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# An automated method to build groundwater model hydrostratigraphy from airborne electromagnetic data and lithological borehole logs

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## Abstract

Large-scale integrated hydrological models are important decision support tools in water resources management. The largest source of uncertainty in such models is the hydrostratigraphic model. Geometry and configuration of hydrogeological units are often poorly determined from hydrogeological data alone. Due to sparse sampling in space, lithological borehole logs may overlook structures that are important for groundwater flow at larger scales. Good spatial coverage along with high spatial resolution makes airborne time-lapse electromagnetic (AEM) data valuable for the structural input to large-scale groundwater models. We present a novel method to automatically integrate large AEM data-sets and lithological information into large-scale hydrological models. Clay-fraction maps are produced by translating geophysical resistivity into clay-fraction values using lithological borehole information. Voxel models of electrical resistivity and clay fraction are classified into hydrostratigraphic zones using *k*-means clustering. Hydraulic conductivity values of the zones are estimated by hydrological calibration using hydraulic head and stream discharge observations. The method is applied to a Danish case study. Benchmarking hydrological performance by comparison of simulated hydrological state variables, the cluster model performed competitively. Calibrations of 11 hydrostratigraphic cluster models with 1–11 hydraulic conductivity zones showed improved hydrological performance with increasing number of clusters. Beyond the 5-cluster model hydrological performance did not improve. Due to reproducibility and possibility of method standardization and automation, we believe that hydrostratigraphic model generation with the proposed method has important prospects for groundwater models used in water resources management.

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## 1 Introduction

Large-scale distributed integrated hydrological and groundwater models are used extensively for water resources management and research. We use large-scale to refer to models in the scale of 100 to 1000 km<sup>2</sup> or larger. Examples are: water resources management in water scarce regions (Gräbe et al., 2012; Laronne Ben-Itzhak and Gvirtzman, 2005); groundwater depletion (Scanlon et al., 2012); contamination (Li and Merchant, 2013; Mukherjee et al., 2007); agricultural impacts on hydrogeological systems (Rossman and Zlotnik, 2013); and well capture zone delineation (Moutsopoulos et al., 2007; Selle et al., 2013).

Such models are typically distributed, highly parameterized, and depend on data availability to sufficiently represent the modelled systems. Model parameterization includes, for example, the saturated and unsaturated zone hydraulic properties, land use distribution and properties, and stream bed configuration and properties. Hydrological forcing data such as precipitation and temperature are also required. Parameters are estimated through calibration, which requires hydrological observation data commonly in the form of groundwater hydraulic heads and stream discharges. Calibration data should be temporally and spatially representative for the modelled system, and so should validation data sets.

One of the main challenges in modelling large-scale hydrogeological systems is data scarcity (Refsgaard et al., 2010; Zhou et al., 2014). Uncertainty inherent in distributed hydrological models is well known (Beven, 1989). Incorrect system representation due to lack of data contributes to this uncertainty, but most important source of uncertainty in distributed groundwater models is incorrect representation of geologic structures (Refsgaard et al., 2012; Seifert et al., 2012; Zhou et al., 2014).

Lithological borehole logs are the fundamental data source for constructing hydrostratigraphic models. The modelling process is often cognitive, but also geostatistical methods are used (He et al., 2013; Strebelle, 2002). Geostatistical approaches are less suitable for large-scale models because they assume stationarity within the modelled

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geological domain and hence the model area often needs to be subdivided into several stationary geological domains. Spatial inconsistent sampling pattern and scarcity make lithological borehole logs alone insufficient to capture local-scale geological structures relevant for simulation of groundwater flow and contaminant transport.

Airborne **time-domain** electromagnetic (AEM) data is unique with respect to good spatial coverage and high resolution. AEM is the only technique that can provide high-resolution subsurface information at regional scales. Geological structures and heterogeneity, which spatially scarce borehole lithology data may overlook, are well resolved in AEM data. Geophysical data and especially AEM data are commonly used to support lithological borehole information in geological mapping and modelling (Bosch et al., 2009; Høyer et al., 2011; Jørgensen et al., 2010; Jørgensen et al., 2013; Sandersen and Jørgensen, 2003).

Current practice for hydrostratigraphic and geological model generation faces a number of challenges: structures that control groundwater flow may be overlooked in the manual 3-D modelling process; geological models are subjective, and different geological models may result in very different hydrological predictions; structural uncertainty inherent in the model building process cannot be quantified. Currently there is no standardized way of integrating high resolution AEM into hydrogeological models.

Sequential, joint and coupled hydrogeophysical inversion methods have been developed and used extensively in hydrological and groundwater research to capture hydrological processes or estimate aquifer properties and structures from geophysical data (Hinnell et al., 2011). Hydrogeophysical inversion addresses hydrogeological property estimation or delineation of hydrogeological structures. In the context of large-scale groundwater models studies, Dam and Christensen (2003) and Herckenrath et al. (2013) translate between hydraulic conductivity and electrical resistivity to estimate hydraulic conductivity parameters of the subsurface in a joint hydrogeophysical inversion framework. Petrophysical relationships however are not well known and vary in space, which makes a fixed translation between geophysical and hydrological parameter space problematic. Herckenrath et al. (2013) concluded that sequential hy-

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drogeophysical inversion was preferred over joint hydrogeophysical inversion due to the uncertainty associated with the translator function. Structural inversions are often performed as purely geophysical inversions, where subsurface structures (that mimic geological or hydrogeological features) are favoured during inversion by choosing appropriate regularization terms. An example is the layered and laterally constrained inversion developed by Auken and Christiansen (2004), which respects vertically sharp and laterally smooth boundaries found in sedimentary geology. Joint geophysical inversions have been used extensively to delineate subsurface hydrogeological structures under the assumption that multiple geophysical data sets carry information about the same structural features of the subsurface (Christiansen et al., 2007; Gallardo, 2003; Haber and Oldenburg, 1997) but examples of successful joint hydrogeophysical inversion at larger scales are rare.

