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**Efficient pricing
policy definition with
stochastic
programming**

H. Macian-Sorribes et al.

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Definition of efficient scarcity-based water pricing policies through stochastic programming

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Abstract

Finding ways to improve the efficiency in water usage is one of the most important challenges in integrated water resources management. One of the most promising solutions is the use of scarcity-based pricing policies. This contribution presents a procedure to design efficient pricing policies based on the opportunity cost of water at the basin scale. Time series of the marginal value of water are obtained using a stochastic hydro-economic model. Those series are then post-processed to define step pricing policies, which depend on the state of the system at each time step. The case study of the Mijares river basin system (Spain) is used to illustrate the method. The results show that the application of scarcity-based pricing policies increases the economic efficiency of water use in the basin, allocating water to the highest-value uses and generating an incentive for water conservation during the scarcity periods. The resulting benefits are close to those obtained with the economically optimal decisions.

1 Introduction

One of the main challenges on integrated water resources management (IWRM) is improving the efficiency in water usage while balancing it with equity. Given that the building of new water supply systems has well-passed its zenith, water management strategies are now devoted to achieve better operating policies. Several criteria can be considered when designing a policy for water allocation: flexibility in the allocation, security of tenure for the users, real cost recovery, predictability of its performance, fairness and acceptability (Dinar et al., 2007). Each system has a unique configuration and, in consequence, a unique combination of factors that lead to an adequate management policy.

There are four major water allocation mechanisms: public water allocation, water markets, user-based allocation and marginal cost pricing. Public water allocation provides an adequate treatment of water as a public good, allows the development of

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Similarly, for a given location L and time t , the benefit B_t achieved by a change in its state $s_{L,t}$ (water availability) from x_1 to x_2 can be calculated integrating the marginal water value (or MROC) function:

$$B_t = \int_{x_1}^{x_2} \text{MROC}_{L,t}(s_{L,t}) ds \quad (2)$$

The MROC can be defined as the derivative of the benefit function with respect to the system state. Therefore, if the MROC integration obtains the systemwide benefits, the MROC can be calculated as:

$$\text{MROC}_{L,t} = \frac{dB_t(s_{L,t})}{ds} \quad (3)$$

The MROC value for a specific location and time can be estimated: (1) under a simulation approach, as the benefits obtained by an increase of one unit in the available resource at that location and time (Pulido-Velazquez et al., 2008, 2013); and (2) under an optimization approach, as the shadow value, dual variable or Lagrange multiplier associated to the mass-balance equation at the desired place and the specified time (Pulido-Velazquez et al., 2008, 2013; Tilmant et al., 2008).

2.2 MROC assessment through stochastic programming

Stochastic programming (SP) procedures are powerful and useful methodologies to derive optimal management of water systems with uncertain inputs (Tejada-Guibert et al., 1993). Various SP algorithms are available. Among them, Stochastic Dynamic Programming (SDP) has been widely used in water resources management because: (1) it is able to handle non-linearities in the objective function in an efficient way; (2) the inflow uncertainty representation is clear and simple; and (3) it treats the decision-making process sequentially, as done in real-life operation (Labadie, 2004). The SDP

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algorithm solves the Bellman's recursive equation as follows:

$$F_t(\mathbf{S}_t, \mathbf{Q}_t) = \max_{D_t} \left[B_t(\mathbf{S}_t, \mathbf{Q}_t, D_t) + E_{Q_{t+1}|Q_t} \{F_{t+1}(\mathbf{S}_{t+1}, \mathbf{Q}_{t+1})\} \right] \quad (4)$$

where F_t is the total benefit function; \mathbf{S}_t the current (time t) system state vector; \mathbf{Q}_t current inflow vector; D_t decision made at time step t ; B_t immediate benefit function; $E_{Q_{t+1}|Q_t}$ expectation operator between the current and future inflows; and F_{t+1} future benefit function or benefit-to-go function.

