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Use of satellite and modelled soil moisture data for predicting event soil loss at plot scale

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Abstract

The potential of coupling soil moisture and a USLE-based model for event soil loss estimation at plot scale is carefully investigated at the Masse area, in Central Italy. The derived model, named Soil Moisture for Erosion (SM4E), is applied by considering the

- ⁵ unavailability of in situ soil moisture measurements, by using the data predicted by a soil water balance model (SWBM) and derived from satellite sensors, i.e. the Advanced SCATterometer (ASCAT). The soil loss estimation accuracy is validated using in situ measurements in which event observations at plot scale are available for the period 2008–2013.
- ¹⁰ The results showed that including soil moisture observations in the event rainfallrunoff erosivity factor of the RUSLE/USLE, enhances the capability of the model to account for variations in event soil losses, being the soil moisture an effective alternative to the estimated runoff, in the prediction of the event soil loss at Masse. The agreement between observed and estimated soil losses (through SM4E) is fairly satisfactory
- ¹⁵ with a determination coefficient (log-scale) equal to of ~ 0.35 and a root-mean-square error (RMSE) of ~ 2.8 Mg ha⁻¹. These results are particularly significant for the oper-ational estimation of soil losses. Indeed, currently, soil moisture is a relatively simple measurement at the field scale and remote sensing data are also widely available on a global scale. Through satellite data, there is the potential of applying the SM4E model for lorge coefficient and eventification of the coefficient.
- ²⁰ for large-scale monitoring and quantification of the soil erosion process.

1 Introduction

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Soil is the interface between earth, air and water and hosts most of the biosphere. As soil formation is an extremely slow process, soil can be considered essentially as a non-renewable resource. Soil provides us with food, biomass and raw materials. The soil is thus recognized as a strategic non-renewable resource that, in addition to the specific relevant environmental role, assumes also that of a strategic policy frame-





work for competitiveness. Therefore, specific policies and actions designed to limit the consumption of soil are required in order to create, where possible, a barrier to stop the worrying phenomenon of progressive depletion of the resource with a consequent acceleration of erosion and geological instability. The prerequisite for the effective pro-

- ⁵ tection of the territory is to monitor processes at different spatial and temporal scales and use the obtained database to formulate, calibrate and validate predictive models needed to define the "risk areas" and to quantify this risk. Usually, these models must be properly calibrated and validated over the territory in which they are used, making use of databases and studies carried out on a local scale (Bagarello et al., 2011, 2014; Button et al., 2014; Cardà, 1000; Di Stafane, et al., 2005; Kinnell, 2010; Lab et al.
- Butzen et al., 2014; Cerdà, 1998; Di Stefano et al., 2005; Kinnell, 2010; Leh et al., 2013; Morgan and Nearing, 2000; Porto et al., 2014; Vrieling et al., 2014).

As regards soil erosion, the Universal Soil Loss Equation, USLE (Wischmeier and Smith, 1978) is the most used empirical model for the estimation of the long term average annual soil loss of a plot associated with sheet and rill erosion. The USLE

- estimates the soil loss using six factors that are associated with climate, soil, topography, vegetation and soil management. The USLE is considered the best compromise between applicability in terms of required input data and reliability of the soil loss estimates (Risse et al., 1993). It was originally formulated to estimate the soil loss in rural areas of the USA, and then extended in the Revised USLE, RUSLE (Renard et al., 1993).
- ²⁰ 1997) and further modifications (RUSLE1, RUSLE2, Foster et al., 2003). The RUSLE conserves the same mathematical structure of the USLE, the revision being limited to the estimating procedure of some of the involved factors. Currently, the USLE/RUSLE is widely applied in Europe and in many other Mediterranean countries for practical purposes (e.g. Larson et al., 1997; Huang, 1998; Rejman et al., 1999; Bagarello and ²⁵ Ferro, 2004; Morgan, 2005; Parsons et al., 2006; Bagarello et al., 2008, 2010, 2011,
- Ferro, 2004; Morgan, 2005; Parsons et al., 2006; Bagarello et al., 2008, 2010, 201
 2012; Ligonja and Shrestha, 2013).

