- 1 Uniform flow formulas for irregular sections in straight channels
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#### 24 ABSTRACT

Two new methods for uniform flow discharge computation are presented, validated 25 26 and compared with other available formulas. The first method derives from the well-27 known Huthoff algorithm, which is first shown to be dependent on the way the river cross-section is discretized into several sub-sections. The second method assumes the 28 29 vertically averaged longitudinal velocity to be a function only of the friction factor and of the so-called "local hydraulic radius", computed as the ratio between the 30 31 integral of the elementary areas around a given vertical and the integral of the elementary solid boundaries around the same vertical. Both integrals are weighted 32 33 with a linear shape function, equal to zero at a distance from the integration variable which is proportional to the water depth according to an empirical coefficient  $\beta$ . Both 34 formulas are validated against 1) laboratory experimental data, 2) discharge 35 hydrographs measured in a real site, where the friction factor is estimated from an 36 37 unsteady-state analysis of water levels recorded in two different river cross sections, 38 3) the 3D solution obtained using the commercial ANSYS CFX code, computing the steady state uniform flow in a short reach of a prismatic channel, with known water 39 40 level in the downstream section.

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*Keywords*: diffusive model, discharge estimation, irregular section, rating curve,
uniform flow.

## 50 **1 Introduction**

51 Both dynamic and diffusive forms of the Saint Venant equation include a closure 52 relationship linking maximum water depth inside the cross section, discharge and 53 energy slope (or thr piezometric gradient in its diffusive form). This closure 54 relationship is assumed to be the same relationship holding in the case of uniform 55 flow. For this reason, an accurate prediction of uniform flow in channels with 56 compound or irregular section is a central issue for good shallow water modeling.

The uniform flow formula almost universally applied is still the Chezy equation 57 58 (Herschel, C., 1897). The advantage of using the Chezy equation is that the associated 59 Manning's coefficient has been calibrated worldwide for several types of bed surface 60 and a single value is ready to use for each application. However, it is well known that 61 the Chezy equation was derived from laboratory measurements taken in channels with a regular, convex cross-sectional shape. When the section results from the union of 62 different parts, each with a strongly different average water depth, one of two options 63 64 is usually selected. The first option, called Single Channel Method (SCM) is simply to ignore the problem. This leads to strong underestimation of the discharge, because the 65 66 Chezy formula assumes a homogeneous vertically averaged velocity and this homogeneous value provides strong energy dissipation in the parts of the section with 67 68 lower water depths. The second option, called Divided Channel Method (DCM) is to 69 compute the total discharge as the sum of the discharges flowing in each convex part of the section (called subsection), assuming a single water level for all parts (Chow 70 1959; Shiono et al. 1999; Myers and Brennan, 1990). In this approach, the wet 71 perimeter of each subsection is restricted to the component of the original one 72 73 pertaining to the subsection, but the new components shared by each couple of 74 subsections are neglected. This is equivalent to neglecting the shear stresses coming 75 from the vortices with vertical axes (if subsections are divided by vertical lines) and 76 considering additional resistance for higher velocities, which results in overestimation 77 of discharge capacity (Lyness et al. 2001).

Knight and Hamed (1984) compared the accuracy of several subdivision methods for compound straight channels by including or excluding the vertical division line in the computation of the wetted perimeters of the main channel and the floodplains. However, their results show that conventional calculation methods result in larger errors. Wormleaton et al. (1982) and Wormleaton and Hadjipanos (1985) also

discussed, in the case of compound sections, the horizontal division through the junction point between the main channel and the floodplains. Their studies show that these subdivision methods cannot well assess the discharge in compound channels.

The interaction phenomenon in compound channels has also extensively studied by 86 87 many other researchers (e.g., Sellin 1964; Knight and Demetriou 1983; Stephenson and Kolovopoulos 1990; Rhodes and Knight 1994; Bousmar and Zech 1999; van 88 89 Prooijen et al. 2005; Moreta and Martin-Vide 2010). These studies demonstrate that 90 there is a large velocity difference between the main channel and the floodplain, especially at low relative depth, leading to a significant lateral momentum transfer. 91 The studies by Knight and Hamed (1984), Wormleaton et al. (1982) indicate that 92 93 vertical transfer of momentum between the upper and the lower main channels exists, 94 causing significant horizontal shear able to dissipate a large part of the flow energy.

95 Furthermore, many authors have tried to quantify flow interaction among the 96 subsections, at least in the case of compound, but regular channels. To this end 97 turbulent stress was modelled through the Reynolds equations and coupled with the 98 continuity equation (Shiono and Knight, 1991). This coupling leads to equations that 99 can be analytically solved only under the assumption of negligible secondary flows. 100 Approximated solutions can also be obtained, although they are based on some 101 empirical parameters. Shiono and Knight developed the Shiono-Knight Method 102 (SKM) for prediction of lateral distribution of depth-averaged velocities and boundary shear stress in prismatic compound channels (Shiono and Knight, 1991; Knight and 103 104 Shiono, 1996). The method can deal with all channel shapes that can be discretized into linear elements (Knight and Abril, 1996; Abril and Knight, 2004). 105

106 Other studies based on the Shiono and Knight method can be found in Liao and 107 Knight (2007), Rameshwaran and Sjiono (2007), Tang and Knight (2008) and Omran 108 and Knight (2010). Apart from SKM, some other methods for analysing the 109 conveyance capacity of compound channels have been proposed. For example, 110 Ackers (1993) formulated the so called empirical coherence method. Lambert and Sellin (1996) suggested a mixing length approach at the interface, whereas more 111 112 recently Cao et al. (2006) reformulated flow resistance through lateral integration using a simple and rational function of depth-averaged velocity. Bousmar and Zech 113 (1999) considered the main channel/floodplain momentum transfer proportional to the 114 product of the velocity gradient at the interface times the mass discharge exchanged 115 116 through this interface due to turbulence. This method, called EDM, also requires a geometrical exchange correction factor and turbulent exchange model coefficient forevaluating discharge.

119 A simplified version of the *EDM*, called Interactive Divided Channel Method 120 (*IDCM*), was proposed by Huthoff et al. (2008). In *IDCM* lateral momentum is 121 considered negligible and turbulent stress at the interface is assumed to be 122 proportional to the span wise kinetic energy gradient through a dimensionless 123 empirical parameter  $\alpha$ . *IDCM* has the strong advantage of using only two parameters, 124  $\alpha$  and the friction factor, *f*. Nevertheless, as shown in the next section,  $\alpha$  depends on 125 the way the original section is divided.

126 An alternative approach could be to simulate the flow structure in its complexity by 127 using a three-dimensional code for computational fluid dynamics (CFD). In these codes flow is represented both in terms of transport motion (mean flow) and 128 129 turbulence by solving the Reynolds Averaged Navier Stokes (RANS) equations 130 (Wilcox, 2006) coupled with turbulence models. These models allow closure of the 131 mathematical problem by adding a certain number of additional partial differential 132 transport equations equal to the order of the model. In the field of the simulation of 133 industrial and environmental laws second order models (e.g. k- $\varepsilon$  and k- $\omega$  models) are widely used. Nonetheless, CFD codes need a mesh fine enough to solve the boundary 134 135 layer (Wilcox, 2006), resulting in a computational cost that can be prohibitive even 136 for river of few km.

In this study two new methods, aimed to represent subsection interactions in a 137 compound channel, are presented. Both methods estimate the discharge as an integral 138 of the vertically averaged velocities. The first method, named "INtegrated Channel 139 140 Method" (INCM), derives from the previous Huthoff formula, which is shown to give results depending on the way the river cross section is discretized in sub-sections. The 141 same dynamic balance adopted by Huthoff is written in differential form, but its 142 143 diffusive term is weighted according to a  $\xi$  coefficient proportional to the local water 144 depth.

The second one, named "local hydraulic radius method" (*LHRM*), derives from the observation that, in the Manning formula, the mean velocity per unit energy gradient is proportional to a power of the hydraulic radius. It should then be possible to get the total discharge as an integral, along the span wise direction, of the elementary values computed around each vertical, using for each elementary value the Manning formula,

but also changing the original hydraulic radius with a "local" one. This "local" hydraulic radius should take into account the effect of the surrounding section geometry, up to a maximum distance which is likely to be proportional to the local water depth, according to an empirical  $\beta$  coefficient. The method gives up the idea of solving the Reynolds equations, due to the uncertainty of its parameters, but relies on the solid grounds of the historical experience of the Manning equation.

