## Response to Interactive comment by H. Bogena (Referee)

Comments from referee are printed in black. Authors' responses are printed in red.

## Résumé

This study concerns the application of the cosmic-ray neutron method to monitor soil moisture in a mixed forest in the lowlands of north-eastern Germany. The authors tested several calibration procedures using soil samples taken 10 times within one year inside the footprint of the sensor. A two-point calibration is assumed to be adequate to correctly define the shape of the N0-calibration function with adjusted parameters when calibration points were taken during both dry and wet conditions covering at least 50% of the total range of soil moisture.

This paper is an interesting presentation of a forest application of the cosmic-ray neutron method giving some new insights into the calibration process. It is also very well written and fits well to the scope of HESS. However, some methodological improvements need to be undertaken as outlined in my comments. In addition, the results should be better discussed in the light of existing publications on the calibration of the cosmic-ray neutron probe.

We want to thank Heye Bogena for a detailed and thoughtful review that helped in significantly improving our manuscript.

## General comments

The calibration results might have been affected by the unfavourable locations of the sampling locations. As demonstrated by Köhli et al. (2015), the highest contribution comes from the first 10 m radius, whereas the nearest sampling locations are still 25 m away from the CRNS probe. Please add a discussion on how thus soil moisture differences between the close-up area and the sampling locations might have affected the calibration results.

Fortunately, the conditions within the closest 30 m around the CRS are quite homogenous at our field site since the sensor is located within a pure beech stand. So we expect a similar range of soil moisture conditions at our sampling locations at a distance of 25 m away as compared to those at locations closer to the sensor. Thus, the near-field sampling design should not influence the calibration results. Our aim was to make the sensor work for our purposes in our environment. However, in the future we have to think about what it really is that we are measuring. Is the CRS a measuring device that can only give us reliable information on soil moisture within a radius of 10 m? Maybe the change in the shape of the calibration function that we found is also a result of trying to counteract/compensate for spatial heterogeneity. We added some of this discussion to the manuscript (in section 4.2).

The vegetation within the footprint of the CRS probe is quite heterogeneous (please add a table of the landuse contributions), which complicates the spatial averaging of soil moisture. For instance, as shown by the authors, the coniferous sites are consistently dryer compared to the areas covered by beech. Thus, the limited number of sampling locations could be an additional reason for the differences in the CRS calibrations.

This is true. We state in the manuscript that this variability within the footprint is a possible cause for the differences in our calibration results. We also tested whether an

area-weighting function based on the different tree stands significantly changes our results. We found that it did not make a difference. We will add a table of land use as recommended.

Iwema et al. (2015) already showed that using only one calibration data can lead to large uncertainties especially in humid regions with large hydrogen pools. They showed that the best trade-off between number of calibration dates and calibration accuracy can be achieved by using 6 calibration dates. Please discuss your results in the light of the results of this recent publication.

As far as we understand, Iwema et al. state that using more than 6 random sampling dates does not further improve the calibration results. They also state that using sampling dates with dissimilar moisture conditions ('appropriate soil wetness conditions') can reduce the required number of sampling dates. We found that using only 2 sampling dates with a large enough difference in soil water content suffices to achieve a good calibration. We added a discussion of Iwema et al. (2015) to the section 5.1 (lines 687-695).

This study also considers the vegetation correction developed by Baatz et al. (2015). However, since the method considers only linear scaling of the neutron counts, its application should not alter the calibration accuracy in case of temporally stable above ground biomass (as in this study). Therefore the application makes only sense where temporal biomass dynamics are expected and temporal information on biomass changes are available or in case of cosmic rover applications.

This is true. Once we had analyzed this scenario, the expected outcome (i.e. that it makes no difference) became obvious. We have removed this approach from the entire manuscript. We also tried a different approach by Baroni & Oswald which accounts for seasonally changing biomass in the weighting function. This approach also did not improve our results (probably because the amount of seasonally variable biomass in between the sensor and the soil is not large enough at our filed site).

## Specific comments

L143-145: On the web-site of the sensor manufacturer no specification of the measurement technique is given. I suspect that these sensors are actually based on an oscillator-ring as described in Qu et al. (2014) and not on the time-domain transmission technique. In addition, a problem of these sensors could be the top shielding, influencing the soil water content below. Since these kind of sensors only measure soil moisture at a very small volume (only very few centimeters around the sensor blade) this might lead to systematic underestimations of soil moisture.

According to our sensor manual the sensors are indeed based on time-domain transmission. It is hard to find other online information: <u>http://www.ibot.cas.cz/en/kalibrace\_stanice\_projekt</u>. When calibrating the sensors in the field, we actually found a systematic overestimation at low soil water contents that we corrected for. We did not detect a shielding effect which would cause an underestimation of soil water content.

L147-148: Is the sensor blade actually 15 cm long (at the web site there is no information on the seize and the pictures suggest that the sensor blade to be much shorter)

The sensor blade is actually 16 cm long.

L149: Why didn't you use all data for the calibration?

The sensors were installed in May 2014 only, so we could not use the data for the first 5 calibration campaigns.

L205-208: No scaling needed since this correction considers the relative changes in incoming neutron flux. However, the cutoff rigidity of the Jungfraujoch Station is somewhat different from the study site given is lower latitude. An good choice for the neutron monitor is be the Lomnicky station, Slovakia (LMKS).

We agree that the scaling is unnecessary. Therefore we shortened the paragraph and moved the figure to the supplements. We still use the scaled and gap-filled time series we computed since omitting the scaling does not affect the results.

L206: The correct unit for incoming neutrons is "counts/sec"

We changed all occurrences of  $n h^{-1}$  to 'counts  $h^{-1}$ '. To stay consistent and avoid confusion we also use hours for the incoming flux corrections.

L224: The methods to determine soil organic carbon and root biomass water equivalents are not presented.

A description of the methods has been added. (See lines 190-195)

L230: This statement is too vague. I think what you meant here is that the objective performance measure is minimized, right?

True. The sentence was removed since we decided to omit the last approach.

L315: What about the other tree species?

We added to the text (Line: 342): 'We did not conduct surveys on the other tree species. Table 1 shows that the beech stand covers 56% of the footprint area around the CRS (when assuming the exponential distance-weighting from Zreda et al. (2008)). Pine covers 16%, spruce 13%, oak 8%. With the new distance weighting function of Köhli et al. (2015), the cover fractions of the other tree species will decrease even further. Also, the seasonal variation in spruce and pine above-ground biomass is very small and thus we consider it to be constant in this study.'

L317: On which grounds did you assume these values?

These values are taken from the literature (papers by Gravano et al. (1999) and Bouriaud et al. (2004)). See line 320.

L359: The correct unit for incoming neutrons is "counts/sec" Corrected in the revised manuscript.

L380: Change to "the same value for the N0 calibration parameter" Changed to: 'Following the standard N0-calibration approach of Desilets et al. (2010), we should have ended up with the same N0 value for each of the 10 calibrations.' L381: The correct unit for the CRS measured neutron intensity is "counts/h" Corrected in the revised manuscript.

L382-387: According to Zreda et al. (2012) the presence of other hydrogen pools than soil moisture increases the stopping power of the soil, which leads to a change in the slope of the calibration function. Thus, calibration has to be performed using the total hydrogen pool, and soil moisture is then computed by subtracting other hydrogen pools than soil moisture from the measured neutron-derived soil moisture. It is unclear whether this procedure was applied in this study. If not, this would partly explain the differences in soil moisture estimates.

As outlined in the description of our four approaches (esp. Lines 267-285), we used the total hydrogen pool for calibration before subtracting other than soil moisture contributions according to Eq. 4 (Line 240).

L388: The term "new calibration function" is misleading. Changing the "a" parameters of the N0 calibration function is not new and was already presented by Iwema et al. (2015). They called this more adequately "modified N0 method". However, they only calibrated 3 parameters (the N0 parameter was omitted), because of strong correlations between the parameters leading to ambiguous calibration results (equifinality problem). Did you check for this calibration issue?

You are right that 'new calibration function' is misleading. We changed all occurrences to 'modified calibration function'. It is true that the N0 parameter has a very similar influence on the shape of the calibration function as the a0 parameter. Still we don't think that in this case equifinality (we agree that it exists) is a real problem for this application because the goal of the calibration simply is to find an efficient function that represents the calibration points. There is no reason to consider any potential adverse implications of the adjusted parameter values or combinations of them. As a side note: we also tested whether simple exponential or gamma functions would perform as well as the 4 parameter calibration function and we found that they in fact did not. So there seems to be justification for the specific set of shapes that is described by the N0-calibration function.

L400-402: Do you have any idea why?

Yes. If you look at Fig. 5 you see that at higher water content a smaller change in neutron counts is associated with a larger change in soil water content (the function is steeper). Therefore the uncertainty during the calibration is also larger.

L414-416: Please provide a figure showing the comparison. We have prepared a figure and added it as a supplement (Fig S2).

L422-424: Shouldn't the relationships vary with soil moisture content due changing sensor penetration depths?

Yes, that is what we expected and that is also what we found for the first two approaches. When it is wetter, the penetration depth is reduced for the CRS measurements and the wetter shallower layers receive more weight. Therefore, the CRS measurements show higher SWC than the gravimetrically determined SWC. However, it seems that the distance weighting counters this effect. A probable explanation is that the

formula used for the distance-depth weighting increases the critical depth. This causes higher weights for deeper (drier) soil layers even under wet conditions and could counteract the trend.

L429-430: This finding is quite obvious given the insignificant changes in above biomass. Generally, the application of the vegetation correction makes only sense, when temporal biomass dynamics are expected and temporal information on biomass changes are available.

We removed the whole part on vegetation correction.

L441: This investigation is very similar to Iwema et al. (2015). Please discuss your results in the light of this study. We added a discussion in section 5.1 (lines 687-695).

L450-457: The results plotted in Fig. 12 show clearly, that only the most extreme dry and wet samplings result in an acceptable calibration result, whereas sampling at intermediate soil moisture will lead to very uncertain calibration of the modified N0-method. On the other hand, this illustrates the value of the standard N0-method that will also produce stable results in case only one sampling date is available. Please add this to the discussion.

Fig. 9 shows that the best 2-point-calibrations are achieved with one sampling point taken under very dry conditions and another sampling point taken either under intermediate or wet conditions. In our case it is hard to see the value of the standard N0-method since it always resulted in too much soil moisture variability no matter whether the calibration was performed during wet, intermediate or dry conditions (because the standard calibration of N0 does not allow a change of the slope of the calibration function).

L458: This chapter belongs to discussion.

We moved parts of this chapter to discussion and only left the parts that really describe results. We also added results on other hydrogen pools, so we renamed the chapter.

L471-474: This is only true when assuming that the CRS footprint is completely covered by beech, which is however not the case.

This is true. So for this calculation, we assume an extreme case since the other vegetation types experience smaller seasonal changes in above-ground biomass. In reality we should expect even less variation in neutron counts due to foliation/defoliation. We will add this statement to the revised manuscript.

L484-485: So the whole discussion of this chapter is unimportant and should be reduced to 1-2 sentences.

Would you say that just because our results suggest that seasonally-varying aboveground biomass does not influence the neutron count significantly the discussion of this finding is not important? We think this finding is very important for the use of CRS in forested areas and worth the extended calculation and discussion. (In the end, it makes life much easier when applying CRS in forests).

L488-518: This section is a summary, not a discussion and thus should be omitted.

We restructured the discussion section.

L520-528: Please discuss your results in the light of the results found by Iwema et al. (2015).

We added a discussion of the findings of Iwema et al. (2015).

L558-560: This statement is not clear to me. Please explain in more detail.

We changed and added more detail: 'Following the argumentation of Lv et al. (2014), the fact that distance weighting improved our results can be regarded as an indication that non-homogeneous soil moisture conditions indeed lead to changes in the shape of the calibration function. At our site distance weighting reduced the spatial variability within the footprint of the sensor since it assigned higher weights to the closest sampling sites which were all located in the homogenous and relatively wet beech forest, while the influence of the drier soils under the coniferous trees was reduced.'

L564-569: This part is somewhat misleading. Corrections of the neutron count rate (Eqs. 1-3) are essential for any application of the CRS (e.g. Zreda et al., 2012). Vegetation correction is only needed for sites with significant biomass changes. On the other hand, the characterization of the temporal stable hydrogen pools is important for the application of the N0-method. However, the abundance of different pools and the uncertainties in the sensing depth estimation will always lead to uncertainties in the sensing depth estimation will always lead to uncertainties in the study, this issue can be partly circumvented by the using site specific calibration parameters estimated at using in-situ samples taken during dry and wet conditions. Please reformulate in this sense.

Changed to: 'If it was possible to fully correct for all factors that influence footprint size, depth-weighting and neutron count, a one-time calibration of the CRS would be sufficient. However, the abundance of different hydrogen pools and the uncertainties in the sensing depth estimation will always lead to uncertainties in the calibration process. Therefore we argue that for using the CRS as a simple tool to measure soil water content at intermediate scales, the efforts of measuring all necessary parameters are not justified. As shown by Iwema et al. (2015) and by the results of this study, this issue can be partly circumvented by using site-specific calibration parameters estimated from insitu samples taken during dry and wet conditions. Hence, we recommend a two-time calibration that – although being empirical in nature – inherently incorporates many of the required corrections.'.

L583-584: Actually, the seasonal changes of the hydrogen pools in this forest site are negligible. Thus vegetation correction can be omitted. Agreed.

L594-600: This statement is based on Köhli et al. (2015), but not on results of this study and thus should be omitted.

Since this a very important statement and should be considered by everybody using a CRS, we would like to keep it. But we added the proper reference (Köhli et al.).

L606-608: This step is obvious and should be omitted.

When we first set up the sensor and calibrated it for the first time we brought a battery with us to let the sensor run. After we had finished the soil collection, we took the battery back home with us. Only later it became clear that we should have collected neutron counts for a longer period of time. So we could not use the data from our first calibration effort. This was a hard lesson to learn and we want to make sure that other people do not make the same, admittedly stupid, mistake.

L614: The sampling locations should be adapted to the footprint estimates after Köhli et al. (2015).

We adapted the sampling distances to the footprint estimates after Köhli et al. (2015).

Figures

Figure 1: This map should be integrated in figure 2. Done.

Figure 1: According to recent results of Köhli et al. (2015) the footprint is considerably smaller than 300 m. Please adapt the figure. In addition, it would be helpful to color the aerial photograph according to the different tree species.

The figure was changed accordingly. Since this figure is also supposed to illustrate our sampling scheme we would like to keep the 'old' footprint size. To make the difference clear we rephrased: 'The yellow circle approximates the footprint of the CRS as it was assumed when sampling took place'. The distribution of different tree species can be seen on Fig. 3 and it would probably make this Figure too busy adding colors or patterns on top of the photograph.

Figure S1: This figure can be omitted (see comment L205-208) We have moved the Figure to the Supplement (S1).

Figure 2: This schematic figure is wrong in presenting the cosmic-ray neutron intensities as actual rays that are reflected by the soil. The actual processes leading to neutron intensity are far more complex (see e.g. Köhli et al., 2015) and should not be presented in this way in a scientific paper. Also the above ground and below ground footprints are not connected in the simple way as suggested by the schematic drawing. Thus, the figure should be omitted.

We acknowledge the fact that this figure simplifies the actual processes a lot and have added this statement to the caption. We have modified the figure to resolve two of your concerns. The neutron intensities are not any longer depicted as rays and the aboveground footprint was removed entirely. We still think that the figure helps to get an overview over the many parameters that have to be accounted for before/during the use of the CRS method.

Figure 9: The Pareto front needs to be discussed in the text as well.

We realized that it is actually not a Pareto front. So we added to the text: 'The existence of a rather clear front in Fig. 9 indicates that the calibrated neutron count-soil water content conversion will always perform well if the soil moisture differences between the two calibrations are sufficiently large.'

## Response to Interactive comment by Anonymous Referee #2

Comments from referee are printed in black. Authors' responses are printed in red.

The authors present a straight forward paper looking at mutil-calibration estimates and methods for a study site in Germany. While the methods in the paper have been previously tested in a variety of ecosystems around the globe the application to this particularly ecosystem is insightful and help further advance the CRNP method. In particular, this site contains a relatively large amount of the total hydrogen in the forest canopy given the sandy and dry soils. The paper is well written and appropriate for the HESS community. My comments and assessment largely follow Heye Bogena so I will only add new comments here or reiterate key points.

We thank reviewer #2 for assessing our manuscript and for providing useful comments on how to improve it.

Major:

The site is interesting in that a potentially a large part of the hydrogen is contained in the biomass instead of the pore water content. A figure like Figure 3 in McJannet 2014 WRR for each calibration data point would be interesting to look at. In addition, perhaps some of the bias in the N0 parameter is because of how hydrogen is more distributed in the clumped biomass instead of distributed throughout the soil. Plotting the differences of N0 vs. relative biomass hydrogen to total hydrogen ratio might show this influence. Franz 2013 GRL supplemental figure S2 illustrated the influence of neutron intensity/counts due to clumped hydrogen in the tree canopy vs. more distributed hydrogen in the soil. Perhaps these detailed calibration datasets might help validate or refute these modeling results.

Very good suggestion. We prepared a figure (similar to the one of McJannet) for 3 distinct soil moisture conditions and added it (Fig. 11). In order to do this we refined our calculations of the different hydrogen pools (now also including SOM, lattice water as well as canopy and litter interception) and also added more detail to the discussion. This new analysis supports the idea that interception can have a significant influence on soil water content measurements performed with a CRS.

The conclusion that the deviation of a single calibration point is upwards of 0.12 m3/m3 is technically correct at the wet end. However, this is a bit misleading given that the neutron counts are never this low or soil moisture this high, particularly at the daily average level, because of the sandy soils. I suggest the authors use the min and max observed counts to properly assess the maximum uncertainty of the method. Looking at Figure 6 it looks like the CRNP never reads above 0.27 m3/m3. All in all, this a fairly small change. Also might be more useful to look at percent absolute error instead of just the difference.

We modified this section stressing the fact that 0.12 m<sup>3</sup>/m<sup>3</sup> is the largest deviation that we observed. Due to the sandy soils, the absolute range of soil water content is fairly small at our site. Following your suggestion we changed absolute error to percent absolute error both in the figure and in the text.

Comment: For timescales below the daily level, and thus estimates of the peak soil moisture, clearly some cleaver smoothing filters are needed to estimate the "true peak"

and separate out the signal from the noise. This estimation of the true peak will help constrain things like calculating effective infiltration flux and maybe even runoff depths for water balance studies using the CRNP data.

This is true. We hope that such clever smoothing filters will be developed in the future to provide us with the true peaks using additional information (like time series of precipitation).

The method of determining lattice water by weighing the sample at 105, 400 and 1000 C has not been used by the USA COSMOS community (pg9820 L 18-30). Are they any refs suggesting this is a defensible method compared to the more rigorous approach used by Actlabs? I suspect this difference will be small here as you account for the burn off of carbon. However, for certain soil groups (volcanics?) I imagine this might be problematic. Please add any supporting refs or comment on the pragmatic approach taken here vs. the more rigorous laboratory approaches taken in previous COSMOS work.

The method to determine SOM proposed in this paper is officially called the loss on ignition method. We chose this method since it is indeed pragmatic and does not require the acquisition and handling of toxic chemicals (like for example the Walkley-Black method does). References that describe this method are for example Ball (1964), Ben-Dor & Banin (1989), Davies (1974), Howard & Howard (1990), Schulte et al. (1991). In clay-rich soils the loss on ignition method overestimates SOM content since also some of the lattice water evaporates. This leads to an underestimation of soil hydrogen content (since lattice water contains a higher fraction of hydrogen than soil organic matter). One complication for calcareous soils is the thermal breakdown of carbonates at high temperatures. Although this thermal breakdown can be avoided at temperatures below 430°C (Davies, 1974) at temperatures above that the burned off carbonates would contribute to the lattice water account. We still think that the results obtained with this method provide good estimates of SOM and LW for our purposes with minimal error for most soil groups.

### Minor:

P9816 L25. Already is awkward transition. Maybe something like "As early as 1966. . ." Changed accordingly.

P9837 L8. Franz 2013 WRR investigated the impact of horizontal heterogeneity on the signal.

We are discussing the topic of horizontal heterogeneity in lines 724-739. Here, we are just comparing the count rates of different studies (and in Franz et al. (2013) the lowest count rates are also above 1000 cph).

P9839 L21-25. Again, is this method for lattice water supported by refs? If not then should be noted that this is a pragmatic procedure with expected minimal error for most soil groups other than volcanics, . . . etc. (?). Unfortunately I don't know all the soil groups this might be affected by so hopefully a pedologist can set us straight.

The method of heating the samples to a temperature of 1000°C to determine lattice water was used in many CRS studies (e.g. Zreda et al., 2012; Bogena et al., 2013). The only complication we found occurs in carbonate-rich soils where thermal breakdown of

carbonates will contribute to the lattice water account. We will add two cautions to the recommendations we give in the appendix.

## Response to Interactive comment by Anonymous Referee #3

Comments from referee are printed in black. Authors' responses are printed in red.

The manuscript describes an improved calibration of cosmic-ray soil moisture probes. The problem of calibration has surfaced many times before and different scientists have proposed improvements. But even with those improvements, some problems have remained. This paper adds a valuable component to the growing body of knowledge of how cosmic-ray neutrons respond to surface moisture and how best to calibrate the response functions. The work described in the paper is thoughtfully designed and carefully executed and analyzed. The conclusion is simple, but important: calibration function is different than that originally proposed, and that difference can be captured by doing only two calibrations at two different levels of soil moisture. The good quality of work and the important conclusion make the paper important. I recommend that it be published with minor revisions suggested on the annotated copy (attached).

Thanks to reviewer #3 for a considerate and helpful review that helped in improving the paper.

Line 9: this is instrument, not technique. The technique is "measuring soil moisture with cosmic-ray neutrons".

Changed to: 'Measuring soil moisture with cosmic ray neutrons is a promising technique for intermediate spatial scales.'

Line 12: Desilets' function was computed using MCNPX Changed to: 'The calibration is based on soil water content derived directly from soil samples taken within the footprint of the sensor.'

Line 21: this conclusion is based on ten calibration data sets, but these ten sets span a narrow range of average soil moisture values between 7% and 16% (Fig. 3) - so how solid is this conclusion?

Soil moisture in our very sandy soils only ranges between 5% and 25%. So although 16% still appears to be on the dry end (when comparing it to more silty/clayey soils) we are covering 50% of the total range of possible soil moisture. Moreover, it will be difficult to calibrate at even higher soil water contents since they usually only appear for a short period of time after large precipitation events. At that time, however, conditions for calibration are not optimal since there will still also be intercepted water in the canopy and litter layer. Also, keep in mind that the values on Fig. 3 are non-weighted averages of all 108 soil samples. The weighted averages used for calibration range from 8% to 22% (see Table 4, column:  $\theta_{depthW}$ ). We added some of this information to the manuscript in chapter 4.1.

