Editor Decision: Publish subject to minor revisions

(Editor review) (25 Mar 2016) by Prof. Mauro Giudici Comments to the Author:

Based on the assessment by the referees, I ask the Authors to provide a new version, in order to fix the residual flaws of the mansucript.

Non-public comments to the Author:

Since I will take the final decision by myself, i.e., without another round of review, I ask you to be as precise and comprehensive as possible in the answer to the referees.

I also stress that one of the referees clearly expressed his disappointment for the way in which the referees' suggestions were considered in the previous revisions. Therefore, I ask you to make an additional effort to carefully reconsider also previous comments and the whole discussion on this manuscript, to possibly improve the quality of the final paper.

Authors' response to the editor.

We have now gone through the list of minor comments made by referee #3 to the previous version of the manuscript. We have responded to these comments in our reply letter below, and the responses have also led to minor edits of and additions to the new revised manuscript.

We are confused by the somewhat disappointment expressed by referee #1 after the latest revision. Our confusion arises when we consider the referee's comments to the previous revision: "The new manuscript is a vast improvement and most sweeping statements of the previous version have been removed. It is overall a nice contribution that will be of interest to hydrogeophysicists and hydrogeologists around the world. I don't agree with all the responses made by the reviewers in their response letter, but I find mostly that the new version of the manuscript is mature and convincing."

Mentioning his/her disappointment, Referee #1 refers back to the disappointment expressed by referee #3 after the first revision. Referee #3 gave a list of major and minor comments to that revision which we should address. We did address these comments, and referee #3 now finds that most of those comments "are tackled in the revised version of the manuscript". The logical conclusion for us is that both referee #3 and referee #1 should now be satisfied. We do not know of what else to improve except to completely redesign our experiments, and this is impossible at this stage.

Referee #1: The author's response and corrections

Like the new reviewer 3, I am a bit disappointed by the very minimalistic revisions that are made by the authors in response to detailed reviews and constructive comments. I have provided two very detailed rounds of reviews in the past, and I see little need to provide yet another detailed review. The review comments and the changes made respond to the minimum required. The paper is suitable for publication in Hess and the paper has a sufficient level to be published in Hess. More careful and in-depth revisions would have led to a better paper, but so be it. Also, it is a bit disconcerting to see suggested edits and missing references be introduced in one version and then see them disappear in the next version.

Authors response to referee #1

First, we would like to thank referee #1 for the many constructive and useful comments given during the review process. They have indeed helped to improve the manuscript in many ways.

We are a bit confused about the disappointment now expressed by referee #1, considering the referee's comments to the previous revision: "The new manuscript is a vast improvement and most sweeping statements of the previous version have been removed. It is overall a nice contribution that will be of interest to hydrogeophysicists and hydrogeologists around the world. I don't agree with all the responses made by the reviewers in their response letter, but I find mostly that the new version of the manuscript is mature and convincing."

We put a lot of effort into making the first (previous) revision, and we also put a lot of effort into making the second revision by responding satisfactorily to the many useful comments made by the new referee #3. Now Referee #3 finds that most of those comments "are tackled in the revised version of the manuscript". We acknowledge that some suggestions made by referee #1 that was worked into the first revised manuscript may have been rephrased, moved or discarded in the later revision, but this was done as response to comments made by referee #3.

Referee #3: The author's response and corrections

Dear authors,

I think that most of my comments are tackled in the revised version of the manuscript. I have a few minor comments related to this updated version:

Comment from referee	Authors response	Author's changes in manuscript
1. P5L5-7. For clarity, I would switch the sentence as "the simulated response of one model (geophysical model) is used as input to constrain the other model (hydrologic model)" because it is generally the hydrologic model which is the objective (the one which is used for predictions).	We have reversed the order and deleted our example.	Done
 2. P6L15-16. It is true that the specific scheme of Ruggeri et al. has not been extended to groundwater modelling, but other stochastic Bayesian schemes have. For example, the study of Hermans et al. (2015) uses multiple-point statistics and probability perturbation method, it integrates geophysical data to the groundwater model in a Bayesian way, with a link to hydrofacies (indirectly linked to hydraulic conductivity) in a field case. I would also remove the sentence in parenthesis ("Such extension will probably") as it is speculative. Other stochastic schemes have already been used, it could probably be the case for this one, too. Hermans et al. 2015. Uncertainty in training imagebased inversion of hydraulic head data constrained to ERT data: Workflow and case study. Water Resources Research, 51, 5332-5352. 	We agree with the referee.	We have removed: "(Such extension will probably turn out to be yet computationally infeasible.)" We have added a few sentences on P6.L21-24 about the study of Hermans et al. (2015)

3. P6LL20-21. "Such data set is rare for investigation of the systems and scale considered here". This sentence is a little-bit strong as it suggests that it could not be applied in practice. What is needed are co-located boreholes and EM soundings, which is not that rare if the geophysical survey is well-designed. Especially in Denmark where a huge database is available, some work is currently done to link resistivity to lithology (and therefore hydraulic conductivity). I thus expect that Bayesian method will be extended in the future and should not be presented as impractical	We think our statement is fair, also for Denmark. (We are talking about "hydraulic conductivity", not just "lithology".) Anyhow, since the statement is unimportant we will delete it.	Statement deleted.
4. P6L25. The paper by Irving and Singha does not have a small number of parameters (more than 500) but it is simplified in term of lithology.	What we meant with "small number of parameters" was that K within each of the facies was assumed constant and known, while it is in "reality" varying spatially within the facies – meaning that the model parameterization is much simpler than the reality (Irving and Singha, 2010, p. 6). Anyhow, to avoid misunderstanding we will remove the last part of the sentence.	We have removed: "and very few unknown parameters".
5. P19L9. I think it should be equation 2 instead of 4.	The referee is correct. It is equation 2.	Done.
6. P19L16. I would give here the reference to Herckenrath et al. (2013) so that it is clear which paper the reader should read to understand the method in details (for example, how the parameters are updated). I think some of the confusion arises from the fact that it is not specified here that resistivity is also considered as unkown in JHI and inverted together with K using Pest.	We agree.	Herckenrath et al. (2013) have been added to p19L16. Two lines above, we inserted for clarification of joint inversion of resistivity and K: "(hydraulic conductivity and electrical resistivity at the pilot points)".
7. P21L3-7. Why in parenthesis? Note that it is not case-specific as some authors found improvement by using a filtering scheme.	We agree that the choice of weighting may indeed be important in other cases than the one studied here.	We added: "Choice of weights can be important in other cases (Beaujean et al., 2014)".

(reference to Beaujean et al., 2014). Beaujean et al. 2014. Calibration of seawater intrusion models: Inverse parameter estimation using surface electrical resistivity tomography and borehole data, Water Resources Research, 50, 6828-6849.	We think that the problem in our case is that the hydrological data have low sensitivity to the K distribution within the deepest part of the buried valley which is also where the resistivity estimates are most uncertain. Therefore, weighting in eq. 6 will have very little influence on the hydrological inversion result for the deepest part of the valley; this mainly depends on the choice of initial parameter values, see comment p22.L20-23. Similar is seen by a	
	comparison of JHI-H and JHI-G results in Figure 5. We find that this explanation is complicated to give on p. 21, so we restrict ourselves to just add: "Choice of weights can be important in other cases".	
8. P24L16-17. I would replace "may not be unique" by "is non-unique". This problem is well-known in geophysics for underdetermined, ill-posed problems. Changing the parameters in Pest doesn't make the minimization unique, it would just be a specific case (if it exists) for which the solutions tend to the same result. So I would remove the last sentence.	We agree.	"may not be unique" changed to "is non-unique". And we have removed: "However, we did not investigate if PEST parameters could have been set differently to thereby make the JHI minimization unique."
9. P26L2-4. This affirmation is somehow in contradiction with the fact that the filtering scheme did not improve the results.	We agree; we commented on the unimportance of the filtering scheme under comment 7 above.	Nothing changed.
10. P26L23-24. " show wider horizontal scatter". I would rephrase. As it is, the sentence sounds negative, whereas the wider scatter enables to encompass the 1:1 line to some extent, and is thus an improvement (at	We agree and remove the sentence. The following sentence gives a fair description of the estimates of JHI-G and JHI-H, respectively, and favors the buried-valley estimates of the former for	We have removed: "For sand and gravel deposits Error! Reference source not found. shows wider horizontal scatter for JHI-G than for JHI-H."

least, a few hydraulic conductivities are	those of the latter.	
correctly estimated).		
11. P27L5. Deepest instead of deeper?	The referee is correct.	Changed "deeper" to "deepest"
12. P29L26. Do you mean column 5 of Figure 7,	Yes, we mean column 5.	Done.
because there are only 5 columns, not 6.		
13. The reference list should be updated with the	We have carefully gone through the	Done
new references.	bibliography to ensure that all reference	
	are present.	

Testing alternative uses of electromagnetic data to reduce the prediction error of groundwater models

4 N. K. Christensen¹, S. Christensen¹, and T.P.A Ferre²

5 [1]{Department of Geoscience, Aarhus University, Aarhus, Denmark}

6 [2]{Department of Hydrology and Water Resources, University of Arizona, Tucson, USA.}

7 Correspondence to: N. K. Christensen (phda.nikolaj.kruse@geo.au.dk)

8

9 Abstract

10 Despite that geophysics is being used increasingly, it is often unclear how and when the 11 integration of geophysical data and models can best improve the construction and predictive capability of groundwater models. This paper uses a newly developed HYdrogeophysical TEst-12 13 Bench (HYTEB) which is a collection of geological, groundwater and geophysical modeling 14 and inversion software to demonstrate alternative uses of electromagnetic (EM) data for 15 groundwater modeling in a hydrogeological environment consisting of various types of glacial 16 deposits with typical hydraulic conductivities and electrical resistivities covering impermeable 17 bedrock with low resistivity (clay). The synthetic three dimensional reference system is 18 designed so there is a perfect relationship between hydraulic conductivity and electrical 19 resistivity. For this system it is investigated to what extent groundwater model calibration and, 20 often more importantly, model predictions can be improved by including in the calibration 21 process electrical resistivity estimates obtained from TEM data. In all calibration cases, the 22 hydraulic conductivity field is highly parameterized and the estimation is stabilized by (in most 23 cases) geophysics-based regularization.

24 For the studied system and inversion approaches it is found that that resistivities estimated by 25 sequential hydrogeophysical inversion (SHI) or joint hydrogeophysical inversion (JHI) should 26 be used with caution as estimators of hydraulic conductivity or as regularization means for subsequent hydrological inversion. The limited groundwater model improvement obtained by 27 using the geophysical data probably mainly arises from the way these data are used here: the 28 29 alternative inversion approaches propagate geophysical estimation errors into the hydrologic 30 model parameters. It was expected that JHI would compensate for this, but the hydrologic data 31 were apparently insufficient to secure such compensation. With respect to reducing model 32 prediction error, it depends on the type of prediction whether it has value to include geophysics 33 in a joint or sequential hydrogeophysical model calibration. It is found that all calibrated models 34 are good predictors of hydraulic head. When the stress situation is changed from that of the 35 hydrologic calibration data, then all models make biased predictions of head change. All calibrated models turn out to be a very poor predictor of the pumping well's recharge area and 36 37 groundwater age. The reason for this is that distributed recharge is parameterized as depending

- on estimated hydraulic conductivity of the upper model layer which tends to be underestimated.
 Another important insight from our analysis is thus that either recharge should be parameterized
 and estimated in a different way, or other types of data should be added to better constrain the
 recharge estimates.

Testing alternative uses of electromagnetic data to reduce the prediction error of groundwater models

3 N. K. Christensen¹, S. Christensen¹, and T.P.A Ferre²

4 [1]{Department of Geoscience, Aarhus University, Aarhus, Denmark}

- 5 [2]{Department of Hydrology and Water Resources, University of Arizona, Tucson, USA.}
- 6 Correspondence to: N. K. Christensen (phda.nikolaj.kruse@geo.au.dk)

Field Code Changed

7

8 Abstract

9 Despite that geophysics is being used increasingly, it is often unclear how and when the integration 10 of geophysical data and models can best improve the construction and predictive capability of 11 groundwater models. This paper uses a newly developed HYdrogeophysical TEst-Bench (HYTEB) 12 which is a collection of geological, groundwater and geophysical modeling and inversion software 13 to demonstrate alternative uses of electromagnetic (EM) data for groundwater modeling in a 14 hydrogeological environment consisting of various types of glacial deposits with typical hydraulic 15 conductivities and electrical resistivities covering impermeable bedrock with low resistivity (clay). 16 The synthetic three dimensional reference system is designed so there is a perfect relationship 17 between hydraulic conductivity and electrical resistivity. For this system it is investigated to what 18 extent groundwater model calibration and, often more importantly, model predictions can be 19 improved by including in the calibration process electrical resistivity estimates obtained from TEM data. In all calibration cases, the hydraulic conductivity field is highly parameterized and the 20 21 estimation is stabilized by (in most cases) geophysics-based regularization.