As a response to lack of global petro-physical relationships, clustering algorithms as an extension to structural inversion methods have been applied in geophysics (Bedrosian et al., 2007). Fuzzy *c*-means and *k*-means clustering algorithms have been used with sequential inversion schemes (Paasche et al., 2006; Triantafyllis and Buchanan, 2009) and joint inversion schemes (Di Giuseppe et al., 2014; Paasche and Tronicke, 2007). These studies have focused on the structural information contained in geophysical information, and hydrogeological or geological parameters of the subsurface are assumed uniform within the delineated zones. This approach corresponds well with the common practice in groundwater modelling where degrees of freedom of the subsurface are reduced by zoning the subsurface.

We present an objective and semi-automatic method to model large-scale hydrostratigraphy from geophysical resistivity and lithological data. The method is a novel sequential hydrogeophysical inversion for integration of AEM data into the hydrological modelling process. First, resistivity data is translated into clay fraction values by inverting for the parameters of a spatially variable petrophysical relationship (Foged et al., 2014). Second, a cluster analysis is performed on the principal components of resistivity data and clay fraction values. The zones identified in the cluster analysis are

assumed to have uniform hydrogeological properties, and thus form the hydrostratigraphic model. Third, the hydraulic conductivity (*K*) of each zone in the hydrostratigraphic cluster model is estimated in a hydrological model calibration. The hydrological performance is benchmarked against a geological reference model. Results are shown for a Danish case study.

**2 Materials and methods**

We propose a data-driven 3-D zonation method to build groundwater model hydrostratigraphy. Hydrostratigraphic structures and parameters are determined sequentially by geophysical/lithological and hydrological data respectively. As shown in Fig. 1 zonation is completed in two steps, (1) delineation of hydrostratigraphic structures (see Fig. 2c) through *k*-means cluster analysis on resistivity data (see Fig. 2a) and clay fraction values (see Fig. 2b), and (2) estimation of hydraulic parameters of the hydrostratigraphic structures in a hydrological calibration using observations of hydraulic head and stream discharge.

11 hydrostratigraphic cluster models consisting of 1–11 zones are set up and calibrated.

**2.1 Study area**

Norsminde study area is located on the eastern coast of Jutland, Denmark, and covers a land surface area of 154 km<sup>2</sup>. Figure 3 shows a map of the area delineating study area boundary, streams, and hydrological data. An overview of the geophysical and lithological data is shown in Fig. 4. Within 5–7 km from the sea, the land is flat and rises only to 5–10 m a.s.l. Further to the west the land ascends into an up-folded end-moraine at elevations between 50–100 m a.s.l. The town of Odder with approximately 20 000 inhabitants is located at the edge of the flat terrain in the middle of the model domain.

Palaeogene, Neogene and Quaternary deposits characterize the area. The Palaeogene deposits are thick clays, and define the lower geological boundary. Neogene marine clays interbedded with alluvial sands overlay the Palaeogene deposits in the elevated northern and western parts of the model domain. Quaternary deposits are glacial meltwater sediments and tills found throughout the domain. A large WE striking tunnel valley (2 km by 14 km) incises the Palaeogene clay in the south (Jørgensen and Sandersen, 2006). The unconsolidated fill materials are meltwater sand and gravel, clay tills, and waterlaid silt/clay.

Groundwater is abstracted for drinking water supply, mainly from tunnel valley deposits and the elevated south-western part of the domain. The groundwater resource is abstracted from 66 abstraction wells, with a total production of 18 000–26 000 m<sup>3</sup> yr<sup>-1</sup>, excluding smaller private wells. Maximum annual abstraction from one well is 12 400 m<sup>3</sup> yr<sup>-1</sup>. Actual pumping variation among the 66 wells and inter-annual variation of pumping rates are unknown. Abstraction is planned locally by water works and only information about permissible annual rates has been obtained for this study.

Groundwater hydraulic heads are available from 132 wells at various depths, see Fig. 3 for the spatial distribution. Hydraulic head data are collected from the Danish national geological and hydrological database Jupiter (GEUS, n.d.).

Average annual precipitation is 840 mm yr<sup>-1</sup> for the years 1990–2011. Most of the area is tile-drained. The catchment is drained by a network of 24 streams; the main stream is gauged at the three stations 270035, 270002 and 270003 (see Fig. 3). Streams vary from ditch-like channels to meters wide streams. Low and high flows respectively are in the order of 0.05–0.5 and 0.5–5 m<sup>3</sup> s<sup>-1</sup>. Daily stream discharge data is available from three gauging stations. Discharges are calculated from mean daily water table measurements and translated with QH curves, which are available from approximately monthly discharge measurements.

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## 2.2 Geophysical data

Time-domain electro-magnetic (AEM) data collected through ground and airborne surveys is available for most of the study area; brown dashed areas in Fig. 4a show the extent of the ground-based surveys and dots in Fig. 4a show locations of AEM soundings. AEM data was collected using the SkyTEM<sup>101</sup> system in 2011 (Schamper et al., 2014a). SkyTEM<sup>101</sup> is developed for near-surface exploration by measuring also very early time gates, which requires careful system calibration and data processing (Auken et al., 2009; Schamper et al., 2014a). Depth of investigation (DOI) (Auken et al., 2014; Christiansen and Auken, 2012) varied between 50 and 150 m. The survey was completed with a flight line spacing of 100/50 m and sounding spacing of 15 m (total of 1856 line km, equivalent to 106 770 1-D resistivity models). Data was inverted using spatially constrained inversion (SCI), which mimics 3-D distribution of subsurface resistivity by passing information through lateral and vertical constraints along and between flight lines (Viezzoli et al., 2008). In the SCI, single soundings were modelled as smooth 1-D resistivity models consisting of 29 layers with fixed layer boundaries. DOI was used to terminate the resistivity models with depth. For the airborne survey an acceptable match of almost 90 % was found when checking resistivity results against borehole data (Schamper et al., 2014b). Ground based TEM soundings were collected during the 1990's with the Geonics TEM47/PROTEM system, and were inverted individually as 1-D layered resistivity models. Depending on optimal fit these models have 3–5 layers.

