

1 Quantifying river form variations in the Mississippi Basin 2 using remotely sensed imagery

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7 8 **Abstract**

9 Geographic variations in river form are often estimated using the framework of downstream
10 hydraulic geometry (DHG), which links spatial changes in discharge to channel width, depth,
11 and velocity through power-law models. These empirical relationships are developed from
12 limited *in situ* data and do not capture the full variability in channel form. Here, we present a
13 dataset of 1.2×10^6 river widths in the Mississippi Basin measured from the Landsat-derived
14 National Land Cover Dataset that characterizes width variability observationally. We
15 construct DHG for the Mississippi drainage by linking DEM-estimated discharge values to
16 each width measurement. Well-developed DHG exists over the entire Mississippi basin,
17 though individual sub-basins vary substantially from existing width-discharge scaling.
18 Comparison of depth predictions from traditional depth-discharge relationships with a new
19 model incorporating width into the DHG framework shows that including width improves
20 depth estimates by, on average, 24%. Results suggest that channel geometry derived from
21 remotely sensed imagery better characterizes variability in river form than do estimates based
22 on DHG.

23 **1 Introduction**

24 River systems connect the terrestrial and oceanic reservoirs of the hydrologic cycle and play a
25 crucial role in landscape development and freshwater resources. Because spatial changes in
26 river form are physical expressions of interaction between a river's flow and the surrounding
27 environment, they are critical to a wide range of scientific and engineering fields. For
28 example, channel geometry, which includes the key variables of width, depth, velocity, slope,
29 and planform shape, reflects local and regional uplift in bedrock and alluvial rivers and

1 responds to changes in bedrock lithology [Bjerklie, 2007; Whipple, 2004; Montgomery, 2004;
2 Harbor, 1998; Amos and Burbank, 2007; Montgomery and Gran, 2001; Garrett, 1986]. River
3 width and depth play a vital role in CO₂ and nutrient exchange [Butman and Raymond, 2011;
4 Alexander et al, 2000; Wollheim et al., 2006; Peterson et al., 2001]. Aquatic habitat
5 distribution is partially dependent on channel geometry, which both influences the spatial
6 extent of habitats and acts as a barrier to terrestrial species migration [Jowett, 1998; Newson
7 and Newson, 2000; Ayres and Clutton-Brock, 1992; Hayes and Sewlal, 2004]. Humans
8 depend on accurate assessments of river form for understanding flooding hazards,
9 transportation planning, and fisheries management [Hobley et al., 2012; Apel et al., 2009;
10 McCartney, 1986; Troitsky, 1994; Prevost et al., 2003]. Channel shape is also a principal
11 parameter in hydrologic and hydrodynamic models [Paiva et al., 2013; Neal et al., 2012;
12 Yamazaki et al., 2011]. Because of their wide-ranging importance to science and engineering,
13 spatial patterns of channel shape have been studied since at least the work of Leonardo Da
14 Vinci in the 16th century (Humphrey and Abbott, 1867; Bellasis, 1913; Shepherd and Ellis,
15 1997).

16

17 The framework of downstream hydraulic geometry (DHG), developed by Leopold and
18 Maddock [1953], relates spatial patterns of river form to variations in constant-frequency
19 discharge throughout a basin. Three fundamental power-law equations relate width (w), depth
20 (d), and velocity (v) to downstream changes in discharge (Q):

$$21 \quad w = aQ^b \quad (1a)$$

$$22 \quad d = cQ^f \quad (1b)$$

$$23 \quad v = kQ^m \quad (1c)$$

24 where b , f , m , a , c , and k are exponents and coefficients either derived from physical
25 characteristics or, more commonly, calculated empirically. To facilitate comparison of
26 channel shapes over a large geographic extent, the discharge used in DHG is spatially variable
27 and, ideally, of a constant return period. Some subsequent analyses of natural channels have
28 shown consistency in geometric exponents ($b \approx 0.5$, $f \approx 0.4$; $m \approx 0.1$) [Leopold and Maddock,
29 1953; Leopold and Miller, 1956; Moody and Troutman, 2002; Chaplin, 2005], while others
30 have found variability in exponents related to changes in basin size, tectonic activity, bedrock
31 lithology, channel vegetation, and levels of human influence [Park, 1977; Klein, 1981;

