1 Complex networks for streamflow dynamics

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3 B. Sivakumar^{1,2} and F. M. Woldemeskel¹

4 [1]{School of Civil and Environmental Engineering, The University of New South Wales,

5 Sydney, Australia}

6 [2]{Department of Land, Air and Water Resources, University of California, Davis, USA}

7 Correspondence to: B. Sivakumar (s.bellie@unsw.edu.au)

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9 Abstract

10 Streamflow modeling is an enormously challenging problem, due to the complex and 11 nonlinear interactions between climate inputs and landscape characteristics over a wide range 12 of spatial and temporal scales. A basic idea in streamflow studies is to establish connections 13 that generally exist, but attempts to identify such connections are largely dictated by the 14 problem at hand and the system components in place. While numerous approaches have been 15 proposed in the literature, our understanding of these connections remains far from adequate. The present study introduces the theory of networks, and in particular complex networks, to 16 17 examine the connections in streamflow dynamics, with a particular focus on spatial 18 connections. Monthly streamflow data observed over a period of 52 years from a large 19 network of 639 monitoring stations in the contiguous United States are studied. The 20 connections in this streamflow network are examined primarily using the concept of 21 clustering coefficient, which is a measure of local density and quantifies the network's 22 tendency to cluster. The clustering coefficient analysis is performed with several different 23 threshold levels, which are based on correlations in streamflow data between the stations. The 24 clustering coefficient values of the 639 stations are used to obtain important information 25 about the connections in the network and their extent, similarity and differences between 26 stations/regions, and the influence of thresholds. The relationship of the clustering coefficient 27 with the number of links/actual links in the network and the number of neighbors is also addressed. The results clearly indicate the usefulness of the network-based approach for 28 29 examining connections in streamflow, with important implications for interpolation and 30 extrapolation, classification of catchments, and predictions in ungaged basins.

1 **1 Introduction**

2 Streamflow forms an important input for a wide range of applications in hydrology, water resources, environment, and ecosystem. However, its estimation or prediction is an 3 4 enormously challenging problem, since streamflow arises as a result of complex and 5 nonlinear interactions between climate inputs (external factors) and landscape characteristics 6 (internal factors) that occur over a wide range of spatial and temporal scales. For instance, 7 streamflow is governed not only by the distribution of rainfall (in both space and time) but 8 also by the nature and state of the catchment (e.g. topography, vegetation, soil, geology); see 9 Beven (2006) for a compilation of, and stimulating insight into, some early 'benchmark' studies (1933-1984) on streamflow generation processes. Attempts to monitor, model, and 10 predict streamflow have been a central topic in hydrology during the last century or so; see, 11 for example, Salas et al. (1995), Grayson and Blöschl (2000), Duan et al. (2003), Mishra and 12 13 Coulibaly (2009), and Hrachowitz et al. (2013) for comprehensive accounts on streamflow monitoring, modeling, and prediction. 14

15 Despite their efforts and contributions, studies on streamflow have and continue to encounter 16 at least two major challenges: (1) determination of the locations, number, and density of streamflow gaging stations for monitoring data and representation of process variability; and 17 18 (2) identification of the appropriate scientific concepts and mathematical techniques/models 19 for a more solid conceptual understanding of the catchment systems, proper analysis of the 20 data, and reliable interpretation of the outcomes. It is true that recent developments in measurement technology, computational power, and mathematical sophistication have 21 22 generally played an important role in overcoming these challenges to a certain extent. It can 23 also not be denied, however, that the same developments have, at times, played an indirect 24 role in creating imbalance and hindering true progress, as they have contributed to the perhaps unnecessary complexification in models (rather than simplification), highly specialized 25 conceptual notions that are often suitable only for specific situations (rather than 26 generalization frameworks that suit all conditions), difficult-to-bridge gaps between theory 27 28 and practice, and lack of communication among researchers as well as between researchers 29 and practitioners; see, for example, Perrin et al. (2001), Beven (2002), Kirchner (2006), Sivakumar (2008), and Young and Ratto (2009) for some details. 30

31 It is important to recognize that a fundamental idea in streamflow (and other hydrologic) 32 studies is to establish connections that generally exist between the different elements or items

(known or assumed) of the underlying system. Depending upon the situation (e.g. catchment, 1 2 purpose, problem), these elements include hydroclimatic variables, catchment characteristics, model parameters, and others (and their combinations), and their connections are often 3 different with respect to space, time, and space-time. Unraveling the nature and extent of 4 5 these connections has always been a great challenge, not to mention the challenge in the identification of all the relevant elements in the first place. Thus far, a plethora of concepts 6 7 and methods has been proposed and applied for studying the connections associated with 8 streamflow, including those based on time, distance, correlation, variability, scale, patterns, 9 and many other properties/measures as well as their combinations and variants, in both single-10 variable and multi-variable perspectives; see, for example, Gupta et al. (1986), Salas et al. 11 (1995), Grayson and Blöschl (2000), Yang et al. (2004), Archfield and Vogel (2010), and Li 12 et al. (2012) for some details. Despite the progress made through these concepts and methods, 13 our understanding of the connections in streamflow is still far from adequate.