## 2.3 Hydrostratigraphic model

Geophysical and lithological data are used to zone the subsurface. Geophysical data consists of resistivity values determined from inversion of airborne and ground-based electromagnetic data. Lithological information is represented in clay fraction values determined through inversion within the clay fraction concept (CF-concept). Zonation is performed in 3-D.

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The CF-concept is formulated as a least squares inversion problem to determine the parameters of a petro-physical relationship that translates geophysical resistivities into clay fraction values. The concept is described in detail in Foged et al. (2014) and (Christiansen et al., 2014), and only a brief introduction is given here. The inversion minimizes the difference between observed clay fraction as determined from borehole lithological logs (in the inversion this is the data) and translated clay fraction as determined from geophysical resistivity values (in the inversion this is the forward data). Clay fraction expresses relative accumulated thickness of clay material over an interval. In this context clay refers to material described as clay in lithological logs, and not clay minerals. Clay definitions include, among others, clay till, marl clay, mica clay, and silty clay. Lithological borehole information is available at approximately 700 locations (see Fig. 4b). Descriptions are from the Danish Jupiter database (GEUS, n.d.) and level of detail and quality varies from detailed lithological description at 1 m intervals to more simple sand, clay, till descriptions at layer interface depths. Boreholes are categorized according to quality of lithological information where 1 is the highest quality and 5 is the lowest (see Fig. 4b). The quality rating is presented in Schamper et al. (2014b).

In the CF-inversion, the petrophysical relationship (in the inversion this is the forward model) is a two-parameter function defined in regular horizontal 2-D grids which are vertically constrained to form a 3-D model. The translator model parameters are interpolated from grid nodes to the locations of the geophysical resistivity models. Using the location-specific model, geophysical resistivities are translated into clay fraction values. Using kriging the simulated clay fractions are interpolated to the location of the lithological borehole logs. The misfit between the observed and simulated clay fractions are then calculated at the borehole locations. The objective function, which contains data misfit and vertical and horizontal smoothness constraints, is optimized iteratively.

Delineation of subsurface structures is performed as a  $k$ -means cluster analysis on geophysical resistivities and clay fraction values. Information contained in clay fraction values is to some extent duplicated in the geophysical resistivity values. Heterogeneity captured in the resistivity data however is simplified in the translation to clay fraction; for

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example till and Palaeogene clay have respectively medium and low resistivity values while the clay fraction for both materials is 1.

$K$ -means clustering is a well-known cluster analysis which finds groups in multivariate data based on a measure of similarity between cluster members (Wu, 2012). Similarity is defined as minimum squared Euclidean distance between each cluster member and cluster centroid, summed over all cluster members. The number of clusters that data is divided into is defined by the user. We use the  $k$ -means analysis implementation in MATLAB R2013a, which use a two-phase search, batch and sequential, to minimize the risk of reaching a local minimum.

Because clay fraction values are correlated with geophysical resistivities  $k$ -means clustering is performed on principal components (PC) of the original variables. Principal components analysis (PCA) is an orthogonal transformation based on data variances (Hotelling, 1933). PCA thus finds uncorrelated linear combinations of original data while obtaining maximum variance of the linear combinations (Härdle and Simar, 2012). The uncorrelated PCs are a useful representation of the original variables as input to a  $k$ -means cluster analysis. Original variables must be weighted and scaled prior to PCA, as PCA is scale sensitive, and the lack of explicit physical meaning of the PCs makes weighting difficult. Clay fraction values are unchanged as they range between 0 and 1.

The normalized resistivity values are calculated as  $\rho_{\text{norm}} = \frac{\log \rho - \log \rho_{\text{min}}}{\log \rho_{\text{max}} - \log \rho_{\text{min}}}$ . Where  $\rho_{\text{min}}$  is and  $\rho_{\text{max}}$  is minimum and maximum resistivity values respectively.

## 2.4 Integrated hydrological model

Hydrological data are used to parameterise the structures of the hydrostratigraphic model. Stream discharges and groundwater hydraulic heads are used as observation data in the hydrological calibration.

The hydrological model is set up using MIKE SHE (Abbott et al., 1986; Graham and Butts, 2005), which is a physically based integrated hydrological model code simulat-

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- The river leakage coefficient.
  - The horizontal hydraulic conductivities of all zones of the 11 hydrostratigraphic cluster models. Figure 5 shows sensitivity to  $K$  of the zones of the 5-cluster model.  $K$  of the zones are unknown; hence all  $K$  values have been calibrated. Vertical
- 5  $K$  values are tied to horizontal  $K$  with an anisotropy factor of 10. Initial horizontal  $K$  values are  $10^{-4}$ ,  $10^{-6}$  or  $10^{-8}$   $\text{ms}^{-1}$  depending on mean clay fraction value of a zone.

Storage parameters were set to a priori values and not calibrated.

10 Calibration is performed using the Marquardt–Levenberg local search optimization implemented in PEST (Doherty, 2005). Observations are 632 hydraulic heads from 132 well filters and daily stream discharge time series from three gauging stations, see Fig. 3. Observation variances are estimated, and, in the absence of information, observation errors were assumed to be uncorrelated. Objective functions for head and discharge have been scaled to balance contributions to the total objective function.

15 The aggregated objective function,  $\Phi$ , shown in Eq. (1) is the sum of the scaled objective function for head and discharge. The subjective weight,  $w_s$ , was determined through trial and error by starting numerous calibration runs;  $w_s$  was chosen to be 0.8.

$$\Phi = w_s \sum_{i=1}^{N_h} \left( \frac{h_{\text{sim},i} - h_{\text{obs},i}}{\sigma_i} \right)^2 + (1 - w_s) \sum_{i=1}^{N_q} \left( \frac{q_{\text{sim},i} - q_{\text{obs},i}}{\sigma_i} \right)^2 \quad (1)$$

20 Hydraulic head observation errors are determined following the guidelines following Henriksen et al. (2003). They suggest an error budget approach which accounts for contributions from (1) the measurement (e.g. with dip meter), (2) inaccuracy in vertical referencing of wells, (3) interpolation between computational nodes to observation well location; and (4) heterogeneity that is not represented in the lumped computational

25 grid. The total error expresses the expected uncertainty between observation and corresponding simulation. The approach for estimating these uncertainties can be found in Appendix A. Total errors amount to 0.95, 1.4 and 2.2 m.

