

1 **Estimating evaporation with thermal UAV data and two**  
2 **source energy balance models.**

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11

12 **Abstract**

13 Estimating evaporation is important when managing water resources and cultivating crops.  
14 Evaporation can be estimated using land surface heat flux models and remotely sensed land  
15 surface temperatures (LST), which have recently become obtainable in very high resolution  
16 using light weight thermal cameras and Unmanned Aerial Vehicles (UAVs). In this study a  
17 thermal camera was mounted on a UAV and applied into the field of heat fluxes and  
18 hydrology by concatenating thermal images into mosaics of LST and using these as input for  
19 the two source energy balance modelling scheme (TSEB). Thermal images are obtained with  
20 a fixed-wing UAV overflying a barley field in western Denmark during the growing season of  
21 2014 and a spatial resolution of 0.20 m is obtained in final LST-mosaics. Two models are  
22 used: the original TSEB model (TSEB-PT) and a dual-temperature-difference model (DTD).  
23 In contrast to the TSEB-PT model, the DTD model account for the bias that is likely present  
24 in remotely sensed LST. TSEB-PT and DTD have already been well tested, however only  
25 during sunny weather conditions and with satellite images serving as thermal input. The aim  
26 of this study is to assess whether a lightweight thermal camera mounted on a UAV is able to  
27 provide data of sufficient quality to constitute as model input and thus attain accurate and

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1 high spatial and temporal resolution surface energy heat fluxes, with special focus on latent  
2 heat flux (evaporation). Furthermore, this study evaluates the performance of the two source  
3 energy balance scheme during cloudy and overcast weather conditions, which is feasible due  
4 to the low data retrieval altitude (due to low UAV flying altitude) compared to satellite  
5 thermal data that are only available during clear sky conditions. TSEB-PT and DTD fluxes  
6 are compared and validated against eddy covariance measurements and the comparison show  
7 that both TSEB-PT and DTD simulations are in good agreement with eddy covariance  
8 measurements with DTD obtaining the best results. The DTD model provides results  
9 comparable to studies estimating evaporation with similar experimental setups, but with LST  
10 retrieved from satellites instead of a UAV. Further, systematic irrigation patterns on the  
11 barley field provide confidence to the veracity of the spatially distributed evaporation  
12 revealed by model output maps. Lastly, this study outlines and discusses the thermal UAV  
13 image processing that result in mosaics suited for model input. This study shows that the  
14 UAV platform and the lightweight thermal camera provide high spatial and temporal  
15 resolution data valid for model input and for other potential applications requiring high  
16 resolution and consistent LST.

17

## 18 **1 Introduction**

19 Evaporation (latent heat flux) serves as a key component in both hydrological and land-  
20 surface energy processes. However, it is often estimated indirectly because spatially  
21 distributed, physical measurements of evaporated water are cumbersome. Provided  
22 information on net solar radiation ( $R_n$ ), sensible- ( $H$ ) and soil heat flux ( $G$ ), the latent heat flux  
23 (LE) can be estimated as a residual using the assumption of surface energy balance in cases  
24 with no significant heat advection:

$$25 \quad R_n = H + LE + G \quad (1)$$

26 All terms in the above equation are related to the land surface temperature (LST). Since the  
27 1980s estimates of evaporation have been obtained through remotely sensed LST and  
28 advanced land surface heat flux models accounting for vegetation, soil and atmospheric  
29 conditions (Anderson et al., 1997; Kalma et al., 2008) and a large number of heat flux models  
30 exist with significant variations in physical system conceptualisation and input requirements  
31 (Boulet et al., 2012; Kustas and Norman, 1996; Stisen et al., 2008). Norman et al. (1995)  
32 applied the two source energy balance model (TSEB) (Shuttleworth and Wallace, 1985) to

1 remotely sensed data and this modelling scheme has proven to estimate reliable surface heat  
2 fluxes over cropland, rangeland and forest at various spatial scales (Anderson et al., 2004;  
3 Norman et al., 2003). The TSEB modelling scheme generates robust estimates of surface heat  
4 fluxes despite a simple solution scheme demanding relatively few input data. It was  
5 developed to be operational using thermal satellite images (Anderson et al., 2011) which  
6 serves as a key boundary condition in simulations. The TSEB modelling scheme partitions the  
7 remotely sensed LST into two layers; a canopy temperature and a soil temperature, using the  
8 Priestley-Taylor approximation (Norman et al., 2000). This enables a partition of heat flux  
9 estimations into its components from canopy and soil respectively. This approach is hereafter  
10 referred to as TSEB-PT in order to differentiate it from other TSEB approaches, such as  
11 TSEB-LUE (Houborg et al., 2012), based on the Light Use Efficiency concept, or TSEB-  
12 2ART, which utilizes dual angle LST observations for direct retrieval of soil and canopy  
13 temperatures (Guzinski et al., 2015).

14 Remotely sensed LST may deviate from the actual surface temperature by several degrees  
15 Kelvin due to atmospheric and surface emissivity effects. Consequently thermal-based models  
16 utilizing remotely sensed LST that do not address this issue are prone to producing less  
17 accurate results. Trying to overcome this issue, Norman et al. (2000) developed the Dual-  
18 Temperature-Difference model (DTD) by incorporating two temperature observations into the  
19 TSEB modelling scheme; one conducted an hour after sunrise and another conducted later the  
20 same day when flux estimations are desired. One hour after sunrise, the surface heat fluxes are  
21 neglectable and observations acquired at this time represent a ‘starting point’ for the  
22 temperatures collected later the same day. For agricultural and some hydrological purposes,  
23 there is a shortcoming in spatial and temporal resolution of satellite observations (Guzinski et  
24 al., 2014). This is especially true in areas where overcast weather conditions often occur, such  
25 as in northern Europe where the present study is conducted, as satellite thermal infrared and  
26 visible observations cannot penetrate clouds (Guzinski et al., 2013). Unmanned aerial vehicles  
27 (UAVs) (or Remotely Piloted Aircraft System, RPAS, in its most recent terminology) enable  
28 a critical improvement for spatial and temporal resolution of remotely sensed data. UAVs can  
29 operate at any specific time of day and year provided that strong wind and rainfall are absent.  
30 The relative low flying height enable both data collection during overcast conditions (Hunt Jr  
31 et al., 2005) and data with higher spatial resolution than what can be obtained from satellite  
32 data. Here we hypothesis that UAV data can substitute satellite images and in combination  
33 with the presented heat flux models, can be used to generate spatially detailed heat flux maps

1 that provide insight to different evaporation rates and plant stress at decimeter scale. There is  
2 rapidly growing interest in the potential of data collection with UAVs, particularly in the  
3 science of precision agriculture but also in a range of different scientific and commercial  
4 communities (Díaz-Varela et al., 2015; Gonzalez-Dugo et al., 2014; Swain et al., 2010;  
5 Zarco-Tejada et al., 2013, 2014). As scientists strive to understand the potential of UAVs and  
6 the new applications to which they are suited, the development of efficient workflows,  
7 operational systems and improved software that capture and process UAV data are continuing  
8 (Harwin and Lucieer, 2012; Lucieer et al., 2014; Turner et al., 2012; Wallace et al., 2012).  
9 However, research in possibilities and limitations of UAV platforms is still at an early stage  
10 and the present paper introduces the usage of UAV platforms into the fields of heat fluxes and  
11 hydrology.

12 In this study, surface energy balance components are estimated using LST retrieved with a  
13 UAV and used as input for the physically-based, two source energy balance models: TSEB-  
14 PT and DTD. The aim is to assess whether a lightweight thermal camera installed on board a  
15 UAV is able to provide data of sufficient quality to attain high spatial and temporal resolution  
16 surface energy heat fluxes. Besides facilitating high resolution LST, the UAV platform enable  
17 the application of TSEB-PT and DTD models in cloudy and overcast weather conditions.  
18 Model outputs are quantitatively validated with data from an eddy covariance system located  
19 at the same barley field over which the UAV flights were conducted and known irrigation  
20 patterns provide confidence to the spatially distributed evaporation variations revealed within  
21 the barley field. Additionally, this study outline thermal UAV image processing which result  
22 in mosaics suited for model input.

23

## 24 **2 Materials and methods**

### 25 **2.1 Site**

26 The TSEB models are applied in the HOBE (Hydrological OBsErvatory) agricultural site  
27 within the Skjern River catchment, western Denmark, see Fig. 1. The 400 x 400 m site is  
28 located in the maritime climate zone where mild winters and cold summers result in a mean  
29 annual temperature of 8.2°C and a mean annual precipitation of 990 mm. The prevailing  
30 winds are westerly and windy conditions are common; with 30% of wind in 2014 coming  
31 from westerly direction and an average wind speed of 3.8 ms<sup>-1</sup>. Cloudy and overcast weather

1 conditions are frequent with 1727 hours of sunshine in 2014, which is 16% above normal  
2 (Cappelen, 2015). The site was cultivated with barley during UAV campaigns. The soil  
3 profile consists of an upper 0.25 m plow layer of homogeneous sandy loam soil and a lower  
4 layer of coarse sand. Soil porosity of the upper and lower layer range between 0.35 and 0.40  
5 and soil moisture content at field capacity is 26%. The ability of the sandy material to retain  
6 water is limited and frequent irrigation is necessary to maintain crop growth during growing  
7 seasons (Ringgaard et al., 2011). The overall area is somewhat heterogeneous consisting of  
8 three barley fields separated by a gravel road to the south and a row of conifers to the west.  
9 Conifers are bordering the barley fields at several places. A meteorological tower with an  
10 eddy covariance system consisting of a Gill R3-50 sonic anemometer and a LI-7500 open  
11 path infrared gas analyser, is located in the middle of the site (black square in Fig. 1).  
12 Meteorological data used as input to the models and as heat flux-validation are measured at  
13 this tower.