14 In view of this, there is indeed a need to greatly advance our studies on streamflow 15 connections. Some important current and foreseeable future problems, including our everincreasing demands for water, the potential impacts of climate change on water security and 16 17 hydroclimatic disasters, and the numerous issues associated with the management of our 18 environment and ecosystems, further reflect the urgency to this need. A greater understanding 19 of streamflow connections will also enhance our recent and current efforts in the estimation of 20 data at ungaged locations (e.g. predictions in ungaged basins – PUB) (see Hrachowitz et al., 21 2013) and development of a generalization framework for hydrologic modeling (e.g. 22 catchment classification) (see Sivakumar et al., 2014), among others. The question, however, 23 remains on the identification of a suitable theory that can help bring advancement to studies 24 on streamflow connections. In this regard, recent developments in the field of complex 25 systems science can offer some crucial clues. The present study introduces the theory of complex networks, or simply networks, for studying connections in streamflow. In particular, 26 27 the study focuses on spatial connections in streamflow.

The origin of the concept of networks can be traced back to the works of Leonhard Euler, during the first half of the eighteenth century, on the Seven Bridges of Königsberg (Euler, 1741), which laid the foundations of what would become popularly known as *graph theory*. Graph theory witnessed several important theoretical developments in the nineteeth century, including *topology* (originally introduced as *topologie* in German) (Listing, 1848) and *trees* (Cayley, 1857). Further significant advances were made during the twentieth century,
 especially with the development of *random graph theory* by Erdös and Rényi (Erdös and
 Rényi, 1960). The concepts of graph theory, and random graph theory in particular, have
 found a wide variety of applications in numerous fields, including linguistics, physics,
 chemistry, biology, sociology, engineering, economics, and ecology; see, for example, Berge
 (1962), Bondy and Murty (1976), and Bollobás (1998) for extensive reviews.

7 Despite the above-mentioned developments and applications, studies on graph theory, 8 including random graph theory, had some major deficiencies. First, the studies largely 9 focused on networks that are regular, simple, small, and static. As a result, they are generally unsuitable for examining real networks, as such networks are often highly irregular, complex, 10 11 large, and dynamically evolving in time. Second, even while examining complex and large-12 scale networks, they assumed that such networks are wired randomly together (Erdös and 13 Rényi, 1960). Such an assumption, however, is not necessarily valid for real networks, since 14 order and determinism are inherent in real systems and networks. Indeed, real networks are 15 neither completely ordered nor completely random, but generally exhibit important properties of both. These observations motivated a renewed and fresh look of random graph theory 16 17 towards the end of the last century (e.g. Watts and Strogatz, 1998; Barabási and Albert, 1999), 18 and gave birth to a new movement of interest and research in studying real and complex 19 networks, under the umbrella of the new science of networks. They also led to new 20 discoveries about complex networks, including small-world networks (Watts and Strogatz, 21 1998), scale-free networks (Barabási and Albert, 1999), network motifs (Milo et al., 2002), as 22 well as other notable advances, such as a new method for identifying *community structure* 23 (Girvan and Newman, 2002). Since then, the science of networks has found applications in 24 many different fields, including natural and physical sciences, social sciences, medical 25 sciences, economics, and engineering and technology (e.g. Albert et al., 1999; Bouchaud and Mézard, 2000; Newman, 2001; Liljeros et al., 2001; Tsonis and Roebber, 2004; Davis et al., 26 27 2013). In hydrology, applications of networks are just starting to emerge, and so far include river networks, virtual water trade, precipitation, and agricultural pollution due to 28 29 international trade, among others (Rinaldo et al., 2006; Suweis et al., 2011; Dalin et al., 2012; Boers et al., 2013; Scarsoglio et al., 2013). In a very recent study, Sivakumar (2014) has 30 31 argued that networks can be useful for studying all types of connections in hydrology and, 32 hence, can provide a generic theory for hydrology.

With the encouraging results reported by the above studies, the present study explores the 1 2 usefulness of the theory of networks for studying connections in streamflow, especially the spatial connections. To this end, monthly streamflow data observed over a period of 52 years 3 (1951–2002) from each of 639 gaging stations in the contiguous United States are studied. 4 5 The connections are examined primarily using the concept of *clustering coefficient*. The 6 clustering coefficient is a measure of local density and, hence, quantifies the tendency of a 7 network to cluster. The implications of the clustering coefficient results for 8 interpolation/extrapolation of streamflow data as well as for classification of catchments are 9 also discussed. To put the clustering coefficient analysis in a proper perspective, traditional 10 linear correlation analysis (Pearson correlation coefficient) and another simple network-based 11 analysis (degree centrality) are also performed.

The rest of this paper is organized as follows. Section 2 introduces the concept of networks and describes the procedure for calculation of degree centrality and clustering coefficient in a network. Section 3 presents details of the study area and streamflow data considered. Section 4 reports the results, first from the traditional linear correlation analysis and then from the network-based degree centrality and clustering coefficient analysis. Section 5 highlights the implications of the results.