1 Osterkamp and Hedman, 1982; Montgomery and Gran, 2001; Montgomery, 2004; Piestch and
2 Nanson, 2011].

3

4 Most prior investigations of geographic variability in equilibrium channel form rely on *in situ*
5 measurements of river geometry, which are usually available only at widely-spaced locations.
6 This methodology faces two fundamental obstacles in characterizing spatial variations in
7 width and depth. First, the time-intensive nature of *in situ* channel measurement limits the
8 number of measurement locations to a maximum of hundreds [Moody and Troutman, 2002]
9 to thousands [Lee and Julien, 2006]. This restricts either the spatial extent of study areas to
10 smaller basins [e.g. Wolman, 1955] or the density of measurements to wide spacing over
11 larger areas [e.g. Moody and Troutman, 2002; Leopold and Maddock, 1953]. Second, *in situ*
12 channel measurements are often acquired at permanent streamflow gauging sites where
13 accuracy of discharge measurements is usually prioritized, potentially biasing site selection
14 towards desired features such as stable, single-channel cross-sections that may not accurately
15 represent the full range of channel characteristics [Rantz, 1982; Ibbitt, 1997]. These factors
16 suggest that traditional investigations of river shape may not always encompass the full range
17 of spatial variability in channel geometry. Despite these limitations of DHG in describing
18 geometric variations over regional and continental scales, it is often used to estimate channel
19 characteristics in studies of landscape evolution [Tucker and Bras, 1998], nutrient flux
20 [Carleton and Mohamoud, 2013], carbon emissions [Butman and Raymond, 2011; Raymond
21 et al, 2013], width and depth distributions [Andreadis et al., 2013] and the movement of
22 materials, energy, and organisms [Sabo and Hagen, 2012].

23

24 Due to the importance of river form and the difficulty of obtaining wide-scale *in situ* channel
25 measurements, remote sensing has increasingly been used to characterize river width, depth,
26 and velocity [e.g. Legleiter, 2012; Fonstad and Marcus, 2005; Pavelsky and Smith, 2009;
27 Mersel et al., 2013]. As the river parameter most readily observable from remotely sensed
28 data, river width has been quantified using a variety of passive and active sensors since the
29 early stages of the Landsat satellite program in the 1970s [Rango and Salomonson, 1974;
30 Watson, 1991; Smith et al., 1996, Allen et al., 2013]. While remote sensing of channel width
31 has generally covered single rivers or limited spatial extents, recognition of the potential for

1 large-scale width measurement has recently led to regional and global studies [Pavelsky et al.,
2 accepted; Yamazaki et al., in review; Andreadis et al., 2013].

3

4 The RivWidth software tool allows automated and spatially continuous channel width
5 measurements from remotely sensed imagery or other gridded data sources [Pavelsky and
6 Smith, 2008]. In this study, we use RivWidth and the Landsat-based National Land Cover
7 Dataset (NLCD) to quantify the spatial variability of river width at approximately mean
8 annual discharge in the Mississippi River Basin and its major sub-basins (Figure 1). We then
9 match width measurements with mean annual discharge values estimated from discharge-
10 drainage area relationships to construct DHG relationships for the basin as a whole and for
11 major sub-basins. Finally, we use our measured widths and estimated discharge values along
12 with *in situ* channel width, area, and discharge measurements from U.S. Geological Survey
13 (USGS) streamflow gauging stations to estimate continuous mean channel depths using a
14 multiple linear regression framework. With these high-resolution, spatially extensive datasets
15 we test the large-scale applicability of downstream hydraulic geometry and create a dataset
16 that replaces DHG-based estimates for many applications.

17

18 **2 Data and Methods**

19 **2.1 Calculating river widths**

20 To develop a high-resolution dataset of river widths over a large area it is necessary to
21 automate width measurement. The RivWidth software tool is designed to calculate river
22 widths from a gridded map of inundation extent [Pavelsky and Smith, 2008]. Its functionality
23 allows calculation of river width at each pixel in an automatically-derived river centerline,
24 and it can be used on both single-channel and multichannel river reaches. Previous studies
25 have used inputs from MODIS, Landsat, SPOT-5 satellite images, and the U.S. Geological
26 Survey's National Land Cover Dataset (NLCD) [Pavelsky and Smith, 2008; Smith and
27 Pavelsky, 2008; Allen et al., 2013; Pavelsky et al., In Press]. In this study, we used the open
28 water class in the NLCD as input to calculate river widths for the Mississippi basin. The
29 NLCD, derived from 30 m Landsat imagery, is an integration of land cover extents from
30 early, peak, and late growing seasons [Homer et al., 2001]. Although inundation extents are
31 not explicitly calibrated to any discharge frequency, we hypothesize that they will, on

1 average, represent mean growing season streamflow. Tests of this hypothesis are described in
2 Sections 2.2 and 3.2. The NLCD classification was selected for this study because it is a
3 well-established product with thoroughly-described methods, and because it covers nearly the
4 entire Mississippi Basin. A small portion of the basin extends outside the coverage of the
5 NLCD into Canada, and this area was not included in our analysis because the techniques
6 used to classify open water would be inconsistent with the rest of the basin. To create as
7 complete and continuous a dataset as possible, bridges, dams and other small gaps in river
8 extent were manually removed. Widths were measured at one pixel intervals (every 30 to ~42
9 m) for all visible continuous channels as narrow as one pixel (30 m) in width, although not all
10 rivers as narrow as 30 m were measured (see Section 3.1 for details).