## 14 **2.2 UAV campaign**

15 UAV data was collected on seven days distributed evenly during spring and summer 2014  
16 (Table 1). In total 19 flights were conducted, of which 7 were flown early in the morning,  
17 constituting the additional input data for the DTD model. The entire airborne campaign thus  
18 resulted in 12 sets of input data for the TSEB-PT and DTD model. Dates with (c) in Table 1  
19 mark days where the UAV flights were conducted in cloudy or overcast conditions.

20 A fixed-wing UAV (Q300, QuestUAV, UK) with a wingspan of 2.2 m was used as platform  
21 for the airborne operations. It was able to carry a payload of 2 kg for approximately 25 min in  
22 the air. With a speed of 60 km h<sup>-1</sup> and flying height of 90 m above ground, the 400×400 m site  
23 area was covered in a single flight. The UAV was controlled by the SkyCircuits Ltd SC2  
24 autopilot in a dual redundant system with separate laptop and transmitter control.  
25 Communication between autopilot and ground was performed by a radio link that transmits  
26 position and attitude. Landing was conducted manually using the transmitter. SkyCircuits  
27 Ground Control Station software was used for generating the flight route and for visual  
28 inspection of the UAV, while it was in the air.

## 1 **2.3 Thermal data and image processing**

2 An Optris PI 450 LightWeight infrared camera of 380 g was mounted on the UAV. The  
3 camera detects infrared energy in the 7.5-13  $\mu\text{m}$  thermal spectrum and surface temperatures  
4 were computed automatically using a fixed emissivity of unity. Thermal images were stored  
5 at 16 bit radiometric resolution. According to manufacturer specifications, the system has an  
6 accuracy of  $\pm 2^\circ\text{C}$  or  $\pm 2\%$  at an ambient temperature of  $23\pm 5^\circ\text{C}$ . The thermal detector  
7 within the camera collects an image array of  $382\times 288$  pixels with a nadir viewing footprint of  
8  $50\times 40$  m per image at 90 m flying height, resulting in an effective ground resolution of  
9 approx. 0.13 m per pixel.

10 Time synchronization between camera and autopilot was necessary in order to link the logged  
11 GPS and rotation position with each image. This was performed before launching the UAV  
12 with a USB GPS connected to the camera thus synchronizing the timestamp on each image  
13 with the GPS clock. Timestamps were recorded in UTC time and accurate to within 1 second.  
14 Re-calculation of camera position was therefore necessary and performed using a self-  
15 calibrating bundle adjustment in Agisoft PhotoScan software (Professional Edition version  
16 1.0.4). No ground control points were used, nor needed, during camera alignment and bundle  
17 adjustment. Images were converted into unsigned 16 bit data to enable processing in  
18 Photoscan.

19 Between 700 and 1000 images were collected for each flight with camera recording in  
20 continuous mode, triggering an image every second. Generally half of the images were  
21 suitable for further processing. Non-suitable images occur due to strong gusts of wind  
22 affecting flight velocity which causes poor quality recording and blurry images. Images  
23 collected during take-off and landing were likewise discarded before post-processing. In  
24 addition to re-calculating the camera positions, the self-calibrating bundle adjustment  
25 computed three dimensional point clouds from which thermal ortho-mosaics were built using  
26 a mean value composition. The view zenith angle of ortho-mosaics was set to  $0^\circ$  for all pixels,  
27 hence the largest possible amount of soil was assumed visible.

28 The thermal mosaics served as key boundary conditions to TSEB-PT and DTD. Resulting  
29 resolution on thermal mosaics from midday flights was 0.20 m. However, the software was  
30 not able to mosaic the early morning data, presumably because temperatures were too  
31 homogeneous to enable the detection of common features between images needed for the  
32 bundle adjustment. Consequently, LST from early morning flights were extracted manually

1 and only the average LST for the barley fields was used as the additional data input for DTD  
2 model runs. This average was a satisfying representation of early morning LST because of its  
3 homogenous nature.

## 4 **2.4 Heat flux models**

5 The original TSEB model developed by Norman et al. (1995) is a two-layer model of  
6 turbulent heat exchange. Observations of remotely sensed LST are split into two layers: a  
7 canopy ( $T_C$ ) and a soil ( $T_S$ ) temperature. This is performed with the Priestley-Taylor  
8 approximation that enables calculations of canopy sensible heat flux using estimates of net  
9 radiation divergence. The initial estimate of canopy sensible heat flux thus permits separation  
10 of sensible and latent heat flux between canopy and soil. Further it eliminates the need for an  
11 empirical excess resistance term (Monteith, 1965) which address a substitution of directional  
12 radiometric temperature with aerodynamic temperature when calculating sensible heat fluxes  
13 (Eq. 5, 8 and 9 in Norman et al. (1995)). The TSEB modelling scheme uses directional  
14 radiometric temperature (collected with the thermal camera and UAV) and therefore no  
15 substitution of temperatures or correction via the excess resistance is needed. Section 2.2.1  
16 and 2.2.2 contain TSEB-equations of relevance for the present study and highlight the  
17 difference between TSEB-PT and DTD computations.

### 18 **2.4.1 TSEB-PT**

19 Net radiation ( $R_n$ ) and the three resistances in this soil-canopy-atmosphere heat flux network:  
20 the aerodynamic resistance to heat transfer ( $R_A$ ), the resistance to heat transport from soil  
21 surface ( $R_S$ ) and the total boundary layer resistance of leaf canopy ( $R_X$ ) (all in  $s\ m^{-1}$ ) remain  
22 constant during the individual model runs. For calculations of  $R_A$  and  $R_S$ , see Norman et al.  
23 (2000) Eq. 10 and 11, for calculations on  $R_X$  see Norman et al. (1995) Eq. A8.  
24  $R_n$  is calculated as a sum of short- and long wave radiation:

$$25 \quad R_n = (R_{s,in} - R_{s,out}) + (R_{l,in} - R_{l,out}) \quad (2)$$

$$26 \quad R_{s,in} - R_{s,out} = R_{s,in}(1 - \alpha) \quad (3)$$

$$27 \quad R_{l,in} - R_{l,out} = \epsilon_{surf}\epsilon_{atm}\sigma T_A^4 - \epsilon_{surf}\sigma T(\theta)_R^4 \quad (4)$$

28 where  $R_s$ ,  $R_l$  is short- and long wave radiation respectively and  $_{in}$  and  $_{out}$  refers to the direction  
29 of the radiation,  $\alpha$  is the combined vegetation and soil albedo,  $\sigma$  is Stefan-Boltzman constant,

1  $T_A$  is air temperature (K),  $T(\theta)_R$  is radiometric land surface temperature (K),  $\epsilon_{\text{surf}}$  is combined  
2 vegetation and soil emissivity and  $\epsilon_{\text{atm}}$  is atmosphere emissivity.  $\alpha$  was estimated from  
3 incoming and outgoing short wave radiation from a four-component radiation sensor (NR01,  
4 Hukseflux Thermal Sensor). Albedo for bare soil was measured before the first barley shoots  
5 appeared on the surface and was kept fixed (although some changes are expected with soil  
6 humidity) whereas albedo for vegetation was retrieved for each flying day and hence varied  
7 between individual model runs. Combined vegetation and soil albedo for each flying day is  
8 shown in Table 2.  $T_A$  was attained from the meteorological tower (section 2.1) and  $T(\theta)_R$  was  
9 collected with a UAV.  $\epsilon_{\text{surf}}$  was obtained under similar conditions from Guzinski et al. (2014)  
10 and  $\epsilon_{\text{atm}}$  was computed as in Brutsaert (1975):

$$11 \quad \epsilon_{\text{atm}} = 1.24 \left( \frac{e_a}{T_A} \right)^{0.14286} \quad (5)$$

12 where  $e_a$  is water vapor pressure (mb) attained from meteorological tower.

13 Assuming neutral atmospheric stability and the Monin-Obukhov length tending to infinity, the  
14 iterative part of the model is then initiated.

15 During first iteration the net radiation divergence, partitioning  $R_n$  into radiation reaching the  
16 soil ( $R_{n,s}$ ) and the canopy ( $R_{n,c}$ ) respectively, is computed as in (Norman et al., 2000):

$$17 \quad \Delta R_n = R_n \left[ 1 - \exp\left(\frac{-\kappa F \Omega_0}{\sqrt{2} \cos(\theta_s)}\right) \right] \quad (6)$$

18 Where  $\Omega_0$  is the nadir view clumping factor that depends on the ratio of vegetation height to  
19 plant crown width which is set to 1.0,

20

21  $\theta_s$  is the sun zenith angle calculated by model from time of the day,  $\kappa$  is an extinction  
22 coefficient varying smoothly from 0.45 for LAI more than 2 to 0.8 for LAI less than 2, and F  
23 is the total Leaf Area Index (LAI). Measurements of LAI were obtained with a canopy  
24 analyzer LAI2000 instrument three times during the UAV campaign: 21 May 2014, 3 June  
25 2014 and 18 June 2014. A LAI-average from six measurement locations in the barley site was  
26 computed for each of the three dates: 3.9, 6.6 and 4.0 respectively. LAI values for each model  
27 run were extrapolated from the measurements taking canopy height and fraction of green  
28 vegetation into account.



