

“Characterizing the space-time structure of rainfall in the Sahel with a view to estimating IDAF curves”

by Panthou et al (hess-2014-292)

Dear Editor

We are grateful to you for your careful reading of our paper, that allowed to detect a number of typos and to suggest providing additional explanations on a few methodological points. You will find below the detailed description of the corrections that were brought to the paper.

Thanking you again for your work on this paper.

With best regards

G. Panthou

Editor comment

The paper “Characterizing the space-time structure of rainfall in the Sahel with a view to estimating IDAF curves” by Panthou et al. was reviewed by two referees. The authors responded to the reviews and provided a first draft of a revised manuscript. I agree with the referees that despite the fact that methodologically this paper does not produce novelty, new knowledge gained from applications to new datasets in poorly studied and monitored areas, such as western Africa, are indeed valuable.

Based on the HESS Discussion and the assessment of the reviewers I consider the manuscript to be fit for publication in HESS. I do however have some minor technical/editorial requests to improve the final manuscript before accepting it in HESS. I ask that the authors consider these and revise their final manuscript accordingly, providing also a short response to me on how they dealt with each of the questions below.

1) Firstly, I am confused with your response to the referees regarding the definition of the areal reduction factor (ARF) as the ratio between point rainfall and areal rainfall (beginning of section 2.3). Indeed as Referee 1 pointed out the most common definition is that it is the ratio of areal/point rainfall, bounding ARF between 0 and 1. You say the opposite in section 2.3, yet your equations (9) and (10) are indeed showing that ARF is the ratio of areal/point rainfall as it should be. Please correct the text at the beginning of the paragraph or explain where the problem is.

Response: You are absolutely right, this is a pure mistake of formulation (the kind of error you do not detect at first glance, because the definition is so obvious in your mind !!); corrected as :

“In its most general sense, the Areal Reduction Factor is the ratio between areal rainfall and point rainfall, either for a given observed rain event or in a statistical sense.”

and

“this ARF thus denotes the ratio between the areal distribution and the point distribution of the annual rainfall maxima”

2) In section 3.1 you describe the interpolation method by which you generate gridded precipitation 1x1 km from the point measurements by Vischel et al. (2011). I think this deserves a few more lines to explain the method, e.g. what does dynamic kriging mean, how exactly are the gridded data generated, are station values replicated exactly, is elevation used, what is the shape of the semi-variogram, etc. This is important in conjunction with the application of your space-average in equation (18). In your revision you explain now that equation (18) is used on the gridded data, this was unclear in the first manuscript.

Response: Some more details were added at the end of section 3.1, as follows:

“To estimate areal rainfall intensities, this study makes use of the dynamical kriging interpolation method proposed by Vischel et al. (2011). Rainfields are produced over the domain of study at a time resolution of 5 minutes and a spatial resolution of 1 km². Dynamical kriging takes advantage of the time structure of 5-min rainfields to complement the purely spatial information provided by the gauge network. Instead of using a 3-D variogram (the inference of the space-time cross covariance being notoriously non robust), the method relies on the construction of Lagrangian rainfields which display a stable spatial structure represented by a nested exponential variogram. Dynamical kriging is an exact interpolator in the sense that the measured point values are replicated exactly; this interpolator is then used to produce 5-min rainfall grids, with a grid mesh of 1 km².”

3) The message in the paper is that the at-a-station estimation of IDAF parameters (Fig 5) is not indicating a systematic geographical variability, so the region is considered homogeneous and the data are pooled for the final estimation of the global IDAF model. The spatial variability is indeed captured by the new Fig 5, but I would consider summarizing these plots also for instance in box plots of the estimates to better show the real variability between stations. An option would be an 8th panel where for each parameter on the x-axis a box plot of the parameter values would be shown. Or an additional line to Table 1, where the (between-station) mean and standard deviation would be listed together with the new estimates for the global IDAF model. This is only a suggestion, the authors can decide if this information has added value to their work.

Response: Thanks for the suggestion. We have opted for box plots in figure 5. We have thus added the following sentence to the caption : *“The grey box shows box plots of the parameter values obtained at the different rain gauges.”*

4) In section 2.2 the authors begin by stating that the simple scaling framework is the right way to go arguing that multi-scaling is not tractable. I think I understand what you mean, but the fact is that the concept of the areal reduction factor has been analytically treated for the multiscaling (multifractal) setup of which simple scaling is one particular case (e.g. Veneziano and Langousis, 2005). It would be advisable to read and cite this work (and perhaps others) to give recognition to where it is due on methodology.

Response: Good point, we were indeed aware of this work, and we now mention it in the following way:

“The simple scaling framework has been extensively used for deriving IDF curves (Menabde et al., 1999; Yu et al., 2004; Borga et al., 2005; Nhat et al., 2007; Bara et al., 2009; Ceresetti, 2011). An analytical formulation of the ARF was also given by Veneziano and Langousis (2005) in a multiscaling framework. However, simple scaling provides is much more tractable than the multi-scaling approach and is more robust in terms of parameter inference. This is thus the approach chosen here.”

5) In section 2.4 equations (15) and (16) should the term representing lambda not be the ratio D/Dref?

Response: You are absolutely right. In our case $\lambda = D$ because $D_{ref} = 1$; thus our equations are correct, conditionally to the fact that $D_{ref}=1$. In order to make them more general, we have replaced D by lambda in these equations which then become valid for all D_{ref} .

6) I advise to call the last section “Discussion and Conclusions”.

Response: Done

7) Both reviewers wrote to me that the figures need to be improved. The main deficiency is that all figures need to have captions which are fully explaining the figure. In other words, just by reading the caption the message of the figure has to be clear. Please critically revise all your figure captions and consider if they submit to this requirement. Some more detailed comments are:

- Fig 2: In my version the label $q=3$ is missing

Response: Corrected

- Fig 3: In panel b the labels for 5 min and 1 hr resolutions must be mixed. The caption is also not sufficiently explanatory.

Response: Yes, you are right; we have corrected this point in the legend.

And the new caption is : *Figure 3. Space and time aggregation procedures. (a) illustration of the procedure leading to select (right case) or to reject (left case) a gauge for becoming a center for spatial aggregation; (b) time aggregation at a point : comparing a hyetograph of 5-min rainfall to a hyetograph of 1-hour rainfall.*

- Fig 4: Why are there two lines (linear equations) for the simple scaling fit in a)? Is not one, which is mentioned in the text sufficient? Please put units to μ_{ref} and σ_{ref} (this applies to everywhere in the text). In the label of 2) “biais” is misspelled and I suggest putting r^2 instead of $r_squared$.

Response:

a) We have deleted the black line which correspond to $\eta=k(1)$.

b) We have added units

c) We have replaced $r_squared$ by r^2 and biai by bias

- Fig 6: Same question as above, why list two lines for simple scaling in the legend? Is this necessary?

Response: We have deleted the black line

- Figs 7 and 8: In the label “biais” is misspelled.

Response: Replaced

- Fig 10: In my version the symbols in the legend are missing.

Response: Yes, we have modified the figure.

8) Other text editing (in the draft of the revised manuscript with track changes):

- p2 line 20: say “and equally important”

Response: Done

- p3 line 17: the item (i) does not make sense, drop “having produced”?

Response: Done

- p4 line 25: say “for a range of durations”

Response: Done

- p5 line 15: say “analytical formulation”

Response: Done

- p7 line 9: the brackets for the eta term seem wrong

Response: We have deleted the second part of the sentence since we does not use the property $\eta=k(1)$ in figures 4 and 6 anymore.

- p9 line 8: would it make sense to stress that these parameters are “computed for the arbitrary reference duration D_{ref} at a point”?

Response: Yes, we have added it.

p9 line 13: will allow “to verify” or will allow the “verification of”

Response: Done : “will allow to verify”

p10 line 4: “all years with more than”

Response: Done

References

Veneziano, D., Langousis, A.: The areal reduction factor: a multifractal analysis, Water Resour. Res., 41, W07008, doi:10.1029/2004WR003765, 2005.