For the studied system and inversion approaches it is found that that resistivities estimated by sequential hydrogeophysical inversion (SHI) or joint hydrogeophysical inversion (JHI) should be used with caution as estimators of hydraulic conductivity or as regularization means for subsequent hydrological inversion. The limited groundwater model improvement obtained by using the geophysical data probably mainly arises from the way these data are used here: the alternative inversion approaches propagate geophysical estimation errors into the hydrologic model parameters. It was expected that JHI would compensate for this, but the hydrologic data were

1 apparently insufficient to secure such compensation. With respect to reducing model prediction 2 error, it depends on the type of prediction whether it has value to include geophysics in a joint or 3 sequential hydrogeophysical model calibration. It is found that all calibrated models are good 4 predictors of hydraulic head. When the stress situation is changed from that of the hydrologic 5 calibration data, then all models make biased predictions of head change. All calibrated models turn 6 out to be a very poor predictor of the pumping well's recharge area and groundwater age. The 7 reason for this is that distributed recharge is parameterized as depending on estimated hydraulic 8 conductivity of the upper model layer which tends to be underestimated. Another important insight 9 from our analysis is thus that either recharge should be parameterized and estimated in a different 10 way, or other types of data should be added to better constrain the recharge estimates.

11

12 **1** Introduction

13 **1.1** Using hydrologic models for decision support

14 Groundwater models are commonly constructed to support decision-makers in managing 15 groundwater resources. The model can, for example, be used to predict the impact of changes in 16 groundwater pumping on hydraulic head and wellhead protection areas or to predict the fate and 17 transport of groundwater pollution. In general terms, process models are used to base predictions of 18 interest on all of the knowledge that we have about the physical/chemical system and the driving 19 key processes. In this paper we will focus on 3D models typically used for decision support on large 20 spatial scale (from tens to thousands of square-kilometers) with a heterogeneous and possibly complex geology. Deterministic groundwater modelling is generally used in such cases because the 21 22 model simulation time is too long to make it feasible to use stochastic modeling. We will therefore 23 mainly focus on deterministic groundwater modeling in the following.

A deterministic groundwater model is based on a conceptual model that encapsulates prior knowledge of important physical and chemical conditions and processes of the complex real world system. The conceptual model is translated into a numerical groundwater model whereby its reasonableness can be tested by comparing forward simulations with field observations. If the conceptual model appears reasonable, the groundwater model is calibrated by adjusting model parameters until simulated values fit corresponding field observations sufficiently well. The

1 calibrated model is subsequently used to make predictions (Reilly 2001; Reilly and Harbaugh 2 2004). However, the prediction will be uncertain for various reasons of which we will emphasize 3 three. (i) Model calibration is done by fitting uncertain data. The calibrated parameters will therefore also be uncertain and this uncertainty is propagated to the model predictions (Hill 1998; 4 Moore and Doherty 2006; Tonkin et al. 2007). A model's predictive uncertainty will only be 5 6 reduced by calibration if the information content of the calibration dataset constrains the parameter 7 values that significantly influence the prediction (Harvey and Gorelick 1995; Feyen et al. 2003; 8 Franssen et al. 2003). Thus this source of uncertainty can only be reduced by collecting more or 9 more accurate data of type(s) and location(s) that constrain parameter values important to the 10 prediction. The data will typically be hydrologic or hydraulic, but it can also be geophysical. (ii) Because of scarcity and lack of sensitivity of data, there will always be small scale heterogeneity 11 12 that cannot be resolved. A groundwater model will therefore always contain small scale structural 13 errors, which may not cause bias in predictions but may still cause large prediction uncertainty 14 (Cooley 2004; Cooley and Christensen 2006; Refsgaard et al. 2012). (iii) A model is also prone to 15 possess large-scale structural errors that can cause significant bias and uncertainty of estimated parameters and simulated predictions (Doherty and Welter 2010; Doherty and Christensen 2011; 16 17 Refsgaard et al. 2012). This bias and uncertainty can be reduced by collecting data that resolve the 18 large-scale structures of the studied hydrogeological system, which can then be accurately 19 represented in the model. This can, for example, be spatially dense geophysical data sets.

Model errors will lead to errors and uncertainties in predictions of interest. One of the key questions to address in creating models for decision support is: which additional data are most likely to improve key predictions? The types of data available for use in hydrologic analysis are increasingly diverse, including physical, chemical, isotopic, and geophysical data. In light of this complexity, it can be very difficult to compare the likely contributions of diverse data to modelbased decision support.

26

27 **1.2** Informing hydrologic models with geophysics

Over the last three decades, noninvasive geophysical methods have been used increasingly to construct groundwater models (Hubbard and Rubin 2000; Vereecken et al. 2004). This is particularly true for data collected by Airborne Electromagnetic Methods (AEM) because they can be collected quickly, densely, and at a relatively low cost for the very large spatial coverage (Steuer

1 et al. 2008; Viezzoli et al. 2010b; Abraham et al. 2012; Sànchez et al. 2012; Refsgaard et al. 2014; 2 Munday et al. 2015). Large-scale AEM (or ground-based EM) investigations have been used to 3 delineate aquifers, aquitards, and buried valleys or other structures containing aquifers (Auken et al. 2003; Sandersen and Jørgensen 2003; Jørgensen et al. 2003; Abraham et al. 2012; Oldenborger et 4 5 al. 2013), to assess aquifer vulnerability (Refsgaard et al. 2014; Foged et al. 2014a), to map 6 saltwater intrusion (Fitterman and Deszcz-Pan 1998; Viezzoli et al. 2010b; Lawrie et al. 2012; 7 Herckenrath et al. 2013b), and to map freshwater resources (Steuer et al. 2008; Sànchez et al. 2012; 8 Munday et al. 2015). The main drawbacks of electromagnetic (EM) data are: 1) ambiguity in 9 relating electrical properties to hydraulic properties; and 2) reduced lateral and vertical resolution 10 with depth. The former effect can limit the quantitative use of geophysical data for parameterizing groundwater models. The latter effect makes identification of deep structures difficult (Danielsen et 11 12 al. 2003; Auken et al. 2008), which will have different influences on predictions that are dominated 13 by shallower or deeper flow paths.

Geophysical data must be related to properties or states of hydrologic relevance to use them in constructing hydrologic models. Whether the geophysical data are used to define hydrostratigraphic units or subregions or to parameterize the model, the data are often inverted. The way in which hydrologic and geophysical data are inverted and integrated can impact the extraction of information from geophysical data (Dam and Christensen 2003; Day-Lewis 2005; Moysey et al. 2005; Linde et al. 2006; Singha and Gorelick 2006; Singha and Moysey 2006; Hinnell et al. 2010).

20 The simplest inversion approach is sequential hydrogeophysical inversion (SHI). In the first step of 21 this approach, the geophysical data are inverted independent of the hydrologic data or model. In the 22 second step, the inverted geophysical properties are used to zonate or directly parameterize the hydrologic model (Hubbard et al. 1999; Dam and Christensen 2003; Seifert et al. 2007; Koch et al. 23 24 2009; Di Maio et al. 2013; Marker et al. 2015). This is based on the assumption that the geophysical 25 responses are sensitive to some of the same structures and property distributions that the hydrologic data are sensitive to. Using the SHI approach has built-in challenges. In the first step, the 26 geophysical inversions are typically stabilized by using regularization and smoothing constraints 27 28 that do not reflect real physical conditions (Day-Lewis 2005; Linde et al. 2006; Singha and Gorelick 29 2006; Singha and Moysey 2006). Therefore one must be cautious when using such geophysical 30 property estimates to infer hydraulic zones or property estimates to be used in the second step of the SHI (Day-Lewis 2005; Slater 2007; Hinnell et al. 2010). Furthermore, with the SHI approach used 31

in the following the geophysical models cannot be easily updated to conform to the hydrologic
 observations. Such updating is allowed by the SHI approach of Dam and Christensen (2003).

3 Two inversion alternatives to SHI are coupled hydrogeophysical inversion (CHI) and joint 4 hydrogeophysical inversion (JHI) (Hinnell et al. 2010). For both alternatives, the hydrologic and 5 geophysical data sets are inverted simultaneously. In CHI, the simulated response of one model 6 (e.g. the geophysical model) (e.g. the hydrologic model) is used as input to constrain the other model-(e.g. the hydrologic model) (e.g. the geophysical model). (For example, during the inversion 7 8 a water table simulated by the hydrologic model is used to constrain the depth of a layer boundary of the estimated geophysical model.) CHI has been applied successfully for reducing parameter 9 10 uncertainty by using ground penetrating radar and electrical resistivity tomography data in hydraulic models (Kowalsky et al. 2005; Hinnell et al. 2010). In JHI, the hydrologic and geophysical models 11 12 are coupled directly through some of their parameters using assumed relationships among the 13 geophysical and/or hydrologic parameters (Hyndman et al. 1994). For EM data, JHI is typically 14 done using a relationship between hydraulic conductivity and electrical resistivity inspired by 15 Archie's law (Archie 1942; Revil and Cathles 1999; Purvance and Andricevic 2000; Slater 2007).

16 Applications of sequential and joint version of hydrologic and geophysical data using a 17 petrophysical relationships in groundwater modeling have been demonstrated by Herckenrath et al. 18 (2013a) and Vilhelmsen et al. (2014). Herckenrath et al. (2013a) were comparing a SHI with JHI 19 for a large-scale groundwater model using ground-based EM data. Vilhelmsen et al. (2014) were 20 demonstrating a method for joint inversion of aquifer test data, magnetic resonance sounding data, 21 and ground-based electromagnetic data. For synthetic benchmarking, both of these studies were 22 using a simple model with few layers with constant parameter values, and they were evaluating the model performance by the means of improved model parameter values and reduction of parameter 23 24 uncertainty. However, as concluded by e.g. Zhou et al. (2014) the goal of groundwater model 25 calibration is not just parameter identification, but also to increase the model's prediction capability.

Petrophysical relationships between hydraulic conductivity and electrical resistivity are difficult to establish, because such translation tend to be site, scale and facies specific (Hyndman and Tronicke 2005; Slater 2007). Therefore methods have been developed that do not rely on a petrophysical relationship between a property of the geophysical model and the property of the hydrological model. For example, Marker et al. (2015) developed a deterministic SHI approach where spatially dense AEM data is first inverted; then combined with scarce lithological data from boreholes to

1 form a clay fraction model for the sediments of the subsurface (Foged et al. 2014b); subsequently 2 cluster analysis of electrical resistivity and clay-fraction values is used to generate one or more 3 structural model realizations for the subsurface (Foged et al. 2014a); finally the structural model(s) 4 are used in the groundwater model that is calibrated against hydrological data. He et al. (2014,2015) 5 developed a similar methodology where the transition probability method is used to generate the 6 structural model realizations from borehole data and AEM estimated resistivities. The 7 methodologies of Marker et al. (2015) and He et al. (2015) were both used by them on large spatial 8 scale. However, the number of calibrated parameters was kept small by assuming hydraulic 9 conductivity to be constant within an entire deposit or structure. The methodologies are thus 10 stochastic in term of generating structure but deterministic in term of representing and estimating 11 property fields.

12 Full stochastic approaches have been developed. For example, Ruggeri et al. (2013) developed a 13 Bayesian simulation approach to estimate the hydraulic conductivity field from measurements of 14 geopysical parameters. So far the method has only been used for estimation along short profile 15 lines (Ruggeri et al. 2013;2014), and the Bayesian scheme has not yet been extended to also involve hydrological data and groundwater modeling. (Such extension will probably turn out to be yet 16 17 computationally infeasible.) - Furthermore, the methodology of Ruggeri et al. (2013) requires 18 existence of a petrophysical relationship between electrical resistivity and hydraulic conductivity; 19 the relationship does not need to be known in which case a data set of collocated measurements of electrical resistivity and hydraulic conductivity are required. Such a data set is rare for 20 21 investigations of the systems and scale considered here. An alternative Bayesian approach has been was presented by Hermans et al. (2015), who integrate multiple and multiscale data types to falsify 22 alternative structural models using a stochastic search method. The methodology was demonstrated for a 23 24 field case using hydraulic head data and electrical resistivity tomography to constrain a hydrological 25 model. Stochastic inversion approaches have been developed that invert electricial resistivity (ER) 26 and hydrological data. Irving and Singha (2010), for example, describe a Markov-chain-Monte-27 Carlo (McMC) method to estimate a binary hydraulic conductivity field from ER and tracer test 28 data. So far this McMC method seems to be applicable only for small domains and very few 29 unknown parameters (Irving and Singha, 2010).

³⁰ In the following we therefore keep focus on use of geophysics in connection with deterministic 31 groundwater modeling. We particularly focus on application and comparison of SHI and JHI when

used in connection with groundwater investigation of large domains with three-dimensional
 heterogenous hydrogeological and geophysical systems.

- 3
- 4

5 **1.3 Testing the worth of using geophysics**

It is intuitively clear that spatially dense geophysics can offer valuable information for improved 6 7 groundwater modeling for decision making. However, many important questions can be raised. For 8 example: how beneficial is it to collect and use EM data in groundwater modeling for a complex 3D 9 hydrogeological system; how much can be gained by using for example JHI instead of SHI for 10 model calibration; are both inversion approaches prone to lead to biased parameter estimates or 11 model predictions; and what model prediction types will benefit from using EM data in connection with the model development and calibration. The answers to these questions will to some (large?) 12 13 extend depend on the actual hydrogeological setting as well as on what types of prediction are going 14 to be made by the groundwater model.

15 To provide such answers we have developed a cross-disciplinary, flexible platform to examine the worth of geophysical data for improvement of groundwater model predictions in potentially 16 17 complex environments. The platform can be used to build synthetic experiments that have similarity 18 with the actual hydrogeological and geophysical systems to be investigated, the types of data to 19 potentially be collected, and the types of models to potentially be used. The flexibility of the 20 platform allows easy investigation of the data worth when using alternative data sampling and 21 alternative modeling or inversion strategies. Because of the supposed similarity between the 22 synthetic and the actual systems, the conclusions from the synthetic study can be transferred to 23 actual investigation. The platform is called HYTEB, which is an abbreviation of **HY**drogeophysical 24 TEst-Bench. HYTEB builds on a merge of software from different disciplines such as stochastic 25 hydrogeological modeling, groundwater modeling, geophysical modeling, and advanced highly parameterized inversion using SHI, CHI or JHI. HYTEB can also support examination of use of 26 geophysics in a stochastic groundwater modeling context (which will be demonstrated in a 27 28 manuscript in preparation).

