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**Non-stationarity in
annual maxima
rainfall across
Australia**

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A. S. Kiem

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Non-stationarity in annual maxima rainfall across Australia – implications for Intensity–Frequency–Duration (IFD) relationships

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Abstract

Rainfall Intensity–Frequency–Duration (IFD) relationships are commonly required for the design and planning of water supply and management systems around the world. Currently IFD information is based on the “stationary climate assumption” – that weather at any point in time will vary randomly and that the underlying climate statistics (including both averages and extremes) will remain constant irrespective of the period of record. However, the validity of this assumption has been questioned over the last 15 years, particularly in Australia, following an improved understanding of the significant impact of climate variability and change occurring on interannual to multidecadal timescales. This paper provides evidence of non-stationarity in annual maxima rainfall timeseries using 96 daily rainfall stations and 66 sub-daily rainfall stations across Australia. Further, the effect of non-stationarity on the resulting IFD estimates are explored for three long-term sub-daily rainfall records (Brisbane, Sydney and Melbourne) utilising insights into multidecadal climate variability. It is demonstrated that IFD relationships may under- or over-estimate the design rainfall depending on the length and time period spanned by the rainfall data used to develop the IFD information. It is recommended that non-stationarity in annual maxima rainfall be explicitly considered and appropriately treated in the ongoing revisions of Engineers Australia’s guide to estimating and utilising IFD information, “Australian Rainfall and Runoff”, and that clear guidance needs to be provided on how to deal with the issue of non-stationarity of extreme events (irrespective of whether that non-stationarity is due to natural or anthropogenic climate change). The findings of our study also have important implications for other regions of the world that exhibit considerable hydroclimatic variability and where IFD information is based on relatively short data sets.

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1 Introduction

Information on rainfall event intensity, frequency and duration (IFD, or IDF as it is known in some countries) plays a critical role in the design of dams, bridges, stormwater drainage systems and floodplain management. Dependent upon the application, information is required for event-durations ranging from hours to several days. The development of IFD relationships were first proposed by Bernard (1932) and since then different versions of this relationship have been developed and applied worldwide (e.g. Bara et al., 2009; Chen, 1983; Hershfield, 1961; IHP-VII 2008; Nhat et al., 2006; Raiford et al., 2007).

Historically, in Australia, IFD design rainfall curves were developed by the Australian Bureau of Meteorology (BoM) for durations ranging from 5 min to 72 h and Average Return Intervals (ARI) of 1 to 100 years (however, recently additional durations and ARIs have also been developed). Up until very recently IFD information available to (and used by) engineers and hydrologists were developed 25 years ago, as part of Engineers Australia publication Australian Rainfall and Runoff (AR&R) in 1987. New IFD information was released early in 2013 after a major revision of IFD information carried out by Engineers Australia. Importantly, the revised IFD information is based on a longer and more extensive rainfall data set (<http://www.bom.gov.au/water/designRainfalls/ifd/>). However, the BoM and Engineers Australia still recommend to use the AR&R 1987 information for existing flood studies and the probabilistic rational method and to conduct sensitivity testing with the revised 2013 AR&R parameters including the new IFD design rainfalls (<http://www.bom.gov.au/water/designRainfalls/ifd/index.shtml>).

At the time of writing, the revised IFD information does not take into account the impact of climate change on IFD estimates. This is part of ongoing research commissioned through Engineers Australia. It is also not yet clear how or if the role of natural climate variability is going to be considered. Of concern is the fact that currently, estimates of IFD are based on the assumption that “climatic trend, if it exists in a region, has negligible effect on the design intensities” (Pilgrim, 1987). This is known as the

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“stationary climate assumption” n (i.e. the statistical properties of the rainfall do not change over time) and implies that the chance of an extreme event occurring is the same at any point in time (past or future). However, the validity of this assumption has been questioned over the last 15 years following demonstration of the significant impact of climate variability occurring on interannual to multidecadal timescales in Australia. For example, research has shown that annual maximum flood risk estimates in Australia vary depending on climate state (e.g. Ishak et al., 2013; Kiem et al., 2003; Leonard et al., 2008). Importantly these studies demonstrate that founding flood risk estimates on an unsuitable time period has the potential to significantly underestimate (or overestimate) the true risks. This may apply to design rainfall also given that current IFD estimates are based on varying lengths of data spanning different time periods (the latest IFD estimates are based on all daily-read stations with 30 or more years of record and all continuously-recording stations with more than 8 years of record).