18 2 Network and clustering coefficient

19 **2.1 Network**

A network or a graph is a set of points connected together by a set of lines, as shown in 20 Figure 1. The points are referred to as vertices or nodes and the lines are referred to as edges 21 or links; here, the term nodes are used for points and the term links are used for lines. 22 Mathematically, a network can be represented as $G = \{P, E\}$, where P is a set of N nodes 23 (P_1, P_2, \dots, P_N) and E is a set of n links. The network shown in Figure 1 has N = 7 (nodes) and n 24 25 8 (links), with Р = $\{1,2,3,4,5,6,7\}$ Ε = and = 26 $\{\{1,7\},\{2,3\},\{2,5\},\{2,7\},\{3,7\},\{4,7\},\{5,6\},\{6,7\}\}.$

Figure 1 is perhaps the simplest form of network, i.e. one with a set of identical nodes connected by identical links. There are, however, many ways in which networks may be more complex. For instance, a network: (1) may have more than one different type of node and/or link; (2) may contain nodes and links with a variety of properties, such as different weights for different nodes and links depending on the strength of nodes and connections; (3) may have links that can be directed (pointing in only one direction), with either cyclic (i.e. containing closed loops of links) or acyclic form; (4) may have multilinks (i.e. repeated links
 between the same pair of nodes), self-links (i.e. links connecting a node to itself), and
 hyperlinks (i.e. links connecting more than two nodes together); and (5) may be bipartite, i.e.
 containing nodes of two distinct types, with links running only between unlike types.

5 There are many different ways and measures to study the characteristics of networks. In the 6 context of the modern theory of *complex networks* (which also include random graphs), 7 degree centrality, clustering coefficient, small-world networks, and degree distribution are 8 some of the prominent concepts. As the present study uses the concepts of degree centrality 9 and clustering coefficient for studying streamflow connections, they are described next.

10 2.2 Degree centrality

11 Centrality is one of the most basic and intuitive measures of a network; see Freeman (1979) 12 for an early comprehensive review. The idea behind the use of centrality as a network 13 measure is that it identifies whether a given node, say, *i* in a network is more central or more 14 influential than another node in the network. The degree centrality of node *i* in a network of *N* 15 nodes is defined as the number of first neighbors (or simply *neighbors*) of node *i* divided by 16 the total number of possible neighbors (N - 1) in the network.

17 Let us consider a selected node *i* in a network of *N* nodes, having k_i links which connect it to 18 k_i other nodes. For illustration, Figure 2 presents a network consisting of nine nodes (i.e. N =19 9), with the node *i* having four links (i.e. with four other nodes) (see Figure 2, left). In this 20 case, the four nodes corresponding to the four links are the *neighbors* of node *i*, which are 21 identified based on some conditions (e.g. correlation between node *i* and other nodes in the 22 network), while the total number of possible neighbors for node *i* is eight (i.e. N - 1).

23 **2.3 Clustering coefficient**

The clustering coefficient quantifies the tendency of a network to cluster, which is one of the most fundamental properties of networks (Watts and Strogatz, 1998). The clustering coefficient of a network is basically a measure of local density. The concept of clustering has its origin in sociology, under the name "fraction of transitive triples" (Wasserman and Faust, 1994). The procedure for calculating the clustering coefficient is as follows.

Let us consider first a selected node *i* in the network, having k_i links which connect it to k_i other nodes, as shown in Figure 2 (left). If the neighbors of the original node (*i*) were part of a cluster, there would be $k_i(k_i - 1)/2$ links between them. As shown in Figure 2 (right), there are 1 4(4-1)/2 = 6 links in the *cluster* of node *i*. The clustering coefficient of node *i* is then given 2 by the ratio between the number E_i of links that actually exist between these k_i nodes (shown 3 as solid lines on Figure 2, right) and the total number $k_i(k_i - 1)/2$ (i.e. all lines on Figure 2, 4 right),

5
$$C_i = \frac{2E_i}{k_i(k_i-1)}$$
 (1)

6 The clustering coefficient of the whole network *C* is the average of the clustering coefficients
7 *C_i*'s of all the individual nodes.

8 The clustering coefficient of a random graph is C = p (where *p* is the probability of two nodes 9 being connected), since the links in a random graph are distributed randomly. However, the 10 clustering coefficient of real networks is generally much larger than that of a comparable 11 random network (i.e. having the same number of nodes and links as the real network). 12 Therefore, the clustering coefficient analysis offers useful information about the nature of the 13 network and, hence, the appropriate model (e.g. level of complexity), among others.

