

1 **Variational assimilation of remotely sensed flood extents**
2 **using a two-dimensional flood model**

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1 **Abstract**

2 A variational data assimilation (4D-Var) method is proposed to directly assimilate flood
3 extents into a two-dimensional (2D) dynamic flood model, to explore a novel way of utilizing
4 the rich source of remotely sensed data available from satellite imagery for better analyzing or
5 predicting flood routing processes. For this purpose, a new cost function is specially defined
6 to effectively fuse the hydraulic information that is implicitly indicated in flood extents. The
7 potential of using remotely-sensed flood extents for improving the analysis of flood routing
8 processes is demonstrated by applying the present new data assimilation approach to both
9 idealized and realistic numerical experiments.

10

11 **Key words:** variational data assimilation (4D-Var); flood extent; satellite imagery;
12 hydrodynamic model; cost function; shallow water equations

13

14 **1 Introduction**

15 Flooding poses a significant threat to human society. Nowadays, floods are becoming more
16 frequent as a result of intensive regional human activities and environmental change.
17 Hydraulic or hydrodynamic models have become reliable and cost-effective tools to analyze
18 and predict flood routing through catchments, rivers and floodplains. These models can
19 provide dynamic outputs, e.g. inundation area, water depth, and/or flow velocity, for flood
20 warning and risk assessment. Nevertheless, models are not perfect and uncertainties and
21 computational errors may arise from various sources, including the uncertainties associated
22 with hydrological parameters, initial and boundary conditions, as well as numerical errors as a
23 result of numerical discretization and mathematical approximations (Le Dimet et al., 2009;
24 Pappenberger et al., 2007a). In order to reduce prediction errors or uncertainties, field
25 measurements are usually used to verify and calibrate a model before applying it to make
26 predictions. Traditional trial and error approaches are commonly used in model calibration
27 but they are well-known to be subjective and tedious (Ding, 2004). Therefore, in order to
28 make a better prediction, it would be more beneficial to have more intelligent calibration
29 methods achieved by fusing a dynamic flood model with observed information to obtain an
30 optimal estimate of model states and parameters.

1 Data and model fusion methods are termed data assimilation, which stems from
2 meteorology and oceanography (McLaughlin, 2002; Reichle, 2008; Wang et al., 2000). The
3 variational data assimilation method, also called the 4D-Var method, is based on the optimal
4 control theory of partial differential equations, which offers a powerful tool for data
5 assimilation (Le Dimet and Talagrand, 1986; Talagrand and Courtier, 1987). As well as its
6 operational application in meteorology and oceanography, this method also attracts great
7 attention of hydrological society. It has been widely applied to assimilate in-situ and remotely
8 sensed hydrological data from multi-sources into the runoff-rainfall model and land surface
9 model (Bateni et al., 2013; Le Dimet et al., 2009; Lee et al., 2012; Reichle, 2008). Also, it
10 has been successfully applied to improve the predictive capability of one-dimensional (1D)
11 and two-dimensional (2D) hydraulic models (Atanov et al., 1999; Bélanger and Vincent,
12 2005; Ding, 2004; Honnorat et al., 2007, 2009; Roux and Dartus, 2006).

13 In river hydraulics, the available measurements commonly include water stage (level) and
14 discharge at hydrological stations, and velocity at gauging points. These measurements are
15 generally sparse even for those study areas with decent monitoring systems and therefore
16 likely to be insufficient to support reliable model calibration. During a flood event, the
17 available measurements may be even scarcer due to malfunctioned operation of some
18 monitoring systems under extreme flow conditions and the difficulty in performing field
19 surveys. Fortunately, rich sources of remote sensing data with different spatial and temporal
20 coverage now become increasingly available. Remote sensing imagery provides spatially
21 distributed information about flood states which is hard to obtain from the traditional point-
22 based field measuring approaches (Hostache et al., 2010). As a whole, due to their low-cost
23 and large coverage, remotely sensed data are now becoming an important source of
24 measurements and widely applied to flood monitoring and loss evaluation for flood hazards
25 (Pender and Néelz, 2007). Furthermore, recent intensive research, such as the direct
26 estimation of hydraulic variables (e.g. flow discharge and water stage) from satellite imagery,
27 the use of remote sensing data to calibrate and validate model, the fusion of these data with
28 dynamic model using data assimilation method and among others, has significantly
29 contributed to the advances of the integrating remotely sensed data from space with flood
30 models (e.g. Schumann et al., 2009; Smith, 1997).

31 Substantial efforts have been made using the 4D-Var and Bayesian-updating methods to
32 demonstrate the potential of assimilating remotely sensed data from space for improving flood

1 prediction (Andreadis et al., 2007; Durand et al., 2008; Giustarini et al., 2011; Komma et al.,
2 2008). Roux and Dartus (2006) attempted to determine flood discharge from remotely sensed
3 river width using a 1D hydraulic model. In 2D river hydraulic modeling, 4D-Var methods
4 have been developed to assimilate spatially distributed water stage (Lai and Monnier, 2009)
5 and Lagrangian-type observations, e.g. remotely sensed surface velocity (Honnorat et al.,
6 2009, 2010). Hostache et al. (2010) employed a 4D-Var method to assimilate the water stage
7 derived from a RADARSAT-1 image of the 1997 Mosel River flood event in France into a
8 2D flood model to improve model calibration. Water stage can be indirectly derived from
9 satellite imagery or directly measured by satellite altimetry. The accuracy of indirect water
10 stage retrieval from satellite imagery is typically in a range of 40 - 50 cm (Alsdorf et al.,
11 2007; Hostache et al., 2010; Matgen et al., 2010). Simple overlay analysis of DEM and flood
12 extent map may lead to high errors to the order of meter even when a 30m-resolution ERS
13 ASAR image is used (Brakenridge et al., 1998; Oberstadler et al., 1997; Schumann et al.,
14 2011). Generally, additional steps must be performed in order to obtain an acceptable
15 estimation of water levels for using with hydrodynamic modeling. The complexity of these
16 steps varies with the methods being applied (Matgen et al., 2007, 2010; Raclot, 2006;
17 Schumann et al., 2007). For instance, Raclot (2006) and Hostache et al. (2010) used a
18 hydraulic coherence constraint to minimize the estimation errors. Schumann et al. (2007)
19 proposed a Regression and Elevation-based Flood Information eXtraction model (REFIX) for
20 water depth estimation and later suggested an alternative for deriving water level from river
21 cross-section data (Schumann et al., 2008). Therefore, the derivation of water level from flood
22 extent with acceptable accuracy is not a straightforward procedure.

23 Inland water level can also be directly measured from satellite altimetry that is originally
24 developed for open oceans. The database of altimetric water level for about 250 sites on large
25 rivers in the world has been developed based on satellite altimetry missions
26 (<http://www.legos.obs-mip.fr/en/soa/hydrologie/hydroweb/>). For oceans and great lakes, the
27 accuracy of estimating water level may reach a few centimeters (Fu & Cazenave, 2001;
28 Crétaux & Birkett, 2006). For rivers and floodplains, the retrieved water level data quality is
29 highly variable (Santos da Silva et al., 2010), most typically 50 cm (Alsdorf et al., 2007).
30 However, despite of its relative high-accuracy for large inland water bodies comparing with
31 the indirectly retrieved water level, the present in-orbit satellite altimetry (four satellites
32 including Saral/AltiKa, Jason-2, HY-2 and Cryosat-2) is still problematic because of the
33 spatial and temporal resolutions and coverage for sampling relative small water bodies. It

1 essentially provides only spot measurements of water level (Alsdorf et al., 2007). To improve
2 this, an exciting satellite mission SWOT using a swath-based technology has been proposed
3 and will be launched for accurate monitoring of inland water bodies
4 (<https://directory.eoportal.org/web/eoportal/satellite-missions/s/swot>). The SWOT mission
5 provides great potential and new opportunity for data collection in the near future (in 2020).
6 However, currently the rich optical and SAR images will be still the main sources of remote
7 sensing data for monitoring flood. Therefore, it is still of great interest to investigate the
8 combined assimilation of the currently available multi-source satellite data.

9 In contrast to water stage, the remotely sensed flood extent can be directly derived from
10 satellite imagery without affecting the original resolution (for example 30 m for Envisat
11 ASAR and 250 m for MODIS data), which is comparable to the mesh size normally adopted
12 in flood modeling. Various simple and mature approaches are available for rapid and
13 automatic extraction of flood extent map from optical and SAR imageries (Matgen et al.,
14 2011; Smith, 1997). However, to the best of our knowledge, there has been no attempt at the
15 direct assimilation of flood extent data into a 2D dynamic flood model using a 4D-Var
16 method to date.

17 Herein, we attempt to use a 4D-Var method to assimilate remotely sensed flood extent
18 data into a dynamic flood model based on the numerical solution to the 2D shallow water
19 equations (SWEs). For this purpose, a new cost function is specifically constructed to
20 effectively fuse the hydraulic information available implicitly in flood extents. The numerical
21 results show that the proposed 4D-Var method can effectively assimilate the flood extent data
22 and improve the prediction accuracy of flood routing. The rest of the paper is organized as
23 follows. First, a short description is given in Section 2 to introduce the 2D flood model
24 coupled with a 4D-Var method. In order to implement the assimilation of the observed flood
25 extent into the 2D flood model, Section 3 proposes a cost function that measures the
26 discrepancy between observed data and modeling results. The new approach is validated by
27 idealized tests in Section 4 before being applied to a realistic case in Section 5. Finally,
28 summary and brief conclusions are drawn in Section 6.

29

1 2 Two-dimensional dynamic flood model with variational data assimilation

2 2.1 Overview of variational data assimilation

3 4D-Var is a method based on the optimal control theory of a physical system governed by
4 partial differential equations (Le Dimet and Talagrand, 1986). It allows us to perform flow
5 state analysis or prediction of a system by combining a physically based dynamic model with
6 observations. To implement a 4D-Var, a cost function must be firstly defined to measure the
7 discrepancy between the computational results and observations. A cost function J without
8 regularization terms may be given as

$$9 \quad J(\mathbf{p}) = \frac{1}{2} \int_0^T \|\mathbf{H}\mathbf{U} - \mathbf{O}\|^2 dt = \frac{1}{2} \int_0^T (\mathbf{H}\mathbf{U} - \mathbf{O})^T \mathbf{W}^{-1} (\mathbf{H}\mathbf{U} - \mathbf{O}) dt \quad (1)$$

10 where \mathbf{p} is the control vector, $\|\cdot\|$ is the Euclidean norm, \mathbf{H} is the observation operator that
11 maps the space of the state variables to the space of observations, \mathbf{U} is the vector of state
12 variables, \mathbf{W} is the error covariance matrix, and \mathbf{O} is the observed data. Herein, the statistical
13 information can be incorporated into the norm through the error covariance matrix \mathbf{W} .

