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Precipitation Ensembles conforming to Natural Variations derived from Regional Climate Model using a New Bias Correction Scheme

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20 **Abstract**

21 This study presents a novel bias correction scheme for Regional Climate Model (RCM) precipitation
22 ensembles. A primary advantage of using model ensembles for climate change impact studies is that the
23 uncertainties associated with the systematic error can be quantified through the ensemble spread. Currently,
24 however, most of the conventional bias correction methods adjust all the ensemble members to one reference
25 observation. As a result, the ensemble spread is degraded during bias correction. Since the observation is only
26 one case of many possible realisations due to the climate natural variability, a successful bias correction
27 scheme should preserve the ensemble spread within the bounds of its natural variability (i.e. sampling
28 uncertainty). To demonstrate the proposed methodology, an application to the Thorverton catchment in the
29 southwest of England is presented. For the ensemble, 11-members from the Hadley Centre Regional Climate
30 Model (HadRM3-PPE) Data are used and monthly bias correction has been done for the baseline time period
31 from 1961 to 1990. In the typical conventional method, monthly mean precipitation of each of the ensemble
32 members is nearly identical to the observation, i.e. the ensemble spread is removed. In contrast, the proposed
33 method corrects the bias while maintain the ensemble spread within the natural variability of the observations.

34

35 Keywords: bias correction, RCM ensemble, spread, natural variability

36 **1. Introduction**

37 The growing evidence of global climate change is clear in the past century (Stocker, 2013). Therefore, future
38 projections of climate that incorporate the effects of an underlying changing climate are of great importance,
39 particularly because of reliance of mitigation and adaptation on realistic projections. Interest in the impacts of
40 climate change is increasing from water resources managers in the context of the hydrological cycle and water
41 resources (Bates et al., 2008; Compagnucci et al., 2001). Global Climate Models (GCMs) are usually used for
42 the projection of future climate and the accuracy of GCMs has been enhanced in simulating large scale global
43 climate. Nevertheless, GCMs have difficulties in providing reliable climate data at local scales due to their
44 coarse resolutions (100-250km) (Maraun et al., 2010). Therefore, for regional impact studies Regional
45 Climate Models (RCMs) have been widely used which are compatible to the catchment scales (25-50km).

46 Although RCMs produce more reliable information than GCMs at a regional scale, hydrological variables
47 from RCMs still cannot be used directly in hydrological models because of the systematic errors (i.e., biases)
48 (Chen et al., 2011b; Feddersen and Andersen, 2005). Therefore, for hydrological impact studies, post
49 processing of the model outputs is normally needed to reduce biases (Chen et al., 2013). Research has shown
50 that systematic model errors of RCMs are due to imperfect parameterisation, spatial discretisation and spatial
51 averaging within grids (Ehret et al., 2012; Teutschbein and Seibert, 2012). Typical errors are over- or
52 underestimation of climate variables and seasonal dependency (Kotlarski et al., 2005; Maraun et al., 2010),
53 and there are relatively too many low intensity wet days compared with the observations (Ehret et al., 2012;
54 Ines and Hansen, 2006).

55 Numerous studies have been done to develop and evaluate the bias correction methods (Chen et al., 2011a;
56 Chen et al., 2011b; Johnson and Sharma, 2011; Piani et al., 2010; Teutschbein and Seibert, 2012). Evaluation
57 of different bias correction methods has been done by Teutschbein and Seibert (2012): 1) linear scaling
58 (Lenderink et al., 2007), 2) local intensity scaling (Schmidli et al., 2006), 3) power transformation (Leander
59 and Buishand, 2007; Leander et al., 2008) and 4) distribution mapping method (Block et al., 2009; Déqué et
60 al., 2007; Johnson and Sharma, 2011; Piani et al., 2010; Sun et al., 2011). The linear scaling method adjusts
61 the mean value of the model to that of the observation by applying a correction factor which is the ratio
62 between the long-term observation and model data. However, the local intensity scaling method considers
63 wet-day frequency and wet-day intensity as well as the bias in the mean. The power transformation method

64 corrects the mean and variance of the data. The distribution mapping method fits the distribution function of
65 the climate model data to that of the observation. The results have shown that the distribution mapping
66 method is the best, although all the four bias correction methods could improve the raw RCM precipitation.
67 Although the bias correction is commonly applied in climate change studies, correcting the model output
68 towards the corresponding observation is still a controversial issue and applying bias correction could make
69 the uncertainty range of the simulations narrower, i.e. “hides rather than reduces uncertainty” (Ehret et al.,
70 2012).

71 In this study we address the issue which most conventional bias correction methods implicitly neglect: the
72 uncertainty associated with the observation sampling uncertainty. We note that adjusting the statistical
73 properties of each of the ensemble members to one observation does not preserve the spread across the
74 ensemble members, thus negating the advantage of quantifying uncertainty through the use of ensemble
75 spread in climate change impact studies. In general, uncertainties in climate change projections can be
76 grouped by three main sources: boundary condition, model structure and natural variability (Hawkins and
77 Sutton, 2009). To account for these sources of uncertainties, ensemble modelling is a generally accepted way
78 by producing a number of simulations using multiple scenarios, different models (structures and parameters)
79 and initial conditions (Collins et al., 2006; Good and Lowe, 2006; Meehl et al., 2005; Murphy et al., 2004;
80 Palmer and Räisänen, 2002; Stainforth et al., 2005; Tebaldi et al., 2006; Webb et al., 2006; Weisheimer and
81 Palmer, 2005) which are possible due to increase in data availability through high-performance computing
82 systems. There are two approaches for ensemble schemes in the context of model uncertainty. The first is
83 multi-model ensembles (MMEs) method to address the structural uncertainty associated with the
84 understanding and parameterisation of the GCMs. The second is the perturbed-physics ensembles (PPEs)
85 method which is complementary to the MME approach, and is applied in the Intergovernmental Panel on
86 Climate Change (IPCC) assessments (Meehl et al., 2007; Solomon, 2007; Taylor et al., 2012). However, when
87 bias correction is applied to the ensemble of the GCM/RCM scenario simulation, the advantage of the
88 ensemble in representing the uncertainty is often negated. The statistical properties of all the ensemble
89 members are usually matched to that of the observations so that the advantage of the ensemble with respect to
90 a single model simulation is lost. Therefore, the natural variability of the observation should be estimated first,
91 and then the spread (i.e. variance) of the ensemble should be adjusted to not only one observation but to range

92 of the possible observations, through incorporating sampling uncertainty. In this study we propose a new bias
93 correction scheme which conforms to the ensemble spread. In other words, in this scheme the ensemble
94 spread is preserved to a certain degree, after bias correction, which corresponds to the observation sampling
95 uncertainty.

96 Another issue presented in this study is associated with how to correct the PPEs' bias to preserve the spread.
97 Should the bias correction be applied individually for each ensemble member or applied as an ensemble? The
98 former method is to apply different transfer functions for different ensemble members, while the latter method
99 is to apply only one transfer function for the whole ensemble members. In stochastic hydrology, the synthetic
100 rainfall and streamflow should have statistical properties (e.g. mean, variance, skewness, etc) similar to the
101 real system so that they are not distinguishable between the observed data and the modelled data. In this study
102 we have followed the same philosophy. The bias corrected rainfall ensembles should have statistical
103 properties (in this study, the mean value and the spread of ensembles) similar to the observations. The same
104 principle has been applied to the UKCP09 Weather Generator (Jones et al., 2009) (WG) used in the UK. The
105 synthetic weather variables from WG have statistical properties similar to the observations since the WG is
106 calibrated on the observations.

107 There are many aspects (e.g. mean, variance, skewness, autocorrelation etc) of the rainfall series which cannot
108 be all corrected simultaneously. The way of correcting the RCM data should therefore depend on what
109 properties are relevant to the data usage. In this study we have focused on the mean value and the spread of
110 bias-corrected RCM precipitation.

111 The paper is structured as follows: Section 2 describes the study catchment and data; in Section 3 the
112 conventional bias correction method is presented. Next we show how the observation sampling uncertainty
113 (i.e. natural variability) is estimated and how the ensemble is evaluated. Finally the concepts of conventional
114 and proposed bias correction methods are compared. In Section 4 we show the results followed by discussion
115 and conclusions in Section 5 and Section 6.

