

# Long-term and high frequency non-destructive monitoring of water stable isotope profiles in an evaporating soil column

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## Abstract

The stable isotope compositions of soil water ( $\delta^2\text{H}$  and  $\delta^{18}\text{O}$ ) carry important information about the prevailing soil hydrological conditions and for constraining ecosystem water budgets. However, they are highly dynamic, especially during and after precipitation events. In this study, we present an application of a method based on gas-permeable tubing and isotope-specific infrared laser absorption spectroscopy for *in situ* determination of  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$ . We conducted a laboratory experiment where a sand column was initially saturated, exposed to evaporation for a period of 290 days, and finally rewatered. Soil water vapor  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  were measured daily at each of eight available depths. Soil liquid water  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  were inferred from those of the vapor assuming thermodynamic equilibrium between liquid and vapor phases in the soil. The experimental setup allowed following the evolution of soil water  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  profiles with a daily temporal resolution. As the soil dried, we could also show for the first time the increasing influence of the isotopically depleted ambient water vapor on the isotopically enriched liquid water close to the soil surface (i.e., atmospheric invasion). Rewatering at the end of the experiment led to instantaneous resetting of the stable isotope profiles, which could be closely followed with the new method.

From simple soil  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  gradients calculations, we showed that the gathered data allowed to determinate the depth of the Evaporation Front (EF) and how it receded into the soil overtime. It was inferred that after 290 days under the prevailing experimental conditions,

1 the EF had moved down to an approximate depth of  $-0.06$  m. Finally, data was used to  
2 calculate evaporation lines' slopes and test the formulation for isotope kinetic effects. A very  
3 good agreement was found between measured and simulated values (Nash and Sutcliffe  
4 Efficiency - NSE = 0.92) during the first half of the experiment, i.e., until the EF reached a  
5 depth of  $-0.04$  m. From this point, calculated kinetic effects associated with the transport of  
6 isotopologues in the soil surface air layer above the EF provided slopes lower than observed.  
7 Finally, values of isotope kinetic effects that provided the best model-to-data fit (NSE > 0.9)  
8 were obtained from inverse modelling, highlighting uncertainties associated with the  
9 determinations of isotope kinetic fractionation and soil relative humidity at the EF.

10

## 11 **1 Introduction**

12 Stable isotopologues of water, namely  $^1\text{H}^2\text{H}^{16}\text{O}$  and  $^1\text{H}_2^{18}\text{O}$  are powerful tools used in a wide  
13 range of research disciplines at different and complementary temporal and spatial scales. They  
14 provide ways of assessing the origin of water vapor (e.g., Craig, 1961; Liu et al., 2010),  
15 solving water balances of lakes (Jasechko et al., 2013) and studying groundwater recharge  
16 (Blasch and Bryson, 2007; Peng et al., 2014). Analysis of the isotope compositions ( $\delta^2\text{H}$  and  
17  $\delta^{18}\text{O}$ ) of soil surface and leaf waters allows for partitioning evapotranspiration into  
18 evaporation and transpiration (e.g., Dubbert et al., 2013; Hu et al., 2014; Rothfuss et al., 2012;  
19 Yopez et al., 2005).

20 Moreover, from soil water  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  profiles, it is also possible to derive quantitative  
21 information, such as soil evaporation flux, locate evaporation fronts, and root water uptake  
22 depths (Rothfuss et al., 2010; Wang et al., 2010). Zimmermann et al. (1967) and later Barnes  
23 and Allison (1983, 1984) and Barnes and Walker (1989) first analytically described soil  
24  $^1\text{H}^2\text{H}^{16}\text{O}$  and  $^1\text{H}_2^{18}\text{O}$  movement at steady / non-steady state and in isothermal/ non-isothermal  
25 soil profiles. Between precipitation events, the soil water  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  profiles depend on  
26 flux boundary conditions, i.e., fractionating evaporation and non-fractionating capillary rise as  
27 well as on soil properties (e.g., soil tortuosity). In a saturated soil, the isotope excess at the  
28 surface due to evaporation diffuses back downwards, leading to typical and well documented  
29 exponential-shaped  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  profiles. For an unsaturated soil, assuming in a first  
30 approximation that isotope movement occurs in the vapor phase above the soil "evaporation  
31 front" (EF) and strictly in the liquid phase below it, the maximal  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  values are no  
32 longer observed at the surface but at the depth of EF. Above the EF, in the so-called "vapor

1 region”, according to Fick’s law, soil water  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  decrease towards the depleted  
2 ambient atmosphere water vapor  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$ . Braud et al. (2005), Haverd and Cuntz (2010),  
3 Rothfuss et al. (2012), Singleton et al. (2004), and Sutanto et al. (2012) implemented the  
4 description of the transport of  $^1\text{H}^2\text{H}^{16}\text{O}$  and  $^1\text{H}_2^{18}\text{O}$  in physically based soil-vegetation-  
5 atmosphere transfer (SVAT) models (HYDRUS 1D, SiSPAT-Isotope, Soil-Litter iso,  
6 TOUGHREACT). In these models, movement of soil  $^1\text{H}^2\text{H}^{16}\text{O}$  and  $^1\text{H}_2^{18}\text{O}$  occur in both  
7 phases below and above the EF, and heat and water transports are properly coupled.

8 However, these tools suffer from the comparison with other “traditional” methods developed  
9 to observe and derive soil water state and transport. In contrast with soil water content and  
10 tension measured by, e.g., time-domain reflectometry and tensiometry, isotope compositions  
11 of soil water are determined either following destructive sampling or non-destructively but  
12 with poor spatial and temporal resolution (i.e., with section cups in combination with  
13 lysimeters for soil water tension higher than  $-600$  hPa, e.g., Goldsmith et al., 2011, Litaor,  
14 1988). This greatly limits their informative value. Only since recently, non-destructive  
15 methodologies based on gas-permeable membrane and laser spectroscopy can be found in the  
16 literature (Rothfuss et al., 2013; Herbstritt et al., 2012; Volkmann and Weiler, 2014, Gaj et  
17 al., 2015).

18 The central objective of this study was to demonstrate that a direct application of the method  
19 of Rothfuss et al. (2013) to a soil column would allow monitoring soil water  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$   
20 profiles in the laboratory with high temporal resolution and over a long time period. We will  
21 demonstrate that the obtained isotope data can be used to locate the evaporation front as it  
22 recedes into the soil during the experiment. Finally, data will be also used to test the  
23 expression proposed by Gat (1971) and based on the Craig and Gordon (1965) of evaporation  
24 lines’ slopes.

25

## 26 **2 Material and methods**

### 27 **2.1 Isotopic analyses**

28 Isotopic analysis of liquid water and water vapor was performed using a cavity ring-down  
29 spectrometer (L1102-i, Picarro, Inc., Santa Clara, CA, USA), calibrated against the  
30 international primary water isotope standards V-SMOW2, GISP, and SLAP by liquid water  
31 injection into the vaporizer of the analyzer. Primary and working standards’ isotope

1 compositions were measured at 17,000 ppmv water vapor mixing ratio (number of replicates  
2 = 4, number of injections per replicate = 8). Mean values and standard deviations were  
3 calculated omitting the first three values of the first replicate to account for a potential  
4 memory effect of the laser spectrometer. The laser spectrometer's dependence on water vapor  
5 mixing ratio was also investigated according to the method of Schmidt et al. (2010).  
6 Hydrogen and oxygen isotope ratios of water are expressed in per mil (‰) on the  
7 international "delta" scale as defined by Gonfiantini (1978) and referred to as  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$ ,  
8 respectively.

## 9 **2.2 Soil column and measurements**

10 The experiment was conducted in a  $0.0057\text{ m}^3$  acrylic glass column (0.11 m inside diameter,  
11 0.60 m height, Fig. 1a). The bottom of the column consisted of a porous glass plate ( $10\text{ }10^{-6}\text{ m}$   
12  $<$  pore size diameter  $< 16\text{ }10^{-6}\text{ m}$  (4<sup>th</sup> class), Robu® GmbH, Hattert, Germany) connected to a  
13 two-way manual valve (VHK2-01S-06F, SMC Pneumatik GmbH, Germany).

14 Three ports were available at each of eight different depths (−0.01, −0.03, −0.05, −0.07, −0.10,  
15 −0.20, −0.40, and −0.60 m): one inlet for the carrier gas, i.e., synthetic dry air (20.5 % O<sub>2</sub> in  
16 N<sub>2</sub>, with approx. 20-30 ppmv water vapor; Air Liquide, Germany), one sample air outlet, and  
17 one duct for a soil temperature ( $T_s$ ) sensor (type K thermocouple, Greisinger electronic  
18 GmbH, Regenstauf, Germany; precision: 0.1°C). An additional fourth port at depths −0.01, −  
19 0.03, −0.05, −0.10, −0.20, and −0.60 m was used for the measurement of soil volumetric water  
20 content ( $\theta$ ) (EC-5, Decagon Devices, USA; precision:  $0.02\text{ m}^3\text{ m}^{-3}$ ).

21 At each depth inside the column a 0.15 m long piece of microporous polypropylene tubing  
22 (Accurel® PP V8/2HF, Membrana GmbH, Germany;  $1.55\text{ }10^{-3}\text{ m}$  wall thickness,  $5.5\text{ }10^{-3}\text{ m}$   
23 inside diameter,  $8.6\text{ }10^{-3}\text{ m}$  outside diameter) was connected to the gas inlet and outlet port.  
24 The tubing offers the two advantages of being gas-permeable (pore size of  $0.2\text{ }10^{-6}\text{ m}$ ) and  
25 exhibiting strong hydrophobic properties to prevent liquid water from intruding into the  
26 tubing. It allows sampling of soil water vapor and, hence, the determination of the isotope  
27 composition of soil liquid water ( $\delta_{\text{Sliq}}$ ) in a non-destructive manner considering  
28 thermodynamic equilibrium between liquid and vapor phases as detailed by Rothfuss et al.  
29 (2013).

## 1 **2.3 Internal isotope standards**

2 Two internal standards (“st1” and “st2”) were prepared using the same procedure as described  
3 by Rothfuss et al. (2013). Two closed acrylic glass vessels (0.122 m i.d., 0.22 m height), in  
4 each of which a 0.15 meter long piece of tubing as well as a type K thermocouple were  
5 installed, were filled with FH31 sand (porosity =  $0.34 \text{ m}^3 \text{ m}^{-3}$ , dry bulk density =  $1.69 \cdot 10^3 \text{ kg}$   
6  $\text{m}^3$ , particle size distribution: 10% ( $> 0.5 \cdot 10^{-3} \text{ m}$ ), 72% ( $0.25 - 0.5 \cdot 10^{-3} \text{ m}$ ), and 18% ( $< 0.25$   
7  $\cdot 10^{-3} \text{ m}$ )) (Merz et al., 2014; Stingaciu et al., 2009). Each vessel was saturated with water of  
8 two different isotope compositions:  $\delta^2\text{H}_{\text{st1}} = -53.51 (\pm 0.10) \text{ ‰}$ ,  $\delta^{18}\text{O}_{\text{st1}} = -8.18 (\pm 0.06) \text{ ‰}$   
9 and  $\delta^2\text{H}_{\text{st2}} = +15.56 (\pm 0.12) \text{ ‰}$ ,  $\delta^{18}\text{O}_{\text{st2}} = +8.37 (\pm 0.04) \text{ ‰}$ . Soil water vapor from each  
10 vessel was sampled eight times per day for 30 min during the whole experiment.