Line 32: meaning? seems unnecessary Agreed. Removed.

Line 34: the largest spatial variance is usually at intermediate moisture levels, and decreases towards both dry and wet ends

Changed to: '...especially under intermediate wetness conditions...'

Line 37: delete "very". perhaps rephrase this to provide more specific information, for example: "this is time-consuming and expensive" Changed to: 'This can be time-consuming and expensive.'

Line 45: not from the sun (not energetic enough to produce cascade neutrons); say something like "Cosmic-ray neutrons on Earth are formed by high-energy protons coming from galactic sources, such as supernovae." cascade neutrons are high-energy neutrons, not fast neutrons. Fast neutrons are produced by secondary neutrons via the process of evaporation. So the fast neutrons are tertiary neutrons, by that term is not used; term evaporation neutrons is used instead.

Thanks for this clarification. This is quite complicated. Changed to: 'Cosmic ray neutrons on Earth are formed when high-energy protons deriving from galactic sources (such as supernovae) enter the Earth's atmosphere. Once in the atmosphere, the protons interact with atomic nuclei (mainly nitrogen and oxygen) producing cascades of secondary neutrons (also called high-energy neutrons) that travel towards the Earth's surface and into the soils. When secondary neutrons interact with air or soil they trigger the release (evaporation) of fast (but low-energy) neutrons.'

Line 61: specify that Kodama's detector was buried in the soil. Added: '...with a neutron sensor buried in the soil.'

Line 63: larget than what? perhaps say "large" or specify that area (~30 ha). Added: '...(~30 ha)...'.

Line 68: this is not appropriate reference; the range 10 cm - 70 cm was given in Zreda et al., 2008. Also, the dependence on soil water content was specified, but not dependence on soil type and distance from sensor. Koehli et al., 2015 worked out the dependence on distance.

Exchanged the references.

Line 102: why unwanted? perhaps better to say "adds additional signal" that complicates analysis (or complicates extraction of soil moisture signal).

Changed to: '...and adds additional temporal variability to the CRS time series complicating the extraction of the soil moisture signal.'

Line 108: please make sure that this is true; I think the idea is to fix the calibration parameter at the high end (water), rather than low end (dry soil, in Desilet's calibration function), but that is a regression parameter, not measured value.

In the 2013 paper they say that this parameter can be easily retrieved from measurements over a large water body. We think you are right in noting that it is in fact a regression parameter. So we changed the wording to make this clearer.

Line 135: Are they applicable also at the site? 1.6 km seems close, but precipitation and humidity can vary at smaller scales.

We compared the climate data with data we collected ca. 400 m away from our site and the differences were marginal. We decided to use the data from 1.6 km since it was a longer data set (we only installed the 400 m sensors in the middle of 2014).

Line 175: and assuming the sensitivity decrease with distance given in Zreda et al., 2008, for the footprint radius of ca 300 m. The new footprint estimate by Koehli et al., 2015, gives smaller footprint, so the sampling distances for equal weights will be smaller than your 25 m, 75 m and 200 m.

This is true. We now discuss this in more detail later in the manuscript (see Section 4.2):' Sampling distances with equal weights according to Köhli et al. (2015) would have differed from our sampling pattern (~1 m, ~33 m, ~140 m instead of 25 m, 75 m, 200 m), a condition which we balance by adjusting the distance weights. Furthermore the conditions within 30 m around our CRS are quite homogenous since the sensor is located within a pure beech stand and we are expecting little difference in soil moisture content between locations at 1 and 25 m distance.'

Line 204: this correction uses shielding depths (g/cm2), not pressure (hPa); however, the difference in this case would be cosmetic (or zero, if the value of 133.3 hPa was obtained from the equivalent shielding depth), so it does not matter for the results; on the other hand, if you want to be consistent with cosmic-ray literature, please make the change to shielding depth.

We changed the units to shielding depth. Thanks for providing us with the conversion factor.

Line 207: reference Zreda et al., 2012 for this correction Added the reference.

Line 216: this difference (309 vs 327) cannot possibly be due to difference in altitude between the monitors (which should be a factor of four or more). I think these data sets are pressure corrected, and the difference idiosyncrasies of the two neutron monitors. Deleted the mention of altitude.

Line 219: reference Rosolem et al., 2013 for this correction Reference to Rosolem et al., 2013 is now given.

Line 320: is this 0.6 kg of H2O per kg of dry biomass? or wet biomass? clarify. It is actually 0.6 kg of H2O per kg of wet biomass. We clarified this in the manuscript.

Line 321: this seems low. does this figure include free water (H2O in xylem) and cellulose-bound water (OH group)?

No, this just includes free water. The cellulose-bound water is calculated in the next step (assuming hydrogen content in dry biomass is 0.0622 kg kg-1).

Line 335: isn't there a seasonality or some other temporal variability (eg, with droughts) in the free water within trunks and branches?

Yes, there is some seasonality also in this regard (there is even daily fluctuations indicating variations in transpiration flux). This, however, was not part of our analysis since it is difficult to determine the exact numbers and it is likely that these variations are too small to influence the neutron count.

Line 342: This section should provide more information, not just the equation. What is KGE? How is it used? What is compared with what? How are these variables computed (eg, r)? What is the significance of the result? Etc...

$$r = \frac{\sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2} * \sqrt{\sum_{i=1}^{n} (y_i - \bar{y})^2}}$$

We added the equation for the correlation coefficient r and some more information on the KGE': 'The KGE' measures the Euclidian distance in a 3-D space where the correlation coefficient r is on one axis, the variability ratio  $\beta$  is on the second axis and the bias ratio  $\gamma$  is on the third axis. KGE' scores range from 1 (representing a perfect fit) to -  $\infty$ . Due to the composite nature of the KGE' it is relatively simple to analyze which feature of the time series (correlation, bias, variability) contributes most to the good/bad performance of a model.'

Line 398: this is inaccurate; one time series shown in Fig. 7 has differences of that magnitude, whereas the other nine have considerably smaller deviations; please, state this result correctly, without creating undue alarm.

You are right in that our formulation is unclear and could be interpreted in different ways. So we will modify the statement: 'As a consequence, the 10 computed time series based on the standard N0-calibration function of Desilets et al. (2010) also showed differences in volumetric soil water content (Fig. 4 illustrates results for the DDW approach). In the most extreme case, these differences were larger than 0.1 m3 m-3 (which is equal to 30 % of the total range of soil water content at the site).'.

Line 403: It is unclear how this conclusion was reached. Please describe in detail what was done, what were the results and how to interpret them.

We conclude that there is no unique calibration parameter and describe the calibration procedure in detail in the methods section (lines: 256-303). The results are presented in Table 5 and Fig. 4 & 5. We will add a more detailed interpretation of the results to the discussion section.

Line 420: There is a lot of noise in Figure 5 and the difference between standard N0 and the improved data is not clear. Can you add error bars to the data points? We are not sure about this comment. In our view, this difference between the standard and the modified calibration functions is clearly represented by the dotted and the solid lines respectively. Since there is already a lot going on in this figure, we decided not to add error bars and we were not sure of the added value they would provide.

Line 553: The absolute count rate has no influence on the shape of the response function, just on the precision of calibration. I would remove this conclusion or reword it to make this conclusion ("it clearly does not at our site") less strong. Ok. We removed this conclusion.

Line 564: but on page 9831 (of my copy) you stated that the sensitivity is better when using your calibration. Please, make these two statements consistent. On page 9831 we stated that the sensitivity of the sensor is essentially higher than it should be (not better). This means that already a small difference in neutron counts indicates a large difference in soil moisture. The modified calibration accounts for this by decreasing the slope of the calibration function and thereby reducing the sensitivity of the sensor (so that now a bigger difference in neutron counts is required to cause differences in the soil water content reading). We modified our statement on page 9831 (= manuscript line 475) to: '...essentially the sensor has a higher resolution/sensitivity than one would expect.'

Line 642: Franz et al 2012 is not the correct reference; Franz et al merely repackaged the information given in Zreda et al 2012.

We decided to recommend sampling distances according to Köhli et al. (2015). Concerning the sampling pattern we used: Franz et al. 2012 describe 3 circles with distances around the CRS of 25, 75 and 200 m. Zreda et al. 2012 describe 3 circles with distances around the CRS of 25, 75 and 175 m. Since we used 25, 75 and 200 m the more correct citation to describe our calibration setup would be Franz et al. 2012. However, to recognize the contribution of Zreda et al. we inserted the reference in line 174: '…we followed the recommended sampling pattern for the calibration of CRS which was developed by Zreda et al. (2012) and slightly modified and detailed in Franz et al. (2012b).'.

### Table 4: Insert line!

I would love to. Actually there was a line when we submitted the manuscript. But it seems that HESS does not allow lines within tables. However, I will try to convince them to leave this line in there because I also think it is necessary.

Table 5: I am not sure how to read these results. Can you clarify in the figure caption or in text (which also glosses over this in one short paragraph at the end of section 4.3). We modified the text to make the table clearer: 'All resulted in largely deviating N0-values between the individual calibrations (see means and standard deviations in column 1 and 2 of Table 5). This in turn led to differences in the time series of volumetric soil water content between the individual calibrations (see means and standard deviations in column 3 and 4 of Table 5).'

Fig. 2: can you group these factors into two groups: (1) constant in time (eg, WL), and (2) variable in time (eg, water vapor)? And then perhaps also into another groups: (3) those measured at calibration (eg, WL), and (4) those measured as time series (eg, water vapor)? The significance is that some parameters are easy to handle, others are difficult, and the two should not be commingled.

We revised the figure according to your suggestions. We grouped the factors into two groups and mentioned which of them need to be monitored continuously and which can be accounted for during calibration.

Use of cosmic ray neutron sensors for soil moisture
 2 monitoring in forests

#### 3

### 4 Ingo Heidbüchel<sup>1</sup>, Andreas Güntner<sup>1</sup>, Theresa Blume<sup>1</sup>

5 [1] {GFZ German Research Centre for Geosciences, Helmholtz Centre, Potsdam, Germany}

6 Correspondence to: I. Heidbüchel (ingo.heidbuechel@gfz-potsdam.de)

7

### 8 Abstract

Measuring soil moisture with cosmic ray neutrons sensors (CRS)-isare a promising technique to 9 measure soil moisture at for intermediate spatial scales. To convert neutron counts to average 10 volumetric soil water content a simple calibration function can be used (the  $N_0$ -calibration of 11 12 Desilets et al., 2010). Theis calibration function is based on soil water content derived directly from soil samples taken within the footprint of the sensor. We installed a cosmic-ray neutron 13 sensor (CRS) in a mixed forest in the lowlands of north-eastern Germany and calibrated it 10 14 times throughout one calendar year. Each calibration with the  $N_0$ -calibration function resulted in 15 a different CRS soil moisture time series, with deviations of up to 24 % of the total range  $0.12 \text{ m}^3$ 16  $\mathbf{m}^2$  for individual values of soil water content. Also, many of the calibration efforts resulted in 17 time series that could not be matched with independent in situ measurements of soil water 18 content. We therefore suggest a modified<del>new</del> calibration function with a different shape that can 19 vary from one location to another. A two-point calibration proved to be adequate to correctly 20 define the shape of the modifiednew calibration function if the calibration points were taken 21 during both dry and wet conditions covering spanning at least 50 % half of the total range of soil 22 moisture. The best results were obtained when the soil samples used for calibration were linearly 23 24 weighted as a function of depth in the soil profile and non-linearly weighted as a function of distance from the CRS, and when the depth-specific amount of soil organic matter and lattice 25 water content was explicitly considered. The annual cycle of tree foliation was found to be a 26

Kommentar [A1]: Rev3: this is instrument, not technique. The technique is "measuring soil moisture with cosmic-ray neutrons"

Kommentar [A2]: Rev3: Desilets' function was computed using MCNPX

Kommentar [A3]: Rev3: this is very important for users

Kommentar [A4]: Rev3: this conclusion is based on ten calibration data sets, but these ten sets span a narrow range of average soil moisture values between 7% and 16% (Fig. 3) so how solid is this conclusion?

**Kommentar [A5]:** Reply: Soil moisture in our very sandy soils only ranges between 5% and 25%. So although 16% still appears to be on the dry end (when comparing it to more silty/clayey soils) we are covering 50% of the total range of possible soil moisture. Moreover, it will be difficult to calibrate at even higher soil water contents since they usually only appear for a short period of time after large precipitation events. At that time, however, conditions for calibration are not optimal since there will still also be intercepted water in the canopy and litter layer. Also, keep in mind that the values on Fig. 3 are non-weighted averages of all 108 soil samples. The weighted averages used for calibration range from 8% to 22% (see Table 4, column:  $\theta_{depthW}$ ). We added some of this information to the manuscript in chapter 4.1. negligible factor for calibration because the variable hydrogen mass in the leaves was small
compared to the hydrogen mass changes by soil moisture variations. <u>As a final pointFinally</u>, we
provide a best practice calibration guide for CRS in forested environments.

30

### 31 1. Introduction

Measuring Determining average soil moisture content comprehensively over larger areas is 32 difficult, mainly for two reasons. Firstly, soil moisture can be highly variable already even at 33 34 small <u>spatial</u> scales, especially <u>under intermediatedry wetness</u> conditions (e.g. Western et al., 2004). Secondly, most common in situ measurement techniques only yield point measurements. 35 To obtain a valid estimate of area-average soil moisture one needs to collect data from numerous 36 37 locations within a given area. This can be very-time-consuming and expensive-cumbersome. More recently, remote sensing of soil moisture at larger scales has become a research focus (e.g. see 38 Ochsner et al., 2013 for a recent review); however, up to this point the measurement depth of 39 40 many of these methods is still limited to the upper 5 cm of the soil. Also, both spatial and temporal resolution is rather coarse. A technique that intends to bridge the scale gap between 41 point measurements of soil moisture and remote sensing is the use of cosmic ray neutrons as 42 indicators of soil moisture. A detailed description of the functioning of the cosmic ray neutron 43 sensors (CRS) can be found in Zreda et al. (2008, 2012), here we will only describe the basic 44 measurement principle. Cosmic ray neutrons on Earth are formed when high-energy 45 protonscosmic ray particles deriving from the sun (and also from other galacticxies) sources 46 (such as supernovae) enter the Earth's atmosphere. Once in the atmospherethere, the protonsy 47 start interacting interact with other atomic nuclei (mainly nitrogen and oxygen) producing 48 cascades of secondary<del>fast</del> neutrons (that are also called high<del>low</del>-energy neutrons) that travel 49 towards the Earth's surface and into the soils. When secondary neutrons interact with air or soil 50 they trigger the release (evaporation) of fast (but low-energy) neutrons. The number of fast 51 neutrons above the soil surface depends strongly on the number of hydrogen atoms in the 52 surroundings because hydrogen atoms have a very high capacity to moderate fast cosmic ray 53 neutrons (that means to slow them down and turn them into thermal neutrons with even less 54 energy – effectively removing the fast neutrons from the system). The number of hydrogen atoms 55 increases with increasing soil water content and hence soils with high water contents re-emit 56

Kommentar [A6]: Rev3: meaning? seems unnecessary

Kommentar [A7]: Rev3: the largest spatial variance is usually at intermediate moisture levels, and decreases towards both dry and wet ends

Kommentar [A8]: Rev3: delete "very"

perhaps rephrase this to provide more specific information, for example: "this is time-consuming and expensive"

Kommentar [A9]: Rev3: not from the sun (not energetic enough to produce cascade neutrons); say something like "Cosmic-ray neutrons on Earth are formed by high-energy protons coming from galactic sources, such as supernovae."

Kommentar [A10]: Rev3: cascade neutrons are high-energy neutrons, not fast neutrons. Fast neutrons are produced by secondary neutrons via the process of evaporation. So the fast neutrons are tertiary neutrons, by that term is not used; term evaporation neutrons is used instead.

2

fewer fast neutrons than soils with low water content. That leads to fewer fast neutrons being 57 detected above-ground by the CRS which is generally installed 1-2 m above the soil surface. 58

#### Already in As early as 1966 Hendrick and Edge reported that the intensity of fast (low-energy) 59

neutrons (~1 keV) detected above the- ground depended on the hydrogen content of the soil, and 60

Kodama (1985) found an inverse correlation of neutron intensity and soil moisture content 61

whenith a burying a neutron sensor buried in the soil. In 2008, Zreda et al. introduced a method to 62

measure average soil water content over a larger area ( $\sim$ 30 ha) with CRS. The footprint of CRS,

64 i.e. the area around the sensor where 86 % of detected neutrons originate from, covers a circle

with an approximate radius of 300 m (Desilets and Zreda, 2013). However, the radius can 65

decrease with increasing air density and humidity, with increasing vegetation density and with 66

increasing soil moisture to about 100 m (Köhli et al., 2015). The eritical effective measurement 67

depth of CRS, i.e. the soil depth where 86 % of detected neutrons originate from, varies between 68

10 and 70 cm below surface (Zreda et al., 2008Franz et al., 2012a), depending on soil type, water 69

content and distance from the sensor (Köhli et al., 2015). To account for the contributions of 70

neutrons from different soil depths, various Different depth-weighting approaches have been 71

proposed, some of them assuming a linear decrease of weights with depth (Franz et al., 2012a), 72

others assuming a non-linear decrease with depth (Köhli et al., 2015). 73

63

74 The original measurement method uses a relationship between neutron flux and volumetric soil water content with the shape of the relationship being known from neutron transport simulations. 75 76 For this relationship, Desilets et al. (2010) presented an equation with three constant shape parameters  $(a_0, a_1, a_2)$  and one calibration parameter  $(N_0)$  which has to be calibrated with soil 77 78 moisture values determined by the gravimetric method from field soil samples. The influence of soil lattice water and soil organic matter on the signal was investigated by Zreda et al. (2012). 79 80 They found that both lattice water and soil organic matter contain fixed amounts of hydrogen that further attenuate the neutron signal and need to be taken into account. Lattice water and soil 81 82 organic matter corrections to the original relationship by Desilets et al. (2010) are provided for examplee.g. in Lv et al. (2014). 83

-Other external factors influencing the neutron count that need to be corrected for are (a) 84 atmospheric pressure (Bachelet et al., 1965), (b) incoming neutron flux (see e.g. Zreda et al., 85 2012, Bogena et al., 2013) and (c) specific humidity (Rosolem et al., 2013). More recently, the 86 3 Kommentar [A11]: Rev2: Already is awkward transition. Maybe something like "As early as 1966 '

Kommentar [A12]: Rev3: specify that Kodama's detector was buried in the soil.

Kommentar [A13]: Rev3: larger than what? perhaps say "large" or specify that area (~30 ha).

Kommentar [A14]: Rev3: this is not appropriate reference; the range 10 cm - 70 cm was given in Zreda et al., 2008. Also, the dependence on soil water content was specified, but not dependence on soil type and distance from sensor. Koehli et al., 2015 worked out the dependence on distance.

effects of living biomass on the neutron signal have been discussed. Bogena et al. (2013) noted 87 88 that aboveground biomass reduced the neutron count rate and thus decreased the sensitivity of the 89 sensor. To counter this loss of sensitivity they recommended a 24 h integration time for their forested catchment as a compromise between decreased uncertainty and decreased time 90 resolution. Hawdon et al. (2013) and Baatz et al. (2015) compared neutron counts for locations 91 with different amounts of biomass. Hawdon et al. (2013)and reported that the variation in 92 biomass could explain 80 % of the variation in neutron counts when assuming a nonlinear 93 relationship between biomass and neutron counts, Baatz et al. (2015) also related biomass to 94 95 neutron counts, but explained 87 % of the variation proposinged a linear relationship between the 96 two variables. Baroni and Oswald (2015) suggested that the influence of above-ground biomass between the sensor and the ground which decreases the eritical effective measurement depth of 97 98 the CRS can be incorporated into the weighting approach of Franz et al. (2012a). This is 99 especially important in locations where frequent large biomass changes occur, for example in agricultural fields. Coopersmith et al. (2014) found that soil moisture in a corn crop is often 100 overestimated when the leaf area index (LAI) is relatively high while it is underestimated when 101 102 LAI is relatively low - circumstances which could cause differences in the calibration and resulting soil moisture measurements-between the seasons. The influence of the litter layer in 103 forested environments was investigated by Bogena et al. (2013). Water content in the litter layer 104 changes rapidly and adds additional<del>unwanted</del> temporal variability to the CRS time series 105 complicating the extraction of the soil moisture signal. Therefore, Bogena et al. (2013) 106 recommended considering the water dynamics in the litter layer explicitly in the calibration 107 108 approach. Franz et al. (2013) introduced a new approach (the universal calibration function) that takes into account all sources of hydrogen thereby requiring estimates of lattice water, soil 109 organic carbon, and vegetation biomass as well as a calibration-regression factor that can be 110 111 derived from calibration or also bemay directly be retrieved from neutron count measurements over a large water body (500 m on all sides and deeper than 1 m). 112

Since the launch of the cosmic ray neutron method many changes and corrections have been brought forward that altered the way the method is applied. These changes and corrections can be divided into two groups. On the one hand, there are corrections that are applied to the raw neutron count in order to remove the influence that of other variables have on the signal (such as air pressure and humidity variations or fluctuations in incoming neutron counts). On the other Kommentar [A15]: Rev3: why unwanted? perhaps better to say "adds additional signal" that complicates analysis (or complicates extraction of soil moisture signal).

Kommentar [A16]: Rev3: please make sure that this is true; I think the idea is to fix the calibration parameter at the high end (water), rather than low end (dry soil, in Desilet's calibration function), but that is a regression parameter, not measured value.