1 1.4 Objectives

2 The paper has the following objectives. First, it will present the important elements and steps in use 3 of HYTEB. Since HYTEB and its use is interdisciplinary, the presentation and the following case 4 study introduce geophysicists to the methods, challenges, and purposes of groundwater modeling, 5 and groundwater modelers to some of the challenges of using mainly electromagnetic data for 6 groundwater model calibration purposes. Second, HYTEB is used to examine the worth of adding a 7 ground based time-domain electromagnetic data set to a hydrological data set when making a 8 groundwater model for a glacial landscape of a kind that is typical to parts of Northern Europe and 9 North America. It is investigated if the worth of adding the geophysical data depends on the type of 10 groundwater model prediction as well as on whether the geophysical and hydrological data are 11 inverted sequentially or jointly. Section 2 of this paper describes the elements of HYTEB and how 12 they are used, Section 3 describes the case study, Section 4 presents the results, while Section 5 13 makes a summary and draw conclusions.

14 2 The elements and concept of HYTEB (HYdrogeophysical TEst-Bench)

15 Our primary objective in developing HYTEB is to provide a synthetic environment that allows users to determine the value of geophysical data and, further, to investigate how best to use those 16 17 data to develop groundwater models and to reduce their prediction errors. We suggest that this can 18 best be investigated by using a synthetic case study for which the "generated synthetic", in the 19 following termed "reference", hydrologic and geophysical systems are known and the influences of 20 different sources of error can be investigated. We use physical and geophysical forward simulators 21 to generate measurements that would be collected from the reference systems in the absence of 22 noise. We then examine the influence of measurement error and other sources of error on model 23 predictions of interest. By repeating this for different synthetic system realizations (i.e. for different reference systems) and for different data sets it becomes possible to statistically quantify the worth 24 25 of the various data for improving the predictions of interest. The work flow of HYTEB is shown in 26 Figure 1Figure 1. The procedure is divided into 6 steps, which will be described separately and 27 briefly in the following subsections.

1 2.1 Step 1 - Generation of geological realization

2 The first step is to generate a synthetic realization of the type of geological system under study. The 3 generation can be made conditional on lithological data from boreholes. The borehole data can be 4 imaginary, a real data set, or a combination of data, hydrogeologic structure, and geostatistics. 5 Figure 1Figure 1, step 1, displays an example of a generated system consisting of categorical geological deposits on a plain as well as in a valley buried under a part of the plain. The deposits are 6 7 underlain by impermeable bedrock (not shown). Such categorical geological settings can, for 8 example, be generated using T-PROGS (Carle 1999) or BlockSIS (Deutsch 2006). The spatial 9 discretization used for the geological realization also defines the spatial discretization of the 10 numerical model used to simulate groundwater flow or any other process model that a user decides 11 to integrate into HYTEB.

12

13 2.2 Step 2 - Generation of reference groundwater system, data set, and predictions

14 Using the same spatial discretization as in step 1, the second step is to define the boundary 15 conditions and the hydraulic and solute transport property values for the generated geological 16 system. The hydraulic and solute transport properties can include, for example, hydraulic 17 conductivity, specific storage, and effective porosity. For categorical deposits (as in Figure 1) the 18 value of each type of property will typically vary among categories as well as within each category. Such variation can be simulated as categorical random fields by using e.g. SGSIM (Deutsch and 19 20 Journel 1998) or FIELDGEN (Doherty 2010). The generated realization of boundary and property 21 values is used in a numerical simulator of groundwater flow and solute transport to simulate a set of 22 state variables to be used in step 5 as hydrologic observations used for model calibration; random 23 error is typically added to this observation data to represent all sources of noise that corrupt real 24 observations. The numerical simulator is also used to simulate a set of predictions that are considered of particular interest to the study. We have implemented MODFLOW-2000 (Harbaugh 25 26 et al. 2000) as the numerical simulator of groundwater flow and MODPATH (Pollock 1994) to 27 simulate solute transport by particle tracking.

In the following, the numerical simulators using the boundary conditions and property values that represent the system realization are called "the reference groundwater system", and the predictions (for example forecasts) simulated for this system are called "reference predictions".

1

2 2.3 Step 3 - Generation of reference geophysical system and data set

3 The third step is to define the property values of the geophysical system corresponding to the 4 geological realization generated in step 1. Like the hydraulic properties, the geophysical properties 5 can be considered and simulated as categorical random fields. A geophysical property of relevance can, for example, be the electrical resistivity of the spatially variable geological deposits. For some 6 7 geological systems, it is found or assumed that there is correlation between electrical resistivity and 8 hydraulic conductivity. In this case, the hydraulic and geophysical property fields must be generated 9 to be dependent. Various empirical petrophysical relationships between hydraulic conductivity and 10 electrical resistivity have been proposed (Slater 2007). Both positive and negative relationships 11 have been reported, and there can be significant uncertainty in the relationship (e.g. Mazáč et al. 12 1985). It is common to use a linear log-log relationship which is given some theoretical support by 13 Purvance and Andricevic (2000). Having defined the property values of the geophysical reference 14 system, the geophysical instrument responses are simulated to produce a noise-free geophysical 15 data set that can be corrupted by adding method specific and random error. Ideally a 3D code 16 should be used. Codes for 3D computation of TEM responses have been developed (e.g. Árnason 17 1999), but the computation is impractical and burdensome. As a practical alternative we suggest to 18 simulate TEM responses by a 1D code, where the 1D geophysical model is created from the 19 reference system by pseudo-3D sampling, that is by taking the logarithmic average of the cells 20 within the radius of the EM foot print at a given depth. Modeling TEM in 1D can be problematic in connection with mineral exploration, but for sedimentary environments the 1D approach should 21 22 work well (Auken et al. 2008; Viezzoli et al. 2010a). In HYTEB we use AarhusInv (Auken et al. 23 2014) to simulate electromagnetic instrument responses.

Field Code Changed

In the following, the geophysical simulator using the actual realization of geophysical parameter values is called the "reference geophysical system".

26

27 2.4 Step 4 - Model construction and parameterization

In this step, the synthetic data are used to constrain parameter estimation for a groundwater model of the reference groundwater system. Each property of the real groundwater and geophysical systems needs to be parameterized in the groundwater model. This step thus corresponds to the 1 construction of a groundwater model of a real field system on the basis of the available real data. In 2 the synthetic case, the groundwater model can be discretized exactly as the "reference groundwater 3 system" or it can use a coarser discretization. Here we adopt the former alternative to reduce 4 numerical discretization error. However, this effect could be examined if it were of interest to a 5 particular study.

6 In studies of real systems, the groundwater model is often constructed to consist of zones of 7 uniform hydraulic properties. The subdivision into zones is typically done subjectively by an expert 8 on the basis of geological, hydrological, and geophysical data (Seifert et al. 2007; Di Maio et al. 9 2013). This principle can also be used to define zones of a model of the synthetic groundwater 10 system by using the synthetic lithological data from boreholes used in step 1, the hydrological data 11 set generated in step 2, and geophysical models estimated by inverting the geophysical data sets 12 generated in step 3. In this case, the geophysical data must be inverted between step 3 and step 4. 13 The inverted data are used either in step 4 to support parameterization of the groundwater model or 14 in step 5 for groundwater model calibration. To avoid over-reliance on the geophysical data, it may 15 be argued that they should not be used in both steps 4 and 5. If the geophysical data are used in step 4, they must be inverted before inverting the hydrological data (carried out in step 5); this is an 16 17 example of sequential hydro-geophysical inversion (SHI).

An alternative parameterization approach uses the concept of pilot points (Certes and De Marsily 1991) to parameterize the property fields and to let the data determine the variation of the model 20 property fields (e.g. Doherty, 2003). Pilot point approaches result in a smooth property variation 21 within the model domain (Doherty 2003) rather than sharp zonal parameter fields. Pilot points can 22 be used in combination with zones e.g. to represent property variation within categorical deposits.

HYTEB allows any type of parameterization, for example zones, pilot points, or combinationshereof.

It is emphasized that in the following we use the term "groundwater model" for a simulator that is set up, parameterized, and calibrated to make "model predictions" of states occurring in the reference groundwater system. States occurring in (i.e. simulated for) the reference groundwater system are here termed "reference predictions". The objective of model calibration is to make the model predictions as similar as possible to the reference predictions.

1 **2.5** Step 5 – Calibrate the model(s)

2 The fifth step is to calibrate the groundwater model by using the data set produced in step 2 to 3 estimate the model parameters. The step may also include estimation of geophysical model 4 parameters on the basis of the data sets produced in step 3. The simultaneous estimation of the 5 hydrologic and geophysical parameters can be done by using either the coupled (CHI) or joint (JHI) 6 hydro-geophysical inversion approaches (Hinnell et al. 2010; Vilhelmsen et al. 2014). When the 7 number of parameters is large compared to the number of data, the minimization can be aided by 8 using a regularization technique (for example singular value decomposition or Tikhonov 9 regularization); see Oliver et al. (2008) for an overview.

10

11 2.6 Step 6 - Simulate model predictions, then repeat steps 1-6

12 After successful calibration, the groundwater model is used to make model predictions equivalent to 13 the reference predictions of step 2. (A prediction is a state-variable different from the calibration 14 data, for example a forecast.) For each prediction, this produces one value computed by a calibrated 15 model that can be compared with the equivalent reference value. It is not possible to make 16 meaningful inference about a model's ability to make a specific prediction from just one 17 experiment. To test the reproducibility the experiment, steps 1 to 6 needs to be repeated a number of 18 times. Each repetition involves generation of a new realization of the geological system and the 19 corresponding reference groundwater and geophysical systems, new data sets (i.e. new reference 20 systems), model calibration, and predictions. The number of repetitions should be sufficient to 21 provide a basis for making consistent statistical inference on the model prediction results.

22

23 2.7 Step 7 - Evaluate model prediction results

When steps 1 to 6 have been completed, an ensemble of pairs of model prediction and equivalent reference prediction are plotted to evaluate the model performance. As discussed by Doherty and Christensen (2011), if the plotted data do not scatter around the identity line, it indicates bias in the model prediction. If the intercept of a regression line through the scatter of points deviates from zero it indicates consistent bias in the prediction due to consistent errors in null space parameter components omitted from the parameterized groundwater model; if the slope of the regression line deviates from unity it indicates parameter surrogacy incurred through model calibration (see
 Doherty and Christensen, 2011, for further explanation).

3 Ultimately, calibrated models are used to make predictions of interest. These predictions are 4 generally in the future and may describe the response of the system to alternative management 5 actions. The calibrated model, or model ensemble, can be used to predict future hydrologic 6 responses to near-term actions, thereby providing information critical to informed decision making. 7 Increasingly, these decisions consider both the accuracy (bias) and the uncertainty of model 8 predictions in a probabilistic framework (Freeze et al. 1990; Feyen and Gorelick 2005; Nowak et al. 9 2012)

10

11 **3 Demonstration model**

12 We demonstrate the use of HYTEB through a synthetic case focusing on making three types of 13 model predictions that are commonly useful for groundwater management: (i) hydraulic head; (ii) 14 head recovery and change of groundwater discharge related to abandoning pumping from a well; 15 and (iii) the recharge area and the average age of groundwater pumped from that well. The synthetic demonstration model used here is, to a large degree, inspired by the model of Doherty and 16 17 Christensen (2011). The hydrogeological setting of the model domain is typical for large areas of 18 northern Europe and North America: a glacially formed landscape with a buried tunnel valley eroded into impermeable bedrock (fat clay) with very low electrical resistivity (Wright 1973; 19 20 Piotrowski 1994; Clayton et al. 1999; Jørgensen and Sandersen 2006). The case is designed to have 21 a perfect relationship between hydraulic conductivity and electrical resistivity. This is chosen to make a best possible case for resolving change of lithology and change of hydraulic conductivity 22 23 inferred from of electrical resistivity. The deposits above the bedrock are glacial of different types. 24 For the sake of clarity, the synthetic model will be described in the section below, and the 25 exceptions and changes from the setup of Doherty and Christensen (2011) will be highlighted. Each HYTEB step will be presented in order following Figure 1. 26

1 3.1 Generation of geological system realizations (Step 1)

2 The domain is rectangular, 7 km north-south (N-S) and 5 km east-west (E-W). It is capped by 50 m 3 of glacial sediments deposited as gently N-S elongated layered structures composed of sand, silt or 4 clayey till. The bedrock consists of impermeable clay with a horizontal top surface in most of the 5 catchment, but a 150 m deep and 1500 m wide valley has been eroded into it in the central part of the domain (Doherty and Christensen, 2011, used a 1000 m wide valley). The valley has sloping 6 7 sides with an angle of approximately 17 degrees and runs in the N-S direction from the coast and 5 8 km inland (Doherty and Christensen, 2011, used a steeper 21 degree slope). The valley is filled with 9 glacial sediments deposited in highly N-S elongated layered structures consisting of gravel, sand, 10 silt or clayey till. The exact stratigraphy is only known at the locations of 35 synthetic boreholes of 11 varying depth (Figure 2Figure 2). This borehole stratigraphy was used to condition all generated 12 geological system realizations.