156 The present paper is organized as follows: Two of the most popular approaches 157 adopted for discharge estimation are explained in details, along with the proposed *INCM* and *LHRM* methods. The  $\xi$  and  $\beta$  parameters of respectively the *INCM* and 158 159 LHRM methods are then calibrated from available lab experimental data and a 160 sensitivity analysis is carried out. The INCM and LHRM methods are finally validated 161 according to three different criteria. The first criterion is comparison with other series 162 of the previous laboratory data, not used for calibration. The second criterion is comparison with discharge data measured in one section of the Alzette river Basin 163 164 (Luxembourg). Because the friction factor is not known a priori, INCM and LHRM formulas are applied in the context of the indirect discharge estimation method, which 165 166 simultaneously estimates the friction factor and the discharge hydrograph from the unsteady state water level analysis of two water level hydrographs measured in two 167 168 different river sections. The third validation criterion is comparison with results of a 169 3D numerical solver, applied to a small reach of the Alzette river. Conclusions follow.

# 170 2 Divided Channel Method (*DCM*) and Interactive Divided Channel 171 Method (*IDCM*)

In the *DCM* method the river section is divided into subsections with uniform velocities and roughness (Chow, 1959). Division is made by vertical lines and no interaction between adjacent subsections is considered. Discharge is obtained by summing the contributions of each subsection, obtained applying of the Manning formula:

177 
$$q = \sum_{i} q_{i} = \sum_{i} \frac{R_{i}^{2/3} A_{i}}{n_{i}} \sqrt{S_{f}}$$
(1),

where *q* is the total discharge,  $A_i$ ,  $R_i$  and  $n_i$  are the area, the hydraulic radius and the Manning's roughness coefficient of each sub section *i* of a compound channel and  $S_f$ is the energy slope of each sub section, assumed constant across the river section.

In order to model the interaction between adjacent subsections of a compound section,
the Reynolds and the continuity equations can be coupled (Shiono and Knight, 1991),
to get:

184 
$$\rho \frac{\partial}{\partial y} \left( H \overline{U}_{v} \overline{V}_{d} \right) = \rho g H S_{0} + \frac{\partial}{\partial y} \left( H \overline{\tau}_{xy} \right) - \tau_{b} \left( 1 + \frac{1}{s^{2}} \right)^{1/2}$$
(2)

185 where  $\rho$  is the water density, g is the gravity acceleration, y is the abscissa according 186 to the lateral direction, U and V are respectively the velocity components along the 187 flow x direction and the lateral y direction, H is the water depth, the sub-index d 188 marks the vertically averaged quantities and the bar the time average along the 189 turbulence period,  $S_0$  is the bed slope, s is the section lateral slope, and  $\tau_{\beta}$  is the bed 190 shear stress. The  $\overline{\tau}_{xy}$  turbulent stress is given by the eddy viscosity equation, that is:

191 
$$\overline{\tau}_{xy} = \rho \overline{\varepsilon}_{xy} \frac{\partial U_d}{\partial y}$$
 (3a),

192 
$$\bar{\varepsilon}_{xy} = \lambda U_* H$$
 (3b),

193 where the friction velocity  $U_*$  is set equal to:

194 
$$U_* = \left(\frac{f}{8g}\right)^{1/2} U_d \tag{4}$$

and f is the friction factor, depending on the bed material. The analytical solution of Eqs. (2)-(4) can be found only if the left hand side of Eq. (2) is zero, which is equivalent to neglecting secondary flows. Other solutions can only be found by assuming a known  $\Gamma$  value for the lateral derivative. Moreover,  $\lambda$  is another experimental factor depending on the section geometry. The result is that solution of Eq. (2) strongly depends on the choice of two coefficients,  $\lambda$  and  $\Gamma$ , which are additional unknowns with respect to the friction factor f.

In order to reduce to one the number of empirical parameters (in addition to *f*) Huthoff et al. (2008) proposed the so-called Interactive Divided Channel Method (*IDCM*).

Integration of Eq. (2) over each  $i^{\text{th}}$  subsection, neglecting the averaged flow lateral momentum, leads to:

206 
$$\rho g A_i S_0 = \rho f_i P_i U_i^2 + \tau_{i+1} H_{i+1} + \tau_i H_i$$
(5),

where the left-hand side of Eq.(5) is the gravitational force per unit length, proportional to the density of water  $\rho$ , to the gravity acceleration g, to the crosssectional area  $A_i$ , and to the stream wise channel slope  $S_0$ . The terms at the right-hand side are the friction forces, proportional to the friction factor f and to the wet solid boundary  $P_i$ , as well as the turbulent lateral momentum on the left and right sides, proportional to the turbulent stress  $\tau$  and to the water depth H.

213 Turbulent stresses are modelled quite simply as:

214 
$$\tau_{i+I} = \frac{1}{2} \rho \alpha \left( U_{i+I}^2 - U_i^2 \right)$$
(6),

where  $\alpha$  is a dimensionless interface coefficient,  $U_{i}^{2}$  is the square of the vertically averaged velocity and  $\tau_{i}$  is the turbulent stress along the plane between subsection *i*-1 and *i*. If subsection *i* is the first (or the last) one, velocity  $U_{i-1}$  (or  $U_{i+1}$ ) is set equal to zero.

Following a wall-resistance approach (Chow, 1959), the friction factor  $f_i$  is computed as:

221 
$$f_i = \frac{g n_i^2}{R_i^{1/3}}$$
(7).

where  $n_i$  is the Manning's roughness coefficient and  $R_i (=A_i/P_i)$  is the hydraulic radius of subsection *i*.

Equations. (5) forms a system with an order equal to the number *m* of subsections, which is linear in the  $U_i^2$  unknowns. The results are affected by the choice of the  $\alpha$ coefficient, which is recommended by Huthoff et al. (2008), on the basis of lab experiments, equal to 0.02. Computation of the velocities  $U_i$  makes it easy to estimate discharge *q*.

*IDCM* has the main advantage of using only two parameters, the f and  $\alpha$  coefficients. On the other hand, it can be easily shown that  $\alpha$ , although it is dimensionless, depends on the way the original section is divided. The reason is that the continuous form of Eq. (5) is given by:

233 
$$\rho g \left( HS_o - \frac{f U^2}{g \cos \theta} \right) = \frac{\partial}{\partial y} (\tau H)$$
(8)

where  $\theta$  is the bed slope in the lateral direction. Following the same approach as the *IDCM*, if we assume the turbulent stress  $\tau$  to be proportional to both the velocity gradient in the lateral direction and to the velocity itself, we can write the right-hand side of Eq. (8) in the form:

238 
$$\frac{\partial}{\partial y}(\tau H) = \frac{\partial}{\partial y}\left(\frac{\alpha_{H}}{2}\rho U\frac{\partial U}{\partial y}H\right)$$
(9),

and Eq. (8) becomes:

240 
$$\rho\left(gHS_{o} - \frac{fU^{2}}{g\cos\theta}\right) = \frac{\partial}{\partial y}\left(H\frac{\partial}{\partial y}\left(\alpha_{H}\rho U^{2}\right)\right)$$
(10).

In Eq. (10)  $\alpha_H$  is no longer dimensionless, but is a length. To get the same Huthoff formula from numerical discretization of Eq. (10), we should set:

$$\alpha_H = 0.02 \,\Delta y \tag{11},$$

where  $\Delta y$  is the subsection width, i.e. the integration step size. This implies that the solution of Eq. (10), according to the Huthoff formula, depends on the way the equation is discretized and the turbulence stress term on the r.h.s. vanishes along with the integration step size.

## 248 **3** The new methods

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## 249 3.1 Integrated Channel Method (INCM)

*INCM* derives from the *IDCM* idea of evaluating the turbulent stresses as proportional 250 251 to the gradient of the squared averaged velocities, leading to Eqs. (6) and (10). 252 Observe that dimensionless coefficient  $\alpha$  in the stress computation given by Eq. (6), 253 can be written as the ratio between  $\alpha_{H}$  and the distance between verticals *i* and *i*+1. 254 For this reason, coefficient  $\alpha_{H}$  can be thought of as a sort of mixing length, related to the scale of the vortices with horizontal axes. *INCM* assumes the optimal  $\alpha_{H}$  to be 255 proportional to the local water depth, because water depth is at least an upper limit for 256 257 this scale, and the following relationship is applied:

$$\alpha_H = \xi H \tag{12},$$

259 where  $\xi$  is an empirical coefficient to be further estimated.