14 4D-Var can be considered as an unconstrained optimization problem that seeks an
15 optimal control vector \mathbf{p}^* to minimize the cost function $J(\mathbf{p})$ in Eq. (1). According to the
16 optimal control theory, optimum conditions are reached if the gradient $\nabla J = 0$, which means
17 that an optimal control vector is obtained and the optimal flow analysis results are closest to
18 the true (measured) state. This optimization problem may be solved by a descent-type
19 algorithm and the quasi-Newton minimization subroutine M1QN3 developed by Gilbert and
20 Lemaréchal (1989) is adopted in this work. The algorithm calculates the gradient of the cost
21 function, *i.e.* the vector of its partial derivatives with respect to each of the control variables,
22 which may be efficiently performed using the adjoint method as described in Section 2.3.

23 2.2 Two-dimensional shallow water equations

24 The 2D SWEs are widely used to approximate flood routing over a floodplain. They can be
25 written in a conservative form as follows:

$$26 \quad \frac{\partial \mathbf{U}}{\partial t} + \frac{\partial \mathbf{F}(\mathbf{U})}{\partial x} + \frac{\partial \mathbf{G}(\mathbf{U})}{\partial y} = \mathbf{B}(\mathbf{U}) \quad (2)$$

1 where x and y represent the Cartesian coordinates, t is the time, $\mathbf{U} = (h, hu, hv)^\top = (h, q_x, q_y)^\top$ is a
2 vector containing the flow variables with h being the water depth and u and v the two velocity
3 components, $\mathbf{F} = (hu, hu^2 + 0.5gh^2, huv)^\top$ and $\mathbf{G} = (hv, huv, hv^2 + 0.5gh^2)^\top$ are the flux vectors in the
4 x and y directions, g is the gravitational acceleration, $\mathbf{B} = [0, gh(S_{0x} - S_{fx}), gh(S_{0y} - S_{fy})]^\top$ is the
5 vector of the source terms, $S_{0x} = -\partial Z_b / \partial x$ and $S_{0y} = -\partial Z_b / \partial y$ are the two bottom slopes with Z_b
6 denoting the bed elevation, and $S_{fx} = n^2 q_x h^{-7/3} \sqrt{q_x^2 + q_y^2}$ and $S_{fy} = n^2 q_y h^{-7/3} \sqrt{q_x^2 + q_y^2}$ are the two
7 friction slopes in x and y directions, respectively, with n being the Manning roughness
8 coefficient. Given initial and boundary conditions, the flood routing process over a floodplain
9 may be numerically predicted on different temporal and spatial scales by solving the above
10 governing equations.

11

12 2.3 Adjoint governing equations

13 The adjoint method based on optimal control theory (Le Dimet and Talagrand, 1986) is
14 usually applied to compute the gradient of the cost function, owing to its computational
15 burden independent of the dimension of problems (Cacuci, 2003). The adjoint equations for
16 the 2D SWEs can be derived for the cost function in Eq. (1) as follows:

$$17 \quad \frac{\partial \mathbf{U}^*}{\partial t} + \frac{\partial \mathbf{F}^T}{\partial \mathbf{U}} \frac{\partial \mathbf{U}^*}{\partial x} + \frac{\partial \mathbf{G}^T}{\partial \mathbf{U}} \frac{\partial \mathbf{U}^*}{\partial y} = -\frac{\partial \mathbf{B}^T}{\partial \mathbf{U}} \mathbf{U}^* + \mathbf{H}^T \mathbf{W}(\mathbf{O} - \mathbf{H}\mathbf{U}) \quad (3)$$

18 where the adjoint variable $\mathbf{U}^* = (h^*, q_x^*, q_y^*)$ and the coefficient matrices are given by

$$19 \quad \frac{\partial \mathbf{F}^T}{\partial \mathbf{U}} = \begin{pmatrix} 0 & -u^2 + c^2 & -uv \\ 1 & 2u & v \\ 0 & 0 & u \end{pmatrix} \quad \frac{\partial \mathbf{G}^T}{\partial \mathbf{U}} = \begin{pmatrix} 0 & -uv & -v^2 + c^2 \\ 0 & v & 0 \\ 1 & u & 2v \end{pmatrix}$$

$$20 \quad \frac{\partial \mathbf{B}^T}{\partial \mathbf{U}} = \begin{pmatrix} 0 & gS_{0x} + \frac{7}{3}gS_{fx} & gS_{0y} + \frac{7}{3}gS_{fy} \\ 0 & -gS_{fx} \frac{2u^2 + v^2}{u(u^2 + v^2)} & -gS_{fy} \frac{u}{u^2 + v^2} \\ 0 & -gS_{fx} \frac{v}{u^2 + v^2} & -gS_{fy} \frac{u^2 + 2v^2}{v(u^2 + v^2)} \end{pmatrix}.$$

1 The partial derivative of the cost function J corresponding to the control vector \mathbf{p} is a simple
2 function of the adjoint variables \mathbf{U}^* , which can be found in Lai & Monnier (2009).

3 Adopting the adjoint equations in gradient computation significantly reduces the
4 computational cost because evaluation of the adjoint variables requires only one backward
5 integral in time. Once the adjoint variables are known, the partial derivatives of the cost
6 function with respect to the control variables can be computed in a straightforward way.

7 **2.4 Forward model and adjoint model**

8 The 2D SWEs in Eq.(2) are discretized using a finite volume Godunov-type scheme with the
9 inter-cell mass and momentum fluxes evaluated using the HLLC approximate Riemann solver
10 (Toro, 2001). The scheme has first-order accuracy in space but provides high-resolution
11 representation of flow discontinuities. Time discretization is achieved using an explicit Euler
12 scheme. Readers may consult Honnorat et al. (2007) for a more detailed description of the
13 shallow flow model, which is referred to as the forward model herein.

14 The adjoint model is developed by directly differentiating the source codes of the forward
15 model that solves the 2D SWEs in Eq. (2). The automatic differentiation tool TAPENADE
16 (Hascoët and Pascual, 2004) is adopted in this work to generate the reverse codes. This
17 method, based on source codes, helps to build a consistent adjoint model corresponding to the
18 forward solver.

19

20 **3 Cost function for flood extent assimilation**

21 As mentioned previously in the introduction, the flood extent can be derived from satellite
22 imagery more directly and easily than the water stage. However, the flood extent is not a state
23 variable in the 2D SWEs but basically the union of pixels where water depth is not zero.
24 Therefore it has no explicit relationship to the state variables. As a consequence, it is difficult
25 to define a cost function to implement the assimilation of flood extent in the framework of
26 4D-Var. In this work, we implement the assimilation of flood extent information into a 2D
27 dynamic flood model through an implicit way.

28 If we assume a function f as an observable quantity, the cost function may be defined as:

29
$$J(\mathbf{p}) = \frac{1}{2} \int_0^T \|f - f^{obs}\|^2 dt \quad (4)$$

1 in which, the regularization terms are neglected from the above cost function to facilitate
 2 simplified but more informative verification and validation of the proposed method and allow
 3 direct investigation of the potential benefit of assimilating flood extent data.

4 To determine the cost function for assimilation of the hydraulic information including
 5 implicitly in the remotely sensed flood extent data, a specific form of f should be introduced.
 6 Here, we define the flood extent related quantity f as a function with regard to state variables
 7 of water, \mathbf{U} , namely:

$$8 \quad f(\mathbf{U}) = A(\mathbf{h})\mathbf{U} \quad (5)$$

9
 10 where A is a matrix with regard to water depth that describes the wet-dry status, namely flood
 11 extent information.

12 Normally, the wet-dry status of a computational cell can be determined by its water
 13 depth, h . It is dry if water depth is zero; otherwise it is wet. However, a finite threshold
 14 (critical value) of water depth, h_c , must be defined at water boundary in real-world problems.
 15 This is essential to minimize the effects of the disturbances from different land covers, the
 16 resolution of the image, and other sources of uncertainty as suggested by Aronica *et al.*
 17 (2002). It should be noted that, the matrix, A , describing the wet-dry status of the
 18 computational cells, should be determined according to the difference between the predicted
 19 water depth and h_c so as to keep the consistence with the observed flood extent data derived
 20 from imagery. The matrix A can be simply obtained as:

$$21 \quad A(\mathbf{h}) = \begin{bmatrix} a_{11} & 0 & \dots & 0 \\ 0 & a_{22} & \dots & 0 \\ \dots & \dots & \ddots & \dots \\ 0 & 0 & \dots & a_{mm} \end{bmatrix} \quad (6)$$

22
 23 in which

$$24 \quad a_{ii} = \begin{cases} 1, & h \geq h_c \\ 0, & h < h_c \end{cases}.$$

25 The above expression shows that the matrix A dynamically changes with the flood routing.

1 For the flood extent observation derived from satellite images, the matrix A^{obs} in f^{obs} is an
 2 error matrix of observation describing wet-dry status information. It should be determined by
 3 the specific method for extracting flood extent.

$$4 \quad A^{obs}(\mathbf{h}) = \begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \dots & \dots & \ddots & \dots \\ a_{n1} & a_{n2} & \dots & a_{nn} \end{bmatrix} \quad (7)$$

5
 6 If only error variances are considered, A^{obs} can be simplified as follows:

$$7 \quad A^{obs}(\mathbf{h}) = \begin{bmatrix} a_{11} & 0 & \dots & 0 \\ 0 & a_{22} & \dots & 0 \\ \dots & \dots & \ddots & \dots \\ 0 & 0 & \dots & a_{nn} \end{bmatrix} \quad (8)$$

8 in which, a_{ii} represents the wet-dry status or the degree of certainty of a pixel being wet in a
 9 remotely sensed image. Uncertainty in the observed flood extent can be determined by, e.g.
 10 using the fuzzy set approach (Pappenberger et al., 2007b). In the positions with high
 11 uncertainty, a_{ii} will be assigned by a very low certainty degree. Low certainty can let the
 12 extent information in these positions to take little effect on the estimate of flood states.