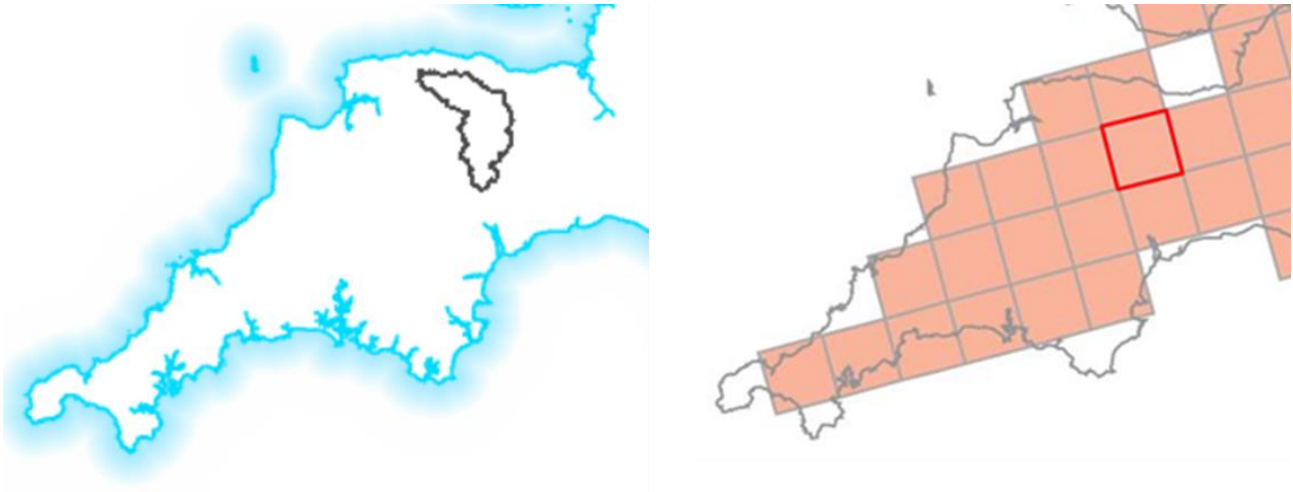
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117 **2. Catchment and data**

118 The Thorverton catchment is used as the case study site. It has an area of 606km², and is a sub-catchment of
119 the Exe catchment. The Exe catchment is located in the southwest of England with an area of 1,530 km² and

120 an average annual rainfall of 1,088 mm. Figure 1 shows the overview of the Exe catchment area. Daily time
121 series of the observed precipitation data (1961-1990) over the Thorverton catchment is obtained from the UK
122 Met Office.

123



124

125 Figure 1. Location of the Thorverton catchment (the left panel) and HadRM3 25km grid boxes (the right
126 panel). The highlighted grid box in red is selected to cover the Thorverton catchment.

127

128 The climate data used in this study is the Hadley Centre Regional Climate Model (HadRM3-PPE) Data which
129 was generated by the Met Office Hadley Centre. This dataset is used to dynamically downscale regional
130 projections of the future climate from the GCM, HadCM3 (Murphy et al., 2009). It is comprised of 11
131 members (one unperturbed and 10 perturbed members). For the perturbation, 31 parameters are chosen from
132 the unperturbed member representing radiation, land surface, boundary layer, sea-ice, cloud, atmospheric
133 dynamics and convection (Collins et al., 2011). The dataset provides the time series of climate data in the
134 period 1950-2100 for the historical and future medium emission scenario A1B. The temporal and spatial
135 resolutions of the HadRM3 climate data are daily and 25km respectively. As presented in Figure 1, the RCM
136 grid boxes are rotated by 0.22° . Here, the daily precipitation series from all 11 members are used to evaluate
137 the ensemble and to test the proposed new bias correction scheme for the baseline period of 1961 to 1990. The
138 grid is chosen to cover the study catchment.

139

140 3. Methodology

141 3.1 Conventional bias correction method

142 Bias correction has been initially proposed for calibrating the seasonal GCM variables (e.g. precipitation and
 143 temperature) and later extended to the daily time scale. Individual months are usually processed independently
 144 from each other, in order to correct seasonal phase errors, after modifying the wet-day frequency of the
 145 climate model precipitation on the wet-day observed frequency by applying a cut-off threshold. Compared
 146 with the observations, the climate model precipitations usually have more wet days at low precipitation. In
 147 this study the two-parameter Gamma distribution is used to fit the observed precipitation:

$$148 \quad f(x) = \frac{1}{\beta^\alpha \Gamma(\alpha)} x^{\alpha-1} e^{-x/\beta}; \quad x \geq 0; \quad \alpha, \beta > 0 \quad (1)$$

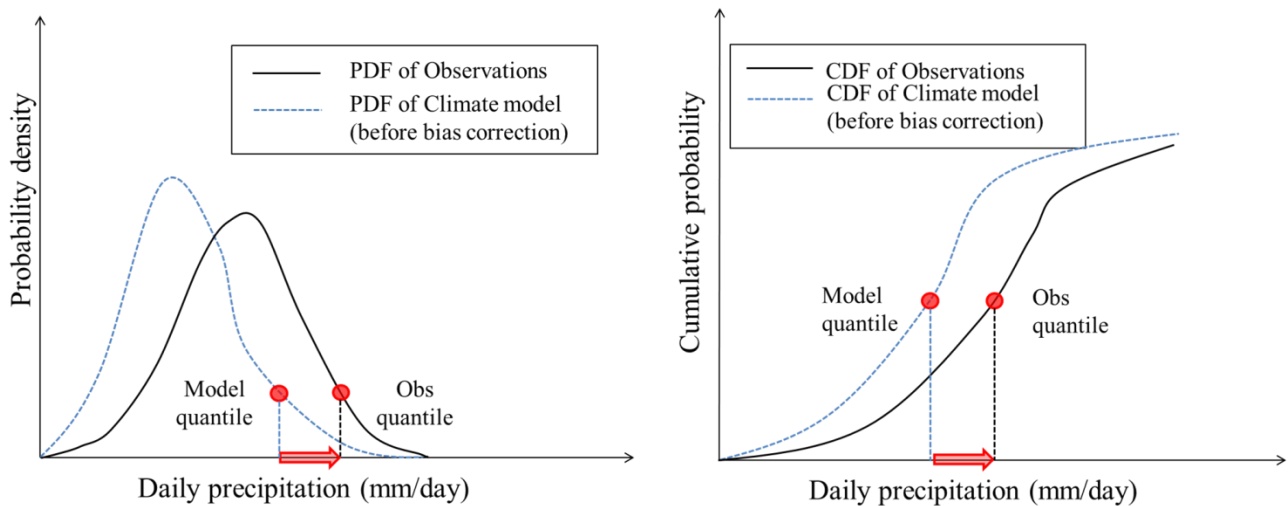
149 where, Γ is the gamma function, α and β are the shape and scale parameters respectively.

150 For the bias correction of the daily RCM precipitation, the quantile mapping method based on the Gamma
 151 distribution which is also referred to as ‘probability mapping’ and ‘distribution mapping’ in the literature is
 152 applied. A schematic representation of the quantile mapping method adopted in this study is shown in Figure
 153 2 and a general process is described as follows. First, before doing the bias correction, the wet-day frequencies
 154 of the observed precipitation and the RCM precipitation are matched by removing the RCM low precipitation.
 155 Second, Gamma distribution functions are fitted to individual months for both the observed and RCM daily
 156 precipitations for the baseline period. The cumulative probability of the RCM is calculated from the fitted
 157 Gamma distribution of the RCM-simulated precipitation. Third, the precipitation value corresponding to the
 158 cumulative probability is found in the fitted Gamma distribution of the observation. This value is the bias
 159 corrected RCM precipitation as described by Eq(2):

$$160 \quad X_{cor} = F^{-1} [F(X_{model}; \alpha_{model} \beta_{model}); \alpha_{obs} \beta_{obs}] \quad (2)$$

161 where, X_{cor} is the bias corrected RCM precipitation, F is Gamma cumulative distribution function (CDF), F^{-1}
 162 is the inverse function of F , α is the shape parameter and β is the scale parameter. The subscripts *model* and
 163 *obs* indicate the parameters from the RCM and observed precipitation.

164



165
 166 Figure 2. A schematic representation of the quantile mapping method for bias correction.
 167

168 In this study, monthly bias correction for precipitation is carried out for all months. December, which is a wet
 169 period in the study catchment, is used to illustrate the new bias correction method in more detail.