## 260 *3.2 Local hydraulic radius method (LHRM)*

*LHRM* derives from the observation that, in the Manning equation, the average velocity is set equal to:

263 
$$V = \frac{R^{2/3}}{n} \sqrt{S_0}$$
(13),

and has a one-to-one relationship with the hydraulic radius. In this context the 264 meaning of a global parameter, measuring the interactions of the particles along all 265 the section as the ratio between an area and a length. The inconvenience is that, 266 267 according to Eq. (13), the vertically averaged velocities in points very far from each other remain linked anyway, because the infinitesimal area and the infinitesimal 268 269 length around two verticals are summed to the numerator and to the denominator of the hydraulic radius independently from the distance between the two verticals. To 270 271 avoid this, LHRM computes the discharge as an integral of the vertically averaged velocities, in the following form: 272

273 
$$q = \int_{0}^{L} h(y) U(y) dy$$
 (14),

274 where U is set equal to:

275 
$$U = \frac{\Re_{l}^{2/3}}{n} \sqrt{S_{0}}$$
(15),

and  $\mathfrak{R}_{l}$  is defined as local hydraulic radius, computed as:

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$$\Re_{i}(y) = \frac{\int_{a}^{b} h(s) N(y,s) ds}{\int_{a}^{b} N(y,s) \sqrt{ds^{2} + dz^{2}}}$$
(16a),

278

$$a = \max(0, y - \beta h) \tag{16b}$$

$$b = \min(L, y + \beta h) \tag{16c}$$

280 where z is the topographic elevation (function of s),  $\beta$  is an empirical coefficient and

281 *L* is the section top width. Moreover N(y, s) is a shape function where:

282 
$$N(y,s) = \begin{cases} -\frac{\left[y - \beta h(y)\right] - s}{\beta h(y)} & \text{if } a < s < y\\ \frac{\left[y - \beta h(y)\right] - s}{\beta h(y)} & \text{if } b > s > y\\ 0 & \text{otherwise} \end{cases}$$

283 (17).

Equations (17) show how the influence of the section geometry, far from the abscissa 284 285 y, continuously decreases up to a maximum distance, which is proportional to the water depth according to an empirical positive coefficient  $\beta$ . After numerical 286 discretization, Eqs (14)-(17) can be solved to get the unknown q, as well as the 287 288 vertically averaged velocities in each subsection. If  $\beta$  is close to zero and the size of each subsection is common to both formulas, LHRM is equivalent to DCM; if  $\beta$  is 289 very large *LHRM* is equivalent to the traditional Manning formula. In the following,  $\beta$ 290 291 is calibrated using experimental data available in the literature. A sensitivity analysis 292 is also carried out, to show that the estimated discharge is only weakly dependent on the choice of the  $\beta$  coefficient, far from its possible extreme values. 293

# 294 3.3 Evaluation of the $\xi$ and $\beta$ parameters by means of lab experimental data

INCM and LHRM parameters were calibrated by using data selected from six series 295 296 of experiments run at the large scale Flood Channel Facility (FCF) of HR Wallingford (UK), (Knight and Sellin, 1987; Shiono and Knight, 1991; Ackers, 1993), as well as 297 from four series of experiments run in the small-scale experimental apparatus of the 298 299 Civil Engineering Department at the University of Birmingham (Knight and Demetriou, 1983). The FCF series were named F1, F2, F3, F6, F8 and F10; the 300 301 Knight and Demetriou series were named K1, K2, K3 and K4. Series F1, F2, and F3 covered different floodplain widths, while series F2, F8, and F10 kept the floodplain 302 303 widths constant, but covered different main channel side slopes. Series F2 and F6 304 provided a comparison between the symmetric case of two floodplains and the 305 asymmetric case of a single floodplain. All the experiments of Knight and Demetriou (1983) were run with a vertical main channel wall, but with different B/b ratios. The 306 307 series K1 has B/b = 1 and its section is simply rectangular. The B/b ratio, for Knight's experimental apparatus, was varied by adding an adjustable side wall to each of the 308

floodplains either in pairs or singly to obtain a symmetrical or asymmetrical cross section. The geometric and hydraulic parameters are shown in Table 1; all notations of the parameters can be found in Fig. 1 and  $S_0$  is the bed slope. The subscripts "mc" and "fp" of the side slope refer to the main channel and floodplain, respectively. Perspex was used for both main flume and floodplains in all tests. The related Manning roughness is 0.01 m<sup>-1/3</sup>s.

- The experiments were run with several channel configurations, differing mainly for floodplain geometry (widths and side slopes) and main channel side slopes (see Table 1). The K series were characterised by vertical main channel walls. More information concerning the experimental setup can be found in Table 1 (Knight and Demetriou, 1983; Knight and Sellin, 1987; Shiono and Knight, 1991).
- Four series, named F1, F2, F3 and F6, were selected for calibration of the  $\beta$  coefficient, using the Nash Sutcliffe (NS) index of the measured and the computed flow rates as a measure of the model's performance (Nash and Sutcliffe, 1970).
- The remaining three series, named F2, F8 and F10, plus four series from Knight and Demetriou, named K1, K2, K3 and K4, were used for validation (no.) 1, as reported in the next section. NS is given by:

$$NS = \left[1 - \frac{\sum_{j=1,2} \sum_{i=1,N_J} \sum_{K=1,M_{N_J}} (q_{i,j,k}^{obs} - q_{i,j,k}^{sim})^2}{\sum_{j=1,2} \sum_{i=1,N_J} \sum_{K=1,M_{N_J}} (q_{i,j,k}^{obs} - \overline{q}_{i,j,k}^{obs})^2}\right]$$
(18)

where  $N_j$  is the number of series,  $M_{Nj}$  is the number of tests for each series,  $q_{i,j,k}^{ann}$  and  $q_{i,j,k}^{obs}$  are respectively the computed and the observed discharge (j = 1 for the FCF series and j = 2 for the Knight series; i is the series index and K is the water depth index).  $\overline{q_{i,j,k}^{obs}}$  is the average value of the measured discharges.

331 Both  $\xi$  and  $\beta$  parameters were calibrated by maximizing the Nash Sutcliffe (NS) 332 index, computed using all the data of the four series used for calibration. See the NS 333 versus  $\xi$  and  $\beta$  curves in Figs. 2a and 2b.

Calibration provides optimal  $\xi$  and  $\beta$  coefficients respectively equal to 0.08 and 9. The authors will show in the next sensitivity analysis that even a one-digit approximation of the  $\xi$  and  $\beta$  coefficients provides a stable discharge estimation.

## 337 3.4 Sensitivity analysis

338 We carried out a discharge sensitivity analysis of both new methods using the 339 computed  $\xi = 0.08$  and  $\beta=9$  optimal values and the data of the F2 and K4 series. 340 Sensitivities were normalized in the following form:

341 
$$I_s = \frac{1}{q_{INCM}} \frac{\Delta q}{\Delta \xi}$$
(19),

$$342 L_s = \frac{1}{q_{LHRM}} \frac{\Delta q}{\Delta \beta} (20),$$

343

where  $\Delta q$  is the difference between the discharges computed using two different  $\beta$  and  $\xi$  values. The assumed perturbations " $\Delta\beta$ " and " $\Delta\xi$ " are respectively  $\Delta\beta = 0.001 \beta$ ,  $\Delta\xi$  $= 0.001 \xi$ .

347 The results of this analysis are shown in Table 2a for the F2 series, where H is the 348 water depth and  $Q_{\text{meas}}$  the corresponding measured discharge.

349 They show very low sensitivity of both the *INCM* and *LHRM* results, such that a one 350 digit approximation of both model parameters ( $\xi$  and  $\beta$ ) should guarantee a computed 351 discharge variability of less than 2%.

352 The results of the sensitivity analysis, carried out for series K4 and shown in Table

353 2b, are similar to the previous ones computed for F2 series.

# 354 **4 Validation criterion**

#### 355 4.1 Validation n.1 - Comparison with laboratory experimental data

A first validation of the two methods was carried out by using the calibrated parameter values, the same Nash-Sutcliffe performance measure and all the available experimental series. The results were also compared with results of *DCM* and *IDCM* methods, the latter applied using the suggested  $\alpha = 0.02$  value and five subsections, each one corresponding to a different bottom slope in the lateral y direction. The NS index for all data series is shown in Table 3.