1 Sensible heat flux of the canopy can thus be estimated using the Priestley-Taylor  
 2 approximation:

$$3 \quad H_C = \Delta R_n \left( 1 - \alpha_{PT} f_g \frac{sp}{sp + \gamma} \right) \quad (7)$$

4 Where  $\alpha_{PT}$  is the Priestley-Taylor parameter set to an initial value of 1.26 assuming unstressed  
 5 vegetation transpiration (Priestley and Taylor, 1972),  $f_g$  is fraction of vegetation that is green  
 6 which was estimated *in situ* for each flying day (Table 2),  $sp$  is the slope of saturation  
 7 pressure curve and  $\gamma$  is the psychrometric constant, both obtained from Allen et al. (1998).

8 Using the sensible heat flux from canopy, canopy temperature ( $T_C$ ) can be computed using  
 9 Eq. A7, A11, A12 and A13 from Norman et al. (1995). Calculations of soil temperature ( $T_S$ )  
 10 can thus be performed:

$$11 \quad T_S = \left( \frac{T(\theta)_R^4 - f_\theta T_C^4}{1 - f_\theta} \right)^{0.25} \quad (8)$$

12 Where  $f_\theta$  is fraction of view of radiometer covered by vegetation calculated as  $f_\theta = 1 -$   
 13  $\exp\left(\frac{-0.5\Omega_\theta F}{\cos(\theta)}\right)$ , where  $\Omega_\theta$  is the clumping factor at view zenith angle ( $\theta$ ).

14 With known resistances and temperatures, fluxes are then calculated in the following  
 15 sequence (all in  $\text{W m}^{-2}$ ):

$$16 \quad H_C = \rho c_p \frac{T_C - T_{AC}}{R_X} \quad (9)$$

17 Where  $H_C$  is sensible heat flux from canopy,  $\rho$  is air density ( $\text{kg m}^{-3}$ ),  $c_p$  is specific heat of air  
 18 ( $\text{J kg}^{-1} \text{K}^{-1}$ ) and  $T_{AC}$  is inter-canopy air temperature (K) computed with  $T_A$ ,  $T_S$ ,  $T_C$ , and  
 19 resistances.

20 Canopy latent heat flux is computed as:

$$21 \quad LE_C = \Delta R_n - H_C \quad (10)$$

22 Sensible heat flux from soil is computed as:

$$23 \quad H_S = \rho c_p \frac{T_S - T_{AC}}{R_S} \quad (11)$$

24 Soil heat flux is computed following Liebenthal and Foken (2007):

$$25 \quad G = 0.3R_{n,S} - 35 \quad (12)$$

26 where  $R_{n,S}$  is net radiation that reaches the soil surface computed as  $R_{n,S} = R_n - \Delta R_n$ .

1 Soil latent heat flux is computed as:

$$2 \quad LE_S = R_{n,S} - G - H_S \quad (13)$$

3 Now it is possible to calculate the total sensible ( $H$ ) and latent heat fluxes (LE) as a  
4 summation of their canopy and soil components:  $H = H_C + H_S$  and  $LE = LE_C + LE_S$ .

5 The Monin-Obukhov length is then re-calculated according to Brutsaert (2005) Eq. 2.46 and  
6 the iterative part of the model is re-run until the Monin-Obukhov length converges to a stable  
7 value, at which point the final flux values are attained.

## 8 2.4.2 DTD

9 The DTD model described in Norman et al. (2000) is a further development of the TSEB-PT  
10 model. DTD similarly split the observed LST into canopy and soil temperatures and computes  
11 surface energy balance components following virtually the same procedure. However, DTD  
12 accounts for the discrepancy between the fact that the TSEB modelling scheme is sensitive to  
13 the temperature difference between land surface and air, and that absolute LST retrieved from  
14 remote sensing data are regarded as inaccurate. This is accounted for by adding an additional  
15 input dataset: LST retrieved one hour after sunrise when energy fluxes are minimal. The  
16 modelled fluxes are hence based on a temperature difference between the two observations,  
17 which is assumed to be a more robust parameter compared to a single retrieval of remotely  
18 sensed LST as it minimizes consistent bias in the temperature estimates. The essential  
19 equation that differs between TSEB-PT and DTD is the one computing sensible heat flux. In  
20 the series implementation of DTD the linear approximation of Eq. (2) is taken together with  
21 Eq. (7) to (9) and applied at midday and one hour after sunrise and subsequently subtracted  
22 from each other to arrive at the following:

$$23 \quad H_i = \rho c_p \left[ \frac{(T_{R,i}(\theta_i) - T_{R,0}(\theta_0)) - (T_{A,i} - T_{A,0})}{(1-f(\theta_i))R_{S,i} + R_{A,i}} \right] + H_{C,i} \left[ \frac{(1-f(\theta_i))R_{S,i} - f(\theta_i)R_{X,i}}{(1-f(\theta_i))R_{S,i} + R_{A,i}} \right] \quad (14)$$

24 where subscripts  $i$  and  $0$  refer to observations at midday and one hour after sunrise  
25 respectively. Since the early morning (time 0) sensible heat fluxes are negligible they are  
26 omitted in the above equation.

27 Computations of soil heat flux ( $G$ ) also differ because the difference in radiometric  
28 temperature between early morning and midday observations can be used as an approximation  
29 of the diurnal variation in soil surface temperature. Soil heat flux computations are derived  
30 from the soil heat flux model of Santanello and Friedl (2003):

1  $G = R_{n,S}A \cos(2\pi \frac{t+10800}{B})$  (15)

2 Where  $t$  is time in seconds between the observation time and solar noon,  $A = 0.0074\Delta T_R +$   
3  $0.088$ ,  $B = 1729\Delta T_R + 65013$  and  $\Delta T_R$  is an approximation of the diurnal variation in the  
4 soil surface temperature from UAV data.

5 For an in-depth review of the TSEB-PT and DTD models including all equations, see  
6 Guzinski et al., (2014) and Guzinski et al. (2015).

## 7 **2.5 Footprint extraction from model output maps**

8 In order to compare modelled  $R_n$ ,  $H$ ,  $G$  and LE to measurements from the eddy covariance  
9 system, a single representative value from each TSEB-PT and DTD output map has to be  
10 extracted in accordance with the coverage of the eddy covariance footprints. Each eddy flux  
11 measurement represents an area for which the size, shape and location are determined by  
12 surface roughness, atmospheric thermal stability and wind direction at a given time – in this  
13 case UAV flight times. Sensible and latent heat fluxes are extracted from TSEB-PT and DTD  
14 maps using a two-dimensional footprint analysis approach as described in Detto et al. (2006).  
15 The twelve footprint outputs were applied to corresponding maps of sensible and latent heat  
16 fluxes by weighing each modelled pixel according to the contribution of that pixel's location  
17 to the measured flux. Approximations of the 70 % eddy flux footprint-coverages are shown in  
18 Appendix B. Net radiation and soil heat flux measurements have footprints that are much  
19 smaller than sensible and latent heat flux measurements and values from  $R_n$  and  $G$  output  
20 maps were extracted from a 5×5 m area on the barley field next to the eddy flux tower.

## 21 **2.6 Validation data**

22 An eddy covariance system consisting of a Gill R3-50 sonic anemometer and a LI-7500 open  
23 path infrared gas analyzer was mounted 6 m above ground in the middle of the site (see Fig.  
24 1). Wind components in three dimensions and concentrations of water vapor were measured  
25 at 10 Hz. Sensible and latent heat fluxes for validation of model outputs were computed from  
26 the eddy covariance system using EddyPro 5.1.1 software (Fratini and Mauder, 2014).  
27 Computations include two dimensional coordinate rotation, block averaging of measurements  
28 in 30 min windows, corrections for density fluctuations (Webb et al., 1980), spectral  
29 corrections (Moncrieff et al., 2005; Moncrieff, et al., 1997) and measurement quality  
30 checking according to Mauder and Foken (2006). Furthermore, the computed heat fluxes were

1 subject to an outlier quality control following procedures described in Papale et al. (2006).  
2 Short- and long wave, incoming and outgoing radiation and soil heat fluxes were measured  
3 with a Hukseflux four component net radiometer (model NR01) and heat flux plate (model  
4 HFP01). Gap-filling of the validation data was not required because no gaps in the data  
5 occurred during the twelve flights. When applying the surface energy balance expression any  
6 residual was assigned to latent heat flux, as recommended by Foken et al. (2011). This  
7 ensures energy balance closure and comparability with TSEB-PT and DTD modelled fluxes.  
8 The average-size of residuals from the twelve datasets was 9 %.

9

### 10 **3 Results and discussion**

11 TSEB-PT and DTD models are executed twelve times with data collected on seven days  
12 during the spring and summer of 2014. Spatially distributed maps of net radiation, soil-,  
13 sensible- and latent heat fluxes are attained with resolutions of 0.20 m.

#### 14 **3.1 Comparison between UAV-fluxes and fluxes from eddy covariance**

15 Modelled fluxes attained with thermal UAV data and measured fluxes from the eddy  
16 covariance system are shown in Table 3. As expected, there are large variations throughout  
17 the season determined primarily by time of year and time of day – dates and hours with  
18 potentially large incoming solar radiation (summer and midday) contain potential for largest  
19 evaporation. Figure 2A-C show modelled versus measured fluxes and a statistical comparison  
20 is presented in Table 4.

21 Calculations for  $R_n$  are alike in TSEB-PT and DTD and generally in good agreement with  
22 measured  $R_n$  with a RMSE value of  $44 \text{ W m}^{-2}$  (11 %) and a correlation coefficient ( $r$ ) of 0.98  
23 (Table 4). Simulated  $R_n$  from 10 April and 2 July 2014 are in less good agreement with  
24 measured  $R_n$  and are underestimated with  $88 \text{ W m}^{-2}$  and  $96 \text{ W m}^{-2}$  respectively.