170

171 3.2 Natural variability of observation

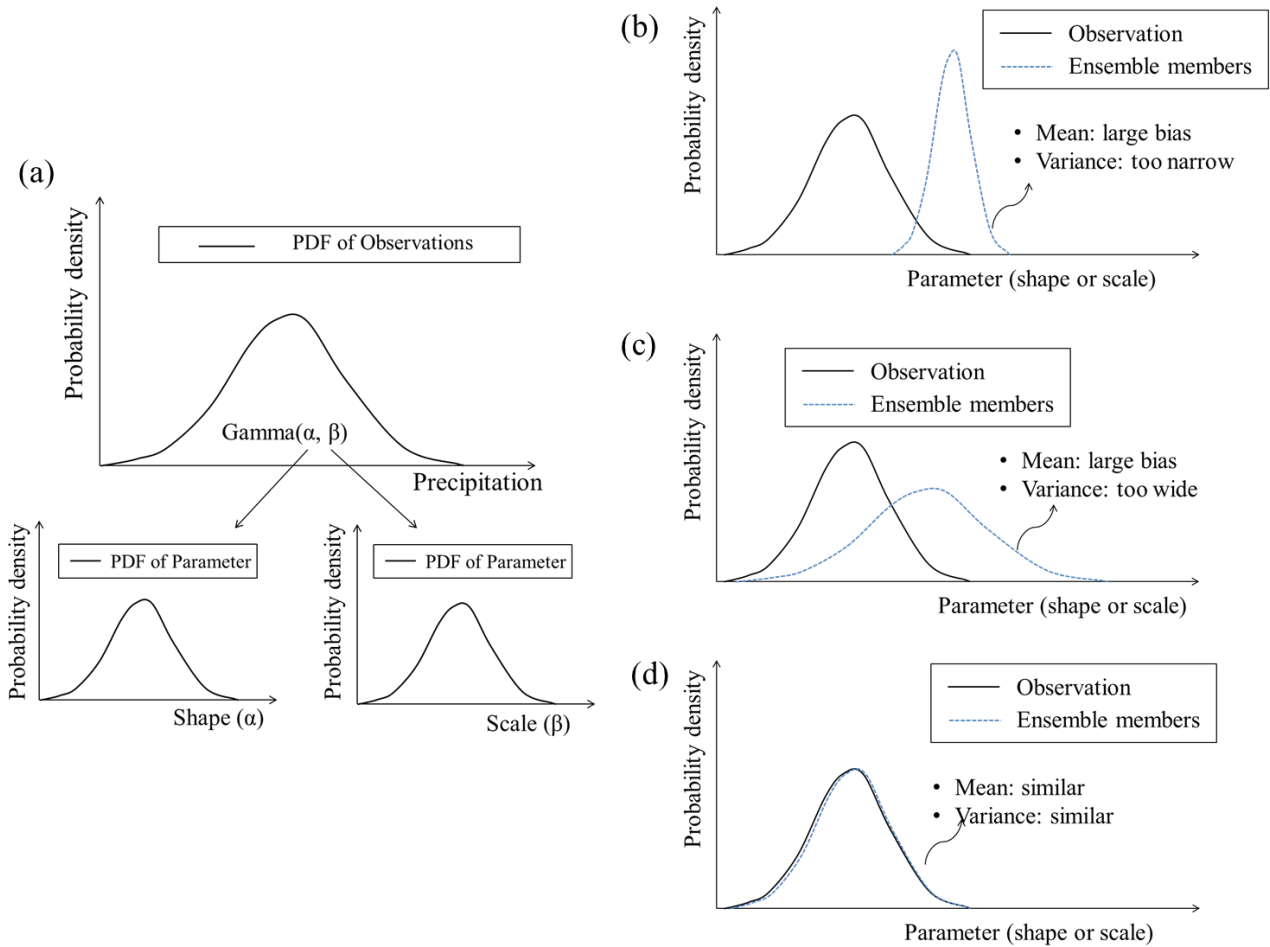
172 The problem with the conventional bias correction methods is that all the ensemble members are adjusted to
 173 one observation as a reference value. As a result, the spread of the ensemble which represents the uncertainty
 174 is removed after bias correction. However, due to the observational sampling uncertainty in terms of climate
 175 variability, the observation is only one case of many possible realisations. Climate natural variability is a
 176 natural fluctuation that occurs without external forcing to the climate system. To estimate the natural
 177 variability of the observed precipitation, the parameters of the Gamma distribution for December daily
 178 precipitation from 1961 to 1990 are assumed to be the true parameters. We use 100,000 sets of 30-year daily
 179 precipitation random samples from the true parameters. For each sample (i.e. 30-year daily rainfall simulation),
 180 we estimate a set of new Gamma parameters (i.e. shape and scale parameter). The re-estimated parameters are
 181 different to those used in the simulations due to the observation sampling uncertainty. In this study, the
 182 distribution of 100,000 sets of parameters is assumed to represent the natural variability of 30-year daily
 183 precipitation.

184 **There has been relevant work recently around the influence of natural variability on bias characterisation in**
 185 **RCM simulations (Addor and Fischer, 2015). They show that different methods of estimating natural**

186 variability give different measures, depending on the method, season, and temporal scale of the observation
187 record which in return influence the bias correction. Overall, they argue that observational uncertainties and
188 natural variability need to be considered for bias correction of RCM simulations. In order to find the
189 optimised number of resampling, the sensitivity analysis between the numbers of resampling and the mean
190 value of the observed precipitation has been done. The result has shown that beyond 20,000 resamples, the
191 mean value becomes stable. Since the running time does not take long in this study we have resampled
192 100,000 times which are sufficient.

193 **3.3 Evaluation of ensemble members**

195 The ensemble members must first be evaluated to assess whether bias correction is necessary. The idea of
196 evaluating the ensemble members is illustrated in Figure 3. The observed daily precipitation is assumed to
197 follow the Gamma distribution defined by the shape and scale parameters. The distribution of the parameters
198 can be derived from the resampling procedure as mentioned in Section 3.2 (Figure 3(a)). Then we compare the
199 distributions of the observation and ensemble members' parameters (Figure 3(b) ~ (c)). If the parameter
200 distribution of an ensemble member looks like Figure 3(b), the member has bias in mean and variance (in the
201 form of a shifted and narrow parameter distribution). If the parameter distribution were biased in the mean and
202 had a wide variance, it resembles something closer to Figure 3(c). Both of these "cases" indicate the need for
203 bias correction. On the other hand, if the parameter distribution of an ensemble member resembles Figure 3(d)
204 (i.e. similar mean and variance of the ensemble member and empirical estimate) then bias correction is not
205 necessary. The basic idea of the proposed bias correction is to match the shapes of parameter distribution
206 between the observation and ensemble members so that they are similar after bias correction rather than
207 matching point estimates of the parameters.



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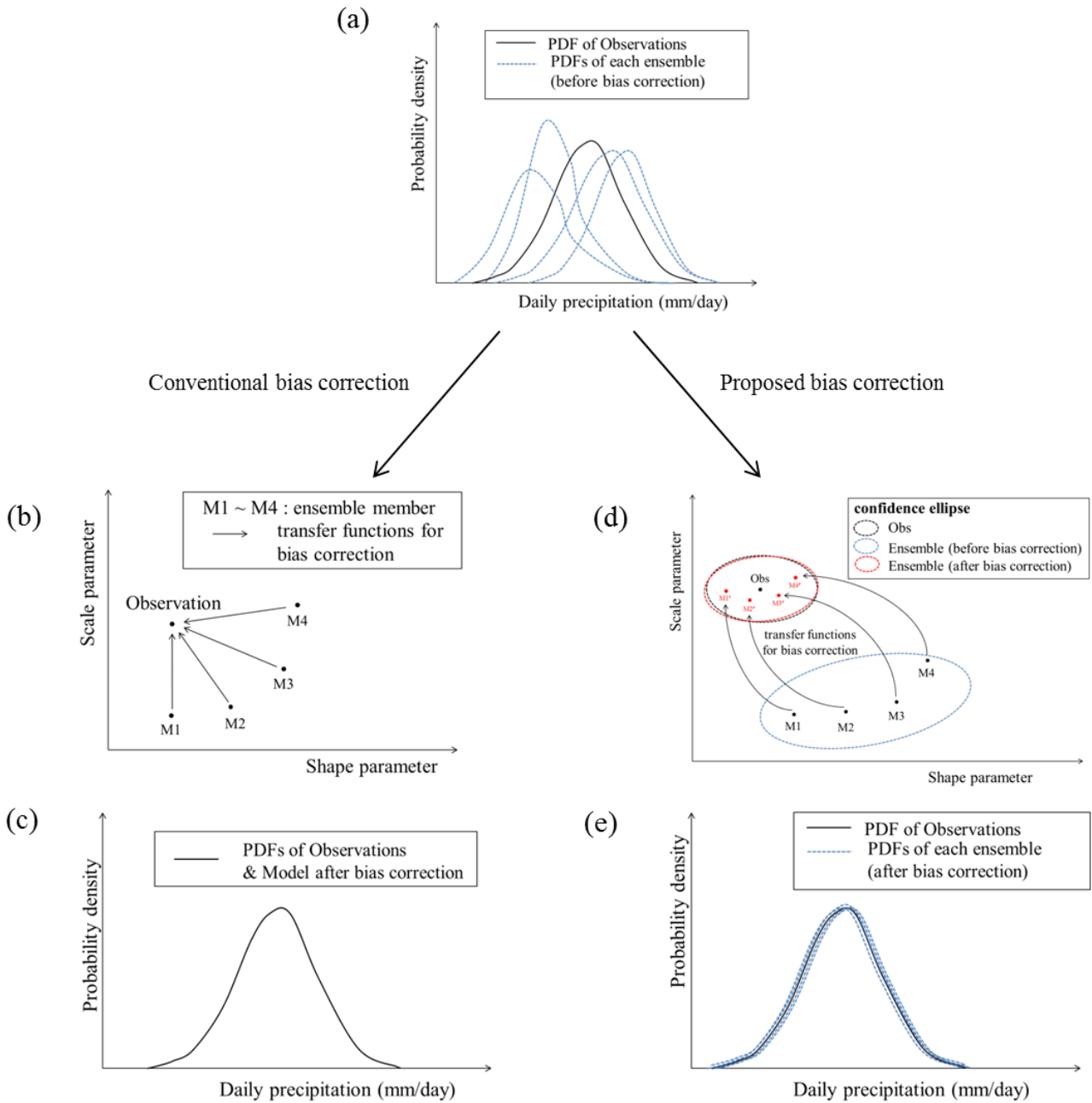
209 Figure 3. A schematic representation of the evaluation of ensemble members.