13 A normalized weight, w (ranging from 0 to 1), is introduced in this work to describe this
 14 certainty. As shown in Fig. 1, $w = 1$ indicates a pixel being definitely wet and $w = 0$ denotes
 15 a pixel being absolutely dry. The value in between is given according to the level of certainty
 16 of a pixel being wet. The observed flood extent map can then be depicted in a 2D raster
 17 format with pixel values equal w (Fig. 1). When observations are used, they should be
 18 mapped into the model space by an observation operator.

19 Assuming $f = A\mathbf{h}$, where $\mathbf{U} = \mathbf{h}$, we can interpret f as a physically meaningful variable, i.e.
 20 a unit water volume. In a view that the weight w in A represents the certainty of a cell being
 21 wet deriving from observations but not the certainty of observed water depth, it is better to be
 22 used to constrain the discrepancy of predicted and observed water depth when defining cost
 23 function. For those overlapping regions between the predicted and observed extents, no
 24 discrepancy information should be used for assimilation and the corresponding cells should be
 25 deactivated in the computation of cost function because the predicted wet-dry status is always

1 the same as the observed one. Considering that, we further modified the cost function to
 2 become

$$3 \quad J(\mathbf{p}) = 0.5 \sum_t (\mathbf{h} - \mathbf{h}^{obs})^T (A - A^{obs})^T (A - A^{obs}) (\mathbf{h} - \mathbf{h}^{obs}) \quad (9)$$

4 The remaining difficulty is to determine the observed water depth. To overcome this, the
 5 computational domain is first separated into two parts as illustrated in Fig. 1, *i.e.* Ω_1
 6 represents the region with predicted water depth $h > h_c$ while Ω_2 is the area outside of Ω_1 . In
 7 either part, the observed water depth is assumed to be identical to the prediction when
 8 computing cost function if the wet-dry status of the computed cell is the same as the
 9 observation owing to the same flood extent. It should be noted that this assumption excludes
 10 those cells in the overlapping regions between the predicted and observed extents from the
 11 computation of cost function. In those non-overlapping regions, different assumptions have to
 12 be made, depending on the specific location under consideration. Inside Ω_1 , the observed
 13 water depth is defined to be “zero” if the cell under consideration is outside the area covered
 14 by the remotely sensed flood extent. As a result, the cost function in Ω_1 may be defined as J_1
 15 $= 0.5(1-w)^2 h^2$, where w is the certainty of flooding as described in the above paragraph.
 16 Obviously, J_1 decreases to zero when the predicted and observed extents coincide. Inside Ω_2 ,
 17 an observed water depth, h_{obs} , is required to construct the cost function in those areas covered
 18 by the remotely sensed flood extent. Numerical experiments show that it is feasible to set h_{obs}
 19 $= 2h$ to keep a similar gradient along the boundary, which leads to a cost function $J_2 = 0.5w^2(-$
 20 $h)^2$ in Ω_2 . J_2 will also decrease to zero when the predicted and observed extents coincide.
 21 Although this assumption seems to be ‘unrealistic’, it is mathematically reasonable in the
 22 computational of cost function and is effective for assimilating flood extent to drive the
 23 assimilation algorithm.

24 Taking into account all of above considerations, the cost function measuring the
 25 discrepancy of observations and predictions over computational domain may be written as:

$$26 \quad J(\mathbf{p}) = 0.5 \sum_t \left(\sum_{\Omega_1} (1-w_i)^2 h_i^2 + \sum_{\Omega_2} w_i^2 (-h_i)^2 \right) \quad (10)$$

27

1 4 Test cases

2 4.1 Dyke-break flood routing over a flat bottom

3 We first consider a flood routing process induced by a dyke break over a 10 m × 8 m
4 rectangular floodplain with a flat bottom, *i.e.* $Z_b = 0$. As shown in Fig. 2a, the left boundary
5 represents a river bank with a breach of 0.4 m in the middle. The floodplain consists of five
6 types of land covers corresponding to Manning's n 0.03, 0.04, 0.05, 0.06 and 0.07
7 respectively, from left to right. The computational domain has been discretized into a uniform
8 mesh of 0.2 m × 0.2 m resolution. During the simulation, a fixed time step of 0.01 s is used.
9 The boundary discharge hydrograph $Q_i(t)$ (half of total discharge through dyke breach to
10 floodplain) is shown in Fig. 2b and imposed on each of the two breach cells. The other three
11 lateral boundaries of the floodplain are assumed to be solid walls. The floodplain is initially
12 dry.

13 With the aforementioned 'accurate' n set for each land cover, the dyke-break flow routing
14 process is firstly simulated by the forward model for 5 s over the floodplain. Synthetic binary
15 maps of the flood extent and the time history of water stage at the middle of the domain are
16 generated and will be used as observed data during the following numerical experiments. Five
17 groups of observations are obtained, as listed in Table 1, with different combinations of
18 synthetic flood extents and/or the stage hydrograph at the central point. The assimilation
19 window is set to be 5 s, the same as the duration of the forward simulation. Three series of
20 numerical experiments are carried out by controlling n , $Q_i(t)$ or both of them, respectively.

21 In this case, a series of numerical experiments are carried out to verify the model using
22 the accurate synthetic data generated that can eliminate the disturbances of numerical and
23 measured errors encountered in an actual case.

24 4.1.1 Experiment series A

25 The control variable of the experiment series A is the distributed Manning coefficient n . Five
26 assimilation experiments are run with the same first guess of $n_0 = 0.02$ over whole floodplain,
27 but with different groups of synthetic data being assimilated. In each run, the optimal analysis
28 of flood routing over the floodplain is undertaken and the distributed n is retrieved, as
29 provided in Table 2.

1 Table 3 lists the root-mean-square (RMS) errors of water depth over the whole
2 computational domain at different output times. For the runs involving the observations of
3 Groups A and B which just assimilate flood extents, the RMS errors decrease by 78% and
4 94%, respectively. This is also clearly demonstrated by comparing the flood extents obtained
5 from different runs that assimilate different observations (Fig. 3a). After data assimilation, the
6 predicted flood extents are significantly improved and agree much more closely with the
7 ‘observed’ extents. The more observed flood extent data being assimilated, the closer the
8 results become to the ‘true’ state. In the numerical experiment involving water stage
9 observations (Group C), only the stage hydrograph is assimilated and the RMS errors
10 decrease by 82% on average. However, the predicted results at $t = 3 - 5$ s are significantly
11 different to the ‘true’ states, which can be also seen evidently from the difference between the
12 predicted and ‘true’ flood extents (Fig. 3a). The results from simulations using Groups D and
13 E observations show that the RMS errors are further decreased by about 95% after
14 assimilating both the time series of water stage and spatial flood extents.

15 As a whole, by assimilating different synthetic data, different level of improvement in
16 flood prediction has been achieved during the numerical experiments, which leads to the
17 assimilated predictions that are always much closer to the ‘true’ state. It confirms that the
18 current assimilation analysis of fusing observed flood extent and relevant information
19 improves the accuracy of flood prediction in both space and time (Fig. 5a). The quality of the
20 assimilated results can also be confirmed from the identified n , as listed in Table 2. The value
21 of n for the first land block can be accurately identified in all of the experiments, regardless of
22 whether flood extent or stage hydrograph is assimilated. However, since the stage hydrograph
23 only provides upstream information, it cannot optimize the values of n for the downstream
24 land blocks 4 and 5. Therefore the n values remain to be their initial guess in the numerical
25 experiment using the Group C observations, which leads to apparent difference between the
26 simulated and ‘true’ extents after $t = 3 - 5$ s (Fig. 3a).

27 **4.1.2 Experiment series B**

28 Taking the inflow discharge as a control variable, we carried out further numerical
29 experiments using the five given groups of observations. The initial guesses of discharge
30 calculated by $Q_i^0 = Q_i(1 + 0.6R)$ with R being a random number between 0 and 1 are imposed
31 through the inflow boundary. With the help of the minimization algorithm, the initial guesses
32 of the discharge boundary condition are corrected and the corresponding analysis results after

1 data assimilation are computed. The hydrographs of inflow discharge for numerical
2 experiments using the Groups B, C and E observations are shown in Fig. 4a. They are slightly
3 corrected to minimize the cost function.

4 The RMS errors of each run at $t = 1, 2, 3, 4$ and 5 s are listed in Table 3. They decrease
5 by 28~32% for those simulations assimilating the flood extents, but only 5% for runs just
6 assimilating point-based data provided as the stage hydrograph. Fig. 3b compares the
7 predicted and ‘true’ flood extents.

8 In this experiment series, it is interesting to note that better prediction over the whole
9 duration and spatial extent (Table 3 and Fig. 3b) is produced by assimilating flood extent,
10 even though poor prediction of water stage hydrograph at the central gauge station is found
11 (Fig. 5b). Assimilation of these data can help to estimate the inflow hydrograph and then
12 increase the assimilation accuracy. On the contrary, point-based time series data only imply
13 part of the inflow discharge information prior to the propagation time from the inlet to the
14 given points. The inclusion of point-based measurements helps to improve the accuracy of the
15 stage hydrograph at the central station but has no obvious benefit for prediction for the whole
16 duration and spatial extent.

17 **4.1.3 Experiment series C**

18 In the experiment series C, both the Manning coefficient and the inflow discharge hydrograph
19 are controlled. The same initial guesses of n and discharge are used. After running the
20 assimilation model, $Q_i(t)$ and the distributed n are corrected to minimize the cost function.
21 Although the discharge hydrograph (Fig. 4b) and n (Table 2) of each run are not well
22 identified, the predictions (Fig. 3c) obtained after assimilating the flood extents are much
23 closer to the ‘true’ one than those just assimilating point-based measurements. The RMS
24 errors of the runs assimilating the observations of Group A, B, C, D and E decrease by 50%,
25 64%, 45% , 48% and 41%, respectively, as listed in Table 3. It is encouraging to observe that
26 almost half of the RMS errors decrease for each run. As in the experiment series B, although
27 the inclusion of point-based measurements improves the accuracy of the stage hydrograph at
28 the central station, no obvious improvement is detected in terms of overall RMS errors.

