The new version of the paper was improved and I feel that authors provide relatively convincing answers to reviewer’s comments. Useless figures were removed and a better description of the originality/novelty of the present paper compared to previous studies was done.
I regret that the paper doesn’t show any quantitative comparison with Wanders et al. study, which would have been able to quantify the improvement of the method. In addition, I have still some difficulties to clearly understand some parts of the paper, and some figure legends really need a detailed description (see below). However, the paper shows some interesting findings related to soil saturation effect and precipitation threshold detectability on the quality of precipitation corrections. Thus, my recommendation is to publish the paper providing that the following minor/technical comments are addressed.

We would like to thank Anonymous Referee #2 for the comments. Please find our response below (comments by Referee #2 are quoted in blue italic and our response are marked in black. Line numbers are marked according to the updated manuscript with tracked changes).

We have included a quantitative comparison of FAR and POD with Wanders et al. and discussion of differences in methods used (line 565-603).

- The legend in Figure 2 should be detailed as it was done in Wanders et al. Only one line in the present paper (about 10 in Wanders) is not enough to correctly understand the Figure.
- Can authors better explain what the two circles in Figure 2 are?

Figure 2 is updated with detailed description added in the caption and Line 183-184.

- Line 385: what is possibly due to lower soil moisture variability …??! Reconsider the sentence.

We revised the sentence in Line 369.

- The legend in Figure 12 should also be detailed to capture the main result of the figure.

We included this information in the caption of Figure 12.

- Indicate the time-period in Figure 9 legend.

The period is from 2003/01/01 to 2007/07/31. This has been clarified in the caption of figure 9.
Report #2

Submitted on 18 Sep 2015

Referee #1: Dr. Luca Brocca, luca.brocca@irpi.cnr.it

I found the paper significantly improved and the reviewers' comments successfully addressed. Specifically, the description of the method and of the results is now clear and detailed as needed (at least for me). The comparison with previous studies is also well done and highly interesting. The differences with Wanders et al. (2015) are now evident. Anyhow, I have completely re-read the paper and I still have some minor comments to be addressed.

We would like to thank Dr. Luca Brocca for the comments. Please find our response below (comments by Dr. Luca Brocca are quoted in blue italic and our response are marked in black. Line numbers are marked according to the updated manuscript with tracked changes).

1) Lines 78-82: does it mean that it is better to use LST data with respect to soil moisture? It is not clear to me by reading this sentence. We revised the sentence in line 80.

2) At lines 83-93 it reads: “But this isn’t always the case, and it is also noted that current low-frequency microwave soil moisture missions (specifically SMAP and SMOS) don’t have radiometers at frequencies useful for estimating land surface temperatures, even though a 37 GHz sensor is part of the AMSR2 system. In fact SMAP and ECMWF/SMOS use LST from weather models analysis fields in their algorithms. Unfortunately the lowest microwave frequency of AMSR2 and SMOS precludes retrieving soil moisture from many areas with heavy vegetation, and AMSR2 has a significant dry bias with less availability than AMSR-E, but is no longer operable. So improvements to satellite precipitation from the Global Precipitation Mission products must rely solely on satellite soil moisture products from SMAP, which promises better soil moisture retrievals due to increased penetration depth, and the improvements to the assimilation algorithms is the goal of this study.” I found this paragraph unfair and also with some wrong sentences. I suggest strongly revise it. I do not believe it is a good justification the use of soil moisture, instead of LST, simply saying that current missions don’t have frequencies useful for estimating land surface temperatures. It is not the case for AMSR2 (currently in orbit) and also for Chinese sensors. B) SMOS is operating at L-band as SMAP. Why SMOS should have a more problems than SMAP in highly vegetated areas? Why “ECMWF/SMOS” and not only SMOS? C) “So improvements to satellite precipitation from the Global Precipitation Mission products must rely solely on satellite soil moisture products from SMAP”. This sentence is wrong and should be changed. D) Note also that scatterometer data from ASCAT are found to provide highly useful information for rainfall correction/retrieval in studies by Crow et al. and Brocca et al. I guess it should be acknowledged. The reference in the original sentence regarding SMOS was inadvertently included, and we thank the reviewer for noting this. We have also edited the statement to better reflect our message. Thus our revised statement (now in line 83-94) now reads:

But this isn’t always the case, and it is also noted that current low-frequency microwave soil moisture missions (specifically SMAP and SMOS) don’t have radiometers at frequencies useful for estimating land surface temperatures, even though a 37 GHz sensor is part of the AMSR2 system. In fact SMAP and SMOS use LST from weather models analysis fields in their algorithms. Unfortunately the lowest microwave frequency of AMSR2 precludes retrieving soil moisture from many areas with heavy vegetation, and AMSR2 has a significant dry bias with less availability than AMSR-E, but is no longer operable. So improvements to satellite precipitation from the Global Precipitation Mission products must rely solely on satellite soil moisture products, and the improvements to the assimilation algorithms is the goal of this study.

3) Lines 219-220: is the correction made pixel by pixel? Please specify. The correction is done pixel by pixel. This has been clarified in line 226.

4) Line 378: Please revise the sentence. We revised the sentence in line 380-381.

5) Line 392: “Consistent with other studies” Add here the references to that studies.
6) Lines 490-491: In Brocca et al. (2014) three global scale DAILY rainfall products are obtained from ASCAT, AMSR-E and SMOS soil moisture products. The performance is computed for 5-day cumulated rainfall as the temporal resolution of the sensors (mainly SMOS) was not suitable for high resolution (daily) rainfall estimation. Therefore, 5-day precipitation is not estimated by considering “soil moisture changed over a 5-day period”. Please change.

We revised the text between lines 499 and 507 to clarify that the estimation algorithm results in the estimation of daily precipitation, and uses soil moisture observations from three satellite derived soil moisture datasets (AMSR-E LPRM, ASCAT and SMOS) whose values were linearly interpolated to daily values for the precipitation estimation algorithm.

Note also that recently in Ciabatta et al. (2015, JHM: http://dx.doi.org/10.1175/JHM-D-14-0108.1) daily rainfall product from ASCAT is obtained through the same approach in Brocca et al. (2014), and the integration of ASCAT-derived rainfall with TRMM provided significant improvements in all performance scores even for 1-day precipitation. Moreover, very recent results with accurate estimation of 1-day rainfall (still in preparation, not yet published on journals but only at conferences) are coming.

This has been acknowledged in line 508-510.

7) Line 518-520: please revise the sentence, something seems missing.