Indeed, the failure of the process-based models to produce better results than the USLE/RUSLE model (Tiwari et al., 2000) encourages the use of the USLE/RUSLE model for purposes for which it was not designed (Kinnell, 2010). In particular, it is





widely used in watershed models even at the event temporal scale. However, it was found in the scientific literature (Todisco et al., 2009; Bagarello et al., 2008; Risse et al., 1993) that the USLE/RUSLE model, and similarly (Tiwari et al., 2000) processoriented models (e.g. Water Erosion Prediction Project, WEEP, Flanagan et al., 1995),

- tend to overestimate (underestimate) soil losses for low (high) erosive events. Foster et al. (1982) noted that the USLE model is somewhat unsatisfactory for estimating soil loss from individual storms, and observed that including rainfall amount, rainfall intensity and runoff amount in the erosivity factor provided better performance. Foster et al. (1982) also noted that erosivity factors with separate terms for rainfall and
- ¹⁰ runoff erosivity were more appropriate. Successively, Kinnell (1997) suggested that the sediment concentration for individual rainfall event is dependent on the event rainfall erosivity index per unit rainfall depth and developed the so-called USLE-M model, including direct measures of the runoff in the event rainfall–runoff erosivity factor (Kinnell and Risse, 1998; Kinnell, 2007, 2010; Bagarello et al., 2011). Bagarello et al. (2010), by
- ¹⁵ using soil loss and runoff data for a relatively high number of simultaneously operating plots of different length (11–44 m) established at the experimental station of Sparacia in southern Italy (clay soil), developed a modified version of the USLE-M, named USLE-MM, in which the event rainfall–runoff erosivity factor is raised to a power greater than one. The USLE-MM was found to perform better than both the USLE and the USLE-
- ²⁰ M at Sparacia site (Bagarello et al., 2008, 2010, 2014), and it was also successfully applied at the Masse station in central Italy, silty–clay–loam soil (Todisco et al., 2009; Bagarello et al., 2013).

Even if by including runoff in the USLE/RUSLE model improves its accuracy, it should be highlighted that the measurement of the event runoff is not straightforward. At ex-

²⁵ perimental stations, the surface runoff is generally collected into specific storage tanks allowing to estimate the event runoff by measuring the amount of water in the tanks after the end of each rainfall event (Todisco et al., 2012a).

However, this procedure is time consuming and expensive, and it requires specific measurement campaigns. Otherwise, the water amount collected in the tanks could





be measured by hydrometric gauges that, unfortunately, require strong maintenance and are not easy to be realized. It should be also underlined that by using the measured runoff, the same quantity (runoff) is used both for estimating the event soil losses (given by the product of runoff and the bulk sediment concentration in the tanks) and
 ⁵ in the rainfall–runoff erosivity factor thus introducing a conceptual issue in the model determination procedure.

In the absence of direct measurements, runoff can be estimated through rainfallrunoff modelling. The latter usually needs a specific calibration of the parameters (and structure) to provide satisfactory results and are not easy to be applied at the plot scale. Therefore, notwithstanding the USLE-M and USLE-MM models have a noticeable practical interest, these models are difficult to be applied over large areas mainly for the need to also predict event runoff (Bagarello et al., 2014). The same issue can be found in other existing USLE-derived models, as MUSLE (Williams, 1975; Williams and Berndt, 1977), EPIC (Williams et al., 1984a, b) and APEX (Williams et al., 2008), that

- explicitly consider the runoff characteristics, even with a certain detail, for the estimation of soil losses. Efforts have been recently made in order to incorporate reliable and parsimonious methods for the runoff estimation in the USLE-derived models. However, it is evident that a poor estimation of event runoff will produce a low accurate forecast of the soil loss. Gao et al. (2012) coupled a modified SCS-CN (Soil Conser-
- vation Service-Curve Number) and RUSLE model for runoff and soil loss simulation at plot scale in the Loess Plateau. In RUSLE2, runoff prediction for storm events is obtained using the SCS-CN method with empirical equations that vary the values of CN in association with both soil moisture and rainfall intensity (Kinnell, 2015). Todisco et al. (2012b) evaluated the efficiency of the MISDc model (Modello idrologico semidis-
- tribuito in continuo, Brocca et al., 2011a), coupled with an USLE-derived model, for the estimation of surface runoff and soil loss at the event time scale at Masse experimental station. The model performance is found to be promising, but it was underlined that the antecedent soil moisture proved to be a good alternative with respect to runoff for correcting the rainfall–runoff erosivity factor in the USLE-MM model. These preliminary





results open interesting scenarios for improving the capability of USLE-derived models in predicting the unit soil loss at the event scale. Indeed, measuring in situ soil moisture is much more easier (e.g. by using Time Domain Reflectometry, Brocca et al., 2014a) and less expensive than estimating surface runoff. Moreover, the recent large availabil-