Manuscript prepared for Hydrol. Earth Syst. Sci. Discuss.
with version 2014/05/30 6.91 Copernicus papers of the L^AT_EX class copernicus.cls.
Date: 3 November 2014

Characterizing the space–time structure of rainfall in the Sahel with a view to estimating IDAF curves

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Abstract

Intensity–duration–area–frequency (IDAF) curves are increasingly demanded for characterizing the severity of storms and for designing hydraulic structures. Their computation requires inferring areal rainfall distributions over the range of space–time scales that are the most relevant for hydrological studies at catchment scale. In this study, IDAF curves are computed for the first time in West Africa, based on the data provided by the AMMA-CATCH Niger network, composed of 30 recording rain gauges having operated since 1990 over a 16 000 km² area in South West Niger. The IDAF curves are obtained by separately considering the time (IDF) and space (Areal Reduction Factor – ARF) components of the extreme rainfall distribution. Annual maximum intensities are extracted for resolutions between 1 and 24 h in time and from point (rain-gauge) to 2500 km² in space. The IDF model used is based on the concept of scale invariance (simple scaling) which allows the normalization of the different temporal resolutions of maxima series to which a global GEV is fitted. This parsimonious framework allows using the concept of dynamic scaling to describe the ARF. The results show that coupling a simple scaling in space and time with a dynamical scaling relating space and time allows modeling satisfactorily the effect of space–time aggregation on the distribution of extreme rainfall.

1 Introduction

Torrential rain and floods have long been a major issue for hydrologists. For one, defining and computing their probability of occurrence is a scientific challenge *per se*, largely because it is a scale-dependent exercise. Secondly, and as equally important, is the fact that they cause heavy environmental, societal, and economical damages – including human losses – thus being a major concern for populations and decision makers.

The request of providing both an objective assessment of the probability of occurrence of high impact rainfall and a tool for civil engineering structure design has found an answer through the calculation of intensity–duration–frequency (IDF) curves. These curves, generally computed from rain gauge data, are intended at characterizing the evolution of extreme rainfall distribu-

tions at a point when the duration of rainfall accumulation changes. However rainfall at point location is not of greatest interest when it comes to the hydrological and socio-economic impacts of extreme events, since it is essentially the convolution of the rainfall intensities over a catchment that characterizes the severity of storms and creates the real threat.

5 This is why intensity–duration–area–frequency (IDAF) curves were conceived as a spatial extension of the IDF curves. Generally established by combining IDF curves and Areal Reduction Factors (ARF), they provide an estimation of extreme areal rainfall quantiles over a range of time and spatial scales.

10 Theoretical studies on IDF and ARF have been an active research topic over the past 20 years or so (Koutsoyiannis et al., 1998; Menabde et al., 1999; De Michele et al., 2001, 2011, among others). IDF practical studies are also numerous but focused on regions where long series of sub-daily rainfall are available (e.g. Borga et al., 2005; Gerold and Watkins, 2005; Nhat et al., 2007; Bara et al., 2009; Ben-Zvi, 2009; Overeem et al., 2009; Awadallah, 2011; Ariff et al., 2012). On the other hand, when ARF are computed from rain gauge networks (Bell, 15 1976; Asquith and Famiglietti, 2000; Allen and DeGaetano, 2005), it requires a fair density of rain gauges in order to obtain accurate estimates of areal rainfall. The computation of IDAF curves must therefore deal with two major data requirements: (i) a high density network of rain gauges **having produced** and (ii) an array of long subdaily rainfall series. In addition to these requirements, scientists face the challenge of producing coherent ARF and IDF models, if they 20 wish their IDAF model to be statistically consistent. This explains why there are so few studies dealing with the implementation of an IDAF model over a given region (e.g. De Michele et al., 2002; Castro et al., 2004; De Michele et al., 2011; Ceresetti, 2011).

25 In fact, in some regions of the world there are virtually no IDF, ARF and IDAF models that have ever been conceived because of data limitations. This is especially the case in many tropical regions, such as West Africa, one reason being that a harsh environment and resource scarcity have make very challenging the operation of recording rain gauge networks. The few IDF studies available in the region (Oyebande, 1982; Mohymont et al., 2004; Oyegoke and Oyebande, 2008; Soro et al., 2010) are essentially empirical with no theoretical background allowing to upgrade their results in order to produce IDAF curves. ARF studies are still fewer,

the most noticeable being an attempt by Rodier and Ribstein (1988) and Ribstein and Rodier (1994) at computing ARF values for a return period of 10 years, with no explicit inference of the areal rainfall distributions. All in all, there has never been any IDAF model derived for West Africa or sub-regions of West Africa. Yet, flood management – for which IDAF curves are a very useful tool – is now a major concern for West African countries. As a matter of fact and despite that West Africa is known for having experienced a major lasting drought over 1970–2000, numerous severe floods and exceptional inundations have struck the region over the last two decades (Tarhule, 2005; Descroix et al., 2012; Samimi et al., 2012). Moreover, the flood damages in the region have been in constant increase since 1950 (Di-Baldassarre et al., 2010).

While operational networks of the West African National Weather Services do not allow the establishment of IDAF curves in a consistent way – because they do not provide any long term subdaily rainfall series – there are other sources of data that can be used for that purpose. Among them are the 5-min rainfall series of the long term AMMA-CATCH observing system covering a 16 000 km² area in South West Niger from 1990 onwards (Fig. 1). In this study we will make use of 30 series providing continuous 5-min rainfall records from 1990 to 2012.

This unique data set enables us to characterize the relationship between extreme rainfall distributions computed at various spatio-temporal scales and to propose IDAF curves for this characteristic Sahelian region.

2 IDAF curves in a GEV distribution and scale invariance framework

IDAF curves are providing an estimate of areal rain-rates – averaged over a given duration D and a given area A – for a given frequency of occurrence (currently expressed in term of return period T_r). In practice, IDAF curves are generally obtained by aggregating a temporal component and a spatial component represented respectively by the intensity–duration–frequency curves (IDF) computed at a point ($A = 0$) and by the Areal Reduction Factors (ARF) computed for a range of [duration durations](#). In this framework, the most general formulation of an IDAF equation is as follows:

$$\text{IDAF}(D, A, T_r) = \text{IDF}(D, T_r) \times \text{ARF}(D, A, T_r). \quad (1)$$

Assessing IDAF curves requires: (i) inferring appropriate statistical distributions of rainfall to estimate the return periods and (ii) describing the statistical links between the distributions obtained at different space–time scales.

Several recent studies have confirmed that the Generalized Extreme Value (GEV) distribution (Coles, 2001) provides a suitable framework to describe the distribution of extreme rainfall at a point (e.g. Overeem et al., 2008; Panthou et al., 2012; Papalexiou and Koutsoyiannis, 2013). Also, many authors have shown that rainfall displays scale invariance properties (Schertzer and Lovejoy, 1987; Gupta and Waymire, 1990; Burlando and Rosso, 1996; Bendjoudi et al., 1997; Veneziano et al., 2006); both in space and time. The temporal scaling properties give access to a direct analytical formulation of IDF curves (Menabde et al., 1999; Borga et al., 2005; Ceresetti, 2011), while the spatial scaling properties allow to upscale IDF curves into IDAF curves (De Michele et al., 2002; Castro et al., 2004; De Michele et al., 2011), thus providing an integrated space–time characterization of extreme rainfall distributions. Under certain assumptions, namely the GEV distribution of point annual rainfall maxima and simple scaling in both time and space, an analytical ~~formulations~~ formulation of the various components of Eq. (1) may be obtained, as will be detailed below.

2.1 GEV distribution

Let us define $I(D, A)$ a random variable representing the annual maxima of rainfall accumulated over a given duration D and area A , and $i(D, A)$ a sample of $I(D, A)$. In the general framework of the block maxima sampling scheme (Coles, 2001), working on annual maxima generally ensures that the block size is large enough for the maxima distribution to follow a GEV distribution (Coles, 2001), written as:

$$G(i; \mu, \sigma, \xi) = \exp \left\{ - \left[1 + \xi \left(\frac{i - \mu}{\sigma} \right) \right]^{-\frac{1}{\xi}} \right\} \quad \text{for } 1 + \xi \left(\frac{i - \mu}{\sigma} \right) > 0 \quad (2)$$

where i is a generic notation for any value associated with a realization of $I(D, A)$, μ being the location parameter, $\sigma > 0$ the scale parameter and ξ the shape parameter of the GEV distribution. The shape parameter describes the behavior of the distribution tail: a positive (resp.

negative) shape corresponds to a heavy tailed (resp. bounded) distribution. When ξ is equal to 0, the GEV reduces to the Gumbel distribution (light tailed distribution):

$$G(i; \mu, \sigma) = \exp \left\{ -\exp \left[-\left(\frac{i - \mu}{\sigma} \right) \right] \right\}. \quad (3)$$

2.2 Simple scaling in time and analytical formulation of IDF curves

5 The simple scaling framework has been extensively used for deriving IDF curves (Menabde et al., 1999; Yu et al., 2004; Borga et al., 2005; Nhat et al., 2007; Bara et al., 2009; Ceresetti, 2011). ~~It provides a~~ An analytical formulation of the ARF was also given by Veneziano and Langousis (2005) in a multiscaling framework. However, simple scaling is much more tractable ~~analytical framework~~ than the multi-scaling approach and is more robust in terms
 10 of parameter inference. This is thus the approach chosen here.