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Uncertainty of stream discharges is mainly due to translation from water stages to discharge (daily mean discharges). Uncertainties originate from infrequent calibration of rating curve, ice forming on streams and especially stream bank vegetation (Raaschou, 1991). Errors can be as large as 50%. Blicher (1991) estimates errors of

5 5 and 10% on the water stage measurement and rating curve respectively. In cases of very low stream flows ( $1 \text{ L s}^{-1}$ ) Christensen et al. (1998) assigned a SD of 200% while flow of 50 and  $5\text{--}10 \text{ L s}^{-1}$  are assigned SD of 5 and 25% respectively. We have assigned an error of 20% to all stream discharge observations.

## 2.5 Benchmarking hydrostratigraphic cluster models

10 The performance of the hydrological model based on the cluster model hydrostratigraphy has been benchmarked against the hydrological performance using a reference geological model (He et al., 2015). The reference geological model is based on geological interpretation and AEM data. The study area was subdivided into seven major geological elements, based on geological interpretation. The seven elements are the

15 Palaeogene clay, the Miocene, Boulstrup tunnel valley, three glacial sequences, and a glaciectonic complex. By collapsing the three glacial sequences into one glacial element, four hydrogeological elements were defined; the Miocene, Boulstrup tunnel valley, the glacial, and the glaciectonic complex. He et al. (2014) performed a geo-statistical analysis with TProGS (Carle and Fogg, 1996) on the lithological information

20 and AEM data in the Miocene element to determine a sand-clay cut-off value for geophysical resistivities. This cut-off value was used to subdivide each of the four elements into units of sand and clay. Surface geology is characterized by a clay, sand and peat unit. The horizontal distribution of clay, sand and peat is taken from the Danish National Water Resources Model (Højberg et al., 2010). Because of problems with drying

25 filters in groundwater abstraction wells, a material with horizontal and vertical hydraulic conductivity of  $3 \times 10^{-5} / 3 \times 10^{-6} \text{ ms}^{-1}$  was added around selected filter screens.

Both the reference geological model and the cluster models are used to construct hydrological models that are calibrated in the hydrological calibration framework de-

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scribed previously. The only difference between the hydrological models and the calibrations are the parameterization (structures and values) of the saturated zone. As for the cluster models the Palaeogene clay surface elevation defines the lower boundary of the hydrological model. A vertical anisotropy of 1/10 is assumed for all geological units. Calibration parameters of the reference model are shown in Table 1. Specific yield values are fixed 0.05 and 0.2 for clay and sand deposits respectively, and specific storage is fixed at  $5 \times 10^{-5}$ .

### 3 Results and discussion

First we show results for the hydrological performance of 11 hydrostratigraphic cluster models consisting of 1–11 zones. Secondly details of the cluster analysis for the case of a 5-cluster hydrostratigraphy are shown. Finally the results of benchmarking with the reference model are presented through comparison of observed and simulated state variables.

#### 3.1 Calibration and validation of hydrological model

Figure 6 shows the weighted RMSE of models consisting of hydrostratigraphic cluster model of 1–11 zones. Values are shown for head and discharge in separate figures. The 1-cluster model is a homogeneous representation of the subsurface resulting in a uniform  $K$  field. The 1-cluster model represents a situation where we have no information about the subsurface. Increasing the number of clusters to represent the subsurface successively adds more information from geophysical and lithological data to the calibration problem. Horizontal dashed lines indicate weighted RMSE of the reference model. The weights used to calculate weighted RMSE are the same weights as used in Eq. (1).

Head and discharge contribute by approximately 2/3 and 1/3 of the total objective function. From the 1-cluster to the 2-cluster model, weighted RMSE for discharge is

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reduced by more than a factor 2. No significant improvement of the fit to discharge data is observed for more than 2 clusters. Fit to head data improves almost by a factor of 2 from the 1-cluster to the 2-cluster model. Improvement of the fit to head data continues up to the 5-cluster representation of the subsurface. Improvements are a factor of 3 from the 1-cluster to the 5-cluster model. Beyond the 5-cluster model, the fit to head observations stagnates. The 7-cluster and 9-cluster hydrostratigraphic models perform worse than the 3-cluster model. The 8-, 10-, and 11-cluster models obtain an equally good or better fits to head data compared to the 5-cluster model.

The blue lines in Fig. 6 illustrate mean SD on  $\log(K)$  values of the cluster models and reference model respectively, based on the post-calibration SD of  $\log(K)$  for each  $K$  zone. The mean SD of the reference model is 0.046, and corresponds to that of the 2- and 3-cluster models. Beyond the 4- and 5-cluster models the precision of the estimated  $K$  values decrease. The mean SD on  $\log(K)$  for the 4- and 5-cluster models are 0.12 and 0.15. The corresponding widths of the 95 % confidence intervals are between 15 and 90 % of the estimated  $K$  value for 3 out of 4 zones and 3 out of 5 zones, respectively. Beyond the 5-cluster model mean SD on  $\log(K)$  are between 0.17 and 0.27, and corresponding width of the 95 % confidence intervals are largely above 100 % for all but two zones.

With the combined information from weighted RMSE values and SD on  $\log(K)$  we are able to address over-parameterisation. The results indicate that we obtain good fit to observations without over-parameterisation with a 4- to 5-cluster hydrostratigraphic model.

