

1 **Hydrological recurrence as a measure for large river basin** 2 **classification and process understanding**

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9 **Abstract**

10 Hydrological functions of river basins are summarized as collection, storage and discharge,
11 which can be characterized by the dynamics of hydrological variables including precipitation,
12 evaporation, storage and runoff. The temporal patterns of each variable can be indicators of
13 the functionality of a basin. In this paper we introduce a measure to quantify the degree of
14 similarity in intra-annual variations at monthly scale at different years for the four main
15 variables. We introduce this measure under the term of recurrence and define it as the degree
16 to which a monthly hydrological variable returns to the same state in subsequent years. The
17 degree of recurrence in runoff is important not only for water resources management but also
18 for hydrologic process understandings, especially in terms of how the other three variables
19 determine the recurrence in runoff. The main objective of this paper is to propose a simple
20 hydrologic classification framework applicable to large basins at global scale based on the
21 combinations of recurrence in the four variables using monthly scale time series. We evaluate
22 it by Lagged Autocorrelation, Fast Fourier Transforms and Colwell's Indices of variables
23 obtained from EU-WATCH dataset composed by eight hydrologic and land surface model
24 outputs. By setting a threshold to define high or low recurrence in the four variables, we
25 classify each river basin into 16 possible classes.

26 The overview of recurrence patterns at global scale suggested that precipitation is recurrent
27 mainly in the humid tropics, Asian Monsoon area and part of higher latitudes with oceanic
28 influence. Recurrence in evaporation was mainly dependent on the seasonality of energy
29 availability, typically high in the tropics, temperate and subarctic regions. Recurrence in

1 storage at higher latitudes depends on energy/water balances and snow, while that in runoff is
2 mostly affected by the different combinations of these three variables. According to the river
3 basin classification 10 out of the 16 possible classes were present in the 35 largest river basins
4 in the world. In humid tropic region, the basins belong to a class with high recurrence in all
5 the variables, while in subtropical region many of the river basins have low recurrence. In
6 temperate region, the energy limited or water limited in summer characterizes the recurrence
7 in storage, but runoff exhibits generally low recurrence due to the low recurrence in
8 precipitation. In the subarctic and arctic region, the amount of snow also influences the
9 classes; more snow yields higher recurrence in storage and runoff. Our proposed framework
10 follows a simple methodology that can aid in grouping river basins with similar
11 characteristics of water, energy and storage cycles. The framework is applicable at different
12 scales with different datasets to provide useful insights into the understanding of hydrologic
13 regimes based on the classification.

14 **1 Introduction**

15 The hydrological cycle, as one of the main earth systems is directly dependent on several
16 periodical cycles with a variety of frequencies. Rotation of the earth on its own axis, rotation
17 around the sun, rotation of the moon around the earth and variations on the earth's axial tilt
18 are the main cause for temporal variations in the land surface and atmosphere. Variations at
19 seasonal scale are the most recognized patterns in most hydrological processes playing
20 important roles in water resource management. Other climatological changes and additional
21 anthropogenic pressure also add to the complexity of the hydrological cycle.

22 Regardless the complexity, the primary function of a river basin in the hydrological cycle is
23 simply characterized with three main functions: collection, storage and discharge (Black,
24 1997). The collection function describes the different paths that supplied water from
25 precipitation follows until it reaches a storage component. This collected water is stored at
26 different states and locations within a basin. Water storage, as the first order state variable of
27 river basins, represents its hydrologic condition and serves as the link between collection and
28 discharge regulating the timing and amount of collected water to be released. The discharge
29 function refers to the processes that release the stored water in the form of evaporation back
30 into the atmosphere or as runoff. Among these functions, the prediction and understanding of
31 the release as runoff has been of high importance to understand water hazards and resource
32 management. Nevertheless, as runoff is highly dependent on the other two functions,

1 understanding the dynamics of water collection and storage is unavoidable in order to
2 understand hydrological processes at river basins.

3 The importance of storage dynamics has been highlighted with emerging new concepts in
4 watershed hydrology. Fill and Spill (Spence and Woo, 2003;Tromp - van Meerveld and
5 McDonnell, 2006;Shaw et al., 2012), connectivity (McGlynn et al., 2013) and threshold (Fu et
6 al., 2013;Ali et al., 2013) are few examples amongst various concepts of runoff generation
7 mechanisms highlighting the importance of water storage and its capacity. Recent studies
8 have demonstrated similar concepts at multiple scales based on water balance analysis
9 (Sayama et al., 2011), combinations of soil moisture and streamflow measurements (Sidle et
10 al., 2000) and numerical simulations (Graham et al., 2010). For larger river basins, there are
11 only a few studies that have identified water storage dynamics at lake/wetland river systems
12 (Spence, 2007;Spence et al., 2010). The stored water volume and its partitioning are
13 important also because they control on residence time and source areas (Sayama and
14 McDonnell, 2009), which ultimately influence on the sensitivity of the system to climate
15 change (Tague and Peng, 2013). Hence storage dynamics should be incorporated as a
16 fundamental metric for catchment classifications and comparisons (Wagener et al.,
17 2007;McNamara et al., 2011).

18 Jothityangkoon and Sivapalan (2009) introduced a simple theoretical framework for
19 classifying different hydrologic regimes based on storage dynamics on different semi-arid and
20 temperate catchments. The framework shows temporal patterns of storage change with
21 periodic rainfall rate and constant potential evaporation. The amount of runoff generated is
22 assumed to be varied significantly depending on water storage being below or above the soil
23 moisture at field capacity and saturation. Therefore with different balances in rainfall,
24 potential evaporation and the soil properties, other variables including ET, storage and runoff
25 exhibit different temporal patterns, and these are further used for a hydrologic regime
26 classification. The assessment further explores the effects of storminess, seasonality and
27 interannual climate variability and their effect on their proposed regimes. Other examples of
28 different approaches for hydrological classification include Weiskel et al. (2014) and the
29 series of papers (Cheng et al., 2012;Coopersmith et al., 2012;Yaeger et al., 2012;Ye et al.,
30 2012). Coopersmith et al. (2012) derived the classification using the aridity index, seasonality,
31 precipitation peak with respect to potential evaporation and the day of peak runoff for 428
32 catchments in the United States. This classification was further used to categorize

1 hydrological change by analyzing the conditions of the indicators (Coopersmith et al., 2014).
2 Berghuijs et al. (2014) utilized the seasonal water balance and temporal interaction of
3 variables to group catchments across the United States.

4 For global scale, several studies have also assessed the interaction of storage variables by
5 using global circulation models. Delworth and Manabe (1988) explored the relations between
6 soil moisture and potential evaporation and how these two interacted and affected climate.
7 Further they explored the relation of the persistence of soil wetness with the persistence of
8 relative humidity by comparing their lagged autocorrelations (Delworth and Manabe, 1989).
9 Also at global scale, the interactions between runoff processes, their feedback with the
10 atmosphere and their effects on simulated water cycle have been thoroughly studied by
11 (Emori et al., 1996). Macroscale effects of water and energy supplies (Milly and Dunne,
12 2002) and their influence on river discharge have been also analyzed using observed data and
13 GCMs (Milly and Wetherald, 2002). For river basin characterization with storage information,
14 Masuda et al. (2001) used basin and atmosphere budgets to evaluate water storage and
15 described similarities among storage patterns for major basins in the world. More recently
16 Kim et al. (2009) used two indices to quantify the significance of different storage
17 components in terrestrial water storage, namely subsurface storage, snow and river storage,
18 and describe their behavior in 29 basins.

19 The objective of the study is to propose a classification framework for large river basins
20 employing the temporal patterns in precipitation, evaporation, storage and runoff utilizing a
21 global dataset. We follow the frameworks of (Masuda et al., 2001; Jothityangkoon and
22 Sivapalan, 2009; Kim et al., 2009) in terms of analyzing the temporal variations of the four
23 main hydrological variables in different climatologies to find similarities and dependencies in
24 runoff generation and variable interactions. Among a variety of metrics, this study focuses on
25 recurrence of hydrologic variables by defining it as the degree to which a monthly
26 hydrological variable returns to the same state in subsequent years. The reason for choosing
27 the recurrence as a metric is practical. The recurrence of runoff and other three hydrological
28 variables are of high importance for a water management perspective. For example, Figure 1
29 compares monthly runoff from two different basins with high and low recurrence
30 characteristics. Although total runoff volume and the seasonality are obviously dominant
31 factors for water resource management, and therefore many previous classification studies
32 have focused on metrics to represent them (Weingartner et al., 2013), anthropogenic systems

1 have already adapted to the local hydrological regimes to some extent. Generally it is more
2 challenging for water managers to handle a random pattern with high fluctuations and
3 different from past experiences, such as floods and droughts happening in unexpected
4 magnitudes in unexpected seasons. The feature of our proposed classification is to show
5 which variables are recurrent or non-recurrent and how different combinations of the
6 recurrence (i.e. our proposed river basin classes) distribute in the world.

7 Section 2 describes the data used in this study, followed by the methodology to calculate
8 recurrence and classification of large river basins in the world in Section 3. Section 4 presents
9 the results and regional characteristics of the basins. In Section 5, we discuss the relationship
10 between our classification and other metrics including aridity, seasonality and phasing
11 between water and energy cycles, as well as future application of the proposed classification.