Khaliq et al. (2006) explained that the traditional idea of probability of exceedance and return period are no longer valid under non-stationarity. Recently, Jakob et al. (2011a) investigated the assumption of stationarity in rainfall frequency analysis and found that quantile estimates derived for Sydney Observatory Hill for the period 1976 to 2005 show significant decreases across durations from 6 min to 72 h. Jakob et al. (2011b) subsequently extended the sub-daily rainfall data analysis to 31 sites located in southeast Australia, assessing variations in frequency and magnitude of intense rainfall events across durations from 6 min to 72 h. This study identified two different trends in the data sets, a decreasing trend in frequency of events at durations of 1 h and longer for sites in the north of the study region, while sites in the south cluster displayed an increase in frequency of events, particularly for sub-hourly durations. Importantly Jakob (2011a, 2001b) concluded that, for at least some regions of Australia, non-stationarity found in historical records has the potential to significantly affect design rainfall estimates. Westra and Sisson (2011) also investigated evidence of non-stationarity in extreme precipitation at sub-daily and daily timescales (1965–2005) using a spatial extreme value model. They identified a statistically significant increasing

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trend in precipitation extremes for the sub-daily data set, however at the daily timescale no change in annual maximum rainfall could be detected with the exception of south-west Western Australia (Westra and Sisson, 2011). Further, Yilmaz and Perera (2014) conducted change point analysis for extreme rainfall data for storm durations ranging from 6 min to 72 h in Melbourne, and found evidence of non stationarity, concluding the year 1966 as a statistically significant change point. Yilmaz et al. (2014) then investigated extreme rainfall non-stationarity through trend analysis, non-stationarity tests and non-stationary GPD models (NSGPD) for Melbourne. They found statistically significant extreme rainfall trends for storm durations of 30 min, 3 and 48 h, however for above storm durations there was no evidence of non-stationarity according to statistical non-stationarity tests and non-stationary GPD.

A limitation of the analysis presented by Westra and Sisson (2011) and Jakob et al. (2011a, b) is that they tested for linear trends in the rainfall data series based on the hypothesis that extreme rainfall events would have either decreased, increased or exhibited no trend over the time period being investigated. However these are not the only attributes of non-stationarity, since annual rainfall maxima may also cycle through interannual to multidecadal periods (note that Westra and Sisson (2011) also investigated possible links between extreme rainfall and annual fluctuations in the El Niño/Southern Oscillation (ENSO)). Therefore, depending on what time period the annual rainfall maxima data are derived from (in reference to any long term cycles or epochs) the observed trends may be misleading or even not apparent (leading to the misconception that non-stationarity is non-significant or not an important consideration). Recently Yilmaz et al. (2014) investigated the potential impact of the Interdecadal Pacific Oscillation (IPO) on extreme rainfall and resulting IFD for a case study in Melbourne. They concluded that, the IPO negative phase can be the driver of higher rainfall intensities for long durations and high return periods. However, the trends in extreme rainfall data and differences in rainfall intensities for short storm durations and return periods could not be explained with the IPO influence. Given that Melbourne is located in South Australia, where the influence of the IPO is temporally variable due to

other climate drivers operating (acting to enhance or suppress impacts, see Kiem and Verdon-Kidd, 2010, 2009), the research by Yilmaz et al. (2014) provides promise for developing relationships between extreme rainfall and the IPO for regions where the IPO has a stronger, more consistent influence (such as north-eastern Australia).

Therefore this paper aims to establish if there is evidence of non-stationarity in the annual maxima rainfall timeseries (1 h to 7 days) across Australia by testing for shifts (regardless of direction or timing) in the long term sub-daily and daily data. Further, the implications for non-stationarity on IFD estimation are explored, along with the potential influence of the IPO on extreme rainfall and resulting IFD for three case study locations – Brisbane, Sydney and Melbourne. Recommendations are then provided as to how these insights may be incorporated in future revisions of AR&R.

2 Data and methods

2.1 Data

2.1.1 Rainfall data

Sub-daily and daily rainfall data for Australia were obtained from the BoM. Sub-daily data records from continuously recording (i.e. pluviograph) rainfall stations in Australia tend to be relatively short, hindering the ability to conduct trend and attribution studies. In this study pluviograph rainfall stations were chosen with data spanning at least 40 years and at least 90 % complete, resulting in 66 stations (see Fig. 1a). In order to address the concerns raised in the Introduction about short term data analysis (note that according to Raiford et al. (2007) ARI should not be extrapolated from more than twice the record length), three long-term data sets, highlighted in Fig. 1a, were chosen for further analysis that contained data from at least 1913 onwards (Brisbane Aero, Sydney (Observatory Hill) and Melbourne Regional Office).

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Daily rainfall stations with data spanning the period 1900 to 2009 were selected in order to capture as much temporal variability as possible (see Fig. 1b). These stations were filtered according to the amount of data missing in order to identify the highest quality stations recording rainfall during this period, resulting in 96 being considered suitable for further analysis. Due to variability in the quality and quantity of rainfall data in each State of Australia, the following selection criteria were applied:

- New South Wales, Queensland and Victoria – selected stations are at least 97 % complete;
- Tasmania – selected stations are at least 90 % complete; and
- South Australia, Northern Territory and Western Australia – selected stations are at least 85 % complete.

