Effects of snow ratio on annual runoff within Budyko framework

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Abstract

Warmer climate may lead to less precipitation falling as snow in cold season. Such a switch in the state of precipitation not only alters temporal distribution of intra-annual runoff, but also tends to yield less total annual runoff. Long-term water balance for 282 catchments across China is investigated, showing that decreasing snow ratio reduces annual runoff for a given total precipitation. Within the Budyko framework, we develop an equation to quantify the relationship between snow ratio and annual runoff from a water-energy balance viewpoint. Based on the proposed equation, attribution of runoff change during past several decades and possible runoff change induced by projected snow ratio change using climate experiment outputs archived in the Coupled Model Intercomparison Project Phase 5 are analyzed. Results indicate that annual runoff in northwestern mountainous and northern high-latitude areas are sensitive to snow ratio change. The proposed model is applicable to other catchments easily and quantitatively for analyzing the effects of possible change in snow ratio on available water resources and evaluating the vulnerability of catchments to climate change.

Keywords: Budyko framework, snow ratio, runoff, climate change

1 Introduction

More than one-sixth of the world's population lives in catchments with snowmelt-dominated runoff (Barnett et al., 2005), and thus change in snowfall may exerts a great influence over available water resources in these regions. In a warmer climate, the rising temperature may decrease the precipitation falling as snow in cold season. Decrease in snowfall amount and increasing in temperature can lead to earlier spring peak river runoff and a reduction in summer-autumn runoff for a given total annual precipitation (Stewart et al., 2005; Godsey et al., 2014). Therefore, the change in the state of precipitation (rainfall or snow) induced by global warming would alter the temporal distribution of intra-annual runoff, thereby increasing the possibility of spring flood disasters (Allamano et al., 2009) and summer water supply crisis in relevant regions. Although the possible events can have catastrophic impacts on those snow-dominated basins, these impacts can be mitigated where existing reservoirs possess adequate storage capacity to buffer the shift in runoff timing (Vörösmarty et al., 1997; Payne et al., 2004). To date, however, little work has been done to investigate the impact and mechanism of this shift in the state of precipitation on mean annual runoff which is a key factor that controls the available freshwater resources for domestic and agricultural needs. Berghuijs et al. (2014) conducted a preliminary analysis using the MOPEX dataset and found that higher snowfall fraction is statistically associated with increased annual runoff at pristine catchments. They also pointed out that mechanistic understanding of this phenomenon is still lacking. Inspired by Berghuijs et al. (2014), we aim to understand and quantify the relationship between snow ratio of precipitation falling as snow to total precipitation and mean annual runoff, as well as assess the hydrological response to snow ratio variation induced by climate change in this study.

In order to address the problem, adopting a distributed hydrological model coupled with Global Circulation Model projections and calibrated with observed data may be a way (Cayan et al., 2008; Huss et al., 2008). However, large numbers of parameters and the site-specific nature of distributed models limit us to clarify the dominant factors affecting the connection between snow ratio and mean annual runoff. Furthermore, the distributed model may perform well over short time scales, but large knowledge gaps still remain at multi-annual time scale that impede the pursuit of better understanding the effect of snow ratio on mean annual runoff. Meanwhile, it can be a very tedious exercise when quantifying the impact of snow ratio change on the mean annual runoff by applying a detailed hydrologic model to hundreds of catchments.

Low-dimensional models may provide us an alternative tool to isolate the key component of the relationship between the above two variables. Budyko (1974) introduced a simplified analytical framework to quantify the long-term averaged hydrological partitioning between runoff and evapotranspiration at catchment scale. Within this framework, the actual evapotranspiration (E) is determined, to first order, by available energy and available water which are measured as potential evapotranspiration (E_p) and precipitation (P), respectively. Subsequently, lots of efforts (Fu, 1981; Choudhury, 1999; Yang et al., 2008) focus on theoretical and empirical development of the framework by introducing an additional parameter accounting for local landscape characteristics (Yang et al., 2009) or seasonality of climate forcing (Feng et al., 2012). This simple framework captures the main features of water-energy balance and is widely employed to evaluate the hydrologic response to climate change and human activities (Roderick and Farquhar, 2011; Wang and Hejazi, 2011). When addressing the influence of snow ratio on the mean annual runoff, the water-energy balance is also the key point which needs to be clarified. Thus, it is a possible way to investigate the influence of snow ratio on mean annual runoff in the context of the Budyko framework.

Here, we study the effects of snow on the mean annual runoff by analyzing the long-term observed records from catchments across China. A theoretical tool is proposed to help us have a deeper understanding of the role of snow on the mean annual runoff quantitatively. In addition, the contributions of changes in snow ratio to the variations in annual runoff during the past several decades and possible changes in annual runoff under projected climate scenario are also presented. Such studies are expected to present important implications for future water management strategy when global warming is considered.

2 Data sources

The daily meteorological data, including precipitation, temperature, relative humidity, wind speed and sunshine hours were collected at 743 national meteorological stations during 1961-2010 from the China Meteorological Administration. In addition, daily solar radiation was collected from 118 stations during the period 1961–2010. Meanwhile, monthly runoff data of 282 catchments across China was collected. These catchments were selected based on the length of records exceeding 25 years and all observed points being within the supply and demand limits of the framework. Furthermore, there is relatively low direct influence of human activities such as, irrigation, damming, and water diversion on the catchments. The areas of these catchments vary from 372 to 142963 km^2 and these catchments cover a sizable portion of land area within China as shown in Fig.1. The catchment average slope was calculated from the HYDRO1k data sets, developed by the U.S. Geological Survey's (USGS) EROS Data Center, at a resolution of 1 km. (available at the web http://eros.usgs.gov/elevation-products)

Because the precipitation type is not available at any of the meteorological stations since 1980, the empirical relationship evaluated for China territory to discriminate precipitation types is called for. The empirical discrimination scheme [Ding et al., 2014] derived from more than 400,000 samples collected from different climate regimes and elevations across China from 1951 to 1979 was adopted. The precipitation is categorized according to:

$$type = \begin{cases} snow, & T_w \leq T_1 \\ sleet, & T_1 \leq T_w \leq T_2 \\ rain, & T_w \geq T_2 \end{cases} \qquad (1)$$

where T_w is daily mean wet-bulb temperature, a function of air temperature, relative humidity and air pressure. T_1 and T_2 are two threshold temperature which can be empirically parameterized by relative humidity and elevation based on the observations. According to this discrimination scheme, if a precipitation event was judged as snow or sleet, the corresponding precipitation quantity was counted in the annual snowfall amount.

To obtain the average daily climate forcing in each catchment, a 10-km grid data across the China was interpolated from the observations of all meteorological stations by angular distance-weighted interpolation, and then catchment values were calculated by averaging values of grids covering the analyzed catchments. The interpolated grid temperature was modified by its elevation. Daily E_p was calculated based on the Penman-FAO equation (Allen et al., 1998) using grid data with consideration of the corresponding land use type. And the E_p of grids which are waters and non-waters were calculated using Eq. (2) and Eq. (3), respectively.

$$E_p = \frac{\Delta}{\Delta+\gamma}\frac{R_n - G}{\lambda} + \frac{\Delta}{\Delta+\gamma}\frac{6.43(1+0.536U_2)(e_s - e_a)}{\lambda} \tag{2}$$

$$E_p = 0.408\frac{\Delta}{\Delta+\gamma^*}(R_n - G) + \frac{\gamma}{\Delta+\gamma^*}\frac{900}{T+273}U_2(e_s - e_a) \tag{3}$$

where T is daily average air temperature [℃] and Δ is the slope of the saturated vapor pressure versus T curve [kPa ℃$^{-1}$]; U_2 is the wind speed at 2m above ground [m s^{-1}]; e_s is the saturated vapor pressure [kPa]; e_a is the actual vapor pressure [kPa]; R_n and G are the net radiation and ground heat flux, respectively [MJ m^{-2} d^{-1}]; λ is the latent heat of vaporization of water [J g^{-1}] and γ is the psychometric constant [kPa ℃$^{-1}$], $\gamma^* = \gamma(1+0.34U_2)$.

The daily climate variables were aggregated to annual values for all catchments. Snow ratio (r_s) was calculated as the ratio of mean annual snowfall amount to mean annual precipitation, which can eliminate the influence of phase difference originating from the snow accumulation and melting in different years.