11
12 To measure river width from remotely sensed imagery, RivWidth: 1) creates a channel mask
13 by removing water bodies not connected to the river channel; 2) determines the distance from
14 each river pixel to the nearest non-river pixel and calculates the derivative of the resulting
15 distance image (Figure 2c, 2d); 3) determines the river centerline based on the derivative map,
16 in which centerline pixels have values close to zero and all other river pixels have values of
17 approximately one; and 4) calculates the flow width along a line segment orthogonal to the
18 direction of flow at each centerline pixel (Figure 2e). Finally, we eliminated measurements
19 for lakes and reservoirs within the channel systems by removing segments where the NLCD
20 open water class included clear tributary streams adjoining rivers. Further descriptions,
21 updates and downloads are available from *Pavelsky and Smith* [2008] and at
22 <http://www.unc.edu/~pavelsky/>.

23

24 **2.2 Width validation**

25 To assess the accuracy of RivWidth measurements and the appropriateness of the NLCD for
26 describing channel form at mean flows, we compared *in situ* USGS channel data
27 corresponding to long-term mean annual discharges to validate width measurements.
28 Bankfull discharge is often used in fluvial studies because it approximates the dominant
29 channel-forming flow [e.g. Wolman, 1955; Leopold and Miller, 1956; Chaplin, 2005; Pietsch
30 and Nanson, 2011]. Long-term mean annual discharge is also commonly used to study fluvial
31 processes [Leopold and Maddock, 1953; Griffiths, 1980; Molnar and Ramirez, 2002], and
32 comparison of DHG exponents from a range of flow frequencies shows relatively minor

1 variation [Knighton, 1974; Griffiths, 1980; Ibbitt, 1997]. Repeated width, depth, and velocity
2 measurements from the USGS at gauging stations throughout the Mississippi Basin are
3 available online [waterdata.usgs.gov/NWIS; Juracek and Fitzpatrick, 2009]. Although
4 unpublished, these data have been used in investigations of channel geometry [Bowen and
5 Juracek, 2011; Stover and Montgomery, 2001]. The number of measurements at each gauge
6 location varies from fewer than ten to thousands across a range of flows. We removed gauges
7 with fewer than 10 years of mean discharge data and those with no discharge or channel
8 measurements after 1970. For each gauge, we estimated the width, depth, and velocity
9 corresponding to mean annual discharge by calculating the mean value of all channel
10 measurements acquired within +/-10% of long-term mean annual discharge. Measurements
11 that are clearly erroneous, listed as “poor” by the USGS, taken more than 60 m (two NLCD
12 pixels lengths) upstream or downstream from the gauge location, or measured using a crane
13 along a bridge not perpendicular to the river (therefore not representing true channel width)
14 were removed. We then calculated total error in our width measurements by comparing *in*
15 *situ* gauge width from the 456 stations meeting our criteria against the mean of the five closest
16 RivWidth-derived width measurements.

17

18 **2.3 Construction of downstream hydraulic geometry**

19 Construction of DHG relationships requires knowledge of downstream changes in discharge
20 (equation 1a-c) [Leopold and Maddock, 1953]. To build DHG relationships continuously
21 downstream, we used upstream drainage area as a proxy for discharge. We calculated
22 drainage area from the 90-m resolution HydroSHEDS digital elevation model [Lehner et al.,
23 2008] and then assigned the nearest drainage area value to each RivWidth pixel using the
24 methodology developed by Allen et al. [2013] (Figure 3). A linear relationship between
25 upstream drainage area and discharge has been commonly assumed in small basins [e.g.
26 Pazzaglia et al., 1998; Montgomery and Gran, 2001], but for larger rivers this relationship
27 may become nonlinear if the basin includes variations in geology, tectonic deformation,
28 climate, or land use [Stall and Fok, 1968; Galster et al., 2006; Tague and Grant, 2004]. To
29 account for these variations, we developed discharge-drainage area relationships for
30 individual subbasins using values of discharge and drainage area for all USGS stations with
31 ≥ 10 years of approved mean annual discharge. Because discharge-drainage area scaling
32 deviates from linearity over large spatial extents in some basins (Figure 4), we calculated

1 least-squares linear regressions for each hydrologic accounting unit (i.e. subbasin) in the
2 Ohio, Upper Mississippi, and much of the Missouri and Lower Mississippi basins. In 7
3 accounting units containing RivWidth measurements in the Missouri, 12 in the Lower
4 Mississippi, and the entire Arkansas basin (excluding the White River), lack of gauging
5 stations, substantial precipitation variability, or large-scale water withdrawals precluded
6 gauge-based discharge estimation (Table 1). These subbasins, along with those not
7 containing rivers large enough to be measured by RivWidth, are not considered in the DHG
8 portion of our analysis.