14 **3** Study area and data

15 In the present study, streamflow data from the United States are studied to explore the 16 usefulness of the theory of networks for identifying connections in streamflow, with a focus 17 on spatial connections. Monthly data from an extensive network of 639 streamflow gaging stations in the contiguous US are studied. The locations of these 639 stations are shown in 18 19 Figure 3. The above streamflow data are obtained from the US Geological Survey database, in 20 particular from the Hydro-Climatic Data Network (HCDN), originally developed by Slack 21 and Landwehr (1992) and subsequently updated at different times, with the last update in 22 2009; see Lins (2012) for details (http://water.usgs.gov/osw/hcdn-2009/). The HCDN is a 23 subset of all USGS streamgages for which the streamflow primarily reflects prevailing 24 meteorological conditions for specified years; see Kiang et al. (2013) for the latest and 25 comprehensive account of USGS streamflow gages across the entire United States. The 26 HCDN streamgage stations were screened to exclude sites where human activities, such as 27 artificial diversions, storage, and other activities in the drainage basin or the stream channel, affect the natural flow of the watercourse. 28

Streamflow data in the US are commonly expressed in "water years," which commence in October. The data used in this study are those observed over a period of 52 years (1951– 2002), obtained from an earlier version of HCDN. The data are average monthly values (not

anomalies). During the past few decades, a large number of studies have investigated the 1 2 above streamflow dataset (or a part or variant of it) in many different contexts (e.g. Slack and Landwehr, 1992; Kahya and Dracup, 1993; Vogel and Sankarasubramanian, 2000; 3 Sivakumar, 2003; Tootle and Piechota, 2006; Patil and Stieglitz, 2012; Sivakumar and Singh, 4 5 2012; Kiang et al., 2013). Some of these studies have explicitly addressed the connections of streamflow between the stations, including in the context of data correlations, catchment 6 7 similarities, and other measures; see, Patil and Stieglitz (2012) and Kiang et al. (2013) for 8 some recent studies. Many studies have explored the connections of streamflow with large-9 scale climatic patterns and relevant indices, including El-Niño, La-Niña, Southern Oscillation 10 Index (SOI), Pacific North America (PNA) Index, and Pacific Decadal Oscillation (PDO). 11 However, within the specific context of the network analysis for connections among 12 streamflow stations presented here, as well as in the broader context of complex systems 13 science for streamflow analysis, the studies by Sivakumar (2003) and Sivakumar and Singh (2012) are worth mentioning, as they have addressed the aspects of streamflow variability, 14 nonlinearity, and dominant governing mechanisms, especially for studies on model 15 simplification, data interpolation/extrapolation, and catchment classification framework. 16

17 The above 639 streamflow stations and the observed streamflow data exhibit tremendous variations in their characteristics, often by about four orders of magnitude. For instance: (1) 18 basin drainage area ranges from 10.62 km² (4.1 mi²) to 35224 km² (13600 mi²) (2) station 19 elevation ranges from 0 m to 2996 m (9830 ft); (3) mean flow ranges from 0.0549 m³/s (1.94 20 ft^{3}/s) to 381.59 m³/s (13476 ft³/s); (4) maximum flow ranges from 0.878 m³/s (31 ft³/s) to 21 2489 m³/s (87900 ft³/s); and (5) number of zero-flow months ranges from none to 424. Figure 22 23 3, for instance, presents the variations in the mean (Figure 3a), standard deviation (Figure 3b), 24 and coefficient of variation (Figure 3c) of flow values in all the 639 stations. The significant 25 differences in catchment and flow characteristics can play important roles in the nature and extent of connections in streamflow between the different stations. While studying their 26 27 influences is clearly important, the present study does not specifically attempt to address this. 28 Rather, the focus of the present study is in identifying the extent of connections among the 29 stations based on streamflow data alone.

30 4 Analysis and results

The usefulness of the theory of networks for studying connections in streamflow is examined primarily through the clustering coefficient analysis on the monthly streamflow data from the above 639 stations in the United States. To put the clustering coefficient analysis in a proper
 perspective, however, linear correlation and degree centrality analyses are also performed.

3 4.1 Linear correlation analysis

A common approach to examine connections between streamflow observed at different 4 5 stations is through a simple linear cross correlation analysis, where the correlation for any given station is given by the average of its correlation with all the other stations. Several 6 7 variants of this procedure are also usually considered. These include: *nearest* neighbors – for 8 example, number of nearby stations based on distance or stations within a pre-defined region 9 of geographic promixity or neighborhood, with equal or unequal weightage (e.g. inverse 10 distance); and *similar* stations – stations with *similar* properties (e.g. in terms of climate, 11 rainfall, basin characteristics, land use), which may or may not include nearest stations. These 12 and many other *correlation-based* procedures (e.g. spline fitting) are routinely employed for interpolation and extrapolation of streamflow and other hydrologic data. 13

14 In this study, two of the above-mentioned procedures are employed for examining the 15 monthly streamflow from the 639 stations: (1) for each station, the correlation is the average of its correlation with all the other 638 stations; and (2) for each station, the correlation is the 16 17 average of correlations for a *certain number of nearest neighbors* – 30, 15, and 5 neighbors. 18 The neighbors are selected based on the geographical distance from the reference station. For 19 the three different number of neighbors (i.e. 30, 15, and 5) considered in the latter, the mean 20 distances are 111, 73, and 41 km, respectively, and the standard deviations are 94, 63, and 37 21 km, respectively. The correlation considered here is the Pearson correlation coefficient, and 22 the streamflow values themselves (rather than their logarithms) are used for computation. The 23 Pearson correlation coefficient can be sensitive to outliers in the data. However, the impact of 24 this sensitivity is minimal for monthly streamflow (when compared to streamflow at shorter timescales, e.g. daily), as the monthly data assumes approximately normal distribution from 25 26 additive errors at finer timescales through the central limit theorem (Anderson, 2010).