25 Sensible heat fluxes ( $H$ ) are well estimated by both models (Table 3 and 4 and Fig. 2B).  
26 TSEB-PT sensible heat fluxes are consistently underestimated, however the correlation  
27 coefficient ( $r$ ) is better (in contrast to RMSE and MAE) than  $r$  calculated for DTD. This  
28 implies a better linear relation between measured and modelled sensible heat flux from  
29 TSEB-PT, see Fig. 2B. The DTD model computes slightly more scattered sensible heat fluxes  
30 but results do not show any systematic errors – they are centered around measured values and

1 are generally in better accordance with measured fluxes with RMSE and MAE values of 59  
2  $\text{W m}^{-2}$  (64 %) and  $49 \text{ W m}^{-2}$  (52 %), compared to TSEB-PT RMSE and MAE values of  $85 \text{ W}$   
3  $\text{m}^{-2}$  (91 %) and  $75 \text{ W m}^{-2}$  (81 %).

4 Soil heat fluxes ( $G$ ) are underestimated by both algorithms and RMSE and MAE values of 48  
5  $\text{W m}^{-2}$  (91 %) and  $45 \text{ W m}^{-2}$  (86 %), and  $38 \text{ W m}^{-2}$  (72 %) and  $35 \text{ W m}^{-2}$  (66 %) are obtained  
6 from DTD and TSEB-PT respectively.

7 Modelled latent heat flux (LE) is in good agreement with measured latent heat fluxes. As a  
8 consequence of underestimation of sensible heat flux in TSEB-PT simulations, a small  
9 overestimation of TSEB-PT latent heat flux appears (Fig. 2C). DTD latent heat flux is again  
10 more scattered but with lower RMSE and MAE values of  $67 \text{ W m}^{-2}$  (26 %) and  $57 \text{ W m}^{-2}$  (22  
11 %), compared to TSEB-PT RMSE and MAE values of  $94 \text{ W m}^{-2}$  (37 %) and  $84 \text{ W m}^{-2}$  (33 %).

### 12 3.1.1 Method discussion

13 The DTD algorithm generally produces results in better accordance with measurements and is  
14 concluded to be a better algorithm when simulating heat fluxes with present experimental  
15 setup. This suggests a consistent bias in the UAV derived LST which can be corrected by  
16 subtracting the early morning observations from the midday ones and demonstrates the  
17 robustness and added utility of the DTD approach.

18 A poor agreement between modelled and measured  $R_n$  was found on 10 April and 2 July  
19 2014. Modelled  $R_n$  consists of short- and longwave incoming and outgoing radiation ( $R_{s,in}$ ,  
20  $R_{s,out}$ ,  $R_{l,in}$ ,  $R_{l,out}$ ) of which  $R_{s,in}$  is provided as model input from eddy tower measurements.  
21 This contributes positively to the agreement between modelled and measured  $R_n$  but it cannot  
22 be assigned to model performance or the quality of collected LST data. Therefore a  
23 comparison is also conducted between modelled and measured net longwave radiation ( $R_l$ ),  
24 which as opposed to modelled and measured  $R_n$ , are entirely independent of each other. The  
25 TSEB modelling scheme produce  $R_l$  estimates to a satisfactory level if results from 10 April  
26 and 2 July are not regarded, see appendix A.  $R_l$  estimates depend on atmospheric emissivity  
27 which in the TSEB modelling scheme are calculated with Eq. 5 (from Brutsaert (1975)). Eq. 5  
28 builds on the assumption of exponential atmospheric profiles for temperature, pressure and  
29 humidity. The stability of atmosphere is affected by relative humidity (RH) (Herrero and  
30 Polo, 2012) and errors between measured and modelled  $R_l$  are related to RH in second graph  
31 in appendix A. A coincidence between the highest errors and the highest RH appears. This

1 suggests that assumptions behind Eq. 5 might not be met on 10 April and 2 July. Different  
2 approaches for estimating  $R_1$  could have been chosen for these two dates (e.g. Brutsaert  
3 (1982)) but for simplicity the approach presented in Brutsaert (1975) is maintained for all  
4 dates. Appendix A show that if algorithm-assumptions are met, UAV collected LST can be  
5 satisfactorily used to estimate  $R_1$  using the TSEB scheme. Eq. 5 also builds on the assumption  
6 of clear skies. Since poor simulations of  $R_1$  is not significant in data collected in overcast  
7 conditions, the larger incoming longwave radiation due to clouds might compensate for the  
8 smaller path between UAV and surface, compared to between satellite and surface.

9 Further, a poor agreement between modelled and measured  $G$  was found.  $G$  was measured  
10 from two heat flux plates located approximately 3 cm below the surface. Heat flux plates  
11 might not provide the best estimate of energy partitioning at the surface (Jansen et al., 2011)  
12 which could lead to uncertainties in measured  $G$ . Further, the difference between heat  
13 conduction of soil and air create a discrepancy between measured  $G$  and  $H$  and LE, since fast  
14 changes in  $R_n$  (as a consequence of intermittent cloud cover) will have a faster response in  $H$   
15 and LE than in  $G$  (Gentine et al., 2012). The TSEB modelling scheme does not account for  
16 the delay in  $G$  response and therefore also a discrepancy between measured and modelled  $G$   
17 will occur. However, the magnitude of  $G$  is small compared to the remaining surface energy  
18 fluxes and therefore has a comparably small impact on LE estimations even though it is  
19 computed as a residual of  $R_n$ ,  $H$  and  $G$ .

20 In average there was a 95 % overlap between the coverage of eddy flux footprints and the  
21 model output maps from all twelve datasets. The lacking percentages of fluxes from maps  
22 were simply added from the flux values obtained from overlapping eddy flux footprints and  
23 maps. This introduces a small uncertainty to the extraction of flux values from model output  
24 and thus also to the comparison between measured and modelled  $H$  and LE.

25 The view zenith angle of ortho-mosaics was set to  $0^\circ$  (section 2.3). However the maximum  
26 view zenith angle of the thermal camera is  $15^\circ$  and setting a theoretical view zenith angle to  
27  $0^\circ$  could lead to a small overestimation of latent heat flux. Any bias due to the  $0^\circ$  view zenith  
28 angle in models could maybe have been accommodated using a maximum value composition  
29 (instead of a mean value composition) when generating LST-mosaics. However, a mean value  
30 composition was used because the mosaics produced with this method compared well with  
31 mosaics produced manually in which the edges of each image were removed. Edges were  
32 removed in order to eliminate the vignetting effect, which generally affects thermal images in

1 particular and therefore also the images collected in this study. Using a mean value  
2 composition is thus assumed to enable the usage of entire images without eliminating or  
3 correcting for vignetting effects. Using entire images allow a larger image overlap which is  
4 crucial when images are mosaicked in Photoscan. The difference between using a mean and a  
5 maximum value composition was approx. 0.3° Kelvin and 5 W m<sup>-2</sup> latent heat flux for mosaic  
6 from 10 April 2014.

7 Disagreement between measured and modelled fluxes may also be due to the presented  
8 approach of handling the residual between eddy covariance surface energy fluxes. The  
9 average-size of residuals from the twelve datasets was as mentioned 9 % (section 2.6). A  
10 different approach to handling the energy balance residual (e.g Foken, 2008) would lead to  
11 slightly different results in the comparison between measured and modelled fluxes.

12 A calibration of the camera with in situ temperatures would likely have improved TSEB-PT  
13 heat flux computations. Further a conversion of brightness temperature to actual LST using a  
14 spatially distributed emissivity would presumably improve both TSEB-PT and DTD results.

### 15 3.1.2 Comparison to other studies

16 Guzinski et al. (2014) applied their TSEB-PT study to the same field site as the present study  
17 but they used thermal satellite images from Landsat as boundary conditions as opposed to  
18 thermal UAV images. A comparison between the two studies shows similar accurate results.  
19 Guzinski et al. (2014) achieve RMSEs of 46 W m<sup>-2</sup> for  $R_n$ , 56 W m<sup>-2</sup> for  $H$  and 66 W m<sup>-2</sup> for  
20 LE (Table 2, column ND<sub>H</sub> in Guzinski et al. (2014)). This study achieves RMSEs of 44 W m<sup>-2</sup>  
21 for  $R_n$ , 59 W m<sup>-2</sup> for  $H$  and 67 W m<sup>-2</sup> for LE, using the DTD model.  $r$  is likewise similar  
22 between the two studies. However, when Guzinski et al. (2014) uses both MODIS and  
23 Landsat data to disaggregate DTD fluxes, modelled sensible and latent heat fluxes were in  
24 better agreement with the observed fluxes (Table 2, column EF in Guzinski et al. (2014)).  
25 Further, a comparison between this study and other studies seeking to estimate surface fluxes  
26 from remotely sensed data (such as Colaizzi et al. (2012); Guzinski et al. (2013); Norman et  
27 al. (2000)) show that measured and modelled fluxes are in same order of agreement.

### 28 3.1.3 Cloudy and overcast situation

29 Contrary to studies using satellite images, the majority of data in this study were retrieved  
30 under cloudy or overcast conditions. Data collected during sunny conditions are enclosed by

1 black circles in Fig. 2A-C and Table 5 shows statistical parameters calculated using only data  
2 from days with cloudy or overcast weather conditions. Based on Fig. 2A-C and on a  
3 comparison between statistical parameters in Table 4 and 5, no significant difference can be  
4 seen between data collected during cloudy, overcast and sunny weather conditions. Thus it is  
5 concluded that the TSEB modelling scheme can be applied to data obtained in all three  
6 weather types. However, it is worth mentioning that data collected during conditions with  
7 scattered clouds, and hence quickly changing irradiance, would lead to large variations in  
8 retrieved LST during a single flight. LST collected with UAVs are instantaneous but also a  
9 mosaic of instantaneous LST collected in a time span of 20 min. Comparing this kind of  
10 measurement to a 30 min flux average from the eddy covariance system can lead to  
11 disagreement between measured and modelled fluxes (Kustas et al., 2002).