In re-reading these sentences, we agree with the reviewer that they are unclear. Since they don’t add additional information, we have decided to remove them for readability.
Correction of real-time satellite precipitation with satellite soil moisture observations

Wang Zhan\textsuperscript{1}, Ming Pan\textsuperscript{1}, Niko Wanders\textsuperscript{1,2}, Eric F. Wood\textsuperscript{1}

[1] Department of Civil and Environmental Engineering, Princeton University, Princeton, NJ, USA
[2] Department of Physical Geography, Utrecht University, Utrecht, the Netherland

Abstract

Rainfall and soil moisture are two key elements in modeling the interactions between the land surface and the atmosphere. Accurate and high-resolution real-time precipitation is crucial for monitoring and predicting the on-set of floods, and allows for alert and warning before the impact becomes a disaster. Assimilation of remote sensing data into a flood-forecasting model has the potential to improve monitoring accuracy. Space-borne microwave observations are especially interesting because of their sensitivity to surface soil moisture and its change. In this study, we assimilate satellite soil moisture retrievals using the Variable Infiltration Capacity (VIC) land surface model, and a dynamic assimilation technique, a particle filter, to adjust the Tropical Rainfall Measuring Mission Multi-satellite Precipitation Analysis (TMPA) real-time precipitation estimates. We compare updated precipitation with real-time precipitation before and after adjustment and with NLDAS gauge-radar observations. Results show that satellite soil moisture retrievals provide additional information by correcting errors in rainfall bias. The assimilation is most effective in the correction of medium rainfall under dry to normal surface condition; while limited/negative improvement is seen over wet/saturated surfaces. On the other hand, high frequency noises in satellite soil moisture impact the assimilation by increasing rainfall frequency. The noise causes larger uncertainty in the
false-alarmed rainfall over wet regions. A threshold of 2 mm/day soil moisture change is identified and applied to the assimilation, which masked out most of the noise.

1 Introduction

Precipitation is perhaps the most important variable in controlling energy and mass fluxes that dominate climate and particularly the terrestrial hydrological and ecological systems. Precipitation estimates, together with hydrologic models, provide the foundation for understanding the global energy and water cycles (Sorooshian, 2004; Ebert et al., 2007). However, obtaining accurate measurements of precipitation at regional to global scales has always been challenging due to its small-scale, space-time variability, and the sparse networks in many regions. Such limitations impede precise modeling of the hydrologic responses to precipitation. There is a clear need for improved, spatially distributed precipitation estimates to support hydrological modeling applications.

In recent years, remotely sensed satellite precipitation has become a critical data source for a variety of hydrological applications, especially in poorly monitored regions such as sub-Saharan Africa due to its large spatial coverage. To date, a number of fine-scale, satellite-based precipitation estimates are now in operational production. One of the most frequently used is the Tropical Rainfall Measuring Mission Multi-satellite Precipitation Analysis (TMPA) product (Huffman et al., 2007). Over the 17 years lifetime since the launch of the Tropical Rainfall Measuring Mission (TRMM) in 1997, a series of high resolution (0.25-degree and 3-hourly), quasi-global (50°S - 50°N), near-realtime, TRMM-based precipitation estimates have been developed and made available to the research and applications communities (Huffman et al., 2007; 2010). Flood forecasting and monitoring is one major application for real time satellite rainfall products (Wu et al, 2014). However, the applicability of satellite precipitation products for near real-time hydrological applications that include drought and flood monitoring has been hampered by their need for gauge-based adjustment.
While it is possible to create such estimates solely from one type of sensor, researchers have increasingly moved to using combinations of sensors in an attempt to improve accuracy, coverage and resolution. A promising avenue for rainfall correction is through the assimilation of satellite-based surface soil moisture into a water balance model (Pan and Wood, 2006). Over land, the physical relationship between variations in soil water storage and rainfall accumulation contain complementary information that can be exploited for the mutual benefit of both types of products (Massari et al., 2014; Crow et al., 2009). Unlike instantaneous rain rate, satellite surface soil moisture retrievals utilize low frequency microwave signals and possess some memory reflecting antecedent rainfall amounts.

Studies have demonstrated that in situ (Brocca et al., 2009, 2013; Matgen et al., 2012) and satellite (Francois et al., 2003; Pellarin et al., 2008, 2013; Brocca et al., 2014) estimates of surface soil moisture could contribute to precipitation estimates by providing useful information concerning the sign and magnitude of antecedent rainfall accumulation errors. In particular, Brocca et al. (2014) estimated daily rainfall on a global scale based on satellite SM products by inverting the soil water balance equation. Crow et al. (2003, 2009, 2011) corrected space-borne rainfall retrievals by assimilating remotely sensed surface soil moisture retrievals into an Antecedent Precipitation Index (API) based soil water balance model using a Kalman filter (Kalman, 1960). However, these studies focused on multi-day aggregation periods and a space aggregated correction at 1° resolution for the corrected precipitation totals. This limits their applicability in applications such as near real-time flood forecasting. Wanders et al. (2015) tried to overcome this limitation by the correction of 3 hourly satellite precipitation totals with a set of satellite soil moisture and land surface temperature observations. One important conclusion by Wanders et al. (2015) is that their results showed the limited potential for satellite soil moisture observations for correcting precipitation at high resolution if “all-weather” – i.e. microwave based – land surface temperatures are not available coincidently, as was the case with AMSR-E.

But this isn’t always the case, and it is also noted that current low-frequency microwave soil moisture missions (specifically SMAP and SMOS) don’t have radiometers at
frequencies useful for estimating land surface temperatures, even though a 37 GHz sensor is part of the AMSR2 system. In fact SMAP and SMOS use LST from weather models analysis fields in their algorithms. Unfortunately the lowest microwave frequency of AMSR2 precludes retrieving soil moisture from many areas with heavy vegetation, and AMSR2 has a significant dry bias with less availability than AMSR-E, but is no longer operable. So improvements to satellite precipitation from the Global Precipitation Mission products must reply solely on satellite soil moisture products, and the improvements to the assimilation algorithms is the goal of this study.

Thus, we focus exclusively on the usefulness of assimilating soil moisture products to improve satellite rainfall. We propose as part of the work how to improve the generation of rain particles and the bias-correction of the satellite soil moisture observations, as well as to enhance the assimilation algorithm to maximize the information that can be gained from using soil moisture alone to adjust precipitation. Due to the very strong and complicated spatial structure of precipitation, that is non-Gaussian and non-stationary in both time and space (Wanders et al., 2015), a more advanced method is applied to generate possible precipitation fields than were used in earlier studies or in Wanders et al, 2015) (see section 2.2.2). Furthermore, a more advanced bias correction method is also applied to account for the reported problems in the second order statistics of the soil moisture retrievals. We used a soil moisture remote sensing product to improve real-time remote sensing precipitation product, TMPA 3B42RT, through a Particle Filter (PF) and therefore offer an improved basis for quantitatively monitoring and predicting flood events, especially in those parts of the world where in-situ networks are too sparse to support more traditional methods of hydrologic monitoring and prediction. The precipitation enhancement experiments are carried out over the continental U.S. (CONUS) and the precipitation skill is validated against the NLDAS gauge-radar precipitation product. Section 5 presents a comparison of the results from this study to the earlier studies related to improving satellite precipitation.
2 Methods

2.1 Overview
Random replicates of satellite precipitation are generated based on real-time TMPA (3B42RT) retrievals and its uncertainty (Pan et al., 2010), which are then used to force the VIC land surface model (LSM) where one output of interest is surface soil moisture. Satellite soil moisture data products are compared and merged with the 3B42RT product to improve the accuracy of the satellite precipitation estimates. A schematic for the study approach is provided in Figure 1. Based on real-time 3B42RT retrievals, a set of possible precipitation estimates (a.k.a. replicates or particles) \( \{ p^i \}_{i=1,2,...,N} \) is generated with assigned initial prior probability weights \( \{ w^i \}_{i=1,2,...,N} \). These rainfall rates are then used to force the VIC land surface model to produce soil moisture predictions \( \{ \theta^i \}_{i=1,2,...,N} \).