The *DCM* results are always worse and are particularly bad for all the K series. The results of both the *IDCM* and *INCM* methods are very good for the two F series not used for calibration, but are both poor for the K series. The *LHRM* method is always the best and also performs very well in the K series. The reason is probably that the K

366 series tests have very low discharges, and the constant  $\alpha$ =0.02, the coefficient adopted

- in the *IDCM* method, does not fit the size of the subsections and Eq. (12) is not a good
- 368 approximation of the mixing length  $\alpha_H$  in Eq. (11) for low values of the water depth.
- 369 In Figs. 3a and 3b the NS curves obtained by using DCM, IDCM, INCM and LHRM,
- 370 for series F2 and K4, are shown.

# 371 4.2 Validation n.2 - Comparison with field data

Although rating curves are available in different river sites around the world, fieldvalidation of the uniform flow formulas is not easy, for at least two reasons:

1) The average friction factor f and the related Manning's coefficient are not known as in the lab case and the results of all the formulas need to be scaled according to the Manning's coefficient to be compared with the actually measured discharges;

377 2) River bed roughness does change, along with the Manning's coefficient, from one
378 water stage to another (it usually increases along with the water level).

A possible way to circumvent the problem is to apply the compared methods in the context of a calibration problem, where both the average Manning's coefficient and the discharge hydrograph are computed from the known level hydrographs measured in two different river cross sections (Perumal et al., 2007; Aricò et al., 2009). The authors solved the diffusive wave simulation problem using one known level hydrograph as the upstream boundary condition and the second one as the benchmark downstream hydrograph for the Manning's coefficient calibration.

It is well-known in the parameter estimation theory (Aster et al., 2012) that the uncertainty of the estimated parameters (in our case the roughness coefficient) grows quickly with the number of parameters, even if the matching between the measured and the estimated model variables (in our case the water stages in the downstream section) improves. The use of only one single parameter over all the computational domain is motivated by the need of getting a robust estimation of the Manning's coefficient and of the corresponding discharge hydrograph.

Although the accuracy of the results is restricted by several modeling assumptions, a positive indication about the robustness of the simulation model (and the embedded relationship between the water depth and the uniform flow discharge) is given by: 1) the match between the computed and the measured discharges in the upstream

section, 2) the compatibility of the estimated average Manning's coefficient with thesite environment.

The area of interest is located in the Alzette River basin (Gran-Duchy of Luxembourg) between the gauged sections of Pfaffenthal and Lintgen (Fig. 4). The river reach length is about 19 km, with a mean channel width of  $\sim$ 30 m and an average depth of  $\sim$ 4 m. The river meanders in a relatively large and flat plain about 300 m, with a mean slope of  $\sim$ 0.08%.

The methodology was applied to a river reach 13 Km long, between two instrumented
sections, Pfaffenthal (upstream section) and Hunsdorf (downstream section), in order
to have no significant lateral inflow between the two sections.

407 Events of January 2003, January 2007 and January 2011 were analysed. For these 408 events, stage records and reliable rating curves are available at the two gauging 409 stations of Pfaffenthal and Hunsdorf. The main hydraulic characteristics of these 410 events, that is duration ( $\Delta t$ ), peak water depth (H<sub>peak</sub>) and peak discharge (q<sub>peak</sub>), are 411 shown in Table 4.

412

In this area a topographical survey of 125 river cross sections was available. The
hydrometric data were recorded every 15 min. The performances of the discharge
estimation procedures were compared by means of the Nash Suctliffe criterion.

The results of the *INCM* and *LHRM* methods were also compared with those of the *DCM* and *IDCM* methods, the latter applied by using  $\alpha = 0.02$  and an average subsection width equal to 7 m. The computed average Manning's coefficients n<sub>opt</sub>, reported in Table 5, are all consistent with the site environment, although they attain very large values, according to *DCM* an *IDCM*, in the 2011 event.

The estimated and observed dimensionless water stages in the Hunsdorf gauged site,for 2003, 2007 and 2011 events are shown in Figs. 5-7.

423 Only the steepest part of the rising limb, located inside the colored window of each 424 Figure, was used for calibration. The falling limb is not included, since it has a lower

- 425 slope and is less sensitive to the Manning's coefficient value.
- 426 A good match between recorded and simulated discharge hydrographs can be427 observed (Figs.8-10) in the upstream gauged site for each event.

428 For all investigated events the Nash Sutcliffe efficiency  $NS_q$  is greater than 0.90, as 429 shown in Table 6.

The error obtained between measured and computed discharges, with all methods, is of the same order of the discharge measurement error. Moreover, this measurement error is well known to be much larger around the peak flow, where the estimation error has a larger impact on the NS coefficient. The NS coefficients computed with the *LHRM* and *INCM* methods are anyway a little better than the other two.

## 435 4.3 Validation n.3 - Comparison with results of 3D ANSYS CFX solver

The vertically averaged velocities computed using *DCM*, *IDCM*, *INCM* and *LHRM* were compared with the results of the well known ANSYS 3D code, named CFX, applied to a prismatic reach with the irregular cross-section measured at the Hunsdorf gauged section of the Alzette river. The length of the reach is about four times the top width of the section.

In the homogeneous multiphase model adopted by CFX, water and air are assumed to share the same dynamic fields of pressure, velocity and turbulence and water is assumed to be incompressible. CFX solves the conservation of mass and momentum equations, coupled with the air pressure-density relationship and the global continuity equation in each node. Call  $\alpha_l$ ,  $\rho_l$ ,  $\mu_l$  and  $\mathbf{U}_l$  respectively the volume fraction, the density, the viscosity and the time averaged value of the velocity vector for phase l (l= w (water), a (air)), that is:

448 
$$\rho = \sum_{l=w,a} \alpha_l \rho_l \tag{21a},$$

449 
$$\mu = \sum_{l=w,a} \alpha_l \mu_l \tag{21b},$$

450 where  $\rho$  and  $\mu$  are the density and the viscosity of the "averaged" phase. The air 451 density is assumed to be a function of the pressure *p*, according to the state equation:

452 
$$\rho_a = \rho_{a,0} e^{\gamma(p-p_0)}$$
 (21c),

453 where the sub-index 0 marks the reference state values and  $\gamma$  is the air compressibility 454 coefficient.

The governing equations are the following: 1) the mass conservation equation, 2) the Reynolds averaged continuity equation of each phase and 3) the Reynolds averaged momentum equations. Mass conservation implies:

$$458 \qquad \sum_{l=w,a} \alpha_l = 1 \tag{22}.$$

459 The Reynolds averaged continuity equation of each phase *l* can be written as:

460 
$$\frac{\partial \rho_l}{\partial t} + \nabla \cdot (\rho_l \mathbf{U}) = S_l$$
(23).

461 where  $S_l$  is an external source term. The momentum equation instead refers to the 462 "averaged" phase and is written as:

463 
$$\frac{\partial(\rho \mathbf{U})}{\partial t} + \nabla \cdot (\rho \mathbf{U} \otimes \mathbf{U}) - \nabla \cdot \left(\mu_{eff} \left(\nabla \mathbf{U} + \left(\nabla \mathbf{U}\right)^{T}\right)\right) + \nabla p' = S_{M}$$
(24),

464 where  $\otimes$  is the dyadic symbol,  $S_M$  is the momentum of the external source term *S*, and 465  $\mu_{\text{eff}}$  is the effective viscosity accounting for turbulence and defined as:

$$\mu_{eff} = \mu + \mu_t \tag{25},$$

467 where  $\mu_t$  is the turbulence viscosity and p' is the modified pressure, equal to:

466

468 
$$p' = p + \frac{2}{3}\rho k + \frac{2}{3}\mu_{eff}\nabla \cdot \mathbf{U}$$
 (26).

469 where *k* is the turbulence kinetic energy, defined as the variance of the velocity 470 fluctuations and *p* is the pressure. Both phases share the same pressure *p* and the same 471 velocity **U**.

472 To close the set of six scalar equations (Eq.22, Eq.23 (two) and Eq.24 (three)), we 473 finally apply the k- $\varepsilon$  turbulence model implemented in the CFX solver. The 474 implemented turbulence model is a two equation model, including two extra transport 475 equations to represent the turbulent properties of the flow.