210

211 **3.4 Comparison between the conventional and proposed bias correction schemes**

212 A schematic representation of the conventional bias correction and the proposed bias correction methods are
 213 presented in Figure 4. As mentioned in Section 3.1, the objective of the quantile mapping method is to match
 214 the statistical properties between the observed and climate model precipitation. Figure 4(a) shows the PDFs of
 215 the observation and each ensemble member. In the conventional method, transfer functions are built by
 216 matching the shape and scale parameters of each ensemble member to those of the observation (Figure 4(b)).
 217 Therefore, the PDFs (or CDFs) of the observation and each ensemble member become identical after bias
 218 correction (Figure 4(c)). However, the problem of this approach is that if every ensemble member is matched
 219 to the observation through bias correction, there is no point of using the ensemble scenarios since the spread
 220 of the ensemble is removed. Hence, we propose a new scheme for bias correction. The idea is to maintain the
 221 variation of the ensemble after bias correction so that they match the variation of the population as if each

222 member is randomly (i.e., equally likely) taken from the population. The population here is assumed to be the
 223 natural variability of the observation. Figure 4(d) illustrates the concept of the new bias correction method.
 224 Each member is corrected by different transfer functions but the parameters' space for the transfer functions is
 225 limited to the natural variability of the observation. As a result, the biases of 11 members are reasonably well
 226 corrected without eliminating the spread of the ensemble (Figure 4(e)).
 227



228
 229 Figure 4. A schematic representation of the conventional bias correction method and the proposed bias
 230 correction method
 231

232 A step by step summary of the proposed procedure is presented as follows and in Figure 5.

233 • (Step 1) Natural variability of the observation is estimated by first randomly resampling precipitation
234 from a Gamma distribution with parameters obtained by fitting the observed precipitation. Next, the
235 parameters of each resampled precipitation time series are estimated, and the bivariate distribution of
236 these parameters over all the samples is established. The shaded area in Figure 5 represents the natural
237 variability of the observation. If the parameters of the ensemble members are in the shaded area, there
238 is no need to do bias correction.

239 • (Step 2) Normalise the parameters of the ensemble members using Eq(3).

$$240 \quad x_N = \frac{x - \mu_x}{\sigma_x}, \quad y_N = \frac{y - \mu_y}{\sigma_y} \quad (3)$$

241 where, x and y are the shape and scale parameters of the distribution of each ensemble member, μ_x , μ_y
242 are the mean values and σ_x , σ_y are the standard deviations of the parameters of all ensemble members,
243 x_N , y_N are the normalised shape and scale parameters.

244 • (Step 3) De-normalise the parameters of the ensemble members by matching the mean and standard
245 deviation to those of the observation as shown in Eq(4).

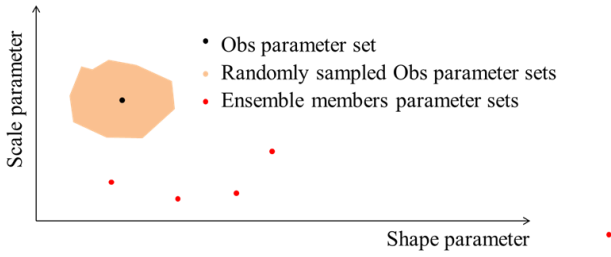
$$246 \quad x' = x_N \cdot \sigma_{x0} + \mu_{x0}, \quad y' = y_N \cdot \sigma_{y0} + \mu_{y0} \quad (4)$$

247 where, μ_{x0} , μ_{y0} are the mean values and σ_{x0} , σ_{y0} are the standard deviations of the parameters of the
248 observation, x' , y' are the de-normalized shape and scale parameters.

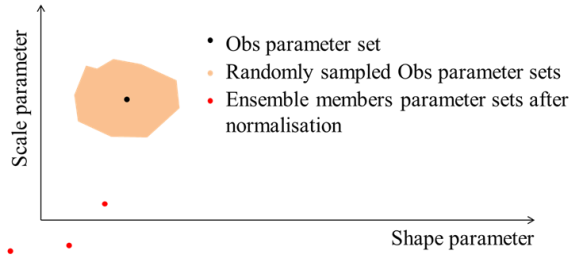
249 (Step 4) In Step 3, the coordinate of the centre of the denormalised ensemble parameter sets is (0, 0).
250 This coordinate is shifted to that of the observation (i.e. black dot in Figure 5 Step 4), which results in
251 the ensemble members' parameter sets to fall into the boundary of the natural variation of the
252 observations. From this, transfer functions for the bias correction can be built.

253

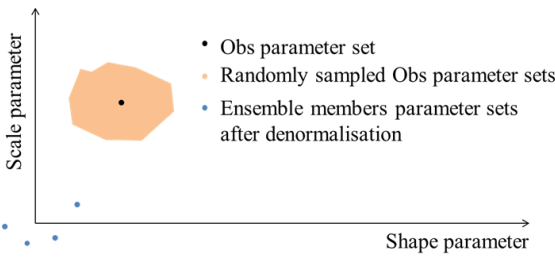
Step 1. Estimate natural variation of observations: randomly sample rainfall from observation parameters, then estimate parameter sets



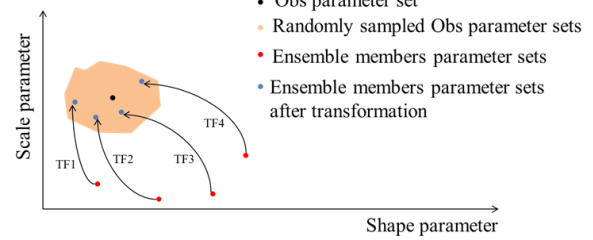
Step 2. Normalise ensemble members



Step 3. Denormalise the ensemble members by matching the mean and standard deviation of the ensemble to that of the observations



Step 4. Move the centre of denormalised ensemble parameter sets to Observation parameter set, then build the transfer functions (TF) for bias correction



254

255 Figure 5. The four step procedure of the proposed bias correction method.

256

257 3.5 Hydrological application

258 To investigate the impact of different bias correction schemes on flow, we have used a conceptual rainfall-
 259 runoff model called IHACRES (Jakeman and Hornberger, 1993). This model has been widely applied to a
 260 variety of catchments for hydrological analysis and climate impact studies (Jakeman et al., 1993; Kim and Lee,
 261 2014; Letcher et al., 2001; Littlewood, 1999). The model is composed of a non-linear module and a linear
 262 module as shown in Figure 6 and the model parameters are listed in Table 1. A non-linear module converts
 263 total rainfall to effective rainfall which is calculated from Eq(5).

$$264 \quad U_k = [C(\phi_k - l)]^p r_k \quad (5)$$

265 where, r_k is the observed rainfall, C is the mass balance, l is the soil moisture index threshold and p is the
 266 power on soil moisture respectively. The soil moisture (ϕ_k) is calculated from:

$$267 \quad \phi_k = r_k + \left(1 - \frac{1}{\tau_k}\right)\phi_{k-1} \quad (6)$$

268 where, τ_k is the drying rate given by:

$$269 \quad \tau_k = \tau_w \exp[0.062f(t_r - t_k)] \quad (7)$$

270 where, τ_w is the drying rate at the reference temperature, f is the temperature modulation, t_r is the reference
 271 temperature, and t_k is the observed temperature. A linear module assumes that there is a linear relationship

272 between the effective rainfall and flow. Two components in this module, quick flow and slow flow, can be
 273 connected in parallel or in series. In this study two parallel storages in the linear module are used because such
 274 a combination reflects the catchment conditions and the streamflow (x_k) at time step k is defined by the
 275 following equations:

$$276 \quad x_k = x_k^{(q)} + x_k^{(s)} \quad (8)$$

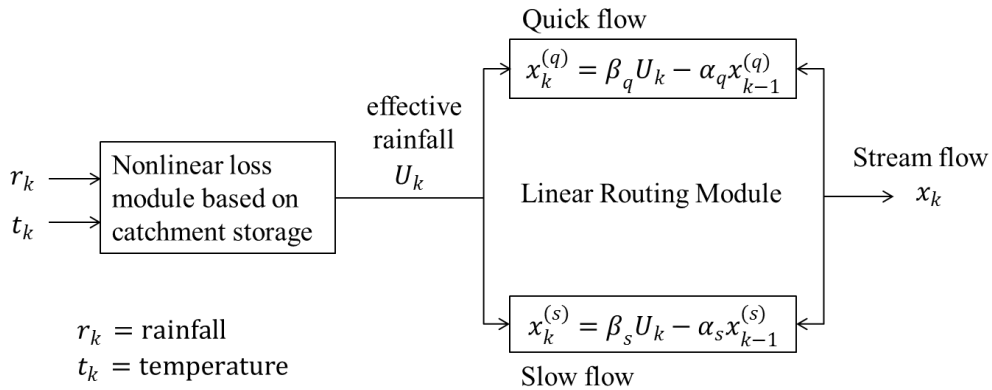
$$277 \quad x_k^{(q)} = \beta_q U_k - \alpha_q x_{k-1}^{(q)} \quad (9)$$

$$278 \quad x_k^{(s)} = \beta_s U_k - \alpha_s x_{k-1}^{(s)} \quad (10)$$

279 where, $x_k^{(q)}$ and $x_k^{(s)}$ are quick flow and slow flow respectively, and α and β are recession rate and peak
 280 response respectively. The relative volumes of quick flow and slow flow can be calculated from:

$$281 \quad V_q = 1 - V_s = \frac{\beta_q}{1 + \alpha_q} = 1 - \frac{\beta_s}{1 + \alpha_s} \quad (11)$$

282



283

284 **Figure 6. Structure of the IHACRES model.**

285

286 **Table 1. Parameters in the IHACRES model**

Module	Parameter	Description
	c	Mass balance
Non-linear	τ_w	Reference drying rate
	f	Temperature modulation of drying rate
Linear	α_q, α_s	Quick and slow flow recession rate
	β_q, β_s	Fractions of effective rainfall for peak response
	τ_s	Slow flow recession time constant, $\tau_s = -\Delta/\ln(-\alpha_s)$

287

288 The hydrological application has been done as follows. First, the model parameters have been optimised with
289 the use of the observed daily precipitation, temperature and flow data.