## 11 **2.4 Atmospheric measurements**

12 Laboratory air was sampled passively with a 1/8” three meter-long stainless steel tubing at 2  
13 m above the sand surface for isotope analysis of water vapor ( $\delta_a$ ). Air relative humidity ( $rh$ )  
14 and temperature ( $T_a$ ) were monitored at the same height with a combined  $rh$  and  $T_a$  sensor  
15 (RFT-2, UMS GmbH, Germany; precision for  $rh$  and  $T_a$  were 2 % and  $0.1^\circ\text{C}$ , respectively).  
16 Vapor pressure deficit ( $vpd$ ) was calculated from  $rh$  and  $T_a$  data using the Magnus-Tetens  
17 formula (Murray, 1967) for saturated vapor pressure. The laboratory was air-conditioned and  
18 ventilated with seven axial fans (ETRI 148VK0281,  $117 \text{ l s}^{-1}$  airflow, ETRI/Rosenberg, USA)  
19 positioned at 1.80 m height above the sand surface.

## 20 **2.5 Sampling protocol and applied isotopic calibrations**

21 The column was filled in a single step with FH31 sand and carefully shaken in order to reach  
22 a dry bulk density close to *in situ* field conditions. The sand was then slowly saturated from  
23 the bottom from an external water tank filled with st1 water on December 2, 2013. After  
24 saturation, the column was disconnected and sealed at the bottom using the two-way manual  
25 valve. It was finally installed on a balance (Miras 2 – 60EDL, Sartorius, USA), and let to  
26 evaporate for a period of 290 days in a ventilated laboratory.

27  $\delta_{\text{Sliq}}$  was determined in a sequential manner at each available depth once a day following the  
28 method developed by Rothfuss et al. (2013) (Fig. 1b). Dry synthetic air at a rate of  $50 \text{ ml min}^{-1}$   
29 from a mass flow controller (EL-FLOW Analog, Bronkhorst High Tech, Ruurlo, The  
30 Netherlands) was directed to the permeable tubing for 30 minutes at each depth. The sampled

1 soil water vapor was diluted with dry synthetic air provided by a second mass flow controller  
 2 of the same type. This allowed (i) reaching a water vapor mixing ratio ranging between  
 3 17,000 and 23,000 ppmv (where L1102-i isotope measurements are most precise) and (ii)  
 4 generating an excess flow downstream of the laser analyser. By doing this, any contamination  
 5 of sample air with ambient air would be avoided. The excess flow was measured with a  
 6 digital flow meter (ADM3000, Agilent Technologies, Santa Clara, CA, USA). The last 100  
 7 observations (corresponding to approx. 10 minutes) at steady state (standard deviations <0.70  
 8 ‰ and <0.20 ‰ for  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$ , respectively) were used to calculate the raw isotope  
 9 compositions of soil water vapor ( $\delta_{\text{Svap}}$ ). The latter was corrected for the water vapor mixing  
 10 ratio dependence of the laser analyzer readings with 17,000 ppmv as reference level.  
 11 Measurements that did not fulfil the above mentioned conditions for  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  standard  
 12 deviations were not taken into account. Finally, these corrected values were used to infer the  
 13 corresponding  $\delta_{\text{Sliq}}$  at the measured  $T_{\text{S}}$  (Eq. (1) and (2); taken from Rothfuss et al., 2013):

$$14 \quad \delta^2\text{H}_{\text{Sliq}} = 104.96 - 1.0342 \cdot T_{\text{S}} + 1.0724 \cdot \delta^2\text{H}_{\text{Svap}} \quad (1)$$

$$15 \quad \delta^{18}\text{O}_{\text{Sliq}} = 11.45 - 0.0795 \cdot T_{\text{S}} + 1.0012 \cdot \delta^{18}\text{O}_{\text{Svap}} \quad (2)$$

16 The isotope composition of laboratory water vapor ( $\delta_{\text{a}}$ ) was measured eight times a day.  $\delta_{\text{a}}$ ,  
 17  $\delta_{\text{Svap}}$ , and  $\delta_{\text{Sliq}}$  values were finally corrected for laser instrument drift with time, using the  
 18 isotope compositions of the two water standards,  $\delta_{\text{st1}}$  and  $\delta_{\text{st2}}$ .

19 Water vapor of the ambient air, of both standards, and from the different tubing sections in the  
 20 soil column were sampled sequentially in the following order: soil (0.60 m) – soil (0.40 m) –  
 21 atmosphere – st1 – st2 – soil (0.20 m) – soil (0.10 m) – atmosphere – st1 – st2 – soil (0.07 m)  
 22 – soil (0.05 m) – atmosphere – st1 – st2 – soil (0.03 m) – soil (0.01 m). Atmosphere water  
 23 vapor was sampled twice as long (i.e., one hour) as soil water vapor from the  
 24 column/standards so that each sequence lasted exactly 10 hours and started each day at the  
 25 same time. The remaining 14 hours were used for additional standard and atmosphere water  
 26 vapor measurements (i.e., on five occasions each).

## 27 **2.6 Irrigation event**

28 On Day of Experiment (DoE) 290 at 09:30 the sand surface was irrigated with 70 mm of st1  
 29 water. This was achieved over one hour in order to avoid oversaturation of the sand and avoid  
 30 preferential pathways that would have affected the evaporation rate. For this, a 2 L

1 polyethylene bottle was used. Its bottom was perforated with a set of 17 holes of 5 mm  
 2 diameter and its cap with a single hole through which a PTFE bulkhead union tube fitting  
 3 (Swagelok, USA) was installed. The bulkhead fitting was connected to a two-way needle  
 4 valve (Swagelok, USA). Opening/closing the valve controlled the flow rate at which air  
 5 entered the bottle headspace, which in turn controlled the irrigation flow rate.

6 To better observe the dynamics directly following the irrigation event, water vapor was  
 7 sampled at a higher rate, i.e., 1, 3, 4, 5, 6, 9, 11, and 11 times per day at -0.60, -0.40, -0.20, -  
 8 0.10, -0.07, -0.05, -0.03, and -0.01 m. Water vapor from both standards was sampled twice a  
 9 day. The experiment was terminated after 299 days on September 26<sup>th</sup>, 2014.

## 10 2.7 Evaporation lines

11 Gat et al. (1971) proposed an expression based on the model of Craig and Gordon (1965) for  
 12 the slope of the so-called “evaporation line” ( $S_{Ev}$ , [-]) which quantifies the relative change in  
 13  $\delta^2\text{H}_{\text{Sliq}}$  and  $\delta^{18}\text{O}_{\text{Sliq}}$  in a water body undergoing evaporation:

$$14 \quad S_{Ev} = \frac{\Delta(\delta^2\text{H}_{\text{Sliq}})}{\Delta(\delta^{18}\text{O}_{\text{Sliq}})} = \frac{\left[ rh \cdot (\delta_a - \delta_{\text{Sliq\_ini}}) + \varepsilon_{\text{eq}} + \Delta\varepsilon \right]_{2\text{H}}}{\left[ rh \cdot (\delta_a - \delta_{\text{Sliq\_ini}}) + \varepsilon_{\text{eq}} + \Delta\varepsilon \right]_{18\text{O}}} \quad (3)$$

15 with  $\delta_{\text{Sliq\_ini}}$  the initial soil water (hydrogen or oxygen) liquid isotope composition, i.e., prior  
 16 removal of water vapor by fractionating evaporation.  $\varepsilon_{\text{eq}}$  [-, expressed in ‰] is the  
 17 equilibrium enrichment in either  $^1\text{H}^2\text{H}^{16}\text{O}$  or  $^1\text{H}_2^{18}\text{O}$ . It is defined by the deviation from unity  
 18 of the ratio between water and isotopologue saturated vapor pressures and can be calculated  
 19 using the empirical closed-form equations proposed by, e.g., Majoube (1971).  $\Delta\varepsilon$  [-,  
 20 expressed in ‰] is the so-called “isotope kinetic effect” associated with  $^1\text{H}^2\text{H}^{16}\text{O}$  and  $^1\text{H}_2^{18}\text{O}$   
 21 vapor transports. Assuming that (i) turbulent transport is a non-fractionating process and  
 22 considering that (ii) the ratio of molecular diffusion resistance to total resistance equals one, it  
 23 follows that (Gat, 2000):

$$24 \quad \Delta\varepsilon = (1 - rh) \cdot \left( \frac{D^v}{D_i^v} - 1 \right) \cdot n \quad (4)$$

1 In Equation (4), the product  $\left(\frac{D^v}{D_i^v} - 1\right) \cdot n$  is the isotope kinetic enrichment ( $\varepsilon_K$ , [-, expressed in  
 2 ‰]). In the present study, values for ratios of diffusivities ( $D^v/D_i^v$ ) were taken from Merlivat  
 3 (1978):

$$4 \quad \begin{cases} \frac{D^v}{D_{2H}^v} = 0.9755 \\ \frac{D^v}{D_{18O}^v} = 0.9723 \end{cases} \quad (5a \text{ and } 5b)$$

5 The term  $n$  accounts for the aerodynamic in the air boundary layer and ranges from  $n_a = 0.5$   
 6 (turbulent diffusion, i.e., atmosphere-controlled conditions) to  $n_s = 1$  (molecular diffusion,  
 7 i.e., soil-controlled conditions) with a value of  $\frac{2}{3}$  corresponding to laminar flow conditions  
 8 (Dongmann et al., 1974, Brutsaert, 1975). We tested the formulation proposed by Mathieu  
 9 and Bariac (1996) where  $n$  is considered as a function of soil water content:

$$10 \quad n = \frac{(\theta_{\text{surf}} - \theta_{\text{res}}) \cdot n_a + (\theta_{\text{sat}} - \theta_{\text{res}}) \cdot n_s}{\theta_{\text{sat}} - \theta_{\text{res}}} \quad (6)$$

11 with  $\theta_{\text{res}}$ ,  $\theta_{\text{sat}}$ , and  $\theta_{\text{surf}}$  the residual, saturated and surface soil water contents [ $\text{m}^3 \text{m}^{-3}$ ].

12 Note that Equation (3) contrasts with the expression for the slope characterizing equilibrium  
 13 processes (e.g., precipitation formation) and therefore strictly temperature-dependant (i.e.,  
 14  $S_{eq} = \varepsilon_{eq}^{2H} / \varepsilon_{eq}^{18O}$ ). While  $S_{eq}$  might range for instance from 7.99 to 8.94 (for temperatures  
 15 spanning between 5 and 30°C), a much wider spread in  $S_{Ev}$  values is possible and has been  
 16 measured between 2 and 6 (Barnes and Allison, 1988, Brunel et al., 1995, DePaolo et al.,  
 17 2004).