2.1.2 Climate index data

The climate of Australia has experienced a number of “shifts” in climate during its history, resulting in sustained periods of above average rainfall and storminess and abnormally cool temperatures, followed by the reverse conditions (i.e. droughts and elevated bushfire risk) (e.g. Erskine and Warner, 1988; Franks and Kuczera, 2002; Kiem et al., 2003; Kiem and Franks, 2004; Verdon et al., 2004). These “shifts” have tended to occur every 20 to 30 years and are associated with changes in the Interdecadal Pacific Oscillation (IPO, Power et al., 1999). The IPO represents variable epochs of warming (i.e. positive phase) and cooling (i.e. negative phase) in both hemispheres of the Pacific Ocean (Folland et al., 2002). Importantly, the IPO has been shown to influence the magnitude and frequency of flood and drought cycles across eastern Australia (Kiem et al., 2003; Kiem and Franks, 2004). In New Zealand, the IPO is also associated with similar shifts in flood frequency (McKerchar and Henderson, 2003). It has been noted that, following the abrupt shift in the IPO in the mid 1970s, the period, amplitude, spatial structure and temporal evolution of ENSO markedly changed (Wang and An, 2001).

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Historically, during negative phases of the IPO there tends to be more La Niña (wet) events and fewer El Niño (dry) events (Kiem et al., 2003; Verdon and Franks, 2006), resulting in an overall “wet” epoch for eastern Australia and New Zealand. While during the positive phase of the IPO there tends to be a higher frequency of El Niño events and fewer La Niña events (Kiem et al., 2003; Verdon and Franks, 2006), resulting in an overall “dry” epoch. In this study negative phases of the IPO were defined as 1913–1920 and 1945–1977, while positive phases included 1921–1944 and 1978 to 2010.

2.2 Statistical tests

A 20 year moving window was used to test for low frequency variability in the annual maxima timeseries (1 h, 1 and 7 days). A Mann–Whitney U test was then used to determine the statistical significance of possible phase shifts by testing if the first 10 years of data was significantly different from the second 10 years, within the 20 year window (the null-hypothesis in this case was that the data was independently distributed). If the difference in medians was found to be statistically significant (i.e. p value < 0.05) and there was a change in sign of the median values (e.g. switch from negative to positive), a climate shift was postulated to have occurred during the 10th year of the window. The Mann–Whitney U test is a robust test that does not place implicit assumptions on the underlying distribution of the data (i.e. it is a distribution free test), which is particularly appropriate here due to the small number of years used in each window (Kundzewicz and Robson, 2004). Note that a number of different size windows were also tested, however this did not change the results or conclusions.

A second test was also applied to identify step changes in the 1 and 7 day annual maxima time series known as the distribution free CUSUM with resampling (note that the test was not applied to the shorter sub-daily data as longer data sets are recommended for this method). CUSUM tests whether the means in two parts of a record are different (for an unknown time of change). The second test was applied as it does not require the use of a moving window (which is a limitation of the Mann–Whitney U test

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described above). However the CUSUM test sequentially splits the timeseries into two halves which may be a problem if more than one cycle/shift is present in the timeseries.

2.3 IFD calculation

The standard process for obtaining IFD information for a location is to refer to the six master charts of rainfall intensity for various durations and ARIs covering all of Australia in Volume 2 of AR&R 2001. Alternatively, IFD curves can be obtained for any location in Australia via the BoM website (both the AR&R 1987 and revised IFDs are available). This information is based on regionalised estimates of IFDs that are spatially and temporally consistent. However, this approach cannot be adopted when using the instrumental rainfall data required for the analysis presented in this study. As such, the IFD information generated for this project follows the methodology on which the IFDs were based for AR&R 1999 which utilises point source data with no regionalisation. It should be noted that it is not the purpose of this paper to compare different methods of generating IFDs, rather, one method has been adopted in order to provide a comparative assessment of the impact of non stationarity on IFD estimation. The AR&R 1999 procedure used to generate IFDs from raw rainfall data (i.e. point based estimates) is summarised as follows:

- A log-Pearson III distribution was fitted to the annual maxima timeseries using the method of moments (for annual maxima series of 30 min to 72 h duration). This is the standard distribution that has historically been adopted for generating IFDs in Australia; however other distributions have recently been tested as part of the revision of AR&R. To test if this distribution is suitable for the region being studied, the goodness of fit for the log-Pearson III was tested using a Kolmogorov Smirnov (KS) test. It was found that distribution gave a statistically significant fit to the annual maxima timeseries data;
- The coefficient of skewness was determined for each duration (30 min to 72 h);

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– The coefficient of skewness was then used to obtain a frequency factor, K_Y , for use with Log-Pearson III Distribution. K_Y was obtained from Table 2.2 (positive skew coefficients) and Table 2.3 (negative skew coefficients) in AR&R 1999 Book 4;

– Rainfall intensities for a range of ARI were calculated using the following formula:

$$\log RI_Y = M + K_Y S \quad (1)$$

Where:

RI_Y = rainfall intensity having an ARI of 1 in Y

M = mean of the logarithms of the annual maxima rainfalls

S = Standard deviation of the logarithms of the annual maxima rainfalls

K_Y = frequency factor for the required ARI of 1 in Y

– ARIs of 2 to 10 years were adjusted to partial-duration series estimates. In AR&R 1999, the following correction factors were used (note: for ARI greater than 10 years, no corrected factor is required): 2 year ARI – 1.13, 5 year ARI – 1.04, 10 year ARI – 1.0.