12 **2 Data**

13 This study uses the “Watch Forcing Data for the 20th Century (WFD) and the “WATCH 20th
14 Century Model Output” from the WaterMIP datasets provided by EU-WATCH. The forcing
15 data are based on the European Centre for Medium Range Weather Forecasting (ECMWF)
16 “ERA-40” reanalysis data (Weedon et al., 2010; Weedon et al., 2011). The model output data
17 set represents contemporary naturalized conditions, with no human interaction such as
18 reservoirs or agricultural withdrawals at 0.5° spatial resolution (Haddeland et al., 2011). The
19 EU-WATCH project includes land surface models (LSMs) and global hydrological models
20 (GHMs) depending on models solving energy balance or not.

- 21 1. *Precipitation*: Precipitation is provided as part of the WFD dataset. LSMs require input
22 rainfall and snowfall independently provided by WFD dataset; whereas GHMs use their
23 own algorithms to separate rainfall and snowfall, using total precipitation as input. Since
24 the partitions within the GHMs are not available in the provided EU-WATCH dataset,
25 this study used total precipitation for the classification as the aggregated variables of
26 rainfall and snowfall.
- 27 2. *Evaporation*: Simulated evaporation for each model is provided as total flux without the
28 distinction of its source (transpiration from vegetation, bare soil evaporation, sublimation,
29 etc.).
- 30 3. *Runoff*: Simulated surface and subsurface runoff for each model are provided
31 independently. However, since the partitions between surface and subsurface differ

1 significantly among models total runoff is used in this study. River discharge is also
2 provided for some models but for comparative purposes generated runoff from land
3 surface is selected for the classification.

- 4 4. *Storage*: Storage is defined in this study as the total amount of water held in a basin
5 regardless its physical state or location. Table 1 summarizes different storage components
6 aggregated to estimate the total storage. In the discussion, further analysis is conducted
7 by using individual components to understand their influence.

8 The time period selected for the analysis is from 1979-2001 at a monthly scale. The original
9 data including precipitation, evaporation, storage and runoff was analyzed first to test their
10 recurrences explained in the next section at each grid-cell. Then for the world's largest 35
11 river basins (Figure 2), the variables are aggregated within the basin and calculated their
12 recurrences to classify the basins.

13 **3 Methods**

14 **3.1 Quantifying recurrence**

15 This section introduces three metrics for evaluating recurrence, which include autocorrelation
16 (AC), Fast Fourier Transform intensity (FFT intensity) and Colwell Index of Contingency
17 (Colwell, 1974). In this study, since our interest is the recurrence of monthly variable defined
18 above, we used a period of 12 months for each metric. The definitions are described below
19 and their characteristics are discussed in section 5.2.

20 **3.1.1 Lagged Autocorrelation (AC)**

21 A serial autocorrelation (AC) defined as (1) describes the correlation of a time series with
22 time lag k :

$$23 \quad r_k = \frac{\sum_{i=1}^{N-k} (x_i - \bar{x})(x_{i+k} - \bar{x})}{\sum_{i=1}^N (x_i - \bar{x})^2} \quad (1)$$

24 where r_k is the AC coefficient for lag k , N is the total number of observations, and \bar{x} is the
25 mean. This AC calculation loses intensity as the lag increases dying down to zero as it
26 approaches N . The AC can further be calculated in terms of the covariance but this
27 computation is considered as a bias calculation of AC. In order to avoid the biased calculation

1 and still be able to calculate a correlation between partial series with larger lags, this series
 2 can be assumed as totally separate series with different mean and variance and the
 3 calculations can be computed as simple correlation with the following equation:

$$4 \quad r_k = \frac{\sum_i^{N-k} (x_i - \bar{x}_{[i, N-k]})(x_{i+k} - \bar{x}_{[i+k, N]})}{\left[\sum_i^{N-k} (x_i - \bar{x}_{[i, N-k]})^2 \right]^{1/2} \left[\sum_{i+k}^N (x_{i+k} - \bar{x}_{[i+k, N]})^2 \right]^{1/2}} \quad (2)$$

5 For the recurrence measure with monthly time series, evaluating the AC of time lag 12 only is
 6 insufficient because it would only take into account the recurrence in contiguous years. We
 7 find more appropriate to include the AC at other multiples of 12. Given the length of the time
 8 series used in this study, we decided to use the mean of AC from time lags 12, 24, 36, 48 and
 9 60.

10 The results will be dependent also on the temporal resolution (e.g. daily or yearly time series).
 11 However in this study we decided to use a monthly resolution and look at yearly cycles
 12 because one year is usually a unit at which most of human activities and natural cycles repeat
 13 themselves.

14 **3.1.2 Fast Fourier Transforms (FFT)**

15 The other measure tested in this study is Fast Fourier Transform (FFT) intensity which can
 16 identify important periods based on a periodogram. The periodical part of a time series can be
 17 described by equation:

$$18 \quad m_\tau = \mu + \sum_{i=1}^h \left(A_i \cos\left(\frac{2\pi i \tau}{p}\right) + B_i \sin\left(\frac{2\pi i \tau}{p}\right) \right) \quad (3)$$

19 where m_τ is the harmonically fitted mean, μ is the population mean, A_i and B_i are the Fourier
 20 coefficients, p is a period (12 for monthly data), and h is the total number of harmonics
 21 (usually $p/2$).

22 The Fourier coefficients are calculates as:

$$23 \quad A_i = \frac{2}{p} \sum_{\tau=1}^p \bar{x}_\tau \cos\left(\frac{2\pi i \tau}{p}\right) \quad (4)$$

1
$$B_i = \frac{2}{p} \sum_{\tau=1}^p \bar{x}_i \sin\left(\frac{2\pi i \tau}{p}\right) \quad (5)$$

2 The intensity can be calculated from these parameters as:

3
$$I_i = A_i^2 + B_i^2 \quad (6)$$

4 The FFT intensity is important to identify the periodicity at a particular frequency. A peak in
5 the plot of intensity vs. frequency (periodogram) identifies a frequency for which a periodical
6 pattern is found. For most hydrological data a peak at a frequency equivalent to a year exists
7 (i.e. 12 months for monthly data, 52 weeks for weekly, and 365 for daily). If a series follows a
8 pattern similar to a sinusoidal function, the intensity will be higher than a series departing
9 from this pattern. Additionally if a series contains much noise the intensity will also be
10 reduced. Hence a recurrent pattern shows higher FFT intensity. Since the FFT intensity is
11 sensitive to the amplitude and magnitude we applied a standard normalization. Discussion
12 upon the characteristics and capability of FFT to measure recurrence is provided in section
13 5.2

14 **3.1.3 Colwell's Contingency Index**

15 Colwell (1974) introduced the indices of constancy and contingency, which together form the
16 index called predictability. These indices have been used to analyze physical and biological
17 temporal fluctuations. The index has been used widely in the analysis of flowering trees
18 (Colwell, 1974), variations in river temperature (Vannote and Sweeney, 1980), variations in
19 flow velocity (Riddell and Leggett, 1981), rainfall distribution at a yearly basis (Miller, 1984),
20 periodicity analysis in streamflow or rainfall data (Gan et al., 1991), classification of flow
21 regimes for environmental flow assessments (Zhang et al., 2012), and description of
22 waterholes in hydrological regimes (Webb et al., 2012). Colwell (1974) defined predictability
23 as the measure of the certainty of knowing a state at a given time, being composed by the sum
24 of two components: constancy, which represent how uniform the state of a variable is at
25 different time cycles, and contingency, which measures the degree to which state and time are
26 dependent on each other.

27 Calculation of the Colwell's Index requires first categorizing the continuous data to prepare a
28 matrix. The columns of the matrix represent time categories and rows represent the states of a
29 phenomenon. In this study the columns represent different months and the rows represent

1 ranges of standard deviations, whose ranges are between minus four to plus four, which is
 2 equally divided into 16 categories with intervals of 0.5σ .

3 Now let N_{ij} be the number of times that a variable falls in state i at time step j . Sum of all
 4 columns for each state i is X_i , sum of all rows for each time step j is Y_j and the total number is
 5 Z . Then Contingency (M) of Colwell's Index is defined as:

$$6 \quad M = \frac{H(X) + H(Y) - H(XY)}{\log s} \quad (7)$$

7 where s is the number of rows, $H(X)$, $H(Y)$, and $H(XY)$ are defined as:

$$8 \quad H(X) = -\sum_j \frac{X_j}{Z} \log \frac{X_j}{Z} \quad (8)$$

$$9 \quad H(Y) = -\sum_i \frac{Y_i}{Z} \log \frac{Y_i}{Z} \quad (9)$$

$$10 \quad H(XY) = -\sum_i \sum_j \frac{N_{ij}}{Z} \log \frac{N_{ij}}{Z} \quad (10)$$

11 Contingency becomes 1 if a variable is at the same state at a particular time step, while the
 12 index becomes 0 if the occurrences in different time steps take place at the same state.
 13 Contingency will be higher as more occurrences in a particular time happen in a particular
 14 state. If the values of a variable in a given month are similar, they will fall under the same
 15 state interval. This will be the case of variables with high recurrence. Further discussion on
 16 the capacity of Colwell's index to represent the concept of recurrence is stated in section 5.2.
 17 For reference, the Constancy (C) and Predictability (P) are defined as:

$$18 \quad C = 1 - \frac{H(Y)}{\log s} \quad (11)$$

$$19 \quad P = 1 - \frac{H(XY) - H(X)}{\log s} \quad (12)$$

20 **3.2 Hydrological Classification**

21 The variables considered in this study are precipitation P , evaporation E , runoff Q and storage
 22 S , which compose the general hydrological cycle and are the main components of the water
 23 balance equation. At global scale or basin scale, each of the four variables are identified as

1 being of high or low recurrence based on the description in previous sections. The first order
2 division of the classification is whether runoff has high or low recurrence, followed by
3 precipitation, evaporation and storage. As a graphical guidance we introduce a classification
4 tree in Figure 3. The figure shows the 16 possible classes, and the combinations that were
5 found and not within the basins of this study. It is provided to be used as a guidance to
6 understand further figures. We used runoff as the first variable for the classification as it is the
7 main concern for water resource management, and other three variables are further used to
8 explain why the runoff in each basin or region shows high or low recurrence. The value used
9 for classifying the basins as high or low recurrence was an AC of 0.75.