Two-equation models account for history effects like convection and diffusion of turbulent energy. The first transported variable is turbulent kinetic energy, k; the second transported variable is the turbulent dissipation,  $\varepsilon$ . The K-epsilon model has been shown (Jones, 1972; Launder, 1974) to be useful for free-shear layer flows with relatively small pressure gradients. Similarly, for wall-bounded and internal flows, the model gives good results, but only in cases where the mean pressure gradients are small.

The computational domain was divided using both tetrahedral and prismatic elements (Fig. 11). The prismatic elements were used to discretize the computational domain in the near-wall region over the river bottom and the boundary surfaces, where a

boundary layer is present, while the tetrahedral elements were used to discretize the remaining domain. The number of elements and nodes, in the mesh used for the specific case are of the order respectively  $4*10^6$  and  $20*10^6$ .

A section of the mesh is shown in Fig.12. The quality of the mesh was verified by
using a pre-processing procedure by ANSYS® ICEM CFD<sup>TM</sup> (Ansys inc.,2006).

491 The six unknowns in each node are the pressure, the velocity components, and the 492 volume fractions of the two phases. At each boundary node three of the first four 493 unknowns have to be specified. In the inlet section a constant velocity, normal to the section, is applied, and the pressure is left unknown. In the outlet section the 494 hydrostatic distribution is given, the velocity is assumed to be still normal to the 495 section and its norm is left unknown. All boundary conditions are reported in Table 7. 496 497 The opening condition means that that velocity direction is set normal to the surface, but its norm is left unknown and a negative (entering) flux of both air and water is 498 499 allowed. Along open boundaries the water volume fraction is set equal to zero. The solution of the problem converges towards two extremes: nodes with zero water 500 501 fraction, above the water level, and nodes with zero air fraction below the water level. On the bottom boundary, between the nodes with zero velocity and the turbulent flow 502 a boundary layer exists that would require the modelling of micro scale irregularities. 503 CFX allows the use, inside the boundary layer, of a velocity logarithmic law, 504 505 according to an equivalent granular size. The relationship between the granular size and the Manning's coefficient, according to Yen (1994), is given by: 506

507 
$$d_{50} = \left(\frac{n}{0.0474}\right)^6 \tag{27}.$$

508 where  $d_{50}$  is the average granular size to be given as the input in the CFX code.

509 Observe that the assumption of known and constant velocity directions in the inlet and outlet section is a simplification of reality. For this reason, a better reconstruction of 510 511 the velocity field can be found in an intermediate section, where secondary currents with velocity components normal to the mean flow direction can be easily detected 512 513 (Peters and Goldberg, 1989, Richardson and Colin, 1996). See in Fig. 13 how the 514 intermediate section was divided to compute the vertically averaged velocities in each 515 segment section and, in Fig.14, the velocity components tangent to the cross section 516 plane.

517 These 3D numerical simulations confirm that the momentum  $\Gamma$ , proportional to the 518 derivative of the average tangent velocities and equivalent to the left hand side of Eq. 519 2, cannot be set equal to zero, if a rigorous reconstruction of the velocity field is 520 sought after.

To compute the uniform flow discharge, for a given outlet section, CFX code is run iteratively, each time with a different velocity norm in the inlet section, until the same water depth as in the outlet section is attained in the inlet section for steady state conditions. Stability of the results has been checked against the variation of the length of the simulated channel. The dimensionless sensitivity of the discharge with respect to the channel length is equal to 0.2%.

527 See in Table 8 the comparison between the vertically averaged state velocities, 528 computed through the *DCM*, *IDCM*, *INCM*, *LHRM* formulas ( $u_{DCM}$ ,  $u_{IDCM}$ ,  $u_{INCM}$ , 529  $u_{LHRM}$ ) and through the CFX code ( $u_{CFX}$ ). Table 9 also shows the relative difference, 530  $\Delta u$ , evaluated as:

531 
$$\Delta u = \frac{u - u_{CFX}}{u_{CFX}} \times 100$$
(28),

532 As shown in Table 8, both INCM and LHRM perform very well in this validation test instead of DCM, which clearly overestimates averaged velocities. In the central area 533 534 of the section the averaged velocities calculated by the INCM, LHRM and CFX code are quite close with a maximum difference  $\sim 7\%$ . By contrast, larger differences are 535 536 evident close to the river bank, in segments 1 and 9, where INCM and LHRM 537 underestimate the CFX values. These larger differences show the limit of using a 1D 538 code. Close to the bank the wall resistance is stronger and the velocity field is more sensitive to the turbulent exchange of energy with the central area of the section, 539 540 where higher kinetic energy occurs. Thanks to the simulation of secondary flows (see 541 Fig. 14) CFX allows this exchange and the related mixing. However, because the near-bank subsections are characterised by small velocities, their contribution to the 542 543 global discharge is relatively small.

## 544 **5** Conclusions

545 Two new methods have been proposed for uniform flow discharge estimation. The 546 first method, named *INCM*, develops from the original *IDCM* method and it is shown 547 to perform better than the previous one, with the exception of lab tests with very

small discharge values. The second one, named *LHRM*, has empirical bases, and gives
up the ambition of estimating turbulent stresses, but has the following important
advantages:

551 1. It relies on the use of only two parameters: the friction factor f (or the 552 corresponding Manning's coefficient n) and a second parameter  $\beta$  which on the basis 553 of the available laboratory data was estimated to be equal to 9.

554 2. The  $\beta$  coefficient has a simple and clear physical meaning: the correlation distance, 555 measured in water depth units, of the vertically averaged velocities between two 556 different verticals of the river cross-section.

3. The sensitivity of the results with respect to the model  $\beta$  parameter was shown to be very low, and a one digit approximation is sufficient to get a discharge variability less than 2%. A fully positive validation of the method was carried out using lab experimental data, as well as field discharge and roughness data obtained by using the unsteady-state level analysis proposed by Aricò et al. (Aricò et al., 2009) and applied to the Alzette river, in the grand Duchy of Luxembourg.

4. Comparison between the results of the CFX 3D turbulence model and the *LHRM*model shows a very good match between the two computed total discharges, although
the vertically averaged velocities computed by the two models are quite different near
to the banks of the river.

567

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#### 572 Notation

573  $A_i$  = area of each subsection "i" of a compound channel

- 574 B = top width of compound channel
- 575 b = main channel width at bottom
- 576 f = friction factor
- 577 g = gravity acceleration

- H = total depth of a compound channel
- $n_{mc}$ ,  $n_{fp}$  = Manning's roughness coefficient for the main channel and floodplain, 580 respectively
- $P_i$  = wetted perimeter of each subsection "i" of a compound channel
- $Q_{\text{meas}}$  = measured discharge
- $R_i$  = hydraulic radius of each subsection "i" of a compound channel
- $S_0 =$  longitudinal channel bed slope
- $S_f$  = energy slope
- $\tau$  = turbulent stress
- $\epsilon = turbulent dissipation$
- <sup>588</sup>  $\rho$  = fluid density
- $\mu$ = flui viscosity
- $\alpha = IDCM$  interface coefficient
- $\beta = LHRM$  coefficient
- $\xi = INCM$  coefficient

# **References**

- 600 Abril, J. B., and Knight, D. W. (2004). Stage-discharge prediction for rivers in flood
- applying a depth-averaged model. J. Hydraul. Res., 42(6), 616–629.
- 603 Ansys Inc., Canonsburg. (2006). ANSYS CFX Reference guide.
- Ackers, P. (1993). Flow formulae for straight two-stage channels. J. Hydraul. Res.,
  31(4), 509–531.