It should be noted that this approach is likely to result in different estimates of IFDs than those obtained from the standard maps provided by AR&R 1999 or the revised IFD estimates released in 2013. Here we are using point based rainfall data, whereas AR&R 1999 have derived regionalised estimates based on multiple rainfall stations with varying lengths of data, varying resolution (daily and pluviograph) and varying quality of records. It is recognised that analysis of rainfall data from single stations is often unreliable, is not temporally or spatially consistent and should generally not be used for design purposes. However, the use of point based rainfall data satisfies the specific aims of this study (which is a comparative analysis) and is therefore considered appropriate.

3 Results

3.1 Test for non-stationarity in the annual maxima rainfall timeseries

Significant step changes identified in the extreme rainfall timeseries are shown in Fig. 2. Of the 66 sub-daily rainfall stations tested, 40 (61 %) displayed at least one step change in the 1 h annual maxima timeseries (Fig. 2a), with some stations exhibiting multiple shifts. Of the 96 daily rainfall stations tested, 86 displayed at least one step change in the 1 day annual maxima timeseries (Fig. 2b), while 92 exhibited at least one shift in the 7 day annual maxima timeseries (Fig. 2c), and some stations exhibited multiple shifts. Figure 2 collectively shows that observed step changes (or non-stationarity) in annual maxima rainfall are not confined to any one particular region of Australia, with most stations analysed exhibiting at least one statistically significant shift.

As shown in Fig. 3, the CUSUM test yielded fewer stations with statistically significant step change in the annual maxima timeseries (only 18 stations out of 96) and many of these were clustered along the coastal fringe of eastern Australia (note that, although the total number of stations displaying significant non-stationarity was the same for both the 1 and 7 day annual maxima, in some cases the location of the stations differed between the two). However, as stated previously a limitation to this method is that only one significant change can be detected using the CUSUM test (given that the data is sequentially split into two halves during testing). This can be a problem if more than one step change or cycle in the data is present (see example timeseries in Fig. 4). Therefore, while the number of stations displaying non-stationarity is reduced using the alternative method, the results do in fact support the theory that non-stationarity in the annual timeseries is present for some stations at different durations.

The temporal consistency of step changes in the annual maxima timeseries was further investigated (Fig. 5a) and it was found that observed shifts were not necessarily consistent across Australia. However, for some regions (e.g. the east coast of Australia) periods such as the 1940s and 1970s display a higher degree of spatial consistency, particular along the east coast (Fig. 5b).

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Instability and storminess can result during periods when a number of climate driving mechanisms interact (e.g. El Niño/Southern Oscillation, Indian Ocean Dipole and the Southern Annular Mode) to influence the occurrence of regional weather systems such as east coast lows and cut off lows (Pook et al., 2006; Verdon-Kidd and Kiem, 2009).

However, the large-scale climate phenomena impact various regions of Australia at different times of the year and to varying degrees, therefore it is not surprising that the timing of shifts in the annual maxima timeseries varies spatially and temporally. This highlights the limitations of trying to assess and attribute variability in annual maxima rainfall based on a single climate driver (e.g. ENSO) or attempting to address the issue of non-stationarity for the whole of Australia using one simple approach or model.

3.2 Effect of non-stationarity on IFD estimation

Section 3.1 provided evidence of non-stationarity in the annual maxima timeseries for a range of durations. This non-stationarity may ultimately influence the IFD estimation depending on the length of data, and the time period it comes from, and therefore the underlying climatic state (or combination of states). Current IFD estimates for Australia (both the 1987 and 2013 versions) are based on data as short as 30 years for the daily-read stations and 8 years for the sub-daily data. Therefore IFD estimates based on relatively short-term data sets may under- or over-estimate rainfall intensities, depending on where the data series fits within the long term context (i.e. before or after a shift in annual maxima).

For many east coast stations a shift in 1 day annual maxima (along with the 7 day) occurred around the 1940–1950s and again in the 1970s. This timing also corresponds to well-known periods of change in the IPO (see Sect. 2.1.2 for a description of the IPO and its influences). Therefore, to further explore the issue of non-stationarity, breakpoints in the IPO were used to stratify the annual maxima rainfall timeseries into IPO positive and negative epochs for the three long sub-daily data sets described in Sect. 2.1.1 (i.e. Brisbane, Sydney and Melbourne, see Fig. 1a for location). The reason for selection of these stations was twofold. Firstly, for all three stations, a shift in the

annual maxima timeseries (for 1 and 7 day) was observed during the 1940s and again in the 1970s, and secondly the stations contain long records of pluviograph data (the shortest being from 1913 onwards). Figure 6a shows the modulating effect of the IPO on total annual rainfall for the three east coast stations. Annual maxima at the three east coast stations during the two IPO epochs are also shown in Fig. 6 (b–d) for event durations of 30 min to 72 h (durations that are critical for flood design applications).