10 First we quantified recurrence at global scale except for Greenland, where models
11 performance is questionable due to its particular conditions, and Antarctica, where the EU-
12 WATCH product did not cover. This global analysis was performed for the given time series
13 at of each variables at each individual grid. The analysis for the world's largest 35 basins was
14 performed for the time series of each variable considering the spatial average of the grids
15 included within the limits of the basin.

16 Among all the model output from EU-WATCH, we put particular attention to the WaterGAP
17 model results because it is the only model that includes a calibration module and is closest to
18 observations (Haddeland et al., 2011). Meanwhile, all other model results are also analyzed to
19 cover different model behaviors and discuss model uncertainty (section 5).

20 **4 Results**

21 In this section, we first describe the results of recurrence based on AC from the WaterGAP
22 model as the representative case. WaterGAP is selected here as it is the only model with a
23 simple calibration module and has better agreement with observations (Haddeland et al.,
24 2011). Autocorrelation fits our goal as it precisely measures the degree of similarity of each
25 year when lagged by 12 months. Section 5 discusses the differences in results for the other
26 metrics and the rest of the different models' results. Figure 4 shows the global distribution
27 maps of the recurrence (i.e. AC in this case) in the four variables: precipitation, evaporation,
28 storage and runoff. From the recurrence calculated for each variable's time series, each grid
29 was identified with red for very low recurrence (<0.5), yellow for low recurrence ($0.5\sim0.75$)
30 and green for high recurrence ($0.75\sim1.0$). To explain the distribution of the recurrences in the
31 four variables, this paper uses the following terms for different latitude zones for both

1 hemispheres: Tropical (0° - 23.5°), Subtropical (23.5° - 35°), Temperate (35° - 55°) and Subarctic
2 and Arctic (55° - 90°).

3 The precipitation in the tropical region is basically characterized by the seasonality caused by
4 the oscillation of the Intertropical Convergence Zone, and energy supply due to the effects of
5 the earth's tilt fluctuation. Because of this seasonality, two bands between (5° - 23.5°) for both
6 hemispheres show high recurrence in all variables, while they are lower in general at the
7 equatorial band between 5° S and 5° N where there is no seasonality. The rest of the variables
8 follow generally the same pattern as precipitation although the high recurrence areas of
9 storage and runoff are comparatively smaller than that of precipitation.

10 The subtropical region is mainly characterized by the latitudinal desert belts. This region is
11 characterized by low humidity and general dryness in soil conditions. In this region,
12 precipitation events are typically sudden and intense without following a certain temporal
13 patterns. During rainfall events the other variables also behave similarly. Hence all the four
14 variables tend to have low recurrence. The Southeast Asia Monsoon area is an exception since
15 its behavior is similar to the humid tropics area, therefore displaying high recurrence in all
16 variables.

17 The temperate region also shows generally low recurrence in precipitation due to continental
18 climates or oceanic climates with no dry season. Eastern Asia is the only region showing high
19 recurrence due to the effects of the Asian Monsoon. Evaporation in this region has high
20 recurrence due to seasonality with exception of dry areas in Europe and Asia. Storage has
21 different geographic patterns throughout the region. Runoff follows the same regionalization
22 as storage except for Europe with comparatively low recurrence in general.

23 Precipitation in the subarctic and arctic region shows low recurrence except for some areas in
24 North America and Eastern Siberia. Evaporation exhibits the higher recurrence in this area.
25 The extent area of high recurrence in storage and runoff is larger in this region mainly
26 attributed to the amount of snow.

27 By taking the spatial average of each variable inside the 35 largest river basins in the world,
28 we calculated recurrence and classified them following the tree illustrated in Figure 3. Figure
29 5 shows the result of the classification, which is described below according to each latitude
30 region. Figure 6 displays graphically the results of the calculations of recurrence for each
31 variable. The figure shows the results of the calculated recurrence from the WaterGAP model

1 output and also shows the maximum, minimum, mean and interquartiles of recurrence
2 calculated using the other models. Table 2 summarizes the characteristics of each class.

3 **4.1 Tropical region (0.0°-23.5°)**

4 The tropical region has the most diversity of classes. In this region we found basins belonging
5 to the QPES, QPS, PES, PE and E. Mainly, there are two distinct patterns observed in runoff.
6 High recurrence in runoff takes place in the most humid basins exemplified in Figure 7a by
7 Amazon (QPES) and **Figure 7b** by Orinoco (QPS). Consistent with the global analysis results,
8 we found that precipitation is highly recurrent for these classes due to a repeating pattern
9 resulting from the oscillation of the ITCZ. Evaporation and Storage are also highly recurrent
10 as they follow the same pattern as precipitation as it can be seen in the Amazon time series in
11 Figure 8a. In Orinoco basin evaporation is maintained rather constant as the basin is energy
12 limited and potential evaporation is constant resulting in low recurrence in evaporation.
13 Storage on the other hand follows the same pattern as precipitation resulting in a highly
14 recurrent pattern.

15 More than half of the basins in the tropics exhibit a low recurrence pattern in runoff. These
16 basins are exemplified by Zambezi (PES) and Congo (PE) in Figure 7 and Figure 8. These
17 basins are drier, with less runoff ratio, than basins with recurrent runoff and water limited in
18 some periods of the year. Precipitation shows high recurrence due to the availability of
19 moisture being related to the ITCZ. In these classes evaporation follows the same pattern as
20 precipitation, following the moisture availability pattern. Storage has high recurrence in PES
21 basins mainly because they are characterized by peaks in precipitation and potential
22 evaporation taking place at a different time of the year as seen on the Zambezi River's
23 climatology in Figure 7. As a result the storage fluctuates largely mainly because it the soil
24 moisture component fills in the wet season and nearly dries in the dry season (Figure 8c and
25 storage component climatology of Zambezi Basin in supplement). This creates a strong
26 seasonal pattern in total storage leading to high recurrence. PE class is characterized by the
27 peaks of potential evaporation and P peaking at the same time (Figure 7d: Congo PE).
28 Compared to Amazon, average precipitation is much lower but potential evaporation is almost
29 the same. The Congo basin can be energy limited ($P > PET$) in the wet season, therefore
30 regardless the amount in precipitation, evaporation will reach its potential creating more
31 recurrent pattern in evaporation. The anomalies in precipitation directly transfer to storage and
32 runoff variations, and since runoff ratio (Q/P) and storage change ratio ($\Delta S/P$) are much

1 smaller, these anomalies are larger relative fluctuations to these variables, hence recurrence in
2 storage and runoff patterns is low. Sao Francisco basin is an exception in this region
3 consisting only of recurrent evaporation. This type of basin is mainly seen in the temperate
4 region and is explained in detail in section 4.3.

5 **4.2 Subtropical region (23.5°-35.0°)**

6 In subtropical region, mainly two patterns classes are observed. QPES river basins are located
7 in Southeast Asian Monsoon, where similar behaviors are observed as the same class river
8 basins in tropical region. On the other hand we can observe the basins that are extremely dry,
9 represented by Orange basin in Figure 7. In these basins, all variables follow the patterns of
10 precipitation being, sudden, abrupt and lacking any defined temporal distribution, leading to
11 class L (i.e. none of the variables are recurrent). The Indus river basin is an exception in this
12 region belonging to the E class.

13 **4.3 Temperate region (35.0°-55.0°)**

14 In the temperate region there are three particular classes observed: PE, ES and E. All of these
15 classes have low recurrence in runoff and high recurrence in evaporation due to the
16 seasonality in energy supply.

17 Basins located in Eastern Asia belong to the PE class explained previously on the Tropical
18 Region section. The reasons for this class to be taking place are the same for the temperate
19 region that for the tropical region, the reason for recurrence in precipitation coming from the
20 moisture supply following the Asia Monsoon Pattern.

21 A dominant class in this region is the ES class exemplified by the Mississippi Basin in Figure
22 7. In this type of basin the precipitation pattern is not recurrent without a distinct dry season.
23 Storage is recurrent in these basins as a result of the energy balance characteristics. Due to the
24 limited energy during the winter season, precipitation is directly transferred to storage
25 increase. During summer, the basins in this class are characterized by being water limited, and
26 therefore most of the precipitated water is evaporated allowing for storage to decrease. In
27 these basins there is some influence of snow, however, the amount of snow is not as high as to
28 create a recurrent runoff pattern.