### 12 **3.2 Spatial patterns in evaporation maps**

13 Combining the high spatial resolution LST with the TSEB modelling scheme, produces  
14 spatially distributed heat flux maps which reveal patterns in the evaporation which could not  
15 have been quantified through more established techniques, such as eddy covariance or when  
16 using satellite data. Twelve evaporation maps computed with DTD are shown in Appendix B.  
17 Patterns of evaporation within the barley fields are the same for TSEB-PT and DTD maps.  
18 The maps differ in size due to different flight routes, which are determined by wind direction  
19 and velocity on the given day. This study does not have access to data with same spatial  
20 resolution that could have validated the evaporation patterns. However, the irrigation system  
21 applied to the barley field constitute valid explanation for patterns seen in maps from the late  
22 growing season, which provides confidence on spatial patterns seen in all maps.

23 During the UAV campaign the barley field was irrigated five times: 23 May, 29 May, 5 June,  
24 15 June and 25 June, 2014. On each occasion 25 mm of water was applied. Irrigation is  
25 performed with a traveling irrigation gun that is automatically pulled across the field in  
26 tramlines that run in north-south direction on northern field and east-west direction on  
27 southern field, Fig. 3. The pattern of which water is irrigated remains the same during the  
28 entire growing season.

29 The evaporation maps from 18 June 2014 and onwards (when irrigation would plausible have  
30 made its mark on plant health) reveal significant differences within the barley fields: patterns  
31 of approx. 20 m wide blueish areas running parallel to the tramlines. The blueish color



1 illustrate that these areas produce less evaporation than surrounding areas. The location of  
2 areas with smaller evaporation rates corresponds well with areas where irrigation guns have  
3 not been able to irrigate as intensively as areas closer to the tramlines (Fig. 3). Areas furthest  
4 away from tramlines thus likely consist of less healthy plants which will generate higher LST  
5 and lower rates of evaporation. Recognition of very likely patterns of evaporation within the  
6 barley field demonstrates a high degree of confidence in the veracity of the spatially  
7 distributed model output.

8

#### 9 **4 Conclusions and outlook**

10 Land surface temperatures (LST) were obtained with a lightweight thermal camera mounted  
11 on a UAV with the ability to cover a 400 x 400 m barley field in a single flight. Thermal  
12 images were successfully concatenated into high resolution LST-mosaics (0.2 m) that served  
13 as key boundary conditions to the two source energy balance models: TSEB-PT and DTD. In  
14 contrast to TSEB-PT, the DTD model accounts for biases in remotely sensed LST, likely to  
15 be present in images from the lightweight thermal camera. Simulated net radiation, soil-,  
16 sensible- and latent heat fluxes were in good agreement with flux measurements from an eddy  
17 covariance system, with the DTD algorithm showing superior results. Patterns from  
18 systematic irrigation on the barley field support the confidence in the veracity of the spatially  
19 distributed evaporation patterns produced by the models. A comparison between present  
20 results and results from other studies estimating surface energy fluxes from heat flux models  
21 and remotely sensed LST, reveal that data from the UAV platform and the lightweight  
22 thermal camera generates surface energy fluxes with similar accuracy as can be generated  
23 using satellite data. The UAV data can thus be used for model input and for other potential  
24 applications requiring good quality, consistent and high resolution LST.

25 Additionally, the UAV platform accommodated validation of the applicability of the TSEB  
26 modelling scheme in cloudy and overcast weather conditions which was possible due to the  
27 low altitude of LST-retrievals compared to satellites that can only retrieve LST during clear  
28 sky conditions.

29 Future improvements will incorporate spatially distributed optical data into the two source  
30 energy balance models in order to estimate spatially varying ancillary variables such as  
31 albedo, leaf area index and canopy height. This will enable flux estimations in areas with  
32 heterogeneous vegetation types and have a positive effect on estimations over maturing crops

1 when differences in irrigation may have impacted their developmental stage. Extending the  
2 present setup to other land cover types would further strengthen the applicability of thermal  
3 UAV data and presented model scheme.

4 A calibration of the thermal camera with *in situ* temperatures should improve TSEB-PT  
5 results with a potential positive effect on DTD results as well.

6 Adjustments in the TSEB modelling scheme that consider differences between satellite and  
7 UAV images might be valuable. The atmospheric path from the ground to satellites and from  
8 the ground to UAVs, differs greatly and a comparison between measured and modelled  
9 longwave radiation in this study (section 3.1) reveal that a different approach for estimating  
10 atmospheric emissivity (when using UAV data) might further improve the TSEB modelling  
11 results.

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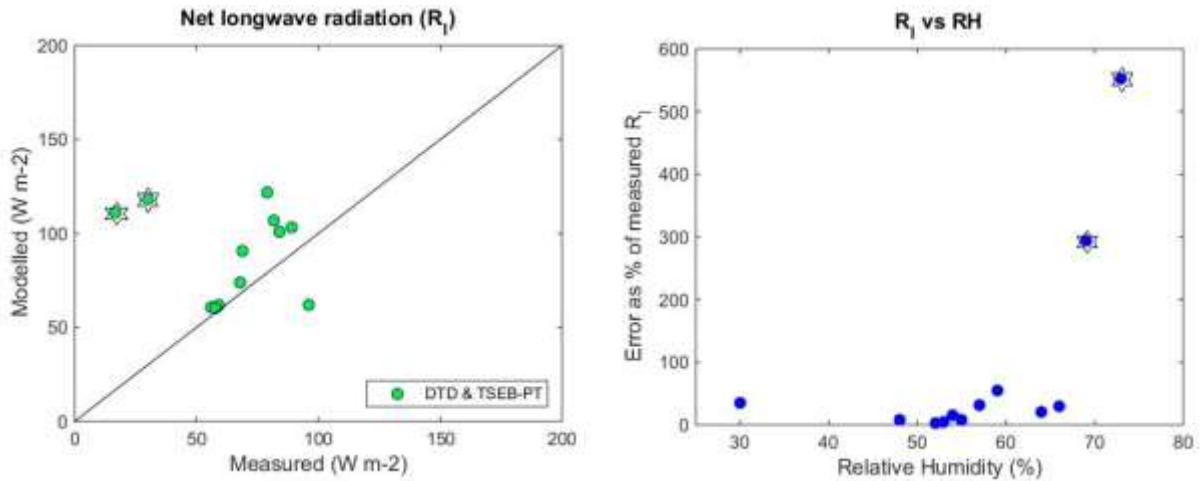
23

24

25

26

# 1 Appendix A



2

3 First graph show measured and modelled net longwave radiation ( $R_l$ ).  $R_l$  from 10 April and 2  
4 July 2014 are enclosed by black stars. Second graph show the error between measured and  
5 modelled  $R_l$  as percent of measured  $R_l$  compared to relative humidity at the time of UAV  
6 flights. Again measurements from 10 April and 2 July 2014 are enclosed by black stars.