In the SDP method, the state variables \mathbf{S}_t and \mathbf{Q}_t are discretized over all the state space forming a grid, allowing only transitions between grid points. The expectation operator is then defined by using a Markov chain that relates the current hydrological state \mathbf{Q}_t with all the possible future states \mathbf{Q}_{t+1} through a set of transition probabilities.

With the application of the previously showed equation, the optimal policies $D_t(\mathbf{S}_t, \mathbf{Q}_t)$, and benefit-to-go function $F_t(\mathbf{S}_t, \mathbf{Q}_t)$ are calculated at the grid points. Then, interpolation methodologies can be applied to obtain the optimal policies $D_t^*(\mathbf{S}_t, \mathbf{Q}_t)$ and the optimal benefits $F_t^*(\mathbf{S}_t, \mathbf{Q}_t)$ over the entire state-space. An alternative is to use a reoptimization approach as in Tejada-Guibert et al. (1993). With this approach, the Bellman function is implemented forward with the SDP-derived benefit-to-go functions as inputs.

$$F_t(\mathbf{S}_t, \mathbf{Q}_t) = \max_{D_t} \left[B_t(\mathbf{S}_t, \mathbf{Q}_t, D_t) + \sum_q \{p_{p,q}^t \cdot F_{t+1}^*(\mathbf{S}_{t+1}, \mathbf{Q}_{t+1})\} \right] \quad (5)$$

Where \mathbf{S}_t and \mathbf{Q}_t are the simulated system state (storage) and inflows at stage t ; and $p_{p,q}^t$ is the transition probability (Markov Chain) between inflow class p at time stage t and inflow class q at time stage $t+1$. The \mathbf{S}_{t+1} and \mathbf{Q}_t values are not subjected to a discrete grid. The reoptimization provides time series of allocation decisions and the corresponding λ values associated to the system's nodes, which correspond to the MROC.

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ing the results in the form of state-MROC steps. To sum up, the method presented in this paper can be divided in the following steps:

1. Definition of the main pricing policy features
2. Development of a hydro-economic stochastic programming model of the system
- 5 3. Determination of MROC (marginal water values or λ -values) time series at the reference nodes (e.g. main reservoirs)
4. Aggregation/disaggregation of previous MROC time series to calculate the combined MROC time series
- 10 5. Development of a statistical analysis over the final MROC time series to obtain their cumulative probability distribution
6. Building of k steps by:
 - (a) Choose k different cumulative probability MROC values (characteristic values)
 - (b) Sort according to the MROC values the system state values obtained in the stochastic programming run
 - 15 (c) Obtain, for each characteristic MROC value, the system states associated to it
 - (d) Summarize all the possible state values associated to each MROC value in the form of steps
- 20 7. Definition of several step pricing policies based on the obtained steps

Pricing policies can be simulated to assess their performance and to compare them to SDP-derived policies. In case the pricing policies' performance is found to be inadequate, the process must be restarted: the pricing policies' features are reassessed and the build-up and analysis stages must be redone.

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2.4 Case study: Mijares river basin (Spain)

The Mijares river basin is located in eastern Spain (Fig. 2). It is characterized by the existence of several relevant water springs in its headwater (Mas Royo and Babor); the implementation of conjunctive use water strategies to improve water management (Andreu and Sahuquillo, 1987); and the existence of an allocation framework accepted by all the users (SCRM, 1974). Regulated by the Arenós (93 Mm³) and Schar (49 Mm³) reservoirs, surface water is mostly devoted to agricultural purposes (mainly orange trees), with groundwater as complementary or substitutive resource; while urban demands are entirely supplied using groundwater. There are 10.499 ha irrigated exclusively by surface water and 11.622 ha irrigated by surface and groundwater.