The monthly Global Inventory Modeling and Mapping Studies normalized difference vegetation index (NDVI) from 1982 to 2006 with 8 km resolution was collected from the Advanced Very High Resolution Radiometer (AVHRR) sensor (Buermann et al., 2002). Likewise, long-term average annual NDVI value for each catchment was calculated from the dataset and the corresponding vegetation coverage (M) was estimated following Gutman and Ignatov (1998),

$$M = \frac{NDVI - NDVI_{\min}}{NDVI_{\max} - NDVI_{\min}} \quad (4)$$

where $NDVI_{\max}$ and $NDVI_{\min}$ are the NDVI signals from dense green vegetation and bare soil , which were chosen to be 0.80 and 0.05, respectively (Yang et al., 2009).

The future climate forcing, monthly precipitation, temperature and snowfall outputs of all the available experiments from two Representative Concentration Pathways (RCPs) archived in the Coupled Model Intercomparison Project Phase 5 (CMIP5) (Taylor et al., 2012) were extracted (38 GCMs for RCP4.5; 40 GCMs for RCP8.5, as shown in Table 1). For each GCM and each RCP, the precipitation, temperature, and snowfall outputs at the archived spatial resolution were regridded to

0.5 °×0.5 ° grid cells. For each catchment, the monthly areal average precipitation, temperature and snowfall from 2050 to 2099 were calculated from above model outputs. Monthly E_p was computed using the Hamon's equation (Hamon, 1961) as:

$$E_p = \alpha \cdot d \cdot D^2 \cdot \rho_w \tag{5}$$

where, *d* is the number of days in a month; *D* is the mean monthly hours of daylight in units of 12 h; $\rho_w = 0.0495e^{0.062T}$ is a saturated water vapor density; and *T* is the monthly mean temperature [℃]. α, the adjustment factor, was calibrated via minimizing the difference between the two mean annual Ep values (2000-2010) obtained by the Penman-FAO and Hamon's equation respectively for each catchment. The projected monthly precipitation, snowfall and potential evapotranspiration were aggregated to annual values for 2050-2099.

3 Methodology

3.1 Inclusion of snow ratio in the Budyko framework

At multi-decades timescale, neglecting the catchment groundwater or glacial storage change, mean annual actual evapotranspiration (E) is estimated as the residual of annual precipitation minus runoff (***Q***). On the other hand, *E* can be given by a function of available energy (E_p) and available water (P) for evapotranspiration, proposed by Budyko (1974):

$$1 - \frac{Q}{P} = \sqrt{\frac{E_p}{P}[1 - \exp(-\frac{E_p}{P})]\tanh(\frac{1}{E_p / P})} \tag{6}$$

Other Budyko-type curves were developed for describing catchment long-term water balance, by introducing a unique parameter to assess differences among catchments (Fu, 1981; Choudhury, 1999; Zhang et al., 2001; Wang and Tang, 2014). Among them, Yang et al. (2008) provided a theoretical solution to the mean annual water-energy balance equation under general conditions through dimensional analysis and mathematic reasoning, which shares the same functional form with Choudhury's equation:

$$1-\frac{Q}{P}=[1+(\frac{E_p}{P})^{-n}]^{-1/n} \tag{7}$$

where, n is a synthesis parameter which represents the effects of catchment factor, such as vegetation type and coverage, soil type and topography, on the precipitation partitioning, referred as specific catchment parameter herein. As shown in Fig.2, the relationship between annual mean runoff index (Q/P) and dryness index (E_p/P) is depicted. A larger value of n is associated with a lower runoff index given the same dryness index.

When snowfall is considered, there are some differences in energy and water terms involved in Eq. (7). For evapotranspiration capacity, it should be noted that part of available energy need be taken away to melt the snowfall compared with "paired catchment" where other conditions are the same but all precipitation falls as rainfall. Meanwhile, little sublimation and runoff are observed during snow accumulation season (Anderson, 1968; Dewalle and Meiman, 1971; Weller and Holmgren, 1974). The snowfall needs to be transferred into liquid phase before it can participate into the hydrological cycle. The melting energy R_m required to convert snowfall to the reference state (0 ℃ liquid phase) reads:

$$R_m = \rho_w W(h_f + C_i \overline{\Delta T}) \tag{8}$$

where, ρ_w is the density of water [1000 kg m^{-3}] and W is snow water equivalence [m], *i.e.* snowfall amount ($r_s \cdot P$); h_f is the latent heat of fusion [335kJ kg^{-1}]. $C_i \overline{\Delta T}$ represents the energy needed in snow warming phase during which the averaged accumulated snow temperature increases until the snowpack is isothermal at 0 ℃ where C_i is the specific heat of ice [2.1kJ kg^{-1} ℃$^{-1}$] and $\overline{\Delta T}$ averaged negative snow surface temperature, order of 10 ℃.

Thus, the effective energy available for evapotranspiration E_p^e is the difference between E_p and melting heat equivalence R_m / L, where L is latent heat of evaporation [2500kJ kg^{-1}]. After a rough algebraic computation, E_p^e reads:

$$E_p^e = E_p - R_m / L = E_p - 0.14 r_s \cdot P \tag{9}$$

In melting season, the magnitude of sensible heat is several times larger than latent heat (Dingman, 2002), implying that only a small part of snow is evaporated or sublimated. For example, according to the energy budget during the accumulation and melt periods for 6 seasons (1968-1973) at the Danwille site, VT, US (Anderson,1976), the average turbulent exchange of latent heat each season are 1160cal/cm^2, equivalent to 1.7cm vaporized water. Compared with the maximum snow depth of 72cm in that location, the evaporation of snowfall is very small.

What is more, the concrete frozen ground is most commonly found in open land and sometimes in forested land (Pierce et al., 1958; Fahey and Lang, 1975), which makes the melting water infiltration difficultly. Given that the frozen ground has extremely low permeability, the surface flow is preferred during the snow melting period (Dunne and Black, 1971). Or, the melting snowfall accumulates to form a basal saturated zone thought which water drains to the stream (Anderson, 1976). Therefore, it is acceptable to assume that melting snow water flow away though channels without evaporation loss. As a consequence, the "effective available water" for evapotranspiration is annual rainfall $(1-r_s)\cdot P$, rather than total precipitation P.

The water-energy balance in form of Eq. (7) with consideration of snow can be rewritten as follows:

$$\frac{P-Q}{(1-r_s)\cdot P}=[1+(\frac{E_p}{(1-r_s)\cdot P}-\frac{0.14r_s}{1-r_s})^{-n'}]^{-1/n'} \quad (10)$$

Normally, the snow ratio r_s is order of 0.1, with a median value of 0.03 among studied catchments in Fig. 1 (median value of 0.09 in MOPEX data set used by Berghuijs et al., 2014). The energy correction term $0.14r_s/(1-r_s)$ in Eq. (10) is about order of 0.01, and can be neglected compared with the revised dryness index $E_p/[(1-r_s)\cdot P]$ which is order of 1. Therefore, with little loss of accuracy, the simplified Eq. (10) can be written as:

$$1-\frac{Q}{P}=[(1-r_s)^{-n'}+(\frac{E_p}{P})^{-n'}]^{-1/n'} \quad (11)$$

3.2 Attribution of runoff change

Given the inclusion of snow ratio, Eq. (11) can be used to analyze long-term water balance of catchment where snow plays a considerable role in hydrological process. Furthermore, this will provide a theoretical tool to attribute the mean annual runoff change to climate variability, especially the snow ratio change, and land use/cover change. An additional assumption that the runoff change is from one steady state to another one without any transient changes is introduced here. We reorganize Eq. (11) and differentiate it to calculate change in Q due to changes in climate factors (P, E_p, r_s) and catchment characteristic (n').

$$Q = P - [P^{-n'}(1-r_s)^{-n'} + E_p{}^{-n'}]^{-1/n'} \tag{12}$$

To first order,

$$dQ = \frac{\partial Q}{\partial P}dP + \frac{\partial Q}{\partial E_p}dE_p + \frac{\partial Q}{\partial r_s}dr_s + \frac{\partial Q}{\partial n'}dn' \tag{13}$$

where,

$$\frac{\partial Q}{\partial P} = 1 - \frac{P-Q}{P}\frac{E_p^{n'}}{[P(1-r_s)]^{n'} + E_p^{n'}} \tag{14a}$$

$$\frac{\partial Q}{\partial E_p} = -\frac{P-Q}{E_p}\frac{[P(1-r_s)]^{n'}}{[P(1-r_s)]^{n'} + E_p^{n'}} \tag{14b}$$

$$\frac{\partial Q}{\partial r_s} = \frac{P-Q}{1-r_s}\frac{E_p^{n'}}{[P(1-r_s)]^{n'} + E_p^{n'}} \tag{14c}$$

$$\frac{\partial Q}{\partial n'} = -\frac{P-Q}{n'}\left(\frac{\ln[(P^{n'}(1-r_s)^{n'} + E_p^{n'}]}{n'} - \frac{[P(1-r_s)]^{n'}\ln[P(1-r_s)] + E_p^{n'}\ln(E_p)}{[P(1-r_s)]^{n'} + E_p^{n'}}\right) \tag{14d}$$

With Eq. (13), we can estimate the change in runoff between pre- and post-period due to variations of precipitation, potential evapotranspiration, snow ratio and catchment parameter, respectively. Specifically, relative contribution of snow ratio variation to annual runoff change, η_{r_s} , is defined as:

$$\eta_{r_s} = \frac{\Delta Q_{r_s}}{\Delta Q}\cdot\frac{|\Delta Q|}{Q_1} = \mathrm{sgn}(\Delta Q)\cdot\frac{\frac{\partial Q}{\partial r_s}\Delta r_s}{Q_1} \tag{15}$$

in which, $\Delta Q_{r_s} = \frac{\partial Q}{\partial r_s} \Delta r_s$. $\Delta Q = Q_2 - Q_1$ and $\Delta r_s = r_{s2} - r_{s1}$ represent difference between post- and pre-period recorded mean annual runoff and snow ratio, respectively. $\Delta n'$ represents change in land cover and can be calculated using the mean annual P and E_p , as well as r_s for each sub-period by Eq. (11).