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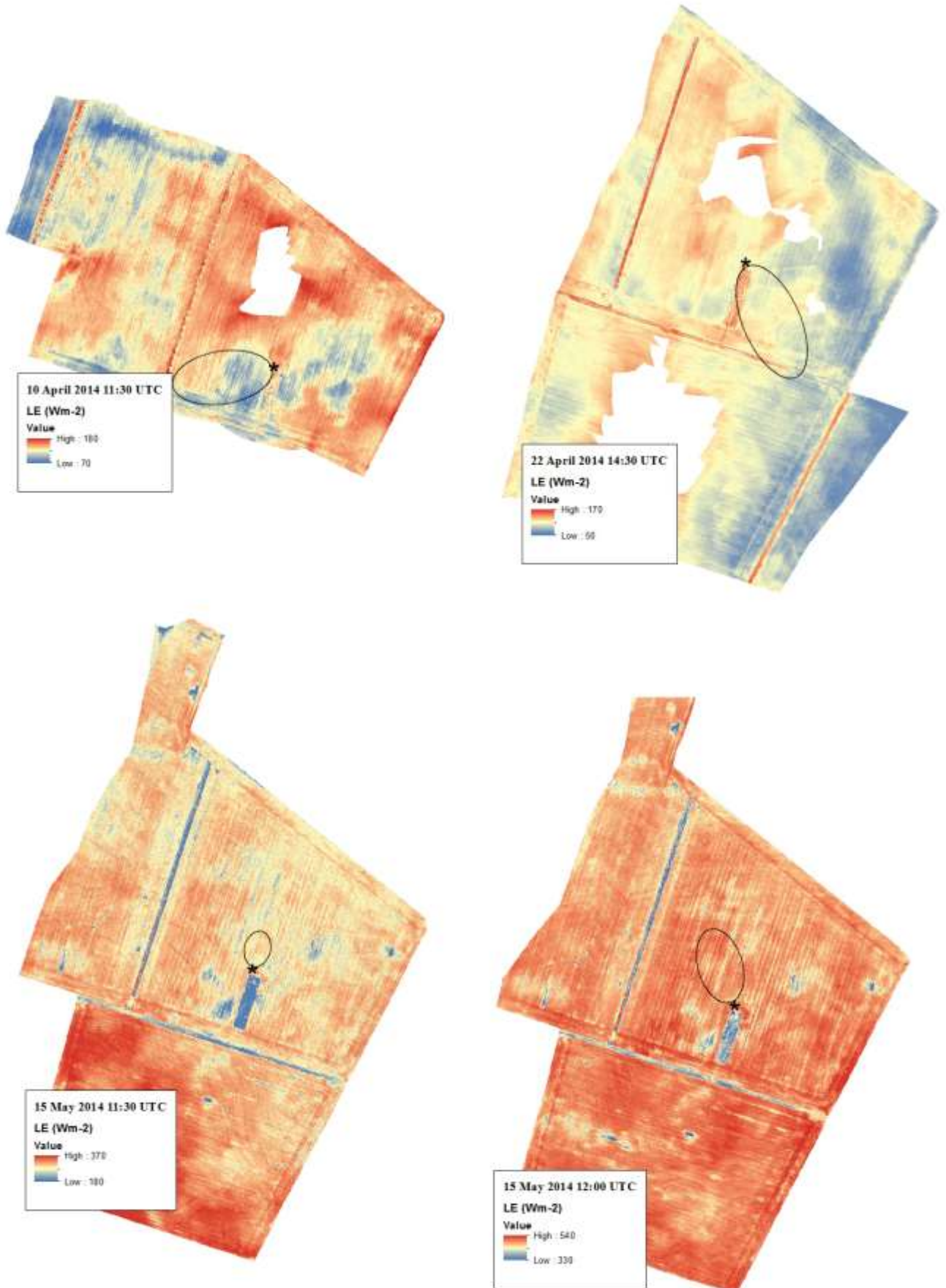
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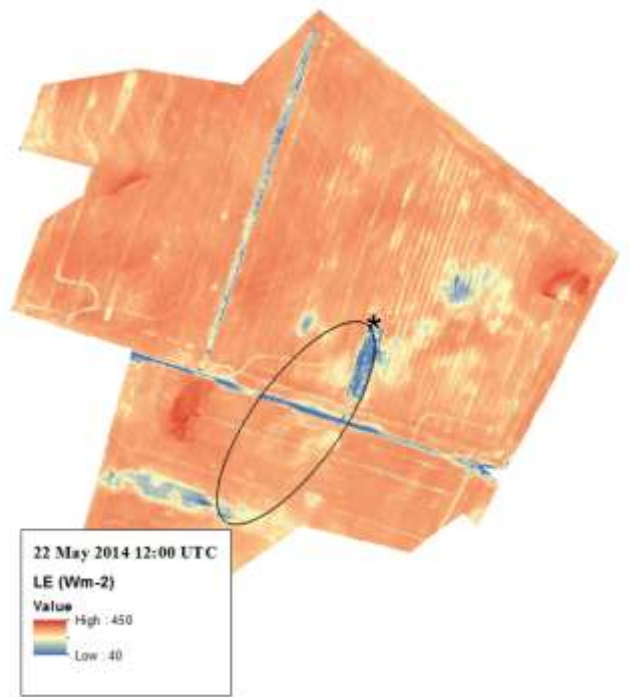
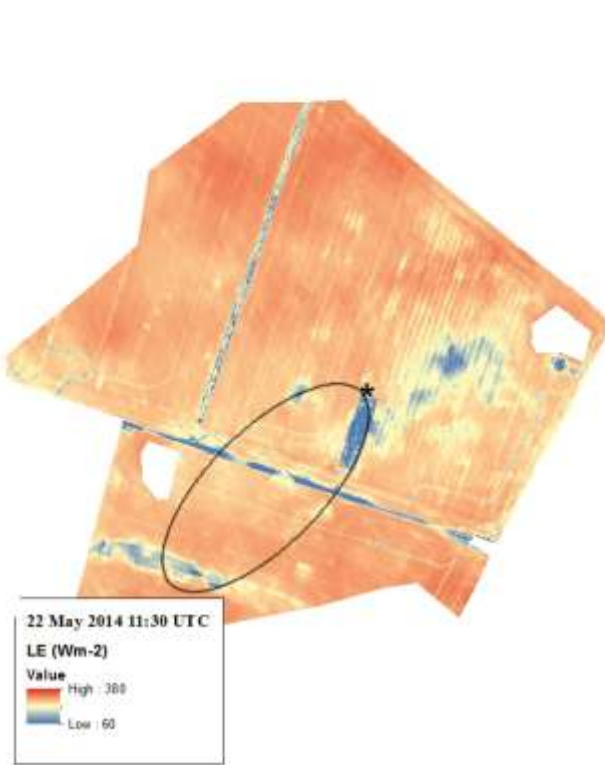
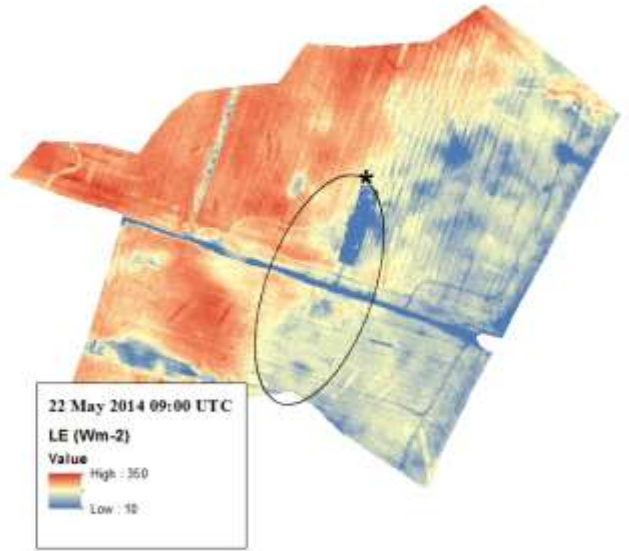
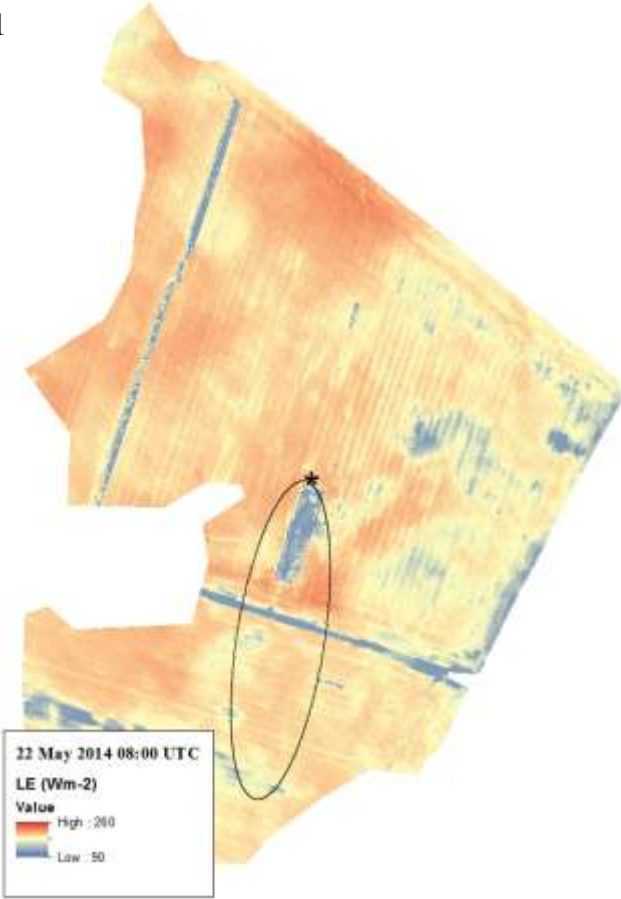
1 **Appendix B**