9

10 **2.4 Depth estimation**

11 We evaluated three methods of calculating spatial depth distributions, each using channel
12 measurements from 358 USGS gauging stations in regions of the Missouri, Upper
13 Mississippi, and Ohio Basins where both RivWidth measurements and DEM-based discharge
14 estimates were available. First, we developed a traditional depth-discharge relationship for
15 the Mississippi using USGS gauge data from within the basin. Second, we estimated depth
16 using the global depth-discharge equation developed by Moody and Troutman [2002].
17 Finally, we performed a multiple linear regression of log-transformed *in situ* depth against
18 log-transformed *in situ* width and discharge measurements. We then used our measured
19 widths and estimated discharge values to calculate depth at each centerline pixel and
20 evaluated whether including river width as a variable improves depth estimates over depth-
21 discharge methods. We assessed the effectiveness of including the influence of width in
22 depth estimation by calculating the mean percentage error of each depth estimate relative to
23 USGS-measured depth values. Due to increasing uncertainty in RivWidth measurements and
24 discharge estimations for smaller rivers, we limited this depth validation to rivers wider than
25 100 m.

26

27 **3 Results**

28 **3.1 Measurement and distribution of river widths**

29 Using the National Land Cover Dataset, we measured 1.194×10^6 individual channel widths
30 representing 42×10^3 km of rivers in the Mississippi basin (Figure 5). Widths ranged from
31 the minimum pixel size of 30 m to 7400 m in the inundated areas of the Upper Mississippi.

1 Measurement count and length for each of the five sub-regions of the Mississippi are shown
2 in Table 2. Overall distribution of river widths greater than 100 m and less than 1500 m
3 (Figure 6) closely follows a negative power-law distribution

$$4 \quad n = 2.1 \times 10^9 W^{-1.9}, \quad (2)$$

5 where n is the number of pixels of a corresponding width and W is the width. Bars for rivers
6 <100 m in width are included in Figure 6 to indicate the distribution of width data analyzed
7 here, but because we do not capture all rivers at these widths our dataset cannot be used to
8 describe the true distribution of rivers <100 m wide. To evaluate the completeness of this
9 dataset and assess its accuracy, we downloaded historical channel measurements from 2,466
10 USGS streamflow gauges taken at long-term mean annual discharge. Of these, widths are
11 greater than 30 m (the minimum width theoretically measurable) at 854 locations. Figure 7
12 shows the percentage of gauges measured in 10 m width increments. Almost all (> 99%)
13 gauge locations wider than 90 m are measured, while the most substantial decrease occurs as
14 width falls below 60 m (two NLCD pixels). The two 100 m gauges not captured by RivWidth
15 are in areas with ambiguous river boundaries, in which the NLCD contains adjacent areas of
16 open water and woody wetlands. At widths between 60 and 100 m, unmeasured stations are
17 more common because not all channels in this size range are adequately captured in the
18 NLCD. The rapid reduction in the percentage of gauges measured at less than 60 m is likely
19 related to difficulties in classifying mixed land-water pixels, which often represent the entire
20 river as width decreases below twice the pixel resolution.

21

22 We use two separate methods to estimate the actual length of rivers between 50 and 100 m in
23 the Mississippi Basin. First, comparison with USGS gauge data suggests that RivWidth
24 measured ~68% of gauges 50-100 m in width. We use this percentage as a correction factor,
25 dividing the number of 50-100 m river measurements made here by 0.68 to estimate the
26 correct number of measurements (the dashed box in figure 6). Second, we use equation 2 to
27 extrapolate from the distribution of measurements for rivers wider than 100 m to those
28 between 50 and 100 m in width (the dot in figure 6). These two methods produce nearly
29 identical values.

30

31 **3.2 Width measurement accuracy**

1 Compared to widths at mean annual discharge from 456 gauging stations in the
2 Ohio/Tennessee, Upper Mississippi, Missouri, and Arkansas regions, mean absolute width
3 error (MAE) is 38 m (Figure 8). Many gauges in the lower Mississippi Region are located in
4 low-lying areas where flow is not confined to a single channel, causing the USGS
5 measurements to include areas that the NLCD classifies as woody wetlands or something
6 other than open water. Because of these complications, gauging stations not on the main stem
7 of the lower Mississippi are excluded. Total mean and median errors of 20 m and 11 m
8 indicate a slight positive bias in RivWidth measurements, although outliers with positive
9 errors of more than 600 m skew the errors substantially. This error can be partitioned into
10 three groups: water mask error, RivWidth error, and inaccuracies in USGS measurements.
11 While stations with measured $W > 60$ m show a median positive bias of only 16 m, stations
12 where $W < 60$ m have a median positive bias of 30 m. This pattern is expected given that
13 small rivers often approach the narrowest width discernable at 30-m spatial resolution.
14 Classification of mixed pixels along banks imparts a theoretical minimum uncertainty of $\frac{1}{2}$
15 the pixel resolution for each bank crossing (i.e. a minimum of 30 m for single-channel rivers
16 at 30 m resolution; Pavelsky and Smith, 2008).