290 Second, the observed precipitation and the two different bias corrected precipitation data from the
291 conventional and proposed bias correction methods are randomly resampled to estimate the spread of the
292 simulated flow ensembles. Third, the optimised parameters and the precipitation time series are then used to
293 simulate daily flow ensembles. Finally, from this daily simulated flow data, thirty-year mean monthly flow
294 has been estimated since the bias correction has been done on monthly basis, and then compared under
295 different bias correction schemes.

296

297 4. Results

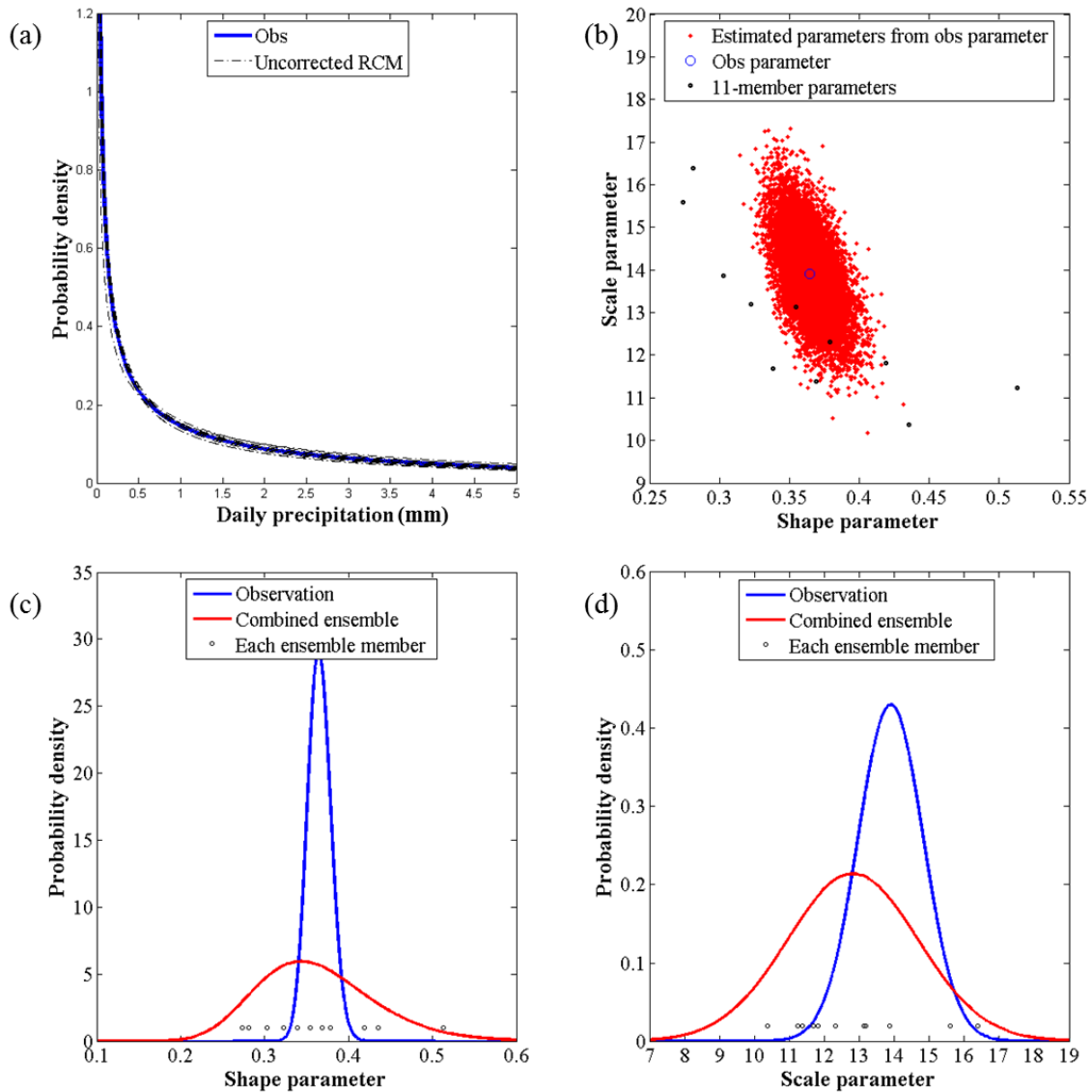
298 The first part of this section compares the parameter distribution of the observed precipitation and bias-
299 uncorrected precipitation. The next part shows the result of the conventional bias correction followed by the
300 proposed bias correction method. In each part, PDFs of precipitation, shape and scale parameter space and
301 PDFs of shape and scale parameters have been evaluated and compared. Finally, the monthly mean
302 precipitation for the time period from 1961 to 1990 is compared among the observation, uncorrected ensemble
303 members and corrected ensemble members by applying both the conventional and new methods.

304

305 4.1 Parameter distribution of the observed and RCM precipitation

306 Before correcting the bias of each member, we compare the statistical properties with the observed
307 precipitation. Figure 7(a) shows the PDFs of the observed and simulated precipitation. The parameter space
308 (i.e. shape vs scale parameter) of these distributions is plotted in Figure 7(b). Note again the parameter space
309 is defined by resampling from the observation, and the distribution of 100,000 sets of parameters is assumed
310 as the natural variability of daily precipitation as illustrated in section 3.2. The red dots represent the natural
311 variability of the observation which is estimated from the observed parameters. Most of the members'
312 parameters are outside the boundary of the natural variability. Figure 7(c) and (d) compare the distribution of
313 each parameter. The distribution of the parameter for the combined ensemble shows large biases of the mean

314 and variance. Since both the mean and variance of 11-members are quite different to those of the observation,
 315 it is apparent that bias correction is needed.
 316