Retrievals of AMSR-E satellite surface soil moisture using the Land Surface Microwave Model (LSMEM) (Pan et al., 2014) are then merged with the LSM-based soil moisture within the Particle Filter (PF) that compares AMSR-E/LSMEM changes in soil moisture, \( \Delta SM \), to the LSM predicted soil moisture changes. From these, posterior weights \( \{ w^{i+} \}_{i=1,2,...,N} \) are calculated for each precipitation member (particle) that takes into account the uncertainties of AMSR-E/LSMEM \( \Delta SM \) retrievals. From these updated weights, an updated precipitation probability distribution is constructed, where the precipitation particle with highest probability is taken as the “best” adjusted precipitation estimate (3B42RT_{ADJ}). The procedure is carried out over the continental US (CONUS) region on a grid-by-grid basis (0.25-degree) and a daily time step. Allowing for 6 months model spin-up period, the adjustment is done from January 2003 to July 2007.

2.2 Modeling, Statistical Tools and Data Sources

2.2.1 The Particle Filter
Data assimilation methods are capable of dynamically merging predictions from a state equation (i.e. the land surface model) with measurements (i.e. AMSR-E retrievals) to minimize uncertainties from both the predictions and measurements. It is assumed that
the source of uncertainty in the land surface model predictions come solely from the real-
time satellite precipitation, so that the particle filter (PF) provides an algorithm to update
the precipitation based on the AMSR-E retrievals. The state evolution of a particle filter
from discrete time t-1 to t can be represented as:

\[ \theta_t = f_t(\theta_{t-1}, p_t, \kappa_t, \alpha_t) \] (1)

where \( \theta_t \) is the 1st layer soil moisture at time t, whose value is predicted by the state
equation Eq.(1) as \( f(\cdot) \), and in the study is the hydrological model VIC, which takes in
forcing data, including precipitation (\( p_t \)) and other forcings (\( \kappa_t \)); and simulates land
surface states (soil moisture and soil temperatures at various levels, snow, etc.) and fluxes
(evapotranspiration, runoff) at time t. Herein we are basically interested only in the 1st
layer (top 10cm) soil moisture state and precipitation forcing, so other states and fluxes
are not explicitly shown. \( \alpha_t \) is the random error in the prediction of \( \theta_t \), whose statistics
are known but not its value at any specific time.

At time t, the satellite surface soil moisture retrieval, \( \theta_t' \), can be related to the VIC
modeled 1st layer soil moisture \( \theta_t \) as:

\[ \theta_t' = h_t(\theta_t, \beta_t) \] (2)

where \( h_t \) is taken as a regression that transforms the VIC simulated 1st layer soil
moisture to satellite surface soil moisture. \( \beta_t \) is the noise in this regression relationship.
The two noises \( \alpha_t \) and \( \beta_t \) are assumed to be independent of each other at all times t.

At time t, given a 3B42RT precipitation estimate, \( p_t^\text{sat} \), a set of \( N \) precipitation replicates
\( \{p_i^t\}_{i=1,2,\ldots,N} \) and their associated initial prior probability weight \( \{w_i^t\}_{i=1,2,\ldots,N} \) are
generated.

\[ g(p_t^\text{sat}) \sim \{p_i^t, w_i^t\}_{i=1,2,\ldots,N} \] (3)

\[ \sum_{i=1}^{N} w_i^t = 1 \] (4)

\( g(\cdot) \) is a probability density function. For \( N \) precipitation replicates, \( \{p_i^t\}_{i=1,2,\ldots,N} \), the
propagation of the states from time step (t-1) to t is by the VIC land surface model
represented in Eq.(1). The VIC land surface model simulates the 10cm 1st layer soil moisture, $\{\theta^l_i\}_{i=1,2,...,N}$ for each precipitation replicate.

$$\{\theta^l_i = f_t(\theta_{t-1}, p^i_t, \kappa_t, \alpha_t)\}_{i=1,2,...,N}$$  \hspace{1cm} (5)

with the associated weights assigned to the precipitation member:

$$\{\theta^l_i, w^i\}_{i=1,2,...,N} = \{f_t(\theta_{t-1}, p^i_t, \kappa_t, \alpha_t), w^i\}_{i=1,2,...,N}$$  \hspace{1cm} (6)

If the satellite soil moisture retrieval at time $t$ is $\theta^*_t$, the update of precipitation forcing is accomplished by updating the importance weight of each replicate given the “measurement” $\theta^*_t$:

$$w^i_{t+} \sim g(\theta^i_t|\theta^*_t)$$  \hspace{1cm} (7)

$$\sum_{i=1}^{N} w^i_{t+} = 1$$  \hspace{1cm} (8)

The likelihood function $g(\theta^i_t|\theta^*_t)$ can be derived from $h_t$ and $g(\beta_t)$. The schematic of the utilized strategy is shown in Figure 2, with a synthetic example of a missing rainfall pattern in the TMPA compared with satellite ∆SM. The primary disadvantage of the particle filter is the large number of replicates required to accurately represent the conditional probability densities of $p^i_t$ and $\theta^i_t$. When the measurements exceed a few hundred, the particle filter is not computationally practical for land surface problems. Considering computation efficiency, we set the number of independent particles, $N$, from the prior distribution to be 200.

### 2.2.2 Precipitation Replicates Generation

We generate precipitation replicates, $\{p^i_t\}_{i=1,2,...,N}$, based on statistics comparing NLDAS and 3B42RT precipitation, as shown in Figure 3. Given a 3B42RT precipitation measurement (binned by magnitude), with bin minimum and maximum indicated in Figure 3, precipitation replicates are generated based on the corresponding 15th, 30th, 70th, 85th percentiles and the maximum NLDAS precipitation of the particular quantile bin as follows: 15% of the replicates are generated with values uniformly distributed from 0 and 15th percentile; 15% of replicates with values from 15th to 30th percentile; 20% of replicates with values from 30th percentile to the median; 20% of the replicates generated
from the median to 70\textsuperscript{th}; 15\% with values from 70\textsuperscript{th} to 85\textsuperscript{th} percentile; and 15\% from the 85\textsuperscript{th} percentile to the maximum precipitation value. Note that although the generation of particles is based on statistics calculated from NLDAS, results show little difference generating precipitation ensembles uniformly distributed between 0 and 200 mm/day.

