

1 **Comprehensive evaluation of water resources security in the Yellow River**
2 **basin based on a Fuzzy multi-attribute decision analysis approach**

3

4 **K. K. Liu^{1,2}, C. H. Li^{1*}, Y. P. Cai^{3,4*}, M. Xu¹, and X. H. Xia¹**

5

6 ¹Ministry of Education Key Laboratory of Water-sediment Science, School of
7 Environment, Beijing Normal University, Beijing, 100875, China

8 ²CERI eco Technology Co., LTD, Beijing 100053, China

9 ³State Key Laboratory of Water Environment Simulation, School of Environment,
10 Beijing Normal University, Beijing 100875, China

11 ⁴Institute for Energy, Environment and Sustainable Communities, University of
12 Regina, 120, 2 Research Drive, Regina, Saskatchewan S4S 7H9, Canada

13

14 [Received: 9 December 2013 – Accepted: 10 December 2013 – Published:](#)

15 Correspondence to: C. H. Li (chunhuili@bnu.edu.cn) and Y. P. Cai
16 (yanpeng.cai@bnu.edu.cn)

17 Published by Copernicus Publications on behalf of the European Geosciences
18 Union.

1 **Abstract**

2 In this paper, a fuzzy multi-attribute decision analysis approach (FMADAA) was
3 developed for supporting the evaluation of water resources security in nine
4 provinces within the Yellow River basin. A numerical approximation system and
5 a modified left-right scoring approach were adopted to cope with the uncertainties
6 in the acquired information. Also, four conventional multi-attribute decision
7 analysis(MADA) methods were implemented in the evaluation model for impact
8 evaluation, including simple weighted addition (SWA), weighted product (WP),
9 cooperative game theory (CGT) and technique for order preference by similarity
10 to ideal solution (TOPSIS). Moreover, several aggregation methods including
11 average ranking procedure, borda and copeland methods were used to integrate
12 the ranking results, helping rank the water resources security in those nine
13 provinces as well as improving reliability of evaluation results. The ranking
14 results showed that the water resources security of the entire basin was in critical
15 conditions such as the insecurity and absolute insecurity states, especially in
16 Shanxi, Inner Mongolia and Ningxia provinces in which water resources were
17 lower than the average quantity in China. Hence, the improvement of water
18 eco-environment statuses in the above-mentioned provinces should be prioritized
19 in the future planning of the Yellow River basin.

1 **1 Introduction**

2 Water is a fundamental resource for sustainable development of human society.
3 Also, it is a critical factor for maintaining natural ecosystems. Water conflicts
4 between human and ecosystems are posing great challenges for maintaining
5 sustainability of water resources at the watershed scale. Along with the increasing
6 consumptions of water resources by multiple users, water security crisis becomes
7 an emerging issue that is facing by decision makers in many regions. How to
8 allocate the water resources effectively among the multiple water users without
9 causing damages on local ecosystems? A balance between human beings and
10 ecosystems need to maintain based on the introduction of water security not only
11 to human society but also to local ecosystems. It is thus desired to develop an
12 effective method to help evaluate water security and facilitate the management of
13 water resources scarcity ([Brown and Hilweil, 1987](#); [Loucks, 2000](#); [WWAP, 2002](#);
14 [Chen, 2004](#); [Zhang, 2010](#)).

15
16 Water resources security is a concept proposed in late 20th century ([Jiang, 2001](#);
17 [Jia et al., 2002](#); [Zheng, 2003](#); [Xia and Zhang, 2007](#)). It is generally believed that at
18 a certain stage of social and economic development, water supply that could
19 ensure both the quality and quantity is able to meet the needs of human survival,
20 social progress, and economic development and to maintain a good ecological
21 environment on the basis of not exceeding the carrying capacity of water
22 resources and water eco-environment. This implies the desire to safeguard
23 sustainable economic and social development based on sustainable water
24 resources utilization. The evaluation and insurance of water security are the core
25 issues of sustainable water resources management. Conventionally, water
26 resources supporting capacity is considered as a basic water security measure
27 which can be adopted for supporting the establishment of an evaluation indicator
28 system. At the same time, some scholars argued that water resources security's
29 core point lies in the sustainability of water use. If water resources in a regiona
30 can be used sustainably, then, its water can be considered safe. According to this
31 theory, the indicator system can be established including targets, criterion and
32 indicators. The evaluation can be carried on in accordance with the indicators in
33 five aspects including water resources availabilities, water resources exploitation

1 and utilization efficiencies, external eco-environment conditions, water resources
2 deployment conditions, and ability in managing water resources (Jia and Zhang,
3 2003; Zhang and Jia, 2003; Jia et al., 2004; Zhang et al., 2005, 2008)..

4
5 At the same time, a lot of evaluation methods were developed for evaluating water
6 resources sustainability, such as those based on statistic analysis, data
7 envelopment analysis, principal components analysis, system dynamics method,
8 “Pressure-state-response” modeling, set pair analysis, vague set evaluation, fuzzy
9 element model, water poor exponential method, and artificial neural networks,
10 element analysis and so forth. Many scholars have applied these methods to many
11 real-world cases (Han et al., 2001; Cong, 2007; Zhu et al., 2008). Because the
12 uncertain factors in the indicator system have great influences on the scientificity
13 of evaluation, in order to deal with non-linear optimization of the evaluation
14 process, the expression of implicit functions, fuzzy and random problems, the
15 uncertainty evaluation methods and intelligent methods of integrated assessment
16 methods gradually emerged. Among thos method, fuzzy multi-attribute decision
17 analysis approach (FMADAA) was one of the effective methods for multiple
18 criteria decision support. For example, itt was adopted in a landfill selection
19 problem in the city of Regina and was considered as a powerful tool for decision
20 analysis. More recently, it has been rapidly developed in numerous fields such as
21 management, engineering, and so on (Buede, 1996; Eom, 1999; Yu et al., 2004;
22 Parviz and Saeed, 2010; George and Mike, 2011; Harrison et al., 2011; Ana et al.,
23 2012).

24
25 In the last two decades, the amount of water resources has decreased significantly
26 in the Yellow River Basin of China. The problem of water shortage becomes
27 extremely serious (Li et al., 2004; Shen and Li, 2009; Li and Yang, 2004).

28 Besides, water supply can not sufficiency meet the needs of industry, agriculture,
29 residential and ecological sectors, which has made water security a particularly
30 prominent problem affecting the economical and social development in the basin.

31 In recent years, many scholars put their effort on the calculation of the supplied
32 water quantity and requirement in order to analyze water utilization and water
33 allocation (Xia et al., 2009) in order to provide support for water resources
34 management in the Yellow River Basin. However, a few researchers have carried

1 out comprehensive water security evaluation in the Yellow River Basin especially
2 in the analysis on the regional differences of the entire basin, which is important
3 to the management in the basin. Therefore, the security evaluation in
4 administrative regions of the basin is extremely necessary in order to promote the
5 overall water resources security and to guarantee the coordinated development in
6 the basin.

7
8 Since MADA aims to identify optimal alternative for decision-makers, it is
9 effective in supporting relevant decision-making processes. That is to say, various
10 alternatives can be ranked according to certain criteria. Each region of the Yellow
11 River basin can be considered as an alternative and each evaluation method can be
12 considered as a criterion or an attribute. Also, in order to reflect uncertainties
13 associated with the process, FMADA needs to be adopted. It is suitable for
14 evaluating water resources security in the Yellow River basin. Moreover, since
15 the ranking results of different methods are inconsistent in practical application,
16 the results will also be integrated, which could enhance applicability and
17 accuracy of the results. In addition, fuzzy information usually encountered in
18 practical evaluation process can also be dealt with. Therefore, in the paper, we
19 will adopt FMADAA to carry on the water resources security evaluation in the
20 Yellow River basin in order to provide support for water management in the
21 basin.

22 23 **2 Overview of the Yellow River Basin**

24 The Yellow River is the second longest river in China. In total, the river flows
25 over 5,400 km, passes through nine provinces and autonomous regions. As the
26 biggest basin in the Northwest and North China, the Yellow River Basin is of
27 utmost importance for China in terms of food production, natural resources, and
28 socioeconomic development. The Yellow River Basin covers approximately 0.752
29 million km² areas (not including inland), accounting for eight percent of the total
30 area of China. Most area of the Yellow River Basin is in arid, semi -arid, and
31 semi-humid climate zones, and it is one of the regions in China with the least
32 water (Figure 1). Affected by human activities and climate change, the Yellow
33 River water resource has decreased significantly in recent years. Hence, water

1 security problems, especially the disparity between supply and demand of water,
2 the gradual deterioration of water eco-environment are particularly prominent and
3 seriously affecting economic and social development. Meanwhile, future climate
4 change may further exacerbate regional droughts and floods, affecting the water
5 supply and security of the Yellow River.

6

7 [Fig. 1 is here](#)

8

9 Considering the data availability, we selected 2006 to be the evaluation year to
10 analyze the current situation of water resources security in the Yellow River Basin.
11 Meanwhile, the data is derived from “Comprehensive Planning in the Yellow
12 River Basin” (Yellow River hydro-conservancy committee, 2009), “Water
13 Resources Comprehensive Planning in the Yellow River Basin” (Yellow River
14 hydro- conservancy committee, 2009), related materials and statistical yearbook
15 of the Yellow River (Yellow River hydro-conservancy committee, 2006).

16

17 **3 Development of a water security evaluation system**

18 **3.1. Evaluation indicators**

19 We established the “Pressure-State-Response” water resources security evaluation
20 model system which covered the indicators reflecting the water security situation
21 in the Yellow River Basin. “Pressure” system refers to those resources, social and
22 economic factors which may cause pressure on the system, and the indicators are
23 the decisive factors of the security of system. “State” system is the system status
24 under the action of resources, social and economic indicators. “Response” system
25 refers to the sensitivity and adaptability of the system to the actions of resources,
26 social and economic indicators and the various measures taken to decrease the
27 aggravation of water resources security. Each sub-system is established from three
28 aspects including water resources, soci-economic and water environment ([Jia et
29 al., 2002](#)).