17

18 Inaccuracies associated with the measurement mechanics of RivWidth arise primarily from
19 orthogonal angle errors. Uncertainty results from the predefined spacing of centerline
20 segment endpoints used to define orthogonals to each centerline pixel. In highly sinuous
21 channels where centerlines change direction rapidly, width measurements can be artificially
22 high when orthogonals are not truly perpendicular to the channel. Basin-wide error analysis
23 of widths calculated with endpoint spacings ranging from 7 to 21 pixels showed that
24 inaccuracies are minimized when 11-pixel centerline segments are used, as we do here. In
25 future studies, it may be possible to reduce this source of error by fitting a cubic spline to the
26 channel centerline pixels as described by Legleiter and Kyriakidis (2006). Finally, although
27 we did not attempt to quantify it here due to the large number of stations used, error
28 associated with USGS measurements is minimized through standardized data collection
29 methods [Buchanan and Somers, 1969; Rantz, 1982] and the careful selection of stations as
30 described in section 2.3.

31

32 **3.3 Estimation of discharge**

1 Using the methods described in section 2.3, we estimated discharge from 0.857×10^6
2 measurements for rivers totaling 28×10^3 km in length and draining 2.2×10^6 km² of the
3 Mississippi Basin. To assess discharge estimate accuracy, we compared mean discharges
4 from 346 gauging stations in the measured drainage area to the mean of the nearest 5
5 discharge estimates. Figure 9 shows the nearly 1:1 relationships between estimated discharge
6 and gauge-measured discharge for major sub-basins and for the entire Mississippi. Because
7 ordinary least-squares linear regressions are greatly influenced by high-discharge outliers, we
8 use the Theil-Sen median estimator [Sen, 1968] to derive robust linear regressions for each
9 sub-basin (Table 3). We use the non-parametric Spearman's ρ to characterize goodness-of-
10 fit, as discharges are not normally distributed. Regression slopes close to one and strong
11 correlation between predicted and measured values indicate that estimates of discharge are
12 likely accurate.

13

14 **3.4 Mississippi Basin downstream hydraulic geometry**

15 Using spatially continuous discharge estimates, we construct width-discharge relationships for
16 the Mississippi Basin and, separately, three of its major sub-basins (Figure 10a-d). Measured
17 widths correspond to discharges ranging from 2.6 m³/s to 19 200 m³/s and drainage areas
18 from 169 km² to 2 940 000 km². Linear least-squares regression of log-transformed width
19 and discharge shows that their relationship can be described by the power-law equation:

$$20 \quad w = 16.0Q^{0.43} \quad (r^2 = 0.62) \quad (3)$$

21 However, these values include 38 654 width measurements corresponding to discharge values
22 less than 10 m³/s, which are lower than would be expected for rivers greater than 30 m based
23 on width-discharge relationships from Moody and Troutman (2002) and Leopold and
24 Maddock (1953). 89 % (34 573) of these low-discharge measurements are found in the
25 Missouri sub-basin, where braided streams with high width-depth ratios are common. Of 38
26 USGS gauging stations with mean discharge < 10 m³/s, width is overestimated in all with a
27 mean bias of 52 m (Fig. 8). As such, it is likely that basin-wide widths for discharges below
28 10 m³/s result from the inability to resolve multiple channels at the 30 m resolution of the
29 NLCD. If we remove these anomalous measurements, the width DHG equation becomes:

$$30 \quad w = 13.4Q^{0.46} \quad (r^2 = 0.64) \quad (4)$$

1 These values of a and b fall close to the range of values calculated for world rivers by Moody
2 and Troutman (2002). However, individual sub-basins show substantial variation from these
3 values, with exponents ranging from 0.3 in the Missouri to 0.63 for the Upper Mississippi
4 (Figure 10). With the exception of the Missouri, variations in discharge account for > 50% of
5 width variability ($r^2 = 0.67$ and 0.73 for the Upper Mississippi and Ohio), indicating that in
6 those sub-basins changes in discharge are the primary control on downstream variations in
7 width. The case of the Missouri Basin will be discussed in more detail in Section 4.

9 **3.5 Estimating depth**

10 Using channel measurements from gauges located on streams measured by RivWidth with
11 corresponding discharge estimates, we compared methods of estimating depth with and
12 without width data. The first method is a simple least-squares linear regression of log-
13 transformed depth and discharge from the gauge station dataset, which results in the power-
14 law expression

$$15 \quad d = 0.18Q^{0.47} \quad (r^2=0.73) \quad (5)$$

16 The second method is a multiple linear regression of log-transformed depth against log-
17 transformed discharge and width, which yielded the equation

$$18 \quad \ln(d)=0.44-0.82\ln(w)+0.83 \ln(Q) \quad (r^2=0.85) \quad (6)$$

19 Figure 11 shows depths calculated from equation 6 for the Ohio, Upper Mississippi, Missouri,
20 and main stem of the Lower Mississippi using our estimated discharge and measured widths.

21
22 Basin-wide mean depth error is 40% for the two DHG estimations, and 31% for the multiple
23 regression method (Table 4). Figures 12a-b compare the percentage error of equation (6) to
24 that of the two simple downstream hydraulic geometry relationships (Equation 5 and Moody
25 and Troutman [2002]). Although mean relative error is nearly identical in the Ohio and
26 Upper Mississippi sub-basins, the two discharge-based methods both substantially
27 overestimate depth for seven gauging stations along the Platte River in the Missouri sub-
28 basin, leading to relative errors of 50%. The disparity between approaches in the Missouri
29 accounts for the higher error of the discharge-based equations in the basin as a whole.