29 Other group in the temperate region is characterized by recurrence in evaporation only as is
30 exemplified by the Danube river basin. In these basins, precipitation has a pattern of low

1 recurrence that transfers to the variables of storage and runoff. As compared to Mississippi,
2 Danube River Basin is not energy limited during summer. This creates a pattern where the
3 anomalies and low recurrence of precipitation also transfer to storage reducing its recurrence.

4

5 **4.4 Subarctic and arctic region (55.0°-90° (N/S))**

6 In the subarctic region we found basins belonging to the QPES, QPE, QES, QE and E classes.
7 As in the temperate region, evaporation is recurrent due to the seasonality of energy supply.
8 All of the basins in this region except Kolyma have recurrent runoff. The runoff pattern is
9 dominated by snowmelt taking place similarly year after year observed in the sudden peak in
10 runoff during spring (Figure 7 h-j).

11 Basins belonging to the QPES and QPE classes have high recurrence in precipitation due to
12 moisture inflow from the ocean(Figure 4s 4 and Figure 5). The recurrence in storage is
13 dependent on the amount of snow. The climatologies of these basins (**Figure 7h-j**) show that
14 storage peaks during the winter months due to the accumulation of snow. Figure 9 shows the
15 climatology of storage in these basins further subdivided into the volume of the different
16 components. Table 3 shows the Component Contribution Ratio (CCR), calculated as (Kim et
17 al., 2009), describing the contribution of each storage variation to the variation of Total
18 Storage. As it can be seen, in these basins the highest contribution takes place from snow. The
19 WaterGAP model in particular has a small groundwater tank which includes only the
20 dynamical part making it small in volume and contribution. Figure 10 and Figure 11 show the
21 snow water equivalent and seasonal precipitation amounts. From these two figures, we can
22 observe that basins with higher snow amount have higher recurrence both in storage and
23 runoff.

24 Basins with not recurrent runoff (QES and QE) are basins located on continental areas
25 experiencing precipitation patterns with no defined dry period. From Figure 9, Figure **10**
26 andFigure **11** we can also conclude that storage is recurrent for these basins depending on the
27 amount of snow; higher SWE and winter precipitation are linked to higher recurrence. For
28 this region, the recurrence in storage and runoff is independent from the recurrence in
29 precipitation but it is dependent on the precipitation and snow amounts.

1 5 Discussion

2 5.1 Characteristics of recurrence measured by AC

3 5.1.1 Recurrence vs. seasonality

4 This section discusses the characteristics of recurrence measured by AC from monthly
5 variables with the lags of 12 month multiples. Firstly we compare the recurrence and
6 seasonality, following the definition of (Walsh and Lawler, 1981):

$$7 \quad SI = \frac{1}{R} \sum_{n=1}^{12} |\bar{x}_n - \bar{R}/12| \quad (13)$$

8 where \bar{x}_n is the mean rainfall of month n and \bar{R} is the annual mean of a hydrological
9 variable. Hence the seasonality measures the degree to which each monthly variable of a
10 regime curve deviates from the overall annual mean. Seasonality is essentially different from
11 the recurrence, which as defined above, measures the degree to which a monthly hydrological
12 variable returns to the same state in subsequent years. Figure 12 displays the relationship
13 between recurrence and seasonality for all the time series in the study, including each variable
14 from every basin. The figure suggests that generally higher seasonal variable tends to have
15 higher recurrence. This is because if a variable has strong seasonality, the influence of the
16 deviation from the climatology has comparatively less impact on the AC. Appendix A shows
17 the distribution of seasonality and recurrence in all variables.

18 Nevertheless, there are exceptions where variables are highly seasonal but not recurrent. For
19 example, Figure 13 shows the monthly average precipitation in Ob and Yenisei. The two
20 basins are located in the same latitudinal region sharing their borders. The climatologies of
21 the both basins are similar with comparable magnitudes at all months. However, the year to
22 year variability in the both basins are different; Ob shows higher variations than Yenisei.
23 Therefore the precipitation in Ob has lower recurrence (0.65) than that in Yenisei(0.88).
24 Similar cases can be observed when comparing the climatologies shown in Figure 7 and the
25 measure of recurrence presented in Figure 6, and in previous work, such as (Kim et al., 2009)
26 where storage climatologies show strong seasonality but the yearly time series does not
27 behave in a recurrent manner.

28 To further explain the difference between recurrence and seasonality, we use Figure 14 to
29 show several examples. Case 1 represents a repeating sinusoidal pattern with small amplitude

1 resulting in low seasonality and high recurrence. Case 2, is a randomly generated series
2 without seasonality and low recurrence. Case 3 and Case 4 are precipitation of Yenisei and
3 Ob with similar seasonality and high recurrence in Yenisei and low recurrence in Ob as
4 discussed above. Case 5 is a sinusoidal pattern repeating the exact same values and show high
5 seasonality but recurrence. Case 6 adds a decreasing trend to the Case 5, but it keeps similar
6 seasonality and recurrence. In summary, seasonality is calculated from the climatology of a
7 variable which results from a long term average, while recurrence measures the year to year
8 variability of the monthly pattern of a variable. Recurrence is an additional feature of
9 temporal patterns of basins providing different information than seasonality.

10 **5.1.2 Recurrence vs. aridity**

11 Recurrence in runoff and storage also has some relation with the aridity of a basin as well as
12 the timings of energy and water availability. These basin characteristics are essential in
13 determining the basins' functionality as they are a descriptor of how much water from
14 precipitation is transferred to evaporation, storage change or runoff and they have been
15 included as classification indices in previous works such as (Jothityangkoon and Sivapalan,
16 2009;Coopersmith et al., 2012;Berghuijs et al., 2014;Coopersmith et al., 2014). **Figure 15**
17 shows the relations between aridity, timing of peaks in precipitation (water supply) and PET
18 (energy supply) with recurrence in runoff and precipitation by region.

19 **Figure 15a** and **b** shows that in humid basins, where the runoff ratio and the storage change
20 ratio are high, runoff and storage follow the patterns in precipitation. Drier basins have low
21 recurrence in runoff (classified as PES, PE, ES or E), essentially due to the high sensitivity of
22 runoff to precipitation under smaller runoff ratios. For example, the case of Amazon and
23 Congo, aforementioned in section 4.1, has difference in recurrence of storage and runoff. For
24 precipitation, both variables have similar relative variations but the total precipitation in
25 Congo is about 70% of the precipitation in Amazon. Additionally, the runoff ratio is smaller
26 in Congo (0.4) than in Amazon (0.45). The physical meaning of this aspect is that there is less
27 water volume in Congo transferring from precipitation into storage fluctuation and runoff
28 generation. Hence, the same anomalies in precipitation have larger impact in Congo than in
29 Amazon. Furthermore, recurrence of storage and runoff depend also on the timing of P and
30 PET peaks. As **Figure 15c** and **d** indicate, the recurrence becomes higher if P and PET are out
31 of phase (>2 months).

5.2 Recurrence measured by FFT intensity and Colwell's Contingency compared to AC

The proposed indices to measure recurrence are lagged AC, FFT intensity and Colwell's Indices. For most of the cases, the basins that show higher AC also have higher values of FFT intensity and Colwell's Predictability. However, it is to be noted that some basins showing lower AC and FFT intensity have high Colwell Predictability, especially in dry conditions. For example, in the arid basins where all the variables are low most of the time except for abrupt peaks, AC and FFT intensity are low, while Colwell's Constancy and Predictability are high. However, these basins are rather low in Colwell's Contingency (Table 4). Contingency measures the degree to which state and time are dependent on each other, measuring the degree to which a particular state takes place at a particular time. For this reason Colwell's Contingency's results are highly consistent with the results of AC and FFT intensity. Colwell's Contingency is not only consistent with the other indices but also adequate for measuring recurrence as defined above. Table 5 shows the classification of each basin using the different metrics.

Figure 16 shows the correlation between AC and FFT intensity and AC and Colwell's Contingency from the WaterGAP model. All indices correlate well although there are particular cases that deviate from the regressions. As mentioned in the methodology section the threshold selected for AC was 0.75. For FFT intensity and Colwell's Contingency measures thresholds of 150 and 0.25 were selected to minimize the number of basins categorized as different classes. Table 5 shows the classification of basins from different metrics.

The FFT procedure is used to represent a time series by fitting a sine and cosine function, therefore the FFT intensity will be higher for variables following a sinusoidal pattern. Figure 17 exemplifies the different periodogram with their respective partial time series and climatology. Figure 17a shows the example of evaporation in Changjiang for which a highly sinusoidal pattern indicates high AC and FFT intensity. Figure 17b shows an example of low recurrence with low AC and FFT intensity. However there are two examples where the FFT intensity value indicates low recurrence while AC indicates high recurrence. First, Figure 17c (Congo-evaporation) shows a bimodal pattern which has a high AC but low FFT intensity, since the peaks in evaporation appear at different frequencies, the intensity at a period of 12 months becomes weaker and other high intensities appear at different frequencies. The second

1 example shown in Figure 17d, takes place with basins in the subarctic region where the
2 highest volume in runoff comes from snowmelt in early spring but the peak in precipitation
3 takes place during summer creating a lump in the recession of the runoff climatology. This
4 second lump reduces the intensity at a period of 12 months and increases other frequencies
5 seen on the periodogram. For both of these cases with deviations from a sinusoidal function
6 AC represents better the concept of recurrence because if the same pattern repeats,
7 independent of the shape of the pattern, AC at lags multiples of 12 will be higher.