## 18 **3 Results**

### 19 **3.1 Example of a measuring sequence**

20 Figure 2 shows exemplarily the measuring sequence for DoE 150. Soil and standards water  
 21 vapor mixing ratios were stable and ranged from 17,200 to 18,200 ppmv during the last 10  
 22 minutes of each sampling period (Fig. 2a).  $\delta_{Svap}$  was within the range spanned by  $\delta_{st1vap}$  and  
 23  $\delta_{st2vap}$  for both  $^2\text{H}$  and  $^{18}\text{O}$  (Fig. 2b). On DoE 150, the soil surface was sufficiently dry so that  
 24 atmospheric invasion of water vapor had started to significantly influence the  $\delta_{Svap}$  of the



1 upper soil layers. Therefore,  $\delta_{\text{Svap}}$  measured at  $-0.01$  m was lower than at  $-0.03$  m for both  $^2\text{H}$   
2 and  $^{18}\text{O}$ , but less pronounced for  $^2\text{H}$ .

### 3 **3.2 Time courses of air temperature, relative humidity and atmospheric $\delta^2\text{H}$** 4 **and $\delta^{18}\text{O}$**

5 During the experiment, the laboratory air temperature ranged from  $15.6$  to  $22.5$  °C (average:  
6  $18.7 \pm 1.5$  °C, Fig. 3a) and the relative humidity from  $19$  to  $69$  % (average:  $40$  %  $\pm 0.08$  %,   
7 Fig. 3a). Lower values of  $\delta_a$  were observed from DoE 0 to 125 at lower air temperatures,  
8 whereas higher values occurred after DoE 125 at higher air temperatures (Fig. 3b).

### 9 **3.3 Evolution of soil water content, temperature, evaporation flux, and $\delta_{\text{Svap}}$** 10 **from DoE 0-290**

11 The soil temperature ranged from  $16.2$  to  $22.3$  °C (average:  $18.6 \pm 1.3$  °C, data not shown)  
12 and closely followed that in the air, i.e., differences between daily mean soil and air  
13 temperatures ranged from  $-0.2$  to  $0.2$  °C during the experiment. Following the saturation of  
14 the column, a strong decrease in water content was observed in the upper  $10$  cm, whereas  
15 after 287 days the sand was still saturated at  $-0.60$  m (Fig. 4a). Figure 4b shows the time  
16 series of evaporation flux normalized by the vapor pressure deficit in the laboratory air  
17 ( $Ev/vpd$ , expressed in  $\text{mm day}^{-1} \text{ kPa}^{-1}$ ).  $Ev/vpd$  ratio was high at the beginning of the  
18 experiment, i.e., ranged from  $2.44$  to  $3.22$   $\text{mm d}^{-1} \text{ kPa}^{-1}$  during the first two experimental  
19 days. After DoE 180 and until the soil was irrigated,  $Ev/vpd$  stabilized to a mean value of  $0.03$   
20 ( $\pm 0.02$ )  $\text{mm d}^{-1} \text{ kPa}^{-1}$ .

21 Due to fractionating evaporation flux, the  $\delta_{\text{Svap}}$  of the topmost layer ( $-0.01$  m) increased  
22 instantaneously (i.e., from DoE 0 onward) from the equilibrium  $\delta_{\text{Svap}}$  value with the input  
23 water ( $-17.3$  ‰ and  $-132.3$  ‰ for  $^{18}\text{O}$  and  $^2\text{H}$ , respectively, at  $16.5^\circ\text{C}$ , Fig. 4c and d).  
24 Through back-diffusion of the excess heavy stable isotopologues from the evaporation front,  
25  $\delta_{\text{Svap}}$  measured at depths  $-0.03$ ,  $-0.05$ ,  $-0.07$ ,  $-0.10$ , and  $-0.20$  m departed from that same  
26 equilibrium value after 2, 3, 10, 25, and 92 days of the experiment, respectively. On the other  
27 hand,  $\delta_{\text{Svap}}$  of the layers  $-0.40$  and  $-0.60$  m were constant over the entire duration of the  
28 experiment. Until DoE 65, the  $\delta_{\text{Svap}}$  of the first  $10$  cm increased. From DoE 65 to 113  $\delta_{\text{Svap}}$   
29 reached an overall stable value in the top layers  $-0.01$  m ( $\delta^2\text{H}_{\text{Svap}} = 4.82 \pm 2.06$  ‰;  $\delta^{18}\text{O}_{\text{Svap}} =$   
30  $11.72 \pm 0.67$  ‰) and  $-0.03$  m ( $\delta^2\text{H}_{\text{Svap}} = 5.61 \pm 3.14$  ‰;  $\delta^{18}\text{O}_{\text{Svap}} = 10.41 \pm 0.81$  ‰), whereas

1  $\delta_{\text{Svap}}$  measured at depths  $-0.05$ ,  $-0.07$ , and  $-0.10$  m still progressively increased; from DoE 72  
2 onward,  $\delta_{\text{Svap}}$  at  $-0.20$  m started to increase.  $\delta^2\text{H}_{\text{Svap}}$  and  $\delta^{18}\text{O}_{\text{Svap}}$  values started to decrease  
3 after about DoE 113 and DoE 155, respectively.  $\delta^2\text{H}_{\text{Svap}}$  at  $-0.01$ ,  $-0.03$ , and  $-0.07$  m on the  
4 one hand and  $\delta^{18}\text{O}_{\text{Svap}}$  at  $-0.01$ ,  $-0.03$ , and  $-0.07$  m on the other followed similar evolutions  
5 with maximum values measured below the surface down to  $-0.05$  m.

### 6 **3.4 Evolution of soil water content, temperature, evaporation flux, and $\delta_{\text{Svap}}$** 7 **from DoE 290 to 299**

8 The layers  $-0.01$ ,  $-0.03$ ,  $-0.05$ ,  $-0.10$ , and  $-0.20$  m showed increases in  $\theta$  of 0.31, 0.22, 0.30,  
9 0.23, and  $0.16 \text{ m}^3 \text{ m}^{-3}$  following irrigation, whereas  $\theta$  at  $-0.60$  m remained constant (Fig. 4e).  
10  $\theta_{-0.01\text{m}}$  and  $\theta_{-0.03\text{m}}$  rapidly decreased down to values of  $0.12$  and  $0.13 \text{ m}^3 \text{ m}^{-3}$ . Note that when  
11  $\theta_{-0.01\text{m}}$  and  $\theta_{-0.03\text{m}}$  reached these values prior to irrigation, the evaporation rate was similar  
12 (i.e.,  $E_v/vpd = 0.65 (\pm 0.12) \text{ mm d}^{-1}$ , Fig. 4f).

13 Immediately after irrigation and for both isotopologues,  $\delta_{\text{Svap}}$  at  $-0.01$ ,  $-0.03$ , and  $-0.05$  m  
14 was reset to a value close to that in equilibrium with soil water (i.e.,  $-17.8 \text{ ‰}$  and  $-132.0 \text{ ‰}$   
15 for  $^{18}\text{O}$  and  $^2\text{H}$ , respectively, at  $21.8 \text{ °C}$  soil temperature, Fig. 4g and h). At  $-0.07$  m,  $\delta_{\text{Svap}}$   
16 reached the above mentioned equilibrium values after about 3.5 days.  $\delta_{\text{Svap}}$  at  $-0.20$  m evolved  
17 in a similar way, whereas at  $-0.10$  m the equilibrium values were reached after six hours.  
18 Finally,  $\delta_{\text{Svap}}$  at  $-0.40$  and  $-0.60$  m and for both isotopologues were not affected by the water  
19 addition, which was consistent with the observed  $\theta$  changes.

### 20 **3.5 Evolution of soil temperature, water content, and $\delta_{\text{Sliq}}$ profiles**

21 In Figure 5,  $T_s$ ,  $\theta$ , and  $\delta_{\text{Sliq}}$  profiles for both isotopologues are plotted in three different panels,  
22 from DoE 0 to 100 (Fig. 5a-d, top panels), from DoE 101 to 287 (Fig. 5e-h, center panels),  
23 and from DoE 288 to 299 (Fig. 5i-l, bottom panels). The represented profiles were obtained  
24 from a linear interpolation of the times series of each variable. Thus, since the measuring  
25 sequence started each day at 08:00 and ended at 18:00, the depicted profiles are centered on  
26 13:00.

27 Even if the soil temperature fluctuated during the course of the experiment, quasi-isothermal  
28 conditions were fulfilled at a given date, as the column was not isolated from its surroundings.  
29 On average,  $T_s$  only varied by  $0.2 \text{ °C}$  around the profile mean temperature at a given date.  
30 The  $\delta_{\text{Sliq}}$  profiles showed a typical exponential shape from DoE 0 to approx. 100. Around DoE

1 100, when  $\theta$  at  $-0.01$  m reached a value of  $0.090 \text{ m}^3 \text{ m}^{-3}$  (i.e., significantly greater than the  
2 sand residual water content  $\theta = 0.035 \text{ m}^3 \text{ m}^{-3}$ , determined by Merz et al. (2014)), the maximal  
3  $\delta_{\text{Sliq}}$  values were no longer observed at the surface and atmosphere water vapor started  
4 invading the first centimeter of soil. Note that this happened slightly faster for  $^1\text{H}^2\text{H}^{16}\text{O}$  than  
5 for  $^1\text{H}_2^{18}\text{O}$ . On DoE 290, when the column was irrigated, the isotope profiles were partly reset  
6 to their initial state, i.e., constant over depth and close to  $-53.5$  and  $-8.2$  ‰ for  $^1\text{H}^2\text{H}^{16}\text{O}$  and  
7  $^1\text{H}_2^{18}\text{O}$ , respectively, with the exception of still enriched values at  $-0.07$  m.

### 8 **3.6 $\delta^2\text{H}$ - $\delta^{18}\text{O}$ relationships in soil water and atmosphere water vapor**

9 Each plot of Figure 6 represents data of 50 consecutive days of the experiment. Laboratory  
10 atmosphere water vapor  $\delta^2\text{H}$  and  $\delta^{18}\text{O}$  (gray symbols) were linearly correlated (linear  
11 regression relationships in gray dotted lines) during the entire experiment ( $R^2$  ranging  
12 between 0.74 and 0.90, F-statistic p-value  $< 0.01$ ), with the exception of the period DoE 125-  
13 155 ( $R^2 = 0.31$ ,  $p < 0.001$ ), when atmospheric water vapor  $\delta^2\text{H}$  was remarkably high in the  
14 laboratory (Fig. 6c and d).