30

31 The indicator selection methods used in this paper contain frequency statistical
32 method, theoretical analysis and expert consultation (Delphi method). Based on
33 the feedback from experts, fuzzy analytic hierarchy process (FAHP) is adopted as

1 the system analysis method to determine the water security evaluation indicator
2 system (Zhang, 2000). Hence, the indicator system can be established, the
3 connotations and calculations of indicators are shown in Table 1.

4

5 [Table 1 is here](#)

6

7 The evaluation criteria of the Yellow River basin has only a relative sense, we
8 took the national data as a benchmark to set the evaluation criteria. The main
9 references for determining the criteria mainly include the statistical data, relevant
10 standards, norms, procedures, development plan, existing research results and so
11 forth. In this paper, five interval evaluation criteria have been formulated,
12 followed by absolute security, security, critical security, insecurity and absolute
13 insecurity. Based on the evaluation criteria, the standards of the evaluation system
14 were determined which were shown in Table 2. Fuzzy analytic hierarchy process
15 (FAHP) is adopted to determine the weights of indicators and the calculation steps
16 are the same as in the establishment of the water resources security evaluation
17 indicator system. The weights of indicators were also obtained which were shown
18 in Table 3.

19

20 [Table 2 and 3 are here](#)

21

22 **3.2. Fuzzy Multi-Attribute Decision Analysis Approach**

23 Fuzzy multi-attribute decision analysis approach (FMADAA) is applied for
24 security evaluation. The proposed FMADAA is composed of four phases. In
25 the first phase, the evaluation alternatives should be established. The second phase
26 is fuzzy impact transformation, which consists of two major steps: 1)
27 Linguistic-term conversion which transforms the impact values into a fuzzy set if
28 they are verbal terms; and 2) conversion from a fuzzy set to a crisp value set
29 where all the fuzzy sets are assigned crisp scores. The result of this phase is to
30 produce a new impact matrix which only contains numeric data. In the third phase,
31 classical MADM methods can be utilized to determine the ranking order of
32 alternatives. At last, in the fourth phase, when the results of different MADM
33 methods are inconsistent, a further aggregation is needed.

1 In this paper, nine provinces in the Yellow River Basin and evaluation criteria
2 constituted the alternatives. Then the numerical approximation system and the
3 modified Left-Right scoring approach were adopted to cope with the uncertainties
4 in the acquired information. Four commonly used multi-attribute decision making
5 (MADM) methods were implemented in the evaluation model for impact
6 evaluation, including Simple weighted addition (SWA) method, Weighted product
7 (WP) method, Cooperative game theory (CGT) method and Technique for order
8 preference by similarity to ideal solution (TOPSIS) method. These MADM
9 methods helped to rank the nine provinces and the criteria alternatives, and three
10 aggregation methods including average ranking procedure, Borda and Copeland
11 methods were used to integrate the ranking results. The details of the four phases
12 are listed bellow.

13

14 **3.2.1. Alternatives establishment**

15 First, the alternatives which will be ranked in the MADM methods should be
16 fixed. In this paper, the nine provinces in the Yellow River Basin were considered
17 to be the nine alternatives (see Fig.2). Because MADM adopted in this paper is
18 aimed to evaluate the water resources security of the Yellow River Basin, the
19 evaluation criteria should also be transformed into different alternatives in order
20 to be compared with the security of the basin. Therefore, thirteen criteria
21 alternatives $A_a, A_b, A_c, A_d, A_e, A_f, A_g, A_h, A_i, A_j, A_k, A_l$ and A_m
22 were obtained here, among which A_a, A_e, A_i and A_m are critical values of the
23 five interval criteria. In addition, three criteria alternatives were added
24 between A_a and A_e, A_e and A_i, A_i and A_m respectively. It's worth noting that the
25 criteria alternatives can be selected according to different conditions or different
26 evaluation purposes.

27

28 *Fig 2 is here*

29

30 **3.2.2. Fuzzy impact transformation**

31 *(a) Linguistic-term conversion*

1 A numerical approximation system is proposed by [Hwang et al. \(1992\)](#) to
 2 systematically transform linguistic terms to their corresponding fuzzy sets.
 3 According to Hwang, the transformation requires eight conversion scales. The
 4 conversion scales are proposed by synthesizing and modifying the work of [Baas et
 5 al. \(1977\)](#), [Bonissone \(1982\)](#) and [Chen \(1988\)](#). It is assumed that the given figures
 6 can adequately cover all expressions of any specific feature-“high” vs. “low”. One
 7 of the figures will be employed when certain terms are provided and the principle
 8 is to simply select a scale figure that contains all the verbal terms given by the
 9 decision-maker and use the membership function set for that figure to represent
 10 the meaning of the verbal terms. For example, if the given certain terms include
 11 “low”, “medium” and “high”, the scale shown in Fig.3 is to be selected.

12

13 *Fig 3 is here*

14

15 *(b) Conversion from fuzzy sets to crisp values*

16 A modified Left-Right scoring approach based on [Jain’s \(1976, 1977\)](#) and [Chen’s
 17 \(1985\)](#) works is introduced. In order to determine a crisp score, it is necessary to
 18 compare the fuzzy sets with a maximizing fuzzy set (fuzzy max) and a
 19 minimizing fuzzy set (fuzzy min) ([Hwang et al., 1992](#)). These two fuzzy sets are
 20 defined as:

21

$$22 \quad \mu_{\max}(x) = \begin{cases} x, & 0 \leq x \leq 1 \\ 0, & \text{otherwise} \end{cases} \quad (1)$$

$$23 \quad \mu_{\min}(x) = \begin{cases} 1-x, & 0 \leq x \leq 1 \\ 0, & \text{otherwise} \end{cases} \quad (2)$$

24

25 The right score refers to the intersections of the fuzzy set M with max. The right
 26 score of M can be determined using (see Fig. 3):

1

$$\mu_R(M) = \sup_x [\mu_M(x) \wedge \mu_{\max}(x)] \quad (3)$$

3

4 Similarly, the left score of M can be determined using:

5

$$\mu_L(M) = \sup_x [\mu_M(x) \wedge \mu_{\min}(x)] \quad (4)$$

7

8 Given the left and right scores of M, the total score of M can be calculated using:

9

$$\mu_T(M) = [\mu_R(M) + 1 - \mu_L(M)] / 2 \quad (5)$$

11 Consequently, the set of μ_{total} can substitute the original linguistic terms and
12 impact matrix with only the crisp values that are formed.

13

14 **3.2.3. Multi-attribute decision making (MADM) methods**

15 MADM methods are management decision aids in evaluating competing
16 alternatives defined by multiple attributes. In this paper, four MADM methods are
17 adopted in the evaluation system. The reason of applying these four methods is
18 because they use the same type of input parameters, whereas other MADM
19 methods use different ones. Before presenting the details of these methods, some
20 basic concepts of decision weight and data normalization should be introduced.

21

22 Firstly, almost all MADM problems require information regarding the relative
23 importance of each attribute, including the methods used in the evaluation system
24 here. The relative importance is usually given by a set of weights which are
25 standardized to a sum equal to 1. Weight set is usually represented as follows:

26

$$W^T = (w_1, w_2, \dots, w_n) \quad (6)$$

27

1

$$\sum_{i=1}^n w_i = 1 \quad (7)$$

3

4 Where n represents the number of attributes, T represents a set of the traverse
5 form, W^T is a set of weights with n attributes. The weights can be assigned by
6 different methods (Saaty, 1977; Chu et al., 1979; Nijkamp et al., 1990). In this
7 paper, FAHP is adopted as referred before.

8

9 Then, according to Hwang et al. (1981), some methods as SWA must apply the
10 normalization method to normalize values in the impact matrix so that any effect
11 introduced by different measurement units is neutralized. In the evaluation system,
12 two ways of normalization are applied to cope with different MADM methods.
13 The linear normalization adopted here is a modified process by Hwang et al.
14 (1981). The normalized value r_{ij} can be defined as:

15

$$\text{For impact value of benefit attributes, } r_{ij}^b = \frac{x_{ij} - x_i^{\min}}{x_i^* - x_i^{\min}} \quad (8)$$

17

$$\text{For impact values of cost attributes, } r_{ij}^c = \frac{x_i^* - x_{ij}}{x_i^* - x_i^{\min}} \quad (9)$$

19

20 where $x_i^* = \max_j x_{ij}$ and x_i^{\min} is the least acceptable impact value of i attribute.

21 The worst outcome of a certain attribute implies $r_{ij} = 0$, while the best outcome
22 implies $r_{ij} = 1$. The vector normalization divides the impact value of each attribute
23 by its norm, so that each normalized value r_{ij} can be calculated as:

24

$$r_{ij} = \frac{x_{ij}}{\sqrt{\sum_{j=1}^m x_{ij}^2}} \quad (10)$$

2

3 where m is the total number of alternatives. Several MADM methods will be
4 adopted, including:

5

6 *(a) Simple weighted addition (SWA) method*

7 The SWA method is the simplest MADM method to handle cardinal data (Hwang
8 et al., 1981). Linear transformation is applied which normalizes the impact matrix
9 and the utility function can be written as:

10

$$U_j = \sum_{i=1}^n w_i r_{ij}, j = 1, 2, \dots, m \quad (11)$$

12

13 where w_i is the importance weight of the attributes and r_{ij} is the normalized
14 impact matrix. The alternative with the highest score is the most preferable one.
15 However, since complementarity often exists among attributes, the assumption of
16 preferentially independent may be unacceptable, and ignoring the dependence
17 among attributes may cause a misleading result (Hwang et al., 1992).

18

19 *(b) Weighted product (WP) method*

20 The WP method was introduced long ago (Starr, 1972; Yoon, 1989) and the
21 normalization is not necessary (Yoon et al., 1995). Formally, the utility value U_j
22 of each alternative is given by:

$$U_j = \prod_{i=1}^n x_{ij}^{w_i}, j = 1, 2, \dots, m \quad (12)$$

24

25 where w_j is the importance weight of the i^{th} attribute and x_{ij} is the impact value

1 of the j^{th} alternative. Similarly, the alternative with the largest utility value is
 2 considered the most preferable one to the decision maker. Theoretically, the utility
 3 value may become infinite due to the characteristic of multiplication and the
 4 distance between the utility values of the most and second most preferable
 5 alternatives would be greater than that derived from SWA method.