Realizations of the 3D geological model were generated on a uniform rectangular grid. The cells of the grid have horizontal dimensions of 25 m x 25 m and 10 m thickness, so the overall dimensions of the grid are $(n_x, n_y, n_z) = (200,280,20)$, giving a total of 1,200,000 cells. The categorical depositional geology of the 3D model grid was simulated using T-PROGS (Carle 1999). The proportions and mean lengths for the different categories of sediments are provided in <u>Table 1Table</u> **1**. The bedding is represented as a maximally disordered system using "maximum entropy" transition frequencies (Carle 1999).

A total of 1000 geologic system realizations were generated. These categorical realizations were all conditioned on the same stratigraphy for the 35 boreholes, but are otherwise independent. Figure Sigure 3 shows one of these realizations.

23

24 **3.2** Reference groundwater system, data, and predictions (Step 2)

The groundwater system is bounded to the south by a large freshwater lake (specified head), while the other lateral boundaries are closed (no flux). The flow is steady state and driven by recharge caused by the difference between precipitation and evapotranspiration. The local recharge depends on the type of sediment at the surface (because this is assumed to influence evapotranspiration). Most of the groundwater discharges into the lake directly from the subsurface, but approximately 35% discharges into a straight stream running 3.5 km inland S-N in the middle of the domain from 1 the southern boundary (coast). (The setup used by Doherty and Christensen, 2011, did not include a 2 stream.) Furthermore, groundwater is pumped from a deep well located in the south-central part of 3 the buried valley. The well is located at x=2487.5m and y=1912.5 and the pumping rate is 0.015 4 m^3s^{-1} . The well screens the deepest 10 meters of the valley in a laterally extensive body of sand and 5 gravel.

Within each category of sediment, the hydraulic conductivity varies as a horizontally correlated
random field. The same is the case for porosity and recharge. The random fields were generated by
FIELDGEN (Doherty, 2010) using the sequential Gaussian simulation method (Deutsch and
Journel 1998) with the geostatistical parameters given in Table 1Table 1.

10 3.2.1 Hydrological data set

11 All 35 boreholes have been constructed as monitoring wells; each well screens the deepest 10 m 12 (deepest cell) of sand registered in the borehole (Table 2Table 2; Figure 2Figure 2). For each 13 realization, groundwater flow was simulated as confined using MODFLOW-2000 (Harbaugh et al. 14 2000). The corresponding set of values for the hydrological observations, consisting of hydraulic 15 head in the 35 wells and the river discharge, were extracted from the MODFLOW-2000 output. Independent Gaussian error with zero mean and 0.1 m standard deviation was added to the true 16 head values to produce the head observations. Gaussian error with zero mean and a standard 17 18 deviation corresponding to 10 % of the true river discharge was added to the discharge to produce 19 the stream flow observation used for model calibration.

20

21 3.2.2 Reference predictions

Collecting and using new geophysical data is likely to constrain some groundwater model parameters more than others. Different predictions of interest will have different sensitivities to different model parameters. As a result, the addition of geophysical data for groundwater model calibration is likely affect the error of model predictions differently. To illustrate this, we present seven types of predictions of interest in Table 3Table 3.

Prediction types 1 to 3 relate to steady-state flow conditions with groundwater being pumped from
the deep well in the buried valley. This is the same situation for which the hydrological dataset was
generated. Type 1 concerns head prediction at ten locations (Figure 2 Figure 2 and Table 4 Table 4).

1 Type 2 is the size of the recharge area of the pumping well. Type 3 is the average age of the 2 groundwater pumped from the well.

3 Prediction types 4 to 7 relate to a new steady-state long after pumping from the well has been 4 stopped. Type 4 is head recovery at the ten locations given in Figure 2 Figure 2 and Table 4 Table 4. Type 5 is the travel time of a particle flowing with the groundwater from the location where it 5 enters the system at the northern domain boundary (x=2500, y= 6975.5, z =0) until it exits the 6 7 system either into the lake (at the southern boundary) or into the stream. Type 6 is the relative 8 location of the exit point of that particle defined as the Euclidean distance between the reference 9 and the model predicted endpoint in a three dimensional space. Type 7 is groundwater discharge 10 into the stream.

11 The prediction types 1, 4 and 7 were simulated by MODFLOW-2000 (Harbaugh et al. 2000). The 12 other prediction types were simulated by forward particle tracking using MODPATH version 5 13 (Pollock 1994) and MODFLOW-2000 results. Types 5 and 6 were simulated by tracking a single particle with MODPATH. Types 2 and 3 were simulated by placing particles in a horizontally 14 15 uniform 25 m grid at the surface (i.e. releasing one particle at the surface at the center of each 16 model cell) and tracking them forward in time until they reached either the river, the southern 17 boundary, or the pumping well. Each particle represents an area of 25 x 25 m². The number of 18 particles ending in the pumping well thus defines the well's recharge area. The average ground-19 water age is computed as the weighted average of the travel time for all of the particles captured by the well. The weight for a particle is calculated as the recharge rate (in m^3/s) from the 25 x 25 m^2 20 21 surface area represented by the particle divided by the pumping rate. This sum of all weights adds to 22 one because water only enters the model through the uppermost layer.

23

24 **3.3** Reference geophysical system and data – step 3

In the demonstration example, the geophysical property of interest is electrical resistivity of the subsurface. For simplicity it is assumed that there is a perfect relationship between hydraulic conductivity and electrical resistivity. The relationship is of the form

$$log_{10}(K) = \beta_1 + \beta_2 \cdot log_{10}(\rho), \tag{1}$$

1 where *K* is the hydraulic conductivity (m/s) derived from resistivity, ρ is the electrical resistivity 2 (ohm-m), and $\beta_1 = log_{10}(1e^{-12})$ and $\beta_2 = log_{10}(4)$ are empirical shape factors that are constant 3 within the model domain. The shape factor values reflect conditions where, for example, clay has 4 low electrical resistivity and also low hydraulic conductivity, and sand has high electrical resistivity 5 and high hydraulic conductivity. Eq. (1)(-1) was used to compute the resistivity within each cell of 6 the geological system from the corresponding cell hydraulic conductivity.

7 Using a perfect relationship to generate resistivity from hydraulic conductivity must be 8 characterized as the ideal case because in this case electrical resistivity data can be expected to 9 provide maximal information about hydraulic conductivity. In practive, when possible, estimation 10 of hydraulic conductivity from electrical resistivity is usually based on a site specific noisy linear 11 log-log relationship (see e.g. Mazáč et al. 1985; Revil and Cathles 1999; Purvance and Andricevic 12 2000; Slater 2007), which has been found to be a positive relationship in some cases (Urish 1981; 13 Frohlich and Kelly 1985), and a negative relationship in other cases (Worthington 1975; Heigold et 14 al. 1979; Biella et al. 1983).

15

16 3.3.1 Geophysical data set

17 It is assumed that measurements of the geophysical system are conducted at 77 uniformly 18 distributed locations within the domain (Figure 2Figure 2) using a ground based time domain electromagnetic system (TEM). It is assumed that the TEM system uses a receiver loop centered 19 inside a 40×40 m² square transmitter loop. Measurements are gathered from about 10 20 microseconds to 10 milliseconds using a steady current of 20 Amperes, which gives a magnetic 21 22 moment of 32000 Am² which, for the studied environment, would provide a penetration depth of 23 around 250 meters (Danielsen et al. 2003). For this system the electromagnetic field is propagating 24 down- and outwards like smoke rings increasing with depth at an angle of approximately 30 degrees 25 (West GF and Macnae JC 1991). In other words, the sounding loses resolution with depth because 26 of its increasing footprint. In the following, we use the 1D simulation code AarhusInv (previously 27 called em1Diny; Auken et al. 2014) to simulate the geophysical responses. To mimic the loss of 28 resolution with layer depth we use the logarithmic average resistivity of all model cells inside the 29 radius of the foot print at a given depth. To obtain the geophysical data set, the simulated data were

1 contaminated with noise consisting of: (i) Gaussian 3 % noise contribution and (ii) "background"

2 contribution with a value of $3nV/m^2$ according to the noise model suggested by (Auken et al.

3 2008). The noise-perturbed data were subsequently processed as field data (Auken et al. 2009).

4

5 **3.4** Model construction and parameterization (Step 4)

The groundwater model uses the true boundary conditions except that recharge is to be estimated 6 7 together with hydraulic conductivity. Because the reference groundwater and geophysical systems 8 were generated with correlation between hydraulic conductivity and electrical resistivity, the 9 hydraulic conductivity is parameterized by placing pilot points in each of the 20 layers at the 10 locations where a geophysical sounding has been made. However, pilot points are excluded at 11 depths of the impermeable bedrock. The number of pilot points used for hydraulic conductivity 12 therefore totals 550 (Figure 2Figure 2). Kriging is used for spatial interpolation (here using the 13 correct correlation lengths) from the pilot points to the model grid. This kind of parametrization 14 creates smooth transition in hydraulic conductivity which may seem problematic to use in the 15 current case where there are "categorical" (lithological) shifts in the reference fields. However, 16 because the property contrasts between categories are so large and the geophysical data and the 17 pilot points so many, it is expected that the categorical shifts in property value can be fairly well 18 resolved by the used interpolation.

Recharge is parameterized by assuming a linear log-log relationship between recharge and hydraulic conductivity of the uppermost layer. The two shape factors of the log-log relationship are chosen as parameters to be estimated; they are assumed to be constant within the model domain. The total number of parameters for estimating recharge from hydraulic conductivity is thus two.

23 Electrical resistivity is sensitive to porosity, but that is not incorporated in the relationship within 24 the present work. Therefore porosity cannot be estimated from the hydrological and geophysical 25 data available here, we always use the reference porosity field for making model predictions. A geophysical model is set up for every location of the 77 TEM soundings. Each geophysical model is 26 27 parameterized to have a fixed number of layers equal to one plus the number of groundwater model 28 layers above bedrock; the layers above bedrock all have fixed 10 m thickness while the bedrock is 29 assumed to be of infinite thickness. The estimated parameters of the model are the resistivity within 30 each model layer. The total number of parameters for the 77 geophysical models is thus 627. The 1 model responses were simulated using AarhusInv neglecting lateral heterogeneity. In other words,

2 the inverse model is 1D, following the state of practice (Viezzoli et al. 2010a; Auken et al. 2014)

3

4 **3.5** Model calibration by inversion (step 5)

Calibration of geophysical and groundwater models are conducted independently. However, for our
demonstration problem, we want to explore the amount of "hydraulic" information contained within
the geophysical dataset. We will do this by applying three different calibration methods.

8

9 **3.5.1** Three calibration methods

Method 1 estimates groundwater model parameters on the basis of hydrologic data only (HI). This estimation involves constrained minimization of the misfit between model-simulated responses and the equivalent observation data. This misfit is quantified by the measurement objective function

$$\Phi_m = n_h^{-1} \sum_{i=1}^{n_h} \left(\frac{h_{obs,i} - h_{sim,i}}{\sigma_{h,i}} \right)^2 + n_r^{-1} \sum_{i=1}^{n_r} \left(\frac{r_{obs,i} - r_{sim,i}}{\sigma_{r,i}} \right)^2,$$
(2)

13

where h_{obs} and h_{sim} are observed and corresponding simulated hydraulic heads; r_{obs} and r_{sim} are observed and corresponding simulated river discharge; σ_h and σ_r are the noise levels (standard deviations) for the head and discharge data, respectively; n_h and n_r are the number of head, discharge observations, respectively. However, equation (2)(2) cannot be minimized uniquely because the number of groundwater model parameters (552) is larger than the number of measurements (36). Method 1 therefore relies on minimization of the regularized objective function

$$\Phi_t = \Phi_m + \mu \cdot \Phi_r \tag{3}$$

20

where ϕ_t is the total objective function, ϕ_m is the measurement objective function given by (42), μ is a weight factor, and ϕ_r is a Tikhonov regularization term. Here, ϕ_r is defined as preferred difference regularization, where the preferred difference between neighboring parameter values is set to zero. The regularization weight factor, μ , is iteratively calculated, based on a linearized model approximation, during each optimization iteration making ϕ_m equal to a user specified target value 1 (for details, see Doherty 2010). In this case, for ϕ_m defined by (2), the target value is set to 2 2 (indicating that the fitted data residuals correspond to the data noise levels).

3 Method 2 is joint hydrogeophysical inversion (JHI). For JHI, the hydrological model and the 4 geophysical models are set up separately, but hydrological and geophysical parameters (hydraulic 5 conductivity and electrical resistivity at the pilot points) are estimated simultaneously by 6 minimization of a joint objective function where the regularization term uses an assumed 7 relationship between electrical resistivity and hydrological conductivity.--(Herckenrath et al. 8 <u>2013a</u>). The minimized objective function is of the same form as (3)(3), but the measurement 9 and regularization terms are different. For Method 2 the measurement objective function is defined 10 as

$$\Phi_{m,joint} = n_h^{-1} \sum_{i=1}^{n_h} \left(\frac{h_{obs,i} - h_{sim,i}}{\sigma_{h,i}} \right)^2 + n_r^{-1} \sum_{i=1}^{n_r} \left(\frac{r_{obs,i} - r_{sim,i}}{\sigma_{r,i}} \right)^2$$
(4)
+ $n_{tem}^{-1} \sum_{i=1}^{n_{tem}} \left(\frac{V_{obs,i} - V_{sim,i}}{\sigma_{tem,i}} \right)^2$

11

where n_{TEM} are of TEM observations, respectively. The first two terms on the right hand side of equation (4)(4) are identical to the terms in (2)(2). The values of V_{obs} and V_{sim} are observed and corresponding simulated decay data from TEM. Finally, σ_{tem} is the noise level for the TEM data. Each of the three terms on the right hand side of equation (4)(4) is divided by the number of respective measurements to promote a balanced weight among the three datasets. The regularized objective term for the joint approach is also preferred differences, now defined as

$$\Phi_{r,joint} = \mu \cdot \sum_{i=1}^{n_{kpar}} \left(\log_{10}(K_{joint,i}) - \log_{10}(K_{mf,i}) \right)^2$$
(5)

18

19 In (<u>5</u>)(<u>5</u>), $K_{mf,i}$ is the estimate of the hydraulic conductivity at the ith pilot point of the 20 groundwater model; $K_{joint,i}$ is also an estimate of hydraulic conductivity but inferred from the 21 estimated electrical resistivity at the same depth and location by using equation (<u>1</u>)(<u>1</u>). In this 22 case, the target value of $\phi_{m,joint}$ is set equal to 3.