15 The linear regression slopes (LRS) between  $\delta^2\text{H}_a$  and  $\delta^{18}\text{O}_a$  ranged from 6.20 (DoE 50-100,  $p$   
16  $< 0.01$ ) to 8.29 (DoE 0-50, gray dotted line,  $p < 0.001$ ). These values were significantly lower  
17 than  $S_{\text{eq}}$ , the calculated ratio between the liquid-vapor equilibrium fractionations of  $^1\text{H}^2\text{H}^{16}\text{O}$   
18 and  $^1\text{H}_2^{18}\text{O}$  (Majoube, 1971) that characterizes meteoric water bodies, which should have  
19 ranged from 8.41 to 8.92 at the measured monthly mean atmosphere temperatures  
20 (Forschungszentrum Jülich wheat station,  $6^\circ 24' 34''$  E,  $50^\circ 54' 36''$  N, 91 m.a.s.l.). Therefore,  
21 it can be deduced that the laboratory air moisture was partly resulting from column  
22 evaporation, typically leading to a  $\delta^2\text{H}$ - $\delta^{18}\text{O}$  regression slope of lower than eight. This also  
23 highlights the particular experimental conditions in the laboratory, where other sources of  
24 water vapor (e.g., by opening the laboratory door) might have influenced the isotope  
25 compositions of the air.

26 Considering all soil depths, the  $\delta^2\text{H}_{\text{Sliq}}-\delta^{18}\text{O}_{\text{Sliq}}$  LRS increased from 2.96 to 4.86 over the  
27 course of the experiment (with  $R^2 > 0.89$ ,  $p < 0.001$ ). These values were much lower than that  
28 of the slope of the Global Meteoric Water Line (GMWL, i.e., slope=8) also represented in  
29 Figure 6. However, Figure 6 highlights the fact that in the upper three layers ( $-0.01$ ,  $-0.03$ ,  
30 and  $-0.05$  m)  $\delta^2\text{H}_{\text{Sliq}}-\delta^{18}\text{O}_{\text{Sliq}}$  LRS followed a significantly different evolution as the soil dried  
31 out. Figure 7 shows average  $\delta^2\text{H}$ - $\delta^{18}\text{O}$  LRS calculated for time intervals of ten consecutive

1 days for the atmosphere (gray line), the three upper layers (colored solid lines), and the  
2 remaining deeper layers (−0.07, −0.10, −0.20, −0.40, and −0.60 m, black dotted line). While  
3 both  $\delta^2\text{H}$ - $\delta^{18}\text{O}$  LRS in the atmosphere and in the first three depths fluctuated during the  
4 experiment, the LRS of the combined remaining deeper layers varied only little between 3.07  
5 and 4.49 (average =  $3.78 \pm 0.54$ ). From DoE 150,  $\delta^2\text{H}$ - $\delta^{18}\text{O}$  LRS of the atmosphere and at −  
6 0.01, −0.03, and −0.05 m were linearly correlated ( $R^2 = 0.73, 0.48, \text{ and } 0.42$ , with  $p < 0.001, <$   
7  $0.01$ , and  $< 0.05$ , respectively), whereas they were not correlated before DoE 125,  
8 demonstrating again the increasing influence of the atmosphere (atmosphere invasion) on the  
9 soil surface layer as the EF receded in the soil. Note the negative  $\delta^2\text{H}_a$ - $\delta^{18}\text{O}_a$  LRS ( $R^2 = 0.26$ ,  
10  $p < 0.001$ ) observed between DoE 125 and 150, due to remarkably high atmosphere vapor  
11  $\delta^2\text{H}$  measured in the laboratory.

12

## 13 **4 Discussion**

### 14 **4.1 Long term reliability of the method**

15 The method proved to be reliable in the long term as the tubing sections positioned at −0.60  
16 and −0.40 m (i.e., where the sand was saturated or close to saturation during the entire  
17 experiment) remained watertight even after 299 days. As demonstrated by Rothfuss et al.  
18 (2013), (i) the length of the gas-permeable tubing, (ii) the low synthetic dry air flow rate, and  
19 (iii) the daily measurement frequency allowed removing soil water vapor which remained  
20 under thermodynamic equilibrium with the soil moisture. Moreover, this was also true for the  
21 upper soil layers even at low soil water content: steady values for water vapor mixing ratio  
22 and isotope compositions were always reached during sampling throughout the experiment.  
23 Finally, our method enabled inferring the isotope composition of tightly bound water at the  
24 surface. This would be observable by the traditional vacuum distillation method with certainly  
25 a lower vertical resolution due to low moisture content. As also pointed out by Rothfuss et al.  
26 (2013), it can be assumed that the sand properties did not cause any fractionation of pore  
27 water  $^2\text{H}$  and  $^{18}\text{O}$ . In contrast, this could not be the case in certain soils with high cation  
28 exchange capacity (CEC) as originally described by Sofer and Gat (1972) and recently  
29 investigated by Oerter et al. (2014).

## 1 4.2 Locating the evaporation front depth from soil water $\delta^2\text{H}$ and $\delta^{18}\text{O}$ profiles

2 From Figure 4b no distinct characteristic evaporation stages, i.e., stages I and II referring to  
3 atmosphere-controlled and soil-controlled evaporation phases, respectively, could be  
4 identified. The opposite was observed by Merz et al. (2014), who conducted an evaporation  
5 study using the same sand. This indicates greater wind velocity in the air layer above the soil  
6 column due to the laboratory ventilation. For higher wind velocities, the boundary layer above  
7 the drying medium is thinner and the transfer resistance for vapor transfer lower than for  
8 lower wind velocities. But, for thinner boundary layers, the evaporation rates depends  
9 stronger on the spatial configuration of the vapor field above the partially wet evaporating  
10 surface. This makes that the evaporation rate decreases and the transfer resistance in the  
11 boundary layer increases more in relative terms with decreasing water content of the  
12 evaporation surface for higher than for lower wind velocities (Shahraeeni et al., 2012).

13 Locating the EF in the soil is of importance for evapotranspiration partitioning purposes: from  
14 the soil water isotope composition at the EF, it is possible to calculate the evaporation flux  
15 isotope composition using the Craig and Gordon formula (Craig and Gordon, 1965). For a  
16 uniform isotope diffusion coefficient distribution in the liquid phase, an exponential decrease  
17 of the isotope composition gradient with depth is expected. However, when evaporation and  
18 thus accumulation of isotopologues occur in a soil layer between two given observation  
19 points, then the isotope gradient between these two points is smaller than the gradient deeper  
20 in the profile. Therefore we can consider the time when the isotope composition gradient is no  
21 longer the largest between these two upper observation depths as the time when the EF moves  
22 into the soil layer below.

23 Figure 8a and b display the evolutions of the isotope compositions gradients  $d(\delta^{18}\text{O}_s)/dz$  and  
24  $d(\delta^2\text{H}_s)/dz$  calculated between two consecutive observation points in the soil (i.e., between  
25  $-0.01$  and  $-0.03$  m in brown solid line, between  $-0.03$  and  $-0.05$  m in red solid line, etc.).  
26 Figure 8c translates these isotope gradients in terms of EF depths ( $z^{18}\text{O}_{\text{EF}}$  and  $z^2\text{H}_{\text{EF}}$ ,  
27 respectively). Each day, the maximum  $d(\delta^{18}\text{O}_s)/dz$  and  $d(\delta^2\text{H}_s)/dz$  define the layer where  
28 evaporation occurs, e.g., when  $d(\delta^{18}\text{O}_s)/dz$  is maximal between  $-0.01$  and  $-0.03$  m on a given  
29 DoE,  $z^{18}\text{O}_{\text{EF}}$  is estimated to be greater than  $-0.01$  m and is assigned the value of 0 m.  
30 When  $d(\delta^{18}\text{O}_s)/dz$  is maximal between  $-0.03$  and  $-0.05$  m on a given DoE,  $z^{18}\text{O}_{\text{EF}}$  is  
31 estimated to range between  $-0.01$  and  $-0.03$  m and is assigned the value  $-0.02$  m. From

1 both  $d(\delta^{18}O_s)/dz$  and  $d(\delta^2H_s)/dz$ , a similar evolution of the depth of the evaporation front  
2 was derived despite the fact that  $\delta^2H_{Sliq}$  and  $\delta^{18}O_{Sliq}$  time courses were different and showed  
3 maxima at different times. It was inferred that after 290 days under the prevailing laboratory  
4 air temperature, moisture, and aerodynamic conditions, and given the specific hydraulic  
5 properties of the sand, the EF had moved down to an approximate depth of  $-0.06$  m.

### 6 **4.3 Isotope kinetic effects during soil evaporation**

7 For each period of ten consecutive days the minimum measured  $\delta^2H_{Sliq}$  and  $\delta^{18}O_{Sliq}$  provided  
8  $\delta^2H_{Sliq\_ini}$  and  $\delta^{18}O_{Sliq\_ini}$  in Equation (3).  $\delta^2H_a$  and  $\delta^{18}O_a$  were obtained from the mean values  
9 of their respective times series. Mean soil surface water content ( $\theta_{surf}$ ) measured in the layer  
10 above the EF (as identified in section 4.2) provided the  $n$  parameter in Equation (6) and  
11 ultimately  $\epsilon_K^{2H}$  and  $\epsilon_K^{18O}$  (Eq. (5a) and (5b)).  $\epsilon_{eq}^{2H}$  and  $\epsilon_{eq}^{18O}$  were calculated from Majoube (1971)  
12 at the mean soil temperature measured at  $z_{EF}$ . Relative humidity was normalized to the soil  
13 temperature measured at the EF. Finally, standard error for  $S_{Ev}$  was obtained using an  
14 extension of the formula proposed by Phillips and Gregg (2001) and detailed by Rothfuss et  
15 al. (2010). For this, standard errors associated with the determination of the variables in  
16 Equation (3) were taken equal to their measured standard deviations for each time period.  
17 Standard errors for the parameters  $\theta_{res}$  and  $\theta_{sat}$  were set to  $0.01 \text{ m}^3 \text{ m}^{-3}$  (i.e., comparable to the  
18 soil water content probes' precision) and for the diffusivity ratios  $D/D^{2H}$  and  $D/D^{18O}$  to zero  
19 (i.e., no uncertainty about their value was taken into account, although debatable, e.g., Cappa  
20 et al., 2003).

21 Figure 9a shows the comparison between time courses of  $S_{Ev}$  and  $\delta^2H_{Sliq}$ - $\delta^{18}O_{Sliq}$  LRS  
22 computed with data below the EF. Both ranged between 2.9 and 4.8, i.e., within the range of  
23 reported values (e.g., Barnes and Allison, 1988, Brunel et al., 1995, DePaolo et al., 2004).  
24 Note that both observed and simulated slopes' values increased over time, even though the air  
25 layer above the EF gradually thickened as the soil dried out. The opposite was observed by  
26 e.g., Barnes and Allison (1983), who simulated isotopic profiles at steady state with constant  
27 relative humidity. In the present study however the atmosphere relative humidity gradually  
28 increased which in turn decreased the kinetic effects associated with  $^1H^2H^{16}O$  and  $^1H_2^{18}O$   
29 vapor transports and thus increased slopes over time. The general observed trend was very  
30 well reproduced by the model between DoE 30 and 150 (Nash and Sutcliffe Efficiency - NSE  
31 = 0.92; Nash and Sutcliffe, 1970), whereas  $S_{Ev}$  departed from data from DoE 150 onwards

1 (NSE < 0). Overall, the Craig and Gordon (1965) model could explain about 62 % of the data  
2 variability with a Root Mean Square Error (RMSE) of 0.58 (and 76 % when data from the  
3 period DoE 0-10 is left out, p-value < 0.001, RMSE = 0.52). At the beginning of the  
4 experiment (DoE 0-20), simulated values were greater than computed  $\delta^2\text{H}-\delta^{18}\text{O}$  LRS, even  
5 when taking into account the high  $S_{\text{Ev}}$  standard errors due to fast changing  $\theta_{\text{surf}}$  (Phillips and  
6 Gregg, 2001). Although  $S_{\text{Ev}}$  was equal to 3.8 for the period DoE 0-10,  $\delta^2\text{H}-\delta^{18}\text{O}$  LRS had  
7 already reached down a value of 2.9, meaning that the EF should have been no longer at the  
8 surface (i.e., between the surface and 0.01 m depth) leading to greater n, therefore lower slope  
9 value.