8 Colwell's Contingency also has high correlation with AC. However, Colwell's Index is
9 mainly used for qualitative descriptions in ecological sciences but it is adjustable to time
10 series when variable intervals are used as states. Limitations of the use of Colwell's Index for
11 hydrological time series has been extensively discussed by Gan et al. (1991) and include the
12 dependence of the results on the amount of classes selected, and the tendency for higher
13 values in contingency with shorter record lengths. These are the intrinsic limitations of
14 Colwell's Index with the discretization of data.

15 **5.3 Result dependency on model structure**

16 Model differences and uncertainties have been widely discussed in literature about model
17 intercomparison (e.g. Haddeland et al., 2011). Main differences among the models are
18 attributed to evaporation and snow modules, as well as their storage components. Here we
19 briefly discuss how the model structural differences affect the results in the calculation of
20 recurrence. Figure 18 shows the boxplots containing the ranges of recurrence for every
21 variable in all basins by the eight different models.

22 Marginal differences on recurrence are found in most of the tropical humid basins on the
23 QPES class. Larger differences are observed in storage variables in these basins. For the case
24 of Brahmaputra GWAVA and MPI-HM are outliers in the recurrence of storage computing
25 0.03 and 0.55 respectively, while other models range between 0.92.-0.96. Haddeland et al.
26 (2011) highlighted the overestimation of evaporation on this basin due to the use of
27 Thornthwaite evaporation scheme. This leads to higher interannual variations on storage
28 components due to higher evaporation. In the case of GWAVA, the storage series for this
29 basin shows a cyclic increase in storage until it is abruptly decreased to a lower volume. This
30 pattern is only observed in the snow component of storage which is highly overestimated in
31 GWAVA as compared to other models. MATSIRO model has a deep groundwater tank which

1 in general generates less seasonal variation in runoff (Haddeland et al., 2011). This has an
2 effect on the recurrence calculation and in many basins recurrence changes from high on all
3 models to low in MATSIRO.

4 Models in the temperate zone show larger differences mostly in runoff and storage recurrence.
5 This is due to the variety of climatologies that are present in this zone and the presence of
6 snow. Snowfall is treated differently in each GHM, with different thresholds for snowfall, and
7 among all models there are different melting schemes. These differences affect mainly in
8 basins that are around the threshold zone between 0 to 1°C where precipitation is partitioned
9 between snow or rain and melting processes start (Haddeland et al., 2011). Despite these large
10 differences, most models indicate the same class for most basins. In subarctic basins where
11 the influence of snow is much more important the differences are low but the WaterGAP
12 represent the lowest recurrent pattern of all models. This is possibly due to the degree day
13 method. Temporal and spatial variations in snow content are larger in the WaterGAP model
14 decreasing recurrence. However, the relation of storage recurrence and snow amount is kept
15 as basins with higher snow content also exhibit higher recurrence.

16 Finally, arid basins have wide uncertainty due to the differences in partition between
17 evaporation and runoff in each model. MATSIRO is an outlier in having high recurrence in
18 evaporation. When inspecting the time series of storage for these catchments, a marked
19 decreasing trend was found. This can be partially attributed to the deep groundwater tank that
20 keeps water available for evaporation despite the lack of water supply through precipitation.
21 Evaporation follows a seasonal cycle in MATSIRO increasing recurrence.

22 The two models with storage subdivided in more components are WaterGAP and LPJmL
23 featuring mainly a groundwater and a surface storage tank. The groundwater stores water
24 infiltrated from soil moisture deeper underground and drains directly into a lake tank. This
25 groundwater component represents a small volume only simulating a dynamical part of the
26 groundwater that actually exists in a basin. Deep groundwater is not represented by these two
27 models. The surface water storage component includes tanks for lakes, wetlands and rivers
28 channel. This tanks receive as input direct runoff, flow from the groundwater tank and direct
29 precipitation. The outflow from the surface water component is given by discharge onto a
30 downstream cell. Due to the inclusion of a river channel tank, the possibility that our results
31 are affected by the time lag in lengthy river channels exists. However, among the difference in
32 the results shown in Figure 6 and Figure 18 there were no differences that could be

1 attributable to the time lag due to the length of the river. Further analysis should be performed
2 in order to understand the effects of the inclusion of river channel storage in the measures of
3 recurrence.

4 **5.4 Future application of the classification framework**

5 By deriving the classification framework based on recurrence we were able to discuss the
6 interactions among the hydrologic variables affecting their temporal pattern. As one of future
7 applications of the proposed classification, we would like to analyze the impact of projected
8 climate change on hydrologic variables depending on the classes in a mechanistic way. A
9 mechanistic approach to analyze hydrological changes is climate elasticity quantification of
10 runoff (Sankarasubramanian et al., 2001; Yang and Yang, 2011; Vano et al., 2012). We believe
11 that sensitivity studies could be further enhanced with this kind of classification highlighting
12 dominant hydrologic processes, especially by incorporating a storage component.

13 The inclusion of storage and to explain its temporal variations is one of the features of this
14 study. The approach adds to previous studies that have identified storage as an important
15 component for runoff generation (Black, 1997; Sayama et al., 2011) and highlighted its
16 interaction with precipitation and evaporation temporal patterns (Jothityangkoon and
17 Sivapalan, 2009). Our classification remarks how storage is controlled and how it controls
18 runoff in different classes. We identified that for particular classes, the effects of precipitation
19 and potential evaporation transfer more directly to runoff, while in other classes runoff is
20 buffered by storage. Our framework can be utilized as a bench state of basins and analyze the
21 shifts in classes or changes in the temporal variations due to hydrological change, similar to
22 (Coopersmith et al., 2014). For this type of study, EU-WATCH provides excellent datasets
23 for the 20th century and projections into the 21st century to analyze the change in temporal
24 patterns under different conditions.

25 **6 Conclusions**

26 This paper presented a framework of hydrologic classification applicable to large scale river
27 basins based on monthly temporal variations of precipitation, evaporation, storage and runoff.
28 The classification was derived from the concept of hydrological recurrence as a metric
29 defined as the degree to which a monthly hydrological variable returns to the same state in
30 subsequent years. The recurrence was measured using the mean of autocorrelations (AC) with
31 the multiples of 12 up to 60 month lags, the intensity of Fast Fourier Transforms (FFT

1 intensity) and Colwell's Contingency Index. These measures were calculated at global
2 gridded scale (0.5°) and at the 35 largest basins of the world based on the model forcing or
3 output of the EU-WATCH dataset.

4 The recurrence of individual variables is generally different in different latitudinal regions.
5 For the recurrence in precipitation, the seasonality of moisture plays an important role, while
6 for that in evaporation, the effect of seasonality in energy is more dominant. Storage
7 recurrence is more dependent on the seasonality of moisture in the tropics and snow at higher
8 latitudes. Finally, all combinations control the characteristics of the recurrence in runoff.

9 According to our proposed classification, which results in 16 possible classes from the
10 combinations of high or low recurrence of the four variables, only 10 classes are present from
11 our study river basins. In the tropical region, essentially recurrence in runoff and storage is
12 dependent on aridity. Humid basins are highly recurrent in all variables. Drier basins have low
13 recurrence in runoff but storage recurrence is dependent on the timing of the peaks in
14 precipitation and PET.

15 In the temperate region, evaporation is always recurrent due to high seasonality, while
16 precipitation shows low recurrence in this region, due to basins' aridity. In these basins, the
17 timing of peaks between P and PET also influence the recurrence in Q and S.

18 In the subarctic region, evaporation is again highly recurrent due to extreme seasonality.
19 Precipitation is recurrent in areas with oceanic currents influences. Recurrence in storage is in
20 the basins with larger amount of snow, whose melting process dominate the patterns of runoff.
21 As a result, the runoff recurrence is high in this region, while the storage recurrence varies in
22 different areas. Therefore, the river basins are mainly classified into QPES, QPE, QES or QE
23 depending on their combinations.

24 The above results were primarily obtained based on the analysis of AC metric with
25 WaterGAP model output. However, the other two metrics, FFT intensity and Colwell's
26 Contingency, and other eight models also essentially showed consistent results.

27 Overall the presented approach is an attempt to define basin similarity accounting for the
28 temporal patterns of water balance components. River basins in the different classes are likely
29 to behave differently even under the similar changes in climate control. The same framework
30 may be applied to long-term time series data from different sources including GCM future
31 projections. Furthermore, by using long-term time series breaking down into partial time

1 series, the proposed framework may identify a hydrologic regime shift from one class to
2 another, as well as the characteristics of hydrologic sensitivity in different classes. For this
3 kind of study, EU-WATCH provides useful datasets for projecting future hydrologic variables.
4 Finally, there are several limitations that are intrinsic to the classification framework.
5 Although, some of the combinations that were not found are considered not feasible (e.g. only
6 recurrent runoff), there are other classes that may be found if the sample of basins is further
7 extended. The classification also considers no landscape controls in the hydrological
8 processes, effects of land use, and human interactions among other important factors that also
9 dominate and influence the temporal variability of hydrological variables. The framework
10 currently uses the spatial average of large river basins, leaving aside heterogeneity in climatic
11 and geographic characteristics. Downscaling to smaller sub-basins can bring insight not only
12 in the behavior at smaller scale but also on how different sub-basins add up to create a general
13 pattern in the large scale basins. Even though the presented method is not a definite and only
14 classification framework, the analysis comparing different classes provide useful insights into
15 the functions of large river basins in the world.