4 Results and Discussion

4.1 Effect of snow ratio on runoff

Mean annual runoff index (Q/P) of the 282 catchments are plotted in Fig.2 as a function of dryness index (E_p/P). Each point represents mean annual record for one basin with different color indicating the various snow ratios. The dashed lines are derived from Eq. (7) with different specific catchment parameter, by neglecting changes in catchment storage at the mean annual scale. There is a general pattern that the catchments with larger snow ratio have higher runoff index for a given dryness index, which is consistent with the finding from dataset in the United States (Berghuijs et al., 2014). However, it is still not sure that the different snow ratio of each catchment results in this kind of variance in runoff index. Before we can make this conclusion, effects of other factors on runoff index need to be excluded.

Due to limitation of available catchment data, as well as recent studies implying that the vegetation coverage (Donohue et al., 2007; Voepel et al., 2011; Xu et al., 2013) and average slope (Yang et al., 2009; Yang et al., 2014a) of catchment may be the key control on long-term hydrological partitioning of precipitation, we assume that vegetation coverage and average slope can be thought as two integrators of catchment properties. We estimated the specific catchment parameter *n* in Eq. (7) from historical observations for each catchment. In order to clear away the impacts that catchment local characteristics (herein the vegetation cover and slope are thought as the proxy of integral characteristics) have on runoff, all catchments are divided into four groups, and catchments in the same group share the similar vegetation coverage or slope. Pearson's linear correlation between specific catchment parameter *n* and snow ratio in the same group is calculated, by which we can tell whether snow ratio still has significant impact on catchment water-energy balance after getting rid of influence of local catchment properties. Figure 3 and 4 show how specific catchment parameters vary with different snow ratios in each group with similar catchment vegetation cover and average slope, respectively. The results suggest that for those catchments with similar local catchment properties, catchment with higher snow ratio tend to have a smaller specific catchment parameter *n*. Moreover, the notable negative correlation between catchment parameter *n* and snow ratio can be seen in the catchments under small and medium vegetation cover (Fig. 3a-c), or large average slope (Fig. 4d).

In other words, when excluding the effects of local catchment characteristics, catchments with larger snow ratio are believed to yield more runoff under the same climatological condition. With the above analysis, we can make a more solid conclusion that snow ratio itself indeed has impact on mean annual runoff in the context of the Budyko hypothesis. Changes in the state of precipitation from snow to rainfall not only affect the seasonal runoff dynamics, but also alter the mean annual runoff amount. Accordingly, how to evaluate the effects of snow ratio on annual runoff variance is meaningful. What's more, quantifying the sensitivity of annual runoff to snow ratio using a new approach based on the Budyko hypothesis, instead of employing least squares estimators of historical records (Berghuijs et al., 2014), may provide more insight into this phenomenon. Therefore, much more elaboration with physic mechanism, like proposed in Sect 3.1, is needed to build.

4.2 Validity of the Budyko framework considering snow effects

We estimated the catchment parameter n' in Eq. (11), and then evaluated the method's validity by investigating the relationship between n' and snow ratio. As shown in Table 2, the correlation between n' value and snow ratio for each catchment was calculated. The correlation approximates to zero and is insignificant, when taking all 282 catchments as a whole. Furthermore, when catchments are grouped by vegetation coverage as Sect 4.1, no significant negative correlation is detected, except for group with vegetation coverage of 0.4 - 0.5, and the findings are similar for catchment groups classified by slope.

Actually, we intend to analyze the long-term water balance of catchment where snow plays a considerable role in hydrological process. Thus, it may be better to investigate the validity of proposed method by excluding the results from where there is little snow. Afterwards, we further calculate the corresponding correlation for catchments with snow ratio larger than 0.01 and 0.02. Among these catchments, a more significant negative correlation between n estimated by Eq. (7) and snow ratio can be seen, and the correlation coefficients are generally larger in catchments with snow ratio of 0.02, implying the obvious effect of snow ratio on runoff there. Overall, the correlations between n' estimated by Eq. (11) and snow ratio tend to be insignificant. It therefore indicates that Eq. (11) has a good performance for evaluating the impact of snow ratio on mean annual runoff.

4.3 Contribution of climate and land use change to runoff

The annual runoff experiences a downward (decreasing) step change across China around 1980 (Zhang et al., 2008). The change in mean annual runoff is calculated as the difference between period of 1980-2005 and period of 1956-1979. As shown in Fig.5, most of the study catchments show decreasing runoff change rate, defined as the ratio of runoff change between two periods to mean annual runoff. The modeled runoff change is calculated by Eq (13). Figure 6 shows the comparison between modeled runoff changes and the observed for all 282 catchments. The points scatter overall along with the 1:1 line, indicating the proposed attribution method has a good performance for most catchments and it is convincing to analyze the relative contribution of each variable to mean annual runoff variation using this method.

The relative contributions of four factors variation to the annual runoff change are depicted in Fig. 7. During the past 50 years, total precipitation amount across China has no obvious trend, while increasing winter precipitation is seen in parts of the northern high latitude and mountains (Sun et al., 2010; Zhang and Cong, 2014). As a result, it is obvious that significant effect of change in snow ratio on annual runoff alteration is found in northwestern mountainous and high-latitude catchments (Fig. 7a) where larger portion of winter precipitation falls in solid state. Generally, the increasing snow ratio makes a negative contribution to the observed decreasing mean annual runoff. And, there is no general spatial pattern where change in total precipitation has a remarkable contribution to annual runoff alteration (Fig. 7b). During the past three decades, northern China, especially the North China Plain (Liu et al., 2003), had been seeing significant land use and land cover change, including urbanization and afforestation. And so, a large difference of catchment property *n* between two studied periods is expected. Among the four variables, the catchment parameter (Fig. 7c) has most significant effects on mean annual runoff change. In most parts of China, the annual E_p shows a decreasing trend, but the decreasing magnitude between post- and pre-period is negligible (Gao et al., 2006). As expected, the overall small negative (<15%) or tiny relative contribution of decreasing E_p to decreasing mean annual runoff is shown in Fig. 7d.

4.4 Plausible future runoff changes

As far as we are concerned, in a plausible future warming climate, quantifying the change in annual runoff resulting from per unit variation in the fraction of precipitation falling as snow is particularly vital for water resources planning. An insight into possible influence of future changing climate, especially snow ratio on annual runoff, is provided here. The 2050-2099 average annual precipitation, snow ratio and E_p of each catchment estimated from the multi-model ensemble averaged values are used as climate forcing to calculate corresponding catchment's future mean annual runoff by Eq. (11), assuming unchanged catchment parameter n' estimated from the past-decade observed data.

The projected mean annual runoff increase for 2050-2099 relative to 1956-2005 is widespread in northern China (Fig.8). On the other hand, a slight decrease is projected in most regions of southern China. The spatial pattern of the projected runoff change is consistent with runoff outputs from atmosphere-ocean general circulation models participating in the CMIP5 (Koirala et al., 2014). . The runoff increase projection in parts of northern China mainly results from future increasing precipitation amount, as well as the increasing snowfall, which is also reported by other climate change impact assessments in East Asia (Immerzeel et al., 2013). As shown in Fig. 9, the contribution of snow ratio to runoff change, defined as the ratio of runoff change due to snow ratio change to the total runoff change, is overall positive and pronounced over the catchments located in northern high-latitude and northwestern mountainous regions. The regions are consistent with areas where catchment runoff is sensitive to snow ratio variation over the past several decades as shown in Fig. 7a. Moreover, the patterns of snow ratio's contribution to runoff for RCP4.5 and RCP8.5 scenarios bear some overall resemblance, including the sensitive areas and magnitudes. Also, some differences exist where snow ratio change contributes more to runoff increasing for RCP4.5 than RCP8.5, mainly in central China. Specifically, the snow ratio's contribution to runoff change for RCP4.5 is overall larger than that for RCP8.5, although the differences are insignificant (Fig.10). This pattern also accords with the projected runoff change relative to the historical observations (not shown here). It indicates that simulated climate outputs forced with a midrange mitigation emissions scenario (RCP4.5) tend to more runoff and larger snow ratio's contribution to runoff change in China, compared with that under a high emissions scenario.