Kommentar [A17]: Reply: In the 2013 paper they say that this parameter can be easily retrieved from measurements over a large water body. We think you are right in noting that it is in fact a regression parameter. So we changed the wording to make this clearer.

hand, changes have been made to the way we average the soil moisture measurements during the 118 119 calibration campaigns in order to get a representative soil moisture value that corresponds to what the sensor actually "sees" at the time of calibration (changing eritical effective measurement 120 depth, changing footprint diameter, inclusion of lattice water and soil organic matter water 121 equivalent). All this has led to improvements in the method's accuracy for many environments. 122 Most of these studies were performed in medium to high-count environments with neutron count 123 rates above 1000 counts per hour, in generally dry environments, at higher elevations and with 124 little vegetation. Only a few studies were performed in low-count environments with count rates 125 126 below 1000 counts per hour (e.g. Rivera Villareyes et al., 2011; Bogena et al., 2013). In the 127 present study, we evaluated whether the CRS also provides reliable and consistent soil moisture measurements in a low-count environment, i.e., in a temperate mixed forest close to sea level. We 128 129 tested several weighting approaches to convert gravimetrically determined soil water content of 130 the top 30 cm into an average soil water content that can be used for the calibration of the CRS. 131 Additionally, we analyzed whether the annual forest cycle of foliation and defoliation is important to consider for instrument calibration. Finally, we We furthermore compiled a best-132 practice for the calibration of CRS in forested, low-count environments which is provided in 133 Appendix A. 134

135

#### 136 2. Field site and instrumentation

The CRS (CRS-1000 by Hydroinnova) was installed in late 2013 in the Müritz National Park in 137 north-eastern Germany (53°19'49.0"N, 13°11'56.5"E) at an elevation of about 84 m a.m.s.l. (Fig. 138 1, inset). Precipitation, temperature and relative humidity data was provided by the climate 139 140 station Serrahn (1.6 km to the north). Average annual air temperature at the site is 8°C with a maximum in July (17.2°C) and a minimum in January (-0.9°C). Average annual precipitation is 141 142 580 mm with a maximum in June (65 mm) and a minimum in February (28 mm). This makes for a maritime temperate climate (Cfb) in the Köppen climate classification. The sensor is located in 143 a sandy outwash plain, a relic from the last glaciation, which causes the soil texture to be 144 relatively homogeneous with sand fractions of about 95% throughout the entire profile. Data 145 from a nearby well shows that the groundwater level at the site is almost 20 m below the terrain 146 surface. The vegetation within the sensor footprint consists of both deciduous and coniferous 147

Kommentar [A18]: Rev3: Are they applicable also at the site? 1.6 km seems close, but precipitation and humidity can vary at smaller scales.

Kommentar [A19]: Reply: We compared the climate data with data we collected ca. 400 m away from our site and the differences were marginal. We decided to use the data from 1.6 km since it was a longer data set (we only installed the 400 m sensors in the middle of 2014).

5

trees. Immediately surrounding the sensor is a mature beech forest (*Fagus sylvatica* L., older than 100 years), also within the footprint (but farther away) with a distance of at least 40 m from the sensor there is young pine (*Pinus sylvestris* L.), oak (*Quercus robur* L.) and spruce (*Picea abies* (L.) H.Karst.) forest (all younger than 50 years) as well as a small strip of open grassland (see Fig. 21 and also Fig. 6Fig. 3 for a map of the forest stands and Table 1 for fractions of the different tree stands within the footprint). Depending on the tree species, the mineral soil is covered by an organic soil layer and a litter layer of variable depth and water holding capacity.

155 For validation of the CRS soil water content measurements, in May of 2014 we installed 18 soil

156 moisture sensors (TOMST) close to the soil sampling/calibration locations. They are based on the

principle of time domain transmission (TDT) and each sensor comes with its own logger and

power supply (more information under: <u>http://www.tomst.cz/tms/TMS-3.html</u>). These sensors

159 were installed vertically from the terrain surface into the soil so that they continuously measure

160 soil water content averaged over the top 15-16 cm of the soil. In order to calibrate the sensors we

used the gravimetric soil moisture data we collected from the upper 15 cm during the last five

162 calibration campaigns which were carried out within the measurement period of the sensors

163 (June-November 2014)(SU, F1-F4). The volumetric water content within the upper 15 cm of the

164 CRS footprint was calculated as the mean of all 18 TDT sensors.

165

#### 166 3. Methods

#### 167 3.1. Calibration

We conducted a total of 10 calibration campaigns throughout one calendar year (2014). The first 168 one (WI) took place in February during winterly conditions with very wet soils. The next four 169 170 calibrations (S1-4) followed in spring (April-May) and covered the entire period of tree foliation. The sixth calibration (SU) was done under very dry conditions in July and the last four 171 172 calibrations (F1-4) in fall (October-November) covering the trees' defoliation. For all the 173 calibration campaigns we followed the recommended sampling pattern for the calibration of CRS which was developed by Zreda et al. (2012) and slightly modified and detailed in Franz et al. 174 (2012b). The sampling pattern prescribes 3 concentric circles around the CRS with radii of 25, 75 175

Kommentar [A20]: Rev1: On the web-site of the sensor manufacturer no specification of the measurement technique is given. I suspect that these sensors are actually based on an oscillator-ring as described in Qu et al. (2014) and not on the time-domain transmission technique. In addition, a problem of these sensors could be the top shielding, influencing the soil water content below. Since these kind of sensors only measure soil moisture at a very small volume (only very few centimeters around the sensor blade) this might lead to systematic underestimations of soil moisture.

Kommentar [A21]: Reply: According to our sensor manual the sensors are indeed based on time-domain transmission. It is hard to find other online information: http://www.ibot.cas.cz/en/kalibrace stanice proj

ekt. When calibrating the sensors in the field, we actually found a systematic overestimation at low soil water contents that we corrected for. We did not detect a shielding effect which would cause an underestimation of soil water content.

Kommentar [A22]: Rev 1: Why didn't you use all data for the calibration?

**Kommentar [A23]:** Reply: The sensors were installed in May 2014 only, so we could not use the data for the first 5 calibration campaigns.

Kommentar [A24]: Rev1: Is the sensor blade actually 15 cm long (at the web site there is no information on the seize and the pictures suggest that the sensor blade to be much shorter)

Kommentar [A25]: Reply: The sensor blade is actually 16 cm long.

and 200 m, respectively (Fig. 21). The 3 circles are intersected by 6 straight lines that point from 176 177 the sensor towards north  $(0^{\circ})$ , north-east  $(60^{\circ})$ , south-east  $(120^{\circ})$ , south  $(180^{\circ})$ , south-west  $(240^{\circ})$ and north-west (300°). Samples are taken in the vicinity of all intersections - the samples do not 178 have to be taken at the exact spot of the intersection. This sampling pattern ensures that each 179 sample has equal weight towards the spatial mean of soil moisture that is detected by the CRS, 180 assuming that the sensitivity of the CRS decreases exponentially with distance. We used a split-181 tube sampler to extract 30 cm soil cores at 18 locations within the footprint of the sensor 182 afterwards dividing each soil core into six 5 cm thick soil samples. For each of the 10 calibrations 183 184 this left us with 108 soil samples which were then transferred in sealed plastic bags to the 185 laboratory where they were immediately weighed, then oven-dried at 105°C for 24 h and then weighed again to determine their volumetric water content and bulk density. Afterwards, lattice 186 water, soil organic matter content and root biomass were determined for six depth-representative 187 188 soil samples. To this end the 108 samples (taken from the last calibration campaign in November) were grouped by sampling depth. We extracted 2 g from each of theall 18 samples from one per 189 sampling depth and combined them to create one bulk sample per depth. Then, the already oven-190 191 dried samples were weighed and put in the oven for another 24 h at a temperature of 400°C. The procedure is called 'loss on ignition' since the organic matter is burned off during the process 192 (Ball, 1964; Davies, 1974). This removed most of the soil organic matter and root biomass from 193 194 the samples. After weighing the samples (to compute the fraction of combined soil organic matter and root biomass) they were again placed in the oven for 24 h, this time at a temperature of about 195 1000°C. After that, the lattice water was also removed from the samples. A final weighing 196 197 yielded the fraction of lattice water per soil depth. In order to make soil organic matter and root biomass comparable to the influence of pure water we converted them into equivalents of water 198 by multiplying their weight by 0.556 which is the ratio of five times the molecular weight of 199 200 water to the molecular weight of cellulose (taking into account that cellulose ( $C_6H_{10}O_5$ ) contains 10 hydrogen atoms per molecule while water (H<sub>2</sub>O) only contains two) (Hawdon et al., 2014). 201

The neutron counts from the sensor were smoothed with a 12 h moving window to reduce measurement noise (see Bogena et al., 2013). The next step was to correct the neutron counts for variations in (a) pressure, (b) incoming neutron flux and (c) water vapor in the air. This was done by applying the following corrections: Kommentar [A26]: Rev3: and assuming the sensitivity decrease with distance given in Zreda et al., 2008, for the footprint radius of ca 300 m. The new footprint estimate by Koehli et al., 2015, gives smaller footprint, so the sampling distances for equal weights will be smaller than your 25 m, 75 m and 200 m.

Kommentar [A27]: Reply: This is true. We now discuss this in more detail later in the manuscript (see Section 4.2): 'Sampling distances with equal weights according to Köhli et al. (2015) would have differed from our sampling pattern (~1 m, ~33 m, ~140 m instead of 25 m, 75 m, 200 m), a condition which we balance by adjusting the distance weights. Furthermore the conditions within 30 m around our CRS are quite homogenous since the sensor is located within a pure beech stand and we are expecting little difference in soil moisture content between locations at 1 and 25 m distance.'

Kommentar [A28]: Rev3: 2 g from each of the 18 samples?

#### a. Pressure correction:

207 
$$N_p = N_{raw} * e^{\left(\frac{XP - XP_0}{L}\right)}$$
  
208 (1),

with  $N_p$  being the pressure corrected neutron counts ( $\frac{n h^{-1}}{n}$ ),  $N_{raw}$  the raw neutron counts 209  $(n h^{+} counts h^{-1})$ , Px the atmospheric shielding depthpressure (g cm<sup>-2</sup>) for every time step (derived 210 <u>from atmospheric pressure</u> measured directly in<u>side</u> the CRS case) for every time step (hPa),  $P_{X_0}$ 211 the average atmospheric shielding depthpressure  $(g \text{ cm}^2)$  for the entire measurement period 212 and L the effective nucleon attenuation length for high-energy neutrons (for our site we assumed 213 a value of 135.9 g cm<sup>-2</sup> which is equivalent to 133.3 hPa) (Desilets and Zreda, 2003). To convert 214 atmospheric pressure (hPa) into shielding depth (g cm<sup>-2</sup>) the atmospheric pressure has to be 215 multiplied by  $1.0194 \text{ s}^2 \text{ m}^{-1}$ . 216

b. Incoming flux correction (Zreda et al., 2012):

218 
$$N_{pi} = N_p * \frac{N_{avg}}{N_{nm}}$$

with  $N_{pi}$  being the sensor neutron count rate corrected for changes in atmospheric pressure and incoming neutrons ( $\mathbf{n} \cdot \mathbf{h}^{-1}$  counts  $\mathbf{h}^{-1}$ ),  $N_{avg}$  the average count rate of incoming neutrons ( $\mathbf{n} \cdot \mathbf{h}^{-1}$  counts  $\mathbf{h}^{-1}$ ) over the entire measurement period and  $N_{nm}$  the neutron count rate of the neutron monitor for each time step ( $\mathbf{n} \cdot \mathbf{h}^{-1}$ ).

As the time series of the closest neutron monitor, located in Kiel, Germany, contains several data gaps, we selected the continuous time series of the Jungfraujoch, Switzerland, for this study. We scaled this time series by adjusting its mean (309 n/h counts h<sup>-1</sup>) to the mean of the Kiel time series (327 n/h counts h<sup>-1</sup>) in order to account for the difference in altitude and latitude between the two neutron monitors. The resulting time series resembles the Kiel time series very closely (Fig. <u>S13</u>).

229 c. Water vapor correction (Rosolem et al., 2013):

230 
$$N_{pih} = N_{pi} * [1 + 0.0054 * (p_{\nu 0} - p_{\nu 0}^{ref})]$$

however, the difference in this case would be cosmetic (or zero, if the value of 133.3 hPa was obtained from the equivalent shielding depth), so it does not matter for the results; on the other hand, if you want to be consistent with cosmic-ray literature, please make the change to shielding depth. **Kommentar [A30]:** Reply: We changed the

Kommentar [A29]: Rev3: this correction uses shielding depths (g/cm2), not pressure (hPa);

units to shielding depth. Thanks for providing us with the conversion factor.

Kommentar [A31]: Rev3: reference Zreda et al., 2012 for this correction

## Kommentar [A32]: Rev1: The correct unit for incoming neutrons is "counts/sec"

Kommentar [A33]: Reply: Changed all occurrences of 'n h<sup>-1</sup>' to 'counts h<sup>-1</sup>'. To stay consistent and avoid confusion we also used hours for the incoming flux corrections.

Kommentar [A34]: Rev3: this difference (309 vs 327) cannot possibly be due to difference in altitude between the monitors (which should be a factor of four or more). I think these data sets are pressure corrected, and the difference idiosyncrasies of the two neutron monitors.

Kommentar [A35]: Rev1: No scaling needed since this correction considers the relative changes in incoming neutron flux. However, the cutoff rigidity of the Jungfraujoch Station is somewhat different from the study site given is lower latitude. An good choice for the neutron monitor is be the Lomnicky station, Slovakia (LMKS).

Kommentar [A36]: Reply: We agree that the scaling is unnecessary. Therefore we shortened the paragraph and moved the figure to the supplements. We still use the scaled and gap-filled time series we computed since omitting the scaling does not affect the results.

Kommentar [A37]: Rev3: reference Rosolem et al., 2013 for this correction

8

(3),

(2),

with  $N_{\text{pih}}$  being the sensor neutron count corrected for changes in pressure, incoming neutrons and water vapor ( $\mathbf{n} \cdot \mathbf{h}^{-1}$  counts  $\mathbf{h}^{-1}$ ),  $p_{v0}^{\text{ref}}$  the average absolute humidity of the air over the entire measurement period (g m<sup>-3</sup>) and  $p_{v0}$  the absolute humidity for each time step (g m<sup>-3</sup>). The constant 0.0054 has units of m<sup>3</sup> g<sup>-1</sup>.

Finally, to convert corrected neutron counts  $(N_{pih})$  into volumetric soil moisture  $(\theta)$ , Desilets et al. (2010) introduced an equation with four parameters – three of which  $(a_0 = 0.0808, a_1 = 0.372, a_2 = 0.115)$  were determined via neutron transport simulations and a fourth one  $(N_0)$  that serves as a calibration parameter accounting for site and sensor specific variations and representing neutron counts over dry soil at reference conditions during calibration:

240 
$$\theta(t) = \left\{ \left[ a_0 * \left( \frac{N_{pih}(t)}{N_0} - a_1 \right)^{-1} - a_2 \right] * \rho_{bd} \right\} - W_L - (SOM + B_R)$$
(4).

241 The other parameters  $\rho_{bd}$ ,  $W_L$ , SOM and  $B_R$  can be measured directly from the calibration soil samples: the bulk density of the soil ( $\rho_{bd}$  in g cm<sup>-3</sup>), the summed volume fraction of lattice water 242 in the soil grains and tightly bound water ( $W_L$  in m<sup>3</sup> m<sup>-3</sup>), the combined volume fraction of soil 243 organic matter and root biomass water equivalent (SOM -+-B<sub>R</sub> in m<sup>3</sup> m<sup>-3</sup>). In order to calibrate the 244 sensor one first has to determine the depth- (and distance-) weighted averages for  $\rho_{bd}$ ,  $W_L$ , SOM-+ 245  $B_{\rm R}$  and  $\theta$  as well as  $N_{\rm pih}$  (averaged over 12 h) for the time of calibration. This is necessary 246 247 because several factors can influence the <u>eritical effective measurement</u> depth  $z^*$  (which is the depth of the soil layer up to which 86 % of the neutrons that the CRS detects originate from) and 248 the footprint size of the sensor (Fig. 4Fig. 2). Afterwards  $N_0$  is adjusted iteratively (e.g. with a 249 250 simple Solver routine in Microsoft Excel) until the right-hand side of the equation equals the left-251 hand side.

We tested four soil moisture weighting approaches (Table  $\pm 2$ ), described in detail below, to determine which information is necessary for an accurate calibration. In a fifth approach we also tested whether including the influence of above ground biomass ( $B_{ag}$ ) further improves the performance of soil moisture retrieval with the CRS.

1. In the first approach (simple depth-weighting, SDW) a linear depth-weighting function was used (Franz et al., 2012b), where wt(z) represents the weight that is applied to the soil moisture measurements from a certain soil depth *z*: Kommentar [A38]: Rev1: The methods to determine soil organic carbon and root biomass water equivalents are not presented.

Kommentar [A39]: Reply: A description of the methods has been added. (See lines 190-195.)

Kommentar [A40]: Rev1: This statement is too vague. I think what you meant here is that the objective performance measure is minimized, right?

Kommentar [A41]: Reply: True. The sentence was removed since we decided to omit the last approach.

259 
$$\begin{cases} wt(z) = a \left[ 1 - \left( \frac{z}{z^*} \right)^b \right] & 0 \le z \le z^* \\ wt(z) = 0 & z > z^* \end{cases}$$

260 where

261 
$$a = \frac{1}{z^* - \frac{z^{*b+1}}{(b+1)z^{*b}}}$$
(6),

262 and

263 
$$z^* = \frac{5.8}{\frac{H_F}{\rho_W}H_p + 0.0829}$$
  
264 (7),

265 and

266 
$$H_n = W_L + SOM + B_R + \frac{\rho_w}{\rho_w}\theta$$

In these equations z is the soil depth below the surface in cm and  $z^*$  is the eritical effective 267 measurement soil-depth in cm, a is a parameter that ensures that the weights are conserved, b268 269 controls the curvature of the weighting function and equals is 1 for linear weighting,  $\rho_w$  is the density of water (here assumed to be 1 g cm<sup>-3</sup>),  $H_p$  is the water equivalent hydrogen content of the 270 belowground hydrogen pools ( $\underline{m^3g}$  m<sup>-3</sup>),  $W_L$  is lattice water ( $\underline{m^3g}$  m<sup>-3</sup>), SOM is soil organic matter 271 water equivalent ( $\underline{m^3g}$  m<sup>-3</sup>),  $B_R$  is root biomass water equivalent ( $\underline{m^3g}$  m<sup>-3</sup>) and  $\theta$  is the 272 gravimetrically determined volumetric soil pore water content (m<sup>3</sup> m<sup>-3</sup>). The original approach by 273 Franz et al. (2012b) was modified by Bogena et al. (2013) using the total hydrogen content of 274 275 belowground hydrogen pools  $H_p$  instead of just using the volumetric soil water content  $\theta$ . Since  $H_{\rm p}$  changes with soil depth we used an iterative approach to determine the appropriate weights. 276 277 Starting with an average value for the upper 30 cm of the soil we computed an eritical effective <u>measurement</u> depth  $z^*$  and weighted  $H_p$  of the different soil depths accordingly. With this new 278 value of  $H_p$  we then recomputed  $z^*$  and the weights. Usually the value of  $H_p$  stabilizes after a few 279 iterations. The bulk density ( $\rho_{bd}$ ) of the soil changes with depth and influences the soil moisture 280 measurements too. Therefore it was also being taken into account during the iterative process of 281 determining the eritical effective measurement depth  $z^*$  and the weighted soil moisture. In this 282 10

(5),

(8).

283 first\_weighting approach we did not use our depth-specific measurements of  $W_L$  and  $SOM+B_R$ , 284 instead we assumed an average weight fraction value of combined  $W_L+SOM+B_R$  for the entire 30 285 cm profile.

286 2. The second approach (depth-specific weighting, DSW) was identical to the first one (SDW) 287 except for using depth-specific measurements of  $W_L$  and SOM-+- $B_R$  (see Table 23 for an 288 example).

3. For the third approach (distance-depth-weighting, DDW), we adopted the weighting approach described in Köhli et al. (2015). This approach introduces distance-dependent variable depth-weighting where the critical effective measurement depth decreases with distance from the sensor.
The critical effective measurement depth z\* is calculated according to:

293 
$$z^* = \rho_{bd}^{-1} \left[ 8.32 + 0.14 * \left( 0.97 + e^{\frac{-r}{100}} \right) * \frac{26.42 + H_p}{0.057 + H_p} \right]$$
 (9),

where  $\rho_{bd}$  is the bulk density of the soil (g cm<sup>-3</sup>), *r* is the radial distance (in meters) from the CRS and  $H_p$  is the <u>water equivalent of the belowground hydrogen pools (m<sup>3</sup> m<sup>-3</sup>)</u> total hydrogen content of belowground hydrogen pools (see Eq. 8). This approach also assumes that the footprint size of the sensor varies with soil water content and atmospheric water content. We computed the varying footprint diameter for each calibration campaign and weighted the samples from 25, 75 and 200 m accordingly.

4. The fourth approach (distance-depth-weighting, non-linear, DDWnl) was identical to the third
one (DDW) except for using the non-linear depth-weighting function recommend by Köhli et al.
(2015) instead of the linear one (from Eq. 5):

303 
$$wt(z) = e^{\frac{-2z}{z^*}}$$

304 5. In the fifth approach, an above ground biomass correction (ABC) was added to the third approach (DDW). This approach differs from the first four weighting approaches by explicitly
306 correcting the neutron counts for vegetation effects, i.e., it corrects neutron counts for the additional damping by above ground biomass without altering the depth weighting of the calibration function itself. To this end, we adopted the method proposed by Baatz et al. (2015) to

Kommentar [A42]: We removed this approach since the proposed above-ground biomass correction was developed for larger differences in biomass than our field site is subjected to.

(10).

further correct the neutron signal already corrected for pressure, incoming flux and water vapor
(N <sub>pih</sub> ) and derive a vegetation-corrected neutron count (N <sub>pih</sub> ). According to Baatz et al. (2015)
vegetation causes a neutron intensity reduction by $0.9\%$ per kg of dry aboveground biomass ( $B_{ag}$ )
<del>per m<sup>2</sup>:</del>

313 
$$N_{pihv} = \frac{N_{pih}}{1 - (0.009 * B_{ag})}$$
 (11).

314 At our field site this means an intensity reduction of 57.3 % due to the beech forest surrounding 315 the CRS ( $B_{\text{tg}} = 63.8 \text{ kg m}^2$ , see Sect. 3.2). The seasonal variation due to the presence of leaves on 316 the trees is negligible (winter:  $B_{ag} = 62.8 \text{ kg m}^2$ ; intensity reduction = 56.5 %), not even 317 considering the fact that the leaves are still present as litter on the ground.