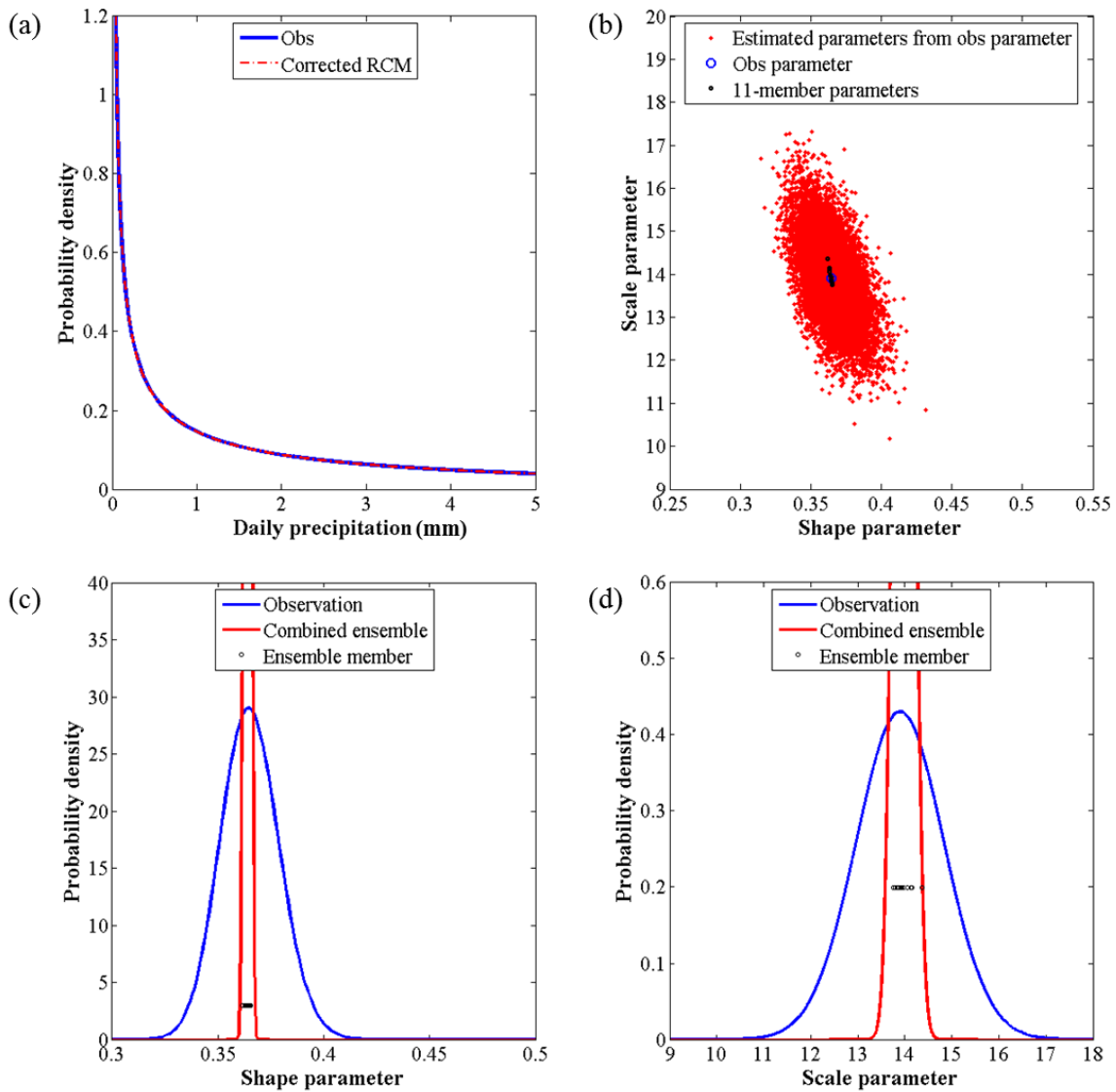


317
 318 Figure 7. Parameter distributions of the observation and 11-members: (a) Probability density function of the
 319 observed and 11-member precipitation time series before bias correction; (b) Scatter plot between shape and
 320 scale parameters of the observed and bias uncorrected precipitation; (c) - (d) Probability density functions of
 321 shape and scale parameters for the observed and bias uncorrected precipitation.
 322

323 4.2 Conventional bias correction

324 Figure 8 illustrates the result of the conventional bias correction method. As expected the PDFs of the
 325 observation and 11-member ensemble are nearly identical to one another (Figure 8(a)) and the parameters of

326 the corrected precipitation are all in the centre of the parameter space of the observation (Figure 8(b), (c) and
 327 (d)). As previously noted, the spread of the ensemble under this conventional approach is greatly reduced, and
 328 in turn, the overall characteristics of hydro-climate variables are nearly identical across different model runs.



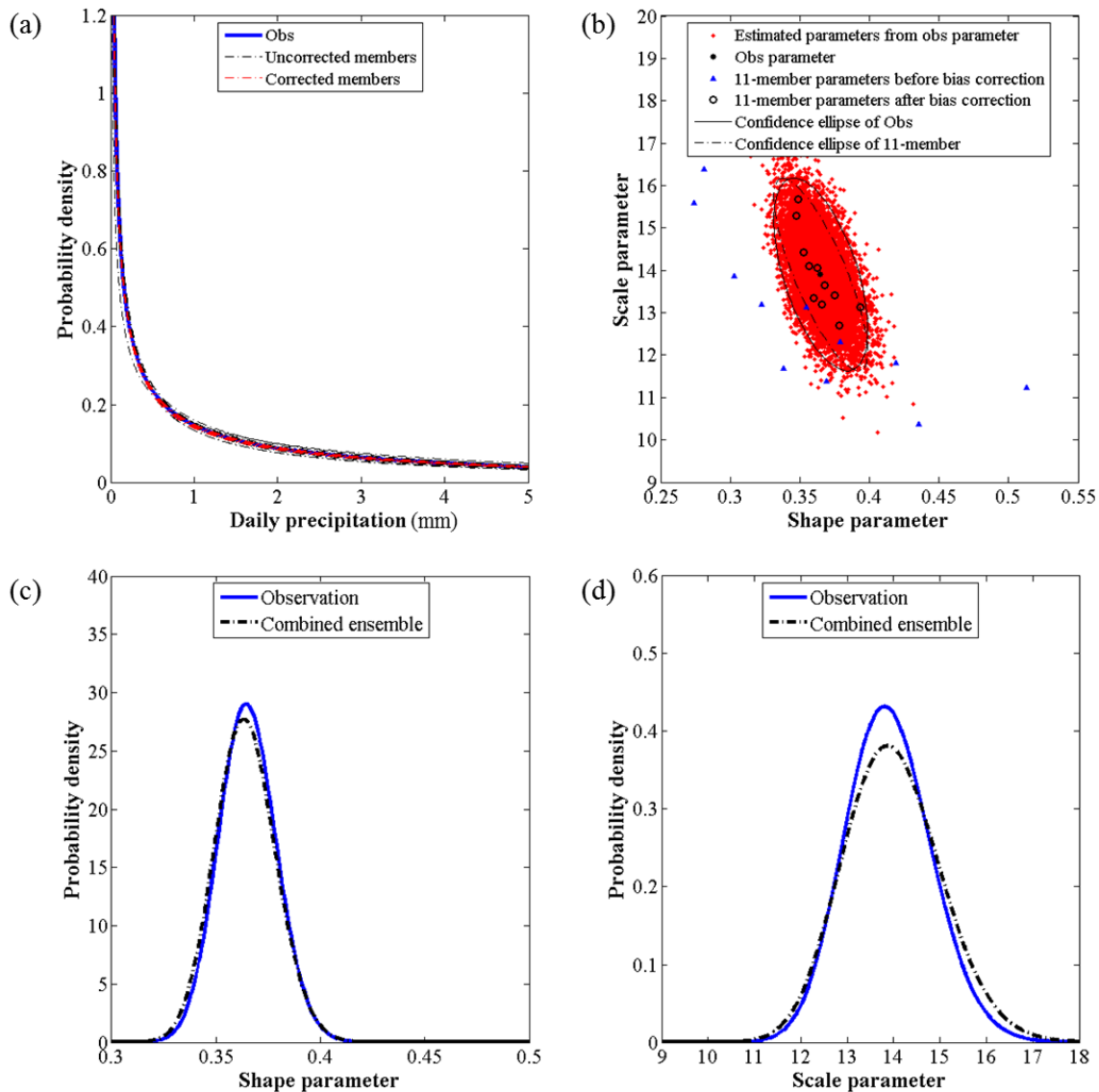
329

330 Figure 8. Results of the conventional bias correction method: (a) Probability density functions of the observed
 331 and simulated (i.e. 11-member) precipitation after bias correction; (b) Scatter plot between shape and scale
 332 parameters of the observed and bias corrected precipitation; (c)-(d) Probability density functions of the shape
 333 and scale parameters of the observed and bias corrected precipitation.
 334

335 4.3 Proposed bias correction

336 To preserve the spread of the ensemble members, a systematic modelling scheme is proposed. Figure 9(a)
 337 presents the PDFs of the observation, bias uncorrected members and bias corrected members. One can see that
 338 the corrected members, although they are not exactly the same as the observation, are closer to the observation

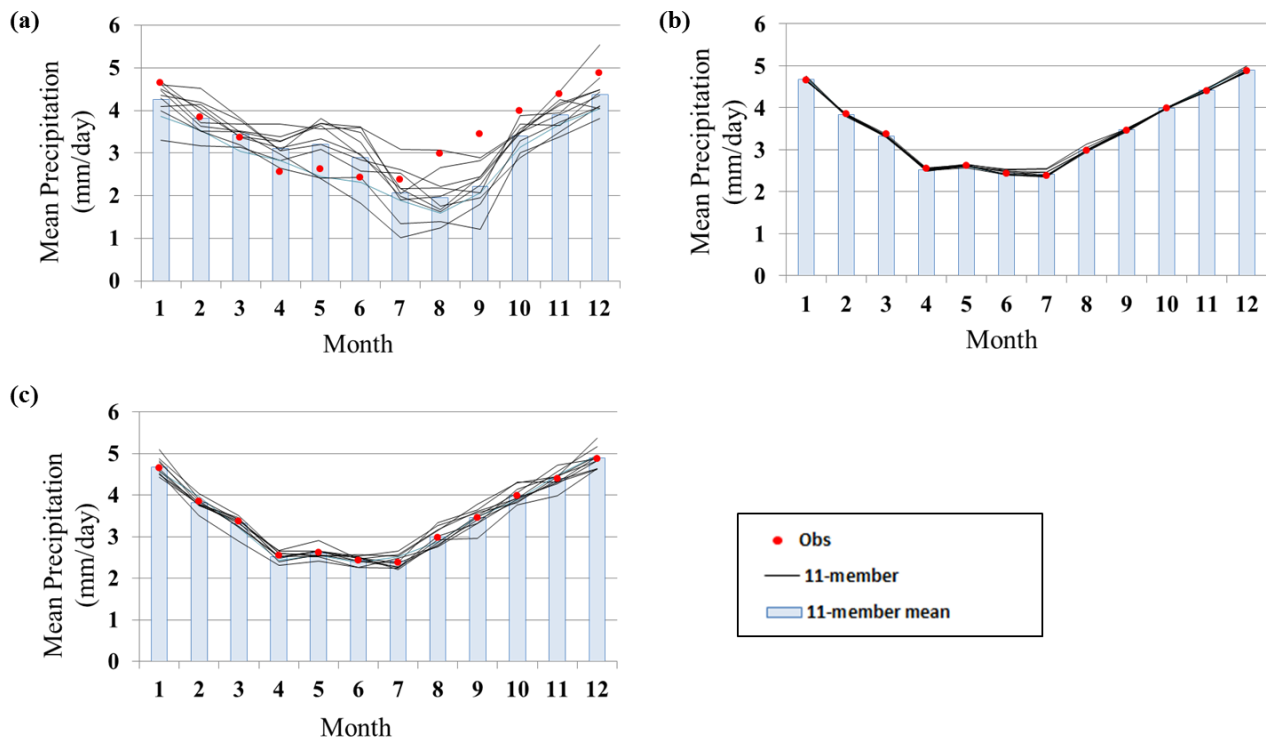
339 than the uncorrected members. It is clearer if we see the result in terms of the parameter space (Figure 9(b)).
 340 The parameters of the corrected members are all within the boundary of the natural variability of the observed
 341 precipitation. In addition, the distributions of the 11-members' parameters after bias correction are quite
 342 similar to those of the observation (Figure 9(c) and (d)). Therefore, one can assume that all ensemble members
 343 represent realistic precipitation scenarios when the natural variability is considered.
 344