4.5 Error analysis of attribution method

Since only the first-order approximation of runoff change is used to calculate the contribution of each variable in the attribution method Eq. (13), we conduct the error analysis to access its performance in the following. Similar with Yang et al. (2014a), the Taylor series of Eq. (12) is employed to show the complete expression of runoff change as:

$$\begin{aligned} &Q(P_1+\Delta P_1, E_{p1}+\Delta E_{p1}, r_{s1}+\Delta r_{s1}, n_1+\Delta n_1) \\ &\quad = Q(P_1, E_{p1}, r_{s1}, n_1) \\ &\quad +(\Delta P_1 \frac{\partial}{\partial P_1} + \Delta E_{p1}\frac{\partial}{\partial E_{p1}} + \Delta r_{s1}\frac{\partial}{\partial r_{s1}} + \Delta n_1 \frac{\partial}{\partial n_1})Q(P_1, E_{p1}, r_{s1}, n_1) \\ &\quad + \frac{1}{2!}(\Delta P_1 \frac{\partial}{\partial P_1} + \Delta E_{p1}\frac{\partial}{\partial E_{p1}} + \Delta r_{s1}\frac{\partial}{\partial r_{s1}} + \Delta n_1 \frac{\partial}{\partial n_1})^2 Q(P_1, E_{p1}, r_{s1}, n_1) + \cdots \end{aligned} \tag{16}$$

The runoff change induced by the snow ratio change can be expressed as:

$$\begin{aligned} \Delta Q_{\Delta r_s} &= \Delta r_{s1}\frac{\partial}{\partial r_{s1}} Q(P_1, E_{p1}, r_{s1}, n_1) \\ &\quad + \frac{1}{2!}(\Delta r_{s1}\frac{\partial}{\partial r_{s1}} + \Delta P_1 \frac{\partial}{\partial P_1} + \Delta E_{p1}\frac{\partial}{\partial E_{p1}} + \Delta n_1 \frac{\partial}{\partial n_1})\Delta r_{s1}\frac{\partial}{\partial r_{s1}} Q(P_1, E_{p1}, r_{s1}, n_1) \end{aligned} \tag{17}$$

in which, we neglect the third- and higher-order terms of Eq. (16) for the third-order is equal to 3% of the second-order according to Yang et al. (2014b). The relative error

(RE) of attribution method to investigate the contribution of snow ratio change is estimated as:

$$RE_{\Delta r_s} = \left|\Delta Q_{\Delta r_s} - \Delta Q_{r_s}\right| / \left|\Delta Q_{\Delta r_s}\right| \tag{18}$$

As shown in Fig.11, the relative errors of attribution method with respect to snow ratio change are small for all 282 catchments. Specifically, as for the contribution of snow ratio change to the historical runoff, the RE of more than 90% catchments is no more than 11%. As to the two projected future climate change scenarios, the REs of more than 90% catchments are less than 8% and 12% for RCP4.5 and RCP 8.5, respectively. Therefore, the proposed first-order approximation attribution method is reliable.

4.6 limitation of revised Budyko framework

It should be noted that the assumption of no evapotranspiration loss in snowmelt adopted in Section 3.1 is not universally applicable. In small catchments, after snowfall is melt and the concrete frozen ground inhibits snowmelt infiltration, the snow water can flow away quickly though channels without evaporation loss. However, if the location of accumulated snow is far away from channels, or the snowfall amount is large, it will take longer for melt water to run off than the frozen soil thaws. In these cases, a part of snow infiltrates into the ground and later is available for evaporation (Dripps, 2012; Jasechko et al., 2014). In fact, it may be more suitable to introduce as “effective available water” for evapotranspiration, where k is a loss parameter requiring further investigation. To better understand and parameterize the snowmelt loss by evapotranspiration, the site-specific modeling and isotope-based field observations may provide tools for more detailed modeling in the future.

Apart from limitation of the assumption, the accurate estimation of snow ratio is also important for this framework. However, direct snow observation records are not available for the case study watersheds in this manuscript and the MOPEX watersheds used by Berguhijs et al. (2014). Mean annual snowfall is estimated by the air temperature-based empirical method. The threshold temperature is critical for calculating the snowfall amount. A higher threshold temperature will overestimate the snow ratio that may lead to an unreasonable conclusion under the framework in our study. According to the sensitivity analysis of catchment parameter estimation, it shows that a small variation in snow ratio can lead to a significant change in catchment parameter when snow ratio is large enough to be comparable to runoff index. Thus, the accuracy of snow ratio is important to this framework especially when the snow ratio is large, which limits the applicability of this framework in those catchments.

5 Conclusions

In this study, we showed that snow ratio could have a pronounced effect on mean annual runoff based on both historical records and theoretical analysis. In the context of the Budyko hypothesis, catchments with larger snow ratio tend to yield more long-term mean annual runoff given the same other climatological and landscape properties. Moreover, a Budyko-type equation considering the water-energy balance is derived to quantify the effects of snow ratio on runoff. With the assistance of proposed relationship, the contribution of snow ratio to change in annual runoff during the past five decades and potential annual runoff variation due to changing fraction of precipitation falling as snow under projected future global warming scenario in China are investigated. The results indicate that those sensitive catchments in northwestern mountainous and north-central high-latitude areas are undergoing remarkable runoff change resulting from snow ratio variance. In addition, the error analysis of attribution method is conducted, implying that the first-order approximation is suitable to assess the contribution of snow ratio change to runoff in this study.

This paper extends the previous work that suggested that precipitation shift from snow towards rain leads to a decrease in runoff based on dataset in U.S. (Berghuijs et al., 2014). We confirm here that the observations in China give a similar conclusion. What's more, we quantify this effect and assess the impact of climate change, especially snow ratio change, on mean annual runoff across China. As major rivers originating from mountainous regions where temperature determines the state of precipitation (Allamano et al., 2009) and afterwards affects annual runoff amount as discussed above, the findings here have valuable implications for future water management policy. The proposed model can be made applicable to other mountainous catchments of the world easily and quantify the effects of possible change in snow ratio on available water resources and analyze the vulnerability of catchments to climate change.

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Table 1. Overview of selected GCMs used in climate impact assessment. More details of the models, modeling centers and meaning of the ensemble codes can be found at http://cmip-pcmdi.llnl.gov/cmip5/availability.html.