### 318 3.2. Estimation of biomass and influence of seasonal changes in biomass

Biomass influences neutron counts due to its hydrogen content. In order to test (and potentially exclude) the influence of seasonal changes in aboveground forest biomass, a survey of the beech tree stand around the CRS was conducted. Wwe estimated living tree biomass and tree biomass changes throughout the year by applying the aboveground dry biomass functions for beech forest (*Fagus sylvatica* L.) from Santa Regina et al. (1997):

324	$B_S = 0.0894 * DBH^{2.4679}$	( <u><del>12</del>11</u> ),
325	$B_B = 0.0317 * DBH^{2.3931}$	( <del>13<u>12</u>),</del>

 $326 \quad B_L = 0.0145 * DBH^{1.9531} \tag{1413}.$ 

B<sub>S</sub> is dry stem biomass (kg tree<sup>-1</sup>),  $B_B$  dry branch biomass (kg tree<sup>-1</sup>),  $B_L$  dry leaf biomass (kg tree<sup>-1</sup>),  $B_L$  dry leaf biomass (kg tree<sup>-1</sup>), and *DBH* is the diameter of the tree stem at breast height (cm). Total dry above-ground biomass  $B_{ag}$  is the sum of the three components.

To apply these functions we conducted a survey of tree diameters and tree density in the beech forest that surrounds the CRS. This allowed us to determine both the total biomass of the beech forest, as well as the seasonally variable fraction of biomass (leaf biomass divided by total biomass). The seasonally variable fraction of hydrogen mass in the trees aboveground can

334	introduce a second temporally dynamic signal on neutron counts. In order to determine this
335	fraction wWe first calculated the water mass $(W_{agb})$ in stems, branches and leaves (assuming a
336	leaf water content of 0.6 kg per kg <sup>4</sup> of wet biomass (Gravano et al., 1999) and a wood water
337	content of 0.11 kg kg <sup>-1</sup> (Bouriaud et al., 2004)). Finally, using the mass fraction of hydrogen in
338	water ( $M_{\underline{w}} = 0.1119 \text{ kg} \text{ H} \text{ per } \text{ kg}^{-1} \text{ H}_2\text{O}$ ) and in dry biomass ( $M_{\underline{b}} = 0.0622 \text{ kg} \text{ H} \text{ per } \text{ kg}^{-1}$
339	<u>Cellulose: <math>C_6H_{10}O_5</math>) one can calculate the total hydrogen densityydrogen mass (<math>H_{agb}</math>) of above-</u>
340	ground biomass in the beech stand was derived:
341	$H_{agb} = W_{agb} * M_w + B_{ag} * M_b$ (1514).
342	We did not conduct surveys on the other tree species. Table 1 shows that the beech stand covers
343	56% of the footprint area around the CRS (when assuming the exponential distance-weighting
344	from Zreda et al. (2008)). Pine covers 16%, spruce 13%, oak 8%. With the new distance
345	weighting function of Köhli et al. (2015), the cover fractions of the other tree species would
346	decrease even further. Also, the seasonal variation in spruce and pine above-ground biomass is
347	very small and thus we consider it to be constant in this study.
240	and then converted the water and dry biomass values into hydrogen equivalents by assuming that
348	the weight fraction of hydrogen in water is 0.1198 kg kg <sup>-1</sup> (H <sub>2</sub> O) and the hydrogen content in
349	biomass is 0.0622 kg kg <sup>4</sup> (Cellulose: $C_6H_{10}O_5$ ).
350	1000000000000000000000000000000000000
351	The tree survey revealed a median diameter of 23.9 cm (Min: 3.2 cm, Q25: 11.5 cm, Q75: 43.7 cm,
352	Max: 93.3 cm) and a tree density of 0.05 trees m <sup>-2</sup> . With these values at hand and Eqs. (12) (14)
353	the dry above ground biomass of the beech stand $(B_{ng})$ was computed to be 63.8 kg m <sup>-2</sup> (with
354	62.8 kg m <sup>-2</sup> from stem and branches and 1.0 kg m <sup>-2</sup> from leaves) (Fig. 5). Assuming a water
355	content of 0.11 kg kg <sup>-1</sup> for wood and a water content of 0.6 kg kg <sup>-1</sup> for leaves results in 9.2 kg m <sup>-2</sup>
356	of biomass water ( $W_{agb}$ ) (with 7.8 kg m <sup>-2</sup> from stem and branches and 1.5 kg m <sup>-2</sup> from leaves).
357	Finally, using the mass fraction of hydrogen in water ( $M_{**}$ = 0.1119 kg kg <sup>+</sup> ) and in dry biomass
358	$(M_b = 0.0622 \text{ kg}^4)$ one can calculate the total hydrogen density $(H_{agb})$ of above-ground
359	biomass in the beech stand:
360	$H_{agb} = W_{agb} * M_{w} + B_{ag} * M_{b} $ (15)

**Kommentar [A43]:** Rev3: is this 0.6 kg of H2O per kg of dry biomass? or wet biomass? clarify.

Kommentar [A44]: Rev3: this seems low. does this figure include free water (H2O in xylem) and cellulose-bound water (OH group)?

Kommentar [A45]: Reply: No, this just includes free water. The cellulose-bound water is calculated in the next step (assuming hydrogen content in dry biomass is 0.0622 kg kg-1).

13

361	Our calculations yielded a hydrogen density of 4.8 kg m <sup>-2</sup> for stem and branches and a hydrogen
362	density of 0.2 kg m <sup>-2</sup> for leaves. Assuming that the hydrogen content of the stem and branches is
363	constant and only the leaves change seasonally one is left with a fraction of variable hydrogen in
364	the above ground biomass that accounts for 7.7 % of the total hydrogen mass. At high soil
365	moisture, a 0.01 m <sup>3</sup> -m <sup>-3</sup> -soil moisture change from 0.19 to 0.20 m <sup>3</sup> -m <sup>-3</sup> -equals a change of 0.07 kg
366	m <sup>-2</sup> -of hydrogen in the soil. At low soil moisture the change from 0.05 to 0.06 m <sup>3</sup> -m <sup>-3</sup> -is equal to a
367	change in hydrogen of 0.25 kg m <sup>-2</sup> (due to the fact that the CRS also receives the neutron signal
368	from deeper soil depths (larger critical depth z*)).
369	3.3. Validation
370	As an objective performance measure to compare the soil moisture time series derived from the
371	CRS with the soil moisture time series from the TDT sensors we used the modified Kling-Gupta
372	efficiency KGE' (Gupta et al., 2009; Kling et al., 2012):
373	$KGE' = 1 - \sqrt{(r-1)^2 + (\beta - 1)^2 + (\gamma - 1)^2} $ (1615)
374	With correlation coefficient $r_{\overline{2}}$
275	$\sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y}) \tag{16}$
375	$r = \frac{\sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2} * \sqrt{\sum_{i=1}^{n} (y_i - \bar{y})^2}} $ (16),
376	-bias ratio $\beta = \mu_{\text{mod}}/\mu_{\text{obs}}$ and variability ratio $\gamma = (\sigma_{\text{mod}}/\mu_{\text{mod}})/(\sigma_{\text{obs}}/\mu_{\text{obs}})$ . The KGE' measures the
377	Euclidian distance in a 3-D space where the correlation coefficient <i>r</i> is on one axis, the variability
378	ratio $\beta$ is on the second axis and the bias ratio $\gamma$ is on the third axis. KGE' scores range from 1
379	(representing a perfect fit) to -∞. Due to the composite nature of the KGE' it is relatively simple
380	to analyze which feature of the time series (correlation, bias, variability) contributes most to the
381	good/bad performance of a model.
382	

Kommentar [A46]: Reply: Parts were moved to the results section (chapter 4.7).

**Kommentar [A47]:** Rev3: This section should provide more information, not just the equation. What is KGE? How is it used? What is compared with what? How are these variables computed (eg, r)? What is the significance of the result? Etc...

### 383 4. Results

#### 384 4.1. Gravimetric soil water measurements and soil physical characteristics

Soil water content in the sandy soils ranged between 0.03 and 0.37 m<sup>3</sup> m<sup>-3</sup> (absolute minimum 385 and maximum values of individual soil core samples during the 10 sampling campaigns). The 386 spatial distribution of volumetric soil water content for the 10 calibration days is shown in Fig. 387 6Fig. 3. At each location the soil water content is an unweighted average value of the six samples 388 taken from 0 to 30 cm depth. The mean volumetric soil water content for the calibration days 389 over all calibration locations ranged from 0.07 up to 0.16 m<sup>3</sup> m<sup>-3</sup> with standard deviations ranging 390 from 0.015 to 0.047  $m^3$  m<sup>-3</sup>. The depth and distance weighted averages used for calibration 391 ranged from 0.08 to 0.24 m<sup>3</sup> m<sup>-3</sup> (see for example Table 4, column:  $\theta_{depthw}$ ). A general soil 392 moisture pattern emerged with the soil moisture under coniferous tree stands being lower and 393 under deciduous tree stands being higher. Especially the uppermost soil layer (0-5 cm) was drier 394 under the coniferous trees - on average about 0.065 m<sup>3</sup> m<sup>-3</sup> - while the deeper soil layers under 395 coniferous trees were about 0.023 m<sup>3</sup> m<sup>-3</sup> drier. The highest spatial variabilities in soil moisture 396 were encountered during spring and fall seasons and more homogenous soil moisture conditions 397 during winter and summer. The wettest calibration we conducted (WISU) yielded an average soil 398 water content of 0.29 m<sup>3</sup> m<sup>-3</sup> for the top 5 cm. Calibration at higher soil water content is difficult 399 as it only occurs for short periods of time after large precipitation events when significant 400 amounts of intercepted water are also present in the canopy and litter layer. 401

The average bulk density ( $\rho_{bd}$ ) measurements for the 10 calibration campaigns ranged from 1.16 to 1.22 g cm<sup>-3</sup> (mean: 1.18 g cm<sup>-3</sup>, standard deviation: 0.02 g cm<sup>-3</sup>). The weight fraction of soil organic matter and root biomass water equivalent ( $\underline{w}SOM$ -+- $B_R$ ) was determined to be 51.4 g kg<sup>-1</sup> in the shallowest soil layer (0-5 cm) with decreasing values at depth. The weight fraction of lattice water ( $\underline{w}W_L$ ) was determined to be 3.2 g kg<sup>-1</sup> in the shallowest soil layer with slightly increasing values at deeper soil depths.

#### 408 4.2. Footprint variability

409 The footprint diameters calculated according to Köhli et al. (2015) and used in approaches 3 and
 410 4 ranged from 185 m for the wettest to 200 m for the driest conditions. This resulted in distance

411	weights of ~0.56 (for samples from 25 m distance), ~0.35 (for samples from 75 m distance) and
412	~0.10 (for samples from 200 m distance). These weighting factors varied only marginally
413	between the individual calibration campaigns despite considerable differences in soil and
414	atmospheric water content. Sampling distances with equal weights according to Köhli et al.
415	(2015) would have differed from our sampling pattern (~1 m, ~33 m, ~140 m instead of 25 m, 75
416	m, 200 m), a condition which we balance by adjusting the distance weights. Furthermore the
417	conditions within 30 m around our CRS are quite homogenous since the sensor is located within
418	a pure beech stand and we are expecting little difference in average soil moisture content between
419	locations at 1 and 25 m distance.

#### 420 4.2.4.3. Calibration

The average reference atmospheric pressure  $(P_0)$  for the entire measurement period was 421 1005.8 hPa; the average reference incoming neutron flux ( $N_{avg}$ ) was 328.3 n h<sup>4</sup> counts h<sup>4</sup>; the 422 average reference absolute humidity ( $p_{v0}^{ref}$ ) was 9.1 g m<sup>-3</sup>. Equations (5) through (10) were used 423 424 to calculate the depth-weighted volumetric soil water content  $(\theta_{depthw} and depth-weighted water)$ equivalent of belowground hydrogen pools (Hp)depthw) according to the four weighting 425 approaches we applied. Equations (1)-(3) were used to compute  $N_p$ ,  $N_{pi}$  and  $N_{pih}$ -(as well as Eq. 11) 426 to compute  $N_{\text{pihv}}$ , and then Eq. (4) to identify  $N_0$  for each calibration. Table  $\frac{23}{2}$  provides an 427 example of the depth-weighting following approach 2 (DSW with depth-specific values of  $W_L$ 428 and SOM-+- $B_R$ ). 429

430 The values in Table 32 result in a depth-weighted average volumetric water content  $\theta_{depthW}$  of 0.150 m<sup>3</sup> m<sup>-33</sup>, a depth-weighted water equivalent of belowground hydrogen poolsvolumetric 431 water content including  $W_{\rm L}$  and  $SOM + B_{\rm R}$  ( $H_{\rm p}$ )<sub>depthW</sub> of 0.179 m<sup>3</sup> m<sup>-3</sup> and a depth-weighted bulk 432 density  $(\rho_{bd})_{depthW}$  of 0.981 g cm<sup>-3</sup>. If  $W_L$  and SOM-+-B<sub>R</sub> were not considered, the values for 433  $\theta_{depthW}$  and  $(\rho_{bd})_{depthW}$  would change to 0.146 m<sup>3</sup> m<sup>-3</sup> and 1.013 g cm<sup>-3</sup> respectively, because the 434 eritical effective measurement depth  $z^*$  increases when the higher amounts of SOM-+-B<sub>R</sub> in the 435 shallow layers are not considered, thus giving more weight to low soil moisture values in deeper 436 437 soil horizons.

Kommentar [A48]: Rev1: The correct unit for incoming neutrons is "counts/sec" Kommentar [A49]: Reply: Corrected.

#### 438 4.3. Footprint variability

439 The footprint diameters calculated according to Köhli et al. (2015) and used in approaches 3-5

440 ranged from 185 to 200 m. This resulted in distance weights of ~0.56 (for samples from 25 m),

441 -0.35 (for samples from 75 m) and -0.10 (for samples from 200 m). These weighting factors

442 varied only marginally between the individual calibration campaigns.

Table <u>43</u> lists the parameters relevant for calibration for all 10 calibration dates (again following approach 2, <u>SDS</u>W, with depth-specific values of  $W_L$  and SOM-+- $B_R$ ).

Following the standard N<sub>0</sub>-calibration approach of Desilets et al. (2010), we should have ended 445 up with the same  $N_0$  value for each of the 10 calibrations. However, the  $N_0$  range we found was 446 considerable – e.g. from 80858 to 895910 counts h<sup>-1</sup> for the DDW approach (mean: 841.978 h h<sup>-1</sup> 447 448 <sup>4</sup> counts h<sup>-1</sup>, standard deviation:  $13.7\frac{2113.58}{2113.58}$  n h<sup>-4</sup> counts h<sup>-1</sup>). As a consequence, the 10 computed time series following Desilets et al. (2010) also showed differences of more than 0.1 m<sup>3</sup> -m<sup>-3</sup>-in 449 volumetric soil water content (Fig. 7 (Fig. 4 illustrates results for the DDW approach)., In the 450 most extreme case, these differences were larger than  $0.1 \text{ m}^3 \text{ m}^{-3}$  (which is equal to 2430 % of the 451 total range of soil water content at the site)especially during conditions of high soil moisture (Fig. 452 7₽. 453

In fact, none of the fourive weighting approaches was able to solve the problem of determining a unique calibration parameter for our field site. All weighting approaches resulted in largely deviating  $N_0$ -values between the individual calibrations (see means and standard deviations in column 1 and 2 of Table 5). This in turn led to differences in the and resulting time series of volumetric soil water content between the individual calibrations (see means and standard deviations in column 3 and 4 of Table 45).

#### 460 4.4. Modified New calibration function

To include all information of our 10 calibration campaigns into our analysis, we fitted modifiednew calibration functions to our fivefour sets of 10 calibration points eachderived from the four4 different weighting approaches (see section 3.1). This was done by using the Microsoft Excel Solver software to optimize the three shape parameters ( $a_0$ ,  $a_1$ ,  $a_2$ ) and  $N_0$  through the Kommentar [A50]: Rev1: The correct unit for the CRS measured neutron intensity is "counts/h"

## Kommentar [A51]: Reply: Corrected throughout the revised manuscript.

Kommentar [A52]: Rev3: this is inaccurate; one time series shown in Fig. 7 has differences of that magnitude, whereas the other nine have considerably smaller deviations; please, state this result correctly, without creating undue alarm.

**Kommentar [A53]:** Reply: You are right in that our formulation is unclear and could be interpreted in different ways. So we modified the statement: 'As a consequence, the 10 computed time series following Desilets et al. (2010) also showed differences in volumetric soil water content (Fig. 4 illustrates results for the DDW approach). In the most extreme case, these differences were larger than 0.1 m<sup>5</sup> m<sup>3</sup> (which is equal to 30% of the total range of soil water content at the site).'.

Kommentar [A54]: Rev3: It is unclear how this conclusion was reached. Please describe in detail what was done, what were the results and how to interpret them.

Kommentar [A55]: Reply: We conclude that there is no unique calibration parameter and describe the calibration procedure in detail in the methods section (lines 256-303). The results are presented in Table 5 and Fig. 4 & 5. We added a more detailed interpretation of the results to the discussion section.

Kommentar [A56]: Rev1: According to Zreda et al. (2012) the presence of other hydrogen pools than soil moisture increases the stopping power of the soil, which leads to a change in the slope of the calibration function. Thus, calibration has to be performed using the total hydrogen pool, and soil moisture is then computed by subtracting other hydrogen pools than soil moisture. It is unclear whether this procedure was applied in this study. If not, this would partly explain the differences in soil moisture estimates.

**Kommentar [A57]:** Reply: As outlined in the description of our four approaches (esp. Lines 267-285), we used the total hydrogen pool for calibration before subtracting other than soil moisture contributions according to Eq. 4 (Line 240).

Kommentar [A58]: Rev1: The term "new calibration function" is misleading. Changing the "a" parameters of the NO calibration function is not new and was already presented by Iwema et al. (2015). They called this more adequately "modified NO method". However, they only

Kommentar [A59]: Reply: You are right that 'new calibration function' is misleading. We changed all occurrences to 'modified calibration function'. It is true that the N0 parameter has a very similar influence on the shape of the calibration function as the a0 parameter. Still

calibration point cloud (solid lines in Fig. 8Fig. 5). Plotting the  $N_{\text{pih}}$ -values of all 10 calibrations 465 466 against the gravimetrically determined and depth- (and distance-) weighted volumetric soil moisture revealed that the standard shape of the soil moisture-neutron count relation is not valid 467 at our field site. Instead of plotting along functions defined by the standard calibration (Desilets 468 et al., 2010) (examples are dotted lines in Fig. 8Fig. 5) our calibration points are better captured 469 by less steep functions (solid lines in Fig. 8Fig. 5 are the best-fit calibration functions for the 470 471 different approaches). Using the  $N_0$ -calibration function with the standard shape parameters may lead to large soil water content deviations between individual calibration campaigns, especially 472 473 under wet soil moisture conditions. The slope of the  $N_0$ -calibration function is essentially too 474 steep, which means that in our environment a change in the neutron count is caused by a more subtle change in soil moisture than is assumed by the standard relationship - essentially the 475 476 sensor has a higher resolution/sensitivityis more sensitive than one would expected.

The optimized parameters for the <u>fivefour</u> approaches are shown in Table <u>56</u>. The resulting soil
moisture time series are shown in <u>Fig. 9Fig. 6</u>.

#### 479 **4.5. Validation**

We tested whether the modifiednew calibration functions improved the performance of the CRS 480 measurements relative to in situ measurements, and if so, which of the weighting approaches 481 performed best. In order to do that we compared the soil moisture time series from the CRS 482 (using the standard  $N_0$ -calibration function from Desilets et al. (2010) and applying our newly 483 484 derived corrected relationships) with the soil moisture time series from the TDT sensors 485 distributed throughout the footprint. As a first step, the CRS measurements had to be converted to a soil water content value representative of the top 15 cm of the soil (the integration depth of the 486 487 TDT sensors). For this purpose we compared the weighted volumetric water content ( $\theta_{depthw}$ ) from the gravimetric measurements of the calibration campaigns (basically what the CRS is 488 supposed to "see") with the unweighted average gravimetric measurements of the top 15 cm 489  $(\theta_{15cm})$  (Fig. S2). We found strong linear correlations for two of the weighting approaches (SDW 490 491 and DSW) with CRS water content being larger than the  $\theta_{15cm}$  values and increasing differences 492 for wetter soil conditions (indicating that for higher soil moisture the CRS overestimates soil 493 water contents in the top 15 cm while for lower soil moisture the overestimation decreases). For Kommentar [A60]: Rev1: Do you have any idea why?

Kommentar [A61]: Reply: Yes. If you look at Fig. 5 you see that at higher water content a smaller change in neutron counts is associated with a larger change in soil water content (the function is steeper). Therefore the uncertainty during the calibration is also larger.

Kommentar [A62]: Rev3: There is a lot of noise in Figure 5 and the difference between standard N0 and the improved data is not clear. Can you add error bars to the data points?

Kommentar [A63]: Reply: We are not sure about this comment. In our view, this difference between the standard and the modified calibration functions is clearly represented by the dotted and the solid lines respectively. Since there is already a lot going on in this figure, we decided not to add error bars and we were not sure of the added value they would provide.

Kommentar [A64]: Rev1: Please provide a figure showing the comparison.

Kommentar [A65]: Reply: We have prepared a figure and will add it as a supplement (Fig S2).

494	approaches 3 <u>and 4-5</u> (DDW <u>and</u> , DDWnl <del>and ABC</del> ) an offsets of $0.0065$ and $0.011$ m <sup>3</sup> m <sup>-3</sup>
495	indicated slightly lower weighted CRS soil water content than the unweighted top 15 cm values.
496	The linear correlations for the first two weighting approaches were expected since when it is
497	wetter, the effective measurementpenetration depth is reduced for the CRS measurements and the
498	wetter shallower soil layers receive more weight. Therefore, the CRS measurements result in
499	higher soil water content than the gravimetric measurements. However, it seems that in
500	approaches 3 and 4 the distance weighting counters this effect. A probable explanation is that the
501	formula used for the distance-depth weighting increases the effective measurement depth. This
502	causes higher weights for deeper (drier) soil layers even under wet conditions and could
503	counteract the trend. We then converted the CRS time series by the above relationships into time
504	series that were representative of the top 15 cm and compared them to the TDT measurements.
505	The modified Kling-Gupta efficiency (KGE') was used as a performance measure. The worst
506	performance was achieved by the simple depth weighting approach (KGE'(SDW) = 0.83, Table
507	$\frac{76}{}$ , the performance improved when depth-specific weighting was included (KGE'(DSW) =
508	0.88) and it further improved when including distance weighting (KGE'(DDW) = $0.892$ ). The
509	linear depth weighting worked better than the non-linear depth weighting (KGE'(DDWnl) =
510	0.837). The inclusion of a vegetation correction did not improve the performance any further
511	(KGE'(ABC) = 0.92). That means that the distance-depth-weighting approach (DDW) improved
512	the neutron sensors performance the most. In comparison, using the single-point standard $N_{0}$ -
513	calibration function and DDW yielded KGE's for the individual calibration campaigns ranging
514	from $0.5846$ to $0.8379$ with a mean KGE' of $0.7168$ ( $\pm 0.089$ ). It is important to note that all of
515	the modifiednew calibration approaches performed better than their standard calibration
516	counterparts. The improvement of performance of the new $N_0$ -calibration functions compared to
517	the standard calibration functions was caused by the better agreement of both the bias ratios $\beta$
518	and the variability ratios $\gamma$ , i.e. both the means and the variabilities of the CRS time series better
519	matched the TDT observations (see also Fig. 10Fig. 7). This supports the hypothesis that at our
520	field site <u>larger than expected</u> changes in neutron count are <u>already</u> caused by more-subtle
521	changes in soil moisture-than expected.