The Mijares river simplified flow network is showed in Fig. 3. Although groundwater supply is significant in the lower basin (Plana de Castellon aquifer), it has not been explicitly represented in the optimization model, as there is not hydraulic connection between the river and the aquifer (disconnected aquifer). Upstream, stream-aquifer interaction is implicit in the inflow (discharge) time series. Seepage equations are also added in certain lower reaches of the river. Consequently, the all-groundwater supplied demands have not been considered, and the mixed-supplied demands have been reduced an amount equivalent to its groundwater supply. The characteristics of each element are showed in Table 1.

Current water management agreements give priority to the supply to the Traditional Irrigation District (ID), which has been using water since the 13th century, over the remaining IDs (established in mid 20th century). In year 1970, before the construction of the Arenós dam (with public funding), an agreement was signed between users to regulate the use of the Schar reservoir (funded by the Traditional ID) (SCRM, 1974). That agreement established a monthly storage limit for the Schar reservoir below which only the Traditional ID can be supplied (see Fig. 4). That agreement has continued to be applied after the construction of the Arenós reservoir, but referred to the total system storage (Arenós and Schar).

The plots show the same values during most of the historical time series. The slight differences between them found in certain time stages correspond to the opportunity cost of the CC220 ID delivery. Water values increase between 1977 and 1986, period that corresponds to the largest drought suffered by the Mijares river basin. The average MROC value is equal to EUR 0.15 m⁻³, ranging from 0 to EUR 0.68 m⁻³.

3.2 Pricing policies in the Mijares river basin

Regarding the aggregation/disaggregation of the MROC time series at Arenós and Schar reservoirs, the pricing policy used was defined at basinwide scale. This decision has been made considering the proximity of the intakes for the demands and the possibility of releasing water from the two reservoirs to satisfy almost all of them. The chosen temporal scale for the pricing policy was annual, with the same pricing policy for all the months. For simplicity, the state variable for defining the pricing schedule was the sum of the storage in Arenós and Schar reservoirs, without considering the corresponding monthly inflow. That departs from the SDP formulation, but it is consistent with the current management policies, based exclusively on storages. The aggregation operation driven by these features was simply a non-weighted average of the MROC values at Arenós and Schar reservoirs, as the MROC values are almost coincident for both reservoirs.

Figure 6 shows the MROC cumulative probability distribution. To establish pricing policies, we sampled the 5 (EUR 0 m⁻³), 25 (EUR 0.06 m⁻³), 50 (EUR 0.13 m⁻³), 75 (EUR 0.24 m⁻³) and 95 (EUR 0.51 m⁻³) percentiles. The MROC-storage pairs were then organized in intervals (as depicted in Fig. 7). Each interval or step represents the range of storage values associated to that MROC.

Those steps were used to define the pricing policies. Firstly, the storage space was divided into intervals of 25 Mm³. A price was then defined for each interval as either the minimum or the maximum or the average over the MROC values associated to the steps found within the interval. As a result, a set of 15 pricing policies was obtained. Figure 7 shows some of them, corresponding to policies regarding maximum between

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of the supply costs (O and M and capital charges) and the environmental externalities have to be added (Rogers et al., 2002). Final pricing policies require estimating all those components and combining them with the results obtained with this methodology.

To gain social acceptability and policy equity, mechanisms of financial compensation can be implemented (e.g., Tilmant et al., 2009). Additional financial resources generated could be them be employed to compensate the users, or to develop adequate infrastructure to increase water security (for example, by financing desalination plant that reduce water scarcity). The main objective in the design of the pricing policies discussed here focuses on the use of water prices as economic instrument for an efficient management of the interaction between supply and demand. The role of pricing for cost-recovery of water services (pricing as financial instruments) will require a complementary analysis.