The annual maximum point rainfall random variable $\{I(D, 0)\}$ follows a simple scaling relation for a given duration D – with respect to a reference duration D_{ref} – if:

$$I(D, 0) \stackrel{d}{=} \lambda^\eta \times I(D_{\text{ref}}, 0) \quad (4)$$

where λ is a scale ratio ($\lambda = D/D_{\text{ref}}$), η is a scale exponent and $\stackrel{d}{=}$ denotes an equality in distribution. Note that, for every duration D for which Eq. (4) holds, the normalized random variable
 15 $\{I(D, 0)/D^\eta\}$ has the same statistical distribution than the normalized reference distribution $\{I(D_{\text{ref}}, 0)/D_{\text{ref}}^\eta\}$; this property will be used in the optimization procedure, in Sect. 4.2. Equation (4) implies (Gupta and Waymire, 1990):

$$E[I(D, 0)] = \lambda^\eta \times E[I(D_{\text{ref}}, 0)] \quad (5)$$

20 and, more generally, a scaling of all the moments, that can be written as:

$$E[I^q(D, 0)] = \lambda^{k(q)} \times E[I^q(D_{\text{ref}}, 0)]. \quad (6)$$

Or:

$$\ln\{E[I^q(D, 0)]\} = k(q) \ln(\lambda) + \ln\{E[I^q(D_{\text{ref}}, 0)]\}. \quad (7)$$

The notion of simple scaling is related to how $k(q)$ evolves with q . When this evolution is linear:

$$k(q) = \eta q \quad (8)$$

then simple scaling holds (as opposed to multi-scaling if this relation is non linear).

5 Checking whether the simple scaling hypothesis is admissible over a given range of durations is thus equivalent to verifying on the data set whether the two following conditions are fulfilled (Gupta and Waymire, 1990):

- Eq. (7): log–log linearity between the statistical moments of any given order q ;
- Eq. (8): linearity between $k(q)$ and q , $\eta (= k(1))$ being the scaling factor at order 1.

10 Figure 2a illustrates these two conditions.

2.3 Spatial scaling, dynamical scaling and ARF model

In its most general sense, the Areal Reduction Factor is the ratio between point rainfall and areal areal rainfall and point rainfall, either for a given observed rain event or in a statistical sense. Here we are interested in deriving a statistical ARF that can be used for obtaining an analytical
 15 formulation of IDAF curves (which implies that the ARF does not depend on the return period considered); this ARF thus denotes the ratio between the point areal distribution and the areal point distribution of the annual rainfall maxima:

$$I(D, A) \stackrel{d}{=} \text{ARF}(D, A) \times I(D, 0). \quad (9)$$

Note that Eq. (9) implies the following relationship:

$$20 \text{ARF}(D, A) = \frac{E[I(D, A)]}{E[I(D, 0)]}. \quad (10)$$

In this study, the ARF model proposed by De Michele et al. (2001) is used. This model is based on two assumptions (which will have to be verified, see Sect. 5):

1. the studied rainfall variable is characterized by a simple scaling relationship both in time and space;
2. time and spatial scales are linked by a so-called dynamic scaling property written as:

$$\left(\frac{D}{D_{\text{ref}}}\right) = \left(\frac{A}{A_{\text{ref}}}\right)^z \quad (11)$$

- 5 where z is the dynamical scaling exponent.

When these assumptions are verified, De Michele et al. (2001) show that the ARF can be written as:

$$\text{ARF}(D, A) = \left[1 + \omega \left(\frac{A^a}{D^b}\right)\right]^{\eta/b} = \left[1 + \omega \left(\frac{A^z}{D}\right)^b\right]^{\eta/b} \quad (12)$$

where:

- 10
- η is the scaling exponent characterising the temporal simple scaling;
 - a and b are two positive constant scaling exponents linked by the relation $z = a/b$;
 - ω is a factor of normalization.

This ARF formulation implies that iso-ARF are lines in the plane $\{\ln(A), \ln(D)\}$ as shown in Fig. 2b (De Michele et al., 2001).

15 2.4 GEV simple scaling IDAF model

By assuming that the maximum annual rainfall is GEV-distributed and that the scaling relations in time and space (Sects. 2.2 and 2.3) are verified, then the IDAF model is:

$$I(D, A) \stackrel{d}{=} I(D_{\text{ref}}, 0) \times \lambda^\eta \times \text{ARF}(D, A). \quad (13)$$

As shown in the Appendix A, the compatibility of the simple scaling and GEV frameworks is defined by the following equations:

$$I(D, A) \sim \text{GEV} \{ \mu(D, A), \sigma(D, A), \xi(D, A) \} \quad (14)$$

$$\mu(D, A) = \mu_{\text{ref}} \times \underline{D}\lambda^\eta \times \text{ARF}(D, A) \quad (15)$$

$$\sigma(D, A) = \sigma_{\text{ref}} \times \underline{D}\lambda^\eta \times \text{ARF}(D, A) \quad (16)$$

$$\xi(D, A) = \xi_{\text{ref}} \quad (17)$$

where μ_{ref} , σ_{ref} , and ξ_{ref} correspond to the GEV parameters computed for the arbitrary reference duration D_{ref} at a point, and $\lambda = D/D_{\text{ref}}$.

10 3 Data and implementation

Rainfall observing systems usually do not provide direct measurements at all the space and time scales required for an IDAF study; it is thus needed to derive from the raw data set, an elaborated data set that will allow verifying-to verify the various assumptions founding the theoretical framework defined in Sect. 2.

15 Accordingly, this section describes both the rainfall samples initially available on our Sahelian region of South-West Niger and the process used to obtain the final data set from which the IDAF curves were computed. This process consists in two major steps:

1. Space–time aggregation of the 5-min point rain-rates in order to obtain the average rain-rates for various space (A) and time (D) resolutions;
- 20 2. Extraction of extreme rainfall samples for each of the above resolutions.

3.1 The rainfall data set: AMMA-CATCH Niger records

The AMMA-CATCH Niger observing system was set up at the end of the 1980s as part of the long term monitoring component of the Hapex-Sahel experiment (Lebel et al., 1992). Since

then, it has operated continuously a large array of meteorological and hydrological instruments, providing a unique set of high resolution hydrometeorological data, covering a 16 000 km² area in South West Niger. For the purpose of this research, a subset of 30 5-min rainfall series was selected (Fig. 1), covering the entire 1990–2012 period. At each station, all year-years with more than 25 % of missing data have been removed in order to limit any sampling effect due to missing data in a particular year. After this quality control, all stations remain with at least 20 years of valid data, constituting our raw data sample.

To estimate areal rainfall intensities, this study makes use of the dynamical kriging interpolation method proposed by Vischel et al. (2011). Rainfields are produced over the domain of study at a time resolution of 5 min-minutes and a spatial resolution of 1 km². Dynamical kriging takes advantage of the time structure of 5-min rainfields to complement the purely spatial information provided by the gauge network. Instead of using a 3-D variogram (the inference of the space-time cross covariance being notoriously non robust), the method relies on the construction of Lagrangian rainfields which display a stable spatial structure represented by a nested exponential variogram. Dynamical kriging is an exact interpolator in the sense that the measured point values are replicated exactly; this interpolator is then used to produce 5-min rainfall grids, with a grid mesh of 1 km².

3.2 Space–time rainfall aggregation

The starting elements of the space-time aggregation process, are the discretized fields of rain accumulated over a time increment $\Delta t = 5$ min and averaged over a square-pixel of side length $\Delta xy = 1$ km. In the following, these rainfields are denoted as $r^*(x^*, y^*, t^*)$, where t^* is the ending time of the 5-min time-step, and $\{x^*, y^*\}$ is the center of the 1 km² pixel.