Kommentar [A66]: Rev1: Shouldn't the relationships vary with soil moisture content due changing sensor penetration depths?

Kommentar [A67]: Reply: Yes, that is what we expected and that is also what we found for the first two approaches. When it is wetter, the first two approaches. When it is wetter, the penetration depth is reduced for the CRS measurements and the wetter shallower layers receive more weight. Therefore, the CRS measurements show higher SWC than the gravimetrically determined SWC. However, it seems that the distance weighting counters this effect. A probable explanation is that the formula used for the distance-depth weighting increases the critical depth. This causes higher weights for deeper (drier) soil layers even under wet conditions and could counteract the trend.

Kommentar [A68]: Rev1: This finding is quite obvious given the insignificant changes in above biomass. Generally, the application of the vegetation correction makes only sense, when temporal biomass dynamics are expected and temporal information on biomass changes are available.

Kommentar [A69]: Reply: We removed the whole part on vegetation correction.

#### 522 4.6. Optimizing calibration efforts

We further tested whether two or more individual calibration campaigns are required to determine a comprehensive calibration function shape, and under which soil moisture conditions these calibrations should be conducted. We paired each individual calibration point (derived from the best-performing weighting approach, DDW) with all the other calibration points (WI and S1, WI and S2, WI and S3, etc.) and computed best-fit calibration functions for all of these pairings [Fig. 11Fig. 8).

529 Then we used the resulting calibration functions to convert the measured neutron counts into time series of volumetric soil water content and compared these to the TDT measurements (again 530 using the KGE' as the performance measure). We found that a two-point calibration proved to be 531 532 sufficient in case that the difference in soil water content between the two calibrations was larger than<del>at least</del>  $0.12 \text{ m}^3 \text{ m}^{-3}$  (i.e. for our sandy soils it covered ~50 % of the observed range of 533 average soil water content). Figure 9 indicates that the calibrated neutron count-soil water content 534 conversion will always perform well if the soil moisture difference between the two calibrations 535 is sufficiently large. Also, it turned out to be more important to capture a calibration point at very 536 dry rather than at very wet soil water contents. This is illustrated in Fig. 12Fig. 9 where 537 predominantly calibrations that involve low soil water contents (red dots) as the minimum value 538 achieve KGE's of 0.9 while these KGE' values are also achieved more frequently with 539 intermediate soil water contents (light blue dots) as the maximum value. 540

### 541 **4.7.** <u>Variability of hydrogen pools</u>Other potential influences on neutron count

542 In search of potentially unaccounted factors that influence the neutron count we compared  $N_0$ -543 values obtained from the 10 calibrations with apparent atmospheric pressure, specific humidity, 544 temperature and estimates of forest crown cover (derived from photographs taken from the 545 ground aiming at the zenith) during the calibration campaigns. No seasonal or other temporal 546 relationships were found.

547	The tree survey revealed a median diameter of 23.9 cm (Min: 3.2 cm, Q <sub>25</sub> : 11.5 cm, Q <sub>75</sub> : 43.7 cm,
548	Max: 93.3 cm) and a tree density of 0.05 stems m <sup>-2</sup> . With these values at hand and Eqs. (11)-(13)
549	the dry above-ground biomass of the beech stand $(B_{ag})$ was 63.8 kg m <sup>-2</sup> (with 62.8 kg m <sup>-2</sup> from

**Kommentar [A70]**: Rev1: This investigation is very similar to lwema et al. (2015). Please discuss your results in the light of this study.

Kommentar [A71]: Reply: We added a discussion in section 5.1 (lines 687-695).

Kommentar [A72]: Rev1: The results plotted in Fig. 9 show clearly, that only the most extreme dry and wet samplings result in an acceptable calibration result, whereas sampling at intermediate soil moisture will lead to very uncertain calibration of the modified N0-method. On the other hand, this illustrates the value of the standard N0-method that will also produce stable results in case only one sampling date is available. Please add this to the discussion.

Kommentar [A73]: Reply: Fig. 9 shows that the best 2-point-calibrations are achieved with one sampling point taken under very dry conditions and another sampling point taken either under intermediate or wet conditions. In our case it is hard to see the value of the standard N0-method since it always resulted in too much soil moisture variability no matter whether the calibration was performed during wet, intermediate or dry conditions (because the standard calibration of N0 does not allow a change of the slope of the calibration function).

Kommentar [A74]: Rev1: This chapter belongs to discussion

Kommentar [A75]: Reply: we moved parts of this chapter to discussion and only left the parts that really describe results. We also added results on other hydrogen pools, so we renamed the chapter

# Kommentar [A76]: Rev1: What about the other tree species?

Kommentar [A77]: Reply: We added to the text (Line: 342): 'We did not conduct surveys on the other tree species. Table 1 shows that the beech stand covers 56% of the footprint area around the CRS (when assuming the exponential distance-weighting from Zreda et al. (2008)). Pine covers 16%, spruce 13%, oak 8%. With the new distance weighting function of Köhli et al. (2015), the cover fractions of the other tree species will decrease even further. Also, the seasonal variation in spruce and pine above-ground biomass is very small and thus we consider it to be constant in this study.'

550	stem and branches and 1.0 kg m <sup>-2</sup> from leaves) (Fig. 10). These values result in 9.2 kg m <sup>-2</sup> of
551	biomass water ( $W_{agb}$ ) (with 7.8 kg m <sup>-2</sup> from stem and branches and 1.5 kg m <sup>-2</sup> from leaves).
552	Further calculations yield a hydrogen mass of 4.8 kg m <sup>-2</sup> for stem and branches and a hydrogen
553	mass of 0.22 kg m <sup>-2</sup> for leaves (Eq.14). Other hydrogen pools within the CRS footprint were also
554	assessed. The thickness of the litter layer was determined to be 5 cm on average. Assuming a
555	porosity of 85 % yields a hydrogen mass of 0.47 kg m <sup>-2</sup> for a dry litter layer. Hence, the hydrogen
556	mass of the static biomass (stem, branches and dry litter) amounted to 5.24 kg m <sup>-2</sup> . Beech litter
557	was found to have a maximum interception capacity of 2.8 mm in a forest in Luxembourg
558	(Gerrits et al., 2010) corresponding to an additional 0.31 kg m <sup>-2</sup> of hydrogen when the litter layer
559	is wet. The canopy interception of beech can be assumed to be up to 1.5 mm (Gerrits et al., 2010)
560	(i.e. another 0.17 kg m <sup>-2</sup> of hydrogen is added to the system when the canopy is wet). The
561	hydrogen contribution of soil organic matter and root biomass changes with soil water content
562	because the effective measurement depth of the sensor changes. Applying the DDW approach we
563	computed a value of 0.36 kg m <sup>-2</sup> for wet conditions (0.29 m <sup>3</sup> m <sup>-3</sup> ), a value of 0.44 kg m <sup>-2</sup> for
564	intermediate conditions (0.17 $\text{m}^3 \text{m}^{-3}$ ) and a value of 0.66 kg $\text{m}^{-2}$ for dry conditions (0.05 $\text{m}^3 \text{m}^{-3}$ ).
565	The hydrogen contribution of lattice water also changes with moisture conditions (wet: 0.05 kg
566	m <sup>-2</sup> ; intermediate: 0.07 kg m <sup>-2</sup> ; dry: 0.15 kg m <sup>-2</sup> ). A pore water content of 0.29 m <sup>3</sup> m <sup>-3</sup> equals a
567	hydrogen mass <del>density</del> of 4.12 kg m <sup>-2</sup> , a pore water content of 0.17 m <sup>3</sup> m <sup>-3</sup> equals a hydrogen
568	mass of 3.26 kg m <sup>-2</sup> and a pore water content of 0.05 m <sup>3</sup> m <sup>-3</sup> reduces the hydrogen mass to $1.77$
569	kg m <sup>-2</sup> . Figure 11 and Table 8 give an overview of the different hydrogen pools for varying
570	moisture conditions within the footprint of the CRS. Assuming a linear depth weighting function,
571	the total amount of hydrogen from pore water that a CRS "sees" is 4.01 kg m <sup>2</sup> for a soil water
572	content of 0.20 m <sup>3</sup> m <sup>3</sup> (critical depth = 17.9 cm) while it reduces to 3.93 kg m <sup>2</sup> for a soil water
573	content of 0.19 m <sup>3</sup> m <sup>3</sup> (critical depth = 18.5 cm). That means that a change in volumetric soil
574	water content of 0.01 m <sup>3</sup> m <sup>3</sup> is equal to a change in hydrogen of 0.08 kg m <sup>2</sup> . However, the same
575	change in soil water content under drier conditions is associated with a larger change in
576	hydrogen: if the soil water content is $0.06 \text{ m}^3 \text{ m}^3$ (critical depth = $31.6 \text{ cm}$ ), the CRS "sees"
577	2.12 kg m <sup>-2</sup> of hydrogen, if the soil water content is 0.05 m <sup>3</sup> m <sup>-3</sup> (critical depth = 33.4 cm) then
578	the CRS "sees" only 1.87 kg m <sup>-2</sup> —so the difference in hydrogen is 0.25 kg m <sup>-2</sup> . The variability in
579	hydrogen due to foliation and defoliation in the beech forest surrounding the CRS amounts to
580	0.22 kg m <sup>-2</sup> . This means that it equals a change in soil water content of about 0.031 m <sup>3</sup> m <sup>-3</sup> (under
581	wet conditions) and 0.009 m <sup>3</sup> m <sup>-3</sup> (under dry conditions). These differences for wet and dry
l	21

582	conditions are due to the fact that the critical depth of the sensor is larger during dry conditions
583	and therefore an equal increase in soil water content requires a larger amount of water since a
584	larger soil column has to be filled. These calculations disregard the fact that fallen leaves still
585	contain hydrogen (which hence is not completely removed from the system immediately and
586	therefore should also reduce the expected variability). At our field site 65 % of the distance-
587	weighted area surrounding the CRS is covered by deciduous trees (mainly beech and oak), the
588	other 35 % do not experience a significant annual cycle of leaf growth and fall (pine, spruce and
589	grassland). This should further reduce the influence of seasonally variable biomass on the cosmic
590	ray neutron counts (with a potential maximum influence of leaf out during wet conditions of
591	0.020 m <sup>3</sup> m <sup>-3</sup> and only 0.006 m <sup>3</sup> m <sup>-3</sup> in dry conditions). In summary, we do not expect a
592	significant impact of seasonally varying above ground biomass on the measurements of soil
593	water content.

## 595 5. Discussion

# 596 5.1. Potential influences on neutron counts

597	The 10 N <sub>0</sub> -calibration parameters derived from our 10 calibrations varied considerably. In a first
598	analysis we found that this was not related to the different soil moisture conditions during
599	calibration. In search of other potentially unaccounted factors that influence the neutron count we
600	compared No-values obtained from the 10 calibrations with apparent atmospheric pressure,
601	specific humidity, temperature and estimates of forest crown cover (derived from photographs
602	taken from the ground aiming at the zenith) during the calibration campaigns. No seasonal or
603	other temporal relationships were found. The contributions of different hydrogen pools (Fig 11)
604	reveal that a large percentage of hydrogen at our field site stems from the above-ground
605	vegetation (52 to 68 %, depending on moisture conditions). Fortunately, most of this hydrogen is
606	static in nature and can be accounted for by the calibration of the CRS. Assuming that the
607	hydrogen content of the stem and branches is constant and only the leaves change seasonally one
608	is left with a fraction of variable hydrogen in the above-ground biomass that accounts for 2-3 %
609	of the total hydrogen mass. The variability in hydrogen due to foliation and defoliation in the
610	beech forest surrounding the CRS amounts to 0.22 kg m <sup>-2</sup> . This means that it equals a change in
	22

Kommentar [A78]: Rev1: So the whole discussion of this chapter is unimportant and should be reduced to 1-2 sentences.

Kommentar [A79]: Reply: Would you say that just because our results suggest that seasonally-varying above-ground biomass does not influence the neutron count significantly the discussion of this finding is not important? We think this finding is very important for the use of CRS in forested areas and worth the extended calculation and discussion. (In the end, it makes life much easier when applying CRS in forests).

**Kommentar [A80]:** We moved parts of this section to discussion (chapter 5.1).

Kommentar [A81]: Rev1: This chapter belongs to discussion

Kommentar [A82]: Reply: Moved.

**Kommentar [A83]**: Rev3: isn't there a seasonality or some other temporal variability (eg, with droughts) in the free water within trunks and branches?

Kommentar [A84]: Reply: Yes, there is some seasonality also in this regard (there is even daily fluctuations indicating variations in transpiration flux). This, however, was not part of our analysis since it is difficult to determine the exact numbers and it is likely that these variations are too small to influence the neutron count.

611	soil water content of about 0.031 cmm <sup>3</sup> cmm <sup>-3</sup> (under wet conditions) and 0.018 cmm <sup>3</sup> cmm <sup>-3</sup>
612	(under dry conditions). These differences for wet and dry conditions are due to the fact that the
613	eritical effective measurement depth $z^*$ of the CRS increases for dry conditions: the sensor
614	receives the neutron signal from deeper soil depths and therefore an equal increase in soil water
615	content requires a larger amount of water since a larger soil column has to be filled. At high soil
616	moisture, a 0.01 m <sup>3</sup> m <sup>-3</sup> soil moisture change from 0.28 to 0.29 m <sup>3</sup> m <sup>-3</sup> equals a change of 0.07 kg
617	$\underline{m}^{-2}$ of hydrogen in the soil. At low soil moisture the change from 0.05 to 0.06 $\underline{m}^{3} \underline{m}^{-3}$ is equal to a
618	change in hydrogen of 0.12 kg m <sup>-2</sup> . The variability in hydrogen due to foliation and defoliation in
619	the beech forest surrounding the CRS amounts to 0.22 kg m <sup>-2</sup> . This means that it equals a change
620	in soil water content of about 0.031 cm <sup>2</sup> cm <sup>2</sup> (under wet conditions) and 0.018 cm <sup>2</sup> cm <sup>2</sup> (under
621	dry conditions) The above calculations with respect to biomass variability disregard the fact that
622	fallen leaves still contain hydrogen (which hence is not completely removed from the system
623	immediately and therefore should also reduce the expected variability). At our field site 65 % of
624	the distance-weighted area surrounding the CRS is covered by deciduous trees (mainly beech and
625	oak), the other 35 % do not experience a significant annual cycle of leaf growth and fall (pine,
626	spruce and grassland). This should further reduce the influence of seasonally variable biomass on
627	the cosmic ray neutron counts (with a potential maximum influence of leaf-out during wet
628	conditions of 0.020 m <sup>3</sup> m <sup>-3</sup> and only 0.012 m <sup>3</sup> m <sup>-3</sup> in dry conditions). In summary, we do not
629	expect a significant impact of seasonally varying above-ground biomass on the measurements of
630	soil water content. Also, we could not find systematic changes in the calibration results connected
631	to the annual cycle of tree foliation/defoliation (i.e. a reduction in counts during summer due to
632	higher hydrogen content in the above-ground biomass). Therefore we deem a correction for
633	variable hydrogen from forest canopy biomass-hydrogen at different times of the year
634	unnecessary.
625	
635	With regard to other varying hydrogen pools we noticed that the influence of interception storage
636	both in the canopy and in the litter layer can potentially have an impact. When both the canopy
637	and the litter layer are wet, the combined hydrogen amount within these two stores can sum up to
638	almost 5 % of the total hydrogen pool equaling a change in volumetric soil water content of 0.067

639  $\underline{m^3 m^{-3}}$  (Fig. 11). It is not possible to solve this problem by calibrating during conditions of high

640 interception storage since then the soil water content would be underestimated as soon as the
 641 canopy is dry. Calibration during conditions of dry canopy and litter layer is recommendable

Kommentar [A85]: Rev1: This is only true when assuming that the CRS footprint is completely covered by beech, which is however not the case.

Kommentar [A86]: Reply: That is true. So we present an extreme case here since the other vegetation types experience smaller seasonal changes in above-ground biomass. In reality we should expect even less variation in neutron counts due to foliation/defoliation.

Kommentar [A87]: Rev1: So the whole discussion of this chapter is unimportant and should be reduced to 1-2 sentences.

Kommentar [A88]: Reply: Would you say that just because our results suggest that seasonally-varying above-ground biomass does not influence the neutron count significantly the discussion of this finding is not important? We think this finding is very important for the use of CRS in forested areas and worth the extended calculation and discussion. (In the end, it makes life much easier when applying CRS in forests). because conditions with an empty interception store are generally prevalent and can be much
better defined than conditions with a filled interception store. A potential solution to the influence
of the variable interception storage filling is the introduction of another neutron count correction
using observed, derived or modeled interception storage values (similar to the pressure or the
water vapor correction).

The tenfold standard calibration of our CRS produced 10 different time series of volumetric 647 water content. The differences between the individual time series at times exceeded 0.1 m<sup>3</sup> m<sup>3</sup>. 648 649 Moreover, the time series of soil water content derived from the neutron counts via the standard  $N_{\rm a}$ -calibration function exhibited a variability that was too high compared to the distributed 650 651 continuous in situ measurements. Altering the shape of the calibration function led to much higher congruence between the individual calibration efforts. Furthermore, the determination of a 652 new calibration function enhanced the performance of the CRS measurements significantly when 653 comparing them with independent distributed measurements of soil water content. Different 654 weighting approaches proved to be more or less useful in identifying appropriate soil water 655 contents for the time of calibration campaigns. The fact that the depth-specific weighting (DSW) 656 657 approach performed better than the simple depth weighting (SDW) is an indication that the depth variations in lattice water, soil organic matter and root biomass content should be explicitly 658 represented accounted for during the calibration of the CRS. The best performance was achieved 659 660 with a weighting approach (DDW) that explicitly takes into account both depth-weighting as well as distance weighting of the soil water content (Table 7). This suggests that the variation in the 661 footprint diameter needs to be considered during individual calibration campaigns. Linear depth-662 weighting resulted in a better CRS performance than non-linear depth-weighting since the non-663 linear depth-weighting basically underestimated soil water contents during wet periods (because 664 higher weights of deeper (drier) soil layers were included). This caused both a decrease in the 665 666 mean soil water content as well as a decrease in the variability of the soil water content time series and hence reduced the performance of the CRS. In soils where water content increases with 667 depth the difference between linear and non-linear depth-weighting could be smaller (even 668 negligible), at our field site, however, the decrease of water content with depth apparently 669 favorsrequires the use of a linear depth-weighting function. Adding a correction for above ground 670 biomass to the time series of neutron counts (converting N<sub>bih</sub> to N<sub>bihv</sub> using Eq. 11) did not 671 improve the performance of the CRS measurements. It only marginally changed the shape of the 672

calibration function and produced almost the same time series of soil water content as the version 673 674 without any correction for above-ground biomass. Also, we could not find systematic changes in the calibration results connected to the annual cycle of tree foliation/defoliation (i.e. a reduction 675 676 in counts during summer due to higher hydrogen content in the above ground biomass). 677 Furthermore, our calculations of variable hydrogen mass in the canopy suggested that these seasonal changes are small compared to the changes of hydrogen mass in the soils caused by 678 changes in soil water content. Therefore we deem a correction for variable forest canopy 679 680 hydrogen at different times of the year unnecessary.

The differences in calibration results are more-likely caused by the fact that the shape of the  $N_0$ -681 682 calibration function is different at our field site. That means that while being temporally stable the shape of the calibration function is spatially variable - there is no standard curve applicable to 683 684 all sites. At our site the function is less steep than the standard  $N_0$ -calibration function suggested 685 by Desilets et al. (2010), i.e. a similar increase in neutron counts is associated with a smaller decrease in soil moisture. A recalibration of the shape of the curve using all calibration points 686 considerably improved the agreement between in situ measurements and CRS measurements of 687 soil moisture. A two-point calibration already proved to be sufficient to define the correct shape 688 of the calibration function given that the soil moisture states at the two calibration times weare 689 sufficiently different. In a recent study Iwema et al. (2015) also investigated temporal field 690 691 sampling strategies for three different calibration methods. They tested combinations of different numbers of random sampling dates and found that using more than six random sampling dates 692 693 did not improve their calibration results much more. However, for the  $N_0$ -calibration method they found that selecting sampling dates with distinct soil wetness conditions could reduce the 694 required number of sampling-dates. In conclusion they also recommended more than one 695 calibration campaign for the N<sub>0</sub>-calibration approach and argued that the shape of the calibration 696 697 function should not be fixed but kept variable during the calibration process. This is in line with our findings on the shape of the calibration function. 698

We can only speculate about the reasons behind this shape inconsistency of the calibration function for our site since we did not do any theoretical neutron modeling. To our knowledge at our site we are dealing with the lowest number of counts of all published studies (average  $N_0 =$  $878 \text{ n-h}^{-1} \text{counts h}^{-1}$ , Table 43). Although the calibration function was theoretically developed for Kommentar [A89]: Reply: We restructured the discussion.

Kommentar [A90]: Rev1: Please discuss your results in the light of the results found by Iwema et al. (2015).