Regarding the established methodology and the case study, several conclusions can be drawn:

1. Stochastic programming is a useful tool for estimating optimal policies and MROC time series under hydrological uncertainty. These time series capture and summarize the overall performance of the optimization policies, and can be therefore used to assess pricing policies able to be applied at the basin scale.
2. Pricing policies defined using MROC data series, after statistical analysis and step building, are adequate to enhance system's global economic efficiency. They establish a univocal relationship between the system state (storages and inflows), and a water price based on the marginal value of water in a reservoir, linking the price concept to the MROC one.
3. It can be used to define pricing policies either under general conditions or drought events.
4. Participatory framework processes are needed to define the features and characteristics that the desired pricing policies should have, as they condition the MROC

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- Macian-Sorribes, H.: Utilización de Lógica Difusa en la Gestión de Embalses, Master Thesis dissertation, Universitat Politècnica de València, Valencia, Spain, 2012 (in Spanish). 783
- Macian-Sorribes, H. and Pulido-Velazquez, M.: Hydro-economic optimization under inflow uncertainty using the SDP-GAMS generalized tool, in: Evolving Water Resources Systems: Understanding, Predicting and Managing Water-Society Interactions, IAHS Press, Wallingford, UK, 410–415, 2014. 781
- Massarutto, A.: El precio de agua: herramienta básica para una política sostenible del agua?, Ingeniería del Agua, 10, 293–326, 2003 (in Spanish).
- Meinzen-Dick, R. and Mendoza, M.: Alternative water allocation mechanisms indian and international experiences, Econ. Polit. Weekly, 31, A25–A30, 1996. 773
- Mousavi, J. J., Ponnambalam, K., and Karray, F.: Reservoir operation using a dynamic programming fuzzy rule-based approach, Water Resour. Manag., 19, 655–672, 2005.
- Nandalal, K. D. W. and Bogardi, J. J.: Dynamic Programming Based Operation of Reservoirs: Applicability and Limits, Cambridge University Press, Cambridge, UK, 144 pp., 2007.
- Pulido-Velazquez, M., Jenkins, M., and Lund, J. R.: Economic values for conjunctive use and water banking in southern California, Water Resour. Res., 40, W03401, doi:10.1029/2003WR002626, 2004.
- Pulido-Velazquez, M., Andreu, J., Sahuquillo, A., and Pulido-Velazquez, D.: Hydro-economic river basin modelling: the application of a holistic surface-groundwater model to assess opportunity costs of water use in Spain, Ecol. Econ., 66, 51–65, 2008. 774, 776
- Pulido-Velazquez, M., Alvarez-Mendiola, E., and Andreu, J.: Design of efficient water pricing policies integrating basinwide resource opportunity costs, J. Water Res. Pl.-ASCE, 139, 583–592, 2013. 774, 776, 784
- Riegels, N., Pulido-Velazquez, M., Doulgeris, C., Sturm, V., Jensen, R., Moller, F., and Bauer-Gottwein, P.: Systems analysis approach to the design of efficient water pricing policies under the EU Water Framework Directive, J. Water Res. Pl.-ASCE, 139, 574–582, 2013. 774
- Rogers, P., de Silva, R., and Bhatia, R.: Water is an economic good: How to use prices to promote equity, efficiency and sustainability, Water Policy, 4, 1–17, 2002. 774, 785
- SCRM: Convenio de Bases para la Ordenación de las Aguas del río Mijares, Ministerio de Obras Públicas, Transportes y Medio Ambiente, Confederación Hidrográfica del Júcar, Valencia, Spain, 50 pp., 1974 (in Spanish). 780
- Stedinger, J. R., Sule, B. F., and Loucks, D. P.: Stochastic dynamic programming models for reservoir operation optimization, Water Resour. Res., 20, 1499–1505, 1984.

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Tejada-Guibert, J. A., Johnson, S. A., Stedinger, J. R.: Comparison of two approaches for implementing multireservoir operating policies derived using stochastic dynamic programming, *Water Resour. Res.*, 29, 3969–3980, 1993. 776, 777

Tilmant, A. and Kelman, R.: A stochastic approach to analyze trade-offs and risks associated with large-scale water resources systems, *Water Resour. Res.*, 43, W06425, doi:10.1029/2006WR005094, 2007.