	RCP4.5			RCP8.5	
NO.	Model	Ensemble	NO.	Model	Ensemble
1	ACCESS1.0	r1i1p1	1	ACCESS1.0	r1i1p1
2	ACCESS1.3	r1i1p1	2	ACCESS1.3	r1i1p1
3	BCC-CSM1-1	r1i1p1	3	BCC-CSM1-1	r1i1p1
4	BCC-CSM1-1-m	r1i1p1	4	BCC-CSM1-1-m	r1i1p1
5	BNU-ESM	r1i1p1	5	BNU-ESM	r1i1p1
6	CCSM4	r1i1p1	6	CANESM2	r1i1p1
7	CESM1-BGC	r1i1p1	7	CCSM4	r1i1p1
8	CESM1-CAM5	r1i1p1	8	CESM1-BGC	r1i1p1
9	CESM1-WACCM	r1i2p1	9	CESM1-CAM5	r1i1p1
10	CMCC-CM	r1i1p1	10	CESM1-WACCM	r1i2p1
11	CMCC-CMS	r1i1p1	11	CMCC-CESM	r1i1p1
12	CNRM-CM5	r1i1p1	12	CMCC-CM	r1i1p1
13	CSIRO-Mk3-6-0	r1i1p1	13	CMCC-CMS	r1i1p1
14	CANESM2	r1i1p1	14	CNRM-CM5	r1i1p1
15	EC-EARTH	r5i1p1	15	CSIRO-Mk3-6-0	r1i1p1
16	FGOALS-g2	r1i1p1	16	EC-EARTH	r2i1p1
17	FIO-ESM	r1i1p1	17	FGOALS-g2	r1i1p1
18	GFDL-CM3	r1i1p1	18	FIO-ESM	r1i1p1
19	GFDL-ESM2G	r1i1p1	19	GFDL-CM3	r1i1p1
20	GFDL-ESM2M	r1i1p1	20	GFDL-ESM2G	r1i1p1
21	GISS-E2-H	r1i1p1	21	GFDL-ESM2M	r1i1p1
22	GISS-E2-H-CC	r1i1p1	22	GISS-E2-H	r1i1p1
23	GISS-E2-R	r1i1p1	23	GISS-E2-H-CC	r1i1p1
24	GISS-E2-R-CC	r1i1p1	24	GISS-E2-R	r1i1p1
25	HadGEM2-CC	r1i1p1	25	GISS-E2-R-CC	r1i1p1
26	HadGEM2-ES	r1i1p1	26	HadGEM2-CC	r1i1p1
27	INMCM4	r1i1p1	27	HadGEM2-ES	r1i1p1
28	IPSL-CM5A-LR	r1i1p1	28	INMCM4	r1i1p1
29	IPSL-CM5A-MR	r1i1p1	29	IPSL-CM5A-LR	r1i1p1
30	IPSL-CM5B-LR	r1i1p1	30	IPSL-CM5A-MR	r1i1p1
31	MIROC-ESM	r1i1p1	31	IPSL-CM5B-LR	r1i1p1
32	MIROC-ESM-CHEM	r1i1p1	32	MIROC5	r1i1p1
33	MIROC5	r1i1p1	33	MIROC-ESM	r1i1p1
34	MPI-ESM-LR	r1i1p1	34	MIROC-ESM-CHEM	r1i1p1
35	MPI-ESM-MR	r1i1p1	35	MPI-ESM-LR	r1i1p1
36	MRI-CGCM3	r1i1p1	36	MPI-ESM-MR	r1i1p1
37	NorESM1-M	r1i1p1	37	MRI-CGCM3	r1i1p1

38	NorESM1-ME	r1i1p1	38	MRI-ESM1	r1i1p1
			39	NorESM1-M	r1i1p1
			40	NorESM1-ME	r1i1p1

Table 2. Summary of correlation between specific catchment parameter and snow ratio for different catchment groups. (*n* is estimated by Eq.(7); *n′* is estimated by Eq.(11))

	all 282 catchments		catchments with $r_s > 0.01$		catchments with $r_s > 0.02$	
	n	n'	n	n'	n	n'
As a whole	-0.21***	0.05	-0.27***	0.04	-0.38***	-0.03
Vegetation Coverage						
0.1 - 0.3	-0.50***	-0.03	-0.50***	-0.03	-0.50***	-0.03
0.3 - 0.4	-0.49***	-0.32*	-0.44***	-0.28	-0.48***	-0.32*
0.4 - 0.5	-0.44***	-0.38*	-0.47***	-0.36**	-0.59***	-0.48***
0.5 - 0.7	-0.09	0.18	0.03	0.08	-0.04	0
Slope (%)						
0.2 - 3.8	-0.24*	0.01	-0.25*	-0.03	-0.30**	-0.07
3.8 - 5.5	-0.14	0.27	-0.06	0.33	-0.16	0.26
5.5 - 8.0	-0.20	-0.03	-0.35***	-0.14	-0.41***	-0.19
8.0 - 18.7	-0.40***	-0.29*	-0.47***	-0.36**	-0.45***	-0.34*

Note: *, ** and *** indicate the significant level at 0.05, 0.01 and 0.001, respectively.

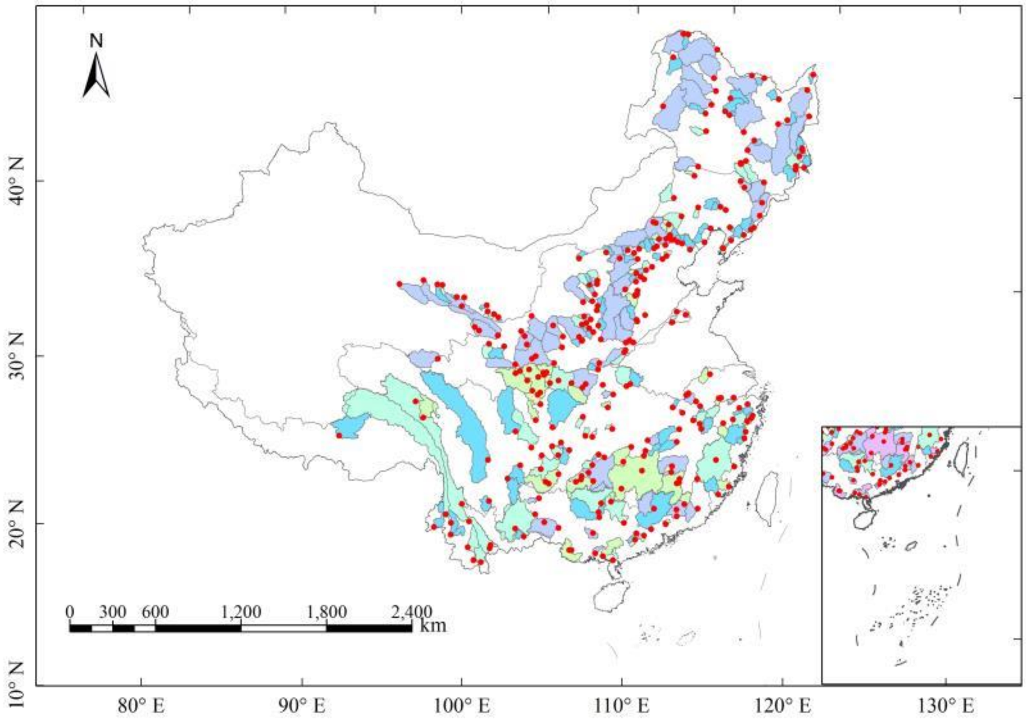

Fig.1 The location of the studied catchments. Red points represent catchment runoff gauge stations.

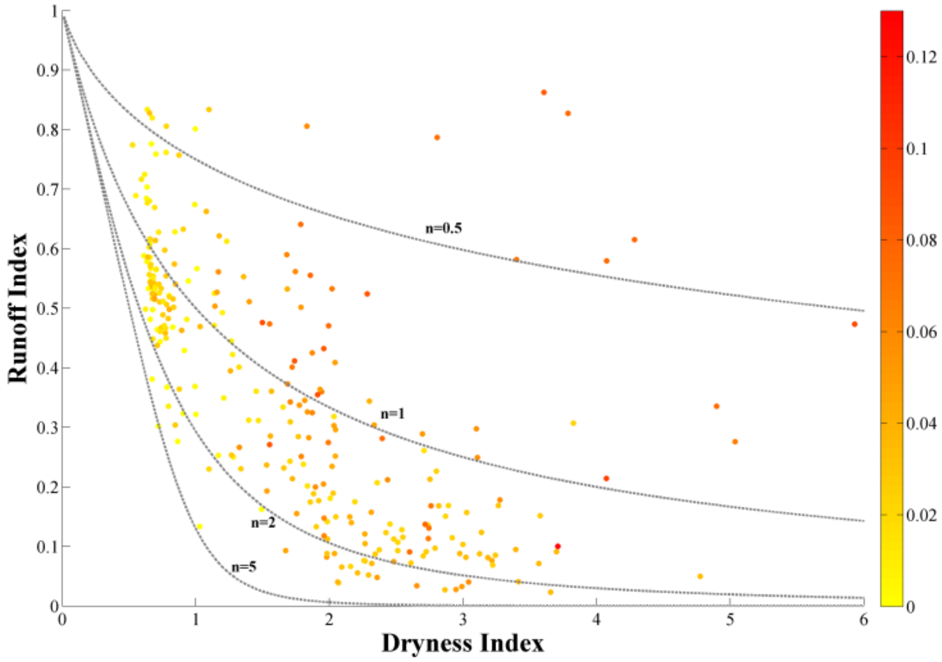

Fig.2 The 282 long-term climatological water budget observations in China. Each point represents a catchment. The color refers to snow ratio. Dashed lines are derived from Eq.(7) with different *n* values.