Kommentar [A91]: Reply: We added a discussion of the findings of Iwema et al. (2015).

all environments it has not probably never yet been tested sufficiently in such low-count, forested 703 704 environments. Moreover, due to the low neutron count the uncertainty in the determination of soil water content during calibration has a much higher influence on the calibration results than in 705 high-count environments. And while the shape of the function seems to work well in high count 706 environments, it clearly does not at our site. Bogena et al. (2013) pointed out another 707 complicating factor that is present in forested environments - the litter layer. They showed that at 708 their sites ( $N_0$ : 913 to 1397 <del>n h<sup>-1</sup> counts h<sup>-1</sup></del>) the <u>model-derived</u> water content within the litter layer 709 (under spruce) was subject to much higher variability than the water content in the underlying 710 711 soil. During wet conditions the water within the litter layer contained 36 % of the hydrogen mass 712 within the footprint of the CRS while during dry conditions it contained only 10 % of the hydrogen mass. This leads to an increase in the variability of the neutron counts and can thus 713 714 cause an overestimation of soil water content during wet conditions. Although the water within the litter layer at our site accounts for a much smaller fraction of the total hydrogen pool (up to 3 715 %) it can still have an influence on the neutron counts and the calibration results. The occurrence 716 of canopy interception would have the same variability-increasing effect on the CRS signal, 717 although it is expected to be significantly smaller than the influence of the litter layer. We argue 718 that an adjustment to the shape of the calibration function is able to solve this problem. By 719 decreasing the slope of the calibration function we effectively reduce the sensitivity of the CRS 720 721 and hence the temporal variability in the output signal (the time series of soil water content). Baatz et al. (2014) working also in a low-count environment ( $N_0$ : 936 to 1242 n-h<sup>-1</sup>-counts h<sup>-1</sup>) 722 with land use ranging from grassland to agriculture to forest compared the standard  $N_0$ -calibration 723 724 method to another calibration method developed by Shuttleworth et al. (2013) (the COSMIC operator) and found that the former interpreted dry periods drier and wet periods wetter - which 725 is also in accordance to our findings that suggest that the standard  $N_0$ -calibration function is too 726 727 steep. Lv et al. (2014), in a study at a mixed-forest/grassland site also recommended more than one calibration. They operated in a high-count environment in Utah ( $N_0 = 2189 \text{ n-h}^+$  counts h<sup>-1</sup>) 728 and attributed the different shape of their calibration function to binary soil moisture patterns at 729 730 their site where the grassland soils were much drier than the forest soils under wet conditions but just as dry under dry conditions. Our field site is subject to similar spatial variability since it is 731 also comprised of multiple areas with non-uniform soil water content (mean values of soil water 732 733 contents differ between different forest stands). Following the argumentation of Ly et al. (2014), 734 the fact that distance weighting improved our results can be regarded as an indication that non-26

Kommentar [A92]: Rev2: Franz 2013 WRR investigated the impact of horizontal heterogeneity on the signal.

Kommentar [A93]: Reply: We are discussing the topic of horizontal heterogeneity in line 724-736. Here, we are just comparing the count rates of different studies (and in Franz et al. (2013) the lowest count rates are also above 1000 cph.

Kommentar [A94]: Rev3: The absolute count rate has no influence on the shape of the response function, just on the precision of calibration. I would remove this conclusion or reword it to make this conclusion ("it clearly does not at our site") less strong.

Kommentar [A95]: Reply: Ok. We removed this conclusion.

Kommentar [A96]: Rev3: but on page 9831 (of my copy) you stated that the sensitivity is better when using your calibration. Please, make these two statements consistent.

Kommentar [A97]: Reply: On page 9831 we stated that the sensitivity of the sensor is essentially higher than it should be (not better). This means that already a small difference in neutron counts indicates a large difference in soil moisture. The modified calibration accounts for this by decreasing the slope of the calibration function and thereby reducing the sensitivity of the sensor (so that now a bigger difference in neutron counts is required to cause differences in the soil water content reading). We modified our statement on page 9831 (= manuscript line 475) to: '...essentially the sensor has a higher resolution/sensitivity than one would expect.'

735	homogeneous soil moisture conditions indeedalso lead to changes in the shape of the calibration
736	function. At our site, distance weighting reduced the spatial variability within the footprint of the
737	sensor since it assigned higher weights to the closest sampling sites which were all located in the
738	homogenous and relatively wet beech forest, while the influence of the drier soils under the
739	coniferous trees was reduced. In a recent study Iwema et al. (2015) investigated temporal field
740	sampling strategies for three different calibration methods. They also recommend more than one
741	calibration campaign for the $N_0$ calibration approach and argue that the shape of the calibration
742	function should not be fixed but variable during the calibration process.
743	If it was possible to fully correct for all factors that influence footprint size, depth-weighting and
744	neutron count, a one-time calibration of the CRS would be sufficient. However, the abundance of
744 745	neutron count, a one-time calibration of the CRS would be sufficient. However, <u>the abundance of</u> <u>different hydrogen pools and the uncertainties in the sensing depth estimation will always lead to</u>
745	different hydrogen pools and the uncertainties in the sensing depth estimation will always lead to
745 746	different hydrogen pools and the uncertainties in the sensing depth estimation will always lead to uncertainties in the calibration process. Therefore we arguethink that forwhen intending to the
745 746 747	different hydrogen pools and the uncertainties in the sensing depth estimation will always lead to uncertainties in the calibration process. Therefore we arguethink that forwhen intending to the use of the CRS as a simple tool to measure soil water content at intermediate scales, the benefit of

751 -<u>situ samples taken during dry and wet conditions. Hence, Therefore</u> we recommend a two-time-

point calibration that – although being empirical in nature – inherently incorporates many of the
 required corrections.

754

## 755 6. Conclusion

756 Our results suggest that a one-time calibration of the CRS using the available neutron count 757 corrections and weighting approaches is not sufficient at our field site. This is mainly due to the fact that the shape of the standard  $N_0$ -calibration function is not able to reproduce apture the 758 dynamics in soil water content we observed with our network of distributed in situ TDT sensors. 759 Several factors could cause this discrepancy, amongst them the presence of <u>a litter layers</u> and 760 spatially heterogeneous soil moisture conditions within the sensor footprint. After calibrating the 761 CRS 10 times in a mixed forest in north eastern Germany we found that a two-point calibration 762 763 already considerably improveds the agreement between soil water content derived from in situ Kommentar [A98]: Rev1: This statement is not clear to me. Please explain in more detail

Kommentar [A99]: Rev1: This part is somewhat misleading. Corrections of the neutron count rate (Eqs. 1-3) are essential for any application of the CRS (e.g. Zreda et al. 2012). Vegetation correction is only needed for sites with significant biomass changes. On the other hand, the characterization of the temporal stable hydrogen pools is important for the application of the N0-method. However, the abundance of different pools and the uncertainties in the sensing depth estimation will always lead to uncertainties in the calibration process. As shown by Iwema et al. (2015) and by the results found in this study, this issue can be partly circumvented by the using site specific calibration parameters estimated at using in-situ samples taken during dry and wet conditions. Please reformulate in this sense

Kommentar [A100]: Reply: Changed to: 'If it was possible to fully correct for all factors that influence footprint size, depth-weighting and neutron count, a one-time calibration of the CRS would be sufficient. However, the abundance of different hydrogen pools and the uncertainties in the sensing depth estimation will always lead to uncertainties in the calibration process. Therefore we argue that for using the CRS as a simple tool to measure soil water content at intermediate scales, the efforts of measuring all necessary parameters are not justified. As shown by Iwema et al. (2015) and by the results of this study, this issue can be partly circumvented by using site-specific calibration parameters estimated from in-situ samples taken during dry and wet conditions. Hence, we recommend a two-time calibration that - although being empirical in nature inherently incorporates many of the required corrections

TDT measurements and from the CRS, given significantly different moisture conditions during 764 765 the two calibration periods/campaigns (for a detailed explanation on the procedure see Appendix A). We found that the explicit consideration of depth-specific values of soil organic matter and 766 root biomass improved the calibration results while taking into account and seasonal changes in 767 above-ground biomass in the forest was unnecessary were found to be negligible-because of their 768 small amplitude. While there is no doubt that further investigationss on of factors that influence 769 the neutron signal are necessary and useful, it is also apparent that it becomes increasingly 770 difficult to distinguish between the effects of the individual correction factors and the uncertainty 771 772 caused by all the corrections. Therefore our goal was to use empirical data to test available 773 methods and combinations thereof and to provide a guideline on how to easily and comprehensively calibrate a CRS in various environments using these methods. Looking beyond 774 775 that objective, investigations in the form of site intercomparison studies along gradients from 776 high to low-count environments and/or from locations with varying litter layers could give rise to the development of simple corrections to the shape of the  $N_0$ -calibration function. 777

When measuring soil water content with a CRS it is important to note that over time the measurements are hardly ever representative of the exact same soil segment around and below one\_the\_sensor\_(Köhli et al, 2015). With the footprint shrinking and expanding and the eritical effective measurement depth inof the soil decreasing and increasing we have to be careful when interpreting and using our results. If we keep that in mind, however, this new technology will indeed be able to bridge the gap between point in-situ and areal remote sensing soil moisture measurements and thus provide a valuable tool for the advancement of hydrologic understanding.

785

## 786 Appendix A: Best practice for calibration in low-count forest environments

787 We provide an Excel file as a supplement to perform the calculations described in the following
 788 step-by-step instructions.

Set up (or use) a weather station that monitors air temperature and relative humidity close to
 the CRS.

Kommentar [A101]: Rev1: Actually, the seasonal changes of the hydrogen pools in this forest site are negligible. Thus vegetation correction can be omitted.

Kommentar [A102]: Reply: Agreed.

Kommentar [A103]: Rev1: This statement is based on Köhli et al. (2015), but not on results of this study and thus should be omitted.

Kommentar [A104]: Reply: Since this a very important statement and should be considered by everybody using a CRS, we would like to keep it. But we added the proper reference (Köhli et al.).

791	2.	Set up the CRS in a location where the conditions within a radius of at least 30 m around
792		the sensor are relatively homogeneous (similar soils, tree species, expected soil moisture
793		conditions).
794	3.	Switch on the CRS and come back later for calibration (or set it up before 6 a.m. and start
795		calibrating on the same day). You should at least have 12 hours of CRS data for one
796		calibration. Do not switch it off after the calibration, let it record continuously.
797	4.	Choose a day with very dry or very wet soil moisture conditions for the first calibration
798		campaign and wait for the opposite conditions for your second calibration (this might take a
799		full year to achieve, but you will not lose any data, you will just not be able to accurately
800		<u>convert</u> the data immediately).
801	5.	Choose days without rain or snow for your calibrations, litter and canopy should be dry.
802	6.	Take 108 soil samples from 18 locations (six directions, three distances) and six depths (0-
803		30 cm). For equal distance weights choose distances according to Köhli et al. (2015) (~1,
804		~33 and ~140 m). according to Franz et al. (2012b)
805	7.	Weigh the samples the same day you take them, let them oven-dry for 24 h at 105°C and
806		weigh them again to determine the volumetric water content ( $\theta$ ) and the bulk density ( $\rho_{bd}$ ).
807	8.	Create six bulk samples from the six different soil depths (2 g from each of the 18 locations
808		suffices for each soil depth).
809	<u>9.</u>	Analyze-Determine the combined soil organic matter (SOM) and root biomass (B <sub>R</sub> ) content
810		of the six bulk samples by weighing them (after regular oven-drying at 105°C) and then
811		heating them to a temperature of 400°C for 24 h before weighing them again. Convert SOM
812		and $B_R$ to water equivalents by multiplying the ir weight by 0.556.
813		Caution: In clay-rich soils this method tends to overestimate soil organic matter content
814		because some of the lattice water is removed already at temperatures around 400°C
815		(Howard and Howard, 1990).
816	<u>10.</u>	<u>Analyze-Determine</u> the lattice water $(W_L)$ content of the six bulk samples by weighing them
817		(after SOM and $B_R$ extraction at 400°C) and then heating them to a temperature of 1000°C
818		for 24 h before weighing them again.
819		Caution: Carbonate-rich soils experience thermal breakdown of carbonates at temperatures
820		above 430°C (Ben-Dor and Banin, 1989).
821	<del>9.<u>11</u></del>	_Determine the water equivalent of the average hydrogen content of belowground hydrogen
822	I	pools (H <sub>p</sub> ) for each soil depth.

Kommentar [A105]: Rev1: This step is obvious and should be omitted.

Kommentar [A106]: Reply: When we first set up the sensor and calibrated it for the first time we brought a battery with us to let the sensor run. After we had finished the soil collection, we took the battery back home with us. Only later it became clear that we should have collected neutron counts for a longer period of time. So we could not use the data from our first calibration effort. This was a hard lesson to learn and we want to make sure that other people do not make the same, admittedly stupid, mistake.

**Kommentar [A107]:** Rev1: The sampling locations should be adapted to the footprint estimates after Köhli et al. (2015).

Kommentar [A108]: Reply: We adapted the sampling distances to the footprint estimates after Köhli et al. (2015).

Kommentar [A109]: Rev3: Franz et al 2012 is not the correct reference; Franz et al merely repackaged the information given in Zreda et al 2012.

Kommentar [A110]: Reply: We decided to recommend sampling distances according to Köhli et al. (2015). Concerning the sampling pattern we used: Franz et al. 2012 describe 3 circles with distances around the CRS of 25, 75 and 200 m. Zreda et al. 2012 describe 3 circles with distances around the CRS of 25, 75 and 175 m. Since we used 25, 75 and 200 m the more correct citation to describe our calibration setup would be Franz et al. 2012. However, to recognize the contribution of Zreda et al. we inserted the reference in line 174: '...we followed the recommended sampling pattern for the calibration of CRS which was developed by Zreda et al. (2012).'.

Kommentar [A111]: Rev2: Again, is this method for lattice water supported by refs? If not then should be noted that this is a pragmatic procedure with expected minimal error for most soil groups other than volcanics, . . . etc. (?). Unfortunately I don't know all the soil groups this might be affected by so hopefully a pedologist can set us straight.

Kommentar [A112]: Reply: The method of heating the samples to a temperature of 1000°C to determine lattice water was used in many CRS studies (e.g. Zreda et al., 2012; Bogena et al., 2013) The only complication we found occurs in carbonate-rich soils where thermal breakdown of carbonates will contribute to the lattice water account. We added two cautions to the recommendations we give in the appendix.

### 823 Equation (8).

824 10.12. Apply a linear weighting function to your gravimetrically determined H<sub>p</sub> measurements accounting for the change in the critical effective measurement depth z\* of the sensor and 825 826 retrieve a weighted average of H<sub>p</sub> within the footprint of the CRS by iteration. Start out by computing the eritical effective measurement depth z\* corresponding to your 827 gravimetrically determined values of Hp and pbd averaged over the entire 30 cm. Then apply 828 the weights for the different soil depths z and update the values. Recalculate the 829 830 eritical effective measurement depth z\* and continue this procedure until all values stabilize. 831 Do this for each sampling/calibration distance ( $\sim$ 1,  $\sim$ 33 and  $\sim$ 140 m<sup>25</sup>, 75 and 200 m) 832 separately.

Equations (5), (6) and (9).

- 834 H.<u>13.</u> Apply an additional distance-weight to the depth-weighted volumetric water contents 835 from the different locations in order to account for variations in the footprint size. Also do 836 this iteratively adjusting  $H_p$  and the distance weights until both become stable.
- Equations are conveniently provided as a supplement by Köhli et al. (2015) in the form of an Excel filesheet.

# 839 $\left| \frac{+2.14.}{Use} \right|$ Use the depth-and-distance weights to compute weighted values of soil water content ( $\theta$ ), 840 bulk density ( $\rho_{bd}$ ), lattice water ( $W_L$ ), soil organic matter and root biomass water equivalent 841 (SOM-+-B<sub>R</sub>).

- 842 13.15 Average raw neutron counts (N<sub>raw</sub>) from the moderated sensor (measuring fast neutrons) 843 over 12 h with a moving window.
- Retrieve data from the neutron monitor close to your location in order to correct for the
  varying intensity of incoming neutrons (you may have to correct this data and fill gaps).
- 846 15.17. Using the entire time series for the period where cosmic-ray data is available determine 847 average atmospheric pressure (P<sub>0</sub>), average incoming neutron intensity (N<sub>avg</sub>) and average 848 absolute humidity (p<sub>v0</sub><sup>ref</sup>).
- 849 <u>16.18.</u> Correct raw neutron counts for atmospheric pressure variations (N<sub>p</sub>).
  850 Equation (1).
  851 <u>17.19.</u> Correct raw neutron counts for incoming neutron intensity variations (N<sub>pi</sub>).
  852 Equation (2).
- 853 <u>18.20.</u> Correct raw neutron counts for absolute humidity variations ( $N_{pih}$ ).

854 Equation (3).

855	19. Plot the N <sub>pik</sub> of both calibrations against the gravimetrically measured, distance and depth-
856	weighted volumetric soil water content ( $\theta$ ) according to the standard $N_{\theta}$ calibration function
857	with fitting parameters.
858	Equation (4).
859	21. Fit a function through the two calibration points altering $N_0$ , $a_0$ , $a_1$ and $a_2$ (e.g. using
860	Microsoft Excel solver). When doing this, use average values of the two calibration
861	campaigns for bulk density ( $\rho_{bd}$ ), lattice water ( $W_L$ ), soil organic matter and root biomass
862	water equivalent (SOM-+-B <sub>R</sub> ).
863	22. Plot the N <sub>pih</sub> of both calibrations against the gravimetrically measured, distance- and depth-
864	weighted volumetric soil water content $(\theta)$ .
865	<u>20.23.</u> Use best fit parameters to convert time series of $N_{pih}$ to volumetric soil water content.

#### Acknowledgement 867

Funding was provided by the Terrestrial Environmental Observatories (TERENO) and the Virtual 868 Institute for Integrated Climate and Landscape Evolution (ICLEA). We would like to thank the 869 Müritz National Park for allowing us to conductsite our research in their forest. Marvin Reich, 870 Iris Heine, Lisei Köhn, Janek Dreibrodt, Stephan Schröder, Erik Reinholz, Christian Rippich, 871 Christopher Gravesen, Jörg Wummel all helped out in the field while Philip Müller and Hans-872 873 Peter Nabein assisted in the lab. Gabriele Baroni, Lena Scheiffele and Katja Mroos lent us their field equipment and Martin Schrön provided us with scripts for depth-distance-weighting. We 874 thank Heye Bogena and two anonymous referees for their constructive feedback which helped us 875 a lot to improve the manuscript. 876

878	References
879	Baatz, R., Bogena, H.R., Hendricks Franssen, HJ., Huisman, J., Qu, W., Montzka, C., and
880	Vereecken, H.: Calibration of a catchment scale cosmic-ray probe network: A comparison of
881	three parameterization methods, J. Hydrol., 516, 231-244, doi:10.1016/j.jhydrol.2014.02.026,
882	2014.
883	
884	Baatz, R., Bogena, H.R., Hendricks Franssen, HJ., Huisman, J.A., Montzka, C., and Vereecken,
885	H.: An empirical vegetation correction for soil water content quantification using cosmic ray
886	probes, Water Resour. Res., 51, 2030–2046, doi:10.1002/2014WR016443, 2015.
887	
888	Bachelet, F., Balata, P., Dyring, E., and Iucci, N.: Attenuation coefficients of the cosmic-ray
889	nucleonic component in the lower atmosphere, Il Nuovo Cimento, 35, 23-35,
890	doi:10.1007/BF02734822, 1965.
891	
892	Ball, D.F.: Loss-on-ignition as an estimate of organic matter and organic carbon in non-
893	calcareous soils, J. Soil Sci., 15, 84-92, 1964.
894	
895	Baroni, G. and Oswald, S.: A scaling approach for the assessment of biomass changes and
896	rainfall interception using cosmic-ray neutron sensing, J. Hydrol., 525, 264-276,
897	doi:10.1016/j.jhydrol.2015.03.053, 2015.
898	
899	Ben-Dor, E., and Banin, A.: Determination of organic matter content in arid-zone soils using a
900	simple "loss-on-ignition" method, Commun. Soil Sci. Plan., 20, 1675-1695, 1989.
901	
902	Bogena, H.R., Huisman, J.A., Baatz, R., Hendricks Franssen, HJ., and Vereecken, H.: Accuracy
903	of the cosmic-ray soil water content probe in humid forest ecosystems: the worst case scenario,
904	Water Resour. Res., 49, 5778–5791, doi:10.1002/wrcr.20463, 2013.
905	
906	Bouriaud, O., Bréda, N., Moguédec, G., and Nepveu, G.: Modelling variability of wood density
907	in beech as affected by ring age, radial growth and climate, Trees, 18, 264-276,
908	doi:10.1007/s00468-003-0303-x, 2004.

909		
910	Coopersmith, E., Cosh, M., and Daughtry, C.: Field-scale moisture estimates using COSMOS	
911	sensors: a validation study with temporary networks and Leaf-Area-Indices, J. Hydrol., 519, 637-	
912	643, doi:10.1016/j.jhydrol.2014.07.060, 2014.	
913		
914	Davies, B.E.: Loss-on-ignition as an estimate of soil organic matter, Soil Sci. Soc. Am. J. 38,	
915	<u>150-151, 1974.</u>	
916		
917	Desilets, D. and Zreda, M.: Spatial and temporal distribution of secondary cosmic-ray nucleon	
918	intensities and applications to in situ cosmogenic dating, Earth Planet. Sc. Lett., 206, 21-42,	
919	doi:10.1016/S0012-821X(02)01088-9, 2003.	
920		
921	Desilets, D. and Zreda, M.: Footprint diameter for a cosmic-ray soil moisture probe: theory and	
922	Monte Carlo simulations, Water Resour. Res., 49, 3566-3575, doi:10.1002/wrcr.20187, 2013.	
923		
924	Desilets, D., Zreda, M., and Ferré, T.: Nature's neutron probe: Land surface hydrology at an	
925	elusive scale with cosmic rays, Water Resour. Res., 46, W11505, doi:10.1029/2009WR008726,	
926	2010.	
927		
928	Franz, T., Zreda, M., Ferre, T., Rosolem, R., Zweck, C., Stillman, S., Zeng, X., and Shuttleworth,	
929	W.: Measurement depth of the cosmic ray soil moisture probe affected by hydrogen from various	
930	sources, Water Resour. Res., 48, W08515, doi:10.1029/2012WR011871, 2012a.	
931		
932	Franz, T., Zreda, M., Rosolem, R., and Ferre, T.: Field validation of a cosmic-ray neutron sensor	
933	using a distributed sensor network, Vadose Zone J., 11, doi:10.2136/vzj2012.0046, 2012b.	
934		
935	Franz, T., Zreda, M., Rosolem, R., and Ferre, T.: A universal calibration function for	
936	determination of soil moisture with cosmic-ray neutrons, Hydrol. Earth Syst. Sc., 17, 453-460,	
937	doi:10.5194/hess-17-453-2013, 2013.	