345
 346 Figure 9. Results of the proposed bias correction method: (a) Probability density functions of the observed,
 347 bias uncorrected and bias corrected precipitation; (b) Scatter plot between the shape and scale parameters of the
 348 observed, bias uncorrected and bias corrected precipitation; (c)-(d) Probability density functions of the
 349 shape and scale parameters of the observed and bias corrected precipitation.
 350

351 **4.4 Comparison of bias corrected monthly mean precipitation**

352 Figure 10 compares the result of the conventional and proposed bias correction schemes in terms of
 353 reproducing the mean precipitation. Figure 10 (a) shows that the monthly mean precipitations of 11-members
 354 for the period 1961-1990 are quite different to that of the observation. The ensemble means are similar to the
 355 observation only in February and March. The ensemble means generally overestimate the observations from
 356 April to June and underestimate the observations from July to January. When we apply the conventional
 357 method, the corrected monthly mean precipitation of all 11-members is very similar to the observation and the
 358 spread of ensemble is almost entirely removed (Figure 10 (b)). Correction through the proposed method
 359 results in simulated rainfall that has reasonable means, does not have systematic bias in the mean (i.e. no
 360 consistent over- or under-estimation is not present), and represents the spread due to the natural variability
 361 (Figure 10 (c)).



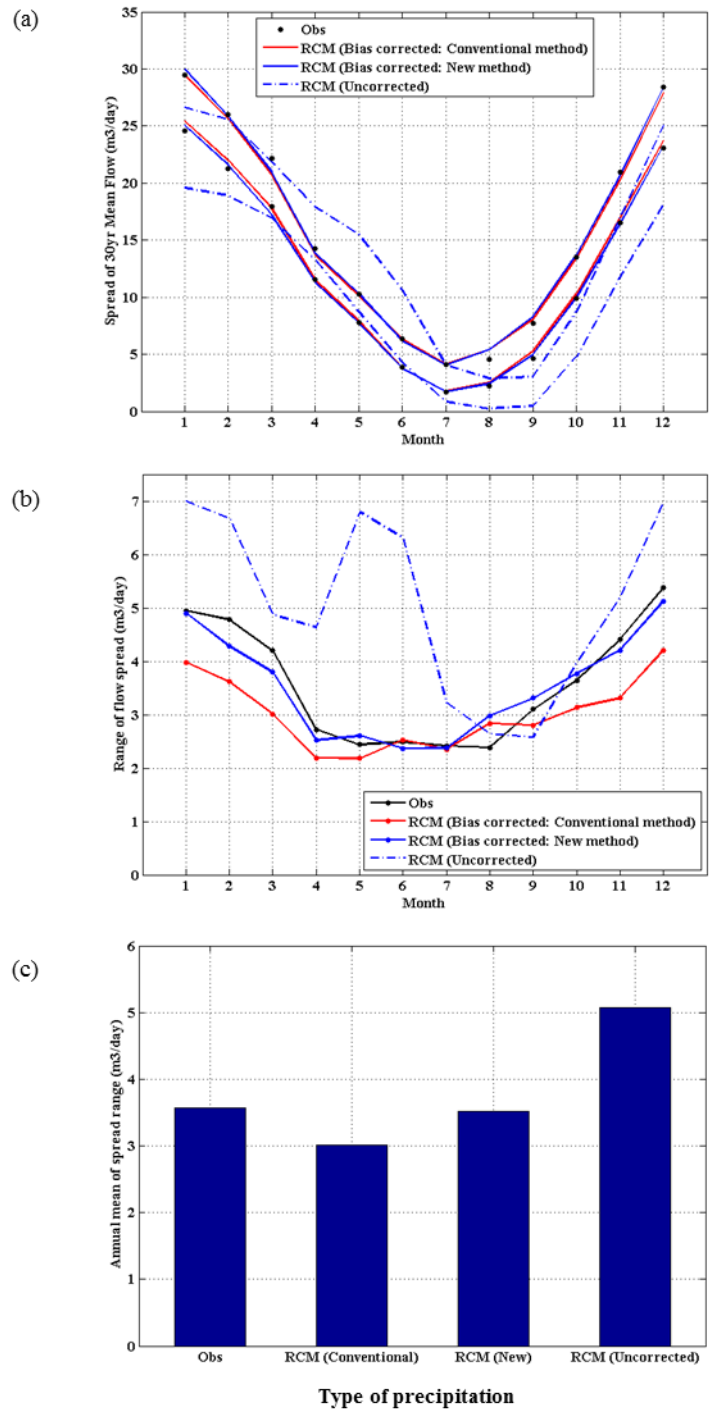
362

363 Figure 10. Monthly mean precipitation for the period 1961-1990 derived from the simulated precipitation. The
 364 mean values for the observation and 11-members are displayed as well. (a) Uncorrected 11-members; (b)
 365 Corrected 11-members by the conventional bias correction; and (c) Corrected 11-member by the proposed
 366 bias correction.

367

368 **4.5 Hydrological application**

369 As presented in Figure 10, the bias and spread of monthly mean precipitation using the proposed bias
370 correction method is more realistic than the conventional method. Next, to investigate the impact of these two
371 different bias correction schemes on flow simulations, we used the aforementioned hydrological model
372 IHACRES. Since the focus of the proposed bias correction scheme is on correcting the mean value and the
373 spread of RCM precipitation ensembles, the same characteristics have been examined in the simulated flow.
374 Figure 11(a) shows the spread of monthly mean flow simulated from the precipitation ensembles for the
375 period 1961-1990. The 5-95 percentile spread has been plotted. Figure 11(b) shows the range of monthly
376 spread and Figure 11(c) shows the annual average value of the spread range. The flow ensemble simulated
377 from the uncorrected 11-member (blue dashed line) obviously has bias and the range of the spread is
378 inconsistent compared with that of the observed flow (black straight line). The flow ensemble simulated using
379 bias corrected RCM precipitation (both conventional and proposed methods) is similar to that of the observed
380 flow since the bias of the precipitation has been removed. However, when we focus on the range of the spread,
381 the overall trend of using the proposed method (blue straight line) is closer to the observation than using the
382 conventional method (red straight line). Specifically, in wet seasons, it is apparent that the proposed method is
383 better while in dry seasons, there are no differences between different bias correction schemes. From this
384 result, our new bias correction scheme is indeed an improvement to the current practice in agreeing with the
385 spread of the simulated flow ensemble.