2.2.3 AMSR-E/LSMEM Soil Moisture Retrievals

The soil moisture product is derived from multiple microwave channels of the Advanced Microwave Scanning Radiometer for EOS (AMSR-E) instrument. The retrieval algorithm by Pan et al. (2014) is an enhanced version of the Land Surface Microwave Emission Model (LSMEM). The near surface soil moisture and vegetation optical depth (VOD) are estimated simultaneously from a dual polarization approach that utilizes both horizontal (H) and vertical (V) polarizations measurement by the space-borne sensor. The input AMSR-E brightness temperature comes from the NSIDC AMSR-E/Aqua Daily Global Quarter-Degree Gridded Brightness Temperatures product (overlapping swaths in the same day are truncated so that only the latest one is present). Consequently, the soil moisture retrievals are also gridded at 0.25-degree with one ascending map and one descending map at the daily time step. A maximum threshold value of 0.6 m\textsuperscript{3}/m\textsuperscript{3} has been applied manually to reduce error from open water bodies. According to Pan et al. (2014), the soil moisture dataset based on observations from AMSR-E are shown to be consistent at large scales in terms of reproducing the spatial pattern of soil moisture from VIC land surface model simulation. Ascending soil moisture retrievals (equatorial crossing time 1:30PM local time) is assimilated in this study.

Similarly, while the spatial patterns of the basic statistics of AMSR-E/LSMEM SM retrievals compare well to VIC simulations (Pan et al., 2014), VIC has its top layer (10 cm), which is deeper than the detection depth of AMSR-E, so that the mean and temporal variability of the retrievals are higher than the VIC simulated soil moisture (Figure 4 in Pan et al., 2014). Considering this difference between detection depths, we pre-process soil moisture retrievals for each pixel as follows:

1) Rescale soil moisture retrievals (AMSR-E/LSMEM SM) to have the same minimum and maximum range as VIC simulated 1\textsuperscript{st} layer soil moisture.
2) Calculate a daily soil moisture change. As satellite retrievals are manually truncated to be no more than 0.6 m$^3$/m$^3$ (equivalent to 60mm of water in the top soil layer in VIC), retrievals larger than 0.6 m$^3$/m$^3$ are excluded.

3) Fit a 2$^{nd}$ order polynomial regression model with $\Delta SM$ (all units in mm of water in the top layer) from satellite and VIC simulation on a monthly basis and 3×3 grid scale (window).

After pre-processing, the distribution of soil moisture change matches fairly well with $\Delta SM_{VIC}$ (Figure 4). The mean absolute difference reduces from a spatial average of 5.25 mm/day to 0.71 mm/day, with relatively larger value over eastern CONUS. According to Pan et al. (2014), the no-skill or negative-skill areas occur mostly over eastern dense forests due to vegetation blockage of the soil moisture signal (Pan et al., 2014). The accuracy of soil moisture retrievals is also limited by mountainous topography and the occurrence of snow and frozen ground during winter whose identification from satellite observations is often difficult. For the purpose of this study, we assign zero weight to the 3B42RT$^{ADJ}$ and rely exclusively on the initial 3B42RT precipitation for time steps when the VIC model predicts snow cover or frozen surfaces.

2.2.4 VIC Land Surface Model

The Variable Infiltration Capacity (VIC) model (Liang et al., 1994; Gao et al., 2010) is used to dynamically simulate the hydrological responses of soil moisture to precipitation, surface radiation and surface meteorology. The VIC model solves the full energy and water balance over each 0.25-degree-grid-cell independently, thus ensuring its computational efficiency. The assumption of independency poses limitation on the application of LSM at very high spatial resolution (e.g. 1km×1km) over large areas. Three-layer-soil-moisture is simulated through a soil-vegetation-atmosphere transfer (SVAT) scheme, which also accounts for sub-grid scale heterogeneity of vegetation, soil and topography. A detailed soil moisture algorithm description can be found in Liang et al. (1996). The VIC model has been validated extensively over CONUS by evaluating soil moisture and simulations to observations (Robock et al., 2003; Schaake et al., 2004).
3 Idealized Experiment

Before applying the Particle Filter assimilation algorithm on 3B42RT precipitation estimates, we conducted an idealized experiment where we treat the NLDAS precipitation as the “truth” and the NLDAS precipitation forced VIC simulations as “satellite observed” soil moisture. As an idealized experiment, we adjust TMPA real-time precipitation estimates based on these “satellite observations”. Phase 2 of the North American Land Data Assimilation System (NLDAS-2) rainfall forcing combines hourly WSR-88D radar analyses from the National Weather Service (NWS) and daily gauge reports (~13,000/day) from the Climate Prediction Center (CPC) (Ek et al., 2011). The dataset, with a spatial resolution of 0.125 degree and hourly observations, was pre-processed into 0.25-degree daily precipitation to be consistent with that of 3B42RT and AMSR-E/LSMEM SM datasets. Hourly NLDAS and 3-hourly 3B42RT precipitation is aggregated into daily precipitation defined by a period shifted ~7.5 hours into the future (9:00PM-9:00PM), allowing for a necessary delay for soil moisture to respond to incoming rainfall. The idealized experiment is designed to test whether the algorithm is able to retrieve rainfall forcing with soil moisture change, assuming that the soil moisture observations are 100% accurate.

Results show that, with the knowledge of 1st layer soil moisture change (via the “satellite observations”), the adjustment is able to recover intensity and spatial pattern of forcing precipitation (Figure 5g). Average mean absolute error (MAE) of daily rainfall amount is reduced by 52.9% (2.91 mm/day to 1.37 mm/day) over the region. Figure 5a to Figure 5e shows an example of the recovered rainfall field from the idealized experiment for 27th Oct. 2003. The spatial pattern matches the original NLDAS precipitation well.

3.1 Effect of surface soil saturation

While successfully recovering the general pattern of NLDAS precipitation based on first layer soil moisture, the idealized experiment is not always able to recover the precipitation volume due to the fact that the top layer soil moisture alone does not contain the complete memory of the previous day’s rainfall. Deeper soil moisture, evapotranspiration and runoff also carry part of this information. As the surface gets
wetter, the VIC 1st layer soil moisture has smaller variation. If the incoming precipitation brings the surface to saturation, the VIC model redistributes the soil moisture vertically though vertical moisture flow and generates runoff. Hence soil moisture increments, ΔSM, near saturation are less correlated with incoming precipitation as they change minimally to additional incoming rainfall. An example demonstrating this saturation effect is shown in Figure 5f to Figure 5j. When incoming precipitation brings the surface SM to (near) saturation, there is very limited improvement after the adjustment. Because of the low sensitivity of the soil surface to precipitation, there is little change in ΔSM in response to precipitation variations among the replicates. It is almost always the case that the algorithm is not able to find a “matching” ΔSM. We separately evaluate the skill improvement in the recovered NLDAS precipitation with and without surface saturation. Figure 6 confirms the effect of surface saturation on adjusted precipitation, which is well described in previous studies (e.g. Brocca et al., 2013, 2014). The recovered precipitation, when the surface soil is saturated, only contributes more noise rather than an improvement to the rainfall estimates. The VIC model computes the moisture flow between soil layers using an hourly time step. If the 1st layer soil moisture exceeds its maximum capacity, it is considered to be a surface saturation case. As seen in Figure 5, there is very limited or negative skill in the recovered precipitation under saturated surface soil moisture conditions. Such circumstances are identified and the AMSR-E/LSMEM ΔSM observation disregarded by assigning zero weight to the 3B42RTAdj values. Thus for wetter areas with heavy precipitation that potentially would bring the surface soil moisture to saturation, the 3B42RT product is less likely to be adjusted according to satellite ΔSM and the best precipitation estimate is 3B42RT.