3.2.1 Spatial aggregation of 5 min rainfields

Let A be a surface over which the rainfall intensity is averaged. In this study, A is a square of side $Nx \times \Delta xy$ km = $Ny \times \Delta xy$ km (corresponding to $Nx \times Ny$ pixels of 1 km²). From the 5-min rainfields we can compute series of space averaged 5-min rainfield accumulations r_A^* , as:

$$r_A^*(x^*, y^*, t^*) = \frac{1}{A} \sum_{m=0}^{Nx-1} \sum_{n=0}^{Ny-1} r^* \left\{ x^* + \left(m - \frac{Nx-1}{2} \right) \Delta xy, y^* + \left(n - \frac{Ny-1}{2} \right) \Delta xy, t^* \right\}. \quad (18)$$

From these spatially averaged rainfields, spatial rainfall series have been extracted at rain-gauge locations. For each rain-gauge location (located at $\{x, y\}$), the nearest spatial rainfall series r_A^* (located at $\{x^*, y^*\}$) is extracted. Figure 3a illustrates this approach (the black circle of the right panel represents a rain-gauge located at $\{x, y\}$). In total, 12 scales of spatial aggregations have been retained to build the rainfall series: 1 km² (the pixel on which the station is located is selected) then 4, 9, 16, 25, 49, 100, 225, 400, 900, 1600 and 2500 km².

To limit border effects, the spatial aggregation is performed only in areas where the spatial distribution of stations is more or less isotropic. Each of the 30 measurement stations is considered individually; a circle centered on the station is plotted and divided in eight cardinal sectors (each sector has an angle of 45 °). Only rain gauges having at least one other rain gauge present in at least seven of the eight sectors are retained for spatial aggregation (see Fig. 3a); the distance of the other gauges from the center station is not taken into account for the selection, only matters the presence or absence of a rain gauge in the sector. Only 13 gauges (out of 30) satisfy this criterion (Fig. 1). They are referred to in the following as central rain-gauges (CR) because their localization is used as a central point, from which the 12 areas of aggregation are delimited. In total there are thus 156 areal series (12 areas of aggregation centered on 13 different locations).

3.2.2 Time aggregation of 5-min point series and 5-min spatial series

A time aggregation procedure is applied to the 30 point 5-min rainfall series and to the 156 spatial rainfall series.

Let D be a given duration of Nt 5-min time-steps ($D = Nt \times \Delta t$). The time aggregation is done by using a moving time window of length D over which the 5-min rainfall intensity is averaged (this moving window procedure is carried out in order to make sure that we will be able to extract the maximum maximum for each duration considered). The time aggregation can be written as:

$$r_{D,0}^*(x, y, t^*) = \frac{1}{D} \sum_{p=0}^{Nt-1} r_0^*(x, y, t^* - p \times \Delta t) \quad (19)$$

in the case of 5-min point series located at $\{x, y\}$ ($A = 0$), and

$$r_{D,A}^*(x^*, y^*, t^*) = \frac{1}{D} \sum_{p=0}^{Nt-1} r_A^*(x^*, y^*, t^* - p \times \Delta t) \quad (20)$$

for a given surface A in the case of 5-min spatial rainfall series located at $\{x^*, y^*\}$.

Thus, $Nt = 12$ for $D = 1$ h, $Nt = 24$ for $D = 2$ h and so forth. This procedure is illustrated in Fig. 3b. The 11 different time resolutions considered in this study range from 1 to 24 h (1, 2, 3, 4, 6, 8, 10, 12, 15, 18 and 24 h) and are all obtained from the original 5-min series.

3.2.3 Extraction of extreme rainfall: annual block maxima

The use of GEV distribution to model the extreme rainfall series requires using the block maxima procedure to extract rainfall extremes. It consists of defining annual blocks of observations separately for each of the 11 different time resolutions considered and to take the maxima within

each block. A sample of 23 (1990–2012) annual maximum rainfall values $\{i(D, A)\}$ is thus obtained for each spatial aggregation and duration.

In summary:

- there are 13 reference locations;
- 5 – around each of the 13 reference locations, 12 areas of increasing size 1, 4, 9, 16, 25, 49, 100, 225, 400, 900, 1600 and 2500 km² are defined;
- for each of these 156 (13 × 12) areas, 11 time series of 23 (1990–2012) annual maximum values are constructed, corresponding to 11 different durations of rainfall accumulation 1, 2, 3, 4, 6, 8, 10, 12, 15, 18, 24 h.

10 4 Inferences of the individual components of the model

The proposed model has seven parameters: the temporal scale exponent (η), the three ARF parameters (a, b, ω) and the three GEV parameters ($\mu_{\text{ref}}, \sigma_{\text{ref}}, \xi_{\text{ref}}$). After having tested different optimization procedures (most notably a global maximum likelihood estimation and the 2-step method proposed by Koutsoyiannis et al., 1998) a 3-step method was finally retained, since it
 15 gave the best results in the evaluation of the IDAF model (see Sect. 5). These three steps are explained in the following paragraphs (Sects. 4.1 to 4.3). For each step, an illustration based on the result obtained for the Niamey Aéroport station is given in Fig. 4.

4.1 Temporal simple scaling: estimation of η

The temporal scaling of the IDAF model is described by the η parameter. The inference of η is
 20 achieved in two steps. The first one consists in computing $k(q)$ for different moments q through a linear regression between the logarithm of the statistical moments of order q ($E[I^q]$) and the durations D (see Fig. 4a, left panel). Then, η is obtained by a linear regression between $k(q)$ and q (see Fig. 4a, right panel). At the Niamey Aéroport station, the value obtained for η is equal to -0.91 .

4.2 GEV parameters: μ_{ref} , σ_{ref} , ξ_{ref}

The GEV parameters μ_{ref} , σ_{ref} , ξ_{ref} are estimated on the point samples, using the property that all normalized samples $\{i(D,0)/D^n\}$ must come from the same distribution if simple scaling holds. All normalized samples are pooled in one single sample on which the GEV parameters are estimated (this methodology corresponds to the second step of the 2-step method proposed by Koutsoyiannis et al., 1998). Figure 4b illustrates this process at the Niamey Aéroport rain gauge: initial samples are displayed on the left panel, normalized samples are plotted on the right panel. The fitted GEV and the estimated GEV parameters are also given in this figure.

In comparison with fitting the GEV parameters separately to each sample constituted for each duration, this method aims at limiting sampling effects by fitting the GEV parameters on a single sample gathering all rainfall durations. The maximum Likelihood and the L-Moments methods were tested for estimating the GEV parameters. The estimation provided by these methods gave similar results, probably due to the large sample size. The results of the L-Moments method are presented here, this method being generally considered better than the MLE for the estimation of high quantiles when the length of the series are short (Hosking and Wallis, 1997).

4.3 Spatial scaling

The estimation of a , b , ω was carried out by minimizing the mean square difference between the empirical ARF (Eq. 10) and the model ARF (Eq. 12), as originally proposed by De Michele et al. (2001). Other scores (mean and max absolute error, bias, ...) and variables (difference between the observed and model mean areal rainfall) have been tried but gave poorer results in validation (Sect. 5). Figure 4c shows the comparison between the empirical ARF and the model ARF at the Niamey Aéroport station and the parameters obtained for the theoretical ARF model.

4.4 Regional model

The point parameter inference (μ_{ref} , σ_{ref} , ξ_{ref} and η) has been performed on each of the 30 point rainfall series, which thus provide 30 IDF models. The complete IDAF model has been fitted

to each of the 13 rain gauges CR. The obtained IDF and IDAF parameters do not display either any coherent spatial pattern or any trend over the domain, as may be seen in Figure 5. Sampling effects due to the small area and the short length of the series may explain this point, since a trend has been observed on a larger domain at the regional scale for daily rainfall (Panthou et al., 2012).

Assuming a spatial homogeneity of rainfall distribution (no spatial pattern), annual maxima series have been pooled together to obtain regional samples. The regional samples were used to fit the IDAF model over the domain in order to limit sampling effects. The point regional sample pools together the 30 rainfall samples directly provided by the 30 rain gauges $i(D, 0)$; the 12 areal regional samples obtained for each of the 12 spatial resolutions $\{i(D, A); A = 1, \dots, 2500 \text{ km}^2\}$ result from pooling together the 13 individual series (CR rain-gauges) computed as explained in Sect. 3.

Table 1 presents the parameters obtained for the global IDAF model. The obtained GEV parameters are $\mu_{ref} = 40.6 \text{ mm h}^{-1}$, $\sigma_{ref} = 10.8 \text{ mm h}^{-1}$, and $\xi_{ref} = 0.1$. When upscaled to the daily duration $\mu(24 \text{ h}) = 2.29 \text{ mm h}^{-1}$ (55.0 mm day^{-1}) and $\sigma(24 \text{ h}) = 0.61 \text{ mm h}^{-1}$ (14.6 mm day^{-1}). It is worth noting that these latter values are coherent with those obtained for a much larger area in this region by Panthou et al. (2012, 2013), working on the data of 126 daily rain gauges covering the period 1950-1990. Note also that the temporal scale exponent (η) is large (0.9), which means that the intensity strongly decreases as the duration increases. This is not surprising given the strong convective nature of rainfall in this region. Similar values of the temporal scaling exponents are obtained in regions where strong convective systems occur (Mohyont et al., 2004; Van-de Vyver and Demarée, 2010; Ceresetti et al., 2011) while lower values are obtained in regions where extreme rainfall is generated by different kinds of meteorological systems (for example in many mid-latitudes regions, see e.g. Menabde et al., 1999; Borga et al., 2005; Nhat et al., 2007). The dynamic scaling exponent is roughly equal to 1 which means that increasing the surface by a given factor leads to a similar ARF change than increasing the duration by the same factor (keeping in mind that this rule applies only to the range of time-space resolutions explored here).