1 **4 Discussion and Conclusions**

2 In this study, we present one of the first high-resolution, spatially continuous width datasets
3 covering a major river basin. The utility of remote-sensing based measurement of channel
4 geometry is increasingly recognized for both characterizing width-discharge relationships and
5 applications for hydrologic modeling [Andreadis et al., 2013; Pavelsky et al., accepted;
6 Yamazaki et al., in review]. Construction of a width frequency distribution using 1.2×10^6
7 measurements (Equation 2) shows that Mississippi widths follow a power-law distribution (
8 $n = 2.1 \times 10^9 W^{-1.9}$) comparable to that found by Pavelsky et al. [accepted] for the 8.5×10^5
9 km^2 Yukon basin ($n = 1.78 \times 10^9 W^{-1.72}$). Similarities between these two basins—which
10 represent highly contrasting geology, ecology, climate, and flow regimes—suggest that width
11 distributions in other basins may follow similar patterns.

12

13 Basin-wide width-discharge relationships are characteristic of the downstream hydraulic
14 geometry framework proposed by Leopold and Maddock [1953]. However, in the global
15 analysis of Moody and Troutman [2002], changes in discharge account for >94% of width
16 variation compared to 62% for the Mississippi basin in this study. While error inherent in the
17 RivWidth dataset undoubtedly accounts for some of the higher width variability observed
18 here, it seems unlikely that channel width corresponds as precisely to discharge as is shown in
19 previous work. One explanation for this discrepancy is the widely-spaced and non-random
20 site selection for *in situ* channel measurements. To facilitate accurate discharge
21 measurements, USGS gauging station selection criteria suggest using straight channel
22 segments located away from tributary junctions, with only one channel and easy access
23 (Rantz, 1982). It is not unreasonable to assume that similar site selection bias exists for most
24 *in situ* channel and discharge measurement locations. In particular, the measurement bias
25 towards single-channel rivers in previous DHG studies using gauge data may explain the
26 higher width variability observed in this dataset. Finally, previous investigations of DHG
27 have used datasets incorporating a much wider range of discharges [e.g. Moody and
28 Troutman, 2002] than the rivers used in this study, which may result in higher r^2 values for
29 those width-discharge relationships. Conversely, the fact that our dataset does not include
30 smaller streams may result in a less well-defined best-fit regression.

31

1 Individual sub-basins demonstrate different levels of adherence to traditional downstream
2 hydraulic geometry. Missouri sub-basin channel widths increase with discharge at a much
3 lower rate ($b=0.3$) than has been found in previous studies (e.g. Leopold and Maddock, 1953;
4 Moody and Troutman, 2002) with a much lower proportion of width variation explained by
5 discharge increases ($r^2=0.44$). Conversely, the Ohio sub-basin closely matches previous
6 findings ($b=0.48$; $r^2=0.72$). Several factors could explain this discrepancy. Multi-channel
7 rivers are much more common in the Missouri sub-basin than in the Ohio; despite similar
8 total measured lengths (Table 2) the Missouri contains nearly 2.5 times as many multi-
9 channel measurements as the Ohio. While multiple channel crossings increase inherent
10 RivWidth measurement error as explained in section 3.2, braided streams are also likely to
11 show increased width variability in response to changes in climate and flow regime [Schumm,
12 2005]. The Missouri sub-basin also has some of the highest levels of human influence and
13 control in North America, factors that can affect variability in channel form. In particular,
14 dam construction has varied but pronounced effects on channel morphology [Gregory, 2006;
15 Williams and Wolman, 2004]. Williams [1978] documented highly variable channel
16 narrowing on the Platte River as it crosses the Great Plains due to upstream flow regulation.
17 Human impacts on stream form and flow across the central section of the Missouri drainage
18 may lead to the high width variability and lower than expected increase in width with
19 discharge observed in the Missouri sub-basin. In addition, the substantially drier climate and
20 greater topographic relief in the upstream portions of the Missouri, relative to the Ohio or
21 Upper Mississippi, may also influence the variations in DHG observed here by affecting the
22 balance of water and sediment supplies in the different subbasins.

23

24 Human influence also likely plays a role in the high b -value (0.64) observed in the Upper
25 Mississippi sub-basin. In larger rivers—particularly along the main stem of the Mississippi—
26 lock and dam control structures artificially widen the channel or connect it to secondary
27 channels in its floodplain. Because of difficulties in differentiating the main stem of the
28 Mississippi from ancillary channels and inundated floodplains that connect to the main
29 channels in the NLCD, these features are included in the width-discharge dataset. While the
30 high b -value may not represent the natural width changes, we believe it accurately describes
31 present-day inundation extent along the Upper Mississippi more effectively than would a
32 lower width exponent.