1 Method 3 is sequential parameter estimation (SHI) modified from by Dam and Christensen (2003). 2 First, the geophysical model parameters (electrical resistivities) are estimated on the basis of the 3 geophysical data. Secondly, the groundwater model parameters are estimated on basis of the 4 hydrologic data as well as the resistivity estimates that are used as regularizing prior information on 5 the hydraulic conductivity. In the first step, the geophysical inversion is done as "smooth model" 6 inversion (Constable et al. 1987). This means that each geophysical model has fixed 10 m layer 7 thicknesses while the resistivity within the layers is estimated. The 77 1D models are inverted 8 independently using AarhusInv (Auken et al. 2014), but vertical constraints were used to stabilize 9 the inversion of each 1D model (Constable et al. 1987). In the second step, the estimated electrical 10 resistivities are used to constrain the subsequent hydrologic inversion, which is carried out as minimization of equation (3) where the measurement objective function ϕ_m is defined by equation 11 12 (2) while the preferred difference regularization term is defined by

$$\Phi_{r,seq} = \mu \cdot \sum_{i=1}^{n_{kpar}} \omega_i \left(\log_{10} (K_{seq,i}) - \log(K_{mf,i}) \right)^2$$
(6)

As in (5)(5), $K_{mf,i}$ is the hydraulic conductivity at the ith pilot point of the groundwater model; 13 $K_{seq,i}$ is the hydraulic conductivity at the pilot point calculated from the corresponding resistivity, 14 15 estimated in the first step of Method 3, by using equation (1)(1). In (6), ω_i is a weight that can be 16 varied between the terms of the summation in (6). The results presented in the following were obtained by using a weight of 1.0 for all preferred differences. (We also tried using weights 17 determined as $\omega_i = (\beta_2 V(\rho_i))^{-1}$ where $V(\rho_i)$ is the variance of the log-resistivity estimate used to 18 compute $\log_{10}(K_{seq,i})$. Changing the weights did not change the estimation results much; some 19 prediction errors did reduce, others increased, but we found no general improvement by using 20 $\omega_i = (\beta_2 V(\rho_i))^{-1}$ instead of the simple choice $\omega_i = 1$.) Choice of weights can be important in 21 other cases, for example that of -Beaujean et al. (2014). For method 3, the target value of ϕ_m is set 22 23 equal to 2.

For all three methods, the objective function is minimized iteratively by the modified Gauss-Newton method. This involves recalculation of the sensitivity matrix for each iteration, which is time consuming due to the large number of model parameters.

1 3.5.2 Initial parameter values

We did the following to investigate how much the choice of initial parameter values influences the
parameter estimates obtained by the three inversion approaches.

For method 1 (HI), we ran two inversions. In the first run, termed HI-T, we used the reference (true) hydraulic conductivity values at each pilot point as initial values. We acknowledge that this is not a realistic occurrence but it is done as a control to show the supposedly best possible outcome of HI. In the second run, termed HI-H, we assumed a homogeneous initial hydraulic conductivity field with K equal to 1×10^{-6} m/s which is equal to the true mean value of silt.

9 For method 2 (JHI), we ran three inversions. In the first run, termed JHI-T, we used the reference 10 (true) parameter values for hydraulic conductivity and electrical resistivity at the pilot points. As 11 above this is done to show the supposedly best possible outcome of JHI. In the second run, termed 12 JHI-H, we used a constant hydraulic conductivity of 1×10^{-6} m/s and a constant electrical resistivity of 40 ohm-m at the pilot points. In the third run, termed JHI-G, we first ran independent 13 14 geophysical inversions (one for each sounding location) using a homogeneous half space of 40 ohm 15 meter as the starting model. The resulting estimates of electrical resistivity were subsequently used 16 as initial parameter values for JHI-G at the resistivity pilot points, and they were used together with relation (1) to produce the JHI-G initial values of hydraulic conductivity at the hydraulic 17 18 conductivity pilot points.

19 For method 3 (SHI), we present results from only one inversion sequence, termed SHI-G. First we 20 ran the independent geophysical inversions using a homogeneous half space of 40 ohm meter as the 21 initial model. Subsequently we used the estimated resistivities together with relation (1) to produce 22 the initial values for hydraulic conductivity at the pilot points that were used for the hydrologic 23 inversion carried out in step two of SHI-G. (As for JHI, we also tried using an initially homogeneous hydraulic conductivity field for SHI; this gave a more blurred estimated hydraulic 24 conductivity field than what is presented later. So, like it is shown later for JHI, the result of SHI 25 26 was found to depend on the choice of initial parameter values.)

27

28 3.5.3 Inversion software

The objective functions were minimized using BeoPEST, a version of PEST (Doherty 2010) that allows the inversion to run in parallel using multiple cores and computers. We used a new version of BeoPEST modified by John Doherty particularly for our purpose to do gradient based minimization involving several models with each of their parameters; thus the modified BeoPEST exploits that different parts of the sensitivity matrix can be calculated by running just one of the models. However, for method 3, the geophysical data were inverted using AarhusInv (Auken et al., 2014).

6

7 3.6 Picking 10 realizations

For this demonstration, the computational burden would be overwhelming if the entire HYTEB
analysis was to be carried out for each of the 1000 system realizations. We therefore sought a way
to reduce the number of models to just 10 that would maintain a representative diversity of models.
The strategy we used to down sample from 1000 realizations to 10 was as follows.

We first decided to group the models based on the predictions of interest. It would be reasonable to 12 13 group models based on other characteristics, such as underlying conceptual model, or zonation, or 14 imposed boundary conditions. However, we contend that for both practical and scientific 15 applications, it is more often the predictions of models that are of primary interest than the structure 16 or parameterization of the models. We began by creating an ensemble from the 25 predictions of interest listed in Table 3Table 3 over all 1000 realizations. We then used k-means clustering to 17 18 group the prediction sets into 10 clusters within this prediction space. Because the units of the 19 predictions varied, all predictions were whitened, or normalized, before clustering. For stability, we 20 ran 1000 repetitions of the clustering to minimize the effects of initial cluster selection. Once the clusters were defined, we identified the prediction set that was closest to the centroids. This resulted 21 22 in ten models that broadly represent the range of model behaviors, including both the range of each 23 prediction and the correlations among predictions.

1 4 Results

2 4.1 Model Calibration

3 Figure 4Figure 4 shows the measurement objective function value, Φ_m , obtained for the various groundwater model calibration cases and for the 10 different system realizations. It also shows the 4 5 separate terms of the objective function. We aimed at using weights that would make each term 6 contribute by a value of approximately 1.0. For HI and SHI there are two terms, quantifying fit to 7 head data and fit to the flux measurement, respectively; the results in Figure 4 show that the head 8 data are fitted as intended while the flux measurement is fitted more closely than intended. This 9 fitting picture is also seen for JHI. JHI tends to produce better fit to the hydrologic data than HI and SHI. 10

11 For JHI the objective function (4)(4) has a third term quantifying fit to decay data of the TEM 12 measurements. Figure 4 indicates that the actually used weighting for JHI ended by producing 13 slightly better fit to the hydrologic data than to the TEM data. It also shows that for JHI the fit to the 14 hydrologic data is not strongly dependent on the choice of initial parameter values; JHI-T for 15 example did not always produce better fits than JHI-G or JHI-H. That JHI-T, JHI-G, and JHI-H lead to different fits (and different parameter estimates) shows that the JHI minimization problem is non-16 uniquemay not be unique. However, we did not investigate if PEST parameters could have been set 17 18 differently to thereby make the JHI minimization unique.

For two realizations HI-T produced much worse fit to the hydrologic data than HI-H (Figure <u>4Figure 4</u>): the HI-T minimization got stuck at a local minimum where a parameter adjustment improving the fit to head deteriorated the fit to the flux measurement. We did not investigate if PEST parameters could have been set differently to overcome this problem.

23

24 4.2 Estimated hydraulic conductivity fields

Figure 5 Figure 5 shows the reference hydraulic conductivity fields of the uppermost six layers and a representative cross section for one of the 10 chosen system realizations. It also shows the corresponding estimated hydraulic conductivity fields obtained by six different inversion runs. The figure can thus be used to visually compare the estimated hydraulic conductivity fields and to judge whether they resolve the structures of the reference system. Figure 6 Figure 6 shows corresponding 1 pilot-point-by-pilot-point scatter plots of reference versus estimated hydraulic conductivity. Except

when noted specifically, the results in Figure 5Figure 5 and Figure 6Figure 6 for this realization are 2 typical for all 10 chosen system realizations.

3

4 The second and third rows of Figure 5 Figure 5 show results for the two hydrologic inversion (HI) 5 runs. Inversion HI-T, which used true (reference) parameter values as initial values, produces very blurred hydraulic conductivity fields. This is caused by the used Tikhonov regularization constraint 6 7 which guides the inversion to estimate a field as smooth as possible while still fitting the calibration 8 data. The estimated field for layer one has some structural similarity with the reference field but the 9 estimated values vary much less than the reference values. Similar results are seen for layers 2 to 5 10 while structure has disappeared from the deeper layers representing the deposits in the buried 11 valley. Similar results were achieved for three other realizations. For the remaining six realizations HI-T produced very blurred hydraulic conductivity fields for all model layers, having essentially no 12 13 resemblance to the structure of the reference fields. The third row of Figure 5 Figure 5 illustrates 14 that for inversion HI-H, which used homogeneous initial hydraulic conductivity fields, there is 15 almost no structural similarity between the estimated and reference hydraulic conductivity fields, 16 and for most layers the estimated field appears to be almost homogeneous. However, the cross 17 sections show that the structure with high hydraulic conductivity in the bottom of the burried valley is resolved to some degree by both HI-T and HI-H. Figure 6Figure 6 shows that both HI-T and HI-18 19 H underestimate hydraulic conductivities for high-permeability deposits (sand and gravel) but overestimate for low-permeability deposits (silt and clay). For HI-H, the range of estimated 20 conductivities is the same for high-permeability and low-permeability deposits. For HI-T, there is a 21 small difference between the two ranges - they are slightly shifted in the correct directions 22 23 compared to HI-H.

24 The fourth row of Figure 5 Figure 5 shows hydraulic conductivity fields estimated by the sequential 25 geophysical approach (SHI-G). For the upper layers, the true (reference) structures can be recognized, but the resolution decreases with depth. The cross section shows that the true structures 26 of the upper five layers can be identified to some degree from the estimated fields. Because of loss 27 28 of resolution, the structures cannot be identified inside the buried valley. Figure 6Figure 6 shows 29 that for low-permeability deposits, the range of estimated log-hydraulic conductivities is twice as 30 large as the reference range of values, and the horizontal scatter around the identity line is 31 considerable. For high-permeability deposits, the range of estimated values is much larger than the

1 range of reference values, and the estimated values tend to be orders of magnitude too small (Figure <u>oFigure 6</u>). This happens because the resistivities estimated from the TEM data in the first step of 2 3 the SHI scheme often turn out to be too small if the resistivity at depth is high. This is a well-known 4 result from the fact that the sensitivity of TEM data with respect to layers of high resistivity reduces 5 with depth, which causes problems of equivalence for the geophysical models. (This has been 6 demonstrated and discussed by Auken et al. 2008 for a similar type of geological system.) When 7 resistivity estimates that are too small are used to regularize the second hydrologic inversion step of 8 the SHI scheme, the hydraulic conductivity estimates are likely to be too small as well. Similarly, 9 hydraulic conductivity estimates are too high in some high-resistivity parts of the shallow layers 10 (Figure 6Figure 6) because the resistivity estimated from TEM tends to be too high due to low sensitivity of the TEM data. For the studied system, this shows that resistivities estimated by 11 12 independent TEM data inversion must be used with caution as estimators of hydraulic conductivity 13 or as regularization means for subsequent hydrological inversion. In this case, the absolute 14 relationship between hydraulic conductivity and reference electrical resistivity led to an over-15 reliance on the use of inferred resistivities to populate the model's hydraulic conductivity field.