607	
608	Aricò, C. and Tucciarelli, T. (2007). A Marching in Space and Time (MAST) solver
609	of the shallow water equations. Part I: the 1D model. Advances in Water Resources,
610	30(5), 1236-1252.
611	
612	Aricò, C., Nasello, C. and Tucciarelli, T. (2009). Using unsteady water level data to
613	estimate channel roughness and discharge hydrograph, Advances in Water Resources;
614	32(8), 1223-1240.
615	
616 617	Aster, C., Borchers, B., Clifford, H. (2012). Parameter Estimation and Inverse Problems. <i>Elsevier</i> , ISBN: 978-0-12-385048-5.
618	
619	Bousmar, D., and Zech, Y. (1999). Momentum transfer for practical flow computation
620	in compound channels. J. Hydraul. Eng.; 696–706.
621	
622	Cao, Z., Meng, J., Pender, G., & Wallis, S. (2006). Flow resistance and momentum
623	flux in compound open channels. J. Hydraul. Eng.; 1272-1282.
624	
625	Chow, V. T. (1959). Open channel hydraulics. New York: McGraw-Hill.
626	
627	Dey, M., and Lambert, M. F. (2006). Discharge prediction in compound channels by
628	end depth method. J. Hydraul. Res., 44(6), 767-776.
629	
630	Corato, G., Moramarco, T., and Tucciarelli, T. (2011). Discharge estimation
631	combining flow routing and occasional measurements of velocity, Hydrol. Earth Syst.
632	<i>Sci.</i> ,15, pp. 2979-2994.
633	
634	Herschel, C. (1897). On the origin of the Chezy formula, J. Assoc. of Engineering
635	Soc. 18, 363-368.
636	
637	Hu, C., Ji, Z., and Guo, Q. (2010). Flow movement and sediment transport in
638	compound channels. J. Hydraul. Res., 48(1), 23-32.
639	

640	Huthoff, F., Roos, P. C., Augustijn, D. C. M., and Hulscher, S. J. M. H. (2008).
641	Interacting divided channel method for compound channel flow. J. Hydraul. Eng.,
642	1158–1165.
643	
644	Jones, W. P., and Launder, B. E. (1972). The Prediction of Laminarization with a
645	Two-Equation Model of Turbulence, International Journal of Heat and Mass
646	Transfer; vol. 15, pp. 301-314.
647	
648	Kejun Yang, Xingnian Liu; Shuyou Cao and Er Huang. (2013). Stage-Discharge
649	Prediction in Compound Channels, J. Hydraul. Eng.
650	
651	Knight, D. W., and Abril, B. (1996). Refined calibration of a depth averaged model
652	for turbulent flow in a compound channel. Proc. ICE Water Maritime Energy; 118(3),
653	151–159.
654	
655	Knight, D.W., and Demetriou, J. D. (1983). Flood plain and main channel flow
656	interaction, J. Hydraul. Eng., 1073-1092.
657	
658	Knight, D. W., and Hamed, M. E. (1984). Boundary shear in symmetrical compound
659	channels, J. Hydraul. Eng., 1412–1430.
660	
661	Knight, D. W., McGahey, C., Lamb, R., and Samuels, P. G. (2010). Practical channel
662	hydraulics: Roughness, conveyance and afflux. CRC Press/Taylor and Francis,
663	Leiden, The Netherlands, 1–354.
664	
665	Knight, D. W., and Sellin, R. H. J. (1987). The SERC flood channel facility. J. Inst.
666	Water Environ. Manage, 1(2), 198–204.
667	
668	Knight, D. W., and Shiono, K. (1996). River channel and floodplain hydraulics.
669	Chapter 5, Floodplain processes, M. G. Anderson, D. E. Walling, and P. D. Bates,
670	eds., Wiley, New York, 139–181.
671	
672	Knight, D. W., Shiono, K., and Pirt, J. (1989).Prediction of depth mean velocity and

673 discharge in natural rivers with overbank flow. Proc., Int. Conf. on Hydraulic and

- 674 Environmental Modelling of Coastal, Estuarine and River Waters, R. A. Falconer, P.
- 675 Goodwin and R. G. S. Matthew, eds., Gower Technical, Univ. of Bradford, U.K.,
- 676 419–428.
- 677
- 678 Lambert, M. F., and Sellin, R. H. J. (1996). Discharge prediction in straight
- 679 compound channels using the mixing length concept. *J.Hydraul. Res.*,34(3), 381–394.
- 680
- 681 Launder, B. E., and Sharma, B. I. (1974). Application of the Energy Dissipation
- 682 Model of Turbulence to the Calculation of Flow Near a Spinning Disc. Letters in Heat
- 683 and Mass Transfer; vol. 1, no. 2, pp. 131-138.
- 684
- Liao, H., and Knight, D. W. (2007). Analytic stage-discharge formulas for flow in
  straight prismatic channels. *J. Hydraul. Eng.*, 1111–1122.
- 687
- 688 Lyness, J. F., Myers, W. R. C., Cassells, J. B. C., and O'Sullivan, J. J. (2001). The
- 689 influence of planform on flow resistance in mobile bed compound channels *Proc.*,
  690 *ICE Water Maritime Eng.*; 148(1), 5–14.
- 691
- McGahey, C. (2006). A practical approach to estimating the flow capacity of rivers.
- 693 Ph.D. thesis, The Open Univ., Milton Keynes, U.K,. (British Library).
- 694
- 695 McGahey, C., Knight, D. W., and Samuels, P. G. (2009). Advice, methods and tools
- 696 for estimating channel roughness. *Proc. ICE Water Manage*, 162(6), 353–362.
- 697
- Moreta, P. J. M., and Martin-Vide, J. P. (2010). Apparent friction coefficient in straight compound channels. *J. Hydraul. Res.*, 48(2), 169–177.
- 700
- Myers,W. R. C., & Brennan, E. K. (1990). Flow resistance in compound channels. J. *Hydraul. Res.*, 28(2), 141–155.
- 703
- Omran, M., and Knight, D. W. (2010). Modelling secondary cells and sediment
  transport in rectangular channels. *J. Hydraul. Res.*, 48(2), 205–212.
- 706

707	Peters J.J. and Goldberg A. (1989). Flow data in large alluvial channels in
708	Maksimovic, C. & Radojkovic, M. (eds) Computational Modeling and Experimental
709	methods in Hydraulics; Elsevier, London, 77-86.
710	
711	Perumal M, Moramarco T, Sahoo B, Barbetta S. (2007). A methodology for discharge
712	estimation and rating curve development at ungauged river sites. Water Resources
713	Res.
714	
715	Rameshwaran, P. and Shiono, K. (2007). Quasi two-dimensional model for straight
716	overbank flows through emergent vegetation on floodplains J. Hydraul. Res.: 45(3),
717	302-315.
718	
719	Rhodes, D. G., and Knight, D. W. (1994). Velocity and boundary shear in a wide
720	compound duct. J. Hydraul. Res., 32(5), 743-764
721	
722	Richardson R. W. and Colin R. Thorne. (1998). Secondary Currents around Braid Bar
723	in Brahmaputra River, Bangladesh. J. Hydraul. Eng., 124(3), 325-328.
724	
725	Schlichting, H. (1960). Boundary layer theory, 4th Ed., McGraw-Hill, NewYork.
726	
727	Sellin, R. H. J. (1964). A laboratory investigation into the interaction between the
728	flow in the channel of a river and that over its flood plain. La Houille Blanche, 7,
729	793–801.
730	
731	Shiono, K., Al-Romaih, J. S., and Knight, D. W. (1999). Stage-discharge assessment
732	in compound meandering channels. J. Hydraul. Eng., 66-77.
733	
734	Shiono, K., and Knight, D. W. (1991). Turbulent open-channel flows with variable
735	depth across the channel. J. Fluid Mech., 222, 617-646.
736	
737	Stephenson, D., and Kolovopoulos, P. (1990). Effects of momentum transfer in
738	compound channels. J. Hydraul. Eng., 1512–1522.
739	

740	Tang, X., and Knight, D. W. (2008). Lateral depth-averaged velocity distributions
741	and bed shear in rectangular compound channels. J. Hydraul. Eng., 1337-1342.
742	
743	Van Prooijen, B. C., Battjes, J. A., and Uijttewaal, W. S. J. (2005). Momentum
744	exchange in straight uniform compound channel flow. J. Hydraul. Eng., 175-183.
745	
746	Wormleaton, P. R., Allen, J., and Hadjipanos, P. (1982). Discharge assessment in
747	compound channel flow. J. Hydraul. Div., 108(9), 975–994.
748	
749	Wormleaton, P. R., & Hadjipanos, P. (1985). Flow distribution in compound
750	channels. J. Hydraul. Eng., 357–361.
751	
752	Yen, B.C. (1992). The Manning formula in context. Channel Flow Resistance:
753	Centennial of Manning's Formula,. Editor Water Resources Publications, Littleton,
754	Colorado, USA, p. 41.