It is evident from Fig. 6a that the effect of the IPO on annual rainfall totals (as measured by the largest difference between the two rainfall distributions associated with each climate phase) is greatest for Brisbane and Sydney, while Melbourne does not appear to be greatly influenced by the IPO in terms of annual rainfall variability. This is due to the fact that the southern regions of Australia are affected by other climate modes than those arising from the Pacific (i.e. the Southern Annular Mode and the Indian Ocean Dipole (e.g. Kiem and Verdon-Kidd, 2010; Gallant et al., 2012)). Regions such as Brisbane and Sydney tend to be dominated by Pacific Ocean influences (e.g. Verdon et al., 2004). Figure 6b shows annual maxima rainfall tends to be higher during IPO negative on average for durations 6 h and longer at Brisbane (though not statistically significant), while Fig. 6c confirms the same to be true for Sydney for durations 2 h and longer (statistically significant at 95 % using a Wilcoxon Rank Sum test). Interestingly, it was found that IPO positive periods have resulted in higher annual maxima for durations 30 min and 2 h at Brisbane. This result is consistent with Yilmaz et al. (2014) who also found that the IPO could be responsible for higher rainfall intensities for long durations and high return periods but not so for short storm durations and return periods.

Irrespective of the fact that the annual rainfall totals for Melbourne do not show any significant difference between the two phases of the IPO, there does appear to be a consistent relationship between IPO and the sub-daily and daily statistics (Fig. 6d), whereby the median of the IPO positive distribution is higher across all durations, however IPO negative is associated with less frequent but more extreme events. For events 24 h and longer, the IPO negative distribution also shows a much higher degree of vari-

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ability than smaller durations, with the “box and whiskers” extending beyond the IPO positive counterpart for these longer durations. This suggests that while IPO might not be as dominant in southeastern Australia as it is further to the north it still has some influence that needs to be better understood.

5 IFD information was generated using rainfall data from the two IPO phases and the methodology outlined in Sect. 2.1 for durations 30 min through to 72 h and ARI 2 to 100 years. Figure 7 shows the difference in rainfall intensity between IPO positive and IPO negative estimates.

10 Figure 7 demonstrates clear differences in the resulting rainfall intensities estimated for each duration and ARI using the two different data sets (i.e. rainfall data from either IPO negative or IPO positive). The difference in rainfall intensity estimated is as great as 45% in some cases. These results are not unexpected given that the annual maxima rainfall distributions were different between the two climate states. In almost all cases, the magnitude of the difference in rainfall intensity estimated using the different data periods is greater for less frequent events (e.g. 50 year, 100 year ARIs), highlighting that uncertainty is greatest with less frequent events. The results presented in Fig. 7 also highlight the fact that it cannot be assumed that one particular climate state (e.g. IPO negative) will always result in a higher rainfall intensity estimate for all durations and all ARI for all regions in Australia. For example, rainfall intensity for the 30 min events was estimated to be higher in IPO positive for both Brisbane and Sydney, yet the reverse is true for events of duration 2 and 6 h. Similarly, all events (other than 20 72 h) with a 2 year ARI are associated with a higher rainfall intensity estimate in IPO positive for Melbourne, however the reverse is true for the less frequent events. This is consistent with the observations made from Fig. 6d that the median annual maxima of the IPO positive distribution is higher (for Melbourne) across the range of durations, however the IPO negative periods were associated with less common but much more extreme events.

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4 Discussion and conclusions

An analysis of non-stationarity of the annual maxima timeseries (1 h, 1 and 7 day) has been carried out using a set of high quality rainfall stations across Australia. It was found that non-stationarity in the annual maxima timeseries does indeed exist for the majority of stations for various durations. Further it was demonstrated using three long term sub-daily rainfall stations along the east coast that this non-stationarity impacts upon the resulting IFD estimation. The potential for Pacific Influences (i.e. the IPO) to influence the resulting IFD estimation was explored in order to demonstrate the issue of non-stationarity. The authors acknowledge that the IPO is unlikely to be the only driver of variability in the annual maxima timeseries across Australia, and it is recommended that future research should aim to identify other potential drivers of this variability.

These findings highlight the fact that in some instances the IFD estimates currently being used are likely to be either under- or over-estimated at any one time depending on the length of data, and climatic state, from which they were derived. This is a particular concern given that current regionalised IFD information is based on data of varying length (as short as 8 year in the case of sub-daily data) spanning different time periods. An over estimation of rainfall intensity for a given duration could impact on construction costs, while the risks of underestimating rainfall intensities could result in failure of design criteria. That is, the risk is dependent on the application and length of time over which the risk is assessed.