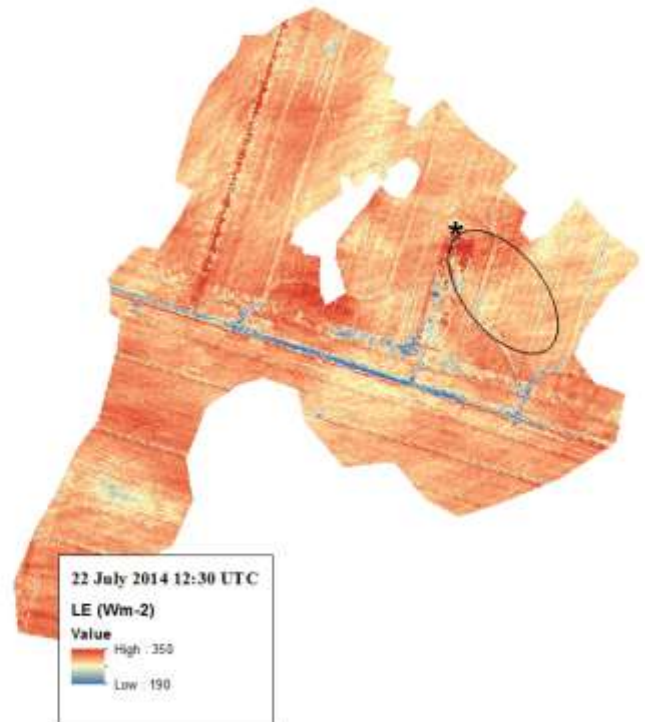
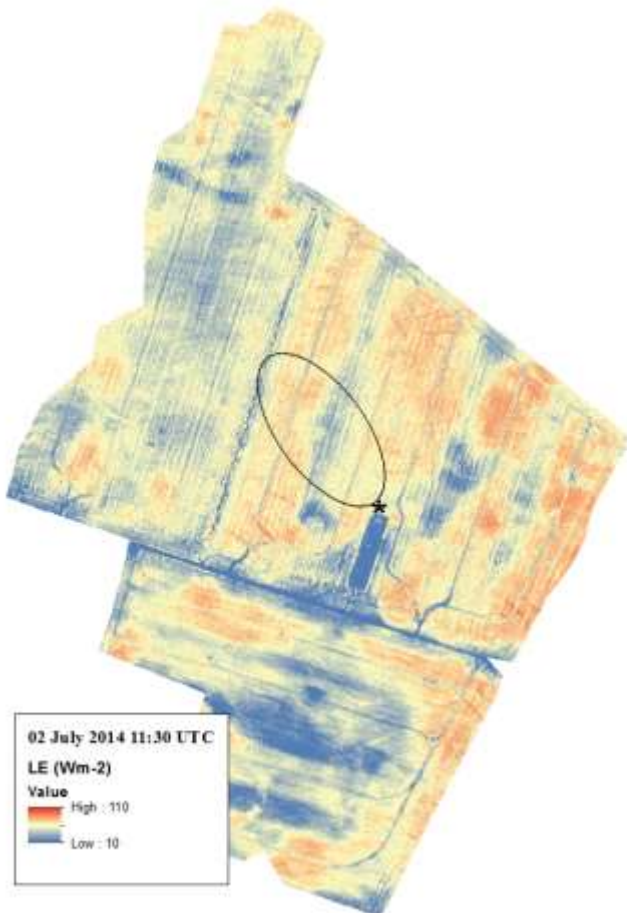
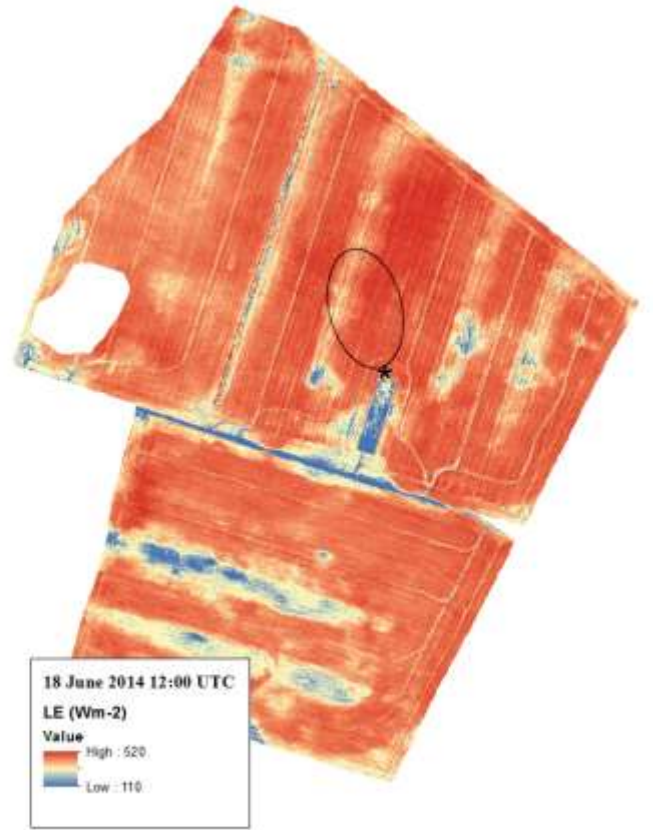
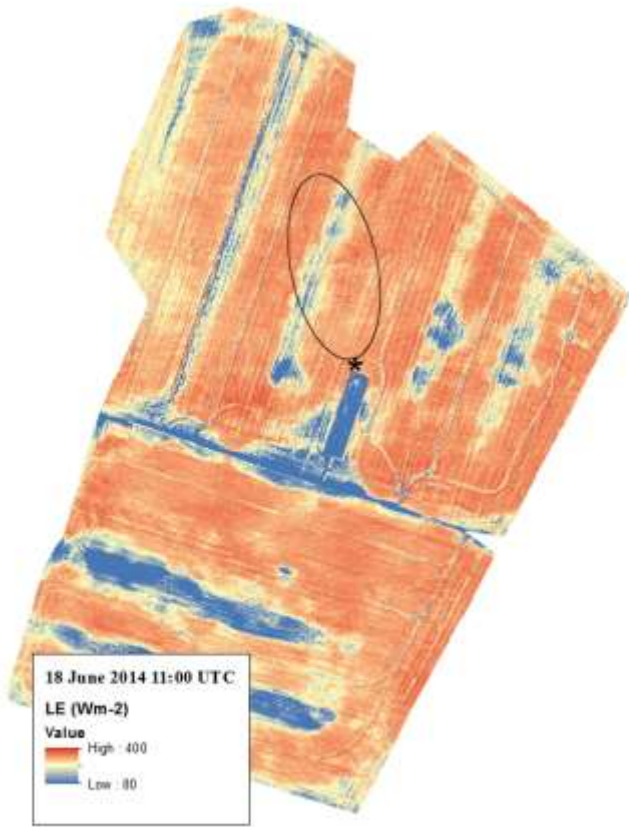
2 Evaporation maps from the DTD model. Black star represent location of eddy flux tower and  
3 black circles mark location of eddy covariance footprint.

4



1





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9

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1 Table 1 - UAV retrievals of LST, constituting 12 sets of input data to TSEB-PT and DTD.  
 2 Early morning flights conducted one hour after sunrise are only used in DTD. (c) means data  
 3 were collected during cloudy or overcast conditions.

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Date		Early flights	Daylight flights				
		( $T_{R,0(\theta)}$ )	( $T_{R,i(\theta)}$ )				
		Time (UTC)					
10 April 2014	(c)	07:00			11:30		5
22 April 2014	(c)	06:00				14:30	6
15 May 2014		05:30			11:00	12:00	7
22 May 2014	(c)	05:00	08:00	09:00	11:30	12:00	8
18 June 2014	(c)	05:00			11:00	12:00	9
02 July 2014	(c)	07:30			11:30		10
22 July 2014		06:30				12:30	11
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1 Table 2 – Changing input parameters for each flying day.

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Date	LAI	Canopy height (m)	Green veg. fraction	Albedo <sub>soil+veg.</sub>
10 April 2014	0.48	0.02	1	0.142
22 April 2014	0.88	0.08	1	0.181
15 May 2014	1.49	0.12	1	0.182
22 May 2014	3.90	0.30	1	0.226
18 June 2014	4.03	0.95	0.7	0.181
02 July 2014	3.43	1.10	0.3	0.202
22 July 2014	3.02	1.20	0.02	0.189

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1 Table 3 – Measured and modelled net radiation ( $R_n$ ), sensible heat flux ( $H$ ), latent heat flux  
 2 (LE) and soil heat flux ( $G$ ). Dates marked with (c) represent days with cloudy or overcast  
 3 conditions.

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Date, time (UTC)		Measured ( $\text{W m}^{-2}$ )				TSEB-PT ( $\text{W m}^{-2}$ )				DTD ( $\text{W m}^{-2}$ )			
		$R_n$	$H$	LE	$G$	$R_n$	$H$	LE	$G$	$R_n$	$H$	LE	$G$
10 April 2014 11:30	(c)	243	87	105	50	155	15	134	2	155	20	121	8
22 April 2014 14:30	(c)	203	73	81	49	180	1	181	4	180	62	118	-2
15 May 2014 11:00		453	124	241	88	401	42	330	27	401	75	295	25
15 May 2014 12:00		619	132	385	102	600	49	492	54	600	97	472	26
22 May 2014 08:00	(c)	270	33	206	31	284	-20	296	2	284	95	179	-1
22 May 2014 09:00	(c)	306	-26	290	43	301	-48	337	10	301	63	231	1
22 May 2014 11:30	(c)	406	-16	367	55	397	-33	418	14	397	101	287	6
22 May 2014 12:00	(c)	440	14	365	61	436	-51	465	21	436	42	387	4
18 June 2014 11:00	(c)	538	158	326	55	505	89	397	27	505	191	309	9
18 June 2014 12:00	(c)	631	200	378	52	612	54	514	43	612	156	450	7
02 July 2014 11:30	(c)	217	54	152	11	121	-9	135	-8	121	52	68	1
22 July 2014 12:30		479	282	161	36	511	125	335	52	511	211	293	6

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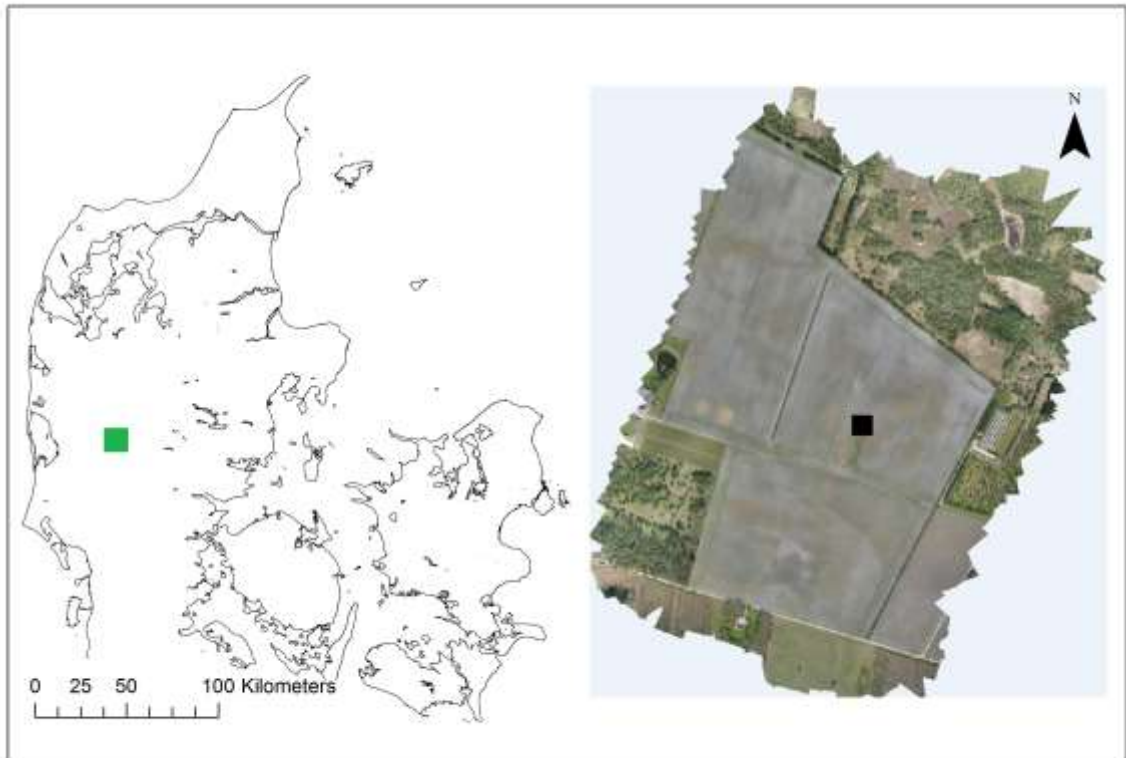
1 Table 4 – Root mean square error (RMSE), mean absolute error (MAE) and correlation  
 2 coefficient (r) computed for TSEB-PT and DTD results. Values in parenthesis are RMSE and  
 3 MAE respectively as percentage (%) of measured fluxes.