- ity of satellite-derived soil moisture data (e.g. Wagner et al., 2013) might allow to easily apply over large areas a modified USLE/RUSLE model incorporating this information. In summary, it could be highly beneficial to find a procedure for incorporating soil moisture in the erosivity factor rather than runoff coefficient as in previous investigations (e.g. Kinnell, 2010; Bagarello et al., 2014).
- ¹⁰ The main objective of this study is to investigate the use of satellite-derived and modelled soil moisture data for improving the prediction of unit soil loss through a modification of USLE-based models. The Masse experimental area (Umbria, central Italy) is used as case study in which rainfall, air temperature, soil losses and runoff are measured at the event time scale for different bare plots in the period 2008–2013. The
- satellite soil moisture product is obtained from the Advanced SCATterometer (ASCAT) through the TUWien algorithm (Wagner et al., 2013). Moreover, modelled soil moisture data obtained from the Soil Water Balance Model (SWBM) developed by Brocca et al. (2014b) are also considered. The specific objective of this study is to evaluate the opportunity of using soil moisture for correcting the erosivity index of USLE
- ²⁰ model. For comparison, the results are compared with those obtained by the standard USLE/RUSLE and USLE-M-based models in previous investigations (Todisco et al., 2012b).



2 Materials

2.1 The Masse experimental station and the soil loss database

The experimental station for soil erosion measurements "Masse" (Fig. 1) of the Department of Agricultural, Food and Environmental Sciences, Perugia University, is located
 20 km south of Perugia, Umbria region (Central Italy).

The soil is Typic Haplustept (Soil Survey Staff, 2006) with a silty-clay-loam texture (clay = 34%, silt = 59% and sand = 7%). The structure of the soil is polyhedral angle and the gravel content is negligible. The depth of the Ap horizon is of approximately 0.40 m. The meteorological data are monitored by a gauging station located within the experimental site and are recorded at a time resolution of 5 min. The station includes plots of different length $\lambda = 11$ and 22 m and width w = 2, 4 and 8 m. All plots are oriented parallel to a 16% slope and are maintained in a cultivated fallow by obliterating the rills at the end of each erosive event. The total runoff amount and the soil loss per unit area are measured in each plot after an erosive event, defined as an event yielding a measurable soil loss. The Masse database was therefore developed by con-15 sidering, for each event, the simultaneous measurements of plot runoff, $Q_{e,i}$, and soil loss, $A_{e,i}$, and of the rainfall data required to derive the erosivity factor, R_{e} , according to Wischmeier and Smith (1978), with a mean interval time MIT = 6h (Bagarello et al., 2004; Mannocchi et al., 2008; Todisco, 2014). The study area and the experimental schemes, installations and procedures are already described more in depth in 20 Bagarello et al. (2011) and Todisco et al. (2012a).

To the purpose of this investigation only data collected on the $\lambda = 22 \text{ m}$ long plots (two plots with w = 4 m and two plots with w = 8 m) were considered: 63 erosive events in the period 2008–2013, 18 occurred during the dry period (from June to September) and the other 45 in the wet period; 62 events yielded a measurable runoff in the 22 × 8

²⁵ and the other 45 in the wet period; 62 events yielded a measurable runoff in the 22×8 experimental schemes corresponding to 113 plot measures; 58 events have affected the 22×4 schemes corresponding to 98 plot measures. The plot data used in this investigation are summarized in Table 1.



2.2 Soil moisture from satellite data

The satellite soil moisture product adopted in this study was obtained from the radar scatterometer ASCAT onboard the Metop satellites. ASCAT measures radar backscatter at the C-band (5.255 GHz) in VV polarization. Global coverage over Europe is achieved in ~ 1.5 days, while in Italy, measurements are available about once a day. The spatial resolution of the soil moisture product is 25 km with a sampling distance of 12.5 km. The surface soil moisture product is calculated from the backscatter measurements through a time series-based change detection approach (Wagner et al., 1999, 2013). The obtained soil moisture product is expressed in terms of degree of saturation between 0% (dry) and 100% (wet). The obtained product provides knowledge of soil moisture for a very thin surface layer (about 2 cm) while for the prediction of soil losses a root-zone soil moisture product would be required. Therefore, the Soil Water Index (SWI) method (Wagner et al., 1999) was employed to convert surface soil moisture observations into a root-zone soil moisture product, i.e. the SWI. The method relies

- ¹⁵ on the estimation of a single parameter, the characteristic time length, *T*, that was obtained by calibration. The reader is referred to Wagner et al. (1999) for more details on the SWI approach. Finally, the data were converted in volumetric unit (m³ m⁻³) through a linear rescaling approach (Brocca et al., 2011b) for matching the range of variability of satellite and modelled soil moisture data provided by the SWBM. The ASCAT data for the pixel cleaset to the Massa study area were employed
- ²⁰ for the pixel closest to the Masse study area were employed.