6

7 (c) *Cooperative game theory (CGT)*

8 It is developed by [Szidarovszky et al. \(1978\)](#) and it is described as the hybrid of
 9 the WP and TOPSIS method. By using CGT, the decision maker looks for a
 10 solution that would be as far away from the worst solution as possible. Therefore,
 11 the safety of the solution is guaranteed. To define a worst solution, one way is to
 12 use the worst impact value of each attribute. Given a set of non-dominant
 13 alternatives, the set of worst impact value, denoted as A^- , is defined as:

14

$$15 \quad A^- = \left\{ (\min_j x_{ij} | i \in I), (\max_j x_{ij} | i \in I^*) | j = 1, 2, \dots, m \right\} = \{x_1^-, x_2^-, \dots, x_i^-, \dots, x_n^-\}$$

16 (13)

17

18 where x_{ij} is the impact value of attribute i and x_i^- is considered as the worst
 19 outcome for each attribute. Once the worst solution is defined, the utility values
 20 U_j for each attribute can be measured by the following formula ([Gershon, 1984](#)).

21

$$22 \quad U_j = \prod_{i=1}^n |x_{ij} - x_i^-|^{w_i}, j = 1, 2, \dots, m, \quad (14)$$

23

24 where w_i is the importance weight for each attribute. After calculating the utility
 25 values, the most preferable alternative can then be defined as the one with the
 26 greatest utility; and the result is given by ranking the values in descending order.
 27 However, due to the fact that multiplying any value by 0 equals 0, using CGT will
 28 automatically screen out all the alternatives that carry at least one worst impact
 29 value. Even if those alternatives might result in better outcomes (impacts) in other

1 attributes, they still will not be considered.

2

3 *(d) Technique for order preference by similarity to ideal solution (TOPSIS)*

4 TOPSIS is a technique that is developed by [Hwang et al. \(1981\)](#). They explain
5 that a MADM problem may be viewed as a geometric system. The m alternatives
6 that are evaluated by n attributes are similar to m points in the n -dimensional
7 space. Therefore, the most preferable alternative should satisfy a condition such
8 that it has the “shortest distance” from the positive-ideal solution and the “longest
9 distance” from the negative-ideal solution.

10

11 **3.2.4. Ranking result aggregation**

12 Due to the different characteristics of the four MADM methods, the outcomes
13 from applying them to solve a decision-making problem might be diverse. If the
14 diversity is small, then the outcome is considered reliable. If the outcomes are
15 inconsistent, further aggregations have to be done. Different approaches of
16 MADM aggregation were adopted in this paper, including:

17

18 *(a) Average ranking procedure*

19 The average ranking procedure is the simplest technique among the three
20 aggregation methods. This technique is based on the concept of statistical
21 calculation and ranks the alternatives according to the average rankings from the
22 MADM methods.

23

24 *(b) Borda method*

25 It is based on the concept of voting and it compares each pair of alternatives
26 separately and forms an $N \times N$ matrix. For each pair of alternatives A_j and $A_{j'}$,
27 the number of votes is defined as the number of “supporting” methods in
28 which A_j is more preferable than $A_{j'}$. Then a $N \times N$ matrix X is generated such
29 that: $x_{jj'} = 1$, if A_j receives more votes than $A_{j'}$, $x_{jj'} = 0$, otherwise. S_j indicates
30 the number of “wins” that A_j has received against other alternatives and it is

1 calculated by summing the x_{jj} in each row of the matrix. Hence, the alternative
2 with the highest S_j is considered the most preferable.

3

4 (c) *Copeland method*

5 It is an extension of the Borda method which is also based on the voting concept.

6 It is believed that the aggregation utility of A_j does not only depends on the
7 number of “wins”, but the number of “losses” also needs to be taken into account.

8 The number of “losses”, denoted as S'_j , is used to compensate the utility value

9 of S_j . S'_j is calculated by summing the values of each column of the matrix and

10 the aggregation utility is simply defined as the difference of S_j from S'_j . As

11 with the Borda method, the Copeland method ranks the alternatives in descending

12 order of their aggregation utilities from largest to smallest. Although using these

13 aggregation methods may still result in inconsistencies among the rankings, some

14 useful patterns can easily be observed by the decision- maker according to the

15 analyzed information.

16

17 **4 Results**

18 **4.1 Indicator value of nine provinces in the Yellow River Basin**

19 First, D_{33} indicator-“perfection degree of management system and legal system”

20 which involves the fuzzy data was transformed into numeric data by applying the

21 conversion scale including five terms (see Fig. 3). The indicator refers to the five

22 terms “absolute good”, “good”, “medium”, “poor” and “absolute poor” which are

23 corresponding to the selected scale involving “high”, “medium high”, “medium”,

24 “medium low” and “low”. Thus, the membership functions of M_1, M_2, M_3, M_4

25 and M_5 can be presented as:

26

$$27 \quad \mu_{M_1}(x) = -\frac{1}{0.3}x + 1, \quad 0 \leq x \leq 0.3 \quad (15)$$

28

$$\mu_{M_2}(x) = \begin{cases} \frac{1}{0.25}x & , 0 \leq x < 0.25 \\ \frac{1}{-0.25}x + 2 & , 0.25 \leq x < 0.5 \end{cases} \quad (16)$$

$$\mu_{M_3}(x) = \begin{cases} \frac{1}{0.2}x - \frac{3}{2} & , 0.3 \leq x < 0.5 \\ \frac{1}{-0.2}x + \frac{7}{2} & , 0.5 \leq x < 0.7 \end{cases} \quad (17)$$

$$\mu_{M_4}(x) = \begin{cases} \frac{1}{0.25}x - 2 & , 0.5 \leq x < 0.75 \\ \frac{1}{-0.25}x + 4 & , 0.75 \leq x < 1 \end{cases} \quad (18)$$

$$\mu_{M_5}(x) = \frac{1}{0.3}x - \frac{7}{3}, \quad 0.75 \leq x \leq 1 \quad (19)$$

Using Equations (3)-(5), the total utility scores were calculated and the set of μ_{total} can substitute the original linguistic terms, which were shown in Table 4. Hence, “absolute good”, “good”, “medium”, “poor” and “absolute poor” were replaced with the values: 0.8846, 0.7000, 0.5000, 0.4333 and 0.1154.

Table 4 is here

Water resources security in the Yellow River Basin is in the middle and the lower level in our country, so there is no need to add the four standard samples (A_a , A_b , A_c and A_d) in order to simplify the calculation process. Therefore, eighteen alternatives were determined in the evaluation including the nine provinces alternatives and nine criteria alternatives. The values of the eighteen alternatives are shown in Table 5 and Table 6.

Table 5 and Table 6 are here

1 **4.2 MADM ranking results**

2 After the evaluation indicator system was established, the values of
3 indicators were normalized by using Equation 8-9. Hence, the ranking
4 results were obtained under the four MADM methods. By using Equation
5 11, the SWA ranking results are: Ae > Af > Sichuan > Ag > Henan > Ah >
6 Shandong > Qinghai > Ai > Shaanxi > Aj > Gansu > Shanxi > Ak > Inner
7 Mongolia > Al > Am > Ningxia. By using Equation 12, the WP ranking
8 results are: Qinghai > Sichuan > Gansu > Ae > Shandong > Af > Ag > Ah >
9 Inner Mongolia > Henan > Shaanxi > Ai > Aj > Ak > Shanxi > Al > Am >
10 Ningxia. It is worth noting that when the negative indicator equals to 0, its
11 negative power does not make sense. Therefore, in order to rank all the provinces
12 in the basin and the standard alternatives, we used 0.00001 to replace the
13 indicator which equals to 0 and the influence on the results can be ignored.
14 By using Equation 14, the CGT ranking results are: Ae > Af > Ag > Ah >
15 Henan > Ai > Aj > Shaanxi > Ak > Al > Gansu > Shandong > Qinghai > Am >
16 Inner Mongolia > Shanxi > Sichuan > Ningxia. Specifically, U_j is 0 when the
17 alternative includes at least one indicator which was selected to be the worst
18 sample, which is not conducive to rank all the alternatives. Under this
19 consideration, the positive indicator in the worst sample was minused by 0.00001,
20 and the negative indicator was plused by 0.00001 during the data processing.
21 By using TOPSIS, the ranking results are: Sichuan > Ae > Af > Qinghai >
22 Henan > Ag > Ah > Shaanxi > Gansu > Shandong > Ai > Shanxi > Aj > Ak >
23 Inner Mongolia > Al > Am > Ningxia.

24 **4.3 MADM aggregation results**

25 The alternatives were ranked according to the mean rankings from the four
26 MADM methods, which are shown in Table 7.

27

28 *Table 7 is here*

29

30 According to Average Ranking Procedure, the final ranking order is: Ae > Af >
31 Ag > Sichuan > Ah, Henan > Qinghai > Shandong > Gansu > Shaanxi > Ai > Aj
32 > Ak > Inner Mongolia > Shanxi > Al > Am > Ningxia. According to Borda, each

1 pair of alternatives were compared separately and the $N \times N$ matrix X was
2 formed which is shown in Table 8. According to the value of S_j , the final ranking
3 order is $A_e > A_f > \text{Sichuan} > A_g > A_h$, $\text{Henan} > \text{Qinghai} > \text{Shaanxi}$, $\text{Shandong} >$
4 A_i , $\text{Gansu} > A_j > A_k > \text{Shanxi}$, and $\text{Inner Mongolia} > A_l > A_m > \text{Ningxia}$. For
5 Copeland method, according to the value of $S_j - S'_j$, the final ranking order is A_e
6 $> A_f$, $\text{Sichuan} > A_g > \text{Qinghai} > A_h$, $\text{Henan} > \text{Shaanxi}$, $\text{Shandong} > A_i$, $\text{Gansu} >$
7 $A_j > A_k > \text{Shanxi} > \text{Inner Mongolia} > A_l > A_m > \text{Ningxia}$.

8

9 *Table 8 is here*

10

11 Based on the ranking results of the three aggregation methods, the water resources
12 security degrees of the nine provinces in the Yellow River Basin were shown in
13 Table 9.