10 After DoE 150 and until DoE 290 when evaporation flux was lower than 0.40 mm d<sup>-1</sup>,  
11 difference between model and data progressively increased. For a better model-to-data fit, the  
12  $^1\text{H}^2\text{H}^{16}\text{O}$  and  $^1\text{H}_2^{18}\text{O}$  kinetic effects should decrease, through either (i) decrease of n, which is  
13 from a theoretical point of view counter-intuitive and e.g., contradicts the formulation of  
14 Mathieu and Bariac (1996) or (ii) decrease of term  $(1 - rh)$ , or else (iii) a combination of (i)  
15 and (ii). In another laboratory study where  $\delta^{18}\text{O}$  of water in bare soil columns was measured  
16 destructively and  $\delta^{18}\text{O}$  of evaporation was estimated from cryoscopic trapping of water vapor  
17 at the outlet of the columns' headspaces, Braud et al. (2009a and b) could capture  
18  $\varepsilon_{\text{K}}^{18\text{o}}$  dynamics by inverse modelling. In their case,  $\varepsilon_{\text{K}}^{18\text{o}}$  generally reached values close  
19 to  $\varepsilon_{\text{K}}^{18\text{o}} = 18.9\text{‰}$  corresponding to laminar conditions above the liquid-vapor interface (n =  
20 2/3). They however determined at the end of their experiments, when the soil surface dry  
21 layer thickened and soil surface relative humidity was significantly lower than 100%, values  
22 lower than reported in the literature (i.e.,  $\varepsilon_{\text{K}}^{18\text{o}} < 14.1\text{‰}$ ). These results were partly explained  
23 by the particular experimental conditions leading to uncertainties in characterizing  
24 evaporation isotope compositions when the dry soil surface layer was the most developed.  
25 Nevertheless, the same observation could be made in the present study while having a  
26 different soil texture (silt loam *versus* quartz sand) and noticeable different atmospheric  
27 conditions ("free" laboratory atmosphere *versus* sealed headspace circulated with dry air).  
28 Figure 9c displays the evolution of  $\varepsilon_{\text{K}}^{2\text{H}}$  (resp.  $\varepsilon_{\text{K}}^{18\text{o}}$ ) that provided the best fit with data (NSE =  
29 0.99) through fitting of the n parameter (shown Figure 9b) instead of calculating it with  
30 Equation (6). In this scenario, n decreased from one to 0.59, with a mean value of  $0.96 \pm 0.03$   
31 during the period DoE 0-150.

1 Instead of changing the value of  $n$  over time (and therefore those of  $\varepsilon_K^{2H}$  and  $\varepsilon_K^{18O}$ ), another  
2 possibility is to consider that after some time the relative humidity at the EF ( $rh_{EF}$ ) was  
3 different from 100%, although the EF was still at thermodynamic equilibrium. In that case  
4 kinetic effects would have depended on the difference ( $rh_{EF} - rh$ ) instead of  $(1 - rh)$ . Figure  
5 9b shows the  $rh_{EF}$  time course that provided the best model-to-data fit (NSE = 0.92), when  
6  $\varepsilon_K^{2H}$  and  $\varepsilon_K^{18O}$  were calculated (Eq. (5a-5b-6)). In this second scenario,  $rh_{EF}$  decreased from 100  
7 to 81 % with a mean value of  $99.5 \pm 0.03$  % for the period DoE 0-150, i.e., in a similar  
8 fashion than fitted  $n$  values obtained in the 1<sup>st</sup> scenario. These values were significantly lower  
9 than what is calculated with Kelvin's Equation linking  $rh_{EF}$  with soil water tension at the EF  
10 in the case of liquid-vapor equilibrium, which for the soil retention properties (Merz et al.,  
11 2014) would range between 100 and 99.6 %. In a third scenario one could consider a  
12 combined decrease of  $n$  and  $rh_{EF}$  to smaller extents, for which there are no unique solutions at  
13 each time step. In a fourth scenario, the ratio of turbulent diffusion resistance to molecular  
14 diffusion resistance is no more negligible, leading to  $n'$  values ranging between 0 and  $n$   
15 (Merlivat and Jouzel, 1979). This last scenario was however not verifiable. In any case, only  
16 decreasing kinetic effects could provide a better model-to-data fit. Note that the formulation  
17 of kinetic enrichments proposed by Merlivat and Coantic (1975) and based on the evaporation  
18 model of Brutsaert (1982) was not tested due to lack of appropriate data (i.e., unknown wind  
19 distribution profile over the soil column). The formulations of Melayah et al. (1996) ( $n = 0$ )  
20 and Barnes and Allison (1983) ( $n = 1$ ) were also not tested as they give kinetic enrichments  
21 constant over time and cannot explain a change of  $S_{Ev}$  value through change of  $n$ . Finally,  $S_{Ev}$   
22 calculations using diffusivity ratios determined by Cappa et al. (2003) lead to lower value of  
23  $S_{Ev}$  and less good model-to-data fit.

24 In the present study, information on  $\delta^{2H}$  and  $\delta^{18O}$  of the evaporation flux was missing to  
25 address uncertainties in the determination of  $\varepsilon_K^{2H}$  and  $\varepsilon_K^{18O}$ . The experimental setup would also  
26 have gained from the addition of appropriate sensors (e.g., micro-psychrometers) to measure  
27 the soil surface relative humidity and especially  $rh_{EF}$ , although the dimensions of the column  
28 would certainly be a limiting factor. A more in depth investigation of the behavior of  $S_{Ev}$  (and  
29 isotope composition gradients with depth for that matter) with time could be carried out with  
30 detailed numerical simulations using an isotope-enabled SVAT model such as SiSPAT-  
31 Isotope.



## 1 **5 Conclusion**

2 Since the initial work of Zimmermann et al. (1967), water stable isotopologues have proven  
3 both theoretically and experimentally to be valuable tools for the study of water flow in the  
4 soil and at the soil-atmosphere interface. In this work we present the first application of the  
5 method of Rothfuss et al. (2013). This study constitutes also the very first long-term  
6 application of the series of newly developed isotopic monitoring systems based on gas-  
7 permeable tubing and isotope-specific infrared laser absorption spectroscopy (Herbstritt et al.,  
8 2012; Volkmann and Weiler, 2014). Our method proved to be reliable over long time periods  
9 and followed quantitatively the progressive isotope enrichment caused by evaporation in an  
10 initially saturated soil column. Moreover, it could capture sudden variations following a  
11 simulated intense rain event.

12 Simple calculations of isotope compositions' gradients made it possible to evaluate the  
13 position of the Evaporation Front and observe how it progressively receded with time in the  
14 soil. Confrontation of the model of Craig and Gordon (1965) with data also highlighted  
15 uncertainties associated with the determinations of isotope kinetic fractionations and soil  
16 relative humidity at the EF when the soil surface dry layer was the most developed and  
17 evaporation flux was low.

18 Our method will allow experimentalists to measure and locate the evaporation front in a  
19 dynamic and non-destructive manner and to calculate the isotope compositions of the  
20 evaporation flux using the model of Craig and Gordon (1965) with much higher time  
21 resolution. Provided that the isotope compositions of evapotranspiration and transpiration  
22 fluxes are measured or modelled, this method will be especially useful to test hypotheses and  
23 improve our understanding of root water uptake processes and the partitioning of  
24 evapotranspiration fluxes.