5 IDAF model evaluation

The evaluation of the IDAF model is carried out in two successive stages. First each component used to build the final model (temporal simple scaling, ARF model and GEV distribution) is checked individually; then the global goodness of fit is tested using the Anderson–Darling (AD) and the Kolmogorov–Smirnov (KS) tests.

In Fig. 6 two series of graphs are plotted in order to verify whether the simple scaling hypothesis holds for the time dimension. On the left are the plots of $\ln(E[I^q])$ vs. $\ln(D)$ designed to check the log-log linearity between these two variables (Eq. 7); on the right are the plots of q vs. $k(q)$ aimed at checking the linearity between these two variables (Eq. 8). At all three spatial scales, there is a clear linearity of the plots, meaning that the two conditions for accepting the temporal simple-scaling hypothesis are fulfilled. Note that the graphs shown are those obtained on the regional samples for 3 different spatial scales only (point scale, 100 and 2500 km²), but the quality of the fitting is similar for all the other spatial scales.

Simple scaling in space and dynamical scaling (e.g. the relationship between time and spatial scaling) are checked in Fig. 7. This figure compares the empirical ARFs (Eq. 10) computed on the regional samples and the ARFs obtained with the model (Eq. 12) for all the space and time scales pooled together. With a determination coefficient (r^2) of 0.98, and a very small RMSE, it appears that the model restitutes very well the empirical ARF at all space and time scales, except at the hourly time step and for the three largest surfaces (900, 1600 and 2500 km²), for which the model significantly underestimates the observed reduction factor. At such space–time scales the finite size of the convective systems generating the rain-fields creates a significant external intermittency (see Ali et al., 2003, on the distinction between internal and external intermittency). It thus seems that the simple scaling framework holds only as long as the influence of the external intermittency is negligible or weak. Consequently it is likely that the underestimation of the areal reduction factor by the simple scaling based model would be observed for larger space–time scales than the ones the AMMA-CATCH data set allows to explore.

Figure 8 illustrates that the global model is also able to reproduce very correctly the mean areal rainfall intensity over the whole time-space domain explored here, except again for the hourly time step and the largest surfaces.

As the IDAF model is primarily designed to estimate high quantiles, its ability to represent the mean is not a sufficient skill. It is thus of primary importance to evaluate its ability to also represent correctly high return levels and extreme quantiles. This was realized by visually inspecting return level plots and by using Goodness Of Fit (GOF) statistical tests computed in a cross validation mode (all the stations are used to calibrate the model except one which is used to validate the model prediction). These tests are used to quantitatively assess how well the theoretical GEV distribution based on the IDAF model fits the empirical CDFs of the observed annual maxima for each spatio-temporal resolution. Each test provides a statistic and its corresponding p value. The p value is used as an acceptance/rejection criterion by fixing a threshold of non exceedance (here 1, 5, and 10 %).

The return level plots displayed in Fig. 9 for two reference locations and 3 time steps allow a visual inspection of the capacity of the global IDAF to fit the empirical samples. The p values of the two GOF tests are given in the inset caption. As could be expected, there is a significant dispersion of the results obtained on individual samples. The difficulty of reproducing correctly the empirical distribution when combining the smallest time steps with the largest areas is confirmed. While similar graphs were plotted for the other 11 reference locations, it is obviously difficult to obtain a relevant global evaluation from the visual examination of such plots.

Figure 10 aims at tackling this limitation by representing this information in a more synthetic way. In this figure the percentage of individual series for which the IDAF model is rejected by the Anderson–Darling GOF test is mapped for each duration and spatial aggregation for two levels of significance (1 and 10 %). Here it is worth remembering that we have 30 individual series for the point scale, and 13 different individual series for each of the 12 spatial scales, meaning that, for a given time step, the percentage of rejections/acceptations are computed from a total of 186 ($30 + 12 \times 13$) test values. Here again, the limits of the model for small time steps and large areas are clearly visible; one can also notice a larger number of rejections for small areas and the highest durations (duration higher than 12 h and area smaller than 25 km^2). Apart

from that, the number of rejection of the null hypothesis remains low. The KS test (not shown) display similar result with a little less rejections of the null hypothesis. It thus appears fair to conclude that, over the range of space–time scales covered by the AMMA-CATCH network, a simple scaling approach allows for computing realistic areal reduction factors, the limit of validity being reached for areas roughly larger than 1000 km² at the hourly time step.

6 Discussion and Conclusions

Up to now the rarity of rainfall measurements at high space–time resolution in Tropical Africa, had not permitted to carry out comprehensive studies on the scaling properties of rain-fields in that region. From 1990, the recording rain gauge network of the AMMA-CATCH observing system samples rainfall in a typical Sahelian region of West Africa at a time resolution of 5 min and a space resolution of 20 km, over an area slightly larger than 1° × 1°. This data set was used here for characterizing the space–time structure of extreme rainfall distribution, the first time such an attempt is made in this region where rainfall is notoriously highly variable.

Simple scaling was shown to hold for both the time and the space dimensions over a space–time domain ranging from 1 to 24 h and from the point scale to 2500 km²; it was further shown that dynamical scaling relates the time scales to the space scales, leading to propose a global IDAF model valid over this space–time domain, under the assumption that extreme rainfall values are GEV distributed.

Different optimization procedures were explored in order to infer the 7 parameters of this global IDAF model. A 3-step procedure was finally retained, the global IDAF model being fitted to a global sample built from all the different samples available for a given space–time scale. This model has been evaluated through different graphical methods and scores. These scores show that the areal reduction factors yielded by the IDAF model fit significantly well (in a statistical sense) the observed areal reduction factors over our space–time domain, except for the part of the domain combining the smallest time scales with the largest space scales. This limitation is likely related to the larger influence of the external intermittency of the rain-fields at such space–time scales.

Despite the growing accuracy of rainfall remote sensing devices, this study demonstrates that dense rain-gauge networks operating in a consistent way over long periods of time are still keys to the statistical modeling of extreme rainfall. In the numerous regions where rainfall is undersampled by operational networks and where satellite monitoring is not accurate enough to provide meaningful values of high rainfall at small space and time scales, dense networks covering a limited area may provide the information necessary for complementing the operational networks and satellite monitoring. In West Africa, south to the Niger site, AMMA-CATCH has been operating another site of similar size in a Soudanian climate since 1997 (Ouémé Catchment, Benin), providing ground for a similar study in a more humid tropical climate.

As mentioned in the discussion of Sect. 5, there is however a limitation of these two research networks, linked to their spatial coverage. Extending the area sampled by these networks to something in the order of $2^\circ \times 2^\circ$ would indeed allow studying more finely the effect of the limited size of the convective systems onto the statistical properties of the associated rain-fields. However, this means enlarging the area by a factor 4, making it much more costly and difficult from a logistical point of view to survey properly. For the years to come, AMMA-CATCH remains committed to operating both the Niger and the Benin sites for documenting possible evolutions of the rainfall regimes at fine space and time scales in the context of global change as well as for verifying whether the scaling relationships proposed here still hold for quantiles at higher time periods. As a matter of fact, one strong hypothesis of the model proposed here is that the ARF is independent of the return period. This hypothesis seems verified for return periods smaller than the length of our time series, but it is not possible to infer whether this really holds for higher return periods. Therefore developing an IDAF model able to account for a possible evolution of the ARF with the return period level is a path that has to be explored, copulas being a candidate for such a development (e.g. Singh and Zhang, 2007; Ariff et al., 2012).

It is also envisioned to test other IDAF model formulations based on alternative approaches for modeling the scale relationships, among which the method proposed by Overeem et al. (2010) seems of particular interest.

Appendix A:

A brief explanation of the transition between the simple-scaling framework used to described the space–time scaling of maximum annual rainfall (Eq. 13) and the GEV model used to model the statistical distribution of these maxima (Eqs. 15 to 17) is given here.