Tilmant, A., Pinte, D., and Goor, Q.: Assessing marginal water values in multipurpose multireservoir systems via stochastic programming, *Water Resour. Res.*, 44, W12431, doi:10.1029/2008WR007024, 2008. 774, 776

Tilmant, A., Goor, Q., and Pinte, D.: Agricultural-to-hydropower water transfers: sharing water and benefits in hydropower-irrigation systems, *Hydrol. Earth Syst. Sci.*, 13, 1091–1101, doi:10.5194/hess-13-1091-2009, 2009. 785

Tilmant, A., Arjoon, D., and Fernandes Marques, G.: Economic value of storage in multireservoir systems, *J. Water Res. Pl.-ASCE*, 140, 375–383, 2014. 774

U.S. Army Corps of Engineers (USACE) Hydrologic Engineering Center (HEC): Developing Seasonal and Long-Term Reservoir System Operation Plans Using HEC-PRM, U.S. Army Corps of Engineers, Hydrologic Engineering Center, Davis, California, USA, 1996.

Ward, F. and Pulido-Velazquez, M.: Efficiency, equity and sustainability in a water quantity-quality optimization model in the Rio Grande basin, *Ecol. Econ.*, 66, 23–37, 2008. 774

Wurbs, R. A.: Reservoir-system simulation and optimization models, *J. Water Res. Pl.-ASCE*, 119, 455–472, 1993.

Young, R. A.: Water economics, in: *Water Resources Handbook*, McGraw-Hill, New York, NY, USA, 3.1–3.57, 1996.

Young, R. A.: *Determining the Economic Value of Water: Concepts and Methods*, RFF Press, Washintong D.C., USA, 375 pp., 2005. 774

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Element	Characteristic value
Arenós reservoir	93 Mm ³ capacity
Sichar reservoir	49 Mm ³ capacity
Upper Basin inflow	138 Mm ³ annual discharge
Middle Basin inflow	55 Mm ³ annual discharge
Traditional Irrigation District	83.5 Mm ³ annual demand
MC Canal Irrigation District	7.6 Mm ³ annual demand
CC100 Canal Irrigation District	16.3 Mm ³ annual demand
CC220 Canal Irrigation District	11.9 Mm ³ annual demand
Minimum flow downstream Sichar	0.2 Mm ³ annual requirement

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Table 2. Benefits for the 1940–2009 and 1977–1986 periods with stochastic optimization (SDP), current management rules and pricing policies.

Simulation	Traditional M EUR	MC M EUR	CC100 M EUR	CC220 M EUR	Total M EUR
1940–2009 Benefits per demand and total					
SDP	44.49	4.14	8.56	6.56	63.75
Current policies	46.31	3.60	7.42	5.73	63.06
Pricing policy 10	44.99	4.06	8.29	6.47	63.81
Pricing policy 11	45.00	4.05	8.29	6.46	63.81
Pricing policy 12	45.05	4.04	8.27	6.44	63.81
1977–1986 Benefits per demand and total					
SDP	35.97	3.22	6.80	5.07	51.05
Current policies	42.05	1.69	3.52	2.68	49.93
Pricing policy 4	37.11	3.06	6.09	4.86	51.12
Pricing policy 5	37.11	3.06	6.09	4.86	51.12