Series	$S_0$	h	В	$b_4$	$b_1$	$b_3$	s <sub>fp</sub>	s <sub>mc</sub>
Series	$[\%_0]$	[m]	[m]	[m]	[m]	[m]	[-]	[-]
F1					4.1	4.100	0	1
F2		0.15	1.8	1.8 1.5	2.25	2.250	1	1
F3	1.027				0.75	0.750	1	1
F6					2.25	0	1	1
F8					2.25	2.250	1	0
F10					2.25	2.250	1	2
K1					0.229	0.229		
K2	0.066	0.08	0.15	5 0.152	0.152	0.152	0	0
K3	0.900				0.076	0.076	0	0
K4					-	-		

757 Table 1 Geometric and Hydraulic Laboratory Parameters of the experiment series.

758

Table 2a Sensitivities  $I_s$  and  $L_s$  computed in the F2 series for the optimal parameter values.

H [m]	$Q_{\text{meas}}[m^3 s^{-1}]$	$I_s$	$L_s$
0.156	0.212	0.2209	0.2402
0.169	0.248	0.1817	0.2194
0.178	0.282	0.1651	0.2044
0.187	0.324	0.1506	0.1777
0.198	0.383	0.1441	0.1584
0.214	0.480	0.1305	0.1336
0.249	0.763	0.1267	0.1320

761

Table 2b Sensitivities  $I_s$  and  $L_s$  computed in the K4 series for the optimal parameter

values.

H [m]	Q <sub>meas</sub> [m <sup>3</sup> s <sup>1</sup> ]	$I_s$	$L_s$
0.085	0.005	0.3248	0.3282
0.096	0.008	0.2052	0.2250
0.102	0.009	0.1600	0.1709
0.114	0.014	0.1354	0.1372

0.127	0.018	0.1174	0.1208
0.154	0.029	0.0851	0.0866

Table 3 Nash-Sutcliffe Efficiency for all (calibration and validation) experimentalseries.

	Series	DCM	IDCM	INCM	LHRM
	<i>F1</i>	0.7428	0.9807	0.9847	0.9999
Calibration	F2	0.6182	0.9923	0.9955	0.9965
Set	F3	0.7219	0.9744	0.9261	0.9915
	F6	0.7366	0.9733	0.9888	0.9955
	F8	-0.0786	0.9881	0.9885	0.9964
	F10	-0.0885	0.9965	0.9975	0.9978
Validation	<i>K1</i>	-14.490	-0.7007	-8.2942	0.9968
Set	K2	-0.9801	0.3452	-1.8348	0.9619
	<i>K3</i>	0.1762	0.6479	-0.3944	0.9790
	K4	0.2878	0.888	0.3548	0.9958

Table 4 Main characteristics of the flood events at the Pfaffenthal and Hunsdorfgauged sites.

	Δt [h]	Pfaffenthal Hunsdorf			
Event		H <sub>peak</sub>	$q_{\rm peak}$	H <sub>peak</sub>	$Q_{ m peak}$
		[m]	$[m^3s^{-1}]$	[m]	$[m^3s^{-1}]$
January 2003	380	3.42	70.98	4.52	67.80
January 2007	140	2.90	53.68	4.06	57.17
January 2011	336	3.81	84.85	4.84	75.10

....

	DCM	IDCM	INCM	LHRM
Event	n <sub>opt</sub>	n <sub>opt</sub>	<i>n</i> <sub>opt</sub>	<i>n</i> <sub>opt</sub>
	$n_{\text{opt}}$ [sm <sup>-1/3</sup> ]	$n_{\text{opt}}$ [sm <sup>-1/3</sup> ]	$n_{\rm opt}$ [sm <sup>-1/3</sup> ]	$n_{\rm opt}$ [sm <sup>-1/3</sup> ]
January 2003	0.054	0.047	0.045	0.045
January 2007	0.051	0.047	0.046	0.045
January 2011	0.070	0.070	0.057	0.055

Table 5 Optimum roughness coefficient,  $n_{opt}$ , for the three flood events.

778

Table 6 Nash-Sutcliffe efficiency of estimated discharge hydrographs for the analysed

flood events.

	DCM	IDCM	INCM	LHRM
Event	$NS_q$	$NS_q$	$NS_q$	$NS_q$
	[-]	[-]	[-]	[-]
January 2003	0.977	0.987	0.991	0.989
January 2007	0.983	0.988	0.989	0.992
January 2011	0.898	0.899	0.927	0.930

781

782 Table 7 Boundary conditions assigned in the CFX simulation.

783

Geometry Face	Boundary Condition					
Inlet	All velocity components					
	Velocity direction and					
Outlet	hydrostatic pressure					
	distribution					
Side-Walls	Opening					
Тор	Opening					
	No-slip wall condition, with					
Bottom	roughness given by					
	equivalent granular size d <sub>50</sub> .					

784

Table 8 Simulated mean velocities in each segment section using 1D hydraulic
models with *DCM*, *IDCM*, *INCM*, *LHRM* and *CFX*, and corresponding differences.

Subsectio  $u_{CF}$   $u_{DC}$   $u_{IDC}$   $u_{INC}$   $u_{LHR}$   $\Delta u_{DC}$   $\Delta u_{IDC}$   $\Delta u_{INC}$   $\Delta u_{LHR}$ 

n	X	М	М	М	М	М	Μ	М	М
				[ms <sup>-</sup>		[%]	[%]	[%]	[%]
	-1]	<sup>1</sup> ]	1]	1]	<sup>1</sup> ]	[,*]	[,~]	[,.]	[,~]
									-
	1.3								15.7
1		1.58	1.47	1.23	1.12	18.79	10.52	-7.52	8
2	1.3	1.40	1.4	1.07	1.00	2.65	<b>2</b> 10	0.72	0.72
2		1.42	1.4	1.36	1.38	3.65	2.19	-0.73	0.73
2	1.3	1.50	1 40	1.00	1.4	10.07	7.05	0	1 47
3		1.53	1.48	1.38	1.4	10.87	7.25	0	1.45
4	1.4 7	1 6 4	16	150	1 57	1150	0.01	6 1 2	6.90
4	/ 1.5	1.04	1.0	1.30	1.37	11.30	0 0.84	6.13	0.80
5		1.04	1.0	1 50	1.61	26 70	17.65	3.92	5 22
5	5 1.5	1.94	1.0	1.39	1.01	20.79	17.05	5.92	5.25
6	1.5 7	2.01	1.81	16	1 68	28.02	15 20	1.91	7.00
0	, 1.4	2.01	1.01	1.0	1.00	20.02	15.27	1.71	7.00
7		1.66	1.65	1.49	1.5	13.69	13.01	2.05	2.74
,	1.4	1100	1100	1117	110	10.07	10101	2.00	2., .
8		1.48	1.46	1.44	1.43	4.22	2.82	1.40	0.70
									-
	0.8								21.5
9	8	0.91	0.90	0.70	0.69	3.40	2.27	-20.45	5 9
				В					
		(				<b>→</b>		1	
S <sub>fp</sub>									
<b,< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td><b>b</b><sub>3</sub></td><td>h H</td><td></td></b,<>							<b>b</b> <sub>3</sub>	h H	
		Sme						¥ ¥	
		◄		b <sub>4</sub>					



788 Figure 1 Compound channel geometric parameters.

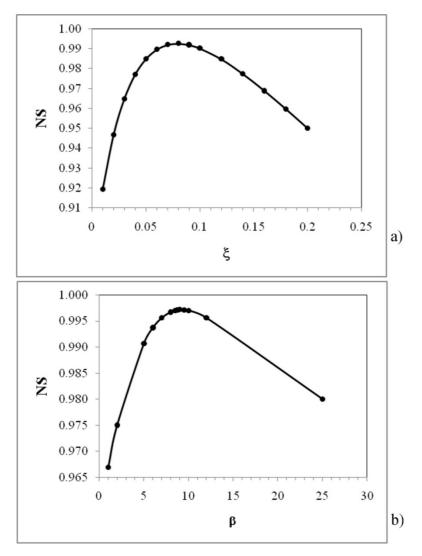
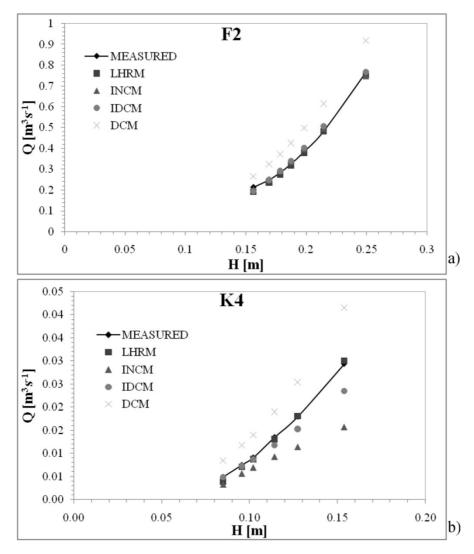


Figure 2 NS versus  $\xi$  and  $\beta$  curves respectively for *INCM* (a) and *LHRM* (b) methods.