25

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3

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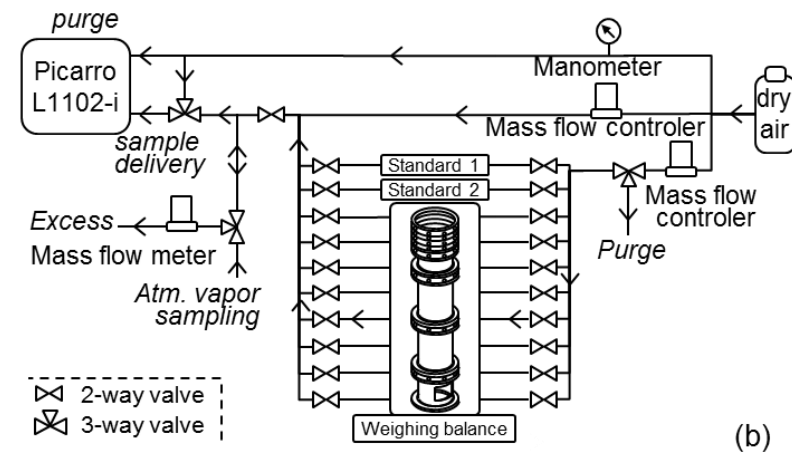
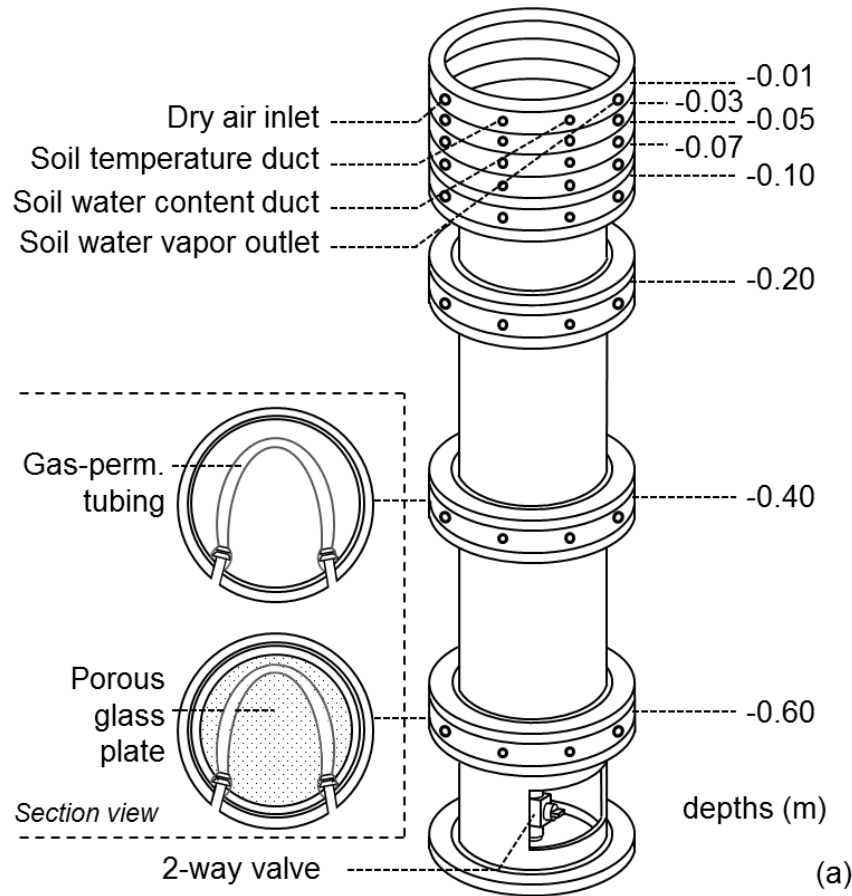
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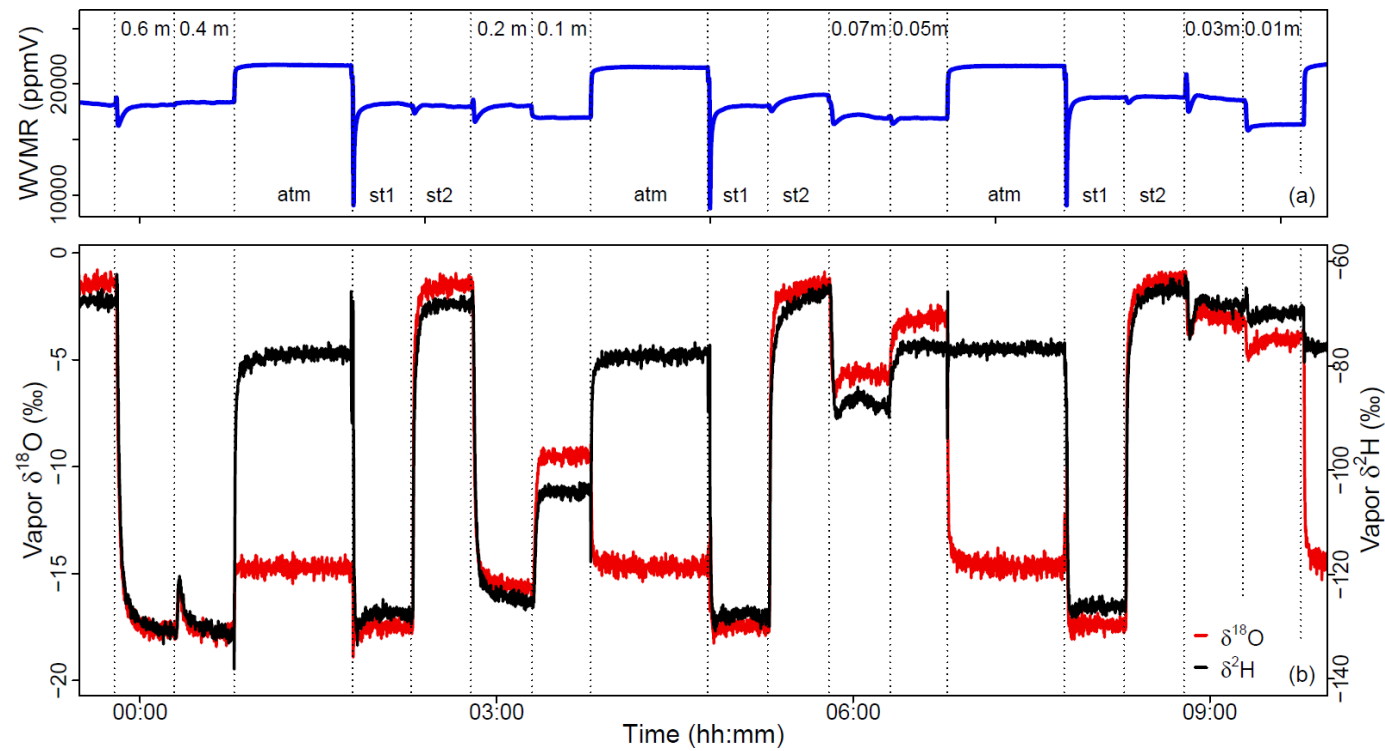
1 **Figures**



2

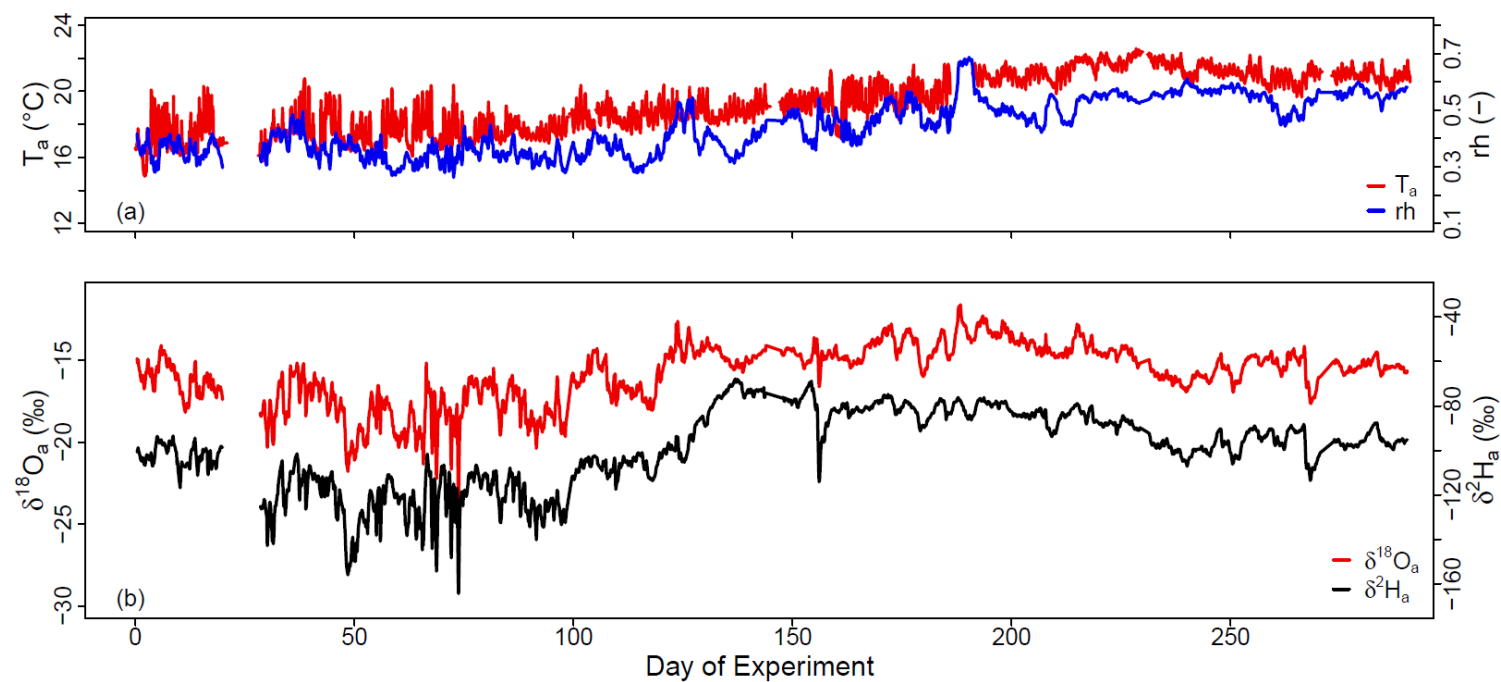
3 Figure 1. (a) Scheme of the acrylic glass column used in the experiment; (b) experimental setup for sampling water vapor at the different soil  
 4 depths of the soil column, from the ambient air, and from the two soil water standards (standard 1 and 2)

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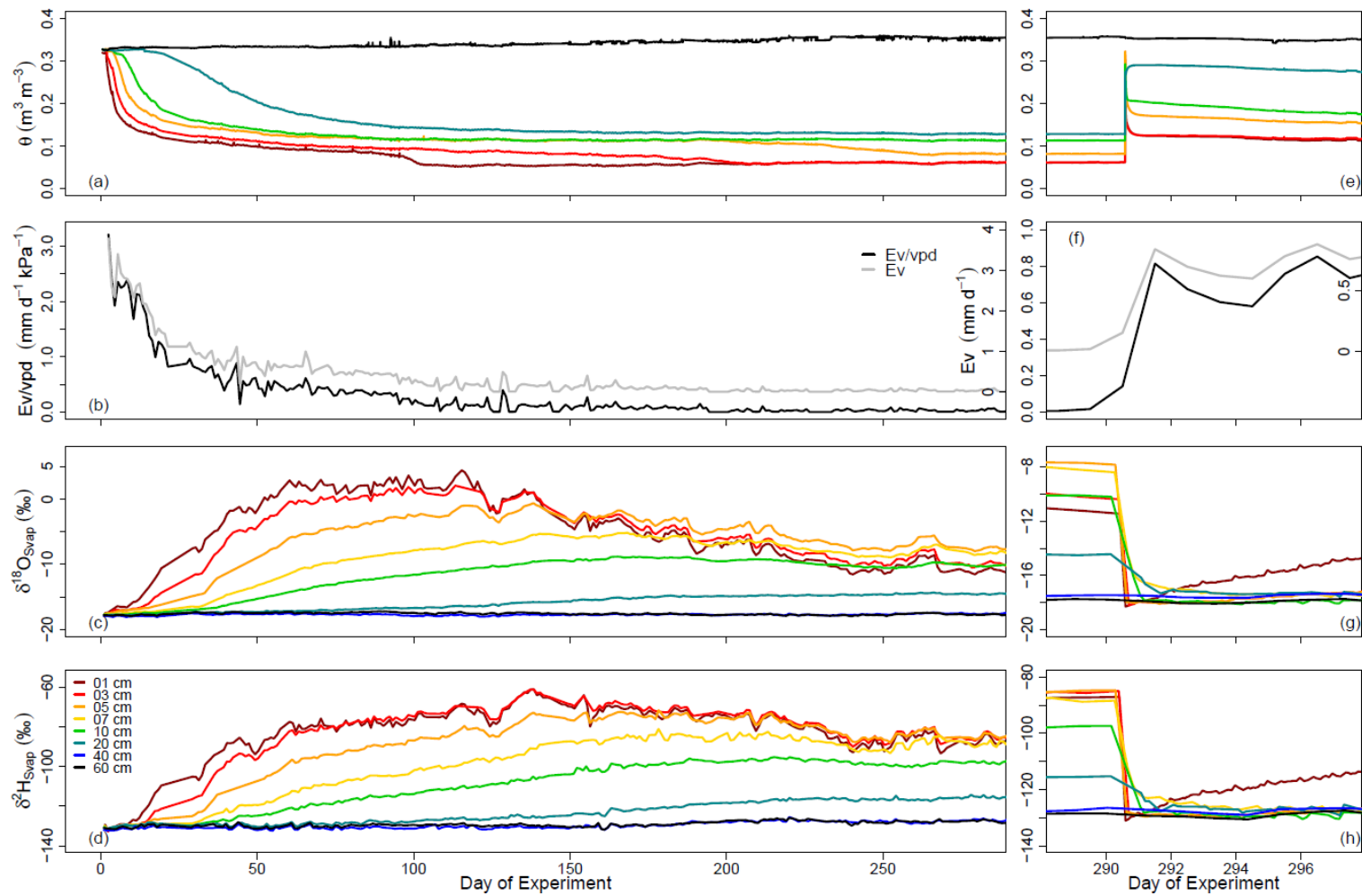
Figure 2. Water vapor mixing ratio (*WVMR*, in ppmv) and isotope composition ( $\delta^{18}\text{O}$  and  $\delta^2\text{H}$ , in ‰ V-SMOW) of the water vapor sampled on Day of Experiment 150 from the ambient air (“atm”), both standards (“st1” and “st2”), and from the tubing sections at soil depths 1, 3, 5, 7, 10, 20, 40, and 60 cm