14

15 *Table 9 is here*

16

17 Copeland aggregation results are shown in Fig. 4 and Table 10.

18

19 *Fig.4 is here*

20 *Table 10 is here*

21

22 Among the nine provinces in the Yellow River Basin, water resources security
23 evaluation condition is relatively poor in Shanxi, Inner Mongolia and Ningxia
24 province. Ranking results of the thirty-three indicator values were obtained in
25 Table 11.

26

27 *Table 11 is here*

28

1 **5 Discussions**

2 In the four MADM methods in FMADAA, CGT ranking results have a significant
3 difference with the other three methods. This is because CGT will automatically
4 rule out (or shrink) all the alternatives which contain at least one minimum
5 indicator value of the worst sample although the other indicators are at a higher
6 level of the whole basin. For example, water resources amount is abundant in
7 Sichuan province, and many indicators of the evaluation system are better than the
8 other provinces. However, the three indicator values are 0 including modulus of
9 groundwater resources, eco-environment water consumption ratio and
10 water-saving irrigation rate, which decreases the whole water resources security in
11 Sichuan province.

12

13 From Table 9, it can be seen that the ranking order is different from Borda and
14 Copeland. This is because in FMADAA, four MADM methods' impacts on the
15 results of average ranking procedure method are the same since it is determined
16 by the mean rankings. Hence, we can see that compared with the Copeland
17 aggregation method, the water resources security condition in Henan province is
18 better than in Qinghai province, which is influenced by the results of CGT method.
19 Meanwhile, the condition in Gansu province is better than that in Shaanxi
20 province and Ai standard alternative because of the impact by the results of WP
21 method. We can also see that the results of Copeland are also a little different
22 from the Borda method because it considers both "wins" and "losses" of the
23 alternatives.

24

25 Although the results of the three aggregation methods are not exactly consistent,
26 some certain and useful information can be obtained that the ranking order is $Ae >$
27 Af , Sichuan, $Ag > Ah$, Qinghai, Henan $> Ai$, Shandong, Shaanxi, Gansu $> Aj >$
28 $Ak >$ Shanxi, Inner Mongolia $> Al > Am >$ Ningxia. The water resources security
29 in these provinces is in the critical state include Sichuan, Qinghai and Henan.
30 Shanxi and Inner Mongolia are in the insecurity state. Meanwhile, Ningxia
31 province is in the absolute insecurity state. Shandong, Shaanxi and Gansu
32 provinces are in the critical or insecurity state.

33

1 As to the ranking order of one province, because it is based on voting principle,
2 Copeland method will rule out the influence of the large difference of evaluation
3 results between one MADM method and the others. Besides, it considers both
4 “wins” and “losses” of the alternatives, so to some extent, it is more reasonable.
5 The ranking order by using Copeland method is $A_e > A_f$, Sichuan $> A_g > A_h$
6 $> A_i$, Henan $> A_j$, Shaanxi, Shandong $> A_k > A_l > A_m > A_n$. From the results shown in Fig. 4 and Table10,
7 we can see that the water resources security of the whole basin is in critical,
8 insecurity and absolute insecurity state, which is at the lower level in China. The
9 provinces whose water resources security is in the critical state include Sichuan,
10 Qinghai, Henan, Shanxi, Shandong and Gansu. Shanxi and Inner Mongolia are in
11 the in the insecurity state. Meanwhile, Ningxia province is in the absolute
12 insecurity state.
13

14

15 For the regional distribution, we can see that water resources security of the
16 provinces located in the upstream of the Yellow River is better than the other
17 provinces such as Qinghai and Sichuan province. The southern provinces are
18 better than the northern provinces such as Sichuan province. Meanwhile, the
19 developed provinces are better than the other provinces such as Sichuan,
20 Shandong and Henan province. This is because that the amount of water resources
21 is relatively abundant in the upstream and the values of socio-economic related
22 indicators are higher in the developed provinces which enhance its whole water
23 resources security.
24

24

25 Among the nine provinces in the Yellow River Basin, water resources security
26 evaluation condition is relatively poor in Shanxi, Inner Mongolia and Ningxia
27 province. From Table 10, we can see that the indicator values of water resources
28 pressure system are smaller in the three provinces, which means that in pressure
29 system, water resources pressure is relatively high in the three provinces.
30 Meanwhile, indicators in water resources state and Water Eco-environment state
31 of state system and socio-economic response system are the worse in Shanxi
32 province. It can be seen that the higher water resources pressure, the worse water
33 resources and Water eco-environment state and the backward responses result in

1 insecure water resources in Shanxi province. Similarly, the higher water resources
2 and socio-economic pressure and worse Water Eco-environment state result in
3 insecure water resources in Inner Mongolia province. Water resource has absolute
4 insecurity in Ningxia province because of the higher pressure in water resources,
5 socio-economic, water environment system and backward socio-economic
6 responses.

7

8 Therefore, the future planning of the Yellow River Basin should focus on soil
9 erosion management, improvement of water quality in water function areas, rivers
10 and groundwater in order to improve water eco-environment status in Shanxi and
11 Inner Mongolia province. Meanwhile, the water utilization efficiency should be
12 improved so that the socio- economic pressure is decreased and water
13 management should be enhanced such as increasing the water conservancy
14 investment, industrial and agricultural water- saving intense and the rural
15 population access to up-to-standard drinking water. In addition, it is also
16 important to raise the water supply capacity in Shanxi province in order to
17 improve the water resources status and enhance the control of sewage disposal in
18 Ningxia province so that the water environment pressure can be decreased.

19

20 In summary, FMADAA can be successfully applied in water resources security
21 evaluation in the Yellow River Basin because it's a combination of Fuzzy method
22 and different MADM methods and it also aggregates various results of MADM
23 methods, which can provide a more rational result. In addition, the system can
24 also deal with fuzzy information which is usually encountered in practical
25 evaluation process. The ranking results showed that the water resources security
26 of the whole Yellow River Basin is in critical, insecurity and absolute insecurity
27 state, which is at the lower level in China especially in Shanxi, Inner Mongolia
28 and Ningxia provinces whose water resources are in the insecurity and absolute
29 insecurity state. Hence, future planning of the Yellow River Basin should focus on
30 the three provinces in order to promote the overall water resources security and to
31 guarantee the coordinated development in the basin.

32

1 **6 Conclusions**

2 Through introducing the concept of water resources security, a
3 “Pressure-State-Response” water resources security evaluation system was
4 developed in this research. Multiple level indicators were identified within the
5 system. Also, a fuzzy multi-attribute decision analysis approach (FMADAA)
6 was proposed not only for dealing with the evaluation based on the
7 developed indicators, but also tackling the inherent uncertainties. As for the
8 ranking order of alternatives under different methods, Copeland aggregation was
9 adopted. The evaluation system was then applied to the Yellow River Basin. The
10 results showed that the water resources security of the basin was critical,
11 insecurity and absolute insecurity states. The provinces whose water resources
12 security was in the critical state included Sichuan, Qinghai, Henan, Shanxi,
13 Shandong and Gansu. Shanxi and Inner Mongolia were in the in the insecurity
14 state. Meanwhile, Ningxia province is in the absolute insecurity state. For the
15 regional distribution, water resources security of the provinces located in the
16 upstream of Yellow River was better than other provinces such as in Qinghai and
17 Sichuan province. The southern provinces were better than northern provinces
18 such as Sichuan province. Normally, provinces with higher economic
19 productivities were better than other provinces such as in Sichuan, Shandong and
20 Henan province. This is because water resources amount was relatively abundant
21 in the upstream and the values of socio-economic related indicators were higher in
22 the developed provinces. Since the water resources security in Shanxi, Inner
23 Mongolia and Ningxia was the worst in the basin, future planning and
24 management should focus on water management in the three provinces.

25

26 **Acknowledgments** This paper was sponsored by National Basic Research
27 Program (973 Program) (2010CB951104), the National Science Foundation for
28 Innovative Research Group (No. 51121003), International Science & Technology
29 Cooperation Program of China (2011DFA72420) and the special fund of State
30 Key Lab of Water Environment Simulation (11Z01ESPCN).

1

2 **References**

- 3 Ana, C. C., John, W. L., and Darrell, G. F.: Multicriteria decision support system
4 for regionalization of integrated water resource management, *Water Resour.*
5 *Manag.*, 11, 1–22, 2012.
- 6 Bass, S. M. and Kwakemaak, H.: Rating and ranking of multiple aspect
7 alternative using fuzzy sets, *Automatica*, 3, 47–58, 1977.
- 8 Bonissone, P. P.: A fuzzy set based linguistic approach: theory and applications,
9 in: *Approximate Reasoning in Decision Analysis*, edited by: Gupa, M. M. and
10 Sanchez, E., North-Holland Publishing Company, [Amsterdam](#), 329–339, 1982.
- 11 Brown, L. R. and Hilweil, B.: China’s water shortage could shake world food
12 security, *World Watch*, 7, 8, 10–18, 1987.
- 13 Buede, D.: Second overviews of the MCDA software market, *Journal of*
14 *Multi-Attribute Decision Analysis*, 5, 312–216, 1996.
- 15 Chen, S. H.: Ranking fuzzy numbers with maximizing set and minimizing set,
16 *Fuzzy Set Syst.*, 2, 113–129, 1985.
- 17 Chen, S. J.: Water resources security concept and its discussion, *China Water*
18 *Resources*, 17, 13–15, 2004.
- 19 Chen, S. M.: A new approach to handling fuzzy decision-making problems, *IEEE*
20 *T. Syst. Man Cyb.*, 6, 1012–1016, 1988.
- 21 Chu, A. T. W., Kalaba, R. E., and Spingarn, K.: A comparison of two methods for
22 determining the weights of belonging to fuzzy sets, *J. Optimiz. Theory App.*,
23 27, 531–538, 1979.
- 24 Cong, X.: Application of fuzzy mathematics in water quality assessment,
25 *Northwestern Water Conservancy and Hydropower*, 276, 55–57, 2007 (in
26 Chinese).
- 27 Eom, S. B. and Min, H.: The contributions of multi-attribute decision making to
28 the development of decision support systems subspecialties: an empirical
29 investigation, *Journal of Multi-Attribute Decision Analysis*, 5, 239–255, 1999.
- 30 Gershon, M.: The role of weights and scales in the application of multiobjective
31 decision making, *Eur. J. Oper. Res.*, 15, 244–250, 1984.
- 32 Gorge, T. and Mike, S.: Planning against long term water scarcity: a fuzzy
33 multicriteria approach, *Water Resour. Manag.*, 4, 1103–1129, 2011.