1 **4.2 Flood routing over a complex bottom**

2 A test case involving flood routing over three mounds are selected to further verify the
3 performance of the proposed model under complex circumstances, which is similar to the
4 previous cases (Begnudelli and Sanders, 2007). The channel in this case has a length of 80 m
5 and a width of 15 m (Fig. 6). Three mounds inside the channel are centered at $(x, y) = (9.5,$
6 $7.5), (25, 3.5), (25, 11.5)$, respectively. The first mound at $(9.5, 7.5)$ is a square island with an
7 elevation of 2 m. The second and third ones at $(25, 3.5), (25, 11.5)$ are conical with a height
8 of 0.2 m and their elevation is assumed to decrease linearly along the radial distance from the
9 center at a rate of 1:4. The computational domain is discretized into a uniform mesh of $1 \text{ m} \times$
10 1 m resolution. The channel bed is initially dry. Cases with both lumped and distributed bed
11 roughness are investigated, respectively. A constant Manning's $n = 0.03$ is set up for the cases
12 with lumped roughness. For the cases with distributed roughness, the Manning's n are set to
13 0.05 when $x \leq 10 \text{ m}$, 0.04 when $10 \text{ m} < x \leq 20 \text{ m}$, 0.03 when $20 \text{ m} < x \leq 30 \text{ m}$, and 0.02 when
14 $x > 30 \text{ m}$. The steady unit discharge of $0.2 \text{ m}^2/\text{s}$ is imposed at $x = 0$. The dyke-break flood
15 routing is firstly simulated by the forward model for 45 s using a fixed time step of 0.05 s.
16 The assimilation window is set to be 45 s, the same as the duration of the forward simulation.
17 Synthetic flood extent data used in the assimilation are generated based on the simulated
18 results.

19 In this test case, a number of numerical experiments are carried out to verify the use of
20 the proposed method under complex circumstances. By using different water depth thresholds,
21 h_c for determining observed flood extent, the model independence on the selection of the
22 thresholds are first validated. Then, the influences of the uncertainties in flood extent data on
23 the assimilation results are examined.

24 **4.2.1 Independence on water depth threshold**

25 To validate the independence of assimilation on the selection of water depth threshold, the
26 numerical experiments with a lumped (constant) roughness are conducted. Based on the
27 simulated flood process using a lumped Manning's $n = 0.03$, we generate the observed flood
28 extents at $t = 24 \text{ s}$, 36 s and 45 s using different water depth thresholds, i.e. $h_c = 0.0001 \text{ m}$,
29 0.001 m and 0.01 m . By controlling the lumped Manning's n , the flood extents are assimilated
30 into the flood dynamic model. The unknown (or guessed) Manning's coefficients are
31 successfully identified after assimilation of a single flood extent at different times. The RMS

1 errors of water depth ($RMSE_h$) decrease significantly in all cases after the assimilation of the
2 given single flood extent data (Fig. 7 and Table 4) although the Manning's coefficients are not
3 well identified in the case that assimilates the flood extent at $t = 24$ s when $h_c = 0.0001$ m.
4 These results indicate that the assimilation performance and accuracy are not sensitive to the
5 selection of water depth threshold in the current method, provided it is in a reasonable range.
6 It should note that water depth threshold is a finite magnitude that presents water depth of
7 water boundary in real-world problems. Thus, the threshold cannot select arbitrarily, but keep
8 the value be close to real water depth at water boundary line as possible. Sensitivity analysis
9 may be conducted if required.

10 **4.2.2 Influence of flood extent uncertainty**

11 In the previous numerical experiments, the observations are assumed to be accurate. However,
12 real observed flood extent may be full of uncertainty due to the contamination caused by
13 complex environment. To examine its influence on the model performance, assimilation of
14 flood extent data with uncertainty is tested. We assume that the flood areas are completely
15 wet if $h > 0.01$ m, completely dry if $h < 0.001$ m, and partially wet or dry if $0.001 \text{ m} < h <$
16 0.01 m. Therefore, the weight or certainty degree of cell being wet, w over whole flood areas
17 can be determined by $w = \max(\min(\max(h, 0.001) - 0.001) / (0.01 - 0.001), 1), 0)$. This
18 results in a grid-based flood extent map for assimilation experiments.

19 Two groups of assimilation experiments with respectively lumped and distributed bed
20 roughness are conducted. For the cases with lumped bed roughness, the accurate weights
21 calculated from water depth are first used in our assimilation experiments (Case U-24, U-36
22 and U-45, as presented in Table 4). The successfully identified Manning's n and the decrease
23 of near 99% in $RMSE_h$ (Fig. 7 and Table 4) show that the flood extent uncertainty can be
24 correctly accounted for in our proposed method. In realistic problems, the ideal weight is
25 almost impossible to be accurately obtained. Considering that, more challenging cases are
26 designed to verify the method (Case B-24, B-36 and B-45, as presented in Table 4). In these
27 three experiments, w is assumed to be 0.5 for areas with uncertainty ($0.001 \text{ m} < h < 0.01 \text{ m}$).
28 After assimilating the given single flood extent, the controlling n is again successfully
29 identified again, which leads to a dramatic decrease in $RMSE_h$ (Fig. 7 and Table 4).

30 Furthermore, the cases with distributed bed roughness are also considered (Case B2-24,
31 B2-36, B2-45, B2-36&45, B2-24&45, and B2-24&36). We still use the observations with

1 inaccurate weight, namely $w = 0.5$ in areas with $0.001 \text{ m} < h < 0.01 \text{ m}$. After assimilating the
2 given single flood extent, the RMSE_h in each experiment is apparently reduced, although the
3 ‘true’ distributed Manning’s n cannot be achieved for these cases (Table 4). However, when
4 new observations are available, the RMSE_h can decrease significantly and the distributed
5 Manning’s n can be identified to become much closer to the ‘true’ values. For example, the
6 RMSE_h decreased by 90% when assimilating the single flood extent at $t = 24 \text{ s}$, and by about
7 93% when further assimilating flood extent at $t = 36 \text{ s}$ or 45 s are used (Table 4). These results
8 indicate that detailed content in the flood extent is important for the assimilation performance.
9 Assimilation experiments also show that the proposed method can directly handle complex
10 flood extents, e.g. the isolated islands inside the flooded areas, with grid-based flood extents
11 defined to be compatible with the numerical grids.

12

13 **5 Assimilation of an actual remotely sensed flood extent**

14 Based on the findings of the previous numerical experiments, this section intends to
15 investigate further the potential of the proposed data assimilation method using actual satellite
16 remote sensing data (here MODIS). The study area, Mengwa Flood Detention Area (MFDA),
17 is located at Fuyang, Anhui Province of China, the middle reach of the Huaihe River. It is the
18 most important region for flood control within this river basin. MFDA covers a narrow and
19 elongated area of 180 km^2 (Fig. 8a), with a population of 148,000 farming 120 km^2 of
20 cropland. The domain is discretized using an unstructured grid (Fig. 8b) consisting of 1222
21 nodes and 1136 quadrilateral and triangular cells. The size of the cell edges ranges from 200m
22 to 400m. The bed elevation at each cell is extracted from a digital elevation model (DEM) of
23 100m resolution, which is generated from a 1:2500 topographic map.

24 The data assimilation experiments are carried out based on the flood routing process over
25 MFDA induced by the flood diversion event happened in the summer of 2007. From 29 June
26 to 15 July 2007, persistent heavy rain was experienced in the Huaihe River basin. To reduce
27 the risk of severe flooding that might cause significant economic and human loss downstream,
28 MFDA was operated by opening the Wangjiaba gate to receive flood water from the Huaihe
29 River starting from 4:28 (UTC) 10 July, with an order from the Chinese central government.
30 Until 12 July 2007, the total diverted volume reached about $0.25 \times 10^9 \text{ m}^3$, which effectively
31 stored and retained flood water and hence reduced flood risk. Fig. 8 plots the 45-hour inflow
32 hydrograph to MFDA through the flood gate, from 4:28 (UTC) 10 July 2007.

1 Two MODIS instruments on the Terra and Aqua spacecraft platforms have provided
 2 daily measurements with the global coverage since 1999. The 250 m resolution with daily
 3 revisits makes them particularly suitable for monitoring the changes of flooding over a
 4 floodplain. Herein, we downloaded one scene of Aqua-MODIS Level-1B and Geo-location
 5 data covering the whole MFDA from the Level 1 and Atmosphere Archive and Distribution
 6 System (LAADS). The MODIS data acquired at 6:00 (UTC) with 250 m resolution capturing
 7 the flood routing during the flood diversion event. Although MFDA was partly covered by
 8 light cloud at that moment, the image is of sufficient quality to identify the flood extent.

9 A simple method is adopted to extract the flood extent based on the luminance of the
 10 composite image from the Band 7-2-1 combination. The luminance L of each pixel is firstly
 11 calculated using the following formula (Gonzales and Woods, 2002)

$$12 \quad L = 0.299b_7 + 0.587b_2 + 0.114b_1 \quad (11)$$

13 where b_7 , b_2 and b_1 are the digital values of Band 7, Band 2 and Band 1. The luminance image
 14 is shown in Fig. 9a, after setting the pixel to null value where heavy cloud covered. The flood
 15 extent is then easily extracted over MFDA by setting a critical value of luminance as a
 16 threshold to separate the water area from image. However, due to the fact that the extraction
 17 of flood extent may be affected by the land surface, such as trees and vegetation cover (Smith,
 18 1997), and the current image is in relatively low resolution of 250 m, there exists certain
 19 uncertainties in the boundary water line. In light of this, the concept of membership degree
 20 from the Fuzzy Set Theory (Huang, 2000; Nguyen and Walker, 2006) is introduced as an
 21 indicator to determine the flood extent. The degree of membership w quantifies the grade of
 22 membership of an element to a fuzzy set, which is herein the possibility of a pixel being wet.
 23 A membership function may be written as (Huang, 2000)

$$24 \quad w = \begin{cases} 1 & , L_i \leq a \\ 0.5 + 0.5 \sin\left(\frac{\pi}{b-a} \cdot \left(L_i - \frac{a+b}{2}\right)\right) & , a < L_i \leq b \\ 0 & , L_i \geq b \end{cases} \quad (12)$$

25 where L_i is the luminance of pixel I , a and b are the upper and lower bounds of the luminance
 26 to separate the water and land. The degree of membership $w = 0$ and $w = 1$ mean that pixel i is
 27 completely dry and wet, respectively. A value between 0 and 1 characterize fuzzy members
 28 that are only partially wet/dry. Misclassification may also occur for this method. For those

1 areas covered by heavy clouds, null values are given to the corresponding pixels and these
2 cells are excluded from the evaluation of cost function.