1

2 In sub-basins with well-developed width-discharge relationships, traditional depth-discharge
3 DHG predicts depth well without inclusion of additional information on river width. In the
4 Ohio and Upper Mississippi sub-basins, depth estimates based on the two $d-Q$ relationships
5 show similar accuracy to that of the multiple regression estimation that incorporates width
6 (Equation 6). In the Missouri sub-basin, however, both traditional DHG methods
7 substantially overestimate depth for wide, shallow rivers compared to the multiple regression
8 analysis. Although basin-wide absolute error is not significantly reduced, consistent
9 overestimation of depth for wide, shallow rivers like the Platte suggests that in applications
10 where depths are based on downstream hydraulic geometry [e.g. Alexander, 2000], factoring
11 width into depth estimations substantially reduces uncertainty. This improvement results from
12 the underlying assumption of continuity in the relationship between depth, discharge, width,
13 and velocity; measuring width while assuming locally constant flow eliminates one degree of
14 freedom from the depth equation.

15

16 Several potential sources of error must be addressed when studying channel form using
17 remotely sensed data. The largest sources of uncertainty in our Mississippi dataset are
18 inherent to the input imagery. Because higher pixel resolution decreases classification error,
19 increases total channel length, and decreases the size of smallest rivers measured, selecting
20 appropriate input data is critical. Figure 7 indicates that all rivers greater than three times the
21 pixel resolution and substantial numbers of smaller rivers are measured. While our results
22 suggest that the NLCD represents an approximation of river extent close to mean discharge,
23 there are clear instances where channels are wider than expected due to connectivity with the
24 surrounding floodplain, misclassification of channel boundary pixels, or potential use of
25 images taken during times of higher than mean flows. To reduce the error associated with the
26 input water mask, future investigations should use a consistent and effective river
27 classification scheme on images taken during periods of the desired flow state. Finally,
28 RivWidth must be configured properly, as the segment length used to calculate the orthogonal
29 direction can create non-perpendicular cross-sections when poorly chosen. Other methods of
30 calculating orthogonals to the river centerline, especially implementation of algorithms
31 described by Legleiter and Kyriakidis (2006), may help to minimize this source of error in
32 future studies.

1

2 Provided these sources of error are addressed, RivWidth offers the capability to measure river
3 width at a high resolution over large basins with small and predictable error. Despite the
4 importance of river form and flow, *in situ* river monitoring capabilities have declined over the
5 last several decades [Vorosmarty et al., 2001], highlighting the importance of remote sensing
6 techniques that can produce high-resolution, spatially continuous observations of river
7 channels over large areas [Alsdorf et al., 2007]. Although significant challenges remain in
8 using remotely sensed channel observations to produce discharge measurements, non-real
9 time estimations of river flow relying on width measurement have been made [LeFavour and
10 Alsdorf, 2004; Smith and Pavelsky, 2008]. In addition, multivariate equations for prediction
11 of streamflow [e.g. Bjerklie et al., 2003] often combine river width measurements with
12 information on slope and other river form data. As the most widely observable of the three
13 primary dimensions of river discharge, understanding variations in width is a critical first step
14 in characterizing discharge from remotely sensed data. Because RivWidth produces maps of
15 river centerline it may be useful in characterizing the planform shape of rivers (e.g. via indices
16 of sinuosity and braiding), which would help to reveal downstream patterns in river form.
17 Additionally, intersection of river centerlines with a high-resolution DEM would allow
18 estimation of mean slope, another key variable in understanding river form (Bjerklie 2007).

19

20 In addition to its importance in the measurement of discharge, remote sensing of river width
21 contributes to the accuracy of hydrologic and hydraulic modeling. While width parameters
22 are often characterized through empirically derived discharge relationships [e.g. Yamazaki et
23 al., 2011, Andreadis et al., 2013], the utility of widths from satellite imagery in improving
24 hydraulic modeling of river and floodplain dynamics is increasingly recognized [Neal et al.,
25 2012; Schumann et al., 2009]. Given growing interest in river modeling at continental and
26 global scales and the importance of rivers in natural and human systems, this paper and other
27 recent studies [e.g. Yamazaki et al., in review] demonstrate how data from future satellite
28 missions such as the Surface Water and Ocean Topography mission (jointly under
29 development by the United States and France) can measure the spatial and temporal
30 variability in Earth's surface water resources [Fu et al., 2012]. These products, combined
31 with ongoing work to produce Landsat-derived width datasets globally, will allow for more

1 accurate characterization of spatial variability in channel form than is currently afforded by
2 empirically-derived estimation methods

3

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9

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19 3467-3480, 2014.