When all the 638 stations are considered, the correlation values are generally very low, as expected, with only 0.5% of the stations exceeding a value of 0.4 (see Figure 4a). This is mainly due to the consideration of a very large region, with the stations coming from different climatic, catchment, land use, and other characteristics. When the number of stations is reduced, the results get generally better – see Figure 4b (30 neighbors), Figure 4c (15 neighbors), and Figure 4d (5 neighbors). Among the three neighborhood cases, the best correlation results are obtained when the neighborhood is the smallest, i.e. 5 neighbors
 (Figure 4d), with a large number of stations having correlations above 0.7.

3 While one can study a large number of combinations in terms of the *neighborhood*, what is 4 evident from even the very few cases presented here is that there are obvious *regional* patterns 5 in terms of correlations, regardless of the number of neighbors. These regional patterns are 6 considered to have important implications for a wide range of studies in hydrology and water 7 resources, as they are commonly used as a basis for interpolation and extrapolation of 8 streamflow and, subsequently, for water resources assessment, planning, and management. 9 However, as Sivakumar and Singh (2012) point out, through their nonlinear dynamic study on 10 streamflow data from the western United States, the use of *regional* patterns as basis for 11 streamflow studies may be misleading, as such patterns are not necessarily a true 12 representation of the actual connections between the stations but may just be spurious. The obvious question, therefore, is: how to identify if the connections are actual or spurious? This 13 14 is where the ideas from the theory of networks can be particularly useful.

15 **4.2 Degree centrality analysis**

The degree centrality is calculated for the monthly streamflow data from the network of 639 16 17 stations in the United States, according to the procedure described in Section 2.2. The essence 18 of the procedure for the streamflow data is as follows. For a given streamflow station or node 19 *i*, the nearest neighbors k_i in the network of 639 stations (more specifically, the remaining 638 20 stations) are identified based on a (pre-specified) threshold value (T). To define the threshold 21 value, the correlations in streamflow data between different stations are considered as a 22 reasonable measure. With this, if, for example, the correlation between station *i* and any other 23 station(s) in the entire network of 639 stations exceeds the threshold value, then that station(s) 24 is considered as a *neighbor(s)*, k_i , for station *i*. The degree centrality of station *i* is then given by the ratio of the number of neighbors to the total number of possible neighbors (i.e. 638). 25

In this study, several different threshold values are considered for calculation of the degree centrality. Although there are no definitive guidelines for selection of the threshold values for streamflow (and other hydrologic) data, our experience in streamflow studies, especially spatial and temporal correlations, offers some useful clues. For instance, streamflow data generally exhibit high spatial correlations (when compared to rainfall values, for example), especially at the monthly scale. With this knowledge, and also with the condition that -1 < T 1 < 1.0, closer intervals of values are considered at the higher end of correlations and vice-2 versa. In addition, very low values (say, T < 0.30) and very high values (say, T > 0.85) do not 3 offer much help in the analysis; for instance, T < 0.30 normally results in a very large number 4 of neighbors, while T > 0.85 results in a very small number. Considering all these, eight 5 threshold values are used for analysis: 0.30, 0.40, 0.50, 0.60, 0.70, 0.75, 0.80, and 0.85.

6 Figure 5a-d, for example, shows the results from the degree centrality analysis for the 639 7 stations for threshold values of 0.70, 0.75, 0.80, and 0.85. The results offer some interesting 8 observations. For instance, only a very small number of streamflow stations (blue circles) 9 have connections with more than 10% of the other stations in the network of 639 stations, 10 while a large number of stations (cyan circles) have connections to less than just 1% of the 11 other stations. Indeed, for thresholds of 0.70, 0.75, 0.80, and 0.85, the number of stations 12 having connections with more than 10% of the stations is only 39, 0, 0, and 0, respectively, 13 while the number of stations having connections with less 1% of the stations is 118, 160, 257, and 429, respectively. This clearly suggests that only a small proportion of stations has 14 15 considerable influence in the network, while a large proportion of stations has only very little 16 or almost no influence. This result has significant implications, for example, in interpolation 17 and extrapolation, especially from the viewpoint of *dominant* stations (as is the case of 39 18 stations for T = 0.70; Figure 5a). It is also important to note, however, that not all of the 19 stations (i.e. neighbors) that a given station has connection with (see Figure 5a-d) are the 20 geographic neighbors, and some are over long geographic distances (see Section 4.3 for 21 further details on this). These observations seem to suggest that the streamflow network of 22 639 stations is neither a completely ordered network nor a random graph, but some other.