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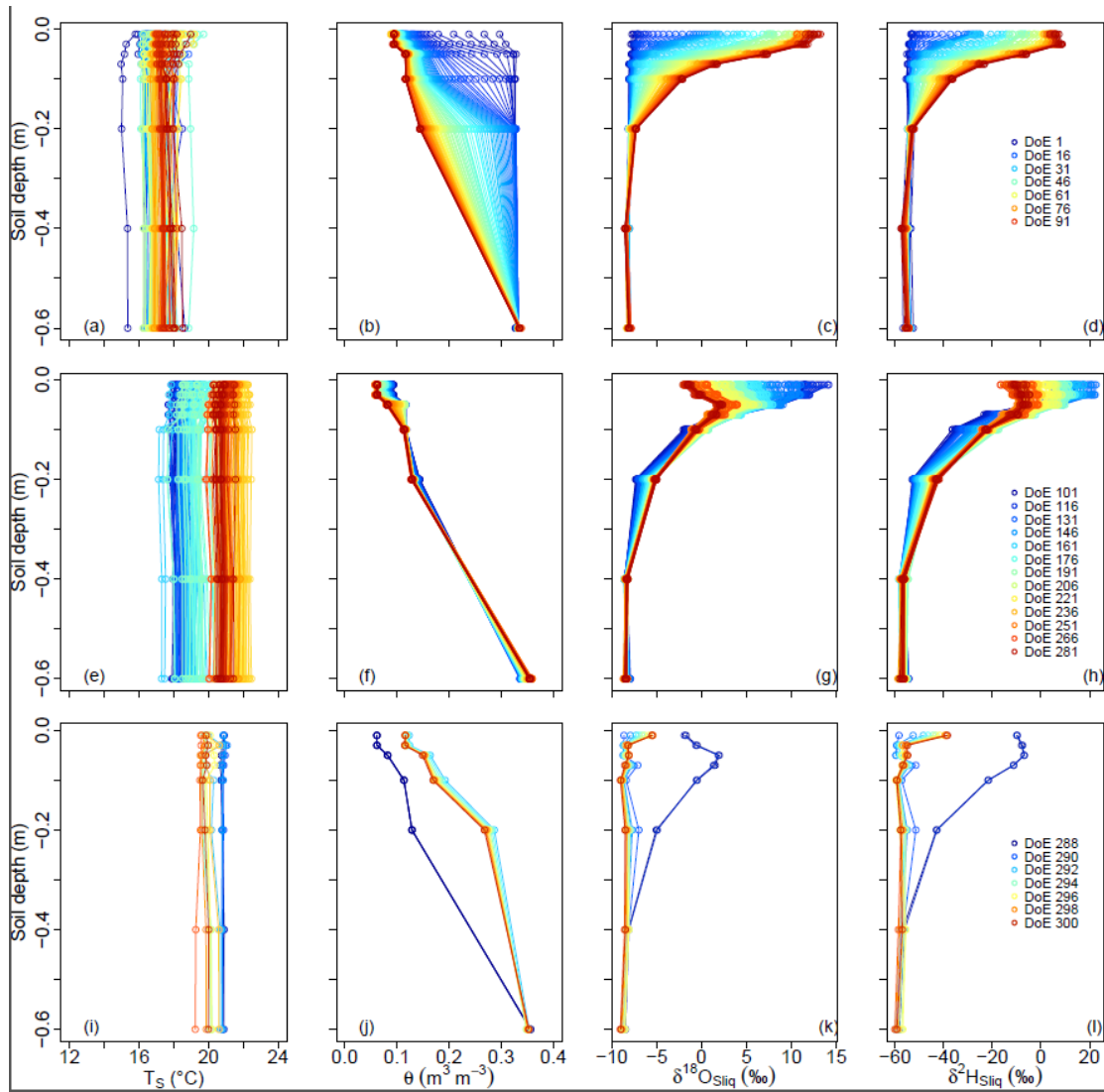
2 Figure 3. Time series of the laboratory ambient air temperature ( $T_a$ , in  $^{\circ}\text{C}$ ), relative humidity ( $rh$ , in %) and water vapor isotope compositions  
 3 ( $\delta^{18}\text{O}_a$  and  $\delta^2\text{H}_a$ , in  $\text{‰}$  V-SMOW) over the course of the experiment

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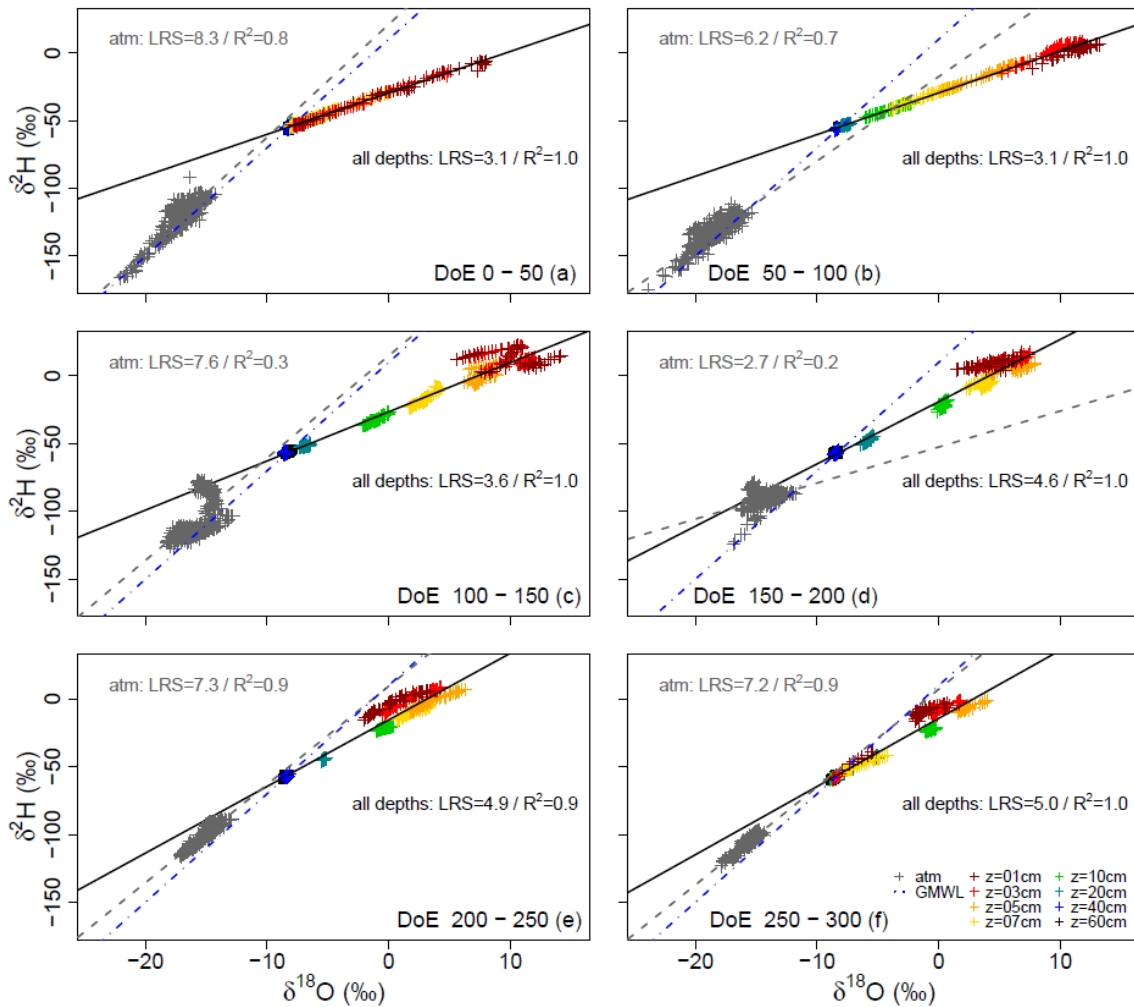
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2 Figure 4. Time series of water content ( $\theta$ , in  $\text{m}^3 \text{m}^{-3}$ ), evaporation flux ( $Ev$ , in  $\text{mm d}^{-1}$ ), and water vapor isotope compositions ( $\delta^{18}\text{O}_{\text{Svap}}$  and  
 3  $\delta^2\text{H}_{\text{Svap}}$ , in ‰ V-SMOW) during the course of the experiment



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 2 Figure 5. Soil temperature ( $T_S$ , in  $^{\circ}\text{C}$ ), water content ( $\theta$ , in  $\text{m}^3 \text{m}^{-3}$ ), and liquid water isotope  
 3 compositions ( $\delta^{18}\text{O}_{\text{Sliq}}$  and  $\delta^2\text{H}_{\text{Sliq}}$ , in ‰ V-SMOW) profiles from Day of Experiment (DoE) 0  
 4 - 100 (top panel), from DoE 101 - 287 (middle panel), and from DoE 288 - 299 (bottom  
 5 panel)