5 The random variables $I(D_{\text{ref}}, 0)$ and $I(D, A)$ are modeled by a GEV model:

$$\text{Prob}\{I(D_{\text{ref}}, 0) \leq i(D_{\text{ref}}, 0)\} = \exp\left\{-\left[1 + \xi(D_{\text{ref}}, 0) \left(\frac{i(D_{\text{ref}}, 0) - \mu(D_{\text{ref}}, 0)}{\sigma(D_{\text{ref}}, 0)}\right)\right]^{-\frac{1}{\xi(D_{\text{ref}}, 0)}}\right\} \quad (\text{A1})$$

and

$$\text{Prob}\{I(D, A) \leq i(D, A)\} = \exp\left\{-\left[1 + \xi(D, A) \left(\frac{i(D, A) - \mu(D, A)}{\sigma(D, A)}\right)\right]^{-\frac{1}{\xi(D, A)}}\right\}. \quad (\text{A2})$$

10 Let introduce, $c = \lambda^\eta \times \text{ARF}(D, A)$ then Eq. (13) becomes:

$$I(D, A) \stackrel{d}{=} I(D_{\text{ref}}, 0) \times c \quad (\text{A3})$$

and if Eq. (13) holds, then:

$$\begin{aligned} \text{Prob}\{I(D, A) \leq i(D, A)\} &= \text{Prob}\{I(D_{\text{ref}}, 0) \times c \leq i(D_{\text{ref}}, 0) \times c\} \\ &= \text{Prob}\{I(D_{\text{ref}}, 0) \leq i(D_{\text{ref}}, 0)\} \end{aligned} \quad (\text{A4})$$

15 and

$$\text{Prob}\{I(D, A) \leq i(D, A)\} = \exp\left\{-\left[1 + \xi(D_{\text{ref}}, 0) \left(\frac{i(D_{\text{ref}}, 0) - \mu(D_{\text{ref}}, 0)}{\sigma(D_{\text{ref}}, 0)}\right)\right]^{-\frac{1}{\xi(D_{\text{ref}}, 0)}}\right\}. \quad (\text{A5})$$

By replacing $I(D_{\text{ref}}, 0)$ by $I(D, A)/c$ we obtain

$$\text{Prob} \{I(D, A) \leq i(D, A)\} = \exp \left\{ - \left[1 + \xi(D_{\text{ref}}, 0) \left(\frac{I(D, A) - \mu(D_{\text{ref}}, 0)}{\sigma(D_{\text{ref}}, 0)} \right) \right]^{-\frac{1}{\xi(D_{\text{ref}}, 0)}} \right\} \quad (\text{A6})$$

or

$$\text{Prob} \{I(D, A) \leq i(D, A)\} = \exp \left\{ - \left[1 + \xi(D_{\text{ref}}, 0) \left(\frac{I(D, A) - \mu(D_{\text{ref}}, 0) \times c}{\sigma(D_{\text{ref}}, 0) \times c} \right) \right]^{-\frac{1}{\xi(D_{\text{ref}}, 0)}} \right\}. \quad (\text{A7})$$

5 The equality between Eq. (A2) and Eq. (A7) gives:

$$\mu(D, A) = \mu_{\text{ref}} \times c \quad (\text{A8})$$

$$\sigma(D, A) = \sigma_{\text{ref}} \times c \quad (\text{A9})$$

$$\xi(D, A) = \xi_{\text{ref}}. \quad (\text{A10})$$

10 Equations (A8) to (A10) correspond to Eqs. (15) to (17) in the main text.

Acknowledgements. This research was partly funded by the LABEX OSUG@2020 (ANR10 LABX56), partly by the French project ESCAPE (ANR10-CEPL-005), and partly by IRD and INSU through the support to the AMMA-CATCH observing system. G er emy Panthou Ph.D. grant is funded by SOFRECO.

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Table 1. Obtained parameters for the global IDAF model (a) and corresponding GEV parameters values for the different durations D for the point scale $A=0$ (b)

μ_{ref}	σ_{ref}	xi	η	a	b	z	ω
40.60	10.81	0.10	-0.90	0.165	0.156	1.06	0.026

(a)

GEV Parameter	1h	2h	3h	4h	6h	8h	10h	12h	15h	18h	24h
μ (mm h ⁻¹)	40.60	21.68	15.02	11.58	8.02	6.19	5.05	4.29	3.50	2.97	2.29
σ (mm h ⁻¹)	10.81	5.77	4.00	3.08	2.14	1.65	1.35	1.14	0.93	0.79	0.61
ξ (-)	0.10										

(b)

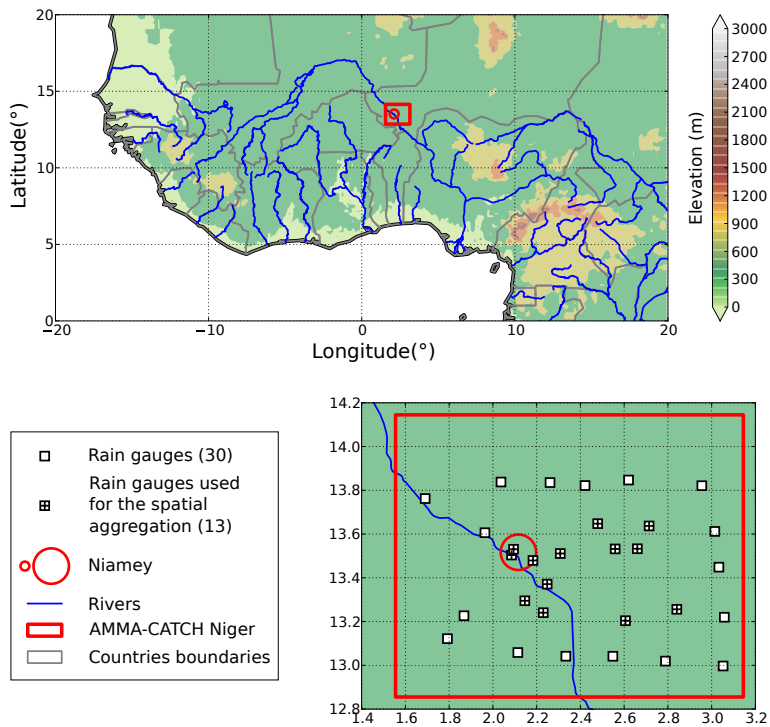


Figure 1. Study area. The background maps displays the elevation (meters).

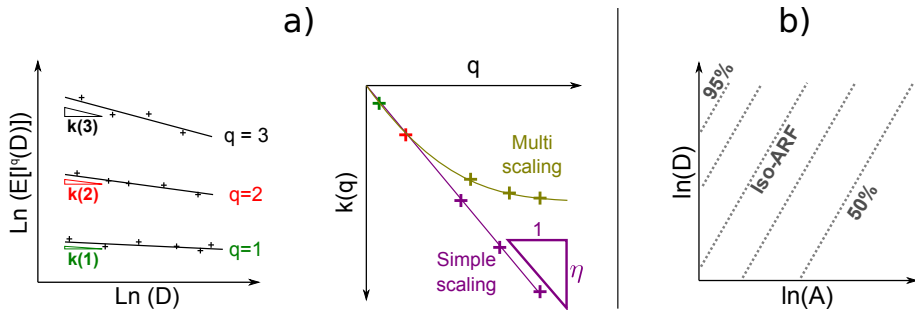


Figure 2. Visual model checks: (a) simple scaling; (b) ARF.