In this paper, we have discussed the performance of the cluster models as a measure of fit to hydraulic head and stream discharge observations. Integrated hydrological models are typically used to predict transport, groundwater age, and capture zones, which are sensitive to geological features. It is likely that the optimal number of clusters is different for these applications. An analysis, as is presented here for head and discharge, for predictive application is more difficult because observations are often unavailable.

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The hydrostratigraphic models are constructed under the assumption that subsurface structures governing groundwater flow can be captured by structural information contained in clay fraction values (derived from lithological borehole data) and geophysical resistivity values. If this is true, an asymptotic improvement of the data fit would be expected for increasing cluster numbers. However, as shown in Fig. 6, this is not strictly the case: weighted RMSE of the 7-cluster and 9-cluster models is higher than weighted RMSE of the 3-cluster, 6-cluster and 8-cluster models, respectively. The likely explanation is that increasing number of clusters does not correspond to pure cluster sub-division, but also to relocation of cluster interfaces in the 3-D model space. We expect the difference in hydrological performance to be due to changes in interface configuration.

It is well-known that an unsupervised  $k$ -means clustering algorithm does not result in unique solution, due to choice of initial (and unknown) cluster centroids. We have sampled the solution spaces (200 samples) of the eleven cluster models. Clustering the principal components of geophysical resistivity data and clay fraction values into 1 to 5 clusters gives unique solutions. Clustering the principal components of geophysical resistivity data and clay fraction values into 6 to 11 clusters results in three or more solutions. The non-unique solutions however have different objective functions (squared Euclidean distance between points and centroids). In all cases the cluster model with the lowest objective function was chosen as the best solution.

Figure 7 shows RMSE and mean errors for calibration and validation periods for all 11 cluster models and the reference model. Horizontal dotted lines are reference model performances. Data used to calculate the statistics are a temporally split sample from 35 wells, which have observations both in the calibration and validation period, and the discharge is for stations 270002 and 270003.

The cluster models as well as the reference model perform similarly in 2000–2003 and 1995–1999. With respect to RMSE, Fig. 7a, for head the validation period is approximately 10% worse than the calibration period. RMSE for discharge, Fig. 7b, is lower in the validation, approximately a third of the calibration values. Mean errors for

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head, Fig. 7c, are lower and higher for the reference model and the cluster models respectively. The hydrological models analysed in this study generally under-simulate the average discharge.

From Fig. 7a and c it appears that the cluster models for 3-4-5 clusters perform better than the reference model with respect to RMSE head, while they have equal performance for ME head. Recalling that the reference model and the 5-cluster model have respectively 6 and 5 degrees of freedom in the hydrological model calibration, this indicates the difference in spatial patterns of the two models.

### 3.2 The cluster model

Figure 8 presents histograms of clay fraction values and resistivity values and how the values are represented in the five clusters, which was chosen to be the optimal number. Counts are shown as percentages of total number of pixels in the domain. The histograms in Fig. 8 show that the clay fraction attribute separates high resistivity/low clay fraction (sandy sediments) from other high-resistivity portions of the domain, while the resistivity attribute separates low resistivity/high clay fraction (clayey sediments) from other high clay-fraction portions. High resistivity/low clay fraction values are represented by clusters 1, 3 and 4 and low resistivity/high clay fraction are represented by clusters 2 and 5 (see Fig. 8a).

Figure 9 shows the data cloud that forms the basis of the clustering. The data cloud is binned into 300 bins in each dimension and the colour of the cloud shows the bin-wise data density. We see that cluster boundaries appear as straight lines in the attribute space. Values with a low resistivity and corresponding high clay fraction, mainly clusters 2 and 5, populate more than half of the domain. Clay is expected to dominate this part of the domain.

The results of the cluster analysis are presented with respect to geophysical resistivity and clay fraction values, while the cluster analysis is performed on the principal components (PC) of geophysical resistivity and clay fraction values. The first PC explains the information where the two original variables, log resistivity and clay fraction,

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are inversely correlated. This corresponds to the situation where a clay fraction of 1 coincides with a low resistivity value, and vice versa for clay fraction values of 0 and high resistivities. This is the information that we expect, i.e. our understanding of how geophysical resistivities relate to lithological information as represented by our translator function (defined under the assumption that variation in geophysical resistivities with respect to lithological information depends on the presence of clay materials). Thus the first principal component is the “clay” information in the geophysical resistivities. The second PC is less straight forward to interpret. Ideally, the second PC represents the data pairs where the resistivity response is *not* dominated or explained by lithological clay material. This might reflect a situation where a low resistivity value – and its associated low clay fraction value – is a result of a sandy material with a high pore-water electrical conductivity due to elevated dissolved ion concentrations. The second PC can also be a result of the CF-conceptualisation. Clay till, categorized as “clay” in the CF-inversion, can have electrical resistivities up to  $60 \Omega\text{m}$  (Jorgensen et al., 2005; Sandersen et al., 2009), which will yield a high clay fraction coinciding with a relatively high geophysical resistivity.

Electromagnetic methods are sensitive to the electrical resistivity of the formation, which is commonly dominated by clay mineral content, dissolved ions in the pore water and saturation. Groundwater quality data is available at numerous sites in the domain. Pore-water electrical conductivity (EC) values were gathered from the coast and inland following the tunnel valley. From the coast and 12 km inland values are stable around  $50\text{--}70 \text{ mS m}^{-1}$  at 28 wells with varying filter depths. Four outliers with EC ranging between 120 and  $250 \text{ mS m}^{-1}$  were identified at various locations and depths. No trend due to salinity from the coast was identified. In theory variations in formation electrical resistivity that are *not* due to lithological changes will implicitly be taken into account by spatial variation of translator function parameters.

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### 3.3 Benchmarking hydrological performance

Table 2 gives an overview of how the performance of the two models compare. The fit to discharge data of the two models is comparable. The weighted RMSE for discharge is below 1, indicating that discharge is over-fitted. The SD of discharge is 20 % of the observation, which is a conservative definition. As presented in the methods section errors may vary between 5–50 %. The 1995–1999 hydrograph and scatter plot in Fig. 10 for the 270002 gauging station show good fit to data. Peak and low flows are fitted, but baseflow recession is generally not matched very well. At gauging station 27003 the models fail to capture dynamics and relative magnitudes of the observations. Peak as well as low flows are under-simulated, which is clearly demonstrated in the scatter plot for station 270003 in Fig. 10.