- 1 Han, P. Q., Lu, J. X., and Song, S. H.: Fuzzy clustering's application in water
2 quality evaluation, *Environ. Sci. Technol.*, 30, 165–167, 2001 (in Chinese).
- 3 Harrison, M., Saroj, S., and Kalanithy, V.: Multi-attribute decision analysis: a
4 strategic planning tool for water loss management, *Water Resour. Manag.*, 4,
5 1–23, 2011.
- 6 Hwang, C. L. and Chen, S. J.: *Fuzzy Multiple Attribute Decision Making:
7 Methods and Applications*, Springer, New York, 1992.
- 8 Hwang, C. L. and Yoon, K.: *Multiple Attribute Decision Making: Methods and
9 Applications*, Springer, New York, 1981.
- 10 Jain, R.: Decision making in the presence of fuzzy variables, *IEEE T. Syst. Man
11 Cyb.*, 6, 698–703, 1976.
- 12 Jain, R.: A procedure for multi-aspect decision making using fuzzy sets, *Int. J.
13 Syst. Sci.*, 8,1–7, 1977.
- 14 Jia, S. F. and Zhang, S. F.: Water resources security appraisalment of Haihe basin,
15 *Progress in Geography*, 4, 379–387, 2003 (in Chinese).
- 16 Jia, S. F., Zhang, J. Y., and Zhang, S. F.: Regional water resources stress and
17 water resources security appraisalment indicators, *Prog. Geogr.*, 6, 538–545,
18 2002 (in Chinese).
- 19 Jia, S. F., He, X. W., and Xia, J.: Problems and countermeasures of water resource
20 security of China, *Bulletin of the Chinese Academy of Sciences*, 5, 347–351,
21 2004.
- 22 Jiang, W. L.: Study on water resource safety strategy for China in the 21st century,
23 *Advances in Water Science*, 1, 66–71, 2001.
- 24 Li, C. H. and Yang, Z. F.: Natural runoff changes in the Yellow River basin, *J.
25 Geogr. Sci.*, 24, 427–436, 2004.
- 26 Li, C. H., Yang, Z. F., and Wang, X.: Trends of Annual natural runoff in the
27 Yellow River basin, *Water Int.*, 4, 447–454, 2004.
- 28 Loucks, D. P.: Sustainable Water Resource Management, *Water Int.*, 1, 3–10,
29 2000.
- 30 Nijkamp, P., Rietveld, P., and Voogd, H.: *Multicriteria Evaluation in Physical
31 Planning*, North-Holland Publishing Company, [Amsterdam](#), 1990.
- 32 Parviz, F. and Saeed, F.: A compromise programming model to integrated urban
33 water management, *Water Resour. Manag.*, 6, 1211–1227, 2010.

- 1 Saaty, T. L.: A scaling method for priorities in hierarchical structures, *J. Math.*
2 *Psychol.*, 15, 234–281, 1977.
- 3 Shen, N. and Li, C. H.: Evolution characteristics of runoff in Yellow River during
4 recent 500 years, *Journal of Water resources & Water Engineering*, 5, 37–40,
5 2009 (in Chinese).
- 6 Starr, M. K.: *Production Management*, Prentice-Hall, Englewood Cliffs, NJ, 1972.
- 7 Szidarovszky, F. and Yakowitz, S.: *Principles and Procedures of Numerical*
8 *Analysis*, Plenum Press, New York, 1978.
- 9 WWAP: *World Water Development Report-WWDR*, Washington D.C., 2002.
- 10 Xia, J. and Zhang, Y. Y.: Water security in north China and countermeasure to
11 climate change and human activity, *Phys. Chem. Earth*, 33, 359–363, 2007.
- 12 Xia, X. H., Yang, Z. F., and Wu, Y. X.: Incorporation eco-environmental water
13 requirements in integrated evaluation of water quality and quantity – a study
14 for the Yellow River, *Water Resour. Manag.*, 6, 1067–1079, 2009.
- 15 Yoon, K.: A reconciliation among discrete compromise situations, *Journal of*
16 *Operational Research Society*, 40, 681–686, 1989.
- 17 Yoon, K. P. and Hwang, C. L.: *Multiple Attribute Decision Making: an*
18 *Introduction*. Sage Publication inc., Thousand oaks, California, 1995.
- 19 Yu, Y. B., Wang, B. D., Wang, G. L., and Li, W.: Multi-person multi-objective
20 fuzzy decision-making model for reservoir flood control operation, *Water*
21 *Resour. Manag.*, 2, 111–124, 2004.
- 22 Zhang, J. J.: Fuzzy analytic hierarchy process (FAHP), *Fuzzy System and*
23 *Mathetic*, 2, 80–88, 2000 (in Chinese).
- 24 Zhang, J. Y.: Impacts evaluation of climate changes on water resources security,
25 *China Water Resources*, 8, 5–6, 2010 (in Chinese).
- 26 Zhang, J. Y., Wang, G. Q., Yang, Y., He, R. M., and Liu, J. F.: The possible
27 impacts of climate change on water security in China, *Advance Climate*
28 *Change Research*, 5, 290–295, 2008 (in Chinese).
- 29 Zhang, S. F. and Jia, S. F.: Water balance and water security study in the Haihe
30 basin, *Journal of Natural Resources*, 3, 684–691, 2003 (in Chinese).
- 31 Zhang, X., Xia, J., and Jia, S. F.: Definition of water security its assessment using,
32 *Resource Science*, 3, 145–149, 2005 (in Chinese).
- 33 Zheng, T. H.: Discussions on water resources safety and water resources safety
34 warning, *China Water Resources*, 6, 19–22, 2003 (in Chinese).

- 1 Zhu, H. Y., Du, S. S., and Gu, Y. Y.: Fuzzy mathematics and its application in
- 2 surface water quality evaluation – take Fuyang River in Handan for an
- 3 example, Groundwater, 5, 80–90,2008 (in Chinese).
- 4

- 1 Table captions
- 2 Table 1. Water resources security evaluation indicator.
- 3 Table 2. Criteria of basin water resources security evaluation
- 4 Table 3. Weights of water resources security evaluation indicator
- 5 Table 4. Determination of μ_{total}
- 6 Table 5. Indicator value of 9 provinces in water resources security evaluation
- 7 system in the Yellow River Basin
- 8 Table 6. Indicator value of 9 standards in water resources security evaluation
- 9 system in the Yellow River Basin
- 10 Table 7. Summary of indicator values in Average Ranking Procedure
- 11 Table 8. N×N matrix used in Borda and Copeland methods
- 12 Table 9. Evaluation level of water resources security by 3 MADM Aggregation
- 13 methods in 9 provinces in 2006
- 14 Table 10. Water resources security levels in administrative regions in the Yellow
- 15 River Basin under Copeland aggregation method (in 2006)
- 16 Table 11. Ranking results of indicator value in Shanxi, Inner Mongolia and
- 17 Ningxia provinces
- 18

1 **Table 1. Water resources security evaluation indicator.**

Evaluation indicator			Calculation formula	Indicator unit	Indicator meaning	Indicator type
Pressure indicators B1	D1	Water production coefficient	Total amount of water resources /precipitation		Reflect the amount of water resources	positive
	D2	Annual runoff	Regional runoff/ evaluation area	mm	Reflect the amount of water resources	positive
Water resources Pressure indicators C1	D3	Modulus of groundwater resources	Groundwater resources amount / evaluation area	10 ⁴ m ³ /km ²	Reflect the amount of groundwater resources	positive
	D4	Modulus of water resources	Total amount of water resources / evaluation area	10 ⁴ m ³ /km ²	Reflect the amount of water resources	positive
Socio-economic Pressure indicators C2	D5	Water utilization rate	Water consumption amount with the exception of eco-environmental water consumption / total amount of water resources×100%	%	Reflect the development and utilization of water resources	negative
	D6	Development degree of surface water	Exploitation amount of surface water / surface water resources amount	%	Reflect the development and utilization of surface water resources	negative
	D7	Development degree of groundwater	Exploitation amount of groundwater /groundwater resources amount	%	Reflect the development and utilization of groundwater resources	negative

		D8	Water consumption per 10,000 Yuan of GDP	Total amount of water consumption /GDP	$m^3/10,000$ Yuan	Reflect the economic water consumption level	negative
		D9	Water consumption per 10,000 Yuan of industrial output	Total amount of water consumption / industrial output	$m^3/10,000$ Yuan	Reflect the economic water consumption level	negative
	Water environment Pressure indicators C3	D10	Ratio of pollutants (COD and ammonia nitrogen)dumped into the river	Pollutants (COD and ammonia nitrogen) amount/ annual runoff	$t/10^4m^3$	Reflect the discharge condition of the contaminants from the waste water	negative
		D11	Area ratio of excessive extraction of groundwater	Excessive extraction area of groundwater(depression funnel)/ evaluation area $\times 100\%$	%	Reflect the excessive extraction condition of groundwater	negative
State indicators B2	Water resources state indicators C4	D12	Index of water resources demand-supply balance(IWDS)	Average water demand amount /water supply amount		Reflect the water demand-supply balance condition	negative
		D13	Water resources amount per capita	Total amount of water resources /total population	$m^3/person$	Reflect the amount of water resources and water scarcity condition	positive
	Socio-economic state indicators C5	D14	Water supply modulus	Water consumption amount / evaluation area	$10^4m^3 \cdot km^{-2}$	Reflect the intensity of water supply	positive
		D15	Water supply amount per capita	Water consumption amount / total population	$m^3/person$	Reflect the intensity of water supply	positive