Further revisions of AR&R are currently underway to include an assessment of the potential impacts of climate change on IFD estimates. However, there are many uncertainties associated with climate change projections, particularly when extracting information on timescales shorter than a season and particularly for hydrological extremes (e.g. Blöschl and Montanari, 2010; Kiem and Verdon-Kidd, 2011; Koutsoyiannis et al., 2008, 2009; Montanari et al., 2010; Randall et al., 2007; Stainforth et al., 2007; Stephens et al., 2012; Verdon-Kidd and Kiem, 2010). Therefore, assessing future changes in extreme events that occur over short durations (e.g. min to days) is in-

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herently difficult. Furthermore, climate projections are presented in terms of a percent change from a particular baseline. However, the baseline is often inconsistent and ill-defined leading to very different estimates of risk depending on the time over which the baseline is calculated (as has been demonstrated in this paper). The research presented here demonstrates that information currently available on natural variability is extremely useful in providing a better assessment of the true risk profile and can act as a guide to the baseline on which climate change projections may be applied.

It is recommended that non-stationarity in annual maxima rainfall be considered and appropriately treated in any further updates of AR&R. One way to do this may be to only utilise data sets of similar length ensuring that they span a sufficient number of years in order to capture data from epochs of both high or low annual maxima (to remove bias towards one climatic phase or another). However, it is acknowledged that this would potentially result in discarding a large amount of data. Further, a separate set of IFDs could be developed for use in high risk modelling for engineers who need to account for the “worst case” (in a similar manner to climate change allowances). This second set of IFD could be developed based on the periods of elevated annual maxima alone (for those stations with clearly defined epochs of annual maxima) such that if we were to enter such an epoch, designs based on these estimates would be robust for the duration of such a period. This would have to be assessed and calculated on a region by region basis given that Australia is a country associated with high spatial and temporal rainfall variability caused by numerous large-scale climate drivers and regional weather phenomena. Finally, any revised estimates of annual maxima should be compared in terms of uncertainty bounds (e.g. following Koutsoyiannis, 2006). Uncertainty analysis, which takes into account both the data availability and variability within the observation period would provide relevant information to practitioners about the reliability of IFD estimates.

Based on the results of this study, and literature cited within this paper, we emphasise that there undoubtedly is non-stationarity in historical short duration rainfall extremes but the characteristics and causes of this non-stationarity vary from location to loca-

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tion and decade to decade – something which must be considered and accounted for when attempting to estimate IFD design rainfalls and prior to quantifying how those IFD estimates might change in the future.

While the analysis presented here has been conducted using rainfall data from Australia alone, the recommendations provided are likely to be applicable for other regions of the world where IFD information is based on short term records and particularly for locations with a highly variable climate.

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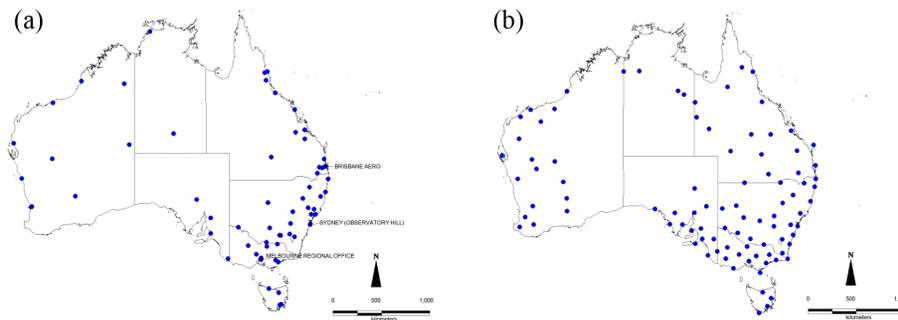


Figure 1. (a) Reference stations for sub-daily stations, (b) Reference stations for daily rainfall. Note the three long term sub-daily stations used in the IFD analysis are also labelled.

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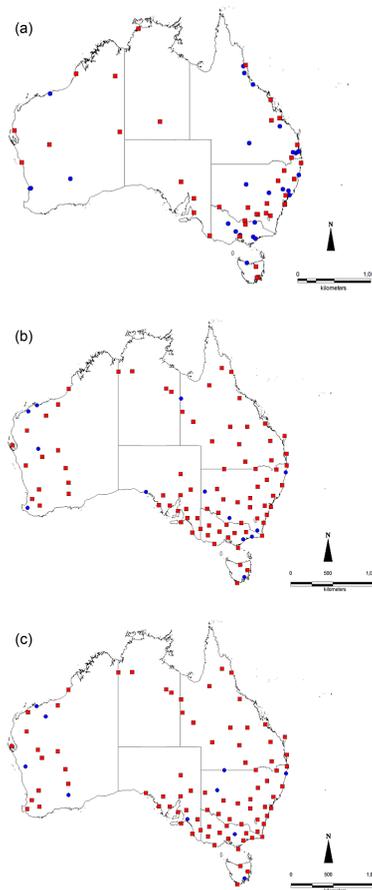
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Figure 2. Stations (in red) with at least one statistically significant step change in the **(a)** 1 h, **(b)** 1 day, **(c)** 7 day annual maximum rainfall (using the Mann–Whitney U test).