3.2 Effect of SM uncertainty

In the idealized experiment, NLDAS-VIC soil moisture is taken as truth with zero uncertainty associated with (θr). However, this assumption is not valid for real satellite SM retrievals, mean absolute error of which is approximately 3% vol./vol. (McCabe et al., 2005). To consider this, we added error to the “truth” SM (normally distributed with zero mean and standard deviations of 1mm, 2mm, 3mm, 4mm and 5mm), and simulated
the effect of SM uncertainty to evaluate the associated adjustment errors. Figure 7 shows that larger soil moisture observation errors lead to larger error variation after adjustment. This also suggests that soil moisture responds to precipitation non-linearly based on different initial conditions. An estimated wetter surface has lower sensitivity to an incoming rainfall amount, resulting in larger error in the recovered NLDAS precipitation. As shown in Figure 7, the error standard deviation of the recovered NLDAS precipitation increases with surface water content (statistics shown in Table 2). As we add noise larger than N(0,1mm) into “true” SM observation, there is a wet bias of approximately 1 mm/day regardless of 1st layer soil moisture level. This suggests that when the difference between 1st layer SM and saturation is less than 8 mm, the median of the errors in the recovered NLDAS precipitation grows from 0.16 mm/day to 1.89 mm/day when we add N(0,5mm) noise, while inter-quantile range (IQR) increases from 1.71 mm/day to 7.04 mm/day. Acknowledging such a wet bias, to avoid introducing any more unintentional bias in the 3B42RT\textsubscript{ADJ} estimates, we take as zero the uncertainty of AMSR-E/LSMEM SM retrievals, i.e. we take $h_t(\theta_t^*)$ as our single observation $\theta_t^*$ and adjust the 3B42RT estimates accordingly.

It is noteworthy that the soil moisture change is calculated based on previous days’ soil water contents. Therefore errors tend to accumulate over time until they are “re-set” when a significant precipitation event takes place. This type of uncertainty accounts for a small portion of the total error in the adjusted precipitation (black being the no error case in Figure 7 with the “true” change in soil moisture from every time step). As complete global coverage is not provided with each orbit of the AMSR-E sensor, on average 44.01\% of the time steps ($<0.6 \, \text{m}^3/\text{m}^3$) during the study period have observations, with more frequent overpasses at higher latitudes (Figure 4e in Pan et al., 2014). This observation gap unavoidably introduces extra uncertainty in the retrieval of the precipitation signal. To further avoid possible additional errors, we update the forcing rainfall when a $\Delta$SM temporal match ($\pm 0.4 \text{mm}$) is available, and keep the original precipitation if a match isn’t available.
4 Improvement on real-time precipitation estimates and their validation

The adjustment of real TMPA 3B42RT retrievals based on AMSR-E/LSMEM ΔSM is carried out using the methods described in Section 2.2.3, and results from the idealized experiment (Sect. 3) with regard to the circumstances where an adjustment is applied.

An example of TMPA 3B42RT adjustment is provide in Figure 8, where a snapshot of the rainfall field is shown (Figure 8b) and compared with NLDAS on May 26th 2006 and the adjusted rainfall pattern based on AMSR-E/LSMEM ΔSM. The 3B42RT_{ADJ} rainfall field (Figure 8c) is similar in terms of its spatial distribution compared to NLDAS precipitation estimates (Figure 8d).

On average TMPA 3B42RT and AMSR-E/LSMEM ΔSM have a spatial Pearson Correlation Coefficient of 0.37 (Shown in Figure 9, left), compared to 0.52 for the correlation between NLDAS and ΔSM. After the adjustment procedure, the Pearson correlation coefficient between 3B42RT_{ADJ} and AMSR-E/LSMEM ΔSM increases to 0.53 (shown in Figure 9), indicating that the correction method is successful. A below average increase in correlation is found over the western mountainous region, the Great Lakes region and eastern high vegetated and populated region. Additionally, the satellite soil moisture suffers from snow/ice/standing water contamination, which affects the potential for improved results after correction. The 3B42RT_{ADJ} has significant improvement over 3B42RT in terms of long-term precipitation bias. The bias in 3B42RT annual mean precipitation is reduced by 20.6%, from -9.32mm/month spatial average in 3B42RT to -7.40mm/month in 3B42RT_{ADJ} (shown in Figure 9, right). Frequency of rain days generally increases significantly everywhere (Figure 10). The NLDAS data (Figure 10, right) suggests an almost constant drizzling rainfall over parts of the western mountainous area (Montana, Idaho, Wyoming and Colorado), while assimilating AMSR-E/LSMEM ΔSM datasets does not have a signal of higher rainfall frequency (Figure 10, middle). This is possibly due to deficiencies in satellite retrievals over the mountainous areas and frequent presence of snow and ice (3B42RT is not updated under such circumstances).

Figure 11 shows the assimilation results for the grids and days with soil moisture observations, using the NLDAS precipitation as a reference. Overall, the method is
successful in correcting daily rainfall amount when 3B42RT overestimates precipitation (3B42RT - NLDAS > 0). Mean standard deviation (STD) of 3B42RT_{ADJ} - NLDAS is between 1 and 3 mm/day (statistics provided in Table 3). When 3B42RT underestimates rainfall (3B42RT - NLDAS < 0), the assimilation has limited improvement on 3B42RT. This is due to the effect of surface saturation. In terms of adding rainfall, effectiveness of the assimilation is limited under the following two circumstances.

1) The presence of wet conditions or (near) saturation. There is higher probability bringing the surface to saturation (wetter condition) when the assimilation adds rainfall into 3B42RT. However soil moisture increments are less sensitive to incoming precipitation on wetter soil. Therefore, an error in \( \Delta SM \) often translates into 3B42RT_{ADJ} in a magnified manner.

2) The presence of very heavy precipitation, which typically brings the surface to saturation, hence not results in an update of 3B42RT, is not updated. If, by a small probability, the surface is wet (nearly saturated) but not completely saturated after a heavy rainfall, the updated 3B42RT also suffers from large uncertainty (explained in 1 above).

The effect of the assimilation conditioned on 3B42RT rainfall amount is further evaluated by skill scores. Figure 12 presents probability of detection (POD) and false alarm rate (FAR) in 3B42RT and 3B42RT_{ADJ}, using NLDAS as the reference dataset. The rain event threshold is set to be 0.1 mm/day and 2 mm/day. This is possibly due to lower soil moisture variability in satellite retrievals over the dry, mountainous areas and frequent presence of snow and ice (3B42RT is not updated under such circumstances). For a 0.1 mm/day threshold, both FAR and POD increases in 3B42RT_{ADJ} except for the mountainous region. Whereas for a 2 mm/day threshold, there is only slight increase in FAR in most of eastern U.S. region. The overestimation of rain days is also absent when 2 mm/day event threshold is applied which suggests that most of the excessive rainy days have less than 2 mm/day rain amount. Consistent with Wanders et al. (2015), spatially, larger improvements are found in the central U.S. The area coincides where higher AMSR-E/LSMEM \( \Delta SM \) accuracy is found (non-mountainous regions with little urbanization and light vegetation). Despite of the regional variability, these excessive
rainy days are a result of the high-frequency noise in AMSR-E/LSMEM soil moisture retrievals identified by Pan et al. (2004) and Wanders et al. (2015).