3 From visual interpretation, we can identify that those areas with luminance L_i less than
4 110 are covered by water and hence $a = 110$. The upper bound b is more difficult to determine
5 owing to the effects of complicated land cover. In this paper, $b = 121$ and 126 are respectively
6 examined. The flood extents retrieved from fixed thresholds 110 , 121 and 126 are shown in
7 Fig. 9b-d.

8 Taking the membership degree computing from Eq. (12) as a weighting factor w and
9 substituting it into Eq. (10), the cost function J is obtained as

$$10 \quad J = \frac{1}{2} \left[0.5 \left(1 - \frac{h - h_c}{|h - h_c|} \right) - w \right]^2 h^2 \quad (13)$$

11 Based on this cost function, data assimilation experiments are conducted with a computational
12 time step of 12 s. The simulation time is set to 36 hours, starting from the gate opening at 4:28
13 (UTC) 10 July 2007. The actual discharge hydrograph for flood diversion to MFDA as shown
14 in Fig. 8c is imposed through the inflow discharge boundary. Simulation starts from an
15 originally dry floodplain. The critical water depth to derive the boundary line of flood extent
16 from remote sensing data, h_c , is set to 0.2 m.

17 The Manning roughness coefficient, n was assumed to be constant over the whole
18 computational domain because of little knowledge about land use or cover. The control
19 variable of the numerical experiments is the lumped Manning's n , namely the control vector
20 contains only one element. Giving different n_0 (Table 5), we carried out six numerical
21 simulations, assimilating one single remotely sensed flood extent from MODIS data at $t =$
22 25.5 h with $b = 121$ and 126 . The minimized cost functions of the experiments with $b = 126$
23 are less than those with $b = 121$, but the values are close to their minimum for an independent
24 b (Table 5).

25 Fig. 10 shows the computed flood extents before and after data assimilation. It can be
26 observed that consistent flood extents are obtained in the assimilation experiments with
27 different n_0 by assimilating the flood extent information from MODIS data. Also, it is obvious
28 that the computed flood extents are improved after data assimilation has been performed in
29 both experiments. The estimated flood extents are much closer to the one extracted from
30 MODIS (Fig. 9). The findings are encouraging, which indicate that hydraulic information

1 from satellite imagery can be directly assimilated into a 2D dynamic flood model via the
2 flood extent using the cost function as suggested in this work.

3 We also identify a consistent n in the assimilation experiments with different n_0 , as listed in
4 Table 5. The identified n is about 0.2~0.25, partly depending on n_0 . It is greater than the
5 empirical value of a normal floodplain, which may be caused by the loss of accuracy from the
6 low resolution MODIS data and uncertainties in the domain topography, *etc.* In addition,
7 minimization procedure of the 4D-Var method seems to be trapped into the local minimal
8 value for different n_0 in our experiments. Taking the experiments with $b = 126$ as an example,
9 the optimized n is 0.208 if $n_0 = 0.025$ or 0.030; but it is close to 0.24 if $n_0 = 0.5$ or 0.8. After
10 checking the relationship between the cost function and n (Fig. 11), two local minimal values
11 of cost function exist when n is close to 0.20 or 0.24. This leads to different estimations of n
12 in our experiments. The double minima may originate primarily from the assumption of a
13 constant n over the study area with heterogeneous landscapes, which is inconsistent with the
14 actual situation. Furthermore, insufficient data (a single low resolution flood extent) may also
15 lead to the appearance of double minima in the cost function.

16

17 **6 Summary and conclusions**

18 To the best of our knowledge, no attempt has been reported to directly assimilate the flood
19 extent data into a 2D flood model in the framework of 4D-Var. In this work, a 4D-Var
20 method incorporated with a new cost function is introduced to advance this research topic.
21 The new approach has been validated using a series of numerical experiments undertaken for
22 an idealized test case before applying to a realistic simulation in MFDA. The main results of
23 this study are summarized as follows:

- 24 ● A new cost function is defined to facilitate assimilation of flood extent data directly using
25 a 4D-Var method. While it can efficiently help the 2D flood model to assimilate the
26 spatially distributed flood dynamic information of the flood extent data from remote
27 sensing imagery, the current approach does not require those additional steps of retrieving
28 water stage (Hostache et al., 2010). Since the flood extent is much easier to map from
29 remote sensing image than water stage and gradients (Schumann et al., 2009), the present
30 scheme provides a more promising way of data assimilation for flood inundation
31 modeling. However, as a new data assimilation method for flood modeling, an interesting
32 research question to answer is whether the direct assimilation of flood extent data can

1 improve the assimilation accuracy comparing with the assimilation of water level
2 observations retrieved from the same data sources of satellite imagery. This is worth a
3 comprehensive comparative study in the future, which may then provide useful guideline
4 for the practical applications of remote sensing data assimilation.

- 5 ● Flood extent is a type of spatially distributed data and implicitly implies hydraulic
6 information of flood routing. The observed flood extent data may provide an alternative
7 to obtaining a denser time series as stated by Roux & Dartus (2006) and to compensating
8 for unavailable field measurements during a flood event (Lai and Monnier, 2009). The
9 assimilation of flood extent data is suitable for improving flood modeling in the
10 floodplains or similar areas (e.g. seasonal lakes with significant wetting and drying
11 processes) with slowly varying bed-slopes. However, it should be noted that this
12 approach has its own limitation. If the flood extent does not contain enough hydraulic
13 information, the assimilation exercise may fail. For example, in the case of flood
14 inundation in a domain constrained by steep slopes, the water stage but not the flood
15 extent varies evidently with time. Since the extent data do not actually represent the
16 physical evolution of such a flood event, they are not suitable for assimilation. Therefore,
17 the correlation between extent and flood dynamics must be established before applying
18 the current data assimilation scheme.
- 19 ● The results of flood modeling are much improved by successfully estimating the
20 roughness parameter over a floodplain even though the low-resolution MODIS data (250
21 m) is adopted in the application of MFDA. This implies that the proposed method may
22 extend the usable data sources for assimilation to the imageries from most of currently in-
23 orbit satellites that provide large spatial and temporal coverage.

24 Overall, this study shows that the assimilation of the flood extent data is effective in
25 improving flood modeling practice. Future work should be carried out to understand the full
26 potential of this new way of making use of spatially distributed data from various existing
27 satellites in data assimilation.

28 29 **Acknowledgements**

30 The research was supported by National Key Basic Research Program of China (973
31 Program) (2012CB417000) and the National Natural Science Foundation of China (Grant No.

1 50709034 and No. 41071021). The authors also thank Dr. Guy Schuman, Renaud Hostache
2 and anonymous reviewer for their valuable comments for improving paper's quality.
3

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- 4

1 **Tables**

2 Table 1. The five groups of observations used in the test case of dyke-break flood routing
3 over a flat bottom.

	Description of observations
Group A	Flood extent at $t = 5$ s
Group B	Flood extents at $t = 1, 3$ and 5 s
Group C	$Z(t)$, time history of water stage at central position of floodplain (time interval of measurement is 0.2 s)
Group D	Flood extent at $t = 5$ s and $Z(t)$
Group E	Flood extents at $t = 1, 3$ and 5 s and $Z(t)$

4

1 Table 2. The identified Manning's n in experiment series A and C

	observations	1	2	3	4	5
True value	-	0.03	0.04	0.05	0.06	0.07
First guess	-	0.02				
Series A	Group A	0.031	0.053	0.053	0.028	0.042
	Group B	0.030	0.038	0.054	0.036	0.074
	Group C	0.030	0.040	0.050	0.020	0.020
	Group D	0.030	0.040	0.050	0.042	0.070
	Group E	0.030	0.04	0.05	0.038	0.072
Series C	Group A	0.024	0.061	0.118	0.099	0.220
	Group B	0.031	0.069	0.057	0.032	0.046
	Group C	0.020	0.052	0.040	0.020	0.020
	Group D	0.052	0.047	0.052	0.039	0.049
	Group E	0.047	0.077	0.026	0.023	0.030

2

1 Table 3. The RMS errors of water depth at $t = 1, 2, 3, 4$ and 5 s in experiment series A, B and
 2 C.

Control Variables	Time(s)	Guess	Group A	Group B	Group C	Group D	Group E
n	1	0.0040	0.0009	0.0002	0.0000	0.0000	0.0000
	2	0.0183	0.0063	0.0010	0.0001	0.0000	0.0000
	3	0.0313	0.0074	0.0017	0.0039	0.0009	0.0012
	4	0.0396	0.0073	0.0026	0.0081	0.0018	0.0022
	5	0.0436	0.0076	0.0032	0.0117	0.0022	0.0028
Q_{in}	1	0.0064	0.0051	0.0044	0.0037	0.0049	0.0049
	2	0.0097	0.0071	0.0076	0.0082	0.0083	0.0086
	3	0.0109	0.0081	0.0082	0.0125	0.0091	0.0091
	4	0.0132	0.0074	0.0076	0.0128	0.0069	0.0071
	5	0.0102	0.0067	0.0068	0.0103	0.0065	0.0064
n and Q_{in}	1	0.0095	0.0065	0.0050	0.0086	0.0073	0.0062
	2	0.0245	0.0102	0.0108	0.0142	0.0178	0.0196
	3	0.0373	0.0217	0.0149	0.0136	0.0198	0.0239
	4	0.0410	0.0191	0.0137	0.0260	0.0196	0.0230
	5	0.0514	0.0243	0.0142	0.0272	0.0201	0.0235

3

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5

1 Table 4. The water depth threshold, h_c , the assimilated observations, identified Manning's n ,
 2 and time-averaged RMS errors of water depth ($RMSE_h$) in the test case of dyke-break flood
 3 routing over three mounds