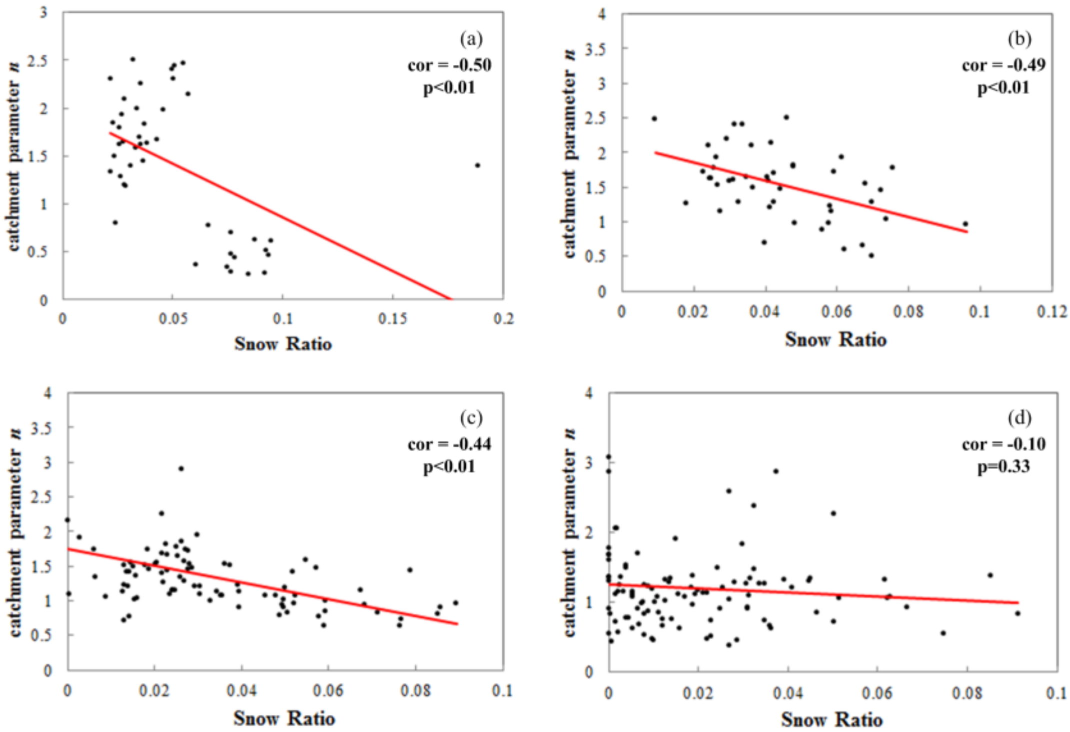

Fig.3 In the context of the Budyko-Choudhury framework, statistical relationships between specific catchment parameter n and snow ratio, under similar vegetation coverage. Least squares regression lines are shown on each of the plots. The small Pearson's linear correlation coefficient clarifies the significant negative correlation between snow ratio and catchment parameter. (a) - (d) indicate the vegetation coverage of < 0.3, (0.3,0.4), (0.4, 0.5), and > 0.5, respectively.

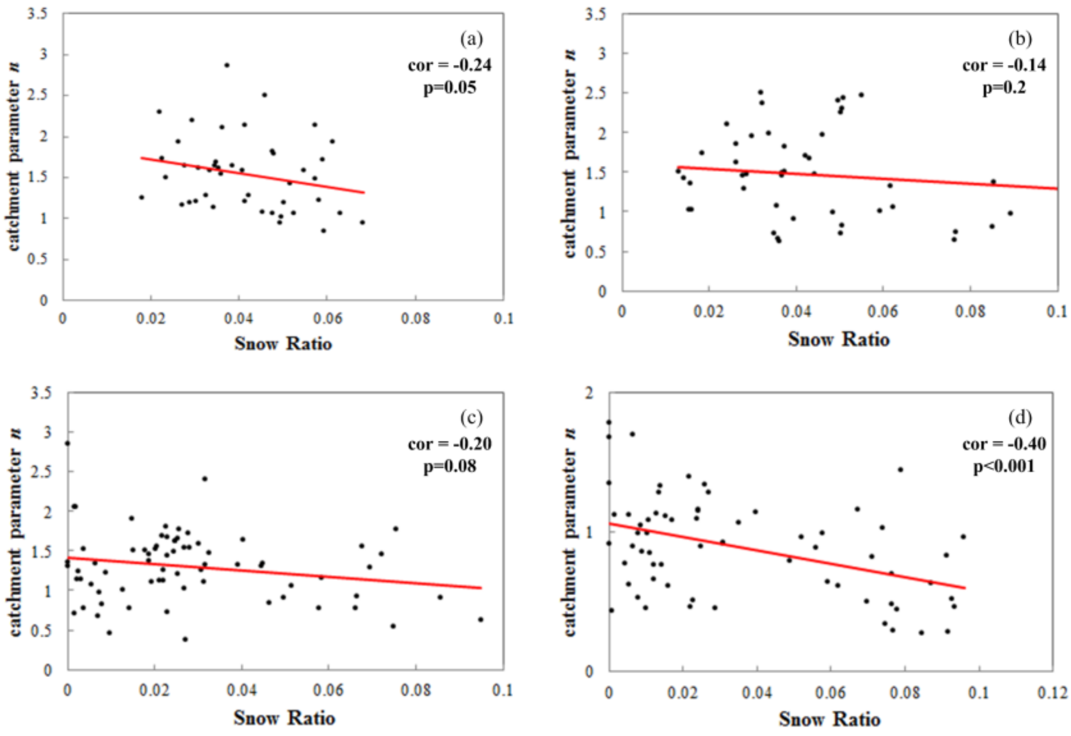

Fig.4 Similar with Fig.3 for catchment average slope. (a) - (d) indicate the average slope (%) of (0.2 3.8), (3.8 5.5), (5.5 8.0), and > 8.0, respectively.

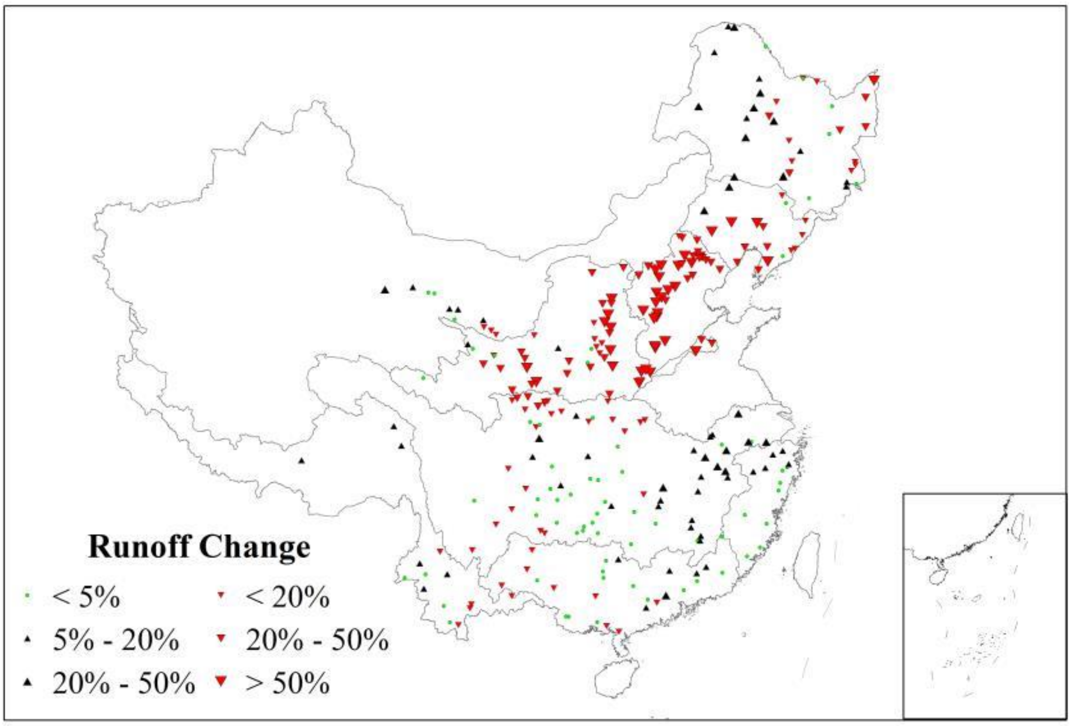

Fig.5 Mean annual runoff change rate between two periods.