The hydraulic head performance statistics in Table 2 show an improved performance of the 5-cluster model over the reference model: the calibration period RMSE/ME for the reference and 5-cluster model respectively is  $3.01/-1.01$  and  $1.99/-0.790$  m. Weighted RMSE for the reference model is 2.63 and 2.93, while weighted RMSE for the 5-cluster model is 1.63 and 1.85. The reference model thus is 2–3 SD from fitting data, while the 5-cluster model is 1–2 SD from fitting data. Assuming head observation error estimates are correct, this indicates model deficiencies such as structural errors and/or forcing data errors. The outliers in the simulated head from the reference model, Fig. 11 red diamonds, are from three wells in the elevated south-western part of the domain. Recalculating performance statistics without the outliers gives RMSE and ME of 2.45 and  $-0.647$  m. Figure 11 shows that the largest differences in simulated heads between the two models are for hydraulic head below 20 m. These observations represent the tunnel valley aquifers (see also Fig. 12a and b). Results indicate that the 5-cluster model performs better in the tunnel valley than the reference model.

Figure 12a and b show simulated head (from the 5-cluster model) and the difference in simulated head between the 5-cluster model and the reference model. Generally hydraulic head in the tunnel valley is disconnected from the elevated terrain (Fig. 12a),

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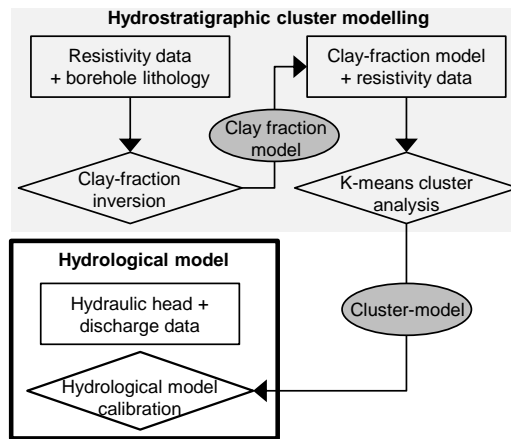


**Table 1.** Calibration parameters of the reference model. Six parameters are calibrated (column 1) to which the remaining six parameters have been tied (column 3). Initial parameters values of free and tied are shown in columns 2 and 4.

Parameter, free	Initial parameter value (m s <sup>-1</sup> )	Parameter, tied	Initial parameter value (m s <sup>-1</sup> )
Glacial sand	3 × 10 <sup>-5</sup>	Miocene sand	3 × 10 <sup>-5</sup>
Glacial clay	3 × 10 <sup>-8</sup>		
Valley sand	3 × 10 <sup>-5</sup>	Glaciotectonic sand	3 × 10 <sup>-5</sup>
Valley clay	3 × 10 <sup>-8</sup>	Glaciotectonic clay	3 × 10 <sup>-8</sup>
Palaeogene clay	1 × 10 <sup>-10</sup>	Miocene clay	3 × 10 <sup>-8</sup>
Surface clay	3 × 10 <sup>-8</sup>	Surface sand	3 × 10 <sup>-5</sup>
		Surface peat	3 × 10 <sup>-7</sup>

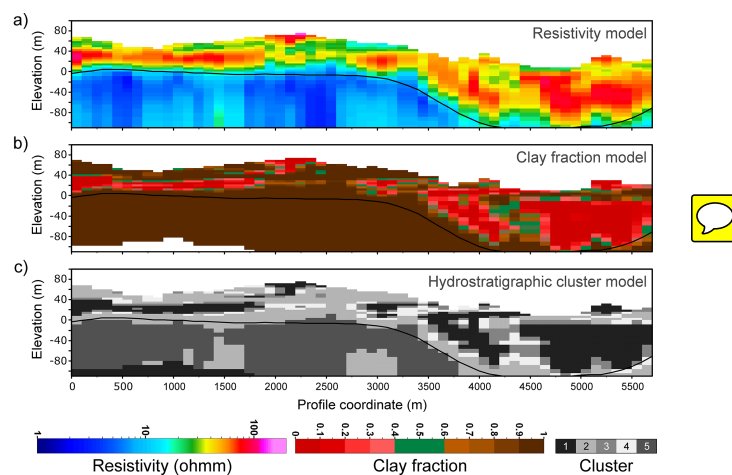
**Table 2.** Calibration and validation statistics for the temporally split sample consisting of observations from 35 wells, which have observations both in the calibration and validation period, and discharge stations 270002 and 270003.

		Reference model			5-cluster model		
		Weighted RMSE (-)	RMSE	ME	Weighted RMSE (-)	RMSE	ME
Calibration 2000–2003	Head (m)	2.63	3.01	-1.01	1.63	1.99	-0.790
	Discharge (m <sup>3</sup> s <sup>-1</sup> )	0.326	0.267	-0.0259	0.338	0.278	-0.0107
Validation 1995–1999	Head (m)	2.93	3.32	-0.816	1.85	2.24	-0.981
	Discharge (m <sup>3</sup> s <sup>-1</sup> )	0.446	0.180	-0.0501	0.524	0.203	-0.0354



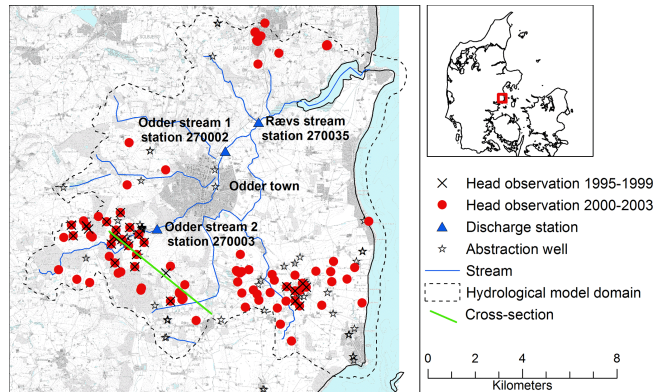
**Figure 1.** Workflow of the two main parts in the method. Top grey box; hydrostratigraphic cluster modelling using the structural information carried in the geophysical data and lithological information. Lower box in bold; hydrological calibration where hydraulic properties of the hydrostratigraphic zones are estimated using hydrological data.