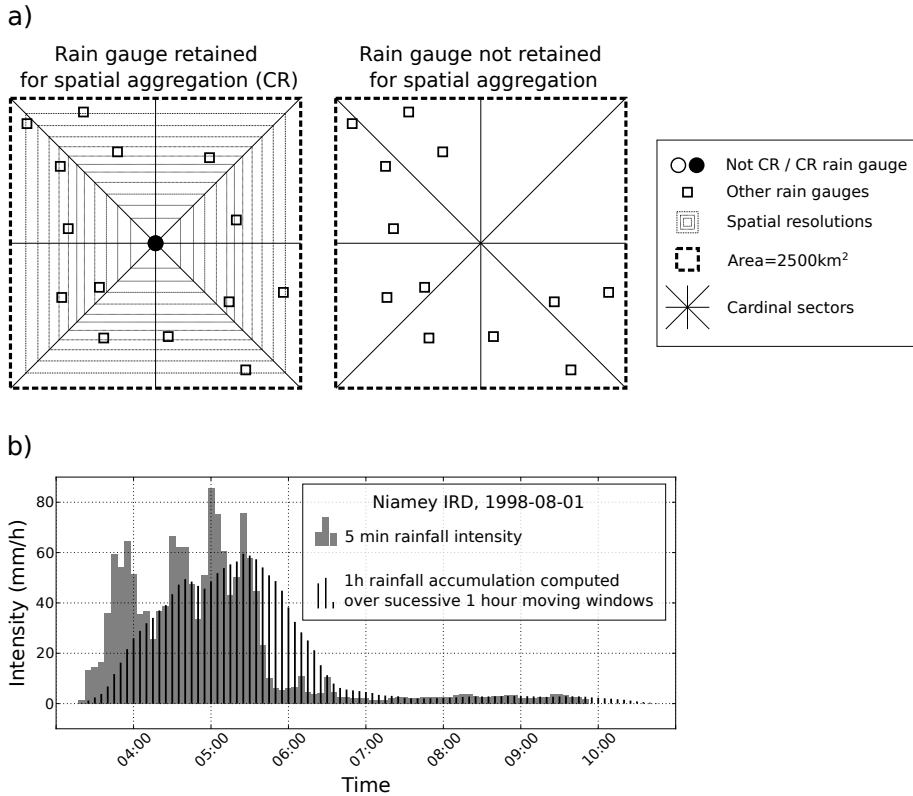


Figure 3. ~~Examples of space- Space~~ and time aggregation ~~used:~~ procedures. (a) illustration of the procedure leading to select (right case) or to reject (left case) a gauge for becoming a center for spatial aggregation; (b) time aggregation at a point : comparing a hyetograph of 5-min rainfall to a hyetograph of 1-hour rainfall.

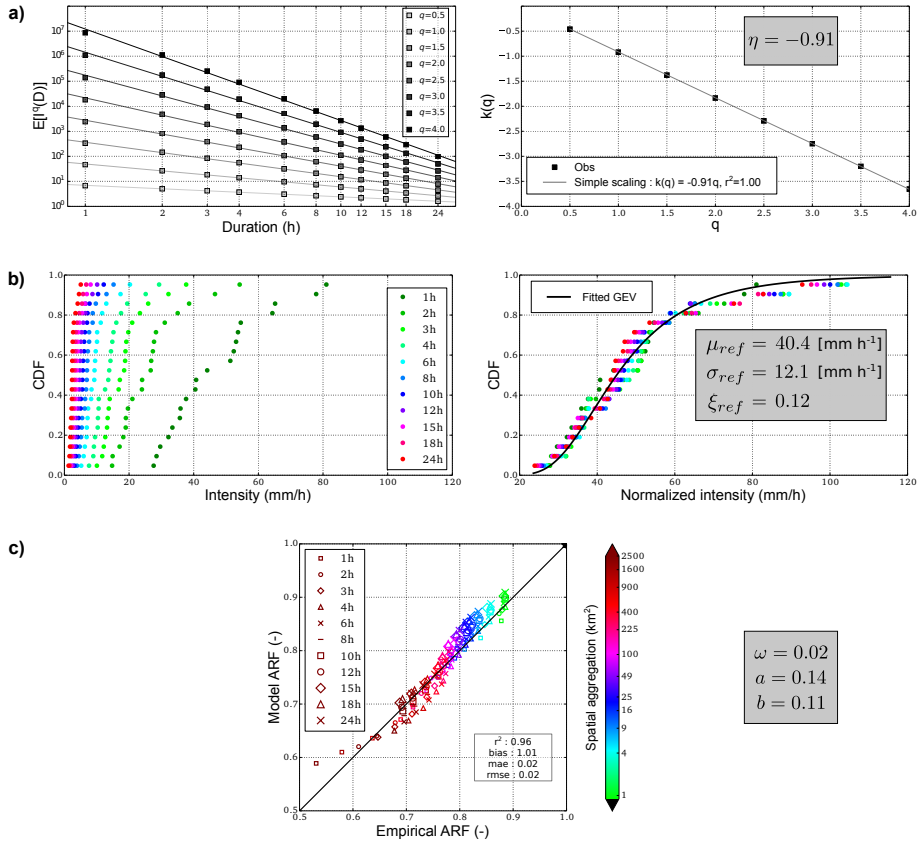


Figure 4. Example of IDAF model inference at the Niamey Airport rain gauge: **(a)** Checking of the temporal simple scaling conditions (left: linear relationship between the logarithm of the statistical moments of order q and the durations D , right: linear relationship between $k(q)$ and q) and estimation of the temporal simple scaling exponent; **(b)** left: empirical cumulative distribution of annual maxima, right: global fitting of the GEV parameters; **(c)** Comparison between empirical and modelled ARF.

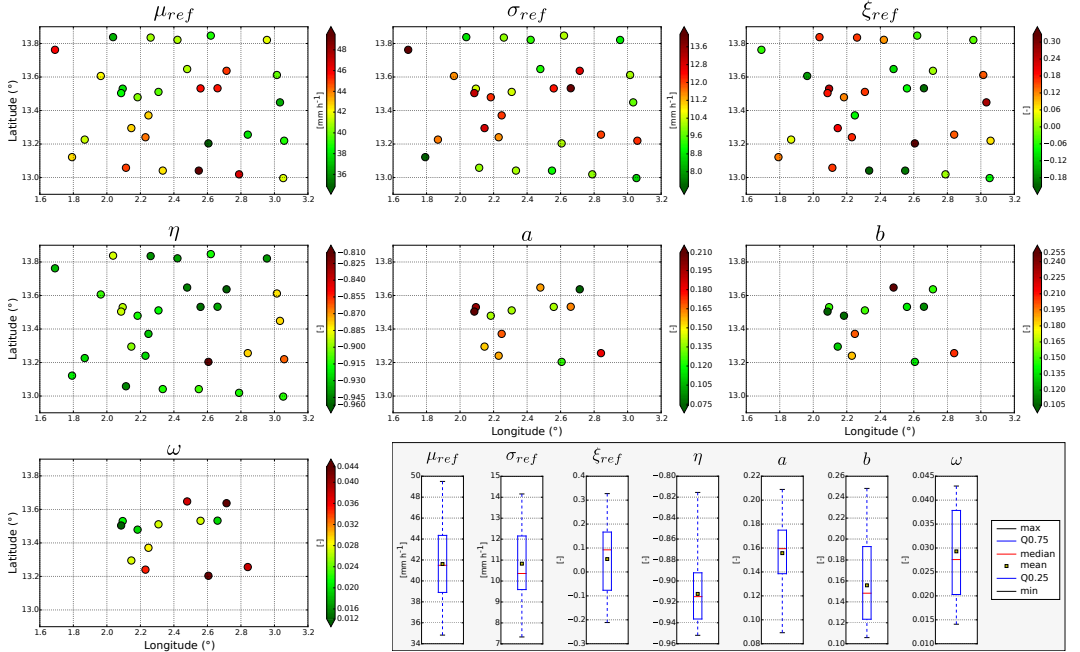


Figure 5. Map of the obtained IDF parameters (η , μ_{ref} , σ_{ref} and ξ_{ref} fitted on the 30 rain gauges samples) and IDAF parameters (η , μ_{ref} , σ_{ref} , ξ_{ref} , a , b and ω fitted on the 13 CR rain gauge samples). The grey box shows box plots of the parameter values obtained at the different rain gauges.