Cases	h_c (m)	Observations	n	n_2	n_3	n_4	Time-averaged $RMSE_h$ (m)
Lumped Manning's n							
True			0.030				
Guess			0.015				0.0222
H1-24	0.0001	Single flood extent at $t = 24$ s	0.028				0.0035
H1-36		= 36 s	0.030				0.0003
H1-45		= 45 s	0.030				0.0002
H2-24	0.001	= 24 s	0.030				0.0000
H2-36		= 36 s	0.030				0.0007
H2-45		= 45 s	0.030				0.0004
H3-24	0.01	= 24 s	0.030				0.0003
H3-36		= 36 s	0.030				0.0000
H3-45		= 45 s	0.031				0.0006
U-24	0.01-0.001	= 24 s	0.031				0.0008
U-36		= 36 s	0.030				0.0001
U-45		= 45 s	0.030				0.0002
B-24	0.01-0.001	= 24 s	0.030				0.0005
B-36		= 36 s	0.030				0.0000
B-45		= 45 s	0.032				0.0026
Distributed Manning's n							
True			0.050	0.040	0.030	0.020	
Guess			0.015	0.015	0.015	0.015	0.0327
B2-45	0.01-0.001	Single flood extent at $t = 45$ s	0.023	0.028	0.030	0.036	0.0199
B2-36		= 36 s	0.031	0.039	0.041	0.032	0.0111
B2-24		= 24 s	0.045	0.048	0.027	0.017	0.0033

B2-36&45	Two flood extents at $t = 36$ s and 45 s	0.039	0.039	0.041	0.025	0.0069
B2-24&45	= 24 s and 45 s	0.048	0.046	0.026	0.019	0.0023
B2-24&36	= 24 s and 36 s	0.047	0.045	0.029	0.021	0.0022

1 Table 5. The identified n and the final cost functions in the application to MFDA

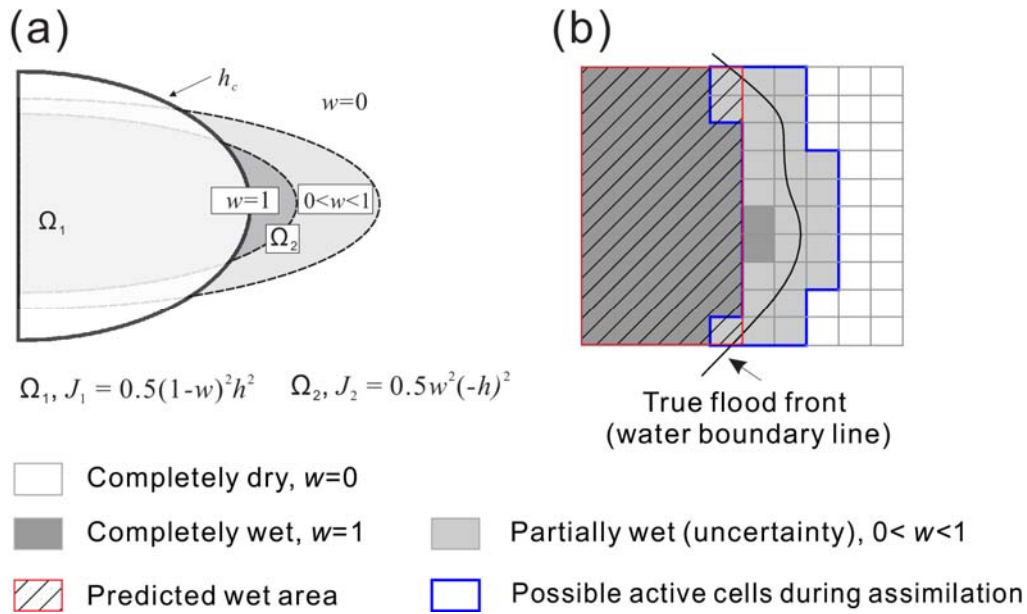
Upper bound of luminance, b	Final function, J	cost	Decrease rate of cost function (%)	Initial guess of n , n_0	Identified n
	28.118		81.2	0.025	0.208
126	28.127		78.0	0.030	0.208
	28.432		14.6	0.500	0.249
	28.319		24.2	0.800	0.240
121	49.071		70.6	0.030	0.219
	48.937		18.6	0.800	0.240

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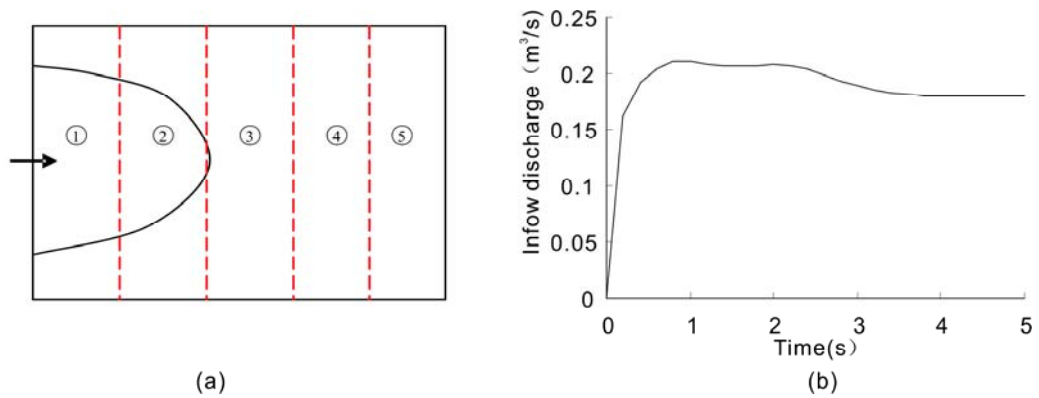
1 **Figure Captions**

2



3
4 Fig. 1 Definition of a cost function. (a) The concept map; (b) Grid-based map for
5 showing the specific definition of cost function and possible active cells during data
6 assimilation.

7

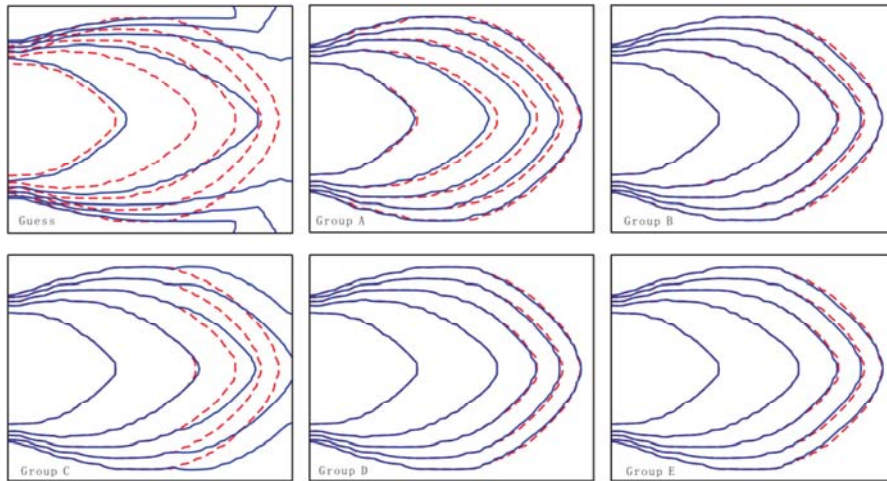


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9 Fig. 2 Idealized test of flood routing over a rectangular floodplain induced by dyke
10 breach: (a) computational domain; and (b) hydrograph of the inflow discharge $Q_i(t)$.

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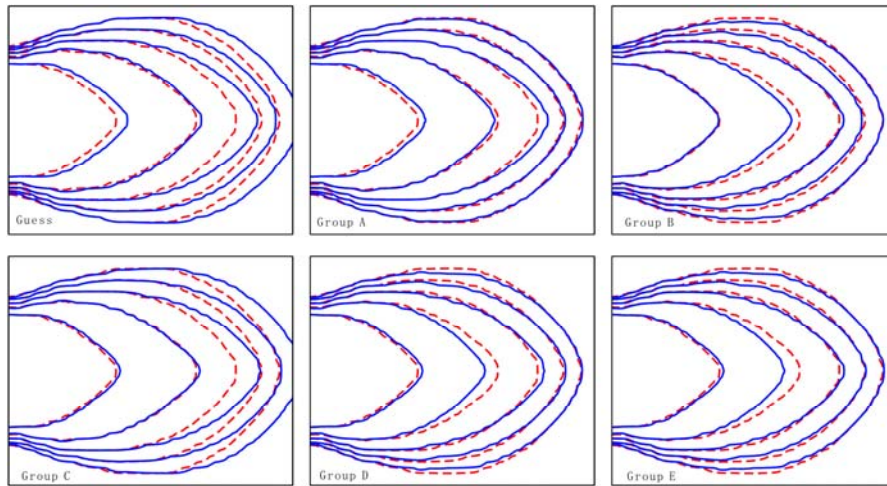
(a)



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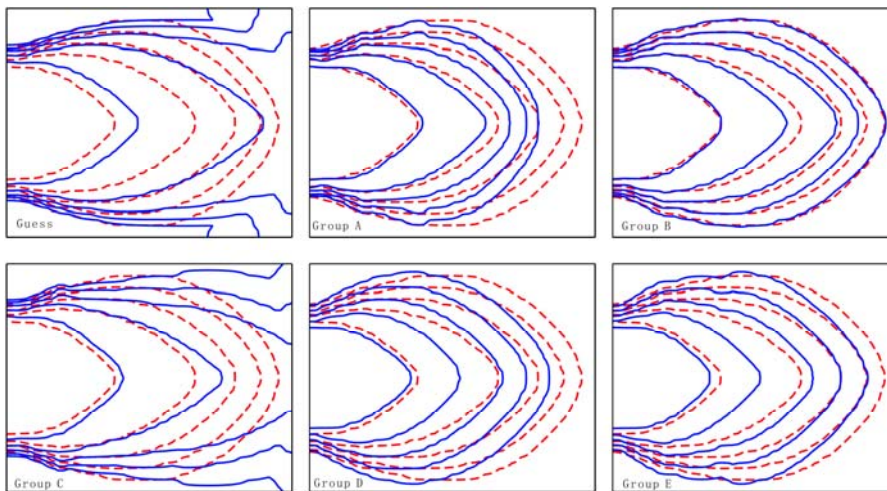
(b)