The applied method is ineffective for light rainfall < 2 mm, where the adjustment tends to over-correct precipitation by adding excessive rainfall – mostly the result of the high frequency AMSR-E noise. MAE of light rainfall (< 2 mm/day) increased from 0.65 mm/day in 3B42RT to 0.99 mm/day in 3B42RT_{Adj}. On the other hand, satellite soil moisture assimilation is very effective in correcting satellite precipitation larger than 2 mm/day: MAE of medium to large rainfall (≥ 2 mm/day) decreased from 7.07 mm/day in 3B42RT to 6.55 mm/day in 3B42RT_{Adj}. The effect of the assimilation is different over the western mountainous region, the north-to-south central U.S. band and the eastern U.S.

The western mountainous region has a dry climatology with more frequent rainfall in small amounts. The white noise in ΔSM, negatively impacting 3B42RT_{Adj}, is comparable to the positive improvement brought by actual light rainfall signals in ΔSM. Therefore, the assimilation of ΔSM has no significant impact in these regions.

The north-to-south band over central U.S. experiences more medium to large (≥ 2 mm/day) rainfall. In addition, the region is lightly vegetated (annual mean LAI <1) with low elevation (< 1500 m), where soil moisture retrievals are of higher accuracy. Soil moisture climatology is wetter in the west, causing larger variations in 3B42RT_{Adj} error from the white noise ΔSM (as discussed in Section 3.2). Despite of that, satellite soil moisture is most effective correcting medium to large rainfall under normal surface conditions.

The decreased skill in 3B42RT_{Adj} over eastern U.S. is primarily attributed to both precipitation and soil moisture climatology, a wet climate with more medium to large rainfall, neither of which is suitable for soil moisture assimilation.

In summary, the high-frequency noise in soil moisture product causes a major limitation. The noise impacts adjusted precipitation by introducing false alarm rain days. It is difficult to distinguish the noise and retrieve the true rainfall signals. A remedy to prevent the excessive rain days is applying a cutoff ΔSM threshold when rain days are added, at the expense of neglecting a part of the true rainfall signals. Figure 13 shows the probability of added rainy days being consistent with NLDAS (NLDAS > 0 mm/day).
with respect to \( \Delta SM \). When a new rainy day is added (3B42RT = 0 mm/day, 3B42RT_{\text{ADJ}} > 0 \text{ mm/day}) based on AMSR-E/LSMEM \( \Delta SM \) of 2 mm/day, there's approximately 78% chance that the added rain day is a true event (NLDAS > 0 mm/day); That is, approx. 22% chance that it is a false alarm (NLDAS = 0 mm/day). When AMSR-E/LSMEM \( \Delta SM \) is larger than 2 mm/day, the probability of added rainy days being true event is even higher, up to 90% chance. Here we applied a threshold of 2 mm/day on AMSR-E/LSMEM \( \Delta SM \). That is, when new rainy days are introduced (3B42RT > 0, 3B42RT_{\text{ADJ}} > 0), we discard the update and keep the no-rain day if AMSR-E/LSMEM soil moisture increment is below 2 mm. Note that, the probability of the false alarms depends on soil moisture climatology: the wetter soil moisture climatology, the larger uncertainty in the signal. Therefore, this threshold should vary in accordance with local soil moisture climatology, i.e. a larger threshold over the wetter east U.S. and smaller threshold over the drier western U.S. Nevertheless, after the 2 mm/day \( \Delta SM \) threshold is applied, expectedly, the statistics are largely improved: FAR is decreased significantly from 0.519 (wo. \( \Delta SM \) threshold) to 0.066 (w. \( \Delta SM \) threshold). MAE of light rainfall (< 2 mm/day) in 3B42RT_{\text{ADJ}} decreased from 0.99 mm/day to 0.64 mm/day, compared to 0.65 mm/day in 3B42RT. For medium to large 3B42RT rainfall (\( \geq 2 \) mm/day), it effectively increased POD (0.362 in 3B42RT vs 0.386 in 3B42RT_{\text{ADJ}} w. \( \Delta SM \) threshold) and decreased FAR (0.037 in 3B42RT vs 0.030 in 3B42RT_{\text{ADJ}} w. \( \Delta SM \) threshold). Further work is needed to characterize, distinguish and decrease the high-frequency noise in SM retrievals. Figure 13 gives an example of evaluating the impact of SM uncertainties in assimilation as curves derived over different topography can be quantitatively compared.

5 Comparison to other studies

Many other studies have utilized satellite microwave brightness temperatures or soil moisture retrievals to constrain satellite precipitation estimates (Pellarin et al., 2008), estimate precipitation (e.g. Brocca et al., 2013) or improve precipitation estimates through assimilation (Crow et al., 2009, 2011). Here, we review their approaches and findings in light of the results of this study, and compare our results with some of these studies to gain insight into their robustness and consistency.
Pellarin et al. (2008) used the temporal variations of the AMSR-E 6.7 GHz brightness temperature (TB) normalized polarization difference, $PR=(TB_V-TB_H)/(TB_V+TB_H)$, to screen out anomalous precipitation events from a 4-day cumulative satellite-estimated precipitation (EPSAT-SG: Chopin et al., 2005) from 22 to 26 of June 2004 over a 100 x 125 km box centered over Niger in west Africa. This was extended in Pellarin et al. (2013) where an API-based water balance model was used to correct three different satellite precipitation products (CMORPH, TRMM-3B42 and PERSIANN) over a 4-year period in west Africa at three 0.25° grids in Niger, Benin and Mali. The new algorithm was evaluated by comparing the corrected precipitation to estimates over the 0.25° grids from ground-based precipitation measurements. A sequential assimilation approach was applied where AMSR-E C-band TB measurements were used to estimate a simple multiplicative factor to the precipitation estimates in order to minimize the difference between observed (AMSR-E) and simulated TBs in term of root mean square error (RMSE). The results show improvements over those found in Pellarin et al. (2009). Specifically, the Pellarin et al. (2013) study shows that the proposed methodology produces an improvement of the RMSE at daily, decadal and monthly time scales and at the three locations. For instance, the RMS mean error decreases from 7.7 to 3.5 mm/day at the daily time scale in Niger and from 18.3 to 7.7 mm/day at the decadal time scale in Mali.

Crow et al. (2003, 2009, 2011) demonstrated the effectiveness of the assimilation of remotely sensed microwave brightness temperatures or retrieved soil moisture in estimating precipitation based on airborne measurements over the Southern Great Plains (USA) region (Crow et al., 2003); 2 to 10 day accumulated precipitation within a simple API water budget model and assimilation scheme over CONUS (Crow et al., 2009); and 3 day, 1° precipitation accumulation over three African Monsoon Multidisciplinary Analysis (AMMA) sites in west Africa with an enhanced assimilation scheme and an API-moisture model (Crow et al., 2011). Crow et al. (2009) recommends against estimating precipitation at a larger scale than three days based on assimilating AMSR-E/LSMEM soil moisture.

