness can assume different values along the river network and on the hillslopes. In particular, the channel roughness in the river network is allowed to vary from a minimum to a maximum value depending on the contributing area. For

the subsurface flows, the kinematic celerity is instead computed as a function of the saturated hydraulic conductivity of the soil.

It is interesting to note that the model describes in a simplified manner the dynamics of the sub surface flows. In particular, it does not distinguish between near surface and deep water flow, and assumes that the calibration parameters H and H_S are constant with respect to both space and time. This simplified description has been used in order to reduce the number of model parameters and, consequently, the amount of historical data required for model calibration. On the other hand, one may expect a significant approximation in the simulation of the low river discharges, especially when referring to highly permeable basins.

Moreover, the formation of the surface runoff is modelled accordingly to a scheme that is very similar to the one adopted by the CN method, which is considered by many authors as an infiltration excess approach (Beven, 2000). Therefore one may expect that the proposed model is better suited for basins characterised by low permeability and prevalently impervious hillslope, where the surface runoff is more likely to be given by excess of infiltration instead of excess of saturation.

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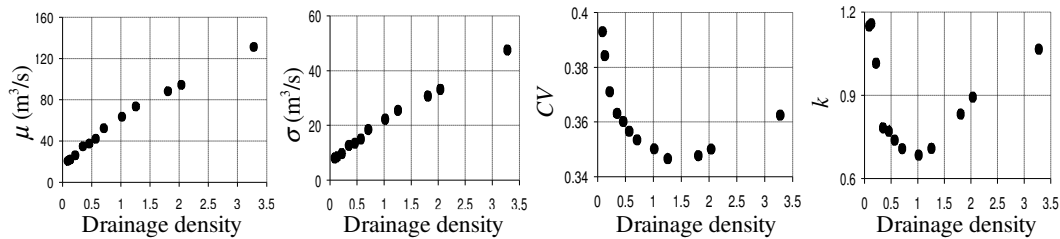


Fig. 1. Progression of μ , σ and CV depending on D_d for the numerical simulation obtained through the AFFDEF rainfall-runoff model.

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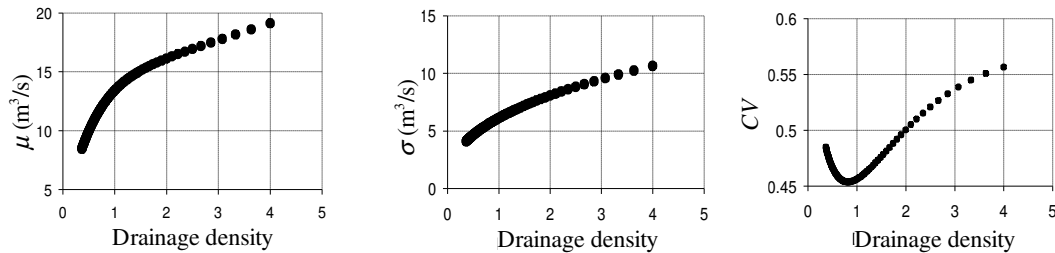


Fig. 2. Progression of μ , σ , CV and k depending on D_d for the analytical derivation obtained through the conceptual model.

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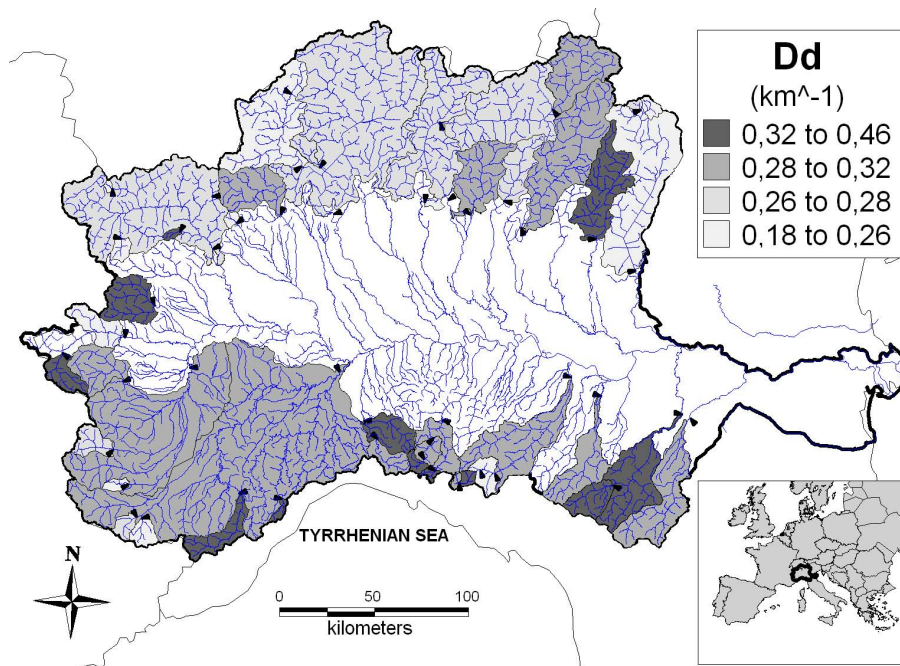


Fig. 3. Schematic map of the Po River watershed and the 44 considered subbasins, with a qualitative representation of their drainage density.