23 4.3 Clustering coefficient analysis

24 Following the description in Section 2.3, the procedure for the calculation of the clustering coefficient for the monthly streamflow data from the network of 639 stations in the United 25 26 States is as follows. For a given streamflow station or node *i*, the nearest neighbors k_i in the network of 639 stations are identified based on a (pre-specified) threshold value (T), as 27 28 explained above. The *cluster* of these k_i neighbors then forms the basis for identifying the 29 actual connections. Therefore, the actual connections are those links in the cluster of stations 30 (not just nearest stations) having correlations among themselves exceeding the threshold value. Similar to the degree centrality analysis above, eight threshold values are considered in 31 32 the cluster coefficient analysis as well: 0.30, 0.40, 0.50, 0.60, 0.70, 0.75, 0.80, and 0.85.

Figure 6a-d, for instance, presents the clustering coefficient values for the 639 stations for 1 2 threshold values of 0.70, 0.75, 0.80, and 0.85. Table 1 presents the number of stations falling 3 under different ranges of clustering coefficient values. For better illustration and discussion, 4 the clustering coefficient values are grouped into six different ranges. In Figure 6 and Table 1, 5 a clustering coefficient of 0.0 indicates that there are no actual connections, while 'NA' indicates there are no nearest neighbors. From an overall perspective, the clustering 6 7 coefficient results indicate certain similarity at some stations/regions but significant 8 differences at others. They also offer some specific observations:

- Even *nearest* stations have significantly different characteristics (e.g. connections), as part of a network. Some stations have very strong connections, while others have almost no or only very weak connections. For instance, the few geographically closer stations in Florida in the southeast region are an excellent example. These few stations have clustering coefficient values varying anywhere from 0 to 1.0, especially for T =0.7 and 0.75 (Figures 6a and 6b).
- 15 Even *distant* stations have significantly similar characteristics, i.e. they have very • 16 strong (or very weak or even no) connections as part of a network. The similar (very high or very low) clustering coefficient values obtained for a number of stations all 17 18 across the United States, regardless of their geographic promixity, offer evidence to 19 this; for example, regardless of the threshold value, the green circles (see Figure 6a–d), 20 representing the clustering coefficient range 0.76-1.0, are present all over the United 21 States, northwest to southwest to midwest to northeast to southeast. Similar 22 observations are made also for other clustering coefficient ranges, for one or more threshold values; see the deep pink circles ($C_i = 0.51-0.75$) and blue circles ($C_i = NA$); 23
- There are significant changes in characteristics with respect to the threshold values.
 For instance, as can be seen from Figure 6 and Table 1, for threshold values of 0.7 and
 0.85, the number of stations falling within the clustering coefficient range of 0.51–0.75
 is 348 and 197, respectively. Indeed, in some cases, further breakdown in the range of
 clustering coefficient values indicate an even wider difference in the (percentage)
 number of stations for these thresholds;
- Although there are changes in the number of stations having similar clustering
 coefficient values with respect to thresholds, there is no consistency in the trend of
 changes (see, for example, the number of stations falling within the clustering
 coefficient range of 0.51–0.75).

While the usefulness of the clustering coefficient values in assessing connections between 1 2 streamflow stations and identifying regions having similarity/differences is abundantly clear, the actual links in the network would certainly offer more specific details as to where and 3 how connections exist. To facilitate this, Figure 7 shows the actual links for four selected 4 5 streamflow stations (red circles) for threshold values of 0.75 (Figure 7a), 0.80 (Figure 7b), and 0.85 (Figure 7c); the nodes and links for T = 0.70 are too many, and so do not offer a 6 7 good visualization. In each of these plots, for the station of interest (red circle), a green circle 8 indicates a station that has a correlation coefficient value exceeding the threshold, and a black 9 circle indicates a station that has a correlation coefficient value smaller than the threshold. 10 The lines are the *actual links* among all the links available for the *cluster of neighbors* (green 11 circles only). The plots clearly indicate which stations are *actually* connected to which other. 12 The plots make it abundantly clear that *geographic promixity* does not always result in greater 13 correlation, and the *actual links* can go for large distances. Among the various observations 14 that can be made, the ones for the two stations in the northwest are certainly interesting. Despite being in the same region, the two stations exhibit significantly different connectivity 15 characteristics, for example, for threshold level 0.85 (Figure 7c), with one showing all the 16 actual connections within a small neighborhood (see the enlarged plot on the top left) while 17 18 the other showing no clear neighborhood for connectivity (see the enlarged plot on the bottom 19 left). The latter station (see bottom left) is an even more curious case, as most of the 20 neighbors of this station seem to be beyond its (perceived) *circle of geographic influence*. The 21 actual links observed for the other threshold values also support the above observations.

These observations clearly suggest that our usual approach with consideration of geographic proximity, nearest neighbors, regional patterns, and linear correlation-based techniques for studying connections in streamflow may have serious limitations. Clustering coefficient, and other network-based techniques, offers a better means to examine streamflow connections. In what follows, we explore the clustering coefficient results even further.