3 Methods

3.1 Soil moisture for erosion model

A USLE-derived model to predict the unit event soil loss was formulated, parameterized and tested with the use of soil moisture in the rainfall–runoff erosivity factor. The model was derived from the USLE:





$A = R \cdot K \cdot L \cdot S \cdot C \cdot P$

where *A* is the mean annual soil loss (Mg ha⁻¹ yr⁻¹) over the long term (e.g. 20 years), *R* (MJ mm ha⁻¹ h⁻¹ yr⁻¹) is the rainfall–runoff erosivity factor, *K* (Mg ha h ha⁻¹ MJ⁻¹ mm⁻¹) is the soil erodibility factor, *L* and *S* are the topographic factors depending on the slope length and gradient, *C* is the crop management factor, *P* is the soil conservation practice factor. Equation (1) with the erosivity factor calculated for the single erosive event, R_e (MJ mm ha⁻¹ h⁻¹), is also used to determine the plot soil loss at the event temporal scale, A_e (Mg ha⁻¹), and the corresponding unit value, A_{ue} , as follows:

$$A_{ue} = \frac{A_e}{L \cdot S \cdot C \cdot P} = R_e \cdot K.$$

¹⁰ Equation (2) estimates fairly well the average event soil losses, but it tends to overestimate the lowest and underestimate the highest values (Kinnell, 2010). The reason for this behavior is to be found in the lack of explicit consideration of runoff. In fact, although the rainfall erosivity and the soil erodibility are responsible for the detachment of soil particles, it is the runoff that transports the detached particles causing the soil loss. For that, the USLE model has been further modified to account for the relationship between soil loss and runoff. Two well-known examples are the USLE-M (Kinnell and Risse, 1998) and the USLE-MM (Bagarello et al., 2008) models, in which the event rainfall-runoff erosivity factor is given by the product of R_e and the runoff coefficient $Q_r = Q_e/h_e$, with Q_e (mm) being the event runoff and h_e (mm) the rainfall depth, as follows:

 $A_{\rm ue} = K_{\rm u} \cdot (Q_{\rm r} \cdot R_{\rm e})^{\alpha}$

with $\alpha = 1$ in the USLE-M and $\alpha > 1$ in the USLE-MM and where K_u varies in accordance with the selected model.



(1)

(2)

(3)



In this study, the Eq. (3) was modified using soil moisture, θ , in place of the runoff coefficient, Q_r , in the rainfall–runoff erosivity factor. The following model was finally formulated and named Soil Moisture for Erosion model (SM4E):

 $A_{\rm ue} = K_{{\rm u},\theta} \cdot (\theta \cdot R_{\rm e})^{\alpha}$

s with $\alpha = 1$ (linear model) and $\alpha > 1$ (power model).

The Eq. (4) was parameterized and tested using soil moisture data estimated by the Soil Water Balance Model (SWBM), $\theta = \theta_{est}$, and derived from satellite observations, $\theta = \theta_{sat}$.

3.2 Soil Water Balance Model

The Soil Water Balance Model (SWBM, Brocca et al., 2008, 2014b) was used to estimate the temporal evolution of soil moisture from standard meteorological data. SWBM considers the surface soil layer as a spatially lumped system, for which the continuous time variation of soil moisture is derived from the application of the soil water balance equation taking into account of the infiltration, evapotranspiration and drainage processes. The infiltration rate is estimated by using the Green–Ampt equation; the empirical relation of Blaney and Criddle, as modified by Doorenbos and Pruitt (1977), is used to determine the potential evapotranspiration, from which the evapotranspiration rate is computed; and the drainage rate is derived with the relation proposed by Famiglietti and Wood (1994). The model requires rainfall and air temperature data as
 input, and incorporates five parameters that are optimized as described later in the

paper. Further details on SWBM are given in Brocca et al. (2014b).

3.3 Calibration and testing

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The SM4E model, Eq. (4), and the SWBM model, require calibration. For that, the measured soil loss data at the different plots of the Masse experimental station were exploited. Specifically, only the plots with length equal to 22 m were considered. Then,



(4)



for each erosive event, the average value of the unit soil loss, A_{ue} , was computed by using Eq. (2) in which, specifically, A_e is the mean of the plot measures; *C* and *P* values are assumed equal to 1 as bare plots were used. The value of the topographic factor, $L \cdot S$, was calculated according to the relations proposed by Nearing (1997) and Renard $_5$ et al. (1997) (see Table 1).