16 **Appendix A: Spatial comparison of recurrence and seasonality**

17 Figure A1 shows the recurrence and seasonality for each variable in each basin. Precipitation
18 shows high recurrence in most of South America, most of Africa, South East Asia, and the
19 majority of basins in Eastern Asia as displayed in Figure A1a. In Figure A1b, it can be noted
20 that seasonality is not that strong for the majority of the basins, aside from a few basins in
21 Africa and Ganges in South East Asia. Figure A1c and A1d show the recurrence and
22 seasonality of evaporation respectively. Evaporation is the most recurrent variable. However,
23 the seasonality is low except for the Sub-arctic basins. Runoff is mostly recurrent in some
24 basins of the Sub-arctic region and some basins in the tropics and South East Asia (Figure
25 A1e), whereas it does not display seasonality except for the Ganges and Lena basins (Figure
26 A1f). Finally, Storage is a recurrent variable in some basins of South America, Africa, and
27 Asia as can be seen from Figure A1g. In the case of storage is does not display significant
28 seasonality around the world (Figure A1h).

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3

1 **References**

- 2 Alcamo, J., DÖLL, P., Henrichs, T., Kaspar, F., Lehner, B., RÖSCH, T., and Siebert, S.:
3 Development and testing of the WaterGAP 2 global model of water use and availability,
4 *Hydrological Sciences Journal*, 48, 317-337, 2003.
- 5 Ali, G., Oswald, C. J., Spence, C., Cammeraat, E. L., McGuire, K. J., Meixner, T., and
6 Reaney, S. M.: Towards a unified threshold - based hydrological theory: necessary
7 components and recurring challenges, *Hydrological Processes*, 27, 313-318, 2013.
- 8 Balsamo, G., Beljaars, A., Scipal, K., Viterbo, P., van den Hurk, B., Hirschi, M., and Betts, A.
9 K.: A revised hydrology for the ECMWF model: Verification from field site to terrestrial
10 water storage and impact in the Integrated Forecast System, *Journal of hydrometeorology*, 10,
11 623-643, 2009.
- 12 Berghuijs, W. R., Sivapalan, M., Woods, R. A., and Savenije, H. H. G.: Patterns of similarity
13 of seasonal water balances: A window into streamflow variability over a range of time scales,
14 *Water Resources Research*, 50, 5638-5661, 10.1002/2014WR015692, 2014.
- 15 Black, P. E.: Watershed functions, *JAWRA Journal of the American Water Resources*
16 *Association*, 33, 1-11, 1997.
- 17 Bondeau, A., Smith, P. C., Zaehle, S., Schaphoff, S., Lucht, W., Cramer, W., Gerten, D.,
18 LOTZE - CAMPEN, H., Müller, C., and Reichstein, M.: Modelling the role of agriculture for
19 the 20th century global terrestrial carbon balance, *Global Change Biology*, 13, 679-706, 2007.
- 20 Cheng, L., Yaeger, M., Viglione, A., Coopersmith, E., Ye, S., and Sivapalan, M.: Exploring
21 the physical controls of regional patterns of flow duration curves--Part 1: Insights from
22 statistical analyses, *Hydrology & Earth System Sciences Discussions*, 9, 2012.
- 23 Colwell, R. K.: Predictability, constancy, and contingency of periodic phenomena, *Ecology*,
24 1148-1153, 1974.
- 25 Coopersmith, E., Yaeger, M., Ye, S., Cheng, L., and Sivapalan, M.: Exploring the physical
26 controls of regional patterns of flow duration curves--Part 3: A catchment classification
27 system based on regime curve indicators, *Hydrology & Earth System Sciences*, 16, 2012.
- 28 Coopersmith, E., Minsker, B., and Sivapalan, M.: Patterns of regional hydroclimatic shifts:
29 An analysis of changing hydrologic regimes, *Water Resources Research*, 50, 1960-1983, 2014.
- 30 Cox, P., Betts, R., Bunton, C., Essery, R., Rowntree, P., and Smith, J.: The impact of new
31 land surface physics on the GCM simulation of climate and climate sensitivity, *Climate*
32 *Dynamics*, 15, 183-203, 1999.
- 33 Delworth, T., and Manabe, S.: The influence of soil wetness on near-surface atmospheric
34 variability, *Journal of Climate*, 2, 1447-1462, 1989.
- 35 Delworth, T. L., and Manabe, S.: The influence of potential evaporation on the variabilities of
36 simulated soil wetness and climate, *Journal of Climate*, 1, 523-547, 1988.
- 37 Emori, S., Abe, K., Numaguti, A., and Mitsumoto, S.: Sensitivity of a simulated water cycle
38 to a runoff process with atmospheric feedback, *Journal of the Meteorological Society of Japan*,
39 74, 815-832, 1996.

- 1 Essery, R., Best, M., Betts, R., Cox, P. M., and Taylor, C. M.: Explicit representation of
2 subgrid heterogeneity in a GCM land surface scheme, *Journal of Hydrometeorology*, 4, 530-
3 543, 2003.
- 4 Fu, C., Chen, J., Jiang, H., and Dong, L.: Threshold behavior in a fissured granitic catchment
5 in southern China: 1. Analysis of field monitoring results, *Water Resources Research*, 2013.
- 6 Gan, K., McMahon, T., and Finlayson, B.: Analysis of periodicity in streamflow and rainfall
7 data by Colwell's indices, *Journal of hydrology*, 123, 105-118, 1991.
- 8 Graham, C. B., Woods, R. A., and McDonnell, J. J.: Hillslope threshold response to
9 rainfall:(1) A field based forensic approach, *Journal of Hydrology*, 393, 65-76, 2010.
- 10 Gudmundsson, L., Tallaksen, L. M., Stahl, K., Clark, D. B., Dumont, E., Hagemann, S.,
11 Bertrand, N., Gerten, D., Heinke, J., and Hanasaki, N.: Comparing large-scale hydrological
12 model simulations to observed runoff percentiles in Europe, *Journal of Hydrometeorology*, 13,
13 604-620, 2012a.
- 14 Gudmundsson, L., Wagener, T., Tallaksen, L., and Engeland, K.: Evaluation of nine large -
15 scale hydrological models with respect to the seasonal runoff climatology in Europe, *Water
16 Resources Research*, 48, 2012b.
- 17 Haddeland, I., Clark, D. B., Franssen, W., Ludwig, F., Voß, F., Arnell, N. W., Bertrand, N.,
18 Best, M., Folwell, S., and Gerten, D.: Multimodel estimate of the global terrestrial water
19 balance: setup and first results, *Journal of Hydrometeorology*, 12, 869-884, 2011.
- 20 Hagemann, S., and Dümenil, L.: A parametrization of the lateral waterflow for the global
21 scale, *Climate Dynamics*, 14, 17-31, 1997.
- 22 Hagemann, S., and Gates, L. D.: Improving a subgrid runoff parameterization scheme for
23 climate models by the use of high resolution data derived from satellite observations, *Climate
24 Dynamics*, 21, 349-359, 2003.
- 25 Hanasaki, N., Kanae, S., Oki, T., Masuda, K., Motoya, K., Shirakawa, N., Shen, Y., and
26 Tanaka, K.: An integrated model for the assessment of global water resources—Part 1: Model
27 description and input meteorological forcing, *Hydrology and Earth System Sciences*, 12,
28 1007-1025, 2008.
- 29 Jothityangkoon, C., and Sivapalan, M.: Framework for exploration of climatic and landscape
30 controls on catchment water balance, with emphasis on inter-annual variability, *Journal of
31 Hydrology*, 371, 154-168, 2009.
- 32 Kim, H., Yeh, P. J. F., Oki, T., and Kanae, S.: Role of rivers in the seasonal variations of
33 terrestrial water storage over global basins, *Geophysical Research Letters*, 36, 2009.
- 34 Koirala, S., Yeh, P. J. F., Hirabayashi, Y., Kanae, S., and Oki, T.: Global - scale land surface
35 hydrologic modeling with the representation of water table dynamics, *Journal of Geophysical
36 Research: Atmospheres*, 2014.
- 37 Masuda, K., Hashimoto, Y., Matsuyama, H., and Oki, T.: Seasonal cycle of water storage in
38 major river basins of the world, *Geophysical research letters*, 28, 3215-3218, 2001.
- 39 McGlynn, B., Nippgen, F., Jencso, K., and Emanuel, R.: Spatial and temporal patterns of
40 hydrologic connectivity between upland landscapes and stream networks, *AGU Fall Meeting
41 Abstracts*, 2013, 03,