3

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(c)

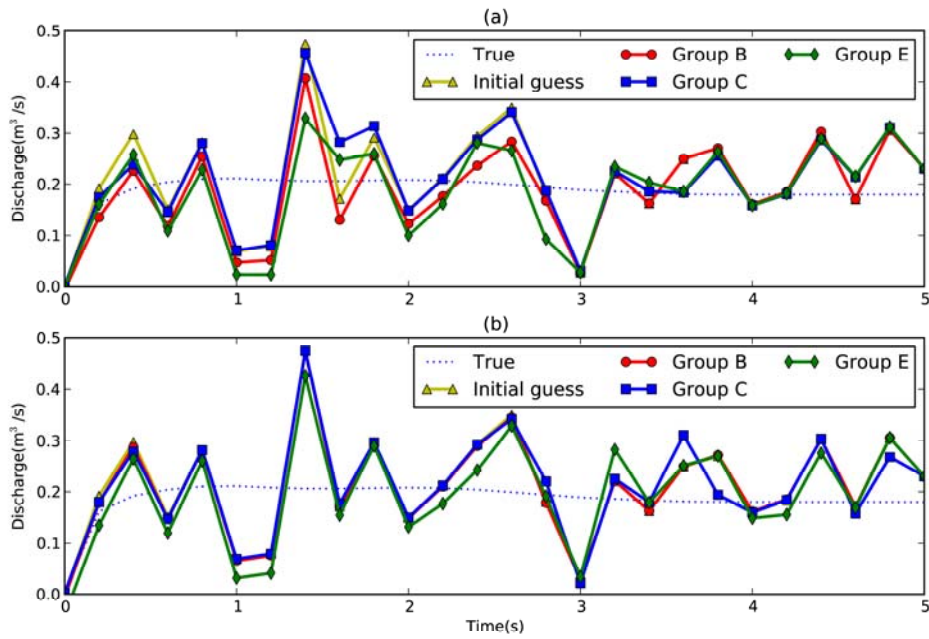


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1 Fig. 3 Comparison of the predicted and ‘true’ flood extents at $t = 1, 2, 3, 4$ and 5 s for
 2 different simulations using guessed Manning’s n and by assimilating the observations
 3 of Group A, B, C, D and E: (a) experiments series A; (b) experiments series B; and (c)
 4 experiments series C. The solid and dashed lines mark, respectively, the predicted and
 5 ‘true’ flood extents.

6



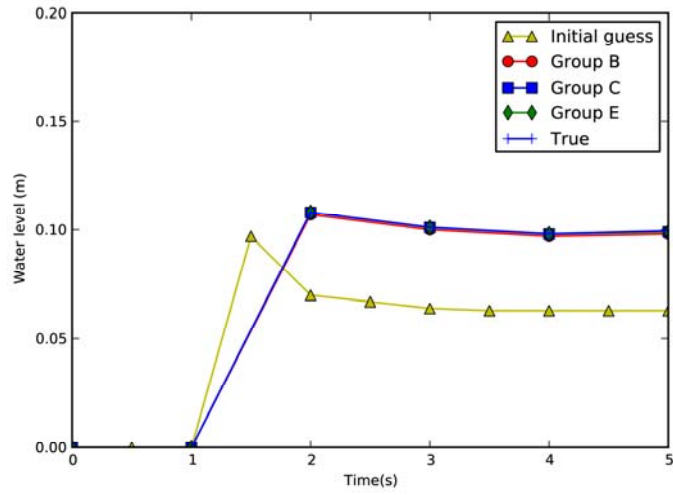
7

8 Fig. 4 Identified discharge hydrograph from (a) experiment series B; and (b)
 9 experiment series C.

10

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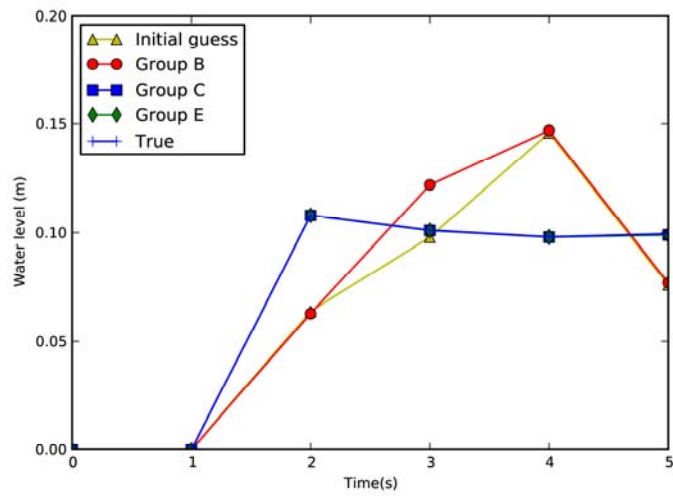
(a)



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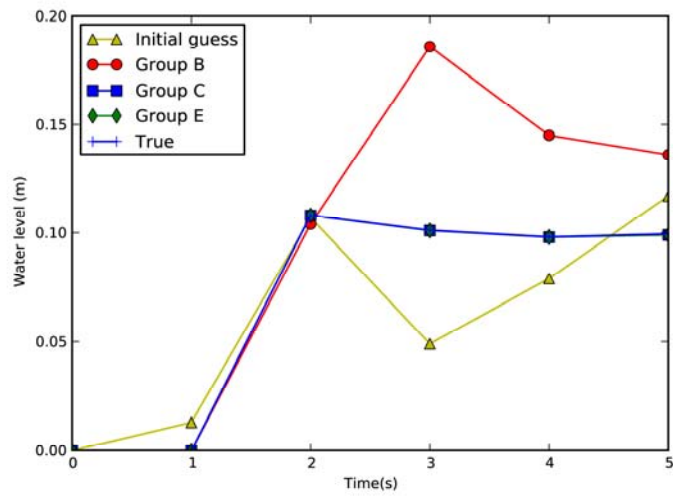
(b)



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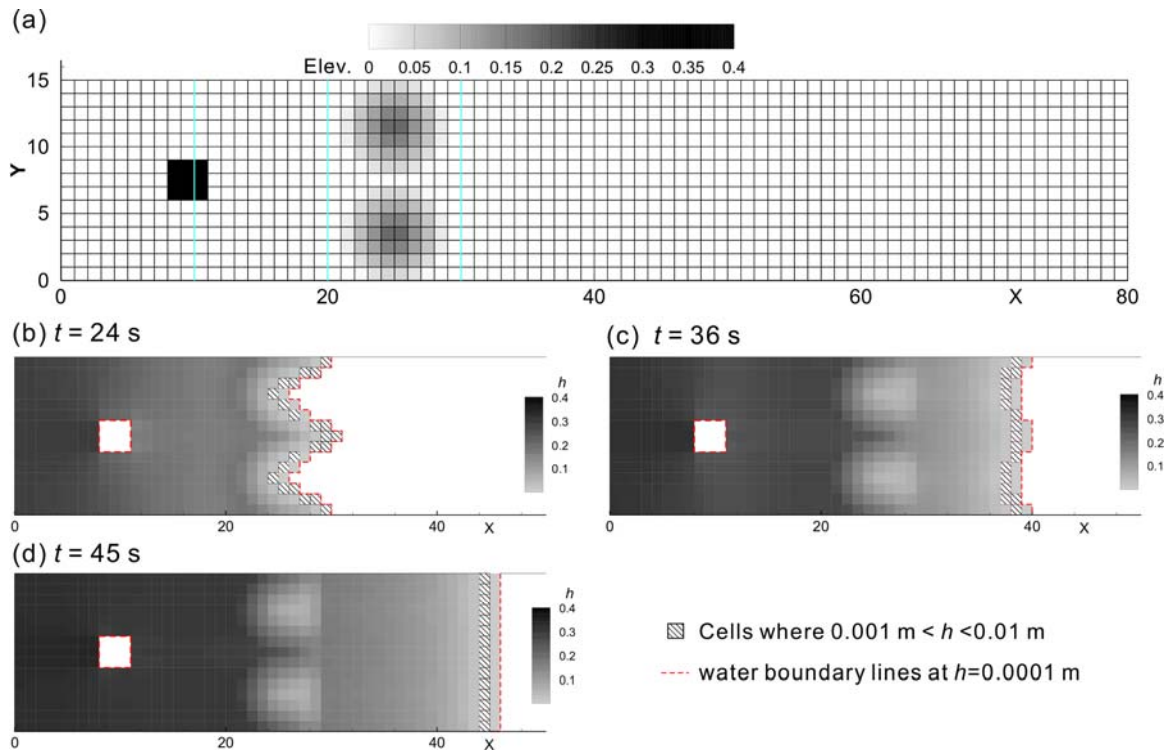
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(c)

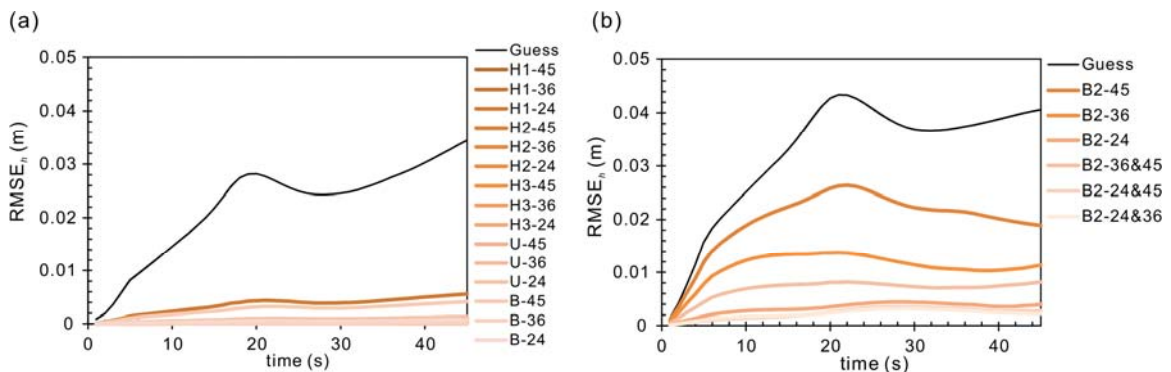


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1 Fig. 5 Water stage validation at the gauge point in (a) experiment series A; (b)
 2 experiment series B; and (c) experiments series C.
 3