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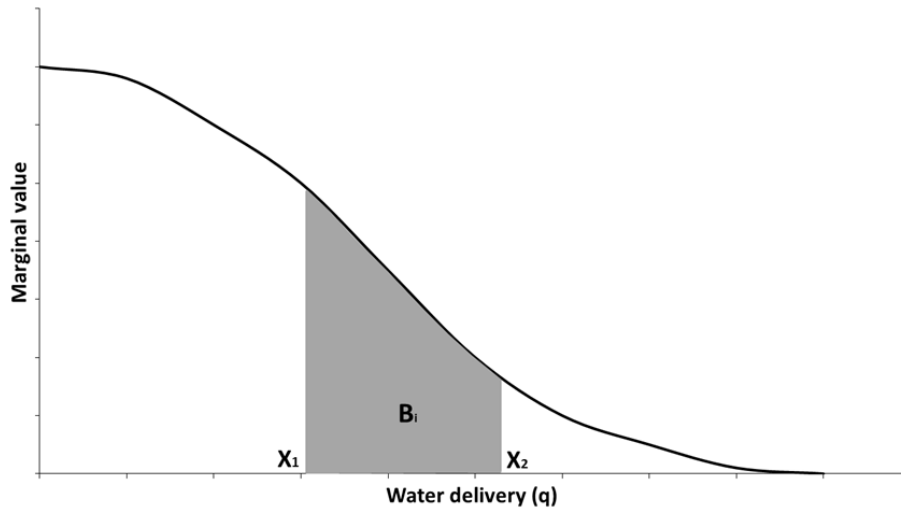


Figure 1. Benefits from an increase of water delivery from x_1 to x_2 .

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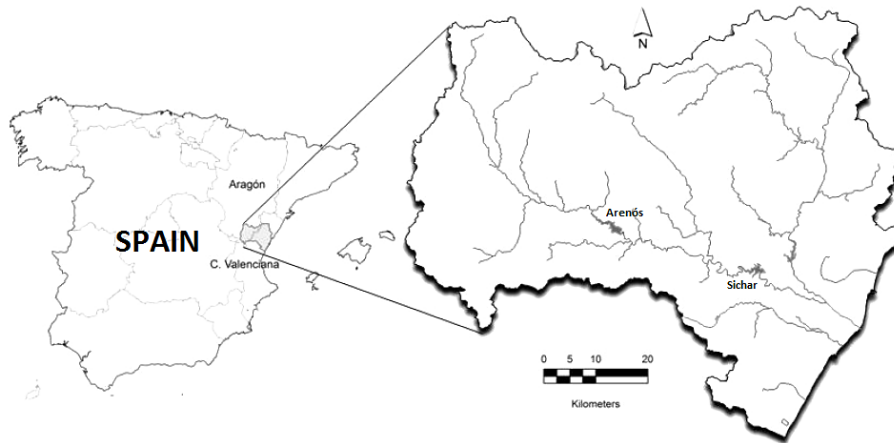


Figure 2. Mijares river basin location (Eastern Spain).

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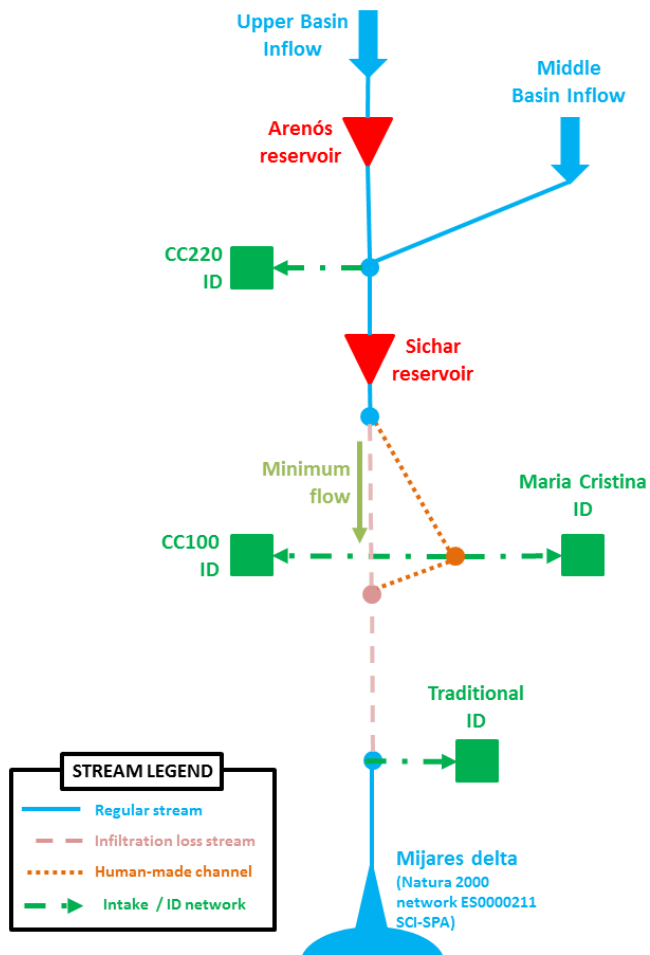


Figure 3. Mijares river network schematic.