For the analysis, the database of erosive events was splitted to define a calibration and a validation set of events: the 63 events were arranged in descending order with respect to the A_{ue} values and alternatively assigned to the calibration (n = 32 events) and the validation set (m = 31 events). The calibration set was used to optimize the five parameters of the SWBM, the characteristic time length of the SWI method, and the two coefficients ($K_{u\theta}$ and α) of the SM4E models. The parameters were defined maximizing the coefficient of determination R^2 , of the regression between the measured A_{ue} and the erosivity factor $\theta \cdot R_e$, with $\theta = \theta_{est}$ and $\theta = \theta_{sat}$. For the power model ($\alpha > 1$) R^2 is computed by a linear regression on a logarithmic scale, while for the linear model ($\alpha = 1$) as the regression between the measured an a linear

($\alpha = 1$), as the regression line is forced to pass for the origin, R^2 is computed on a linear scale as

$$R^{2} = 1 - \frac{\sum_{j=1}^{n} (A_{\text{ue},j} - A_{\text{ue}, \text{ est},j})^{2}}{\sum_{j=1}^{n} (A_{\text{ue},j} - \overline{A}_{\text{ue}})^{2}}$$

20

where $A_{ue, est, j}$ is the estimated value of A_{ue} for the *j*th erosive event (i.e. the soil loss that would result from the regression models), \overline{A}_{ue} is the average value of A_{ue} among the analyzed erosive events, *n* is the number of erosive events in the calibration subset. The validation set was used to test the accuracy and robustness of the regression models SM4E, that were evaluated by the Root Mean Square Error, RMSE, between the measured and the estimated A_{ue} values. The effectiveness of the event soil loss models was also compared with that of the USLE, the USLE-M and USLE-MM models



(5)



obtained updating the analysis performed in Todisco et al. (2012b) to the database used in the paper.

4 Results and discussion

4.1 Soil moisture estimation through modelled and satellite data

- ⁵ Based on the procedure mentioned above, the parameter values of the SWBM and of the SM4E models were obtained by maximizing the R^2 value between the observed and estimated A_{ue} values in the calibration events. Figure 2 shows the temporal evolution of the modelled and satellite soil moisture data at the beginning of the 63 erosive events occurred in the study period 2008–2013.
- ¹⁰ Notwithstanding the parameters of the SWBM and of the SWI method were calibrated for reproducing soil losses, and not to match each other the two soil moisture datasets, a very good agreement among the soil moisture time series is evident. Indeed, a very low RMSE = $0.03 \text{ m}^3 \text{ m}^{-3}$ was obtained, even for the validation sets. These results confirm the capability of the ASCAT-derived soil moisture product to pro-¹⁵ vide high-quality measurements in central Italy (Brocca et al., 2010, 2011b, 2012), even though the spatial mismatch between satellite and ground data is significant. As
- already shown in the scientific literature, these unexpected good results have to be attributed to the statistical properties of soil moisture spatial patterns (i.e. the so-called temporal stability, e.g. Brocca et al., 2014a).

20 4.2 SM4E models parameters estimation

The scatterplots in Fig. 3 show the regressions between the soil loss and the erosivity factor $\theta \cdot R_{\rm e}$ with $\alpha \ge 1$ both with $\theta = \theta_{\rm sat}$ (Fig. 3a and b) and $\theta = \theta_{\rm est}$ (Fig. 3c and d) for the set of calibration events. The linear SM4E models ($\alpha = 1$) are very similar in the scale factors $K_{\rm u,\theta} = 0.178$ and 0.180. The coefficient of determination using satellite



soil moisture data $\theta = \theta_{sat}$, $R^2 = 0.236$, is higher than that obtained with the simulated soil moisture data $\theta = \theta_{est}$, $R^2 = 0.196$. Also the power SM4E models are similar both in the scale factors equal to 0.007 and 0.006, and in the exponent α equal to 1.69 and 1.77 for the modelled and satellite data, respectively. The coefficient of determination is slightly higher for the $\theta = \theta_{est}$ ($R^2 = 0.50$), than for $\theta = \theta_{sat}$ ($R^2 = 0.46$), and in any case much higher than the linear models. The SM4E models parameters are given in Table 2 (all the events). The white dots in Fig. 3 represent the events that occurred during the dry period (from June to September) that will be commented later in the paper. The erosivity index $\theta \cdot R_e$ performs better when is raised at an exponent $\alpha > 1$, allowing to obtain higher coefficients of determination R^2 .