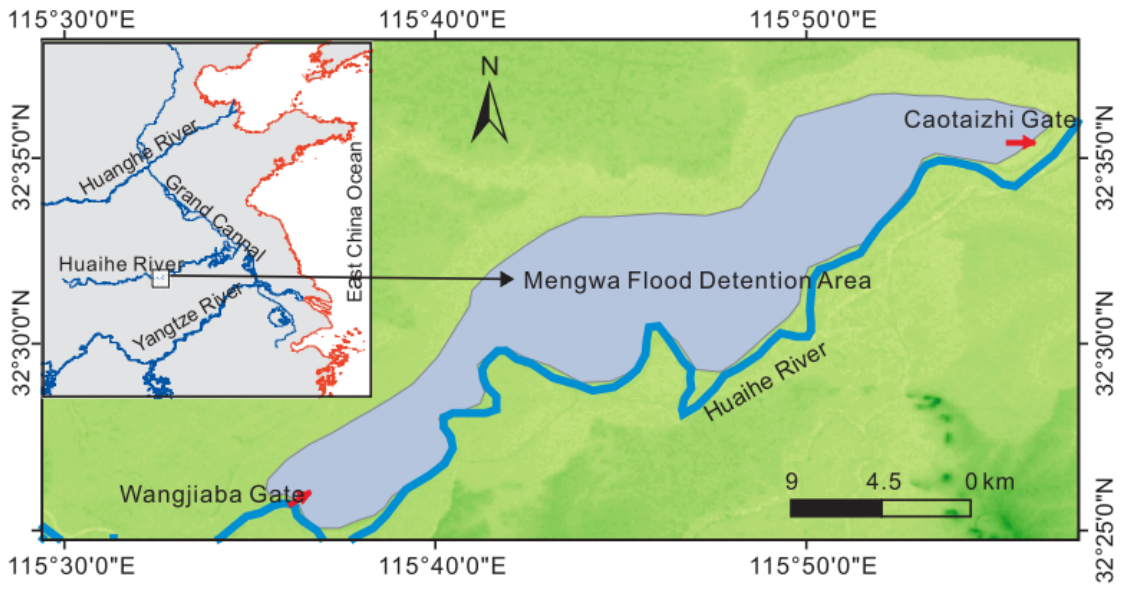


4
 5 Fig. 6 Test case of a flood routing over three mounds. (a) Bed elevation and
 6 computational grids; (b) Flood extent and water depth contour at $t = 24$ s; (c) Flood
 7 extent and water depth contour at $t = 36$ s; and (d) Flood extent and water depth
 8 contour at $t = 45$ s.

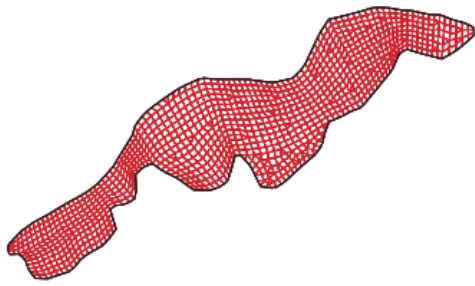


9
 10 Fig. 7 The time series of RMS errors of water depth ($RMSE_h$) in assimilation
 11 experiments with (a) lumped Manning's n , and (b) distributed Manning's n .

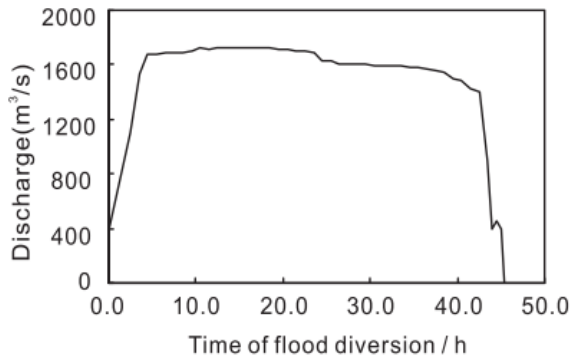
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(a)



(b)

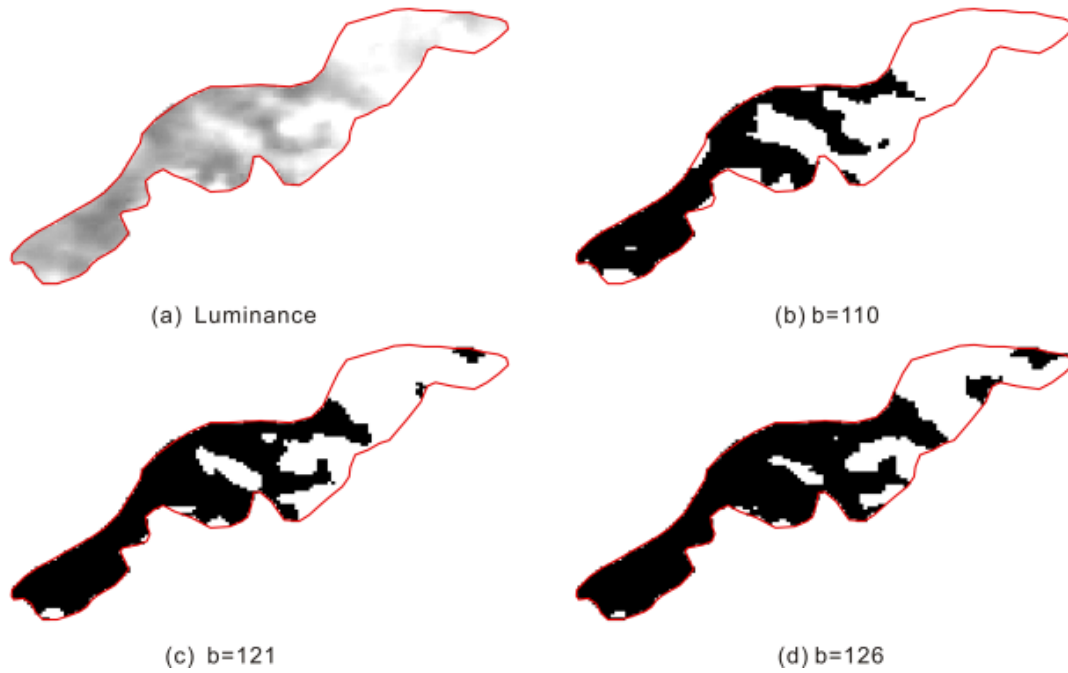


(c)

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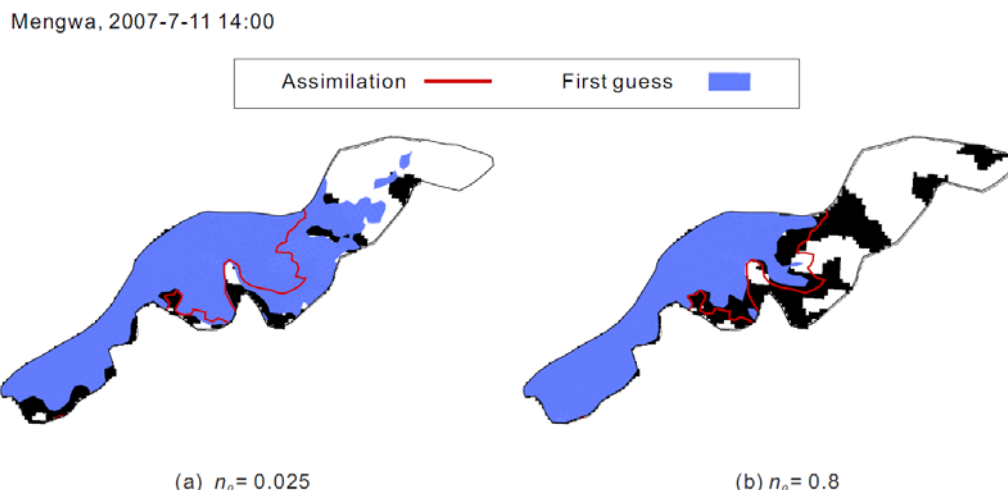
3 Fig. 8 (a) Mengwa Flood Detention Area (MFDA); (b) unstructured grid; (c) inflow
4 discharge hydrograph.

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Fig. 9 (a) Luminance of MODIS image with Band 7-2-1; (b) flood extent extracted from the fixed digital number threshold 110; (c) flood extent extracted from the fixed digital number threshold 121; and (d) flood extent extracted from the fixed digital number threshold 126.

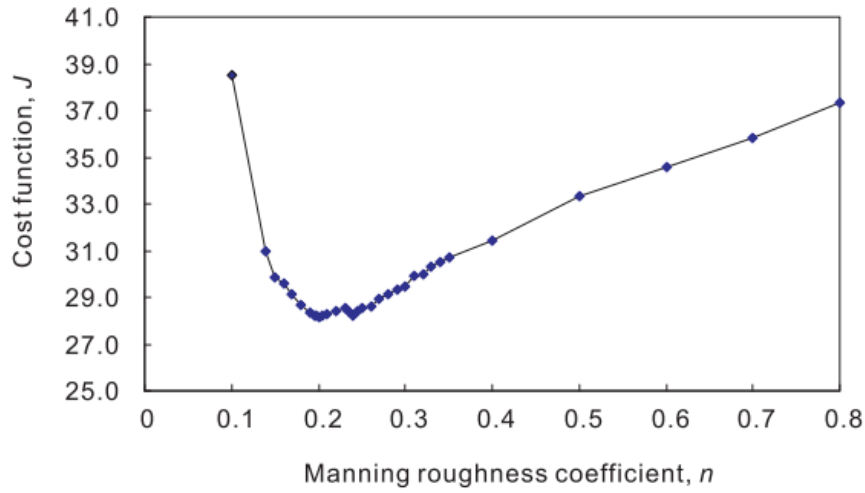


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Fig. 10 Comparing flood extents obtained before and after assimilation of the remotely sensed flood extent from MODIS image specified by $b = 126$ (background

1 map) when (a) $n_0 = 0.025$; and (b) $n_0 = 0.8$. The solid line represents the boundary of
2 the flood extent after assimilation where water depth is equal to h_c . The filled area is
3 the flood extent computed by forward model with n_0 .

4



5

6 Fig. 11 The relationship between the cost function and the Manning's n .

7