The last three rows of Figure 5Figure 5 show hydraulic conductivity fields estimated by the three 16 17 joint hydrogeophysical inversion runs (JHI-T, JHI-H and JHI-G), respectively. JHI-T, which used true (reference) parameter values as initial values, resolves the true structures of the upper five 18 19 layers well while the estimated field of layer six is blurred; the cross section shows that the true structures within the buried valley are also resolved to some degree. Figure 6Figure 6 shows that 20 21 estimated versus reference hydraulic conductivity values plot nicely along the identity line for JHI-22 T. The resolution of structures (Figure 5Figure 5) and the quality of the K estimates (Figure 6Figure 6) 23 6) deteriorate for JHI-H and JHI-G, both of which use less informative initial parameter values. 24 Figure 5Figure 5 visually indicates that JHI-G resolves structures better than JHI-H. For sand and gravel deposits Figure 6 shows wider horizontal scatter for JHI G than for JHI H. Figure 6 25 It also shows that estimated hydraulic conductivity for sand and gravel tends to be much too small 26 27 for both JHI-G and JHI-H (the explanation of which is similar to that given for SHI above), and that 28 particularly JHI-H cannot resolve variations in hydraulic conductivity within the buried valley: the 29 estimated values vary only within roughly an order of magnitude whereas the reference values vary 30 within five orders of magnitude.

1 4.3 Prediction results

2 For each of the ten chosen geological realizations, each of the six calibrated groundwater models 3 were used to make the model predictions described in section 3.2.2. Figure 7Figure 7 shows five 4 examples of scatter plots of reference predictions versus calibrated model predictions; each plot 5 shows ten points, each of which corresponds to a particular geological realization selected by the 6 clustering. Each plot also gives the mean error of the prediction (ME) calculated from the ten model 7 predictions. The five predictions represented in Figure 7 Figure 7 are head in the capping layer at 8 location 1, head recovery at location 1, head recovery within the deeper-deepest part of the buried 9 valley at location 8 near the pumping well (Figure 2Figure 2), groundwater discharge to the river 10 after pumping has stopped, and recharge area of the pumping well.

Figure 8Figure 8 shows the mean absolute relative error (MARE) for the 25 model predictions made by models calibrated with six inversion approaches. The relative error magnitudes are calculated as the absolute value of the difference between the reference and model predicted value for each prediction of interest averaged over the ten geological realizations considered. The prediction results are discussed individually below.

16 4.3.1 Head prediction

17 All calibrated groundwater models appear to be fairly good predictors of hydraulic head. Nearly 18 unbiased head prediction is exemplified by the plots in the first column of Figure 7Figure 7 for 19 which the points scatter around the identity line. This indicates that all calibrated models make 20 unbiased prediction of hydraulic head at location 1. However, the scatter around the identity line 21 appears to be larger for HI calibrated models than for JHI calibrated models. This indicates that the 22 use of geophysical data in JHI reduces the uncertainty of this head prediction as compared to the HI 23 calibrated models. The scatter plots for the other head predictions are similar to those shown for location 1. 24

Figure 8 Figure 8 shows that for all head predictions except at location 2, the use of geophysical data with SHI-G, JHI-H and JHI-G reduces the prediction error when compared to the HI based predictions. It also shows that the relative error magnitude is smaller for head predictions than for most other prediction types. Only change of discharge prediction has a relative error magnitude comparable to the head predictions. The small relative head prediction errors are likely due to the fact that this type of prediction is similar to the head data used for model calibration. Only the location differs between prediction and calibration heads.

1 4.3.2 Head recovery prediction

2 Head recovery due to cessation of pumping is a type of prediction that turns out to be biased for all 3 calibrated models. This is exemplified by the results shown in the second and third columns of 4 Figure 7Figure 7. The two plots in the top of the second column indicate that head recovery at location 1 tends to be underpredicted by the models calibrated by purely hydrologic inversion (HI-T 5 and HI-H). The third plot in this column indicates that SHI-G slightly reduces the bias seen in the 6 7 HI-based model. Finally, the last three plots in the second column of Figure 7 Figure 7 show that all 8 the models calibrated by JHI appear to be better predictors for this head recovery than the HI and 9 SHI-G based models. The quality of this model prediction appears to be unaffected by the choice of 10 initial parameter values used for JHI. However, for JHI the points tend to scatter around a line with an intercept less than zero and a slope larger than unity. The former indicates consistent bias in the 11 12 prediction probably due to consistent errors in null space parameter components omitted from the 13 parameterized groundwater model; the latter probably indicates parameter surrogacy incurred 14 through model calibration (see section 2.7). The appearances of scatter plots for head recovery at locations 2 to 7 are similar to that for recovery at location 1 (Figure 7Figure 7). 15

The second plot in the third column of Figure 7 Figure 7 indicate that head recovery at location 8 16 17 within the deeper part of the buried valley is predicted fairly well for nine out of ten geological realizations when the model is calibrated by hydrologic inversion (HI-H); however, the nine points 18 19 tend to fall slightly below the identity line while the tenth point falls far above the identity line. Generally, the plots indicate a consistent underprediction of head using HI-based inversion. The 20 21 remaining plots in the third column show that recovery prediction at location 8 turns out to be too large for the models calibrated with geophysical data (JHI) or by using geophysics based 22 23 regularization (SHI).

Figure 8 Figure 8 shows that for recovery predictions 1 to 7, the use of geophysical data with SHI-G, 24 25 JHI-H and JHI-G reduces the prediction error when compared to the HI based predictions. For recovery 1, this is confirmed by the scatterplots in column two of Figure 7. On the contrary, 26 for recovery prediction 8, located within the buried valley, both Figure 7Figure 7 and Figure 27 28 8Figure 8 show that including the geophysics in the groundwater modelling with either SHI-G, JHI-29 H or JHI-G tends to increase the prediction error as compared to HI-H and HI-T. Depending on the choice of initial parameter values, a similar result is seen for recovery predictions 9 and 10. 30 31 (Explanation for this predictive degradation is given above, in the end of the first paragraph of this

1 subsection.) It is finally noted that recovery prediction 2 benefits from use of geophysical data while

head prediction at the same location does not, and that the relative error magnitude is larger for
recovery predictions than for head predictions. This is likely because head recovery depends on a
different stress situation than that represented by the head calibration data.

5 4.3.3 Discharge prediction

6 The scatter plots in the fourth column of <u>Figure 7</u>Figure 7 indicate that discharge to the river 7 without pumping is overpredicted except for the HI-T and JHI-T based models. Further, this is a 8 type of model prediction that is not improved by including geophysical data by the SHI or JHI 9 inversions used here (compare for example the HI-H plot with the JHI-G plot). This is confirmed 10 by the relative error magnitudes for discharge shown in <u>Figure 8Figure 8</u>.

11 4.3.4 Recharge area and other particle tracking predictions

12 The plots in the fifth column of Figure 7Figure 7 are for the recharge area prediction. Except for 13 JHI-T and JHI-G, the points in all plots appear to fall along an almost vertical line; the scatter along 14 the vertical axis is much longer than the scatter along the horizontal axis, indicating that all of these 15 models are a poor, highly biased predictor of the pumping well's recharge area. Including TEM data in the model calibration only improves this model prediction for JHI-T and JHI-G. Further analysis 16 17 shows that at least part of the reason for the poor prediction is that the estimated areal average 18 recharge for the model domain in all cases is too low. Lower estimated recharge rates requires a 19 larger predicted recharge area to balance the rate of water pumped from the pumping well. For the 20 JHI-T models, the estimated areal recharge amounts to about two thirds of the actual average 21 recharge. For the JHI-H models the estimated recharge tends to be less than half (for one model 22 realization as low as one third) of the actual area. The estimated areal recharge for the other models is between the JHI-T and JHI-H estimates. It should be mentioned that all calibrated models 23 24 sufficiently fit the river discharge measurement; the underestimated recharge means that the 25 simulated discharge to the lake turns out to be too small (typically less than half of the actual discharge to the lake; for one calibrated model there is almost no simulated lake discharge). 26

It is finally mentioned that the scatter plots look similar to those in column 6-5 of Figure 7 Figure 7 for the prediction of average age of groundwater pumped from the well and for the prediction of particle travel time. The explanation for these poor predictive performances must be because the calibrated hydraulic conductivity field is too smooth (and the hydraulic connectivity therefore exaggerated) in the calibrated models. Figure 8Figure 8 show that use of TEM data does not improve the model performance with respect to prediction of groundwater age and particle travel
 time.

3 **5** Discussion and conclusions

4 It is intuitively clear that geophysics can offer valuable information for improved groundwater 5 modeling, but for an actual investigation it is often unclear how, at what cost, and to what extent 6 modeling can be improved by adding geophysical data. This paper presents a newly developed 7 platform that allows for such an application- and method-specific examination of the potential value 8 of using geophysical data and models to develop a groundwater model and improve its predictive 9 power. We call the platform HYdrogeophysical TEst-Bench (HYTEB). HYTEB allows for 10 treatment of hydrologic and geophysical data and inversion approaches. It can be used to examine 11 the combined use of hydrologic and geophysical data, including model parameterization, inversion, 12 and the use of multiple geophysical or other data types. It can also be used to discover potential 13 errors that can be introduced through petrophysical models used to correlate geophysical and 14 hydrologic parameters. We use HYTEB to work with rather complex, fairly realistic but synthetic 15 systems. In this work we strive at (and recommend) balancing complexity with the advantage of 16 knowing the 'true' system or condition to assess model/data performance, and at avoiding to 17 overextend the likely value of data or models beyond the tested conditions.

18 Our recommended way of using HYTEB is demonstrated by synthesizing a hydrogeological 19 environment that is typical to parts of northern Europe and northern America, consisting of various 20 types of glacial deposits covering low-permeability (in practice impermeable) bedrock of Tertiary 21 clay, which has a surface with the form of a plateau with a deep valley buried by the glacial 22 deposits. HYTEB is used to investigate to what extent groundwater model calibration and, often 23 more importantly, model predictions can be improved for this kind of setting by including in the 24 calibration process electrical resistivity estimates obtained from TEM data in two different ways: by 25 using either sequential hydrogeophysical inversion (SHI) or joint hydrogeophysical inversion (JHI). 26 For simplicity we assumed that the resistivity correlates with hydraulic conductivity and that the 27 relationship is constant and known. The results are compared to those obtained by a groundwater 28 model calibrated by purely hydrologic inversion (HI).

The calibrated groundwater models are parameterized by many pilot points that should allow a reasonable resolution of the hydraulic and geophysical property fields at depths where the properties are resolved by the data. Using PEST (Doherty, 2010), Tikhonov or geophysical
 regularization is used to stabilize the HI, SHI, and JHI inversion problems. In this case, JHI tends to
 produce the best fit to the data while SHI and HI produce comparable fits.

4 For HI, the estimated hydraulic conductivity field turns out to be very smooth in the top layers and 5 almost homogeneous in the deeper layers, which is expected for this type of (Tikhonov) 6 regularization. For SHI and JHI, the estimated hydraulic conductivity field resolves much of the 7 true structures in the shallow layers while less or, in the deeper part, no structure is resolved inside 8 the buried valley. However, the estimated hydraulic conductivities are orders of magnitude wrong 9 in some parts of the model. This occurs because the resistivities estimated for the geophysical 10 models either in the first step of the SHI scheme or during the JHI scheme can turn out to be very 11 erroneous when the sensitivity of the TEM data with respect to resistivity is low. Such uncertain, 12 potentially very erroneous, resistivity estimates should be discarded (or filtered out) from the SHI or 13 JHI. By not doing this, we showed that resistivities estimated by SHI or JHI must be used with 14 caution as estimators of hydraulic conductivity or as regularization means for subsequent 15 hydrological inversion; the use of the absolute relationship between hydraulic conductivity and electrical resistivity led to an over-reliance on the use of inferred resistivities to populate the 16 17 model's hydraulic conductivity field.

With respect to reducing model prediction error, it depends on the type of prediction whether it has value to include geophysics in the model calibration. It was found that all models are good predictors of hydraulic head. However, head prediction errors tend to be reduced for models calibrated by SHI or JHI as compared to models calibrated by HI.

22 When the stress situation is changed from that of the hydrologic calibration data, then all models 23 make biased predictions of head change. Use of geophysical data or models (with JHI or SHI) 24 reduces error and bias of head prediction at shallow depth but not in the deep part of the buried 25 valley near the pumping well (where the stress field change the most). Analyzing the prediction results by the method described by Doherty and Christensen (2011) indicates that geophysics helps 26 27 to reduce parameter null space as well as parameter surrogacy for parameters determining the 28 shallow part of the hydraulic conductivity field. In hindsight, this is obvious since the TEM method 29 better resolves the shallow variations in glacial deposits' resistivity than the variations inside the 30 deep buried valley.

For model prediction of change of discharge to the stream, there is no improvement in using
 geophysics. HI based prediction results are comparable to SHI and JHI based results.

3 All models are a very poor predictor of the pumping well's recharge area and groundwater age. The 4 reason for this is that distributed recharge is here estimated during the model calibration together 5 with distributed hydraulic conductivity. Recharge is parameterized by assuming a linear log-log 6 relationship between recharge and hydraulic conductivity of the upper model layer; two shape 7 factors of the relationship are treated as parameters that are calibrated together with the pilot point 8 parameters for hydraulic conductivity and (for JHI) resistivity. It was assumed that the shape factors 9 could be estimated because stream discharge data were included in the calibration data set. All 10 models fit these data, but the estimated areal recharge turned out to be two thirds or less of the 11 actual areal recharge. The predicted recharge area of the pumping well and the predicted age of the 12 pumped water therefore turn out to be much too large. So another important insight from this study 13 is that recharge should be parameterized and estimated in a different way than it was done in the 14 demonstration example. Alternatively HYTEB could be used to consider adding other types of data 15 to better constrain recharge rates.