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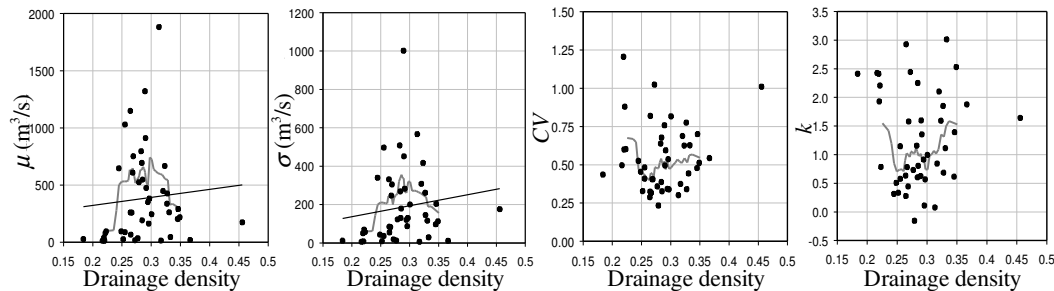


Fig. 4. Progression of μ , σ , CV and k depending on D_d for the considered subwatersheds of the Po River Basin.

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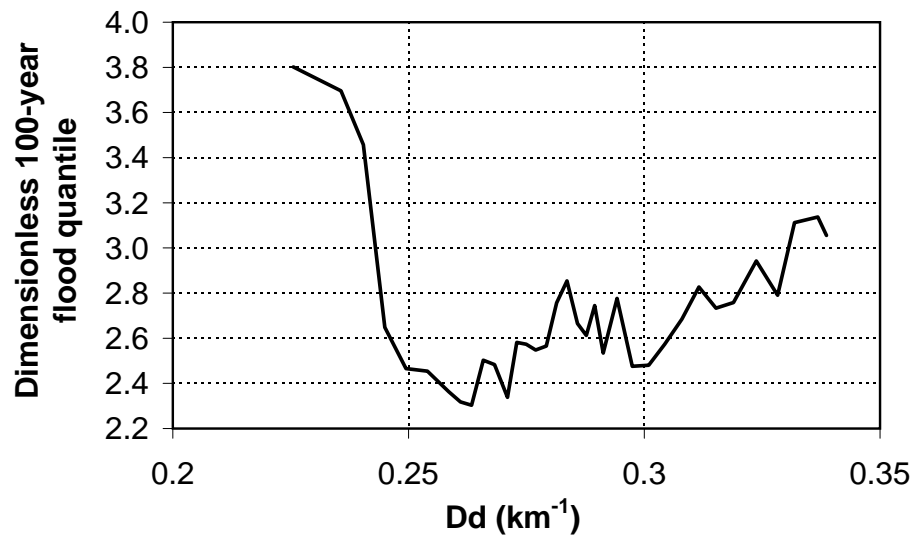


Fig. 5. 100-year dimensionless flood quantile against the corresponding value of D_d .

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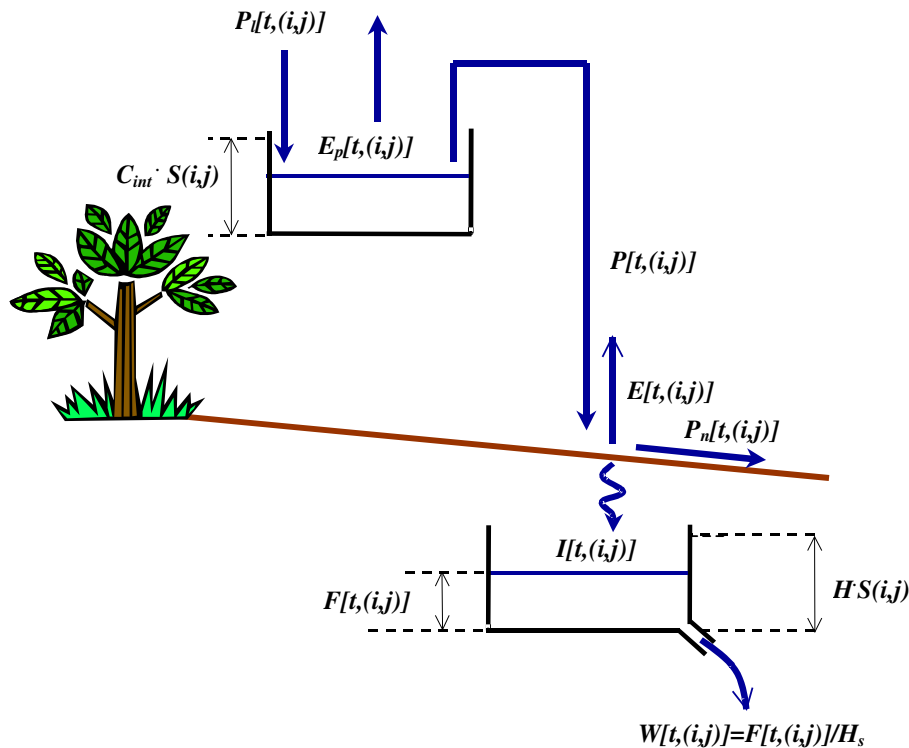


Fig. A1. Schematisation operated by the AFFDEF model of the interaction among soil, vegetation and atmosphere.

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