Brocca et al. (2013) estimated precipitation by inverting the water budget equation such that precipitation could be estimated from changes in soil moisture. The inverted equation
was calibrated using in-situ, 4-day averaged observations at two sites in Spain and Italy. In Brocca et al. (2014), the same approach was used globally to estimate daily precipitation at 1° spatially. 5 Day cumulated rainfall estimates are derived from three satellite derived soil moisture datasets (AMSR-E LPRM, ASCAT and SMOS), and linearly interpolated to daily values, for their precipitation estimation algorithm. No formal data assimilation was carried out. The newly created precipitation data set was compared to two satellite precipitation products (TRMM-3B42RT, GPCC) and two gauge based precipitation products (GPCP, ERA-Interim). Five-day accumulated rainfall data, aggregated to a 1° spatial resolution, are considered in their assessment analyses with promising results. But they do note that their approach has “poor scores in reproducing daily rainfall data”. Ciabatta et al. (2015) derived daily rainfall product using ASCAT over Italy and integrated with TMPA 3B42RT precipitation. The merged product also shows promising results.

In the study reported here, four advances have been made over these earlier studies: (i) we adopted a state-of-the-art dynamic land surface model that has demonstrated high skill in simulating soil moisture when driven by high quality precipitation data (Schaake et al., 2004); (ii) we applied a state-of-the-art data assimilation procedure based on particle filtering so as to extract (and hopefully maximize) the information content from the satellite most effectively; (iii) we increased the resolution of the precipitation estimation window down to 1 day, exceeding the conclusions in these earlier studies that the finest temporal resolution is 3 to 5 days. Additionally we increased (or matched) the spatial resolution to 0.25°, limited primarily by the satellite soil moisture product resolution; and (iv) previous studies are based on the assumption that the SM retrievals are 100% accurate and contain no errors. We evaluated this assumption by analyzing the impact of uncertainties associated with the soil moisture retrievals. These advances offer important benefits when satellite precipitation products are used for applications such as flood forecasting. Admittedly by aggregating in space and time, the improvement is more robust since some errors are averaged out.

Wanders et al. (2015) performed a comprehensive inter-comparison study using multiple satellite soil moisture and land surface temperature (LST) data at fine temporal scale (3-hourly). Compared to their study, ours focuses on using soil moisture exclusively from
one satellite and retrieval algorithm, and in improvements to the assimilation algorithm. Specifically, (i) the longer temporal period (2010-2011 in Wanders, et al. versus 2002-2007 in this study), (ii) the temporal resolution (3-hourly versus daily); (iii) the particle generation and bias correction method. We present in the paper improvements in the generation of rain particles and the bias-correction of the satellite soil moisture observations, as well as enhancements to the assimilation algorithm to maximize the information that can be gained from using soil moisture alone in adjusting precipitation.

Due to the very strong and complicated spatial structure of precipitation, that is non-Gaussian and non-stationary in both time and space, a more advanced method is applied to generate possible precipitation fields than used or presented in earlier studies or in Wanders et al, (2015). Furthermore, a more advanced bias correction method is also applied to account for the reported problems (Wanders et al., 2015) in the second order statistics of the soil moisture retrievals; and (iv) SM retrieval products (and overpasses) used in assimilation. Our improved results are based on soil moisture retrievals from ascending overpasses only (versus both descending and ascending overpasses from multiple datasets, i.e. AMSR-E/LSMEM, ASCAT and SMOS). Our exclusive focus on the usefulness of soil moisture product promises more applicability especially for improving satellite precipitation from the Global Precipitation Mission products. The descending overpasses have generally better performance than the ascending, suggesting the potentials of further improvements.

A quantitative comparison of Wanders et al. (2015) and our results is provided below. Despite of the different time periods between Wanders et al. (2015, 2010-2011) and in our study (2002-2007), Wanders et al. (2015) shows decreasing POD (-15.0% to -46.4% depending on different products used) and FAR (-47.2% to -89.1% depending on different products used) for all rainfall after assimilation using either (single or multiple) SM products alone or SM + LST data combined (see Table 4 of Wanders et al., 2015). While in our study, after applying ΔSM threshold, medium to large 3B42RT_{ADJ} rainfall (≥ 2 mm/day) has an increase in POD (+6.6%) and decrease in FAR (-18.9%). Furthermore, the significant dry bias in adjusted precipitation (see Fig.6 of Wanders et al., 2015) is not present in our results (Figure 9). This is due to improvements in our precipitation ensemble generation and bias correction scheme. Wanders et al. (2015)
applied an additional step generating precipitation particles sampling from a $3 \times 3$ window that over-eliminates most of the excessive rainfall along with some real signal. We suggest loosening this constraint to a larger window size or to sample from adjusted precipitation instead of original 3B42RT precipitation. However, sampling from adjusted precipitation at each time step would significantly increase the computational demand, limiting the potential for a global application at high temporal/spatial resolution.

Furthermore, the outcome is quite different for the distribution of soil moisture retrievals after pre-processing (Fig. 9 of Wanders et al. 2015 vs Figure 4 in our study) due to different methods used. After pre-processing, distributions of soil moisture retrievals is more similar to that of NLDAS precipitation forced, VIC modeled 1st layer soil moisture. CDF-matching used by Wanders et al., (2015) is based on the assumption that satellite soil moisture and modeled soil moisture respond to heavy rainfall in the same way – essentially having a rank correlation of 1. However that is not observed because of shallower detection depth of the satellite soil moisture. On the other hand, using the pre-processing method presented in this study, the signal of near-saturation in AMSR-E/LSMEM ∆SM tends to be overestimated after pre-processing, which indicates a heavy rain event that is often accompanied with surface saturation and thus does not provide effective information for the assimilation. The other benefit of the 2nd order polynomial regression lies in its non-linearity. An error in the soil moisture product impacts the precipitation adjustment in a predictable way, allowing for a more systematic post-processing treatment. Based on the known error characteristics, we demonstrate a potential remedy to deal with the error by applying a 2 mm/day cutoff ∆SM threshold.

Meanwhile, it is also highlighted that the cutoff threshold should be variable and positively correlated with local soil moisture climatology. We acknowledge that the soil moisture product used in Wanders et al. (2015), is a blended product of multiple satellite soil moisture datasets. It is not clear how its error characteristics impact the adjusted precipitation.

6 Conclusion and Discussion

Based on the retrieved soil moisture from AMSR-E using the LSMEM retrieval algorithm, we propose an assimilation procedure to integrate soil moisture information
into the VIC land surface model so as to improve real-time, satellite precipitation estimates. The ability to estimate rainfall amount is now enhanced with the above improvements, especially for correcting medium rainfall amounts. However, constrained by the noise in AMSR-E TBs and thus soil moisture retrievals, the assimilation is not effective in detecting missed rainfall events. The improved precipitation estimates, referred to as 3B42RT\textsubscript{ADJ} estimates, are overall consistent in reproducing the spatial pattern and time series of daily rainfall from NLDAS precipitation. The results illustrate the potential benefits of using data assimilation to merge satellite retrievals of surface soil moisture into a land surface model forced with real-time precipitation. Potentially the method can be applied globally for areas meeting vegetation cover and surface condition constraints that allows for soil moisture retrievals. Under these conditions, the approach can provide a supplementary source of information for enhancing the quality of satellite rainfall estimation, especially over poorly gauged areas like Africa.