4.3 Soil losses prediction

The calibrated models were then tested with the validation set to estimate the soil loss, $A_{ue, est}$, by using the corresponding satellite soil moisture retrievals, $\theta = \theta_{sat}$, or the modelled ones, $\theta = \theta_{est}$, and event rainfall data. The results are given in Fig. 4, by showing the dispersion of the $(A_{ue}, A_{ue, est})$ pairs around the 1:1 line for the linear model (Fig. 4a and c) and the power model (Fig. 4b and d). The results in terms of RMSE are derived and given in Table 2 (all the events). With satellite soil moisture, $\theta = \theta_{sat}$, the RMSE obtained with the linear SM4E model is equal to 3.07 Mg ha⁻¹ (R^2 = 0.188) and slightly decreases to RMSE = $3.04 \text{ Mg} \text{ ha}^{-1}$ ($R^2 = 0.371$) when the power model is used. The errors decrease, even if not substantially, using estimated soil 20 moisture $\theta = \theta_{est}$, with RMSE = 2.85 Mg ha⁻¹ (R^2 = 0.275) and RMSE = 2.80 Mg ha⁻¹ $(R^2 = 0.338)$ with linear and power models respectively. It can be stated that the power relations generally give better estimates than the corresponding linear relations using the same erosivity factor; in particular, the models using $(\theta \cdot R_e)^{\alpha}$ as erosivity factor (both satellite and simulated θ) appear to work guite well. We note that the SM4E 25 model incorporating satellite-derived soil moisture data might effectively and easily be applied over large areas for the estimation of event water soil loss.





4.4 Comparison with the previous studies at Masse site

The results, although provide a clear indication of the higher accuracy of the power models than the linear models, also show that the coefficients of determination of the USLE-derived models that include simulated or satellite retrieved soil moisture in the erosivity factor (SM4E models) never exceed the value of 0.5, that is lower than that obtained by the USLE-M and USLE-MM ($R^2 = 0.82$) that include direct measures of the runoff in the event rainfall–runoff factor (Todisco et al., 2012b). However, the benchmark for a correct assessment of the accuracy of the SM4E models is the performance of the USLE-M and USLE-MM that include predicted runoff coefficient, $Q_{r, est}$, in the event rainfall–runoff factor like that analysed by Todisco et al. (2012b). Specifically, Fig. 5 shows the comparison of the results, in terms of RMSE and R^2 , obtained in the current study by the Eq. (4) with those obtained by extending the analysis performed in Todisco et al. (2012b) to the current 63 erosive events. Only the results of the power models are shown in Fig. 5, and compared with the USLE, since both in this study and in Todisco et al. (2012b) power models have been proven to be better than the

- and in Todisco et al. (2012b) power models have been proven to be better than the linear ones. The accuracy in the estimation of the soil loss by the USLE-MM model that includes predicted runoff coefficient in the event rainfall–runoff factor is quantified in a RMSE = 2.96 Mg ha⁻¹, higher than that obtained with $(\theta_{est} \cdot R_e)^{\alpha}$ and slightly lower than that derived with $(\theta_{sat} \cdot R_e)^{\alpha}$ (Fig. 5). The worst performance is that of the USLE
- ²⁰ model with an RMSE = 3.28 Mg ha⁻¹, while the lowest coefficient of determination is obtained for the USLE-MM with estimated runoff ($R^2 = 0.185$). It is interesting to notice that the accuracy in estimating the event soil loss of the models with erosivity factor that includes the simulated runoff coefficient, i.e. $(Q_{r, est} \cdot R_e)^{\alpha}$, is overcome by at least one model that uses the antecedent soil moisture θ in the erosivity index. In Fig. 5b,
- ²⁵ the deviations between observed and predicted soil loss values are also given with the corresponding runoff coefficient and the mean soil moisture (average of θ_{est} and θ_{sat}) values. On the one hand, it is evident that the introduction of both the soil moisture and the predicted runoff coefficient data significantly reduces the overestimation





issues of the USLE model. The correction is effective also when USLE highly overestimates soil losses, e.g. in May 2009 and August 2013. On the other hand, when USLE underestimates the measured values, the use of soil moisture and predicted runoff coefficient slightly increases the deviations (June and September 2010; July 2011 and August 2012). In Fig. 5b is also given the Mean Absolute Error (MAE) that confirms the ranking of the best performing models and clearly shows that the soil moisture is an

effective alternative at the estimated runoff in the prediction of the event soil loss.

4.5 Model performance in wet and dry periods

in this study.