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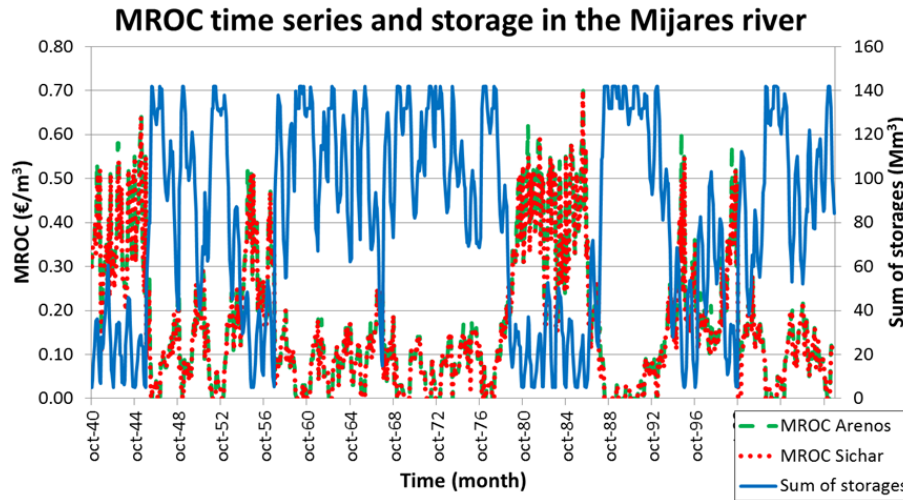


Figure 5. MROC time series and storages in the Mijares river.

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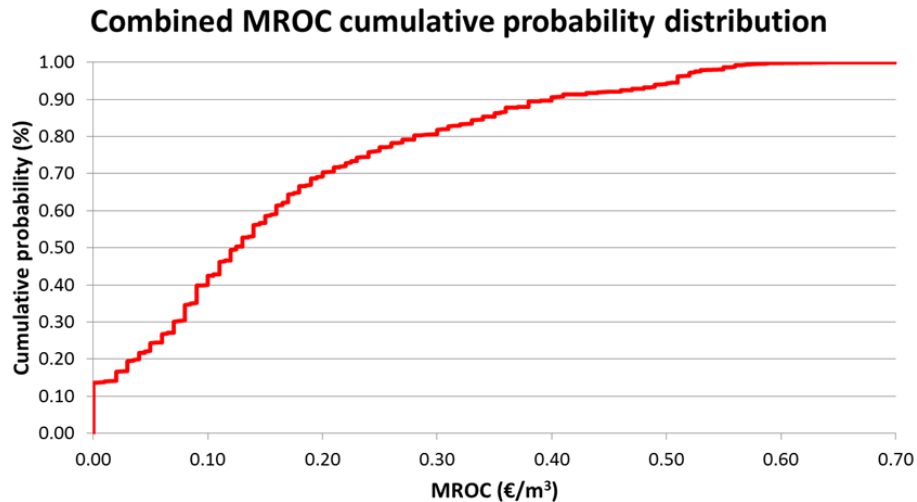


Figure 6. Combined MROC cumulative probability distribution.