Nonetheless, some caution is required. The results of this study show that the adjusted real-time precipitation tends to add additional rain (frequency) resulting in more time steps with rain but lower regional average in the western U.S. and slightly higher regional average in the eastern U.S. It is also noticed that the precipitation adjustments are insensitive under saturated soil moisture conditions. A wetter surface magnifies any error associated with satellite observation by incorrectly adjusting precipitation. These errors, mixed with the “real” signal, generally add approximately $\sim$2mm of precipitation (or higher) depending on the soil moisture climatology. It is important to consider these circumstances when observations are used so as to avoid introducing additional error.

With these identified limitations, continued research is needed to assess the biases in the real-time precipitation retrievals on a local to regional basis so the assimilation system can be modified accordingly.

The assimilation scheme used here assumed that the errors were attributed to the real-time precipitation retrievals, but the precipitation estimates after adjustment includes errors from additional sources. The two primary sources are errors in soil moisture retrievals and errors in the land surface model that include model parameterizations (poorly or insufficiently represented processes as well as scale issues) and parameter errors (insufficient calibration). There are also errors in other model forcing fields besides...
precipitation. Further studies are needed to assess the attribution of these error sources to
the total error. Such research will further improve the use of real-time satellite-based
precipitation for global flood monitoring.

Besides the clear, heavy dependency of the assimilation effectiveness on the accuracy of
satellite soil moisture product, it is also important to acquire adequate knowledge on the
error characteristics of satellite soil moisture retrievals. Knowledge of the soil moisture
ersors could be important and the assimilation methods (including precipitation ensemble
generation and pre-/post-processing method) should be chosen accordingly. On the other
hand, the presence of data gaps between overpasses could be a large source of uncertainty
with data assimilation. Further effort towards reliable spatial-temporal continuous (gap
filled) satellite soil moisture datasets is needed.

While it has been illustrated in this study that the enhancement of real time satellite
precipitation estimates can be realized through an assimilation approach using satellite
soil moisture data products and a particle filter, additional satellite-based observations
(e.g. multi-sensor soil moisture products) or variables (e.g. land surface temperatures as
shown in Wanders et al. 2015, inundated areas), could be added/replaced in the
assimilation process with different levels of complexity; e.g. by applying constraints on
the particle generation. This opens up a great number of opportunities in using space-
borne observations for supplementing direct retrievals of precipitation.

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acknowledged.
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Figure 10 Frequency of rainy days in 3B42RT, 3B42RT_{ADJ} and NLDAS with a) 0.1 mm/day and b) 2 mm/day rainfall threshold to define a rain day.

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Figure 12 FAR and POD of 3B42RT (top) and 3B42RT_{ADJ} (bottom) with a) 0.1 mm/day and b) 2 mm/day rainfall threshold to define a rain event.

Figure 13 Probability that the added rainy days (3B42RT = 0 mm/day, 3B42RT_{ADJ} > 0 mm/day) are true rain events (NLDAS > 0 mm/day) given corresponding AMSR-E/LSMEM ΔSM.
### Table 1: Error statistics of recovered precipitation and effect of surface saturation in the idealized experiment (mm/day).

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Table 2 Error statistics of recovered NLDAS based on ΔSM (with added errors) conditioned on 1st layer soil wetness for the idealized experiment (mm/day).

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*1st layer soil depth is 100mm with a SM capacity of ~45mm depending on porosity.
Table 3 Error statistics of 3B42RT and 3B42RT<sub>ADJ</sub> compared to NLDAS precipitation (mm/day)

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Figure 1 Schematic for the dynamic assimilation of AMSR-E/LSMEM ΔSM into TMPA (3B42RT) with the particle filter (PF).
Figure 2 Schematic for the strategy for processing prior and posterior probability densities in the particle filter. The missing rainfall event in TMPA (circled in the right panel of a), correspond to red triangle in b) against satellite signals as detected by AMSR-E/LSMEM ΔSM (circled in the left panel of a), correspond to red triangle in c)), and recovered by assimilating AMSR-E/LSMEM ΔSM into TMPA (marked by red triangle in d)).
Figure 3 Statistics of NLDAS precipitation given 3B42RT precipitation measurement. Boxplot shows the minimum, 15% quantile, 30% quantile, median, 70% quantile, 85% quantile and maximum value of NLDAS precipitation given 3B42RT precipitation in a certain bin.
Figure 4 Empirical cumulative distribution function of changes in soil moisture from top layer soil moisture from NLDAS precipitation forced VIC simulation (black), and AMSR-E/LSMEM soil moisture retrieval before (red) and after (blue) pre-processing.
Figure 5 Two cases with recovered spatial rainfall pattern in the idealized experiment after merging satellite soil moisture retrieval on: (a-e) 27th Oct. 2003 and (f-j) 22th Mar. 2006.
Figure 6 Accuracy of recovered precipitation in idealized experiment: (a) overall performance and separately comparing the improvement performance of recovered NLDAS precipitation (b) with and (c) without surface saturation condition. Statistics provided in Table 1.
Figure 7 Error in recovered NLDAS precipitation given surface moisture condition. Recovered NLDAS is based on “truth” soil moisture and soil moisture with normal error: N(0.1mm), N(0.2mm), N(0.3mm), N(0.4mm) and N(0.5mm). Statistics provided in Table 2.
Figure 8 May 26th 2006 Rainfall pattern in 3B42RT (b) against NLDAS (d) as detected by AMSR-E/LSMEM ΔSM (a), and recovered rainfall field (3B42RT_{adj}) by assimilating AMSR-E/LSMEM ΔSM (c). Gray shading shows area without soil moisture retrievals.
Figure 9 Pearson correlation coefficient between AMSR-E/LSMEM ΔSM and precipitation (from 2003/01/01 to 2007/07/31): a) NLDAS, b) 3B42RT and c) 3B42RT ADJ; annual mean precipitation in d) NLDAS, e) 3B42RT and f) 3B42RT ADJ of time steps with AMSR-E/LSMEM ΔSM retrievals.
Figure 10 Frequency of rainy days in 3B42RT, 3B42RT\textsubscript{ADJ} and NLDAS with a) 0.1 mm/day and b) 2 mm/day rainfall threshold to define a rain day.
Figure 11 Distribution of 3B42RT and 3B42RT_{ADJ} precipitation error compared to NLDAS. Statistics are provided in Table 3.
Figure 12 FAR and POD of 3B42RT (top) and 3B42RT_{ADJ} (bottom) with a) 0.1 mm/day and b) 2 mm/day rainfall threshold to define a rain event. The significant increase in FAR for all rainfall events (bottom left, a)) is not present for rainfall larger than 2 mm/day (bottom left, b)).
Figure 13 Probability that the added rainy days \((3B42RT = 0 \text{ mm/day}, \ 3B42RT_{\text{adj}} > 0 \text{ mm/day})\) are true rain events \((\text{NLDAS} > 0 \text{ mm/day})\) given corresponding AMSR-E/LSMEM \(\Delta SM\).