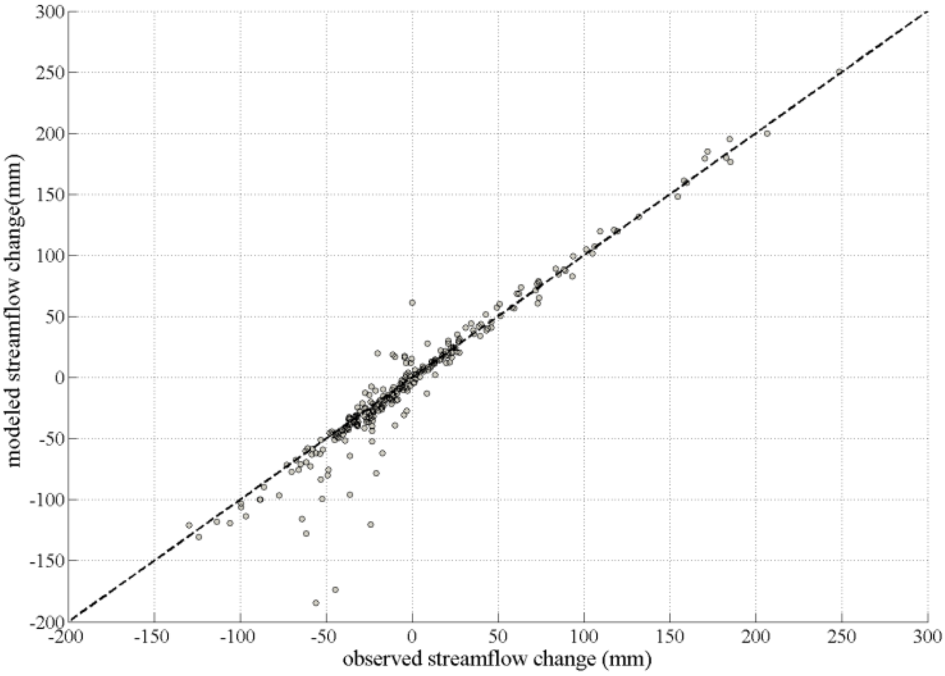

Fig.6 Comparison between observed and calculated mean annual runoff change.

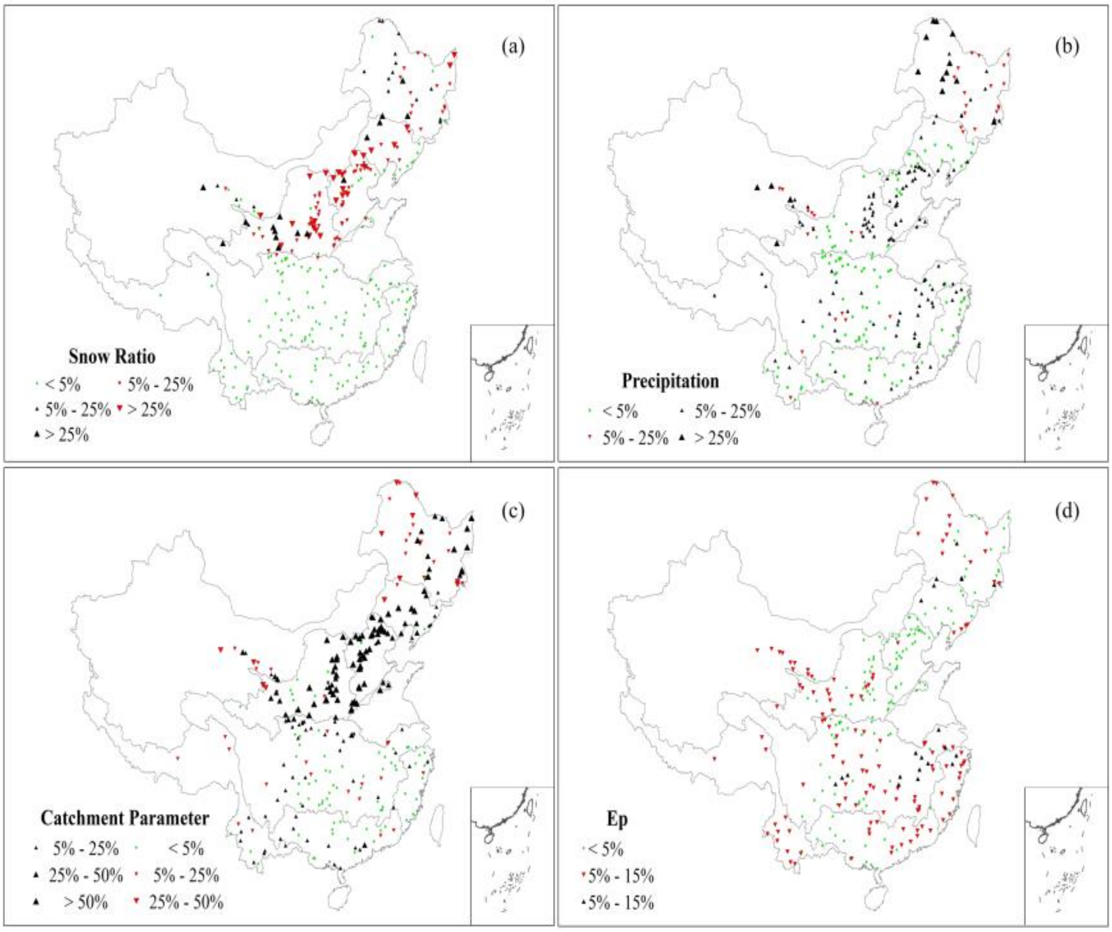

Fig.7 Relative contributions of (a) snow ratio, (b) precipitation, (c) specific catchment parameter, and (d) potential evapotranspiration variance to change in mean annual runoff. Upward triangle represents the positive relative contribution of the variable to change in runoff; downward triangle represents the negative.

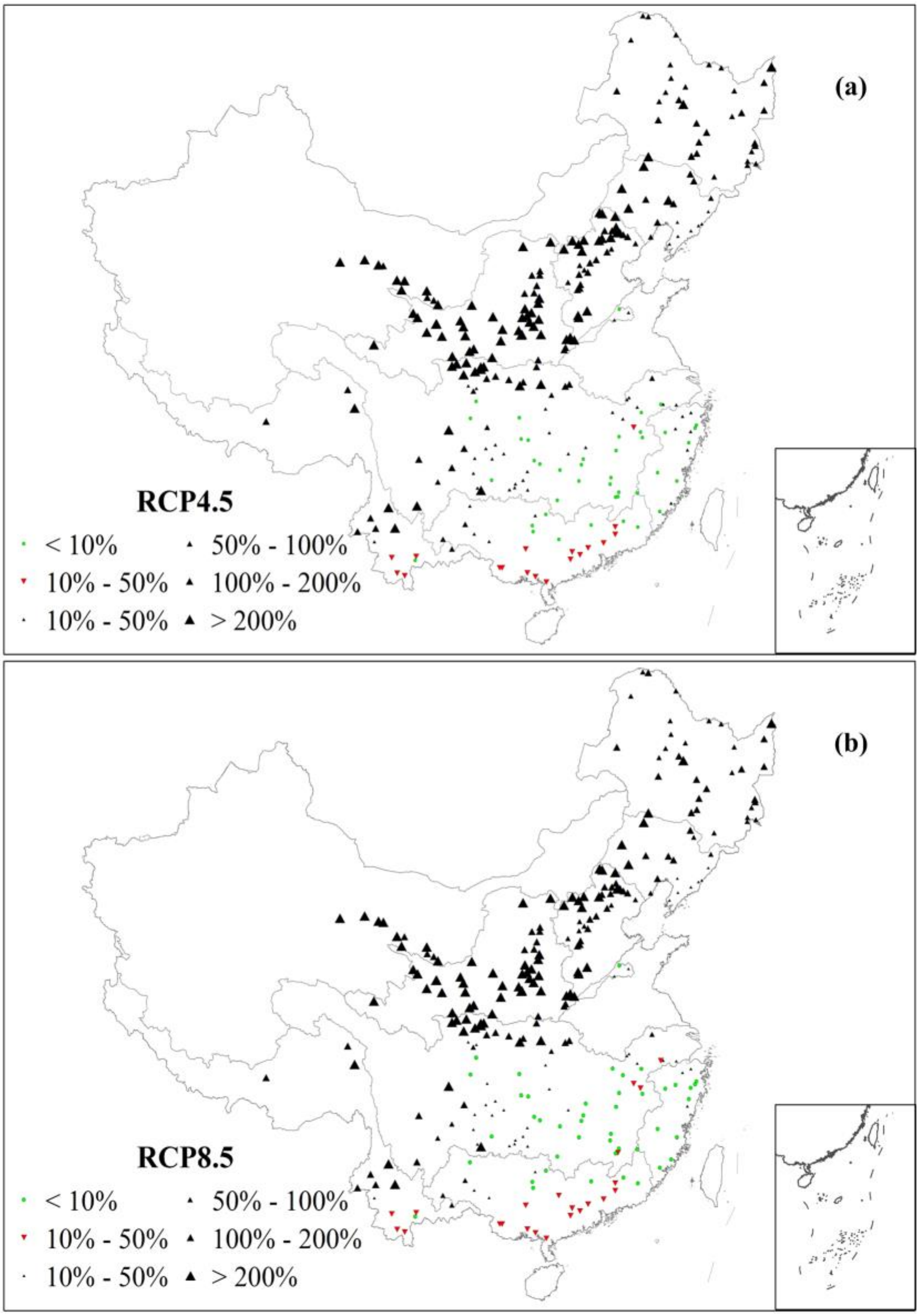

Fig. 8 Change rate of mean annual runoff under projected future climate. (a: RCP4.5; b: RCP8.5).