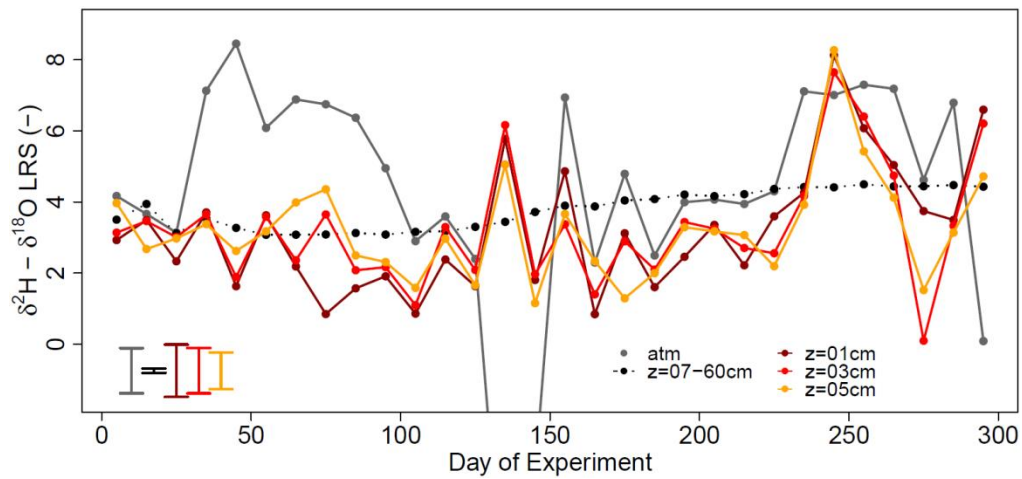
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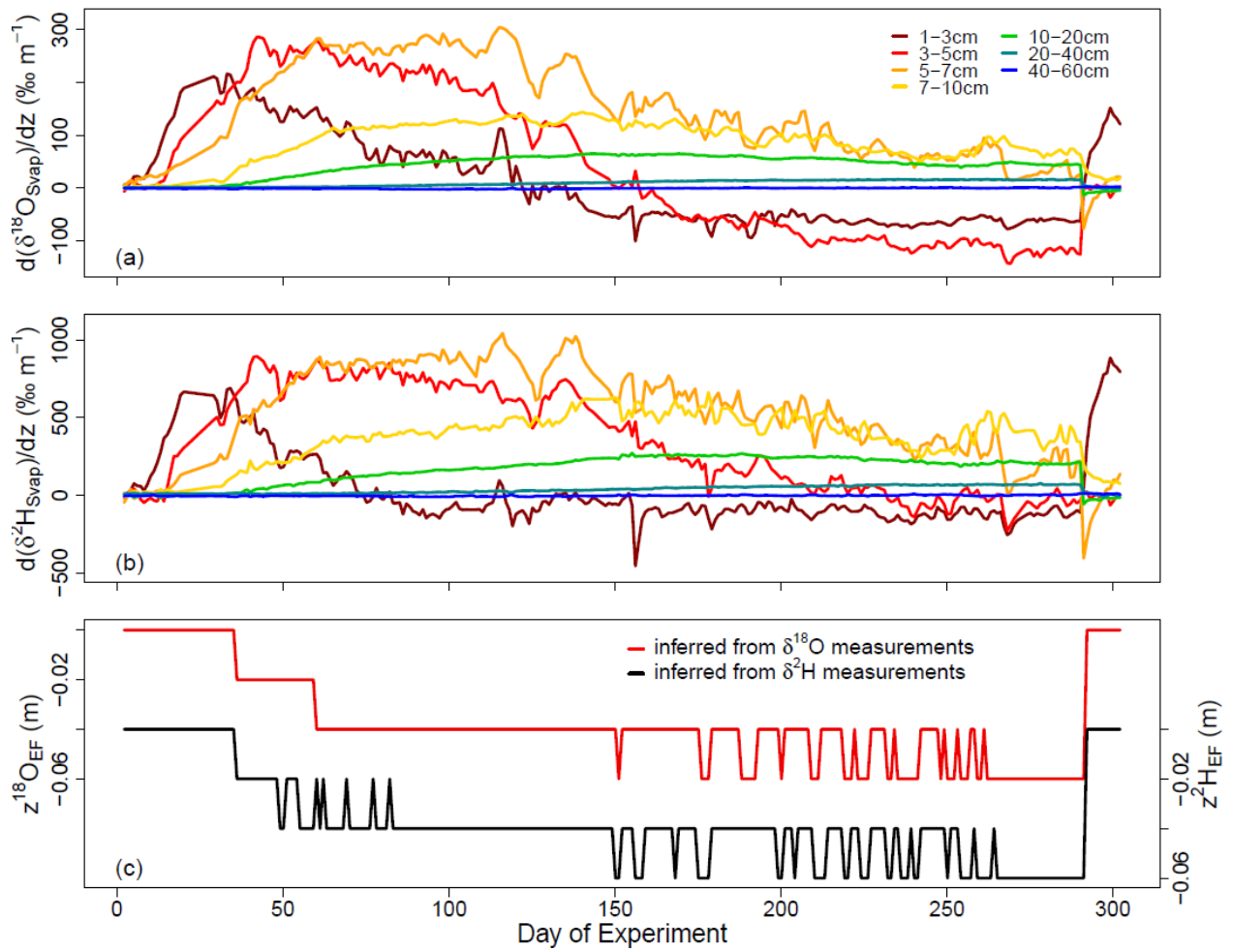
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2 Figure 6. Linear regressions (gray dotted line) between laboratory atmosphere water vapor  
 3  $\delta^{18}\text{O}$  and  $\delta^2\text{H}$  (in ‰ V-SMOW) and between soil water  $\delta^{18}\text{O}$  and  $\delta^2\text{H}$  (solid black line). Each  
 4 plot represents data from 50 consecutive days of experiment (DoE). Global Meteoric Water  
 5 Line (GMWL, define by  $\delta^2\text{H} = 8 * \delta^{18}\text{O} + 10$ , in blue dotted line) is shown on each sub-plot for  
 6 comparison. Coefficient of determination ( $R^2$ ) as well as the slope of the linear regressions  
 7 (LRS) are reported

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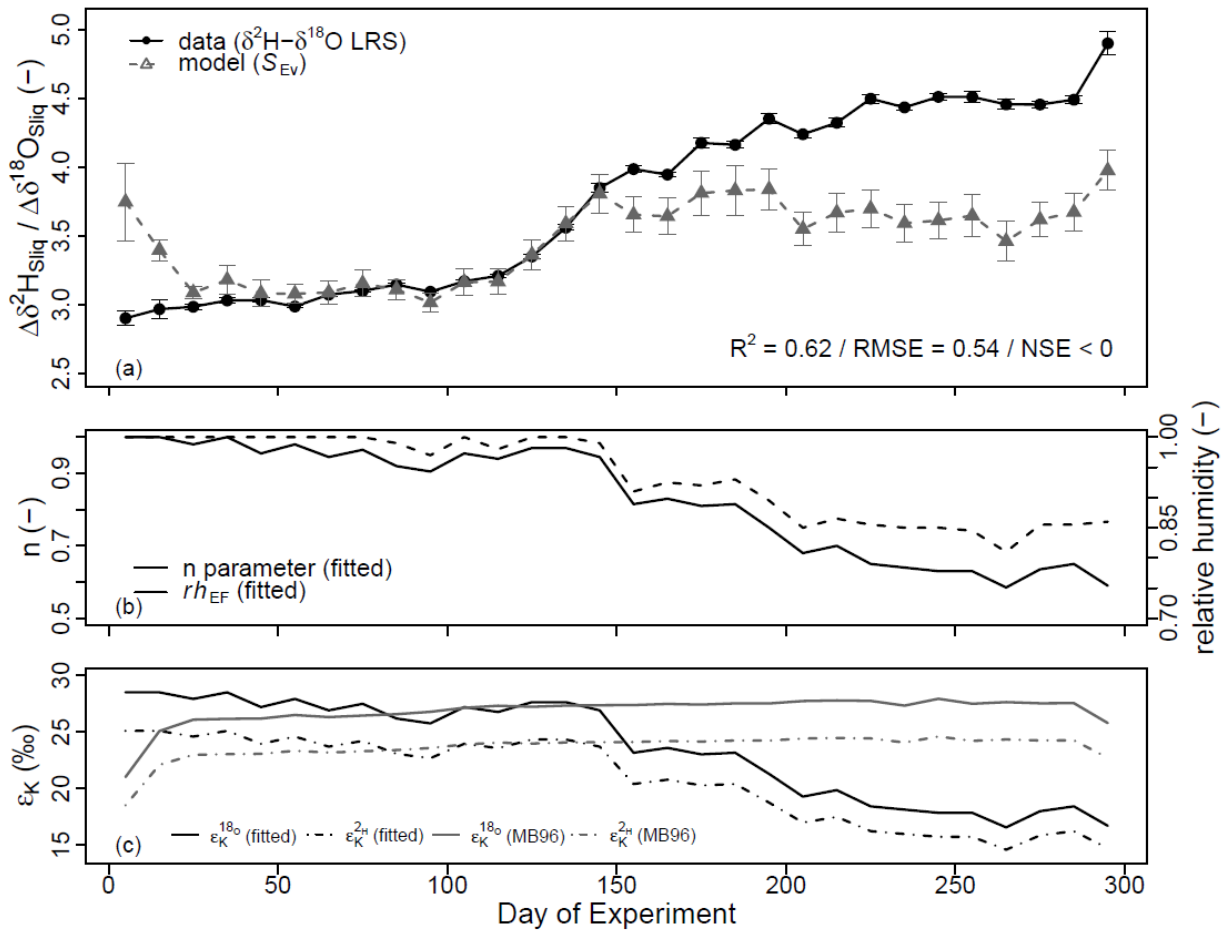
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 2 Figure 7. Time course of the slopes of the  $\delta^{18}\text{O}$ - $\delta^2\text{H}$  linear regressions (LRS) for time  
 3 intervals of ten consecutive days of atmosphere data (gray solid line), soil data from the upper  
 4 three layers (01, 03, and 05 cm, colored solid lines), and combined soil data from the  
 5 remaining bottom layers (from 07 to 60 cm, black dotted line). Mean standard errors are  
 6 represented by the error bars in the bottom left corner  
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Figure 8. (a) and (b)  $^1\text{H}^2\text{H}^{16}\text{O}$  and  $^1\text{H}_2^{18}\text{O}$  composition gradients calculated between consecutive observation points in the soil. (c) Evolution of the evaporation front depths  $z^{18}\text{O}_{\text{EF}}$  (red solid line) and  $z^2\text{H}_{\text{EF}}$  (black solid line) inferred from the  $^1\text{H}^2\text{H}^{16}\text{O}$  and  $^1\text{H}_2^{18}\text{O}$  composition gradients





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2 Figure 9. (a) Comparison between soil liquid water  $\delta^{18}\text{O}$ - $\delta^2\text{H}$  linear regressions slopes (LRS,   
3 solid black line) calculated for time intervals of ten consecutive days and simulated time   
4 series of evaporation line slope ( $S_{\text{Ev}}$ , dotted gray line) obtained from Equations (3-6) (Gat et   
5 al., 1971, Merlivat, 1978, Mathieu and Bariac, 1996). Black error bars give the standard errors   
6 of the estimated  $\delta^{18}\text{O}$ - $\delta^2\text{H}$  LRS. Gray error bars are the standard errors associated with   
7 calculation of  $S_{\text{Ev}}$  following Phillips and Gregg (2001). Coefficient of determination ( $R^2$ ),   
8 Root Mean Square Error (RMSE) and Nash and Sutcliffe Efficiency (NSE) between model   
9 and data are reported. (b) Time series of  $n$  parameter (Eq. (6)) and soil relative humidity at the   
10 Evaporation Front ( $rh_{\text{EF}}$ ) that provided the best model-to-data fit. (c)  $\epsilon_{\text{K}}^{2\text{H}}$  and  $\epsilon_{\text{K}}^{18\text{O}}$  time series   
11 obtained from fitted  $n$  values (“fitted”) and calculated following Mathieu and Bariac (1996)   
12 (“MB96”)