Water Eco-environment state indicators C6	D16	GDP per capita	GDP / total population	10,000 Yuan /person	Reflect the overall economic condition	positive
	D17	Ratio of agricultural water consumption to total consumption	Agricultural water consumption amount/ water consumption amount×100%	%	Reflect the agricultural water consumption level and the structure of water consumption	negative
	D18	Domestic water consumption per capita	Domestic water consumption amount/ total population /365	L/(d·person)	Reflect the living water security condition	positive
	D19	Eco-environment water consumption ratio	Eco-environment water consumption amount/ total population×100%	%	Reflect the eco-environment water security condition	positive
	D20	Ratio of soil erosion area to the total area	Soil erosion area / evaluation area×100%	%	Reflect the soil erosion condition	negative
	D21	Up-to-standard rate of water quality in water function area	Number of up-to-standard water function area / total number of water function area×100%	%	Reflect the water quality condition in the function area	positive
	D22	Ratio of up-to-standard river length of water quality to the total river length	Up-to-standard river length of water quality / total evaluation river length×100%	%	Reflect the river water quality condition	positive
	D23	Ratio of class I , II and III	Class I , II and III groundwater area of water	%	Reflect the groundwater quality	positive

			groundwater area of water quality to the total area	quality / total evaluation area×100%		condition	
Response indicators B3	Socio-economic response indicators C7	D24	Water conservancy investment rate	Water conservancy investment amount /GDP×100%	%	Reflect the water conservancy investment condition	positive
		D25	Industrial water re-utilization rate	Industrial water re-utilization amount/ Industrial water consumption amount×100%	%	Reflect the industrial water-saving condition	positive
		D26	Effective irrigation coverage rate	Effective irrigation area/cultivated land area×100%	%	Reflect the irrigation level	positive
		D27	Water irrigation efficiency	Field water consumption amount/water intake amount in the field		Reflect the quality of the irrigation project, the level of irrigation technology and the water irrigation management condition	positive
		D28	Water-saving irrigation rate	Water-saving irrigation area/ effective irrigation area×100%	%	Reflect the irrigation water-saving condition	positive

D29	Leakage rate of water supply pipe network	(Urban water supply amount –effective water supply amount)/ Urban water supply amount×100%	%	Reflect the urban water-saving condition	negative
D30	Water-saving appliances penetration rate	Water-saving appliances penetration families/total families×100%	%	Reflect the urban water-saving condition	positive
D31	Ratio of urban population access to up-to-standard drinking water to the total urban population	Urban population access to up-to-standard drinking water / total urban population×100%	%	Reflect the urban drinking water condition	positive
D32	Ratio of rural population access to up-to-standard drinking water to the total rural population	Rural population access to up-to-standard drinking water / total rural population×100%	%	Reflect the rural drinking water condition	positive
D33	Perfection degree of management system and legal system	management system and legal system		Reflect the water resources management condition	positive

1 **Table 2. Criteria of basin water resources security evaluation**

Evaluation indicator		Indicator unit	Evaluation criteria					
			Absolute security (class I)	Security (class II)	Critical security (class III)	Insecurity (class IV)	Absolute insecurity (class V)	
Water resources Pressure indicators C1	D1	Water production coefficient		≥ 0.3	0.24~0.3	0.18~0.24	0.12~0.18	< 0.12
	D2	Annual runoff	mm	≥ 130	90~130	50~90	10~50	< 10
	D3	Modulus of groundwater resources	$10^4 \text{m}^3/\text{km}^2$	≥ 5.5	4~5.5	2.5~4	1~2.5	< 1
	D4	Modulus of water resources	$10^4 \text{m}^3/\text{km}^2$	≥ 50	38~50	16~38	4~16	< 4
	D5	Water utilization rate	%	< 1	1~2	2~3	3~4	≥ 4
Pressure indicators B1 C2	D6	Development degree of surface water	%	< 30	30~50	50~70	70~90	≥ 90
	D7	Development degree of groundwater	%	< 30	30~50	50~70	70~90	≥ 90
	D8	Water consumption per 10,000 Yuan of GDP	$\text{m}^3/10^4 \text{yuan}$	< 100	100~200	200~300	300~400	≥ 400
	D9	Water consumption per 10,000 Yuan of industrial output	$\text{m}^3/10^4 \text{Yuan}$	< 30	30~60	60~90	90~120	≥ 120
Water environment Pressure indicators	D10	Ratio of pollutants (COD and ammonia nitrogen) dumped into the river	$\text{t}/10^4 \text{m}^3$	< 0.5	0.5~1	1.0~1.5	1.5~2	≥ 2
	D11	Area ratio of excessive extraction of groundwater	%	< 0.6	0.6~1	1~1.4	1.4~1.8	≥ 1.8

C3

State indicators B2	Water resources state indicators C4	D12	Index of water resources demand-supply balance(IWDS)		<0.8	0.8~1	1~1.2	1.2~1.4	≥1.4
		D13	Water resources amount per capita	m ³ /person	≥1000	750~1000	500~750	250~500	<250
		D14	Water supply modulus	10 ⁴ m ³ ·km ⁻²	≥16	12~16	8~12	4~8	<4
Socio-economic state indicators C5		D15	Water supply amount per capita	m ³ / person	≥800	600~800	400~600	200~400	<200
		D16	GDP per capita	10 ⁴ yuan/ person	≥1.6	1.4~1.6	1.2~1.4	1~1.2	<1
		D17	Ratio of agricultural water consumption to total consumption	%	<55	55~65	65~75	75~85	≥85
		D18	Domestic water consumption per capita	L/(d·person)	≥150	125~150	100~125	75~100	<75
Water Eco-environment state indicators C6		D19	Eco-environment water consumption ratio	%	≥3.6	2.7~3.6	1.8~2.7	0.9~1.8	<0.9
		D20	Ratio of soil erosion area to the total area	%	<15	15~35	35~50	50~75	≥75
		D21	Up-to-standard rate of water quality in water function area	%	≥80	65~80	50~65	35~50	<35
		D22	Ratio of up-to-standard river length of water quality to the total river length	%	≥80	65~80	50~65	35~50	<35

		D23	Ratio of class I , II and III groundwater area of water quality to the total area	%	≥ 75	60~75	45~60	30~45	<30
		D24	Water conservancy investment rate	%	≥ 5	4~5	3~4	2~3	<1
		D25	Industrial water re-utilization rate	%	≥ 80	70~80	60~70	50~60	<50
		D26	Effective irrigation coverage rate	%	≥ 40	30~40	20~30	10~20	<10
		D27	Water irrigation efficiency		≥ 0.65	0.55~0.65	0.45~0.55	0.35~0.45	<0.35
		D28	Water-saving irrigation rate	%	≥ 90	75~90	60~75	45~60	<45
Response indicators B3	Socio-economic response indicators C7	D29	Leakage rate of water supply pipe network	%	<10	10~13	13~16	16~19	≥ 19
		D30	Water-saving appliances penetration rate	%	≥ 60	50~60	40~50	30~40	<30
		D31	Ratio of urban population access to up-to-standard drinking water to the total urban population	%	≥ 99	96~99	93~96	90~93	<90
		D32	Ratio of rural population access to up-to-standard drinking water to the total rural population	%	≥ 85	75~85	65~75	55~65	<55
		D33	Perfection degree of management system and legal system		absolute good	Good	medium	poor	absolute poor

1

Table 3. Weights of water resources security evaluation indicator

	C1	C2	C3	C4	C5	C6	C7	D-B weights	B1	B2	B3	D-A weights
	C-B weights								B-A weights			
	0.4444	0.3222	0.2333	0.3778	0.3111	0.3111	1.0000		0.4111	0.3333	0.2556	
D1	0.1880							0.0836				0.0344
D2	0.1720							0.0764				0.0314
D3	0.2160							0.0960				0.0395
D4	0.2320							0.1031				0.0424
D5	0.1920							0.0853				0.0351
D6		0.2313						0.0745				0.0306
D7		0.2313						0.0745				0.0306
D8		0.2813						0.0906				0.0373
D9		0.2563						0.0826				0.0339
D10			0.6250					0.1458				0.0600
D11			0.3750					0.0875				0.0360
D12				0.5500				0.2078				0.0693
D13				0.4500				0.1700				0.0567
D14					0.2040			0.0635				0.0212
D15					0.2080			0.0647				0.0216
D16					0.2000			0.0622				0.0207
D17					0.1920			0.0597				0.0199
D18					0.1960			0.0610				0.0203
D19						0.2200		0.0684				0.0228
D20						0.2120		0.0660				0.0220
D21						0.1960		0.0610				0.0203

D22	0.1960	0.0610	0.0203
D23	0.1760	0.0548	0.0183
D24	0.0940	0.0925	0.0236
D25	0.0950	0.0938	0.0240
D26	0.0950	0.0938	0.0240
D27	0.0950	0.0938	0.0240
D28	0.0950	0.0938	0.0240
D29	0.0890	0.0863	0.0220
D30	0.0950	0.0938	0.0240
D31	0.1170	0.1213	0.0310
D32	0.1170	0.1213	0.0310
D33	0.1080	0.1100	0.0281

1

1 **Table 4. Determination of μ_{total}**

i	$\mu_R(M_i)$	$\mu_L(M_i)$	$\mu_T(M_i)$
1	0.2308	1.0000	0.1154
2	0.6667	0.8000	0.4334
3	0.5833	0.5833	0.5000
4	0.8000	0.4000	0.7000
5	1.0000	0.2308	0.8846

1
2

Table 5. Indicator value of 9 provinces in water resources security evaluation system in the Yellow River Basin