386

387 Figure 11. The spread of monthly mean flow for the period 1961-1990 derived from the precipitation
 388 ensembles.

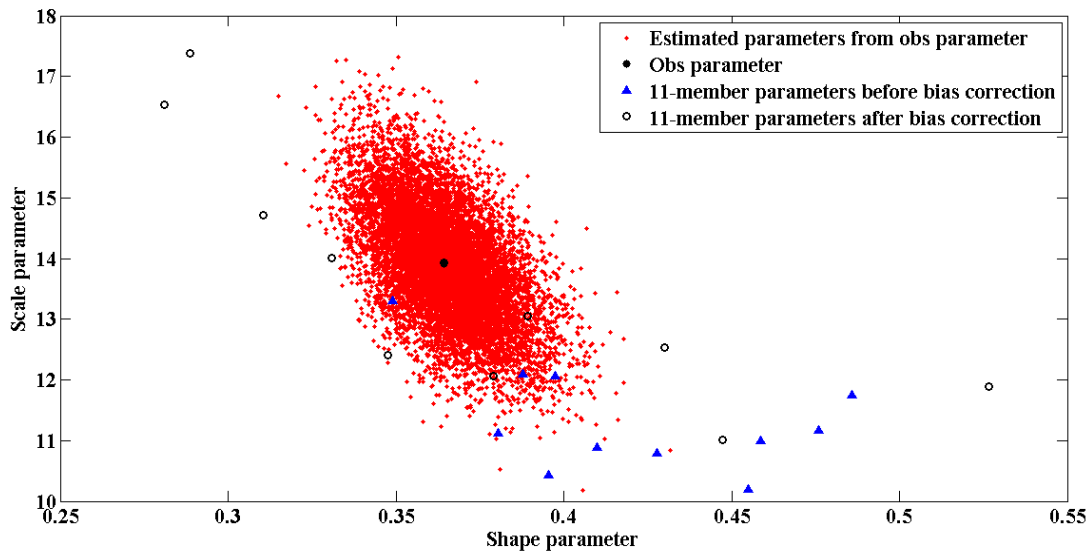
389

390 5. Discussion

391 Climate change scenarios are generated using climate models (e.g. GCMs and RCMs) and emission scenarios,
 392 and are the key information for understanding future changes in hydrologic systems. While RCMs are
 393 designed to better simulate local climate at a finer spatial and temporal scales, it has been acknowledged that

394 bias correction for the outputs from RCMs is generally required to reduce biases due to systematic errors. An
395 ensemble approach has previously been introduced to deal with the systematic errors (i.e. uncertainties) and to
396 provide more relevant scenarios informed by a probability density function. However, the spread of the
397 ensemble, with useful information to understand uncertainties, has not been properly considered in the
398 existing bias correction scheme. In other words, all the ensemble members are matched to that of the
399 observations in terms of statistical characteristics so that the advantage of the ensemble with respect to a
400 single model output is excluded. The major contribution of this study is the proposal of a new bias correction
401 scheme, which reasonably preserves the spread of the RCM ensemble members.

402 Bias in climate models can be introduced by imperfect parameterisation of some climate processes (Ehret et
403 al., 2012; Teutschbein and Seibert, 2012), incorrect boundary conditions and initialization (Bromwich et al.,
404 2013), inadequate reference data sets such as reanalysis data (Dee et al., 2011; Thorne and Vose, 2010), and
405 limitations in input data resolution (Wood et al., 2011). Eleven ensemble members of HadRM3 consist of one
406 unperturbed member and 10 members with different perturbations to the atmospheric parametrisations. Since
407 different members are the outputs from different parameterisations, they would have different biases and be
408 considered as independent (although not totally independent) from other ensembles. Therefore, we believe it
409 is more reasonable to undertake the bias correction independently for each member rather than correcting
410 them with the same bias. An experiment is carried out to identify whether to correct each member individually
411 or to treat them as a group. The idea is that in order to maintain the spread of 11-members, instead of using
412 each transfer function for an individual member, only one transfer function from the unperturbed member is
413 built based on the conventional method and then this transfer function is applied to the rest of the members. If
414 only one transfer function is used for correcting the biases of 11-members, 11-members may maintain the
415 spread after bias correction. However, if the spread is not properly preserved, the corrected ensemble will not
416 represent the true variation of 11-members. Figure 12 shows an example of using one transfer function. The
417 transfer function is built by matching the CDF of an unperturbed member to that of the observation and this
418 transfer function is applied to the other 10 members. As shown in the figure, however, the spread of the 11-
419 member parameters after bias correction is not matched by the spread of the observation. Therefore, the
420 existing approach based on the conventional bias correction scheme generally fails to preserve the ensemble
421 spread.



422

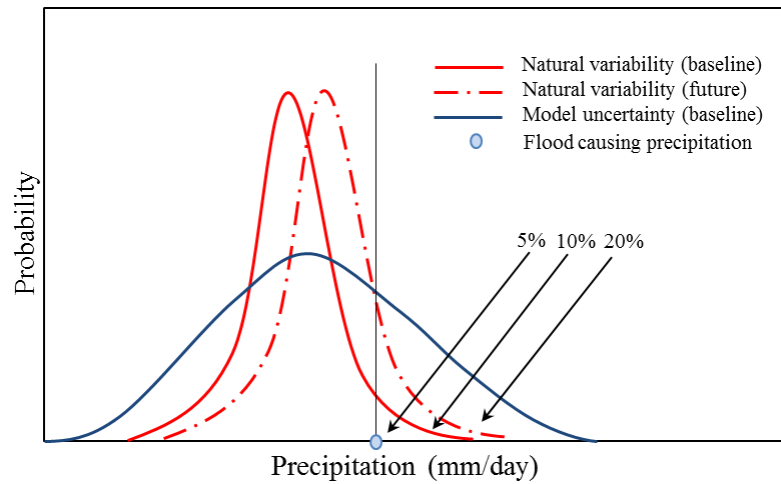
423 Figure 12. Result of using one transfer function for bias correction.

424

425 Ideally if we have numerous numbers of observation data, more reliable climate statistics could be derived.
 426 However, in reality, 30 years of observation data have been used as the reference climate which is just one
 427 realisation of many possibilities, and the uncertainty associated with distributional parametric uncertainty
 428 needs to be considered in designing and conducting impact studies of climate change. Distributional
 429 parametric uncertainty exists when limited amounts of hydrologic data are used to estimate the parameters of
 430 PDF. On the other hand, initial conditions or parameters in climate models can be perturbed to generate a
 431 large number of ensemble members. Given the results we achieve, these ensemble members need to be
 432 examined to ensure that they are plausible.

433 Figure 13 describes why the bias corrected members should originate from within the bounds of the natural
 434 variability of the observation. It is supposed that the probability distributions of the natural variability and
 435 climate model uncertainty look like Figure 13. The range of both the baseline and hypothetical future natural
 436 variability are similar while the model uncertainty is larger. In this case, the chances of floods (i.e. area of the
 437 PDF which are above the flood causing precipitation) for the baseline period and future are 5% and 10%
 438 respectively which we assume are the true values. However, according to the model uncertainty, the odds of
 439 the floods in the future are overestimated by 20% which means more actions are needed to mitigate the flood
 440 risk than in reality. This misinterpretation may, in turn, lead to inefficient efforts to improve the water system

441 since it is related to the mitigation and adaptation plan. Therefore, the spread of the model uncertainty should
442 be similar to that of the climate natural variability.



443
444 Figure 13. Probability distributions of natural variability and climate model uncertainty. The thick red curve,
445 dashed red curve and cyan curve are the probability distributions of the baseline natural variability, future
446 natural variability and baseline model uncertainty respectively. The thick black line is a threshold for flood
447 causing precipitation. The real probabilities of floods for the baseline and the future are 5% and 10%
448 respectively, while the model overestimates the flood risk by 20%.

449
450 This study attempts to evaluate the reliability of the RCM ensemble in terms of natural variability and to
451 propose a new bias correction scheme conforming to the RCM ensembles. However, the proposed scheme is
452 just one of the necessity conditions to assess the RCM ensembles and a comprehensive scheme including
453 more conditions needs to be further developed. It does not mean that the RCM which meets this condition is a
454 good model, but if it does not meet this condition, the RCM ensemble fails to represent the natural climate
455 variation as described in Figure 13 (hence such a condition is a necessity condition, not a sufficiency
456 condition). We believe that there should be a set of necessity conditions to better assess and improve future
457 climate projections in various aspects of uncertainty analysis.

458 459 **6. Conclusions**

460 Conventionally, all climate model simulations are corrected to the observation. With this scheme, the
461 uncertainty of the model from the ensembles will be lost and as a result the 11-member ensemble will be
462 similar to just one member. Another approach is to apply one transfer function based on the unperturbed
463 member to the rest 10 members. This will keep the spread properties of the ensemble but this spread may not

464 conform to the spread from the real natural system. Therefore they do not look like as if they are drawn from
465 the natural system. In this study, we have proposed a new scheme which overcomes the shortcomings of the
466 aforementioned two schemes (i.e. 11 transfer functions all conformed to one observed realisation or one
467 transfer function for 11 members which result in the bias corrected ensembles too narrow or too wide), and the
468 proposed method is a good balance between the two. Therefore, the new bias correction scheme for RCM
469 ensembles is novel and makes better use of the ensemble information. In this scheme the spread of the
470 ensemble is maintained to a certain degree after bias correction which is compatible with the natural
471 variability (i.e. sampling uncertainty) of the observation. This is because the transfer functions are built under
472 the assumption that the corrected members must originate from within the bounds of the natural variability of
473 the observation.

474 We would like to point out a limitation of this study. As previously mentioned, bias correction is a
475 controversial issue. In addition, there is no generic one-suit-fits-all bias correction methods for rainfall data
476 since rainfall time series has many aspects and cannot be all corrected simultaneously. The way of correcting
477 the bias should depend on the data purpose, since the bias depends on the specific rainfall characteristic (Kew
478 et al., 2011). In this study, we have focused on matching underlying statistical properties between the
479 observed and simulated rainfall, which are the cumulative probability distribution and the spread of rainfall
480 series. In the future, other statistical properties for parameter distributions may also be included.

481

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489

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