- 1 McNamara, J. P., Tetzlaff, D., Bishop, K., Soulsby, C., Seyfried, M., Peters, N. E., Aulenbach,
2 B. T., and Hooper, R.: Storage as a metric of catchment comparison, *Hydrological Processes*,
3 25, 3364-3371, 2011.
- 4 Meigh, J., McKenzie, A., and Sene, K.: A grid-based approach to water scarcity estimates for
5 eastern and southern Africa, *Water Resources Management*, 13, 85-115, 1999.
- 6 Miller, G.: Ballooning in *Geolycosa turricola* (Treat) and *Geolycosa patellonigra* Wallace:
7 high dispersal frequencies in stable habitats, *Canadian journal of zoology*, 62, 2110-2111,
8 1984.
- 9 Milly, P., and Dunne, K.: Macroscale water fluxes 2. Water and energy supply control of their
10 interannual variability, *Water Resources Research*, 38, 24-21-24-29, 2002.
- 11 Milly, P. C. D., and Wetherald, R. T.: Macroscale water fluxes 3. Effects of land processes on
12 variability of monthly river discharge, *Water Resources Research*, 38, 1235,
13 10.1029/2001WR000761, 2002.
- 14 Riddell, B. E., and Leggett, W. C.: Evidence of an adaptive basis for geographic variation in
15 body morphology and time of downstream migration of juvenile Atlantic salmon (*Salmo*
16 *salar*), *Canadian Journal of Fisheries and Aquatic Sciences*, 38, 308-320, 1981.
- 17 Rost, S., Gerten, D., Bondeau, A., Lucht, W., Rohwer, J., and Schaphoff, S.: Agricultural
18 green and blue water consumption and its influence on the global water system, *Water*
19 *Resources Research*, 44, 2008.
- 20 Sankarasubramanian, A., Vogel, R. M., and Limbrunner, J. F.: Climate elasticity of
21 streamflow in the United States, *Water Resources Research*, 37, 1771-1781, 2001.
- 22 Sayama, T., and McDonnell, J. J.: A new time - space accounting scheme to predict stream
23 water residence time and hydrograph source components at the watershed scale, *Water*
24 *resources research*, 45, 2009.
- 25 Sayama, T., McDonnell, J. J., Dhakal, A., and Sullivan, K.: How much water can a watershed
26 store?, *Hydrological Processes*, 25, 3899-3908, 2011.
- 27 Shaw, D. A., Vanderkamp, G., Conly, F. M., Pietroniro, A., and Martz, L.: The Fill-Spill
28 Hydrology of Prairie Wetland Complexes during Drought and Deluge, *Hydrological*
29 *Processes*, 26, 3147-3156, 2012.
- 30 Sidle, R. C., Tsuboyama, Y., Noguchi, S., Hosoda, I., Fujieda, M., and Shimizu, T.:
31 Stormflow generation in steep forested headwaters: a linked hydrogeomorphic paradigm,
32 *Hydrological Processes*, 14, 369-385, 2000.
- 33 Spence, C., and Woo, M.-k.: Hydrology of subarctic Canadian shield: soil-filled valleys,
34 *Journal of Hydrology*, 279, 151-166, 2003.
- 35 Spence, C.: On the relation between dynamic storage and runoff: A discussion on thresholds,
36 efficiency, and function, *Water Resources Research*, 43, 2007.
- 37 Spence, C., Guan, X., Phillips, R., Hedstrom, N., Granger, R., and Reid, B.: Storage dynamics
38 and streamflow in a catchment with a variable contributing area, *Hydrological Processes*, 24,
39 2209-2221, 2010.
- 40 Tague, C., and Peng, H.: The sensitivity of forest water use to the timing of precipitation and
41 snowmelt recharge in the California Sierra: Implications for a warming climate, *Journal of*
42 *Geophysical Research: Biogeosciences*, 118, 875-887, 2013.

- 1 Takata, K., Emori, S., and Watanabe, T.: Development of the minimal advanced treatments of
2 surface interaction and runoff, *Global and Planetary Change*, 38, 209-222, 2003.
- 3 Tromp - van Meerveld, H., and McDonnell, J.: Threshold relations in subsurface stormflow:
4 2. The fill and spill hypothesis, *Water Resources Research*, 42, 2006.
- 5 Vannote, R. L., and Sweeney, B. W.: Geographic analysis of thermal equilibria: a conceptual
6 model for evaluating the effect of natural and modified thermal regimes on aquatic insect
7 communities, *American naturalist*, 667-695, 1980.
- 8 Vano, J. A., Das, T., and Lettenmaier, D. P.: Hydrologic Sensitivities of Colorado River
9 Runoff to Changes in Precipitation and Temperature*, *Journal of Hydrometeorology*, 13,
10 2012.
- 11 Wagener, T., Sivapalan, M., Troch, P., and Woods, R.: Catchment classification and
12 hydrologic similarity, *Geography Compass*, 1, 901-931, 2007.
- 13 Walsh, R., and Lawler, D.: Rainfall seasonality: description, spatial patterns and change
14 through time, *Weather*, 36, 201-208, 1981.
- 15 Webb, M., Thoms, M., and Reid, M.: Determining the ecohydrological character of aquatic
16 refugia in a dryland river system: the importance of temporal scale, *Ecohydrology &
17 Hydrobiology*, 12, 21-33, 2012.
- 18 Weedon, G., Gomes, S., Viterbo, P., Österle, H., Adam, J., Bellouin, N., Boucher, O., and
19 Best, M.: The WATCH FORCING DATA 1958-2001: A Meteorological forcing dataset for
20 land surface-and hydrological-models, *WATCH Technical Report*, 22, 44, 2010.
- 21 Weedon, G., Gomes, S., Viterbo, P., Shuttleworth, W., Blyth, E., Österle, H., Adam, J.,
22 Bellouin, N., Boucher, O., and Best, M.: Creation of the WATCH Forcing Data and its use to
23 assess global and regional reference crop evaporation over land during the twentieth century,
24 *Journal of Hydrometeorology*, 12, 823-848, 2011.
- 25 Weingartner, R., Bloeschl, G., Hannah, D. M., Marks, D. G., Parajka, J., Pearson, C. S.,
26 Rogger, M., Salinas, J. L., Sauquet, E., Srikanthan, R., Thompson, S. E., and Viglione, A.:
27 Prediction of seasonal runoff in ungauged basins, in: *Runoff Prediction in Ungauged Basins:
28 Synthesis across processes, places and scales*, edited by: Bloeschl, G., Sivapalan, M.,
29 Wagener, T., Viglione, A., and Savenije, H., Cambridge University Press, Cambridge, UK,
30 102-134, 2013.
- 31 Weiskel, P., Wolock, D., Zarriello, P., Vogel, R., Levin, S., and Lent, R.: Hydroclimatic
32 regimes: a distributed water-balance framework for hydrologic assessment and classification,
33 *Hydrology and Earth System Sciences Discussions*, 11, 2933-2965, 2014.
- 34 Yaeger, M., Coopersmith, E., Ye, S., Cheng, L., Viglione, A., and Sivapalan, M.: Exploring
35 the physical controls of regional patterns of flow duration curves--Part 4: A synthesis of
36 empirical analysis, process modeling and catchment classification, *Hydrology & Earth
37 System Sciences Discussions*, 9, 2012.
- 38 Yang, H., and Yang, D.: Derivation of climate elasticity of runoff to assess the effects of
39 climate change on annual runoff, *Water Resources Research*, 47, 2011.
- 40 Ye, S., Yaeger, M., Coopersmith, E., Cheng, L., and Sivapalan, M.: Exploring the physical
41 controls of regional patterns of flow duration curves--Part 2: Role of seasonality, the regime
42 curve, and associated process controls, *Hydrology & Earth System Sciences*, 16, 2012.

1 Zhang, Y., Arthington, A., Bunn, S., Mackay, S., Xia, J., and Kennard, M.: Classification of
2 flow regimes for environmental flow assessment in regulated rivers: the Huai River Basin,
3 China, *River Research and Applications*, 28, 989-1005, 2012.
4

1 Table 1. Overview of models included in this research and their characteristics. Adapted from
 2 (Haddeland et al., 2011;Gudmundsson et al., 2012a;Gudmundsson et al., 2012b). Model
 3 names in bold are considered as LSMs. Precipitation input is either provided as total
 4 Precipitation (P) or as rainfall (R) and snowfall (S) separately. Storage can be handled in
 5 models as ground moisture (GM), soil moisture (SM), surface storage (SS) and snow water
 6 equivalent (SWE).

Model Name	Precipitation input	Storage components	Provided PET	Reference
GWAVA	P	GM, SM, SWE	No	Meigh et al. (1999)
H08	R, S	SM, SWE	Yes	Hanasaki et al. (2008)
HTESSEL	R, S	SM, SWE	No	Balsamo et al. (2009)
JULES	R, S	SM, SWE	No	Cox et al. (1999);(Essery et al., 2003)
LPJmL	P	GM, SM, SS, SWE	Yes	Bondeau et al. (2007);(Rost et al., 2008)
MATSIRO	R, S	SM, SWE	No	(Takata et al., 2003;Koirala et al., 2014)
MPI-HM	P	SM, SWE	Yes	(Hagemann and Dümenil, 1997;Hagemann and Gates, 2003)
WaterGAP	P	GM, SM, SS, SWE	Yes	(Alcamo et al., 2003)