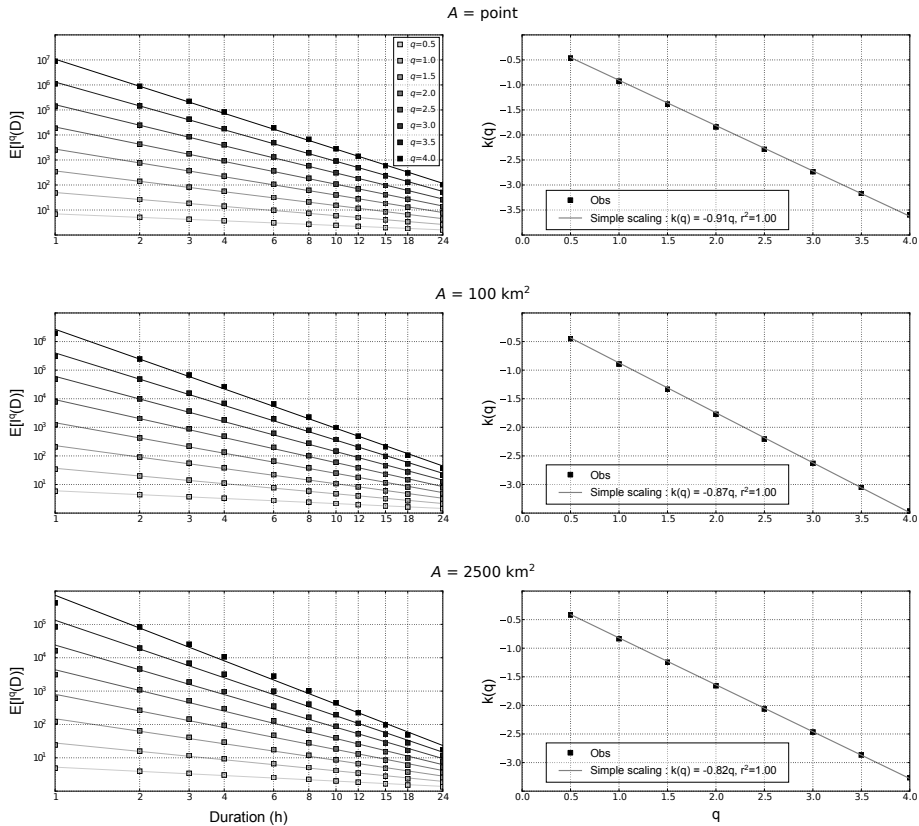


Figure 6. Checking of the temporal simple scaling conditions for the regional samples defined by the 30 available rain gauges for point resolution (top), and the 13 CR rain gauges (see Section 3.2.1) for the resolutions 100 km² (middle) and 2500 km² (bottom).

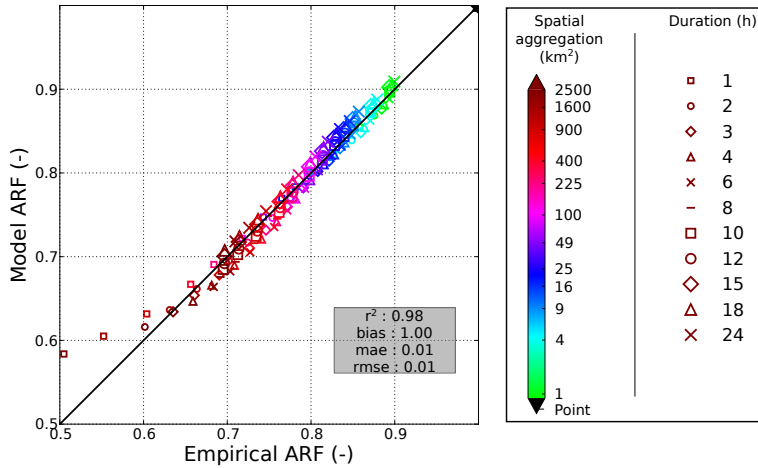


Figure 7. Comparison between empirical ARF (obtained with the regional samples: 30 rain gauges for point resolution and 13 CR rain gauges for other spatial resolutions) and modelled ARF IDAF model.

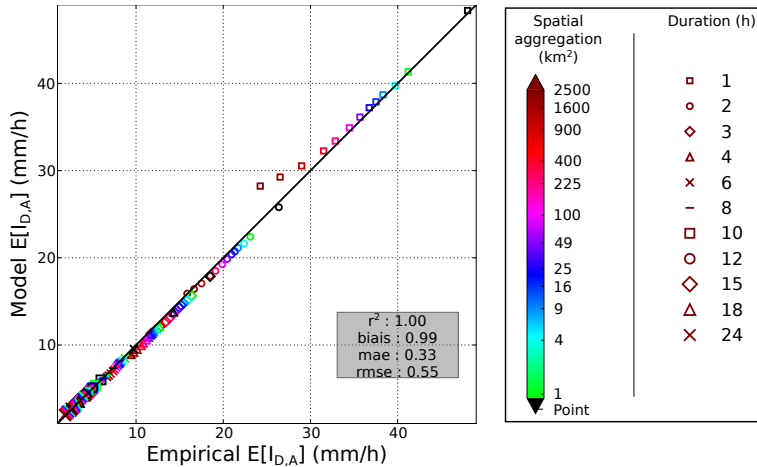


Figure 8. Comparison between empirical mean areal rainfall intensity (obtained with the regional samples: 30 rain gauges for point resolution and 13 CR rain gauges for other spatial resolutions) and global IDAF model for different spatio-temporal aggregations.

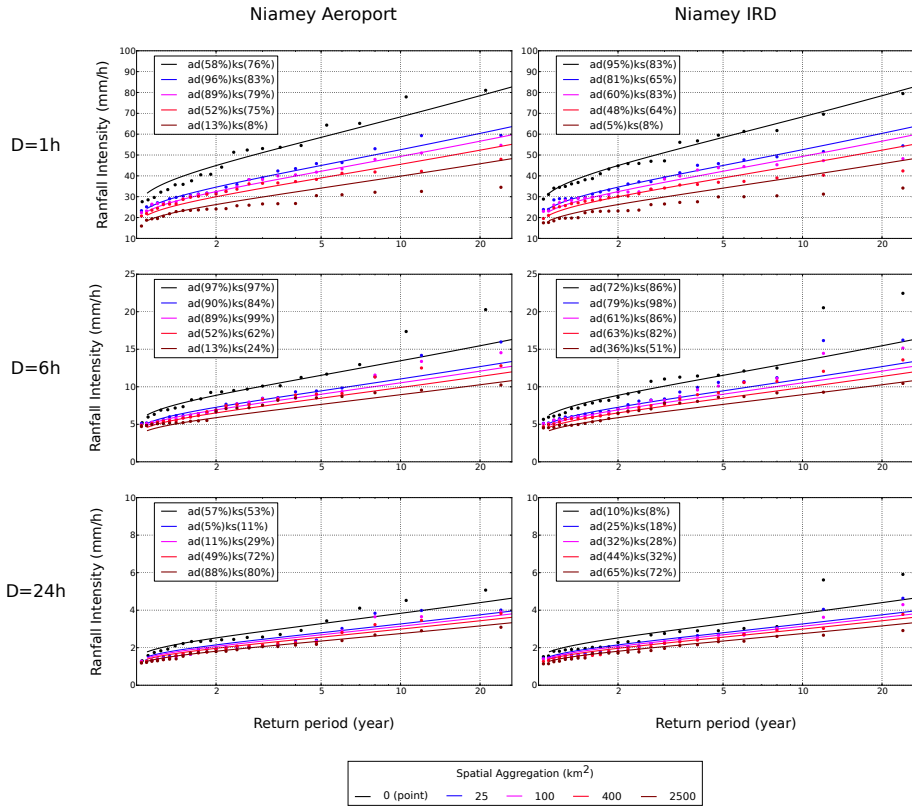


Figure 9. Empirical return level plot obtained at two rain gauges in comparison with the global IDAF model for different durations (1 h, 6 h and 24 h from top to bottom) and different spatial aggregations (from point to 2500 km²).

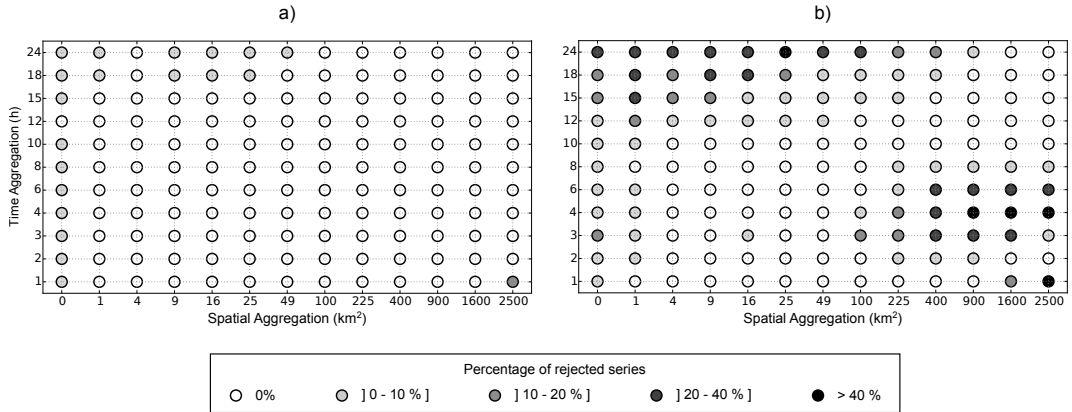


Figure 10. Anderson–Darling GOF test (cross validation): Percentage of rejected series for 1 % (a) and 10 % (b) significance level for the global IDAF model. Note that there are 30 series for the point scale (0 km²) and 13 for the other spatial aggregation (rain gauges CR).