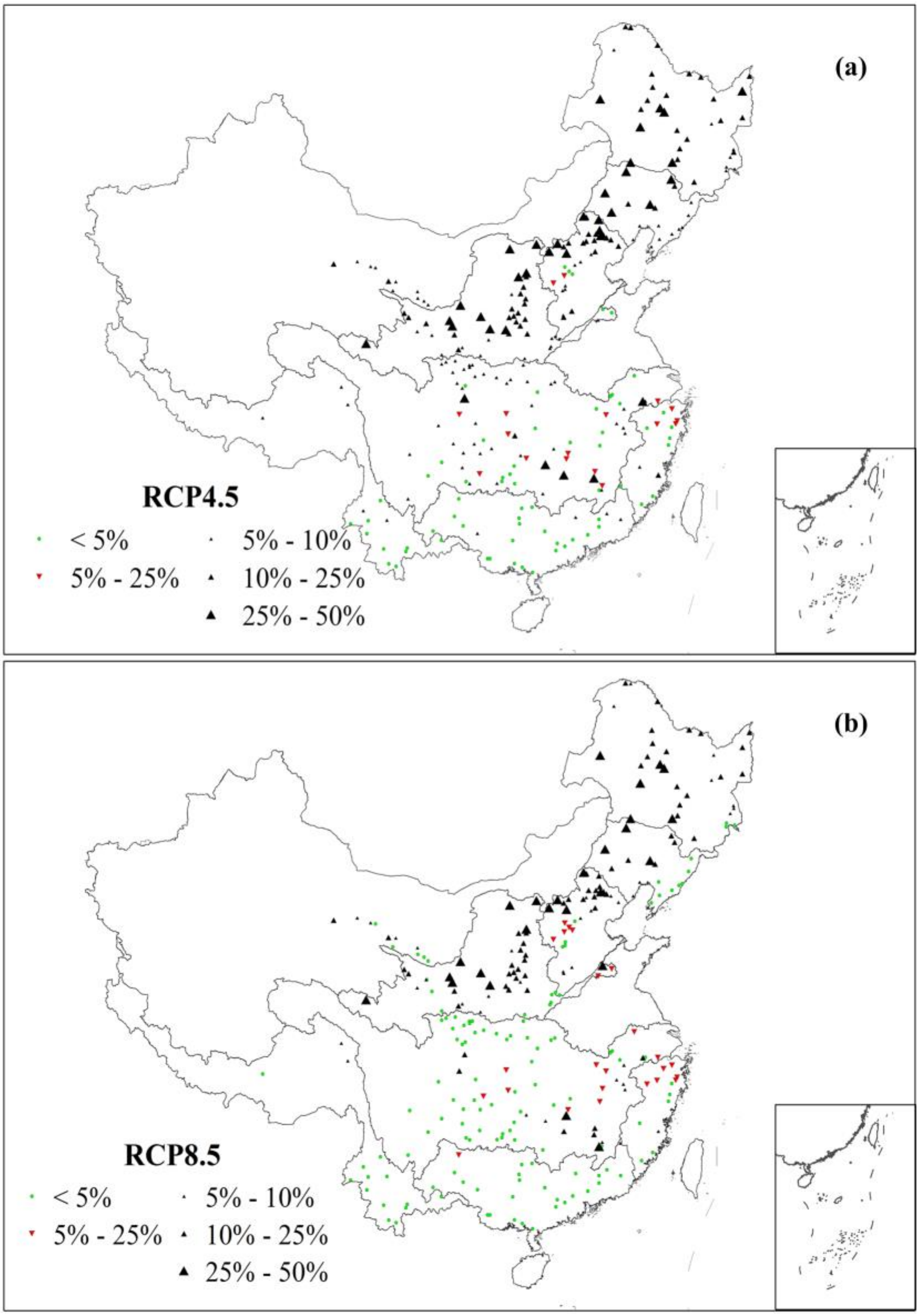

Fig.9 Contribution of snow ratio variance to change in mean annual runoff under projected future climate. (a: RCP4.5; b: RCP8.5).

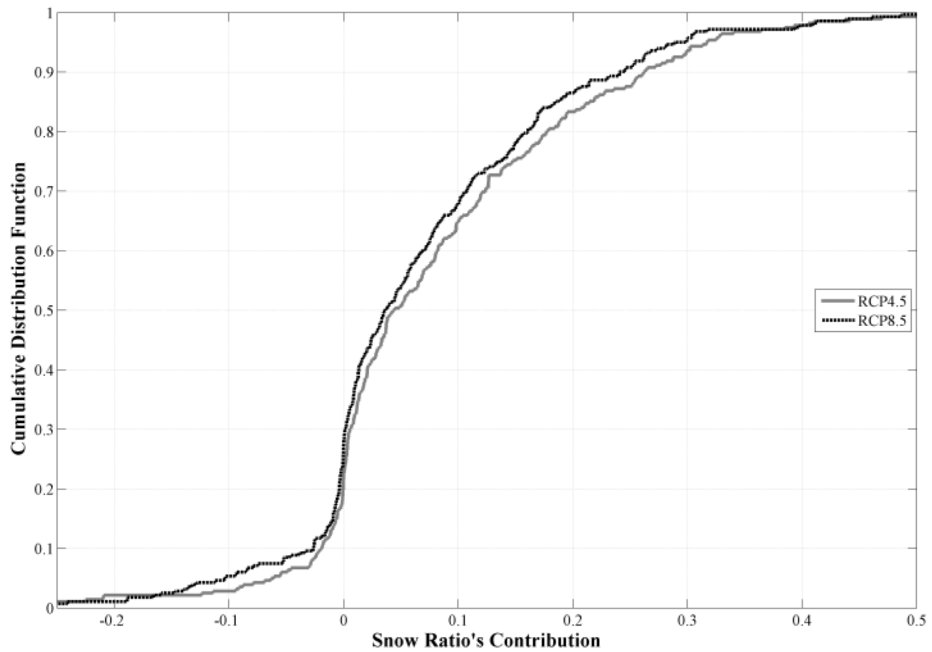

Fig.10 Cumulative distribution function of snow ratio's contribution to runoff change under projected future climate.

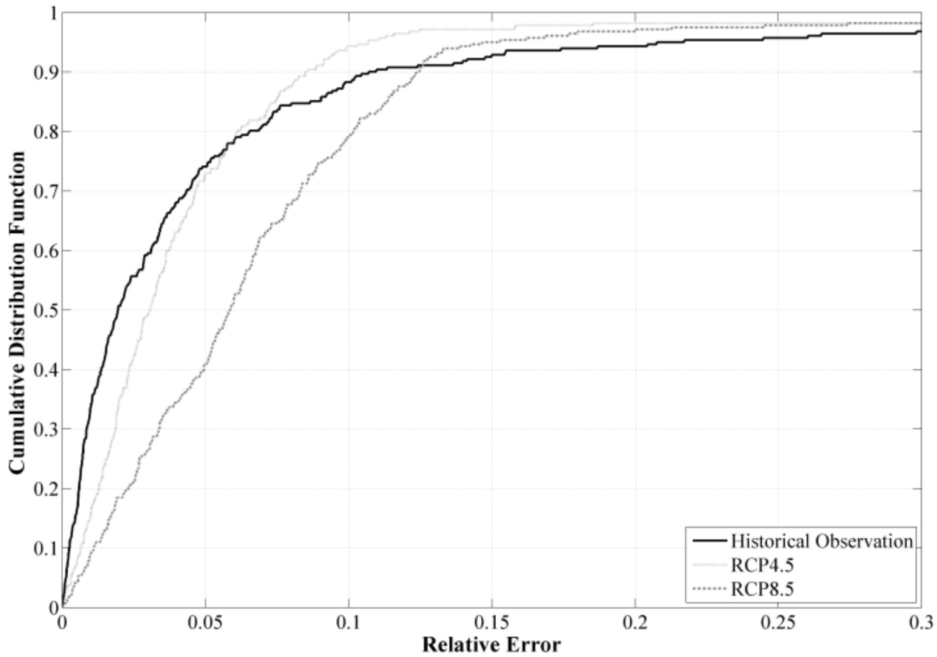

Fig.11 Cumulative distribution function of the relative error of attribution method in three cases.