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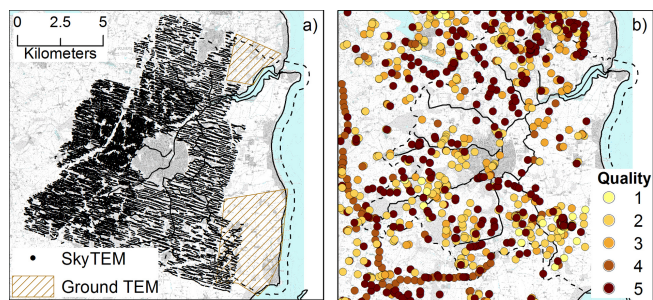
**Figure 2.** Northwest-southeast profiles (vertical exaggeration x5), location is marked in Fig. 3. (a) Resistivity model, (b) clay fraction model, and (c) hydrostratigraphic cluster model for the 5-cluster case.

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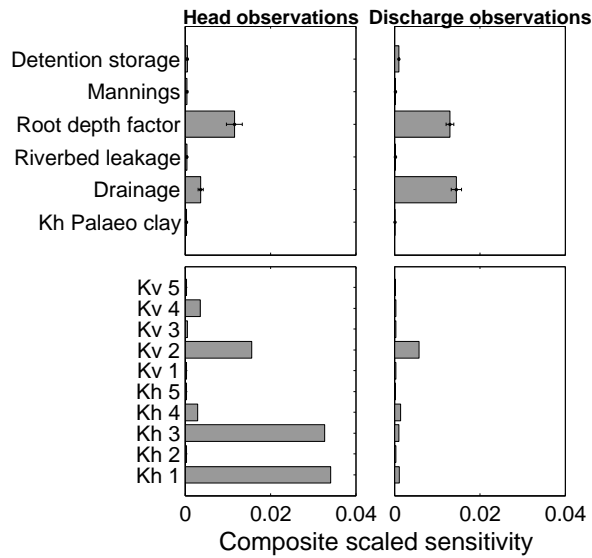
**Figure 3.** Map of Norsminde study area. The map shows the location of the three discharge gauging stations (blue triangles) along the main river, hydraulic head observations for the calibration period (red dots) and the validation period (black crosses), and abstraction wells (stars). The black dashed line delineates the model domain of the hydrological model.

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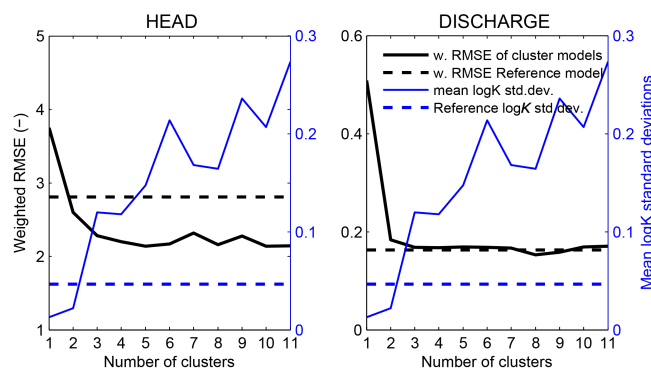
**Figure 4.** Maps showing geophysical and lithological data in the Norsminde area. **(a)** Airborne electromagnetic soundings (small black points) and the extent of the less dense ground-TEM surveys (dashed brown polygons). **(b)** Lithological boreholes used in the clay fraction inversion. Colours indicate quality of the lithological description. The black dashed line delineates the model domain of the hydrological model.

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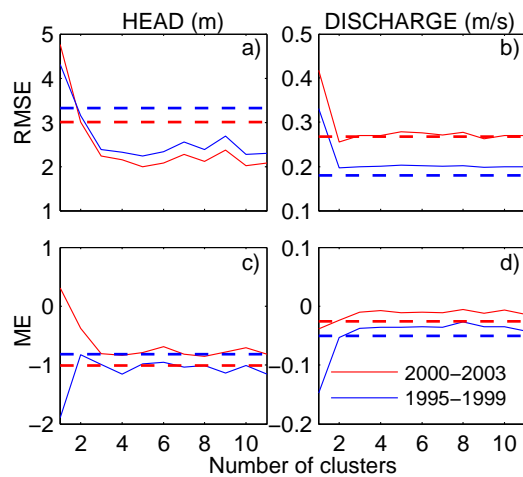
**Figure 5.** Composite scaled sensitivity values of selected parameters in the hydrological model. Sensitivities are shown for head and discharge observation separately. The two top plots show average, minimum and maximum sensitivity of the 11 hydrostratigraphic cluster models. The two lower plots show sensitivity of subsurface parameters given a 5-cluster model. Kh is horizontal hydraulic conductivity and Kv is vertical hydraulic conductivity.

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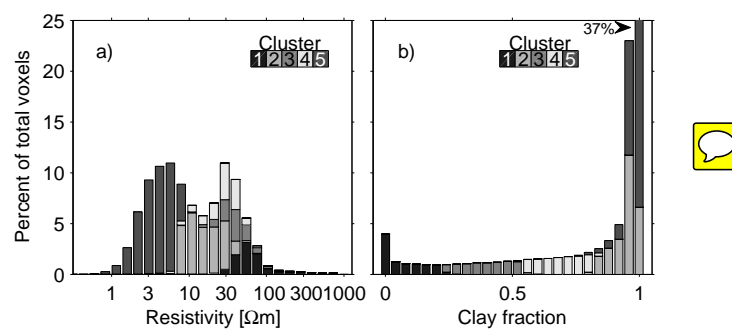
**Figure 6.** Weighted RMSE of hydrological performance of hydrostratigraphic models consisting of 1 to 11 clusters. Data is shown for all calibration observations. Horizontal dotted lines are weighted RMSE for the reference model. Blue lines are mean SD on  $\log(K)$  values; the solid line represents the cluster models and the dashed represent the reference model.