Indicator	A ₁ Qinghai	A ₂ Sichuan	A ₃ Gansu	A ₄ Ningxia	A ₅ Inner Mongolia	A ₆ Shaanxi	A ₇ Shanxi	A ₈ Henan	A ₉ Shandong
D1	0.28	0.30	0.15	0.08	0.13	0.14	0.11	0.25	0.21
D2	114.73	164.59	63.19	16.01	9.18	47.74	31.51	105.51	78.31
D3	0.08	0.00	0.28	0.46	1.88	1.91	2.43	4.63	5.04
D4	11.55	16.46	6.60	2.06	2.80	6.68	5.58	15.18	12.88
D5	0.12	0.01	0.46	7.46	2.32	0.70	0.74	1.01	1.13
D6	9.28	0.79	42.58	908.40	533.79	49.62	48.21	105.96	763.57
D7	339.02	100.00	163.19	212.30	85.95	122.89	108.92	177.87	150.58
D8	441.77	134.08	304.19	1128.89	353.94	195.75	133.50	185.66	153.68
D9	312.00	182.00	235.00	228.00	84.00	92.00	67.00	101.00	71.00
D10	0.05	0.00	0.17	2.44	2.16	0.75	0.96	0.46	1.32
D11	0.00	0.00	0.00	0.97	0.00	0.07	2.19	1.16	0.00
D12	1.11	0.71	1.18	1.14	1.09	1.24	1.41	0.97	1.13
D13	3900.74	31123.47	518.24	175.58	496.71	312.89	245.96	321.24	218.17
D14	1.34	0.14	3.08	15.53	6.52	4.71	4.16	15.65	14.58
D15	451.99	266.96	242.26	1321.36	1156.91	220.68	183.56	331.21	247.08
D16	1.02	1.99	0.80	1.17	3.27	1.13	1.38	1.78	1.61
D17	76.02	83.33	58.56	90.19	87.16	61.42	59.82	69.56	57.59
D18	68.63	60.95	63.88	69.40	80.83	75.58	66.69	73.35	75.78
D19	0.29	0.00	0.91	0.86	0.56	1.15	0.69	1.59	0.61
D20	15.27	21.18	58.44	74.81	82.86	66.30	78.12	54.05	52.20
D21	78.00	50.00	55.00	37.00	43.80	47.10	34.00	48.20	27.60
D22	90.50	58.40	59.90	54.00	38.20	41.80	32.20	44.10	20.00
D23	94.00	100.00	44.83	61.34	49.95	79.14	17.28	18.80	6.06

D24	5.09	0.18	2.38	2.89	0.47	1.29	2.65	1.82	0.50
D25	57.00	65.00	45.00	55.00	58.00	60.00	76.00	72.00	70.00
D26	38.47	2.14	16.34	40.53	60.19	41.93	34.15	59.49	87.71
D27	0.38	0.46	0.47	0.34	0.44	0.57	0.60	0.55	0.62
D28	27.90	0.00	46.80	30.97	42.84	54.61	68.67	34.89	46.00
D29	13.50	18.70	17.80	22.00	16.30	19.00	15.60	18.00	20.00
D30	36.30	22.00	45.50	22.40	55.10	60.30	50.10	53.50	55.00
D31	96.00	100.00	89.00	96.00	54.00	94.00	86.00	90.00	100.00
D32	54.13	64.88	58.54	44.37	58.27	60.92	46.75	60.81	70.87
D33	0.70	0.70	0.50	0.43	0.43	0.50	0.50	0.50	0.50

1

1 **Table 6. Indicator value of 9 standards in water resources security evaluation system in the Yellow River Basin**

2

Indicator	A_e	A_f	A_g	A_h	A_i	A_j	A_k	A_l	A_m
D1	0.22	0.21	0.20	0.18	0.17	0.16	0.15	0.13	0.12
D2	80.00	71.25	62.50	53.75	45.00	36.25	27.50	18.75	10.00
D3	4.00	3.63	3.25	2.88	2.50	2.13	1.75	1.38	1.00
D4	35.00	31.25	27.50	23.75	20.00	16.25	12.50	8.75	5.00
D5	2.00	2.25	2.50	2.75	3.00	3.25	3.50	3.75	4.00
D6	50.00	55.00	60.00	65.00	70.00	75.00	80.00	85.00	90.00
D7	50.00	55.00	60.00	65.00	70.00	75.00	80.00	85.00	90.00
D8	200.00	220.00	240.00	260.00	280.00	300.00	320.00	340.00	360.00
D9	65.00	71.25	77.50	83.75	90.00	96.25	102.50	108.75	115.00
D10	0.90	1.00	1.10	1.20	1.30	1.40	1.50	1.60	1.70
D11	0.80	0.85	0.90	0.95	1.00	1.05	1.10	1.15	1.20
D12	1.00	1.05	1.10	1.15	1.20	1.25	1.30	1.35	1.40
D13	750.00	712.50	675.00	637.50	600.00	562.50	525.00	487.50	450.00
D14	12.00	11.00	10.00	9.00	8.00	7.00	6.00	5.00	4.00
D15	600.00	550.00	500.00	450.00	400.00	350.00	300.00	250.00	200.00
D16	1.80	1.75	1.70	1.65	1.60	1.55	1.50	1.45	1.40
D17	65.00	67.50	70.00	72.50	75.00	77.50	80.00	82.50	85.00
D18	125.00	118.75	112.50	106.25	100.00	93.75	87.50	81.25	75.00
D19	2.70	2.48	2.25	2.03	1.80	1.58	1.35	1.13	0.90
D20	35.00	40.00	45.00	50.00	55.00	60.00	65.00	70.00	75.00
D21	65.00	61.25	57.50	53.75	50.00	46.25	42.50	38.75	35.00
D22	65.00	61.25	57.50	53.75	50.00	46.25	42.50	38.75	35.00
D23	60.00	56.25	52.50	48.75	45.00	41.25	37.50	33.75	30.00
D24	4.00	3.75	3.50	3.25	3.00	2.75	2.50	2.25	2.00

D25	75.00	72.50	70.00	67.50	65.00	62.50	60.00	57.50	55.00
D26	70.00	67.50	65.00	62.50	60.00	57.50	55.00	52.50	50.00
D27	0.55	0.53	0.50	0.48	0.45	0.43	0.40	0.38	0.35
D28	75.00	71.25	67.50	63.75	60.00	56.25	52.50	48.75	45.00
D29	13.00	13.75	14.50	15.25	16.00	16.75	17.50	18.25	19.00
D30	55.00	52.50	50.00	47.50	45.00	42.50	40.00	37.50	35.00
D31	96.00	95.25	94.50	93.75	93.00	92.25	91.50	90.75	90.00
D32	75.00	72.50	70.00	67.50	65.00	62.50	60.00	57.50	55.00
D33	0.70	0.50	0.50	0.50	0.43	0.43	0.43	0.12	0.12

1
2

Table 7. Summary of Indicator values in Average Ranking Procedure

	MADM Methods				Mean Rankings
	M1	M2	M3	M4	
A_1 Qinghai	11	18	6	15	12.50
A_2 Sichuan	16	17	2	18	13.25
A_3 Gansu	7	16	8	10	10.25
A_4 Ningxia	1	1	1	1	1.00
A_5 Inner Mongolia	4	10	4	4	5.50
A_6 Shaanxi	9	8	11	11	9.75
A_7 Shanxi	6	4	3	7	5.00
A_8 Henan	14	9	14	14	12.75
A_9 Shandong	12	14	7	9	10.50
A_e	18	15	18	17	17.00
A_f	17	13	17	16	15.75
A_g	15	12	16	13	14.00
A_h	13	11	15	12	12.75
A_i	10	7	13	8	9.50
A_j	8	6	12	6	8.00
A_k	5	5	10	5	6.25
A_l	3	3	9	3	4.50
A_m	2	2	5	2	2.75

1
2

Table 8. N×N matrix used in Borda and Copeland methods

	A_1	A_2	A_3	A_4	A_5	A_6	A_7	A_8	A_9	A_e	A_f	A_g	A_h	A_i	A_j	A_k	A_l	A_m	S_j	
A_1	0	0	1	1	1	1	1	0	0	0	0	0	0	1	1	1	1	1	1	10
A_2	0	0	1	1	1	1	1	1	1	0	0	1	1	1	1	1	1	1	1	14
A_3	0	0	0	1	1	0	1	0	1	0	0	0	0	0	0	1	1	1	1	7
A_4	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
A_5	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	3
A_6	0	0	1	1	1	0	1	0	0	0	0	0	0	0	1	1	1	1	1	8
A_7	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	3
A_8	0	0	1	1	1	1	1	0	1	0	0	0	0	1	1	1	1	1	1	11
A_9	0	0	0	1	1	0	1	0	0	0	0	0	0	1	1	1	1	1	1	8
A_e	1	0	1	1	1	1	1	1	1	0	1	1	1	1	1	1	1	1	1	16
A_f	1	0	1	1	1	1	1	1	1	0	0	1	1	1	1	1	1	1	1	15
A_g	0	0	1	1	1	1	1	1	1	0	0	0	1	1	1	1	1	1	1	13
A_h	0	0	1	1	1	1	1	0	1	0	0	0	0	1	1	1	1	1	1	11
A_i	0	0	0	1	1	0	1	0	0	0	0	0	0	0	1	1	1	1	1	7
A_j	0	0	0	1	1	0	1	0	0	0	0	0	0	0	0	1	1	1	1	6
A_k	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0	1	1	4
A_l	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2
A_m	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1

S'_j	2	0	8	17	13	7	12	4	7	0	1	3	4	8	10	12	15	16
$S_{j_}S'_j$	8	14	-1	-17	-10	1	-9	7	1	16	14	10	7	-1	-4	-8	-13	-15

1

2 **Table 9. Evaluation level of water resources security by 3 MADM Aggregation methods in 9 provinces in 2006**

	Absolute Security		Critical security						Insecurity				Absolute insecurity
	Aa	Ab	Ac	Ad	Ae	Af	Ag	Ah	Ai	Aj	Ak	Al	
(a) Average ranking procedure method													
Qinghai								√					
Sichuan							√						
Gansu								√					
Ningxia													√
Inner Mongolia												√	
Shaanxi								√					
Shanxi												√	
Henan								√					
Shandong									√				
(b) Borda method													
Qinghai									√				
Sichuan						√							
Gansu									√				
Ningxia													√
Inner Mongolia												√	
Shaanxi									√				
Shanxi												√	
Henan								√					
Shandong									√				

(c) Copeland method

Qinghai		√					
Sichuan	√						
Gansu				√			
Ningxia							√
Inner Mongolia						√	
Shaanxi				√			
Shanxi						√	
Henan			√				
Shandong				√			

1 **Table 10. Water resources security levels in administrative regions in the**
 2 **Yellow River Basin under Copeland aggregation method (in 2006)**