	TSEB-PT			DTD		
	RMSE	MAE	r	RMSE	MAE	r
	(W m <sup>-2</sup> )	(W m <sup>-2</sup> )		(W m <sup>-2</sup> )	(W m <sup>-2</sup> )	
8 <i>R<sub>n</sub></i>	44 (11)	33 (8)	0.98	44 (11)	33 (8)	0.98
9 <i>G</i>	38 (72)	35 (66)	0.58	48 (91)	45 (86)	0.86
10 <i>H</i>	85 (91)	75 (81)	0.96	59 (64)	49 (52)	0.74
11 LE	94 (37)	84 (33)	0.92	67 (26)	57 (22)	0.85

1 Table 5 – Statistical parameters based on data that was collected during only cloudy and  
 2 overcast weather conditions (9 dates). Root mean square error (RMSE), mean absolute error  
 3 (MAE) and correlation coefficient (r) computed for TSEB-PT and DTD results. Values in  
 4 parenthesis are RMSE and MAE respectively as percentage (%) of measured fluxes.

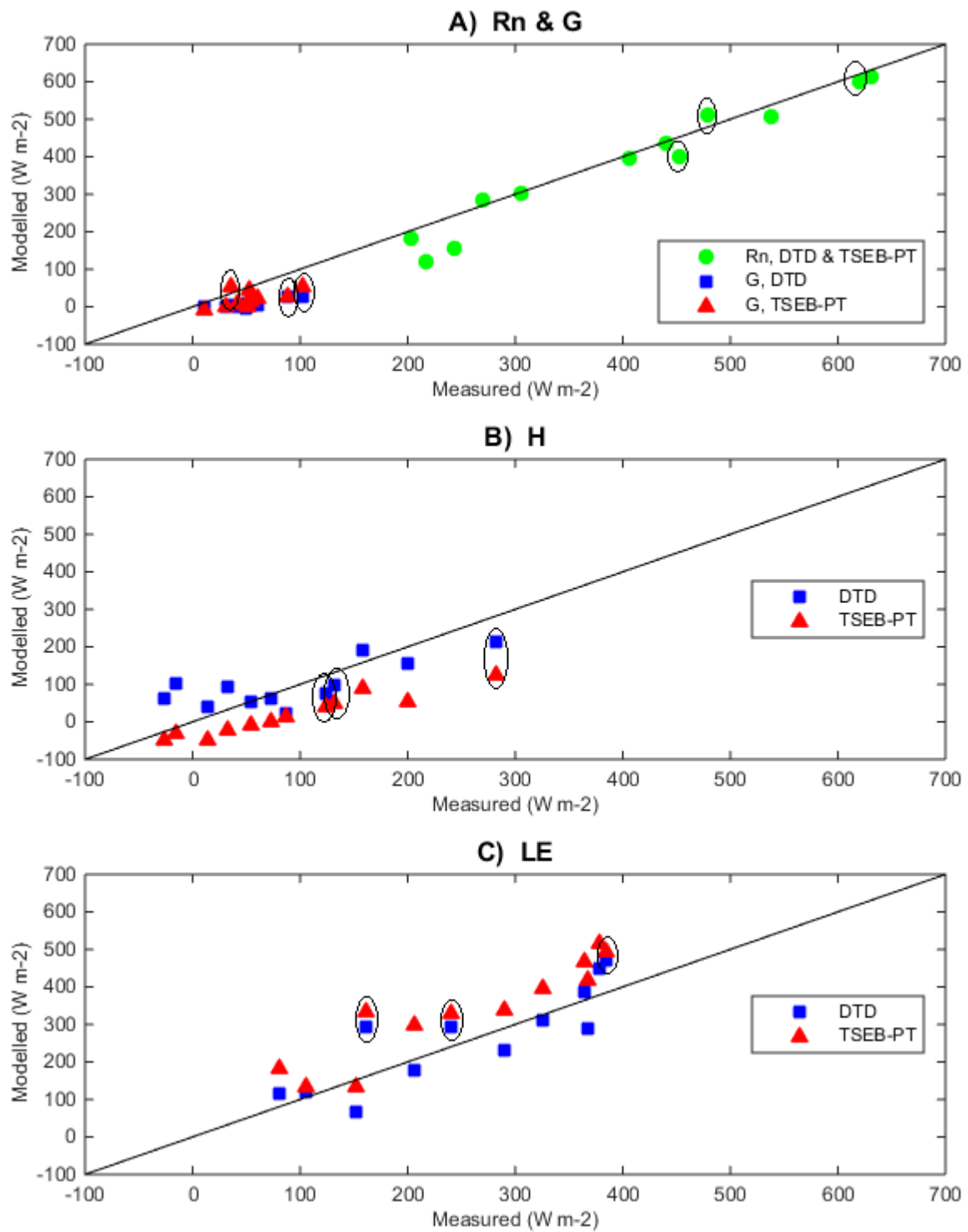
	TSEB-PT			DTD		
	RMSE	MAE	r	RMSE	MAE	r
	(W m <sup>-2</sup> )	(W m <sup>-2</sup> )		(W m <sup>-2</sup> )	(W m <sup>-2</sup> )	
9 <i>R<sub>n</sub></i>	40 (11)	32 (8)	0.99	40 (11)	32 (8)	0.99
10 <i>G</i>	30 (66)	33 (72)	0.66	38 (83)	42 (92)	0.61
11 <i>H</i>	63 (99)	64 (100)	0.84	53 (83)	50 (78)	0.69
12 <i>LE</i>	69 (27)	71 (28)	0.98	46 (18)	46 (18)	0.95





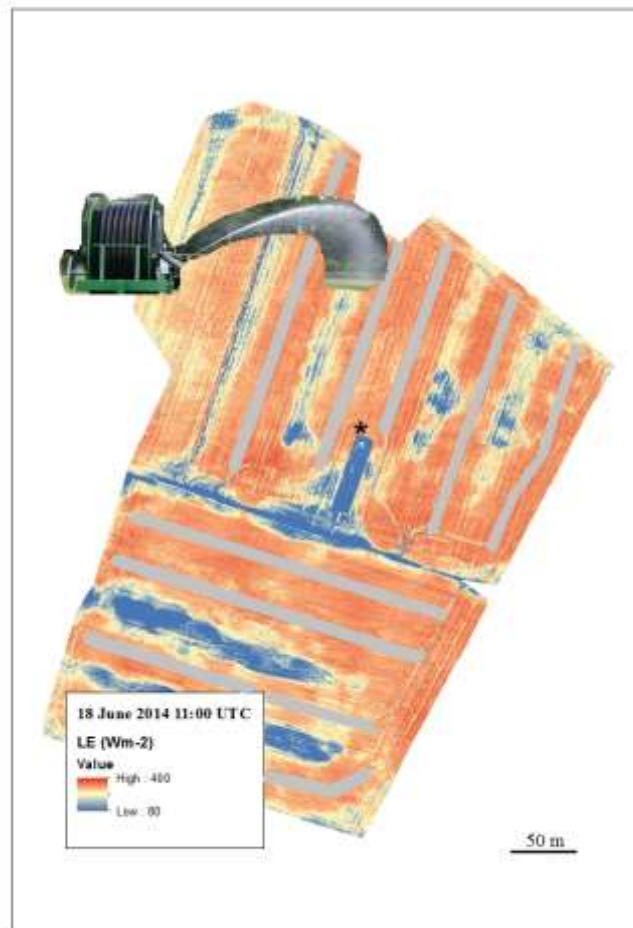
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Figure 1 - HOBE agricultural site in western Denmark (56.037644°N, 9.159383°E). The black square represents location of the eddy flux tower. The green square represents location for zoom inset on the right (RGB image obtained with Lumix camera mounted on UAV).



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 2 Figure 2 - Modelled vs measured net radiation ( $R_n$ ), soil- ( $G$ ), sensible- ( $H$ ) and latent heat  
 3 fluxes ( $LE$ ). Data collected in sunny weather conditions are enclosed by black circles.

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3 Figure 3 – Grey lines highlight tramlines in which irrigation guns are placed at all five  
4 irrigation events in 2014. The underlying map shows evaporation patterns on 18 June 2014.  
5 Red colors are high evaporation and blue colors are low evaporation. Patterns of lower  
6 evaporation correspond well with areas being furthest away from irrigation guns.

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