As the clustering coefficient of a network is based on the *actual links* among *all links* in the *cluster* of neighbors of a node (rather than just the links between a node and its neighbors), it would be interesting to see how it changes with respect to *all links* and *actual links*. To this end, Figure 8a–d shows the clustering coefficient values against the *number of all links* (red circles) and the *number of actual links* (blue circles) for threshold values of 0.70, 0.75, 0.80, and 0.85 for the monthly streamflow data from the United States. The results lead to thefollowing major observations:

- In general, regardless of the threshold value, there is an inverse relationship between
 the clustering coefficient and number of links (both for *all links* and *actual links*), i.e.
 higher clustering coefficient for smaller number of links and vice-versa;
- The inverse relationship between the clustering coefficient and number of links is
 generally more evident for lower thresholds (see Figure 8a and b) when compared to
 higher thresholds (see Figure 8c and d). When the threshold is very high (T = 0.85),
 this relationship seems to cease to exist;
- The clustering coefficient is generally far more sensitive when the number of links is
 smaller (see the significant larger spread of circles on the Y-axis), but has only very
 little or almost no sensitivity for a larger number of links (see the very narrow spread
 followed by a tapering towards a fixed value especially in Figure 8a and b). Further,
 larger numbers of links almost always give lower clustering coefficients;

15 16 • For a given number of links, the clustering coefficient for a lower threshold is generally higher than that for a higher threshold.

17 Another useful way to look at the clustering coefficient of a network is its relationship with 18 the number of neighbors (k_i) , which is defined by the threshold value and dictates the (number of) links and actual links. Figure 9a-d shows the relationship between the clustering 19 20 coefficient values and the number of neighbors for threshold values of 0.70, 0.75, 0.80, and 21 0.85 for the monthly streamflow data. The results generally indicate an inverse relationship 22 between the clustering coefficient and number of neighbors, but such a relationship is far 23 more evident for lower threshold values (see Figure 9a and b) than that for higher threshold 24 values (see Figure 9c and d). Again, the clustering coefficient is generally far more sensitive 25 when the number of neighbors is smaller (see the larger spread towards the left), but becomes 26 less sensitive for a larger number of neighbors (see the narrow spread towards the right). 27 These observations are somewhat consistent with those made in regard to the number of links 28 (Figure 8). It is important to recall, however, that the neighbors are not necessarily geographic 29 but defined by the threshold values (as shown in Figure 7).

30 While these results and observations are still preliminary in nature, they seem to suggest that 31 there is a particular threshold value or range beyond which the inverse relationship between 32 the clustering coefficient and number of neighbors/links/actual links in the streamflow network may not hold well for monthly streamflow data from the United States, and
 streamflow data in general.

3 Finally, the question arises as to the type of network. As mentioned previously, the clustering 4 coefficient of a whole network (C) is the average of the clustering coefficients C_i 's of all the individual nodes. The clustering coefficient of the eight different networks of the above 639 5 6 streamflow stations corresponding to threshold values of 0.30, 0.40, 0.50, 0.60, 0.70, 0.75, 7 0.80, and 0.85 is 0.79, 0.76, 0.71, 0.68, 0.65, 0.63, 0.58, and 0.51 (see Table 1). These 8 generally high clustering coefficient values seem to suggest that the streamflow monitoring 9 network of 639 stations is not a random graph, since a (comparable) random graph, where the links are distributed randomly, will have a typically very low clustering coefficient, i.e. C = p, 10 11 where p is the probability of two nodes being connected. As (natural) streamflow dynamics 12 are neither completely random (there are inherent deterministic patterns) nor completely 13 ordered (there are inherent stochastic components) (see Sivakumar, 2011; Sivakumar and Singh, 2012 for some details), it is also reasonable to assume that streamflow networks are 14 15 not random graphs, but networks of some other nature. Whether they are small-world or 16 scale-free or other types of networks remains to be seen. Studies in this direction are currently 17 underway, details of which will be reported in the future.

18 **5** Study implications

One of the basic requirements in studying streamflow dynamics is to identify connections in space or time or space-time, depending upon the purpose. Although a wide variety of approaches have been developed and applied to identify connections in streamflow dynamics, there is no question that significant improvements are still needed. In this regard, modern developments in the field of network theory, especially complex networks, offer new avenues, both for their generality about systems and for their holistic perspective about connections.

The present study has made an initial attempt to apply the ideas developed in the field of 25 complex networks to examine connections in streamflow dynamics, with particular focus on 26 27 spatial connections. Application of the concepts of clustering coefficient, which is a measure 28 of local density and quantifies the tendency of a network to cluster to monthly streamflow 29 data from a large network of 639 monitoring stations in the contiguous United States has 30 offered some very interesting results. The clustering coefficient values for the 639 stations 31 suggest that: (1) even nearest stations can have significantly different connections and distant 32 stations can have significantly similar connections; (2) connections can be significantly

different for different threshold levels; (3) there is generally an inverse relationship between 1 2 the clustering coefficient and number of neighbors, number of all links, and actual links (in the cluster of neighbors); (4) the clustering coefficient is far more sensitive when the number 3 4 of neighbors/number of links is smaller, but has only little or no sensitivity when the latter is 5 larger; and (5) the high clustering coefficient value obtained for the entire network is not consistent with the one expected for a random graph, suggesting that the streamflow network 6 7 is likely to be small-world or scale-free or some other type. The results from the degree 8 centrality analysis suggest that a very small number of streamflow stations have more 9 influence in the network of 639 stations with connections to more than 10% of the other 10 stations, while a large number of stations have very little influence with connections to just 11 less than 1% of the other stations. These observations seem to further eliminate the possibility 12 of random nature of the streamflow monitoring network.