1 Table 2. Summary of class characteristics.

Class	Basins	Region	Characteristics	Observations
QPES	Amazon, Brahmaputra, Changjiang, Ganges, Mekong, Niger, Nile, Yenisei	Tropics, Subtropics (Asian Monsoon) and Subarctic (Central Eurasia)	Tropical and Subtropical Humid Basins Snow dominated basins with high recurrence in precipitation and high precipitation during winter	Variables follow the same pattern as precipitation fills storage and storage further supplies runoff and evaporation in an equally recurrent pattern
QPE	Lena, Mackenzie	Subarctic (West Eurasia and Central North America)	Snow dominated basins with small precipitation in winter	Precipitation is recurrent but concentrated in summer, winter snow volume is not high enough to make storage recurrent. However the amount of snow does generate a recurrent pattern in runoff
QPS	Orinoco	Tropics	Equatorial basin with highly constant evaporation pattern	Precipitation, Storage and Runoff have a recurrent pattern but the constant high water and low energy supplies result in a low recurrence pattern in evaporation
QES	Ob, Volga	Subarctic (Central Asia)	Snow dominated basins with low recurrence in precipitation, water limited in summer and high precipitation during winter	Important amount of precipitation during winter creates a large snow volume which creates a recurrent runoff pattern regardless of the low recurrence in precipitation
QE	Yukon	Subarctic (Alaska)	Snow dominated basin with low recurrence in precipitation, water limited in summer and rather low precipitation in winter	Low precipitation in winter does not allow a recurrent pattern in storage because of low snow volume, however runoff is recurrent
PES	Tocantins, Zambezi	Tropics (Southern South America and Africa), Temperate (East Eurasian Continent affected by Oceanic atmospheric flow)	Tropical humid basins with PET peaks at different time as P	Desynchronization of the Precipitation and PET cycles allows for filling of storage and also emptying during rainy and dry seasons respectively. Runoff is only generated for extreme precipitation due to lack of saturation in storage
PE	Amur, Congo, Huang He, Okavango, Plata		Basins with high evaporative index (0.7–0.8) with PET peaking at the same time as P	Runoff generation and storage change are highly limited by evaporation due to the synchronization of precipitation and PET storage changes
ES	Columbia, Euphrates, Mississippi, Syr Darya		Mid-latitude basins with important amount of precipitation in winter, some influence of snow, and water limited in summer	Storage increases during winter regardless of the precipitation pattern, however snow volume is not such as to pass the pattern onto runoff
E	Danube, Indus, Kolyma, Nelson, Sao Francisco, St. Lawrence	Temperate (North America, Europe and Central Asia) South America	Winter storage dominated basins due to the presence of snow with low storage fluctuations Tropical basin with no recurrent patterns in precipitation but water availability restrained to one particular season only	Irregular or low precipitation patterns transmit directly on to other variables, but evaporation is recurrent due to the seasonal availability of energy
L	Colorado, Darling, Grande, Orange	Subtropics (Desert Belt)	Arid basins	Irregular precipitation transmits to other variables as isolated events are the only water available for any hydrological process to take place

1 Table 3. Component Contribution Ratio (CCR) for basins located in the subarctic region. The
2 CCR is calculated as (Kim et al., 2009).

Basin	GroundMoist	SoilMoist	SurfStor	SWE
Yenisei	0.056	0.095	0.247	0.602
Lena	0.021	0.076	0.391	0.512
Mackenzie	0.077	0.135	0.109	0.679
Ob	0.077	0.225	0.112	0.586
Volga	0.083	0.271	0.145	0.501
Yukon	0.059	0.052	0.312	0.577
Kolyma	0.011	0.034	0.322	0.633

3

4

1 Table 4. Results of Colwell's Indices (Constancy (C), Contingency (M) and Predictability (P)
 2 for all variables in arid basins. Constancy has high values due to variables being constantly
 3 low increasing the total predictability index.

4

Basin	Variable	C	M	P
Colorado	P	0.303	0.110	0.413
	E	0.284	0.265	0.549
	Q	0.433	0.115	0.548
	S	0.302	0.209	0.511
Darling	P	0.300	0.073	0.373
	E	0.297	0.209	0.506
	Q	0.380	0.179	0.559
	S	0.291	0.170	0.461
Grande	P	0.320	0.173	0.493
	E	0.320	0.207	0.527
	Q	0.432	0.089	0.521
	S	0.297	0.077	0.374
Orange	P	0.339	0.176	0.515
	E	0.311	0.202	0.513
	Q	0.507	0.067	0.574
	S	0.365	0.077	0.442

1 Table 5. Classification using different metrics, AC (AC), Colwell's Contingency (M) and Fast
 2 Fourier Transform intensity (FFT intensity).

3

Basin	AC	M	FFTintensity
Amazon	QPES	QPES	QPES
Amur	QPE	QPE	QPE
Brahmaputra	QPES	QPES	QPES
Changjiang	QPES	QPES	QPES
Colorado	L	E	S
Columbia	ES	ES	ES
Congo	PE	PE	L
Danube	E	E	ES
Darling	L	L	L
Euphrates	ES	PES	QPES
Ganges	QPES	QPES	PES
Grande	L	L	L
Huanghe	PE	PE	PE
Indus	E	E	L
Kolyma	E	QE	E
Lena	QPE	QPE	PE
Mackenzie	QPE	QPE	PES
Mekong	QPES	QPES	QPES
Mississippi	ES	ES	ES
Nelson	E	E	PES
Niger	QPES	QPES	QPES
Nile	QPES	QPES	QPES
Ob	QES	QES	ES
Okavango	PE	PE	PE
Orange	L	L	L
Orinoco	QPS	QPS	QPES
Plata	PE	PE	PES
Sao Francisco	E	E	PES
St. Lawrence	E	E	ES
Syr Darya	ES	ES	ES
Tocantins	PES	PES	QPES
Volga	QES	QES	ES
Yenisei	QPES	QPES	PES
Yukon	QE	QE	QE
Zambezi	PES	PES	PES

1 Figure 1. Schematic representation of different levels of recurrence in runoff (Q) time series from.

2

3 Figure 2. Location of the basins included in the analysis with an assigned identification
4 number. The latitude reference lines identify the latitudes that divide each of the regions
5 geographically separating the basins.

6

7 Figure 3 Hydrological classification tree. Color codes indicate the colors used in further maps to identify
8 the classes to which basins belong. Dashed lines indicate paths into classes that were not found upon the
9 studied basins.

10

11 Figure 4. Recurrence in main hydrological variables at global scale: (a) Precipitation, (b) Evaporation, (c)
12 Storage and (d) Runoff. The map identifies the areas with lowest recurrence (<0.5), low recurrence (0.5 -
13 0.75) and High recurrence (0.75 $<$). Reference latitude lines identify the divisions in latitudinal regions
14 where particular conditions and similarities were found to exist.

15

16 Figure 5. Basin location map with identification by class. A threshold for defining high recurrence or low
17 recurrence was set at 0.75 . Latitude regions were defined between the reference lines shown on the map for
18 both hemispheres delimiting the Tropical Region between (0.0° - 23.5°), Subtropical Region between (23.5° -
19 35.0°), Temperate Region (35.0° - 55.0°), and Subarctic and Arctic Region (55.0° $<$).

20

21 Figure 6. Radar charts depicting the results of recurrence for each variable in each individual basin. Results
22 from the WaterGAP model are highlighted in red, the model mean is shown as a solid black line, the
23 interquartile is shaded in grey, and the max. and min. values are shown with a dashed black line.

24

25 Figure 7. Variable climatologies for selected basins for each class and region. The charts present a
26 particular basin for each of the 10 classes found sorted by region. Comparable axis of precipitation,
27 evaporation, runoff and potential evaporation are shown on the left vertical axis and storage axis is shown
28 on the right vertical axis.

29

30

1 Figure 8. Monthly time series of selected basins in the tropics from each class: (a) Amazon – QPES, (b)
2 Orinoco – QPS, (c) Zambezi PES, (d) Congo - PE. The graphs exemplify time series with high or low
3 recurrence depending on the classification. The averaged AC coefficient is provided in the top right corner
4 of each graph.

5

6 Figure 9. Climatology of storage and the various storage components for subarctic basins.

7

8 Figure 10. Snow water equivalent seasonality of sub-arctic basins.

9

10 Figure 11. Seasonal precipitation climatology of sub-arctic basins.

11

12 Figure 12. Relationship between recurrence and seasonality from all of the time series corresponding to
13 each variable in each basin.

14

15 Figure 13. Seasonal climatologies of precipitation in Yenisei and Ob river basins, a) long term mean, b)
16 and c) 23 years precipitation in Yenisei and Ob river basins respectively. b) and c) show the minimum,
17 maximum quartiles and mean for each month.

18

19 Figure 14 Schematic time serieses representing different levels of recurrence, variability and seasonality.

20

21 Figure 15 Relation of Aridity and Timing of peaks and recurrence in runoff. a) Timing of P and PET with
22 recurrence in runoff, b) relation of timing of peaks in P and PET peaks and recurrence in storage, c) relation
23 of aridity and recurrence in runoff., and d) relation between aridity and recurrence in storage.

24

25 Figure 16. Comparison of AC with Colwell's Contingency (M), and FFT intensity.

26

27

1 Figure 17. Examples of variables with different results in FFT intensity. (a) Changjiang's evaporation (b)
2 Runoff in Yenisei (c) Precipitation in Congo (d) Storage in Orange

3

4 Figure 18. Model differences. Box plots show the recurrence measure for each variable in each basin
5 displaying an interquartile uncertainty band, WaterGAP marked by the red spot, the mean highlighted by
6 the black mark and the maximum and minimum values.

7

8 Figure A1. a) Recurrence of Precipitation, b) Seasonality of Precipitation, c) Recurrence of Evaporation, d)
9 Seasonality of Evaporation, e) Recurrence of Runoff, f) Seasonality of Runoff, g) Recurrence of Storage, h)
10 Seasonality of Storage. Recurrence and Seasonality use the same color scale.