As stated earlier, the white dots in Figs. 3 and 4 represent the events that occurred during the dry period (from June to September). It is evident that for these events the estimated soil losses are distant from the regression line and the 1:1 line, thus reducing the value of R^2 and RMSE. Also in Fig. 5b the highest deviations between the observed and estimated values occur in the dry period events. This is likely due to the particular characteristics of summer rainfall events in central Europe (Todisco et al., 2012b; Todisco, 2014). Summer rainfall events are generally isolated and char-15 acterized by high intensity associated with low antecedent soil moisture but elevated soil losses. Therefore, even with a high $R_{\rm e}$, the erosivity factor $\theta \cdot R_{\rm e}$ is reduced since both θ_{sat} and θ_{est} assume typically low values. As a representative example, the event characterized by the highest soil loss ($A_{ue} = 19.14 \text{ Mg ha}^{-1}$, July 2012) is associated with the lowest pre-event soil moisture, both satellite-derived ($\theta_{sat} = 0.09 \text{ m}^3 \text{ m}^{-3}$) and 20 simulated ($\theta_{est} = 0.05 \,\mathrm{m^3 m^{-3}}$). This issue affects the $Q_r \cdot R_e$ erosivity factor too, if Q_r is derived from runoff simulated by standard rainfall-runoff models in which runoff is increasing with antecedent soil moisture conditions (Todisco et al., 2012b). In the dry period, high surface runoff is observed, despite low values of θ , due to the development of superficial crusts creating a shield that is responsible for low infiltration and high runoff. This aspect is particularly significant for bare soil as in the plots considered





Given the above consideration, another analysis was performed excluding the dry period's events from the database. Among the 45 remaining events, 23 are used to calibrate the models and 22 to validate the results. In this case, as expected, the performances of all the analyzed equations generally increase (Table 2). In particular, for the calibration subset, $R^2 = 0.174$ and $R^2 = 0.496$ are obtained, for the erosivity factor $(\theta_{sat} \cdot R_e)^{\alpha}$ for $\alpha = 1$ and $\alpha > 1$, respectively. The $(\theta_{est} \cdot R_e)^{\alpha}$ factor gives $R^2 = 0.567$ and $R^2 = 0.715$ for $\alpha = 1$ and $\alpha > 1$, respectively. Therefore, particularly when modelled data are used, the performance of the regression significantly increases in terms of R^2 . In validation, RMSE = $1.10 \text{ Mg} \text{ ha}^{-1}$ (1.15 Mg ha⁻¹) is obtained with satellite soil moisture with the linear (power) model; by using modelled soil moisture, the linear 10 model gives RMSE = 1.63 Mg ha^{-1} while the power model gives RMSE = 1.26 Mg ha^{-1} (see Table 2). For comparison, the USLE/RUSLE model provides a RMSE = 1.99 Mg ha⁻¹; thus the modified-USLE models incorporating soil moisture data improved the performance of 45% (37%) when satellite (modelled) data were considered. 15

5 Conclusions

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The attempt made in the paper is to use the pre-event soil moisture to account for the spatial variation in runoff within the area for which the soil loss estimates are required. More specifically the analysis was focused on the evaluation of the effectiveness of the Soil Moisture for Erosion model (SM4E), derived coupling modelled or satellite-derived soil moisture with the USLE model, in predicting event unit soil loss at the plot scale in a silty–clay–loam soil in Central Italy. To this end the database of the Masse experimental station, for the measurement of event soil losses at plot scale, was used. The analyzed formulations are the USLE-derived equations, named SM4E models,

²⁵ in which the event erosivity factor, R_e , is corrected by the antecedent soil moisture, θ , and powered to an exponent $\alpha \ge 1$ ($\alpha = 1$: linear model; $\alpha > 1$: power model). Both satellite measurements from the ASCAT sensor ($\theta = \theta_{sat}$) and modelled values through

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the SWBM ($\theta = \theta_{est}$) were tested. The results showed that including direct consideration of antecedent soil moisture in the event rainfall-runoff erosivity factor of the RUSLE/USLE enhanced the capacity of the model to account for variations in event soil losses.

- The accuracy of the original USLE/RUSLE model was lower than that obtained by incorporating satellite and modelled soil moisture data. The more accurate model is that with the modelled soil moisture data when all the database is used and with the satellite retrieved soil moisture data when only the wet periods events are considered. In fact, it was also verified that much of the inaccuracy of the tested models is due
- to summer rainfall events, probably because of the particular characteristics that the soil assumes in the dry period (superficial crusts causing higher runoff): in this cases, high soil losses are observed in association to low values of soil moisture, and, hence, the model performance decreases. By excluding the summer events, as expected, the performance of all the analysed equations increases. This aspect is particularly impor-
- tant as it highlights the conditions in which the developed models fail to reproduce soil losses and that deserves further investigation. Specifically, the incorporation of mechanism for the formation of superficial crusts in the developed soil water balance model will be the object of future investigations.