16

17 Acknowledgements

18 The presented work was supported by HyGEM, Integrating geophysics, geology, and hydrology for improved groundwater environmental management, Project no. 11- 15 116763. The funding for 19 20 HyGEM is provided by The Danish Council for Strategic Research. John Doherty is thanked for making modifications of BeoPEST. Finally, we thanks Troels N. Vilhelmsen, Esben Auken, and 21 22 Anders V. Christiansen for their participation in discussions and sharing of experiences during the initial phase of the project. HYTEB is available for download on https://github.com/Nikolaj-23 24 KC/HYTEB. With HYTEB can also be downloaded Python scripts demonstrating how to set up HI, 25 SHI and JHI as it is done in the manuscript.

Field Code Changed

1 6 References

- Abraham JD, Cannia JC, Bedrosian PA, Johnson MR, Ball LB, Sibray SS (2012) : Airborne Electromagnetic Mapping of the Base of Aquifer in Areas of Western Nebraska. In: U.S. Geol.
 Surv. Sci. Investig. Rep. 2011–5219. http://pubs.usgs.gov/sir/2011/5219/. Accessed 4 Jan 2016
- Archie GE (1942) : The Electrical Resistivity Log as an Aid in Determining Some Reservoir
 Characteristics. Trans AIME 146:54–62. doi: 10.2118/942054-G
- Auken E, Christiansen AV, H.Westergaard J, Kirkegaard C, Foged N, Viezzoli A (2009) : An
 integrated processing scheme for high-resolution airborne electromagnetic surveys, the
 SkyTEM system. Explor Geophys 40(2):184–192. doi: http://dx.doi.org/10.1071/EG08128
- Auken E, Christiansen AV, Kirkegaard C, Fiandaca G, Schamper C, Behroozmand AA, Binley A,
 Nielsen E, Effersø F, Christensen NB, Sørensen K, Foged N, Vignoli G (2014) : An overview
 of a highly versatile forward and stable inverse algorithm for airborne, ground-based and
 borehole electromagnetic and electric data. Explor Geophys 46(3):223–235. doi:
 10.1071/EG13097
- Auken E, Christiansen A V., Jacobsen LH, Sørensen KI (2008) : A resolution study of buried
 valleys using laterally constrained inversion of TEM data. J Appl Geophys 65:10–20.
- Auken E, Jørgensen F, Sørensen KI (2003) : Large-scale TEM investigation for groundwater.
 Explor Geophys 34(3):188–194. doi: 10.1071/EG03188
- Beaujean J, Nguyen F, Kemna A, Antonsson A, Engesgaard P (2014) : Calibration of seawater
 intrusion models: Inverse parameter estimation using surface electrical resistivity tomography
 and borehole data. Water Resour Res 50:6828–6849. doi: 10.1002/2013WR014020
- Biella G, Lozej A, Tabacco I (1983) : Experimental Study of Some Hydrogeophysical Properties of
 Unconsolidated Porous Media. Ground Water 21:741–751. doi: 10.1111/j.1745 6584.1983.tb01945.x
- 25 Carle SF (1999) T-PROGS: Transition Probability Geostatistical Software. Users Manual.
- Certes C, De Marsily G (1991) : Application of the pilot point method to the identification of aquifer transmissivities. Adv Water Resour 14:284–300. doi: 10.1016/0309-1708(91)90040-U
- Clayton L, Attig JW, Mickelson DM (1999) Tunnel channels formed in Wisconsin during the last
 glaciation. Geological Society of America
- Constable SC, Parker RL, Constable CG (1987) : Occam's inversion: A practical algorithm for
 generating smooth models from electromagnetic sounding data. GEOPHYSICS 52:289–300.
 doi: 10.1190/1.1442303
- Cooley RL (2004) : A theory for modeling ground-water flow in heterogeneous media. In: US
 Geological Survey Professional Paper 1679, 220 pp. US Geological Survey Report,
- Cooley RL, Christensen S (2006) : Bias and uncertainty in regression-calibrated models of
 groundwater flow in heterogeneous media. Adv Water Resour 29:639–656. doi:
 10.1016/j.advwatres.2005.07.012
- Dam D, Christensen S (2003) : Including Geophysical Data in Ground Water Model Inverse
 Calibration. Ground Water 41:178–189. doi: 10.1111/j.1745-6584.2003.tb02581.x
- 40 Danielsen JE, Auken E, Jørgensen F, Søndergaard V, Sørensen KI (2003) : The application of the

Formatted: English (U.S.)

- transient electromagnetic method in hydrogeophysical surveys. J Appl Geophys 53:181–198.
 doi: 10.1016/j.jappgeo.2003.08.004
- Day-Lewis FD (2005) : Applying petrophysical models to radar travel time and electrical resistivity
 tomograms: Resolution-dependent limitations. J Geophys Res 110:B08206. doi:
 10.1029/2004JB003569
- Deutsch C V. (2006) : A sequential indicator simulation program for categorical variables with
 point and block data: BlockSIS. Comput Geosci 32:1669–1681. doi:
 10.1016/j.cageo.2006.03.005
- 9 Deutsch C V., Journel AG (1998) GSLIB: Geostatistical Software Library and User's Guide:
 10 Clayton V. Oxford University Press, Second Edi. Oxford University Press
- Di Maio R, Fabbrocino S, Forte G, Piegari E (2013) : A three-dimensional hydrogeological–
 geophysical model of a multi-layered aquifer in the coastal alluvial plain of Sarno River
 (southern Italy). Hydrogeol J 22:691–703. doi: 10.1007/s10040-013-1087-8
- Doherty J (2010) PEST, Model-Independent Parameter Estimation, User Manual, 5th ed, 336 pp.,.
 Watermark Numerical Computing
- Doherty J (2003) : Ground Water Model Calibration Using Pilot Points and Regularization. Ground
 Water 41:170–177. doi: 10.1111/j.1745-6584.2003.tb02580.x
- Doherty J, Christensen S (2011) : Use of paired simple and complex models to reduce predictive
 bias and quantify uncertainty. Water Resour Res 47(12):W12534. doi:
 10.1029/2011WR010763
- Doherty J, Welter D (2010) : A short exploration of structural noise. Water Resour Res 46
 (5):W05525. doi: 10.1029/2009WR008377
- Feyen L, Gómez-Hernández JJ, Ribeiro PJ, Beven KJ, De Smedt F (2003) : A Bayesian approach to
 stochastic capture zone delineation incorporating tracer arrival times, conductivity
 measurements, and hydraulic head observations. Water Resour Res 39 (5):1126. doi:
 10.1029/2002WR001544
- Feyen L, Gorelick SM (2005) : Framework to evaluate the worth of hydraulic conductivity data for
 optimal groundwater resources management in ecologically sensitive areas. Water Resour Res
 41 (3):W3019. doi: 10.1029/2003WR002901
- Fitterman DV, Deszcz-Pan M (1998) : Helicopter EM mapping of saltwater intrusion in Everglades
 National Park, Florida. Explor Geophys 29:240–243. doi: 10.1071/EG998240
- Foged N, Marker PA, Christansen A V., Bauer-Gottwein P, Jørgensen F, Høyer A-S, Auken E
 (2014a) : Large scale 3-D modeling by integration of resistivity models and borehole data
 through inversion. Hydrol Earth Syst Sci Discuss 11:1461–1492. doi: 10.5194/hessd-11-14612014
- Foged N, Marker PA, Christansen A V., Bauer-Gottwein P, Jørgensen F, Høyer A-S, Auken E
 (2014b) : Large-scale 3-D modeling by integration of resistivity models and borehole data
 through inversion. Hydrol Earth Syst Sci 18:4349–4362. doi: 10.5194/hess-18-4349-2014
- Franssen H-JH, Gómez-Hernández J, Sahuquillo A (2003) : Coupled inverse modelling of
 groundwater flow and mass transport and the worth of concentration data. J Hydrol 281:281–
 295. doi: 10.1016/S0022-1694(03)00191-4

- Freeze RA, Massmann J, Smith L, Sperling T, James B (1990) : Hydrogeological Decision
 Analysis: 1. A Framework. Ground Water 28:738–766. doi: 10.1111/j.1745-6584.1990.tb01989.x
- Frohlich RK, Kelly WE (1985) : The relation between hydraulic transmissivity and transverse
 resistance in a complicated aquifer of glacial outwash deposits. J Hydrol 79:215–229. doi:
 10.1016/0022-1694(85)90056-3
- Harbaugh AW, Banta ER, Hill MC, McDonald MG (2000) MODFLOW-2000, The U.S. Geological
 Survey modular ground-water model: User guide to modularization concepts and the ground water flow process. U.S. Geological Survey Open-File Report 00-92, 121 p.
- Harvey CF, Gorelick SM (1995) : Mapping Hydraulic Conductivity: Sequential Conditioning with
 Measurements of Solute Arrival Time, Hydraulic Head, and Local Conductivity. Water Resour
 Res 31:1615–1626. doi: 10.1029/95WR00547
- He X, Højberg AL, Jørgensen F, Refsgaard JC (2015) : Assessing hydrological model predictive
 uncertainty using stochastically generated geological models. Hydrol Process 29:n/a–n/a. doi:
 10.1002/hyp.10488
- He X, Koch J, Sonnenborg TO, Jørgensen F, Schamper C, Christian Refsgaard J (2014) : Transition
 probability-based stochastic geological modeling using airborne geophysical data and borehole
 data. Water Resour Res 50:3147–3169. doi: 10.1002/2013WR014593
- Heigold PC, Gilkeson RH, Cartwright K, Reed PC (1979) : Aquifer Transmissivity from Surficial
 Electrical Methods. Ground Water 17:338–345. doi: 10.1111/j.1745-6584.1979.tb03326.x
- Herckenrath D, Fiandaca G, Auken E, Bauer-Gottwein P (2013a) : Sequential and joint
 hydrogeophysical inversion using a field-scale groundwater model with ERT and TDEM data.
 Hydrol Earth Syst Sci 17:4043–4060. doi: 10.5194/hess-17-4043-2013
- Herckenrath D, Odlum N, Nenna V, Knight R, Auken E, Bauer-Gottwein P (2013b) : Calibrating a
 salt water intrusion model with time-domain electromagnetic data. Ground Water 51 (3):385–
 397. doi: 10.1111/j.1745-6584.2012.00974.x
- Hermans T, Nguyen F, Caers J (2015) : Uncertainty in training image-based inversion of hydraulic
 head data constrained to ERT data: Workflow and case study. Water Resour Res 51:5332–
 5352. doi: 10.1002/2014WR016460
- Hill M (1998) : Methods and guidelines for effective model calibration; with application to
 UCODE, a computer code for universal inverse modeling, and MODFLOWP, a computer code
 for inverse modeling with MODFLOW. Water-Resources Investig Rep 98–4005. doi:
 10.1061/40517(2000)18
- Hinnell a. C, Ferré TP a., Vrugt J a., Huisman J a., Moysey S, Rings J, Kowalsky MB (2010) :
 Improved extraction of hydrologic information from geophysical data through coupled
 hydrogeophysical inversion. Water Resour Res 46:W00D40. doi: 10.1029/2008WR007060
- Hubbard SS, Rubin Y (2000) : Hydrogeological parameter estimation using geophysical data: a
 review of selected techniques. J Contam Hydrol 45:3–34. doi: 10.1016/S0169-7722(00)00117 0
- Hubbard SS, Rubin Y, Majer E (1999) : Spatial correlation structure estimation using geophysical
 and hydrogeological data. Water Resour Res 35:1809–1825. doi: 10.1029/1999WR900040

- Hyndman D., Tronicke J (2005) : Hydrogeophysical case studies at the local scale: the saturated
 zone. In: Rubin Y, Hubbard SS (eds) Hydrogeophysics. Springer Netherlands, Dordrecht, pp
 391–412
- Hyndman DW, Harris JM, Gorelick SM (1994) : Coupled seismic and tracer test inversion for
 aquifer property characterization. Water Resour Res 30:1965–1977. doi: 10.1029/94WR00950
- Jørgensen F, Sandersen PBE (2006) : Buried and open tunnel valleys in Denmark—erosion beneath
 multiple ice sheets. Quat Sci Rev 25:1339–1363.
- Jørgensen F, Sandersen PBE, Auken E (2003) : Imaging buried Quaternary valleys using the
 transient electromagnetic method. J Appl Geophys 53:199–213. doi:
 10.1016/j.jappgeo.2003.08.016
- Koch K, Wenninger J, Uhlenbrook S, Bonell M (2009) : Joint interpretation of hydrological and
 geophysical data: electrical resistivity tomography results from a process hydrological research
 site in the Black Forest Mountains, Germany. Hydrol Process 23:1501–1513. doi:
 10.1002/hyp.7275
- Kowalsky MB, Finsterle S, Peterson J, Hubbard S, Rubin Y, Majer E, Ward A, Gee G (2005) :
 Estimation of field-scale soil hydraulic and dielectric parameters through joint inversion of
 GPR and hydrological data. Water Resour Res 41 (11):W11425. doi: 10.1029/2005WR004237
- Lawrie KC, Carey H, Christensen NB, Clarke J, Lewis S, Ivkovic KM, Marshall SK (2012) :
 Evaluating the Role of Airborne Electromagnetics in Mapping Seawater Intrusion and
 Carbonate-Karstic Groundwater Systems in Australia. Geoscience Australia, Canberra,
 http://dx.doi.org/10.11636/Record.2012.042
- Linde N, Finsterle S, Hubbard S (2006) : Inversion of tracer test data using tomographic constraints.
 Water Resour Res 42:n/a–n/a. doi: 10.1029/2004WR003806
- Marker PA, Foged N, He X, Christiansen A V., Refsgaard JC, Auken E, Bauer-Gottwein P (2015) :
 Performance evaluation of groundwater model hydrostratigraphy from airborne
 electromagnetic data and lithological borehole logs. Hydrol Earth Syst Sci 19:3875–3890. doi:
 10.5194/hess-19-3875-2015
- Mazáč O, Kelly WE, Landa I (1985) : A hydrogeophysical model for relations between electrical
 and hydraulic properties of aquifers. J Hydrol 79:1–19.
- Moore C, Doherty J (2006) : The cost of uniqueness in groundwater model calibration. Adv Water
 Resour 29:605–623. doi: 10.1016/j.advwatres.2005.07.003
- Moysey S, Singha K, Knight R (2005) : A framework for inferring field-scale rock physics
 relationships through numerical simulation. Geophys Res Lett 32:L08304. doi:
 10.1029/2004GL022152
- Munday T, Gilfedder M, Taylor andrew r, Ibrahimi T, Ley-cooper Y, Cahill K, Smith S, Costar A
 (2015) : The role of airborne geophysics in facilitating long-term outback water solutions to
 support mining in South Australia. Water J Aust Water Assoc 42:138–141.
- Nowak W, Rubin Y, de Barros FPJ (2012) : A hypothesis-driven approach to optimize field
 campaigns. Water Resour Res 48:W06509. doi: 10.1029/2011WR011016
- Oldenborger GA, Pugin AJ-M, Pullan SE (2013) : Airborne time-domain electromagnetics,
 electrical resistivity and seismic reflection for regional three-dimensional mapping and