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**Figure 7.** 2000–2003 Calibration and 1995–1999 validation period performance statistics for the 11 hydrostratigraphic cluster models and the reference model. Horizontal dotted lines are reference model performance statistics. Row one is RMSE and row two is ME.

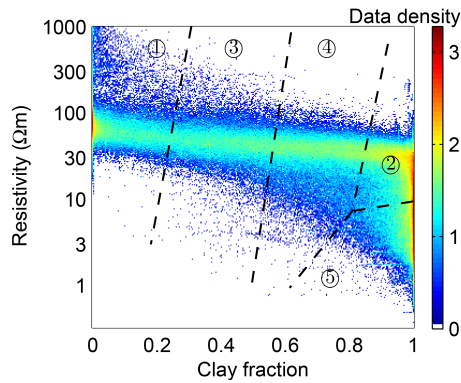
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**Figure 8.** Histograms of (a) logarithmic geophysical resistivity values and (b) clay fraction values. Cluster memberships of the values are identified by colours and the histograms thus show how resistivity values and clay fraction values are represented in the clusters. The histograms are shown as percentage of total number of data values.

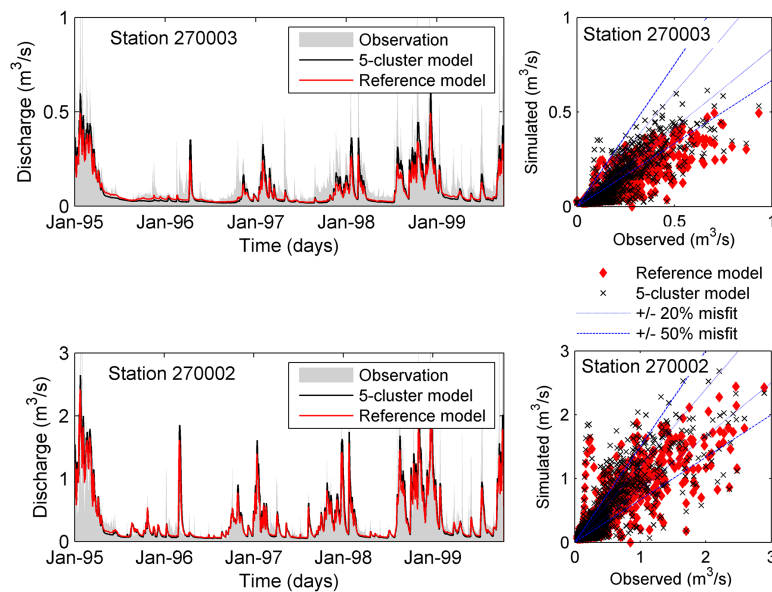
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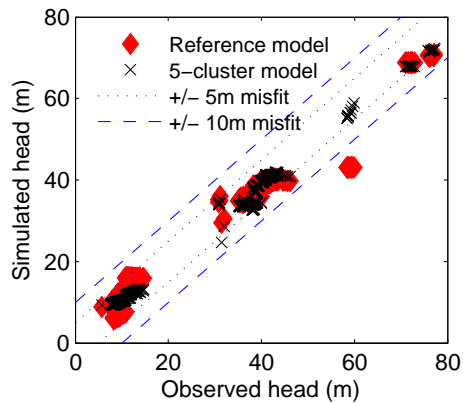
**Figure 9.** Data cloud of geophysical resistivity values and clay fraction values. Dotted black lines indicate cluster interfaces and cluster are labelled with numbers. The cloud colour represents bin-wise data density (300 bins), which is shown in logarithmic scale.

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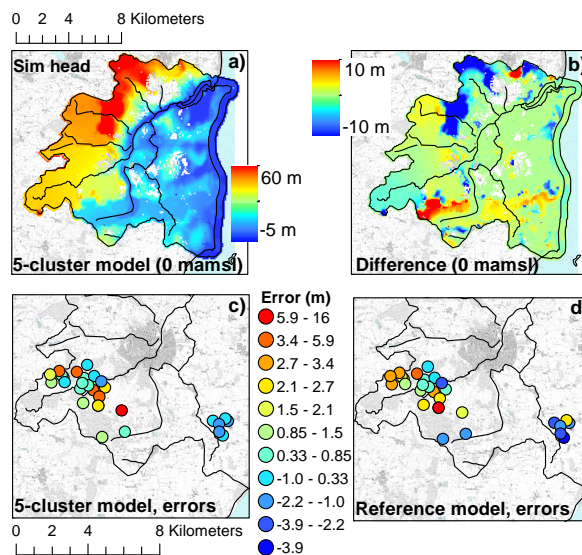
**Figure 10.** Observed and simulated stream discharge at stations 270002 and 270003 from the 1995–1999 validation period. To the left stream discharge hydrographs are shown and to the right scatter plots of observed vs. simulated values. In the scatter plots the dotted blue lines mark misfits of 20% (thin line) and 50% (thick line).

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**Figure 11.** Scatter plot of observed and simulated heads values from the 1995–1999 validation period. Dashed lines mark misfits larger than 10 m and dotted lines mark misfits larger than 5 m.

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**Figure 12.** Distributed head results for the validation period 1995–1999. **(a)** 5-cluster model simulated hydraulic head at 27 July 1997 at 0 m a.m.s.l. **(b)** Difference maps between the reference model and the 5-cluster model at 0 m a.m.s.l. (difference = reference model – 5-cluster model). **(c, d)** Errors (obs-sim) between observed and simulated head; **(c)** 5-cluster model and **(d)** reference model.

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