939	Gerrits, A.M.J., Pfister, L., and Savenije, H.H.G.: Spatial and temporal variability of canopy and
940	forest floor interception in a beech forest, Hydrol. Process., 24, 3011-3025,
941	doi:10.1002/hyp.7712, 2010.
942	
943	Gravano, E., Bussotti, F., Grossoni, P., and Tani, C.: Morpho-anatomical and functional
944	modifications in beech leaves on the top ridge of the Apennines (Central Italy), Phyton Horn, 39,
945	41-46, 1999.
946	
947	Gupta, H., Kling, H., Yilmaz, K., and Martinez, G.: Decomposition of the mean squared error
948	and NSE performance criteria: Implications for improving hydrological modelling, J. Hydrol.,
949	377, 80-91, doi:10.1016/j.jhydrol.2009.08.003, 2009.
950	
951	Hawdon, A., McJannet, D., and Wallace, J.: Calibration and correction procedures for cosmic-ray
952	neutron soil moisture probes located across Australia, Water Resour. Res., 50, 5029-5043,
953	doi:10.1002/2013WR015138, 2014.
954	
955	Hendrick, L.D. and Edge, R.D.: Cosmic-ray neutrons near the Earth, Phys. Rev., 145, 1023-1025,
956	1966.
957	
958	Howard, P.J.A., and Howard, D.M.: Use of organic carbon and loss-on-ignition to estimate soil
959	organic matter in different soil types and horizons, Biol. Fertil. Soils, 9, 306-310, 1990.
960	
961	Iwema, J., Rosolem, R., Baatz, R., Wagener, T., and Bogena, H.R.: Investigating temporal field
962	sampling strategies for site-specific calibration of three soil moisture-neutron intensity
963	parameterisation methods, Hydrol. Earth Syst. Sci., 19, 3203-3216, doi:10.5194/hess-19-3203-
964	2015, 2015.
965	
966	Kling, H., Fuchs, M., and Paulin, M.: Runoff conditions in the upper Danube basin under an
967	ensemble of climate change scenarios, J. Hydrol., 424-425, doi:10.1016/j.jhydrol.2012.01.011,
968	2012.
969	

Kodama, M., Kudo, S., and Kosuge, T.: Application of atmospheric neutrons to soil moisture
measurement. Soil Sci., 140, 237-242, 1985

972

Köhli, M., Schrön, M., Zreda, M., Schmidt, U., Dietrich, P., and Zacharias, S.: Footprint
characteristics revised for field-scale soil moisture monitoring with cosmic-ray neutrons. Water
Resour. Res., 51, 5772-5790, doi:10.1002/2015WR017169, 2015.

976

Lv, L., Franz, T., Robinson, D., and Jones, S.: Measured and modeled soil moisture compared
with cosmic-ray neutron probe estimates in a mixed forest, Vadose Zone J., 13,
doi:10.2136/vzj2014.06.0077, 2014.

980

Ochsner, T., Cosh, M., Cuenca, R., Dorigo, W., Draper, C., Hagimoto, Y., Kerr, Y., Njoku, E.,
Small, E., and Zreda, M.: State of the art in large-scale soil moisture monitoring, Soil Sci. Soc.
Am. J., 77, 1888, doi:10.2136/sssaj2013.03.0093, 2013.

984

<u>Rivera Villarreyes, C. A., Baroni, G., and Oswald, S. E.: Integral quantification of seasonal soil</u>
 <u>moisture changes in farmland by cosmic-ray neutrons, Hydrol. Earth Syst. Sci., 15, 3843–3859,</u>
 <u>doi:10.5194/hess-15-3843-2011, 2011.</u>

Rosolem, R., Shuttleworth, W., Zreda, M., Franz, T., Zeng, X., and Kurc, S.: The effect of
atmospheric water vapor on neutron count in the cosmic-ray soil moisture observing system, J.
Hydrometeorol., 14, 1659-1671, doi:10.1175/JHM-D-12-0120.1, 2013.

992

988

Santa Regina, I., Tarazona, T., and Calvo, R.: Aboveground biomass in a beech forest and a Scots
pine plantation in the Sierra de la Demanda area of northern Spain, Ann. Sci. Forest, 54, 261-269,
doi:10.1051/forest:19970304, 1997.

996

Shuttleworth, J., Rosolem, R., Zreda, M., and Franz, T.: The COsmic-ray Soil Moisture
Interaction Code (COSMIC) for use in data assimilation, Hydrol. Earth Syst. Sci., 17, 3205–
3217, doi:10.5194/hess-17-3205-2013, 2013.

1001	Rivera Villarreyes, C. A., Baroni, G., and Oswald, S. E.: Integral quantification of seasonal soil
1002	moisture changes in farmland by cosmic-ray neutrons, Hydrol. Earth Syst. Sci., 15, 3843-3859,
1003	doi:10.5194/hess 15 3843 2011, 2011.
1004	
1005	Western, A., Zhou, SL., Grayson, R., McMahon, T., Blöschl, G., and Wilson, D.: Spatial
1006	correlation of soil moisture in small catchments and its relationship to dominant spatial
1007	hydrological processes, J. Hydrol., 286, 113-134, doi:10.1016/j.jhydrol.2003.09.014, 2004.
1008	
1009	Zreda, M., Desilets, D., Ferré, T., and Scott, R.: Measuring soil moisture content non-invasively
1010	at intermediate spatial scale using cosmic-ray neutrons, Geophys. Res. Lett., 35, L21402,
1011	doi:10.1029/2008GL035655, 2008.
1012	
1013	Zreda, M., Shuttleworth, W., Zeng, X., Zweck, C., Desilets, D., Franz, T., and Rosolem, R.:
1014	COSMOS: the COsmic-ray Soil Moisture Observing System, Hydrol. Earth Syst. Sc., 16, 4079-
1015	4099, doi:10.5194/hess-16-4079-2012, 2012.
1016	

	<u>Radius</u>	<u>Radius</u>	<u>Radius</u>	
	<u>0-50 m</u>	<u>50-150 m</u>	<u>150-300 m</u>	<u>Total</u>
Beech	<u>85.2</u>	<u>32.8</u>	<u>48.7</u>	<u>55.5</u>
<u>Pine</u>	<u>3.0</u>	<u>26.3</u>	<u>17.6</u>	<u>15.6</u>
Spruce	<u>5.8</u>	<u>20.9</u>	<u>11.1</u>	<u>12.6</u>
<u>Oak</u>	<u>0.0</u>	<u>10.3</u>	<u>12.5</u>	<u>7.6</u>
Open (grass)	<u>6.0</u>	<u>9.7</u>	<u>3.9</u>	<u>6.5</u>
Larch	<u>0.0</u>	<u>0.0</u>	<u>5.5</u>	<u>1.8</u>
Birch	<u>0.0</u>	<u>0.0</u>	<u>0.7</u>	0.2

1017 <u>Table 1. Fractions of different tree stands in percent within the footprint of the CRS.</u>

1019	Table <u>+2</u> . Overview of the fourive weighting and correction approaches for other than soil
1020	moisture effects on the CRS signal.

Approach	1 SDW	2 DSW	3 DDW	4 DDWnl
simple depth-weighting	<del>yes</del>	no	no	no
consideration of depth-specific W <sub>L</sub> and SOM+B <sub>R</sub> -separately	no	yes	yes	yes
distance depth-weighting	no	no	yes	yes
non-linear depth-weighting	no	no	no	yes
consideration of above-ground biomass	no	no	<del>no</del>	<del>no</del>

1022 Table <u>32</u>. Example of depth weighting (DSW) for an <u>critical effective measurement</u> depth of  $z^* =$ 1023 22.1 cm, a = 0.0903 and b = 1. Calibration campaign date 21 November 2014 (F4). Note the 1024 difference in specific weights if only soil water content  $\theta$  is considered (wt(z, $\theta$ )) or if  $W_L$  and 1025 SOM-+- $B_R$  is also considered (wt(z, $H_p$ )).

Layer (cm)	$\theta$ (m <sup>3</sup> m <sup>-3</sup> )	$W_L (m^3 m^3)$	$\frac{\text{SOM+B}_{R}}{(\text{m}^{3}\text{ m}^{-3})}$	$H_{p} (m^{3} m^{-3})$	ρ <sub>bd</sub> (g cm <sup>-3</sup> )
0-5	0.187	0.002	0.034	0.223	0.669
5-10	0.136	0.004	0.024	0.163	1.143
10-15	0.117	0.004	0.019	0.140	1.217
15-20	0.109	0.004	0.015	0.129	1.256
20-25	0.106	0.005	0.013	0.124	1.359
25-30	0.100	0.005	0.012	0.118	1.431

		$\int^{z+5} wt(z,\theta)$	$\mathbf{u}$	$\int_{0}^{z+5} \operatorname{wt}(z, H_p)$
z (cm)	$wt(z, \theta)$	Jz	$wt(z, H_p)$	Jz
0	0.079	0.356	0.090	0.401
5	0.063	0.278	0.070	0.299
10	0.048	0.200	0.050	0.197
15	0.032	0.122	0.029	0.095
20	0.017	0.044	0.009	0.009
25	0.001	0.000	0.000	0.000
		Σ=1.00		Σ=1.00

1028 Table 43. Atmospheric and soil parameters as well as neutron counts for the 10 calibrations. P is the a<u>A</u>tmospheric pressure <u>P</u>,  $p_{v0}$  is the absolute humidity  $\underline{p}_{v0}$ ,  $N_{raw}$  is the raw neutron count <u>N<sub>raw</sub></u>, 1029  $N_{\rm p}$  is the pressure corrected neutron count  $N_{\rm p}$ ,  $N_{\rm pi}$  is the pressure and incoming radiation corrected 1030 1031 neutron count N<sub>pi</sub>, N<sub>pin</sub> is the pressure, incoming radiation and water vapor corrected neutron 1032 count <u> $N_{\text{pih}}$ </u>,  $N_{\theta}$  is the calibration neutron count <u> $N_{0\tau}$ </u>,  $N_{\text{nm}}$  is the incoming radiation from the neutron monitor <u>N<sub>nm</sub></u>,  $\theta_{30cm}$  is the average soil moisture of the top 30 cm  $\theta_{30cm}$ ,  $\theta_{depthW}$  is the depth-1033 weighted soil moisture  $\frac{\theta_{depthW}}{\theta_{depthW}}$ ,  $(W_L + SOM + B_R)_{depthW}$  is the depth-weighted sum of volumetric 1034 1035 lattice water content, soil organic matter and root biomass water equivalent  $(W_L + SOM + B_R)_{depthw}$ , 1036  $(H_p)_{depthw}$  is the depth-weighted water equivalent hydrogen content of below ground hydrogen 1037 pools  $(\underline{H}_p)_{depthW}$ ,  $(\underline{\rho}_{bd})_{depthW}$  is the depth-weighted bulk density  $(\underline{\rho}_{bd})_{depthW}$  and  $\theta_{mod}$  is the average volumetric soil water content  $\underline{\theta}_{mod}$  of the resulting time series using the N<sub>0</sub>-calibration function 1038 (Desilets et al., 2010) with standard parameters. Mean ( $\mu$ ) and standard deviation ( $\sigma$ ) values of 1039 1040 the 10 calibration campaigns are given in the two bottom lines.

Calibration	P (hPa)	p <sub>v0</sub> (g m <sup>-3</sup> )	$\frac{N_{raw} (\mathbf{h} + \mathbf{h})}{\frac{\mathbf{h}}{\mathbf{b}}}$	$\frac{N_p (n - h)^2}{\frac{b - 1}{2}}$	$\frac{N_{pi} \left(\frac{n \cdot h}{b}\right)}{\frac{h}{b} \cdot 1}$	$\frac{N_{pih} (\mathbf{n})}{\mathbf{h}^{-1}}$	$\frac{N_0 \left(\frac{\mathbf{n} \cdot \mathbf{h}}{\mathbf{h}}\right)}{\frac{\mathbf{h}}{\mathbf{h}} \cdot \mathbf{h}}$
Winter	984.0	5.7	606.2	514.9	518.8	509.4	872.4
Spring1	999.3	8.6	549.2	523.0	527.5	526.2	868.7
Spring2	1021.0	4.9	491.1	550.6	542.8	530.5	871.1
Spring3	1002.9	9.6	544.7	533.1	539.9	541.5	869.2
Spring4	1019.0	8.0	503.4	556.0	549.4	546.1	879.0
Summer	1008.7	14.0	613.3	626.6	623.8	640.5	858.2
Fall1	998.7	11.5	624.7	592.4	593.8	601.5	909.5
Fall2	1014.1	7.8	509.3	542.1	546.7	542.8	876.2
Fall3	990.3	8.5	630.4	561.4	580.4	578.5	892.8
Fall4	1016.7	6.6	544.4	591.0	577.7	569.9	885.7
μ	1005.5	8.5	561.7	559.1	560.1	558.7	878.3
σ	11.9	2.6	50.2	33.1	31.1	37.5	13.8

1041

Calibration	$N_{nm} (\mathbf{n} + \mathbf{b})$ $\frac{\mathbf{h}}{\mathbf{b}}$ $\frac{\mathbf{b}}{\mathbf{b}}$ $\frac{\mathbf{b}}{\mathbf{b}}$	$\theta_{30cm}$ (m <sup>3</sup> m <sup>-</sup> 3)	$\theta_{depthW}$ (m <sup>3</sup> m <sup>-</sup> <sup>3</sup> )	$\begin{array}{c} (W_L + SOM \\ + B_R)_{depthW} \\ (m^3 \ m^{-3}) \end{array}$	$(\mathbf{H}_{p})_{depthW}$ $(\mathbf{m}^{3}  \mathbf{m}^{-3})$	(ρ <sub>bd</sub> ) <sub>depthW</sub> (g cm <sup>-3</sup> )	$\theta_{mod}$ (m <sup>3</sup> m <sup>-3</sup> )
Winter	325.8	0.163	0.228	0.0343	0.262	0.985	0.141

Kommentar [A113]: Rev3: Insert line!

Kommentar [A114]: Reply: I would love to. Actually there was a line when we submitted the manuscript. But it seems that HESS does not allow lines within tables. However, I will try to convince them to leave this line in there because I also think it is necessary.

Spring1	325.5	0.153	0.200	0.0340	0.234	1.013	0.143
Spring2	333.0	0.150	0.185	0.0311	0.216	0.955	0.137
Spring3	324.1	0.140	0.175	0.0324	0.207	1.000	0.143
Spring4	332.2	0.139	0.170	0.0302	0.200	0.957	0.145
Summer	329.8	0.073	0.080	0.0278	0.108	1.074	0.151
Fall1	327.4	0.112	0.137	0.0299	0.167	1.016	0.182
Fall2	325.5	0.140	0.174	0.0310	0.205	0.970	0.144
Fall3	317.5	0.119	0.149	0.0316	0.181	1.018	0.166
Fall4	335.8	0.126	0.150	0.0293	0.179	0.981	0.155
μ	327.7	0.131	0.165	0.0312	0.196	0.997	0.151
σ	5.0	0.024	0.038	0.0019	0.039	0.034	0.013

1043 Table 54. Means ( $\mu$ ) and standard deviations ( $\sigma$ ) of calibration parameter  $N_0$  and means ( $\mu$ ) and 1044 standard deviations ( $\sigma$ ) of resulting time series of volumetric soil water content  $\theta_{mod}$  for the

fourive weighting approaches with 10 calibration campaigns each.

1045

Approach	$(N_0)_{\mu} (\frac{\mathbf{n} \cdot \mathbf{h}}{\mathbf{b}})^{4}$	$(N_0)_{\sigma} \left(\frac{\mathbf{n} \cdot \mathbf{h}}{\mathbf{h}}\right)^{\frac{1}{2}}$	$(\theta_{\text{mod}})_{\mu} (\text{m}^3 \text{m}^3)$	$(\theta_{\text{mod}})_{\sigma} (\text{m}^3 \text{m}^3)$
1 SDW	855.0	17.3	0.158	0.015
2 DSW	878.3	13.8	0.151	0.013
3 DDW	841. <mark>90</mark>	<u>1321.7</u> 5	0.13 <mark>98</mark>	0.01 <mark>2</mark> 7
4 DDWnl	82 <u>8</u> 7. <u>1</u> 7	1 <u>3</u> 9. <u>3</u> 4	0.13 <u>4</u> 3	0.01 <mark>26</mark>
<del>5 ABC</del>	<del>1970.9</del>	<del>50.4</del>	<del>0.138</del>	<del>0.017</del>

1046

Kommentar [A116]: Reply: We modified the text to make the table clearer: 'All resulted in largely deviating N0-values between the individual calibrations (see means and standard deviations in column 1 and 2 of Table 5). This in turn led to differences in the time series of volumetric soil water content between the individual calibrations (see means and standard deviations in column 3 and 4 of Table 5).'

**Kommentar [A115]:** Rev3: I am not sure how to read these results. Can you clarify in the figure caption or in text (which also glosses over this in one short paragraph at the end of section 4.3).

	$N_0$	$\mathbf{a}_0$	$\mathbf{a}_1$	$\mathbf{a}_2$
1 SDW	926.3	0.203	0.109	0.238
2 DSW	1007.8	0.203	0.114	0.267
3 DDW	81 <mark>0</mark> 4.7	0.32 <mark>68</mark>	0.001	0.31 <mark>0</mark> 1
		0. <u>314</u> 27		
4 DDWnl	<u>77</u> 9 <del>04</del> .3	2	0.00 <u>1</u> 0	0.28 <mark>5</mark> 3
<del>5 ABC</del>	<del>1249.1</del>	<del>0.502</del>	<del>0.001</del>	<del>0.312</del>
5 ABC	1240.1	0.502	0.001	

1047 Table <u>65</u>. <u>Modified</u> we calibration parameters for the <u>fourive weighting</u> approaches.

1049 Table 67. Performance measures for the fourive\_weighting approaches – comparison of 1050 modifiednew calibration (mdf) with standard calibration (stanSD). KGE' is the modified Kling-1051 Gupta efficiency,  $\beta$  is the bias ratio and  $\gamma$  is the variability ratio.  $\mu$ -(KGE')<sub>µ</sub> and  $\sigma$ -(KGE')<sub>σ</sub> 1052 represent the mean and standard deviation of the KGE' values of the 10 individual single-point 1053 standard calibrations.

	KGE' mdf <del>new</del>	β mdf <del>new</del>	γ mdf <del>new</del>	<mark>♯-(</mark> KGE' <u>stan</u> SĐ)	<del>σ (</del> KGE' <u>stan</u> SĐ)	<del>μ-(</del> β <u>stan</u> SD)	<del>μ (</del> γ <u>stan</u> SD)
1 SDW	0.830	0.849	0.986	0.675	0.045	1.120	1.258
2 DSW	0.880	0.915	0.964	0.727	0.035	1.032	1.231
	0. <u>891<del>92</del></u>		<u>0</u> 1. <u>986</u> 0	0. <u>712</u> 67			
3 DDW	4	1.0 <u>76</u> 18	<del>06</del>	<del>6</del>	0.08 <u>1</u> 7	0.8 <u>7</u> 8 <del>7</del>	1.2 <u>37</u> 58
		1. <u>148<del>09</del></u>			0. <u>096</u> 10		
4 DDWnl	0.8 <u>33</u> 71	θ	1.0 <u>1</u> 51	0.6 <u>81</u> 74	7	0.8 <mark>21</mark> 8	1.24 <mark>46</mark>
5 ABC	<del>0.920</del>	<del>1.025</del>	<del>0.999</del>	<del>0.676</del>	<del>0.087</del>	<del>0.887</del>	<del>1.258</del>

1055	Table 8. Hydrogen pools (in kg hydrogen per m <sup>2</sup> ) in the CRS footprint for different moisture
1056	conditions (wet: 0.29 m <sup>3</sup> m <sup>-3</sup> , full canopy and litter storage; intermediate: 0.17 m <sup>3</sup> m <sup>-3</sup> , dry canopy
1057	and moist litter storage; dry: 0.05 m <sup>3</sup> m <sup>-3</sup> ). Above-ground biomass is split into a static part (AGB
1058	wet static) comprising stem, branches and dry litter and a variable part (AGB wet variable) that
1059	represents leaves.

<u>Hydrogen Pool</u>	<u>Wet (kg m<sup>-2</sup>)</u>	<u>Intermediate (kg</u> <u>m<sup>-2</sup>)</u>	<u>Dry (kg m<sup>-2</sup>)</u>
AGB wet static	<u>5.24</u>	<u>5.24</u>	<u>5.24</u>
AGB wet variable	<u>0.22</u>	<u>0.22</u>	<u>0.22</u>
<u>SOM+R<sub>B</sub></u>	<u>0.36</u>	<u>0.44</u>	<u>0.66</u>
Lattice water	<u>0.05</u>	<u>0.07</u>	<u>0.15</u>
Pore water	<u>4.12</u>	<u>3.26</u>	<u>1.77</u>
Litter water	<u>0.31</u>	<u>0.11</u>	<u>0.00</u>
Interception	<u>0.17</u>	<u>0.00</u>	<u>0.00</u>
<u>Total</u>	<u>10.47</u>	<u>9.35</u>	<u>8.04</u>

1061	Figure 1. Field site location in Müritz National Park in north eastern Germany. Soil sampling	<	Kommentar [A117]: Rev1: This map should be integrated in figure 2.
1062	locations for calibration (blue dots) and forest vegetation around the CRS (red dot in the center).		Kommentar [A118]: Done!
1063	The TDT soil moisture sensors are located in close vicinity to the sampling locations. The larger		
1064	yellow circle approximates the footprint of the CRS as it was assumed when sampling took place		
1065	(diameter approximately 300 m). The smaller yellow circle approximates the footprint of the		Kommentar [A119]: Rev1: According to recent results of Köhli et al. (2015) the footprint
1066	CRS according to newer modeling results by Köhli et al. (2015) (diameter approximately 200 m).	$\backslash$	is considerably smaller than 300 m. Please adapt the figure. In addition, it would be helpful to color the aerial photograph according to the
1067	Inset: Field site location in Müritz National Park in north-eastern Germany.		different tree species.  Kommentar [A120]: Reply: The figure was
1068			changed accordingly. Since this figure is also supposed to illustrate our sampling scheme we would like to keep the 'old' footprint size. To make the difference clear we rephrased: 'The
1069	Figure 2. Soil sampling locations for calibration (blue dots) and forest vegetation around the CRS		yellow circle approximates the footprint of the CRS as it was assumed when sampling took
1070	(red dot in the center). The TDT soil moisture sensors are located in close vicinity to the		place'. The distribution of different tree species can be seen on Fig. 3 and it would probably make this Figure too busy adding colors or
1071	sampling locations. The yellow circle approximates the footprint of the CRS (diameter = $300 \text{ m}$ ).		patterns on top of the photograph. Kommentar [A121]: Rev1: This map should
1072		/	be integrated in figure 2.
1072		$\left  \right\rangle$	Kommentar [A122]: Done!
1073	Figure 42. Simplified representation of $fF$ actors influencing the raw neutron count (N <sub>raw</sub> ) and the		<b>Kommentar [A123]:</b> Rev1: According to recent results of Köhli et al. (2015) the footprint is considerably smaller than 300 m. Please
1074	measurement support of the CRS in terms of eritical effective measurement depth and footprint.		adapt the figure. In addition, it would be helpful to color the aerial photograph according to the different tree species.
1075	Temporally variable factors are shown on the left: bBarometric pressure (P), canopy interception	1	Kommentar [A124]: Reply: Since this figure is
1076	(I), air humidity (H) and litter layer interception (L). Temporally constant factors (for our study		also supposed to illustrate our sampling scheme we would like to keep the 'old' footprint size. To
1077	site) are shown on the right: vegetation above and below the sensor (V), soil organic matter		make that clear we rephrased: 'The yellow circle approximates the footprint of the CRS as it was
1078	(SOM), root biomass ( $B_R$ ) and lattice water ( $W_L$ )., vegetation (V), litter layer (L), soil organic		assumed when sampling took place'. The distribution of different tree species can be seen on Fig. 3 and it would probably make this Figure
1079	matter (SOM), root biomass (B <sub>R</sub> ) and lattice water (W <sub>L</sub> ) <u>All these factors</u> need to be accounted		too busy adding colors or patterns on top of the photograph.
1080	for <u>in order</u> to isolate the <u>signal from</u> soil water content <u>signal (<math>\theta</math>). The time-variable factors</u>		
1081	require permanent monitoring and dynamic correction, the influence of the constant factors is		
1082	taken into account during calibration. The combination of the time-variable and time-constant		
1083	factors leads to a site specific temporally variable effective measurement depth and footprint		
1084	diameter.		
1085			
1086	Figure 5. Mass of hydrogen in individual beech trees in stem and branches (red diamonds) and		
1087	leaves (green triangles) in relation to diameter at breast height (DBH). Fraction of leaf hydrogen		

mass of total aboveground tree hydrogen mass (orange line). 1088

Figure 63. Gravimetrically determined volumetric soil water content patterns in the footprint of the CRS for the 10 calibration dates. The colored dots indicate the unweighted average value from 0 to 30 cm at the 18 calibration locations. Background colors represent the unweighted average value of all 108 soil samples. Different forest stands (pine, beech, oak, spruce) are indicated by the patterned background.