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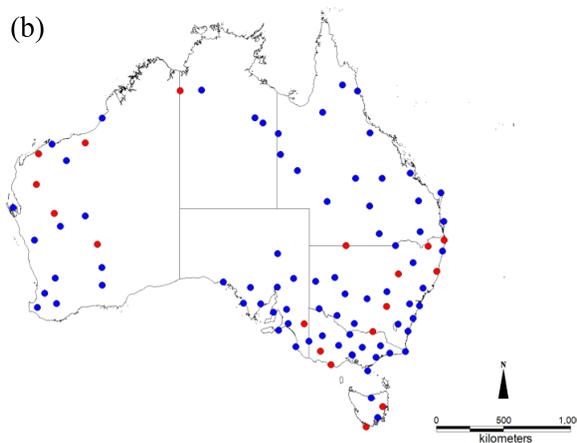
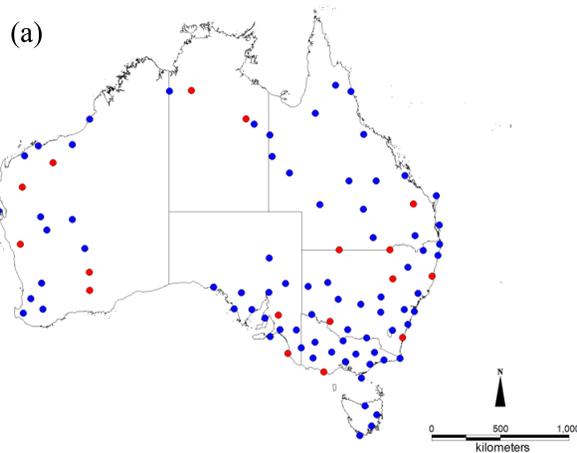


Figure 3. Stations (in red) with at least one statistically significant step change in **(a)** the 1 day and **(b)** 7 day annual maximum rainfall (using the CUSUM test with resampling).

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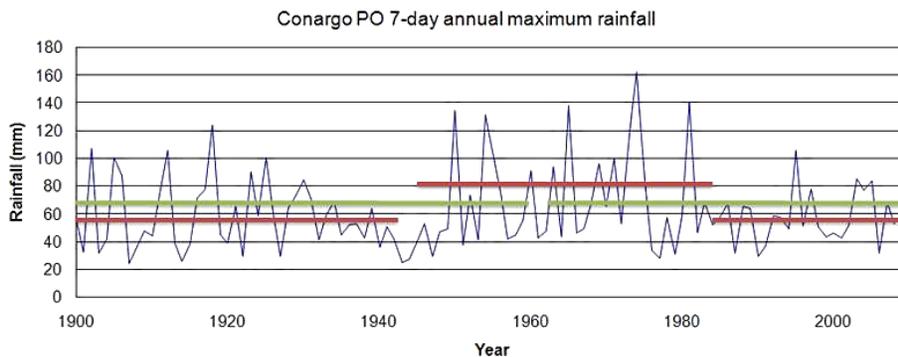


Figure 4. Example of inadequate identification of non-stationarity using CUSUM test (red line highlights three distinct epochs of high/low rainfall, while green line demonstrates effect of splitting the data into two sections for CUSUM test).

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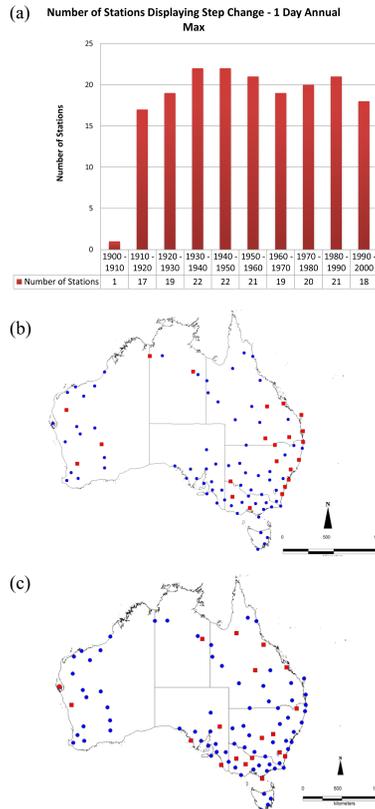


Figure 5. (a) number of stations each decade displaying evidence of a step change in 1 day annual max, (b) Stations (in red) with at least one statistically significant step change in the 1 day annual max during 1940–1950 (using the Mann–Whitney U test), (c) Stations (in red) with at least one statistically significant step change in the 1 day annual max during 1970–1980 (using the Mann–Whitney U test).