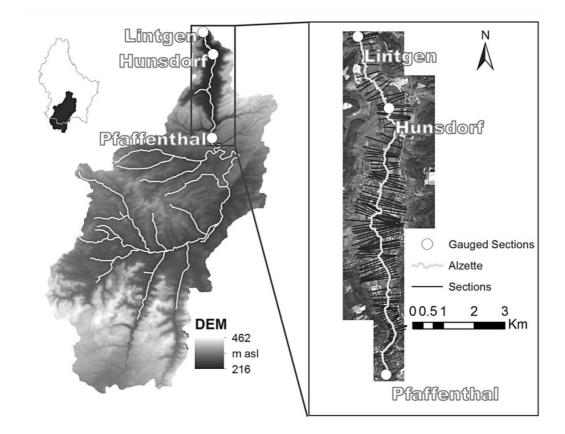
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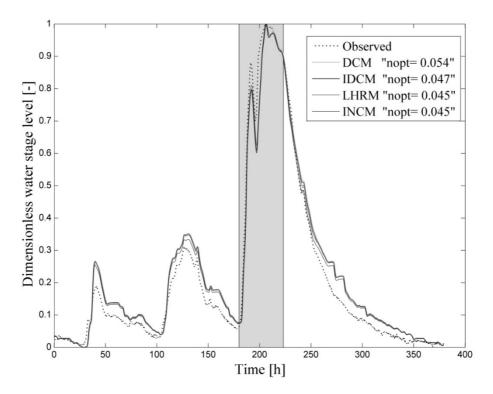
Figure 3 Estimated discharge values against HR Wallingford FCF measures for F2 (a)

and K4 (b) series.





797 Figure 4 The Alzette Study Area.



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Figure 5 Observed and simulated stage hydrographs at Hunsdorf gauged site in theevent of January 2003.

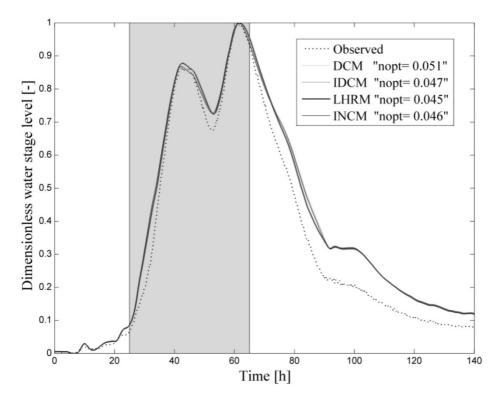




Figure 6 Observed and simulated stage hydrographs at Hunsdorf gauged site in theevent of January 2007.

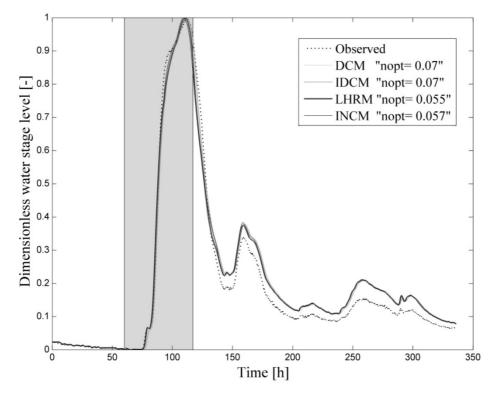
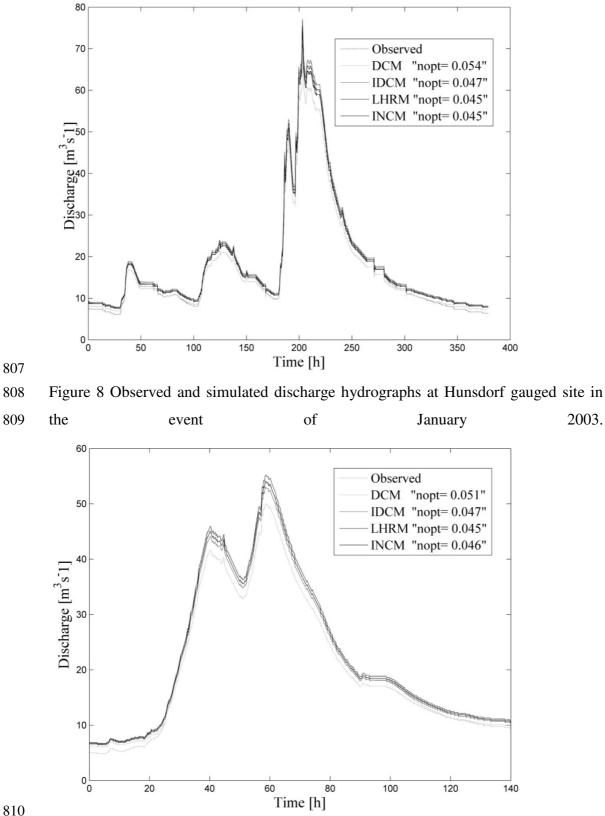
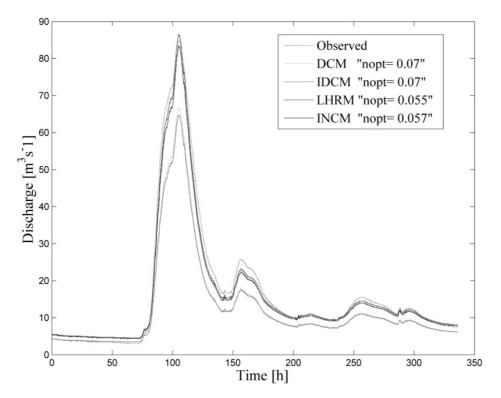


Figure 7 Observed and simulated stage hydrographs at Hunsdorf gauged site in the event of January 2011.



811 Figure 9 Observed and simulated discharge hydrographs at Hunsdorf gauged site in 812 the event of January 2007.

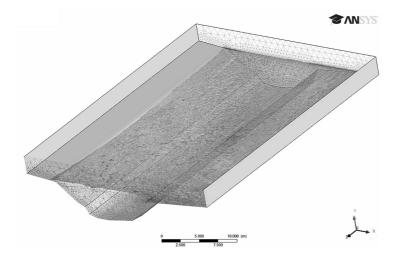


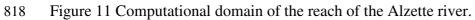


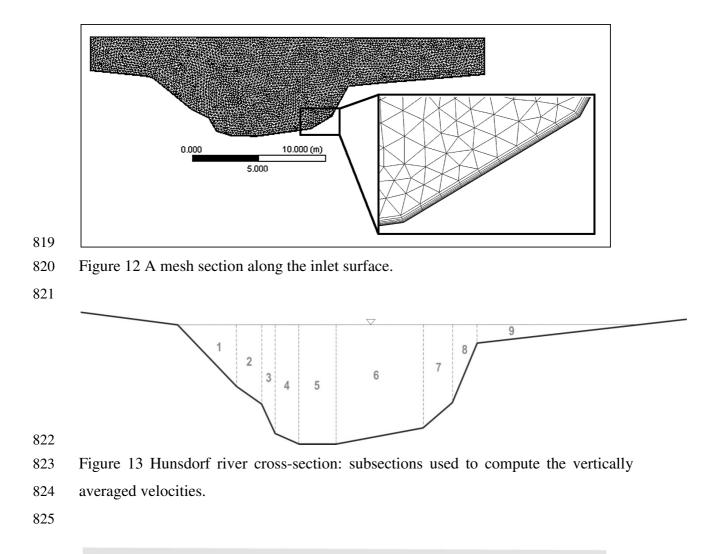
814 Figure 10 Observed and simulated discharge hydrographs at Hunsdorf gauged site in

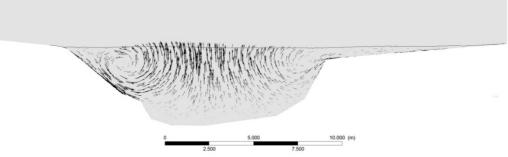
the event of January 2011.

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- 827 Figure 14 Secondary flow inside the intermediate cross section.