

Old Figure 1

New Figure 1

## Demonstration of Eq. 24:

Expressing the continuity and the total component fluxes in each branch can be further developed in Eqs. 22 and 23:

$$H_{s} = \rho c_{p} \frac{T_{s} - T_{a}}{r_{as} + r_{a}} = \rho c_{p} \frac{T_{s} - T_{0s}}{r_{as}} = \rho c_{p} \frac{T_{0s} - T_{a}}{r_{a}}$$
(22)

for the soil, and

$$H_{\nu} = \rho c_p \frac{T_{\nu} - T_a}{r_{a\nu} + r_a} = \rho c_p \frac{T_{\nu} - T_{0\nu}}{r_{a\nu}} = \rho c_p \frac{T_{0\nu} - T_a}{r_a}$$
(23)

for the vegetation.

In Kustas et al. (1999), in both series and parallel versions, stability correction is computed using the MO length L which depends on total H and total LE; in SPARSE, we use the Richardson number which depends on an average aerodynamic temperature  $T_0$  representing also the total  $H = \rho c_p \frac{T_0 - T_a}{r_a}$ . H in the parallel version is computed according to:

$$H = (1 - f_c)H_s + f_cH_v$$
(26)

where  $H_s$  is expressed according to (22) and  $H_v$  to (23).

Since 
$$H_s = \rho c_p \frac{T_{0s} - T_a}{r_a}$$
 (22b)

for the soil, and

$$H_{\nu} = \rho c_p \frac{T_{0\nu} - T_a}{r_a}$$
(23b)

for the vegetation, we have therefore (by combining 22b, 23b and 26):

$$T_0 = (1 - f_c)T_{0s} + f_c T_{0v}$$

Furthermore, (22) and (23) lead to:

$$T_{0\nu} = \frac{r_a T_\nu + r_{a\nu} T_a}{r_a + r_{a\nu}}$$

and

$$T_{0s} = \frac{r_a T_s + r_{as} T_a}{r_a + r_{as}}$$

Thus  $T_{Os}$  and  $T_{Ov}$  are slightly different (they can differ by up to 1.5 degree in our case).

Since computing  $T_{0s}$  and  $T_{0v}$  is not compulsory, we can suppress them throughout the paper and simplify the parallel model presentation by replacing the corresponding paragraph with:

"For the parallel model, the sensible heat flux rate above each patch is:

$$H_s = \rho c_p \frac{T_s - T_a}{r_{as} + r_a} \tag{22}$$

for the soil, and

$$H_{\nu} = \rho c_p \frac{T_{\nu} - T_a}{r_{a\nu} + r_a} \tag{23}$$

for the vegetation.

The value of the Leaf Area Index used for the parallel model is a "clump LAI" obtained by dividing the total LAI by the fraction cover of the vegetation  $f_c$  (Lhomme and Chehbouni, 1999). Total fluxes are the sum of the soil and vegetation components also weighted by their relative contribution,  $f_c$  for the vegetation and  $1-f_c$  for the soil:

$$LE = (1 - f_c)LE_s + f_cLE_v \tag{24}$$

where  $LE_s$  is expressed according to (20) and  $LE_v$  to (21), and

$$H = (1 - f_c)H_s + f_cH_v$$
(25)

where  $H_s$  is expressed according to (22) and  $H_v$  to (23).

The stability correction for the aerodynamic resistance  $r_a$  depends on an average aerodynamic temperature computed from the total sensible heat flux *H*:

$$T_0 = T_a + \frac{Hr_a}{\rho c_p} \tag{26}$$