We highlight that the obtained results open interesting scenarios in the overview of the studies aimed to define USLE-derived models that could improve the unit soil loss estimation at the event scale. In particular, the choice of using soil moisture data to correct the rainfall–runoff erosivity factor acquires a great importance for the practice. Indeed, soil moisture is a relatively simple measure and different techniques are available for providing accurate measurements at the field scale. Moreover, remote sensing

soil moisture data are also widely available on a global scale. Through satellite data, there is the potential of applying the developed USLE-derived model for large-scale monitoring and quantification of the soil erosion process.

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| Plot size | S | $L \cdot S$ | $N_{\rm e}$ | h | l _e | / | R _e | N _m | | 2 _{e, i} | | 4 _{e,i} |
|-----------|----|-------------|-------------|------|----------------|------|----------------|----------------|-----|--------------------------|-----|------------------|
| | | | | μ | CV | μ | CV | | μ | CV | μ | CV |
| 22 × 8 | 16 | 2.04 | 62 | 35.4 | 65.2 | 81.8 | 102.6 | 113 | 3.6 | 136.6 | 4.1 | 221.5 |
| 22 × 4 | 16 | 2.04 | 53 | 33.2 | 66.6 | 75.1 | 110.0 | 98 | 2.4 | 145.7 | 2.8 | 260.7 |

Table 1. Summary statistics of the 22 m long plot data available at the Masse site.

s, slope steepness (%); $L \cdot S$, USLE topographic factors; N_e , number of events per plot scheme; h_e , event rainfall depth (mm); R_e , event rainfall erosivity factor (MJ mm ha⁻¹ h⁻¹); N_m , number of measures per plot scheme; $Q_{e,i}$, plot event runoff volume (mm); $A_{e,i}$, plot event soil loss (Mg ha⁻¹); μ , mean; CV, coefficient of variation (%).





| Table 2. Calibration parameters and validation Root Mean Square Error for the SM4E models | |
|---|--|
| (Eq. 4). | |

| Erosivity factor | All the ev | vents | | Wet period | events | |
|---|----------------------------|-------------------------|------|----------------------------|-------------------------|------|
| | RMSE (Mgha ⁻¹) | $K_{\mathrm{u},\theta}$ | α | RMSE (Mgha ⁻¹) | $K_{\mathrm{u},\theta}$ | α |
| $\theta_{\rm sat} \cdot R_{\rm e}$ | 3.07 | 0.178 | _ | 1.10 | 0.174 | _ |
| $(\theta_{\rm sat} \cdot R_{\rm e})^{\alpha}$ | 3.04 | 0.007 | 1.70 | 1.15 | 0.042 | 1.14 |
| $\theta_{\rm est} \cdot R_{\rm e}$ | 2.85 | 0.180 | _ | 1.63 | 0.270 | - |
| $(\theta_{\rm est} \cdot R_{\rm e})^{lpha}$ | 2.80 | 0.006 | 1.78 | 1.26 | 0.043 | 1.29 |

RMSE: Root Mean Square Error; K_u : scale factor; α : exponent for the erosivity factor.







Figure 1. View of the Masse experimental station for monitoring water soil loss at plot scale in Umbria region (Central Italy).

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Figure 2. Satellite-derived and estimated (through the SWBM) soil moisture at the beginning of 63 erosive events in the study period 2008–2013: time series (a) and scatterplot (b).







Figure 3. Regression models between measured soil loss A_{ue} and the erosivity index $\theta \cdot R_e$ of the calibration subset: linear SM4E model and satellite soil moisture (a); power SM4E model and satellite soil moisture (b); linear SM4E model and simulated soil moisture (c); power SM4E model and simulated soil moisture (d).









Figure 4. Testing of the A_{ue} vs. $\theta \cdot R_e$ models with the validation subset: linear SM4E model and satellite soil moisture (**a**); power SM4E model and satellite soil moisture (**b**); linear SM4E model and modelled soil moisture (**c**); power SM4E model and modelled soil moisture (**d**).





Figure 5. Comparison of the results obtained by the power SM4E model with both satellite and estimated soil moisture, the ULSE-MM including predicted runoff, and the original USLE, in terms of: (a) root mean square error (RMSE) and coefficient of determination (R^2), and (b) deviations between estimated, $A_{ue, est}$, and observed, A_{ue} , soil losses. In (b) the values of the estimated runoff and of the mean soil moisture computed as the mean between the estimated and the satellite retrieved values are also given.