1095

1089

1096 Figure 74. Upper panel: volumetric water content derived from CRS data for each of the 10 calibration dates separately (vertical lines indicate calibration dates, colors correspond to time 1097 1098 series colors). Filled circles represent the depth-weighted volumetric water content at the time of calibration (according to DSDW). Lower panel: differences in water content between calibration 1099 S1 the calibration resulting in the driest time series (S2) and all other calibrations- expressed as a 1100 percentage of the total possible range of soil water content - ranging from 0.04 m<sup>3</sup> m<sup>-3</sup> to 0.34 m<sup>3</sup> 1101 m<sup>-3</sup>at our field site<del>residual water content to saturated water content</del> (color coding corresponds to 1102 calibration dates in the upper panel). 1103

1104

1105 Figure <u>85</u>. <u>ModifiedNew</u> calibration functions (solid lines) for the four different weighting approaches (simple depth-weighting SDW, depth-specific weighting DSW, distance-depth-1106 weighting DDW, distance-depth-weighting, non-linear DDWnl), each one derived from 10 1107 calibration points (circles). Calibration points are better captured by flatter calibration functions 1108 (solid lines) with modifiednew calibration parameters than by any of the standard calibration 1109 functions (dotted lines) based on a single calibration data set only (days S2 and F1 as an 1110 1111 example). Black lines illustrate that differences in soil moisture between the results of individual calibrations are larger when soil moisture is high. The inset magnifies the area around the 1112 calibration points. 1113

Figure 96. Time series of volumetric water content derived with modifiednew calibration functions usingwith new calibration parameters based on the fourive calibration approaches:
simple depth-weighting (SDW), depth-specific weighting (DSW), distance-depth-weighting (DDW) and, distance-depth-weighting, non-linear (DDWnl) and aboveground biomass correction (ABC). Filled circles represent the weighted average of volumetric water content obtained from soil cores at the time of calibration (weighting according to DDW).

1121

Figure 740. Average vVolumetric water content derived from TDT measurements (black line) 1122 and CRS measurements (orange line) using different calibration functions. Upper panel: the 1123 orange line is an average of the volumetric water content derived from the 10 calibration 1124 1125 campaigns of the CRS using the standard  $N_0$ -calibration function from Desilets et al. (2010) applying the DDW weighting approach. Grey dotted lines are results for 10 individual calibration 1126 campaigns (KGE' values range from 0.579 to 0.834). Lower panel: the orange line is the 1127 volumetric water content derived from thea new-calibration function with modified calibration 1128 1129 parameters applying the DDW weighting approach based on all 10 calibration dates. The colored vertical lines mark the days of the last five calibration campaigns. 1130

1131

1132Figure 844. Best-fit  $N_0$ -calibration functions (red-brown colored lines) for all combinations of1133two-point calibrations (blue dots). Best-fit  $N_0$ -calibration function for 10-point calibration (black1134line). Best-fit two-point  $N_0$ -calibration function derived from calibration points with highest and1135lowest volumetric water content (yellow line).

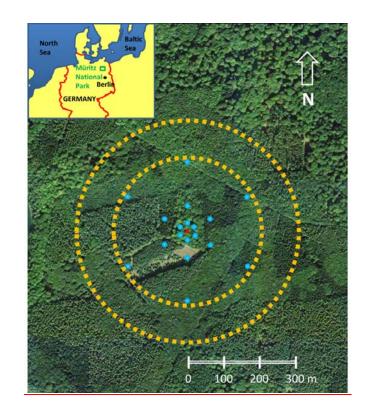
1136

Figure <u>942</u>. Performance of CRS soil water content data derived from two-point calibrations in relation to differencestance between soil moisture states ( $\Delta \theta$ ) at the two calibration dates. The color bar indicates volumetric soil water content. Left panel: points are colored according to the soil water content of the drier calibration date. Right panel: points are colored according to the soil water content of the wetter calibration date. Dashed lines <u>indicate</u>: Pareto front indicating that

1142	soil moisture differences of less than $0.1 \text{ m}^3 \text{ m}^{-3}$ can produce $N_0$ -calibration curves with sub-	
1143	optimal conversions of neutron counts to volumetric soil water content.	Kommentar needs to be d
1144		Kommentar is actually not the text: 'The Fig. 9 indicate
1145	Figure 10. Mass of hydrogen in individual beech trees in stem and branches (red diamonds) and	count-soil wat perform well i between the t
1146	leaves (green triangles) in relation to diameter at breast height (DBH). Fraction of leaf hydrogen	large.'
1147	mass toof total aboveground tree hydrogen mass (orange line).	
1148		
1149	Figure 11: Varying hydrogen pools in the beech forest surrounding the CRS for three different	
1150	site conditions. AGB (above-ground biomass) wet variable represents hydrogen contained in	
1151	deciduous leaves (both in the biomass and in the leaf water). AGB wet static comprises hydrogen	
1152	contained in biomass and water of tree stems and branches as well as in biomass of the litter	
1153	layer.	
1154		
1155	Figure S1. Incoming neutron flux from the neutron monitors in Kiel, Germany and Jungfraujoch,	
1156	Switzerland and synthetic continuous time series of incoming neutron flux combined from these	
1157	two and used for the corrections in this study.	
1158		
1159	Figure S2. Comparison of depth-(and distance-) weighted averages of gravimetrically determined	
1160	soil water content with unweighted gravimetrically determined soil water content of the upper 15	
1161	cm of the soil. The first two weighting approaches overestimate soil water content in the upper 15	
1162	cm especially at high soil water contents. The last two approaches have only a slight negative	
1163	offset and no significant relationship with wetness conditions.	
1164		

# Kommentar [A125]: Rev1: The Pareto front needs to be discussed in the text as well.

Kommentar [A126]: Reply: We realized that it is actually not a Pareto front. So we added to the text: 'The existence of a rather clear front in Fig. 9 indicates that the calibrated neutron count-soil water content conversion will always perform well if the soil moisture differences between the two calibrations are sufficiently larce.'



1166Figure 1. Soil sampling locations for calibration (blue dots) and forest vegetation around the CRS1167(red dot in the center). The TDT soil moisture sensors are located in close vicinity to the1168sampling locations. The larger yellow circle approximates the footprint of the CRS as it was1169assumed when sampling took place (diameter approximately 300 m). The smaller yellow circle1170approximates the footprint of the CRS according to newer modeling results by Köhli et al. (2015)1171(diameter approximately 200 m). Inset: Field site location in Müritz National Park in north-1172eastern Germany.

Kommentar [A127]: Rev1: According to recent results of Köhli et al. (2015) the footprint is considerably smaller than 300 m. Please adapt the figure. In addition, it would be helpful to color the aerial photograph according to the different tree species.

Kommentar [A128]: Reply: The figure was changed accordingly. Since this figure is also supposed to illustrate our sampling scheme we would like to keep the 'old' footprint size. To make the difference clear we rephrased: 'The yellow circle approximates the footprint of the CRS as it was assumed when sampling took place'. The distribution of different tree species can be seen on Fig. 3 and it would probably make this Figure too busy adding colors or patterns on top of the photograph.

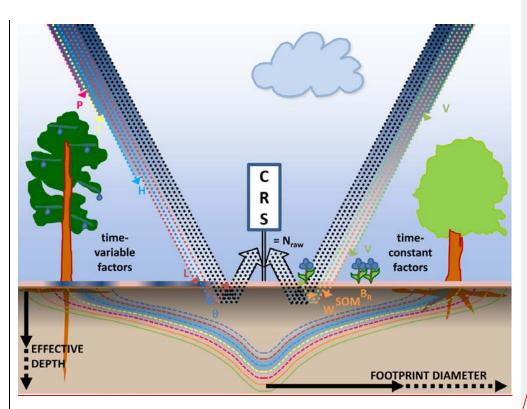


Figure 2. Simplified representation of factors influencing the raw neutron count  $(N_{raw})$  and the measurement support of the CRS in terms of effective measurement depth and footprint. Temporally variable factors are shown on the left: barometric pressure (P), canopy interception (I), air humidity (H) and litter layer interception (L). Temporally constant factors (for our study site) are shown on the right: vegetation above and below the sensor (V), soil organic matter (SOM), root biomass  $(B_R)$  and lattice water  $(W_L)$ . All these factors need to be accounted for in 1180 order to isolate the soil water content signal  $(\theta)$ . The time-variable factors require permanent 1181 monitoring and dynamic correction, the influence of the constant factors is taken into account 1182 during calibration. The combination of the time-variable and time-constant factors leads to a site 1183 1184 specific temporally variable effective measurement depth and footprint diameter.

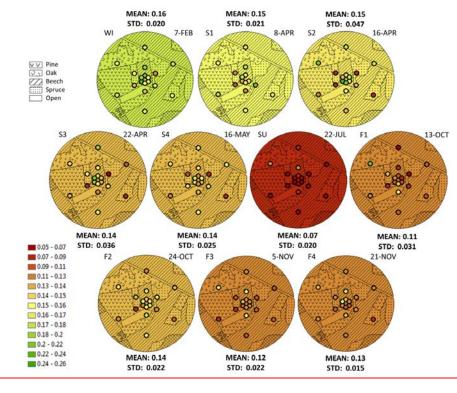
1185

Kommentar [A129]: Rev3: can you group these factors into two groups: (1) constant in time (eg, WL), and (2) variable in time (eg, water vapor)? And then perhaps also into another groups: (3) those measured at calibration (eg, WL), and (4) those measured as time series (eg, water vapor)? The significance is that some parameters are easy to handle. others are difficult, and the two should not be commingled.

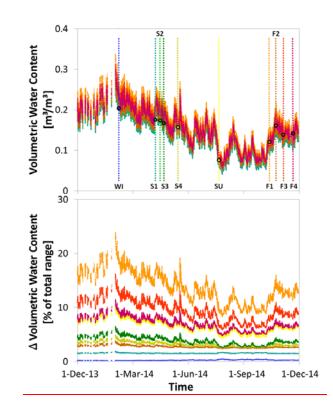
Kommentar [A130]: Reply: We revised the figure according to your suggestions. We grouped the factors into two groups and mentioned which of them need to be monitored continuously and which can be accounted for during calibration

Kommentar [A131]: Rev1: This schematic figure is wrong in presenting the cosmic-ray neutron intensities as actual rays that are reflected by the soil. The actual processes leading to neutron intensity are far more complex (see e.g. Köhli et al., 2015) and should not be presented in this way in a scientific paper. Also the above ground and below ground footprints are not connected in the simple way as suggested by the schematic drawing. Thus, the figure should be omitted.

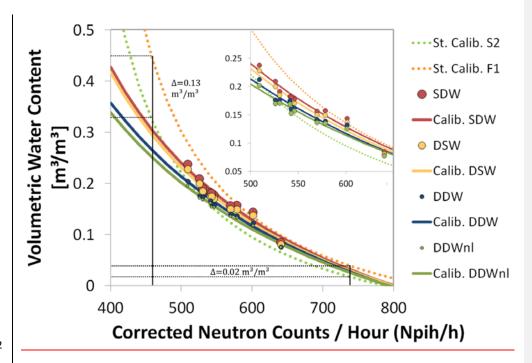
Kommentar [A132]: Reply: We acknowledge the fact that this figure simplifies the actual processes a lot and have added this statement to the caption. We have modified the figure to resolve two of your concerns. The neutron intensities are not any longer depicted as rays and the above-ground footprint was removed entirely. We still think that the figure helps to get an overview over the many parameters that have to be accounted for before/during the use of the CRS method.



1187	Figure 3. Gravimetrically determined volumetric soil water content patterns in the footprint of the
1188	CRS for the 10 calibration dates. The colored dots indicate the unweighted average value from 0
1189	to 30 cm at the 18 calibration locations. Background colors represent the unweighted average
1190	value of all 108 soil samples. Different forest stands (pine, beech, oak, spruce) are indicated by
1191	the patterned background.



1194Figure 4. Upper panel: volumetric water content derived from CRS data for each of the 101195calibration dates separately (vertical lines indicate calibration dates, colors correspond to time1196series colors). Filled circles represent the weighted volumetric water content at the time of1197calibration (according to DDW). Lower panel: differences in water content between calibration1198S1 and all other calibrations expressed as a percentage of the total possible range of average soil1199water content – ranging from 0.04 m³ m⁻³ to 0.34 m³ m⁻³ residual water content to saturated water1200contentat our field site (color coding corresponds to calibration dates in the upper panel).



1202

Figure 5. Modified calibration functions (solid lines) for the four different weighting approaches 1203 (simple depth-weighting SDW, depth-specific weighting DSW, distance-depth-weighting DDW, 1204 distance-depth-weighting, non-linear DDWnl), each one derived from 10 calibration points 1205 (circles). Calibration points are better captured by flatter calibration functions (solid lines) with 1206 modified calibration parameters than by any of the standard calibration functions (dotted lines) 1207 1208 based on a single calibration data set only (days S2 and F1 as an example). Black lines illustrate 1209 that differences in soil moisture between the results of individual calibrations are larger when soil moisture is high. The inset magnifies the area around the calibration points. 1210

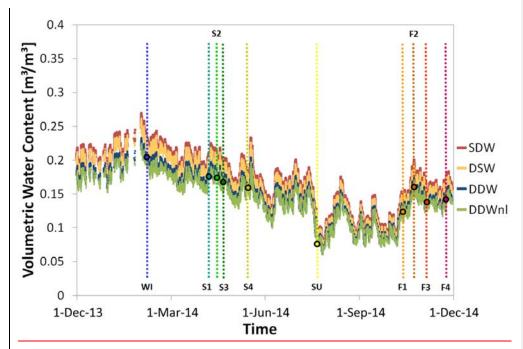


Figure 6. Time series of volumetric water content derived with modified calibration functions
using parameters based on the four calibration approaches: simple depth-weighting (SDW),
depth-specific weighting (DSW), distance-depth-weighting (DDW) and distance-depthweighting, non-linear (DDWnl). Filled circles represent the weighted average of volumetric water
content obtained from soil cores at the time of calibration (weighting according to DDW).

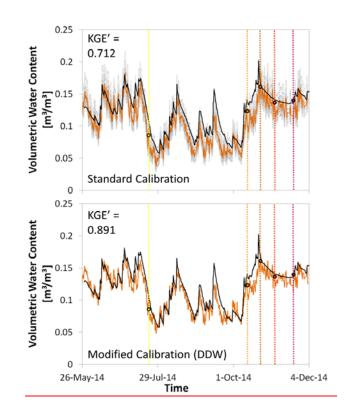
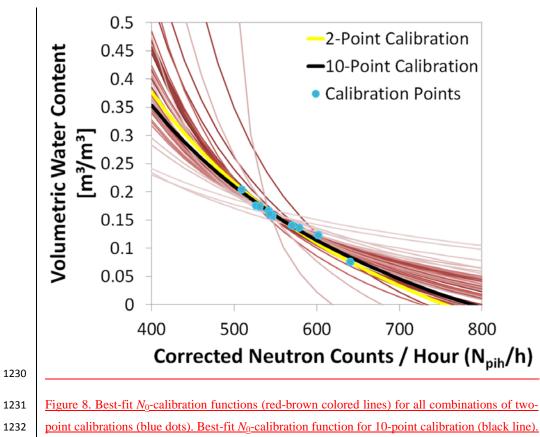
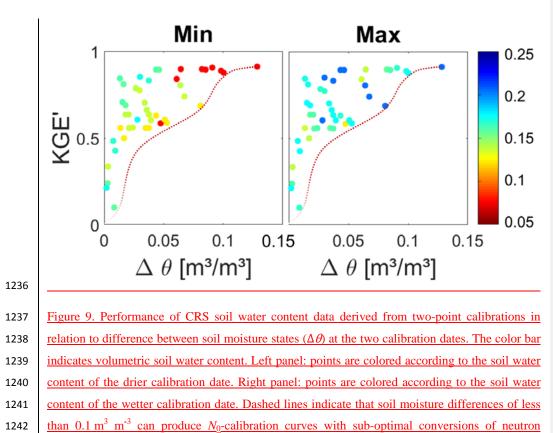


Figure 7. Average volumetric water content derived from TDT point measurements (black line) and CRS measurements (orange line) using different calibration functions. Upper panel: the orange line is an average of the volumetric water content derived from the 10 calibration campaigns of the CRS using the standard No-calibration function from Desilets et al. (2010) applying the DDW approach. Grey dotted lines are results for 10 individual calibration campaigns (KGE' values range from 0.579 to 0.834). Lower panel: the orange line is the volumetric water content derived from the calibration function with modified calibration parameters applying the DDW weighting approach based on all 10 calibration dates. The colored vertical lines mark the days of the last five calibration campaigns. 1228



Best-fit two-point No-calibration function derived from calibration points with highest and lowest

volumetric water content (yellow line).

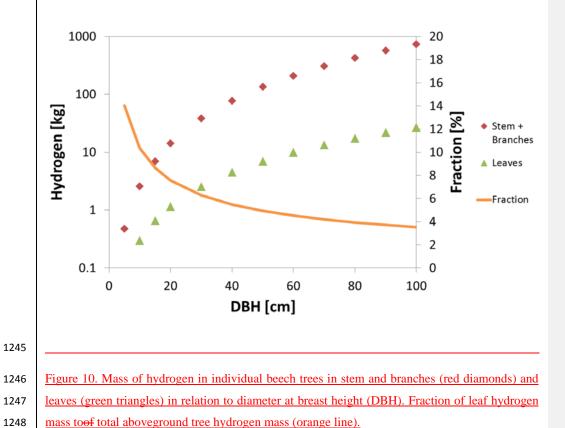


counts to volumetric soil water content

1244

Kommentar [A133]: Rev1: The Pareto front needs to be discussed in the text as well.

Kommentar [A134]: Reply: We realized that it is actually not a Pareto front. So we added to the text: 'The existence of a rather clear front in Fig. 9 indicates that the calibrated neutron count-soil water content conversion will always perform well if the soil moisture differences between the two calibrations are sufficiently large.'



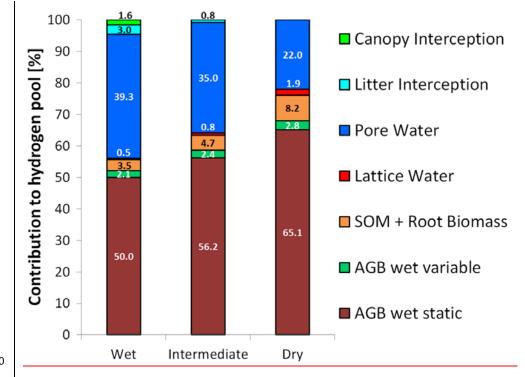
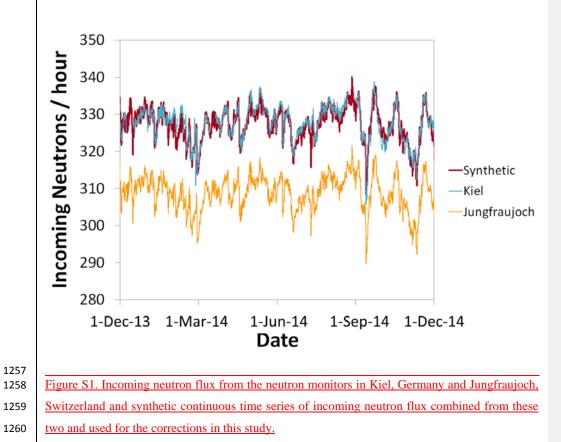


Figure 11: Varying hydrogen pools in the beech forest surrounding the CRS for three different site conditions. AGB (above-ground biomass) wet variable represents hydrogen contained in deciduous leaves (both in the biomass and in the leaf water). AGB wet static comprises hydrogen contained in biomass and water of tree stems and branches as well as in biomass of the litter layer.



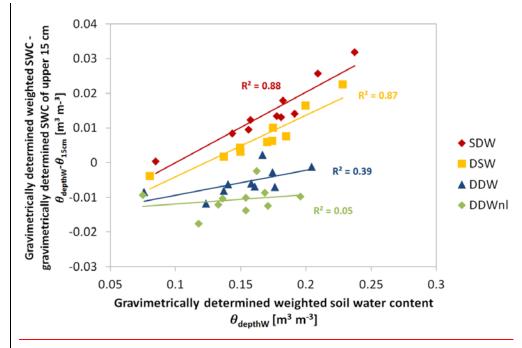


Figure S2. Comparison of depth-(and distance-) weighted averages of gravimetrically determined 1263 soil water content with unweighted gravimetrically determined soil water content of the upper 15 1264 cm of the soil. The first two weighting approaches overestimate soil water content in the upper 15 1265 cm especially at high soil water contents. The last two approaches have only a slight negative 1266 offset and no significant relationship with wetness conditions.