13 Although the present results are preliminary, they offer important information about the 14 connections that possibly exist in the streamflow network, and especially their extent. The 15 clustering coefficient values, and the actual links, are particularly useful in the identification of the specific regions where interpolation and extrapolation of streamflow data may be more 16 17 effective and also of the specific stations whose data can be more reliable for such purposes. For instance, regions consisting of stations with high clustering coefficient values would 18 19 generally provide a more accurate estimation of streamflow when interpolation and extrapolation schemes are employed. It is also important to emphasize, however, that such a 20 21 region is identified based on *cluster of actual connections*, rather than based on our traditional 22 way of geographic proximity, nearest neighbors, regional patterns, and linear correlations. 23 The clustering coefficient values can also offer important clues and guidelines as to the setting 24 up/removal of streamflow monitoring stations in a region. For instance, if a region consists of 25 stations with very high clustering coefficients, then installing additional monitoring stations will not offer any significant benefits. Indeed, one or more monitoring stations from such a 26 27 region may be removed and the resources can be used in regions where additional stations 28 might offer greater benefits (e.g. in regions where the clustering coefficient values are low). 29 The identification of stations that play more influential roles in the network, as is reflected by the degree centrality results, can also be useful in identifying stations/regions around which 30 interpolation/extrapolation might work better. 31

Finally, the present study and the results obtained have important implications for a wide 1 2 range of issues and associated efforts in streamflow modeling, and hydrologic modeling in general. Among these are: (1) predictions in ungaged basins (PUB), where approaches based 3 4 on nearest neighbors, regionalization, similarity, and other concepts are commonly adopted; 5 (2) formulation of a catchment classification framework, for simplification and generalization in our modeling paradigm and better communication among/between researchers and 6 7 practitioners; and (3) development of an integrated framework for water planning and 8 management, including in studies on climate change impacts on water resources, that involves 9 proper consideration and inclusion of stakeholders and concepts from a vast number of 10 disciplines, including climate, hydrology, engineering, environment, ecology, social sciences, 11 political sciences, economics, and psychology. In view of these, ideas gained from the 12 modern theory of complex networks, and network theory at large, seem to have immense 13 potential in hydrology and water resources.

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1 Table 1. Clustering coefficient values for monthly streamflow data from the United Stat	tes
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Clustering	Number of stations within each clustering coefficient range for threshold (T)							
coefficient range	0.3	0.4	0.5	0.6	0.7	0.75	0.8	0.85
0.76–1.0	415	327	242	192	190	186	179	171
0.51-0.75	219	291	372	398	348	323	274	197
0.26–0.50	3	12	10	30	62	72	82	114
0.01–0.25	0	1	2	0	2	1	1	4
0	0	2	3	4	2	4	10	18
NA	2	6	10	15	35	53	93	135
Entire Network	0.79	0.76	0.71	0.68	0.65	0.63	0.58	0.51

1 Figure Captions

2

Figure 1. Network in its simplest form, i.e. an undirected network with only a single type of
node and a single type of link.

5 Figure 2. Connections in networks and calculation of clustering coefficient: nearest
6 neighbors and actual connections.

- Figure 3. Characteristics of monthly streamflow observed at 639 stations in the United
 States: (a) mean; (b) standard deviation; and (c) coefficient of variation.
- 9 Figure 4. Linear correlation for streamflow: average of correlation with (a) all the 638
 10 stations; (b) nearest 30 neighbors; (c) nearest 15 neighbors; and (d) nearest 5 neighbors
- Figure 5. Degree centrality for four correlation thresholds: (a) 0.70; (b) 0.75; (c) 0.80; and
 (d) 0.85.
- 13 Figure 6. Clustering coefficients for four correlation thresholds: (a) 0.70; (b) 0.75; (c) 0.80;

14 and (d) 0.85. The six ranges are chosen for better visualization of results.

- Figure 7a. Links in streamflow network for threshold T = 0.75. Four nodes (stations) are chosen for better visualization.
- Figure 7b. Links in streamflow network for threshold T = 0.80. Four nodes (stations) are chosen for better visualization.
- Figure 7c. Links in streamflow network for threshold T = 0.85. Four nodes (stations) are chosen for better visualization.
- Figure 8. Relationship between clustering coefficient and number of links: (a) T = 0.70; (b)
- 22 T = 0.75; (c) T = 0.80; and (d) T = 0.85. Both *all links* (red circles) and *actual links* (blue 23 circles) are presented.
- Figure 9. Relationship between clustering coefficient and number of nearest neighbors: (a) T = 0.70; (b) T = 0.75; (c) T = 0.80; and (d) T = 0.85.
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