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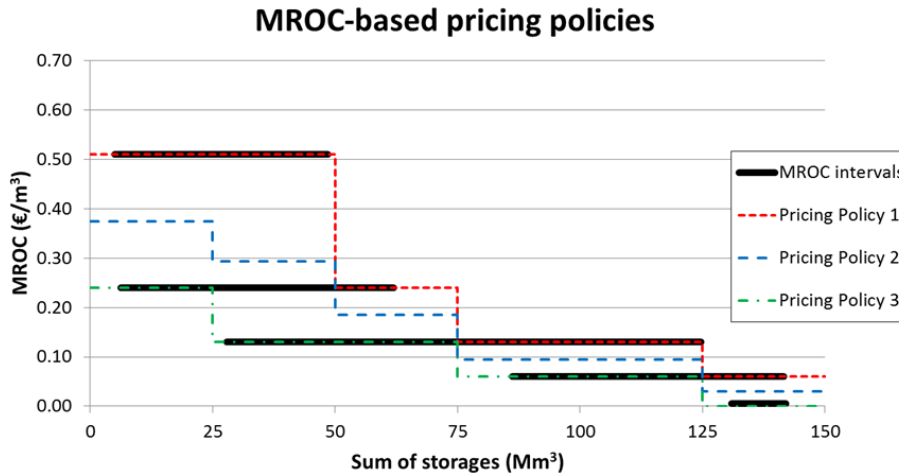


Figure 7. MROC-based pricing policies.

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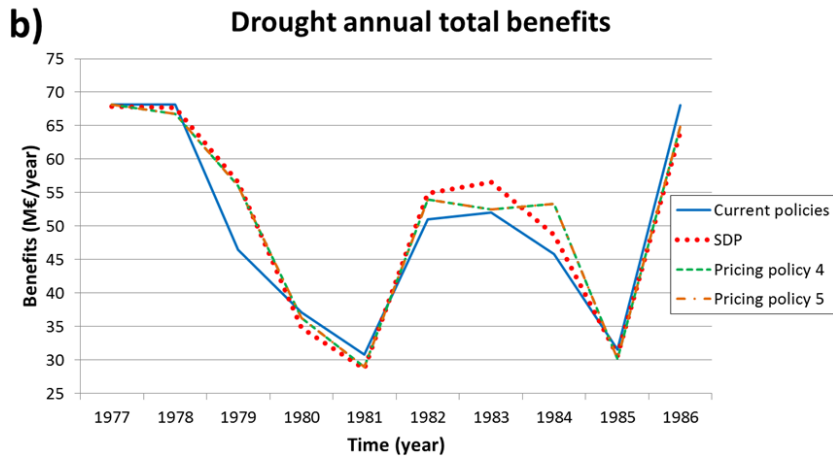
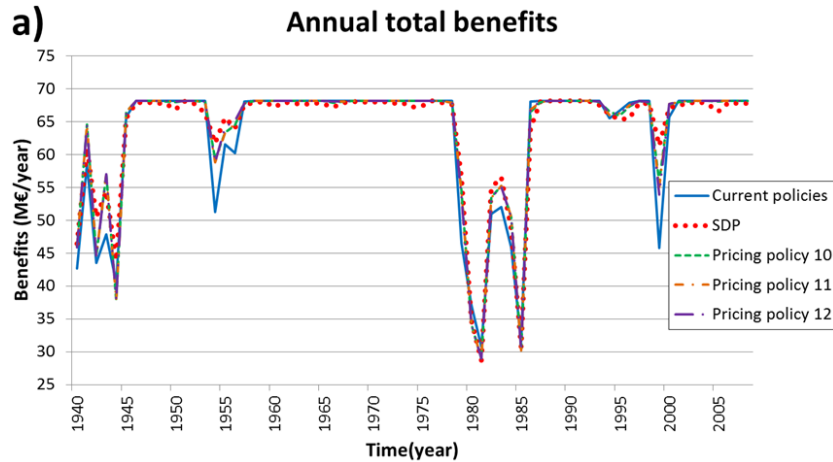


Figure 8. Annual total benefits comparison for the 1940–2009 period (a) and for the 1977–1986 drought (b).

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