Security level					
	Absolute security	security	Critical security	Insecurity	Absolute insecurity
Provinces			Sichuan, Qinghai, Henan, Shaanxi and Shandong, Gansu	Shanxi and Inner Mongolia	Ningxia

3

1
2 **Table 11. Ranking results of indicator value in Shanxi, Inner Mongolia and Ningxia provinces**

Evaluation indicator		Shanxi	Inner Mongolia	Ningxia		
Pressure indicators B1	C1 indicators	D1	Water production coefficient	8	7	9
		D2	Annual runoff	7	9	8
		D3	Modulus of groundwater resources	3	5	6
		D4	Modulus of water resources	7	8	9
		D5	Utilization rate	5	8	9
	C2 indicators	D6	Development degree of surface water	4	7	9
		D7	Development degree of groundwater	1	3	8
		D8	Water consumption per 10,000 Yuan of GDP	1	7	9
		D9	Water consumption per 10,000 Yuan of industrial output	1	3	7
		D10	Ratio of pollutants (COD and ammonia nitrogen)dumped into the river	6	8	9
State indicators B2	C3 indicators	D1	Area ratio of excessive extraction of groundwater	9	2	7
		D1	Index of water resources demand-supply balance(IWDS)	9	3	6
		D2	Water resources amount per capita	7	4	9
	C5 indicators	D1	Water consumption modulus	6	4	2
		D1	Water supply amount per capita	9	2	1
		D1	GDP per capita	5	1	6
		D1	Agricultural water consumption ratio	3	8	9

		D1 8	Domestic water consumption per capita	7	1	4
		D1 9	Eco-environment water consumption ratio	5	7	4
		D2 0	Ratio of soil erosion area to the total area	8	9	7
		D2 1	Up-to-standard rate of water quality in water function area	8	6	7
		D2 2	Ratio of up-to-standard river length of water quality to the total river length	8	7	4
		D2 3	Ratio of class I , II and III groundwater area of water quality to the total area	8	5	4
Response indicators B3	Socio-economic response indicators C7	D2 4	Water conservancy investment rate	7	2	8
		D2 5	Industrial water re-utilization rate	1	6	8
		D2 6	Effective irrigation coverage rate	7	2	5
		D2 7	Water irrigation efficiency	8	3	1
		D2 8	Water-saving irrigation rate	1	5	7
		D2 9	Leakage rate of water supply pipe network	2	3	9
		D3 0	Water-saving appliances penetration rate	5	2	8
		D3 1	Ratio of urban population access to up-to-standard drinking water to the total urban population	8	9	4
		D3	Ratio of rural population access to up to standard drinking water to the total	8	6	9

	2	rural population			
	D3	Perfection degree of management system and legal system			
	3		5	8	9

1

1 Figure captions

2

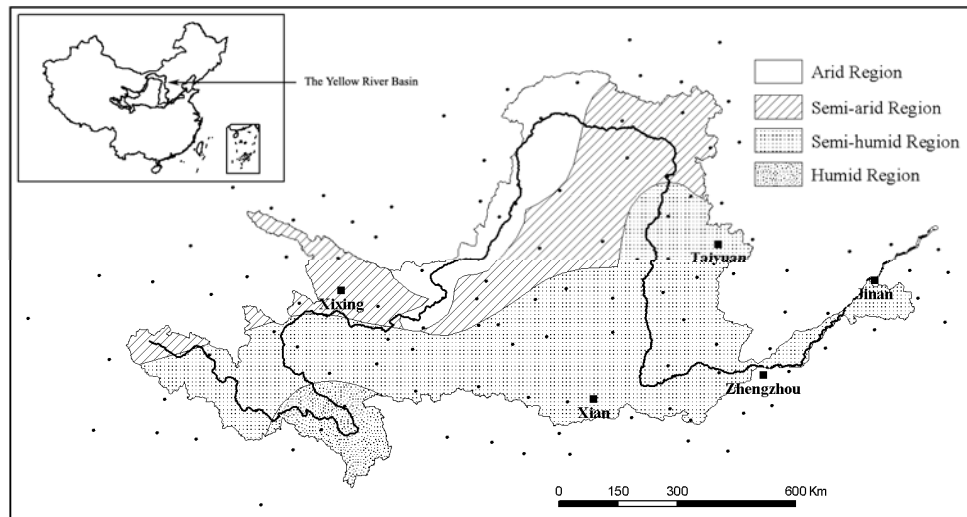
3 Fig. 1. The Yellow River Basin

4 Fig. 2. Administrative regions to be evaluated of the Yellow River Basin

5 Fig. 3. One scale for the graph of membership function (Hwang et al., 1992)

6 Fig. 4. Copeland aggregation results in the nine provinces

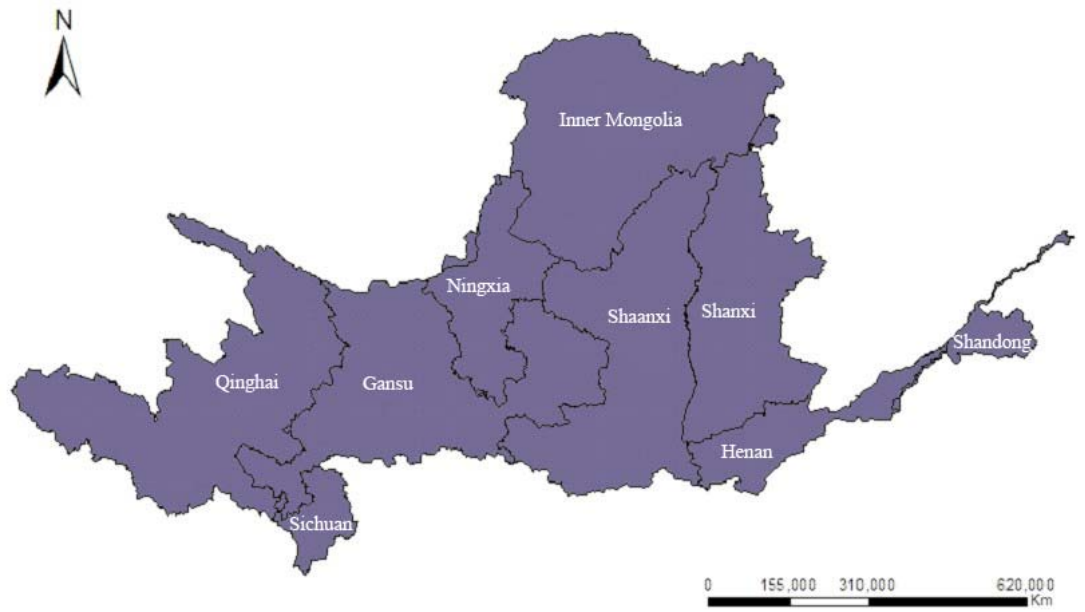
7



1

2

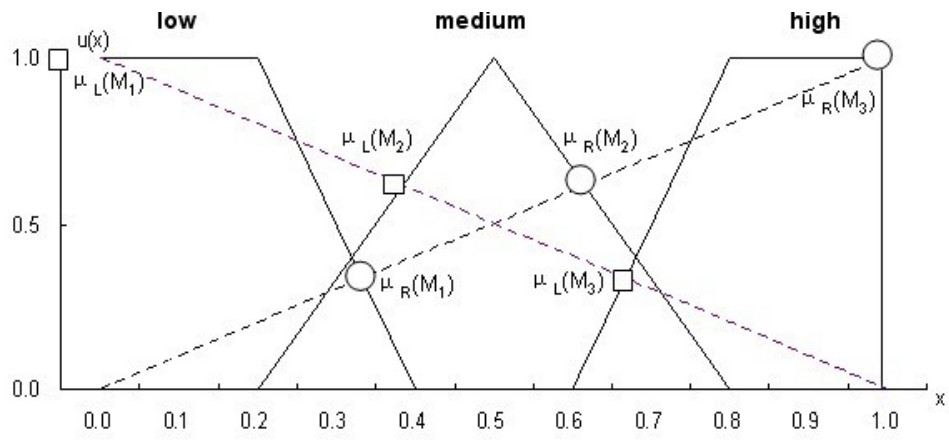
Fig. 1. The Yellow River Basin



1
2
3
4
5
6
7
8
9

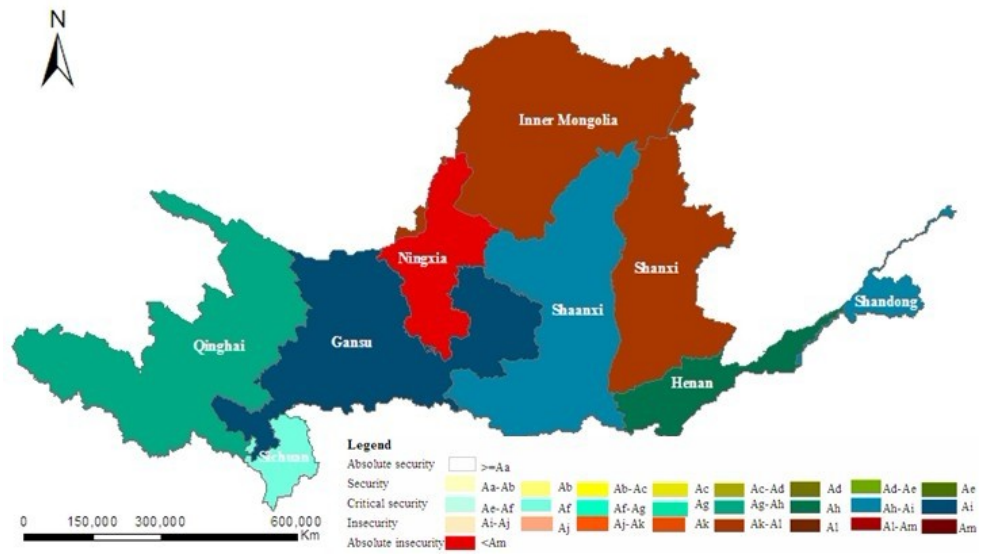
Fig. 2. Administrative regions to be evaluated of the Yellow River Basin

1
2
3



4

5 **Fig. 3. One scale for the graph of membership function (Hwang *et al.*, 1992)**



1

2 **Fig. 4. Copeland aggregation results in the nine provinces**