- characterization of the Spiritwood Valley Aquifer, Manitoba, Canada. Near Surf Geophys
 11:63–74. doi: 10.3997/1873-0604.2012023
- Oliver DS, Reynolds AC, Liu N (2008) Inverse Theory for Petroleum Reservoir Characterization
 and History Matching. Cambridge University Press; University Printing House, Cambridge
 CB2 8BS, United Kingdom
- Piotrowski JA (1994) : Tunnel-valley formation in northwest Germany—geology, mechanisms of
 formation and subglacial bed conditions for the Bornhöved tunnel valley. Sediment Geol
 89:107–141.
- Pollock DW (1994) User 's Guide for MODPATH / MODPATH-PLOT, Version 3: A particle
 tracking post-processing package for MODFLOW, the U. S. Geological Survey finite difference ground-water flow model.
- Purvance DT, Andricevic R (2000) : On the electrical-hydraulic conductivity correlation in aquifers.
 Water Resour Res 36:2905–2913. doi: 10.1029/2000WR900165
- Refsgaard JC, Auken E, Bamberg CA, Christensen BSB, Clausen T, Dalgaard E, Effersø F,
 Ernstsen V, Gertz F, Hansen AL, He X, Jacobsen BH, Jensen KH, Jørgensen F, Jørgensen LF,
 et al (2014) : Nitrate reduction in geologically heterogeneous catchments--a framework for
 assessing the scale of predictive capability of hydrological models. Sci Total Environ 468469:1278–1288. doi: 10.1016/j.scitotenv.2013.07.042
- Refsgaard JC, Christensen S, Sonnenborg TO, Seifert D, Højberg AL, Troldborg L (2012) : Review
 of strategies for handling geological uncertainty in groundwater flow and transport modeling.
 Adv Water Resour 36:36–50. doi: 10.1016/j.advwatres.2011.04.006
- Reilly TE (2001) : Techniques of Water-Resources Investigations of the United States Geological
 Survey, Book 3, Applications of Hydraulics. In: System And Boundary Conceptualization In
 Ground-Water Flow Simulation. U.S. Geological Survey, Denver, CO, USA.,
- Reilly TE, Harbaugh AW (2004) Guidelines for Evaluating Ground-Water Flow Models. U.S.
 Geological Survey Scientific Investigations Report 2004-5038—Version 1.01
- 27 Revil A, Cathles LM (1999) : Permeability of shaly sands. Water Resour Res 35:651–662. doi:
 28 10.1029/98WR02700
- Ruggeri P, Gloaguen E, Lefebvre R, Irving J, Holliger K (2014) : Integration of hydrological and
 geophysical data beyond the local scale: Application of Bayesian sequential simulation to field
 data from the Saint-Lambert-de-Lauzon site, Québec, Canada. J Hydrol 514:271–280. doi:
 10.1016/j.jhydrol.2014.04.031
- Ruggeri P, Irving J, Gloaguen E, Holliger K (2013) : Regional-scale integration of multiresolution
 hydrological and geophysical data using a two-step Bayesian sequential simulation approach.
 Geophys J Int 194:289–303. doi: 10.1093/gji/ggt067
- Sànchez M, Gunnink JL, van Baaren ES, Oude Essink GHP, Siemon B, Auken E, Elderhorst W, de
 Louw PGB (2012) : Modelling climate change effects on a Dutch coastal groundwater system
 using airborne electromagnetic measurements. Hydrol Earth Syst Sci 16:4499–4516. doi:
 10.5194/hess-16-4499-2012
- Sandersen PBE, Jørgensen F (2003) : Buried Quaternary valleys in western Denmark-occurrence
 and inferred implications for groundwater resources and vulnerability. J Appl Geophys
 53:229–248.

- Seifert D, Sonnenborg TO, Scharling P, Hinsby K (2007) : Use of alternative conceptual models to
 assess the impact of a buried valley on groundwater vulnerability. Hydrogeol J 16:659–674.
 doi: 10.1007/s10040-007-0252-3
- Singha K, Gorelick SM (2006) : Effects of spatially variable resolution on field-scale estimates of
 tracer concentration from electrical inversions using Archie's law. GEOPHYSICS 71:G83–
 G91. doi: 10.1190/1.2194900
- Singha K, Moysey S (2006) : Accounting for spatially variable resolution in electrical resistivity
 tomography through field-scale rock-physics relations. GEOPHYSICS 71:A25–A28. doi:
 10.1190/1.2209753
- Slater L (2007) : Near Surface Electrical Characterization of Hydraulic Conductivity: From
 Petrophysical Properties to Aquifer Geometries—A Review. Surv Geophys 28:169–197. doi:
 10.1007/s10712-007-9022-y
- Steuer A, Siemon B, Eberle D (2008) : Airborne and Ground-based Electromagnetic Investigations
 of the Freshwater Potential in the Tsunami-hit Area Sigli, Northern Sumatra. J Environ Eng
 Geophys 13:39–48. doi: 10.2113/JEEG13.1.39
- Tonkin M, Doherty J, Moore C (2007) : Efficient nonlinear predictive error variance for highly
 parameterized models. Water Resour Res 43 (7):W07429. doi: 10.1029/2006WR005348
- 18 Urish DW (1981) : Electrical resistivity-hydraulic conductivity relationships in glacial outwash
 aquifers. Water Resour Res 17:1401–1408. doi: 10.1029/WR017i005p01401
- Vereecken H, Hubbard S, Binley A, Ferre T (2004) : Hydrogeophysics: An Introduction from the
 Guest Editors. Vadose Zo J 3:1060–1062. doi: 10.2113/3.4.1060
- Viezzoli A, Munday T, Auken E, Christiansen A V. (2010a) : Accurate quasi 3D versus practical
 full 3D inversion of AEM data the Bookpurnong case study. Preview 2010:23–31. doi:
 10.1071/PVv2010n149p23
- Viezzoli A, Tosi L, Teatini P, Silvestri S (2010b) : Surface water-groundwater exchange in transitional coastal environments by airborne electromagnetics: The Venice Lagoon example.
 Geophys Res Lett 37:L01402. doi: 10.1029/2009GL041572
- Vilhelmsen TN, Behroozmand AA, Christensen S, Nielsen TH (2014) : Joint inversion of aquifer
 test, MRS, and TEM data. Water Resour Res 50:3956–3975. doi: 10.1002/2013WR014679
- West GF, Macnae JC (1991) Physics of the Electromagnetic Induction Exploration Method. In:
 Electromagnetic Methods in Applied Geophysics, Part A, edited by Nabighian, M.N., Society
 of Exploration Geophysicists, Tulsa.
- Worthington PF (1975) : Quantitative geophysical investigations of granular aquifers. Geophys
 Surv 2:313–366. doi: 10.1007/BF01447858
- Wright HE (1973) : Tunnel Valleys, Glacial Surges, and Subglacial Hydrology of the Superior
 Lobe, Minnesota. Geol Soc Am Mem 136:251–276. doi: 10.1130/MEM136
- Zhou H, Gómez-Hernández JJ, Li L (2014) : Inverse methods in hydrogeology: Evolution and
 recent trends. Adv Water Resour 63:22–37. doi: 10.1016/j.advwatres.2013.10.014
- 39

1 Table 1. Geostatistical parameters for stochastic hydraulic field employed by the hydraulic 2 reference model. K is for hydraulic conductivity (ms⁻¹), R is for recharge (ms⁻¹) to the groundwater 3 model, and phi for porosity. μ is mean value to the log10 of K, *a* is range for small-scale variability, and 4 σ^2 the sill. The semivariograms are exponential.

		log ₁₀ (,	K)		$log_{10}(R)$			$log_{10}(\varphi)$		
Category	μ	а	σ^{2}	μ	а	σ^{2}	μ	а	σ^2	
Gravel	-3.00	200.	0.0227	-8.20	200.	0.007752	-0.60	200.	0.000428	
Sand	-4.00	200.	0.0227	-8.20	200.	0.007752	-0.60	200.	0.000428	
Silt	-6.00	200.	0.0227	-8.60	200.	0.007752	-0.74	200.	0.000428	
Clay	-7.00	50.	0.122	-8.82	50.	0.007752	-1.00	50.	0.000428	

		Location	1	Location			Location				
Borehole	X(m)	Y(m)	Screened layer	Borehole	X(m)	Y(m)	Screened layer	Borehole	X(m)	Y(m)	Screened layer
well_1	3692	6100	4	well_13	2375	4127	19	well_25	1460	2064	5
well_2	2375	5824	8	well_14	1155	3905	3	well_26	2506	2024	20
well_3	850	5662	4	well_15	2616	3720	20	well_27	2611	1990	18
well_4	4308	5602	3	well_16	2394	3637	19	well_28	2468	1750	20
well_5	2717	5570	6	well_17	4073	3565	4	well_29	2893	1741	9
well_6	1201	5550	4	well_18	2828	3498	12	well_30	4255	1632	4
well_7	2144	5477	8	well_19	2140	3421	10	well_31	2542	1482	20
well_8	2384	5006	16	well_20	2412	3184	20	well_32	2357	1047	5
well_9	2634	4830	14	well_21	665	3042	4	well_33	900	705	5
well_10	1174	4583	3	well_22	2311	2823	13	well_34	2838	649	11
well_11	4243	4506	4	well_23	2884	2379	6	well_35	2384	400	12
well_12	2708	4330	15	well_24	2421	2231	20				

1 Table 2. Location and screened layer of boreholes with head measurements for model calibration

1 Table 3. Different types of model predictions with and without a pumping well

With pumping (the flow situation when	Without pumping
calibrating)	
1. Head at 10 locations	4. Head recovery at 10 locations
2. Recharge area	5. Particle travel time
3. Average groundwater age	6. Relative particle endpoint
	7. River discharge

	Loc	cation		Location				
Head pred. p	oint X(n	n) Y(m)	Screen	Head pred. point	t X(m)	Y(m)	Screen	
pred_1	2500	5100	5	pred_6	2260	5650	5	
pred_2	900	2000	4	pred_7	1600	3650	5	
pred_3	1025	5600	5	pred_8	2606	1950	19	
pred_4	4100	5825	4	pred_9	2464	2128	20	
pred_5	2580	3975	15	pred_10	2505	1615	15	

1 Table 4. Head and head recovery prediction points and screened layer



1

Figure 1: Workflow of the HYTEB. Each numbered dashed box marks a major step in the work
flow. In parts 1 and 5 the red, yellow, blue and green colors indicate different categories (types) of

4 geological deposits; color variation within each category (in part 6) indicates variation in hydraulic

5 conductivity





Figure 2: A map of locations of boreholes, a pumping well, geophysical data, pilot points,
predictions of interest and location of a geological cross-section. (The positions of the pilot points
and geophysical measurements are coincident.)





- 2 Figure 3. Hydraulic conductivity field for one of the model realizations. (Red shades are for gravel,
- 3 yellow for sand, green for silt, and cyan/blue for clay.)



1

Figure 4: Measurement objective function value obtained for the various groundwater model calibration cases and for the 10 different system realizations. The two dashed lines in the top plot indicate the target value for the various model calibrations: the upper dashed line is the target value for the JHI, and the lower dashed line is the target value for HI and SHI. The dashed line in the three lower plots similarly marks the respective target value.



1

2 Figure 5: Reference and estimated hydraulic conductivity fields for model realization number 189:

a) shows the fields for layers 1 to 6; b) shows the field along an east-west cross section in themiddle of the domain.

4 m



1

Figure 6. Pilot-point-by-pilot-point scatter plot of reference versus estimated hydraulic conductivity
for the six inversion runs. Black dots are estimated parameter values from the capping part of the

4 model, while the red dots are estimated parameter values within the buried valley.



Figure 7: Scatter plots of calibrated model prediction versus reference prediction for five
predictions (explained in body text). Each plot shows results from ten system realizations.



Figure 8: Mean absolute relative prediction error calculated from the ten geological realization results. The symbol type indicates the inversion approach and the symbol color indicates the initial parameter values used when calibrating the groundwater model. Red labels at x-axis highlight prediction errors that are reduced by using TEM data and TEM models for groundwater model calibration.