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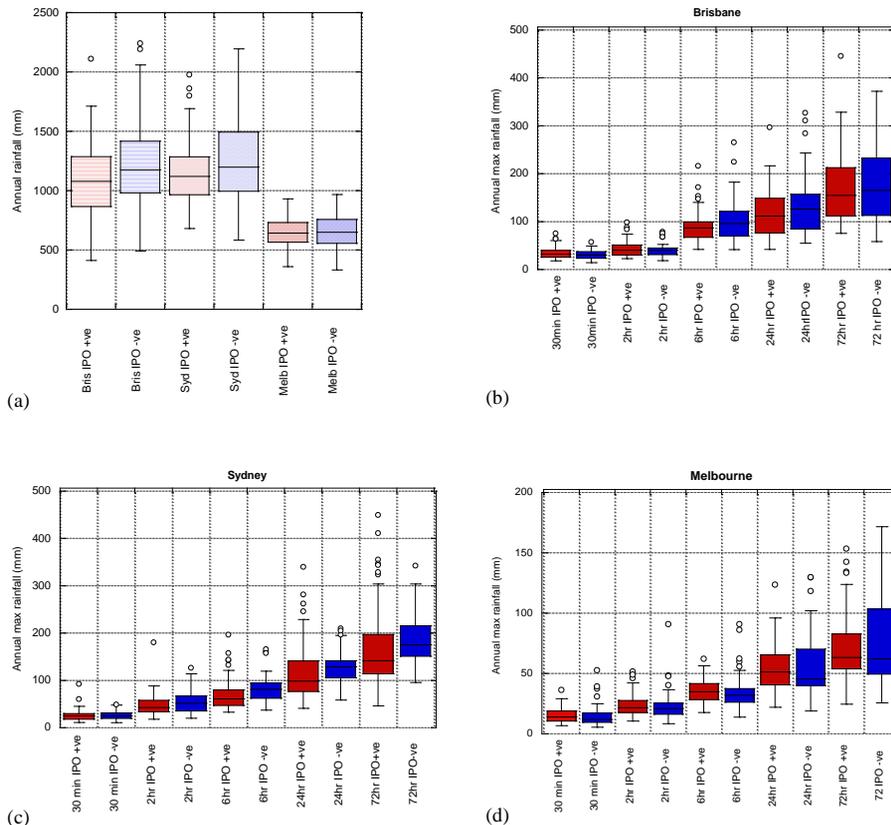


Figure 6. Relationship between IPO and (a) total annual rainfall, and annual maximum rainfall at various durations for (b) Brisbane, (c) Sydney and (d) Melbourne.

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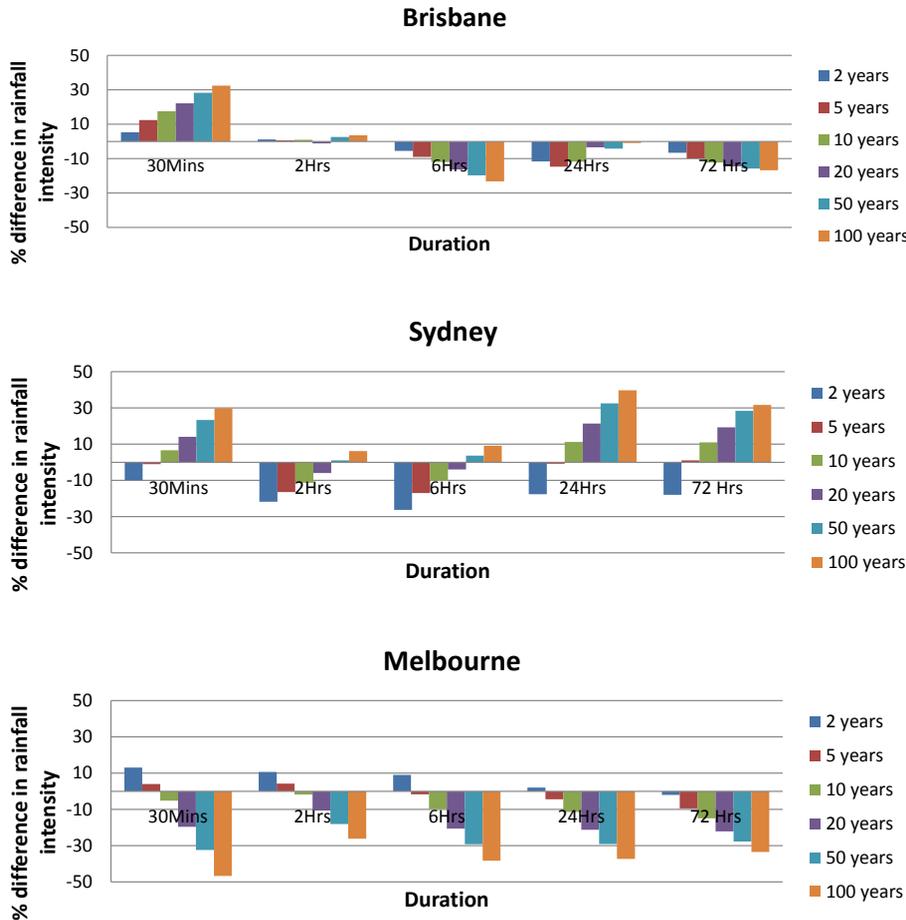


Figure 7. Difference in rainfall intensity for each duration and ARI. Positive (negative) values represent an increase (decrease) in rainfall intensity during IPO positive compared to IPO negative.

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