20

1 Table 1. Portions of the Mississippi Basin included in and excluded from the analysis

	Ohio	Upper Mississippi	Missouri	Arkansas	Lower Mississippi
Accounting units excluded from DHG estimates	None	None	100200, 100302, 100402, 100500, 100901, 100902, 101301, 101302, 101303, 101600, 101702, 101800, 101900, 102100, 102500, 102802	All basins other than 110100 (Upper White River excluded)	080202, 080204, 080302, 080403, 080701, 080702, 080703, 080801, 080802, 080901, 080902, 080903
Total area included (excluded) in DHG	527900 km ² (0 km ²)	429200 km ² (0 km ²)	727600 km ² (621700 km ²)	57900 km ² (584400 km ²)	119600 km ² (129400 km ²)

2

3 Table 2. Width measurement count and river length

Hydrologic Region	Ohio-Tennessee	Upper Mississippi	Lower Mississippi	Arkansas-Red	Missouri	Total
n	304685	223259	137055	218604	311029	1194632
Length (km)	10761	7872	4819	7699	10944	42095

4

5 Table 3. Estimated discharge-measured discharge regressions

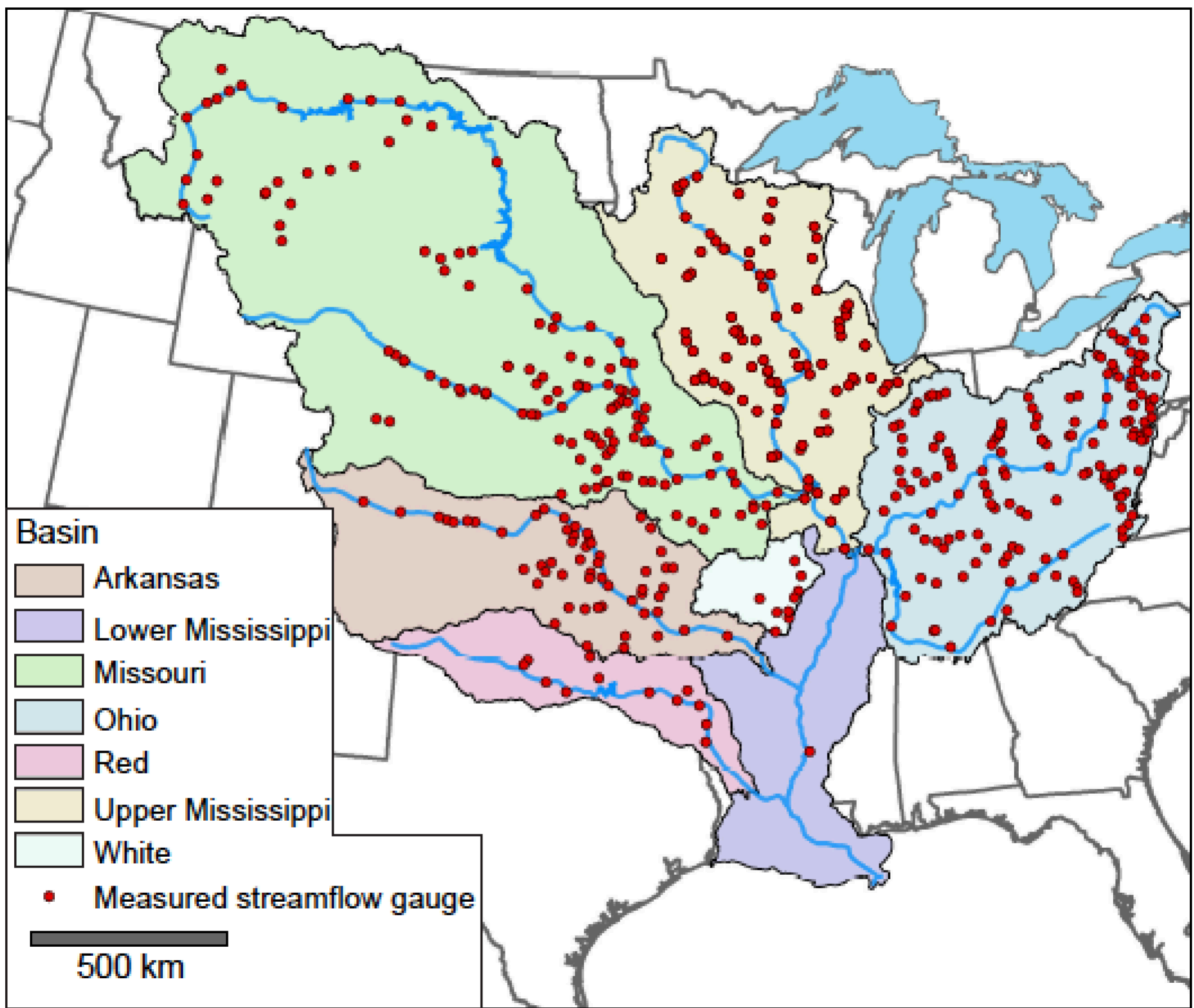
	Ohio	Upper Mississippi/ Lower main stem	Missouri	Total
Regression	y=1.00x-0.59	y=0.98x+1.8	y=0.95x+2.0	y=0.98x+0.8
Spearman's ρ	0.99	0.99	0.99	0.99

6

7 Table 4. Mean absolute depth errors (%)

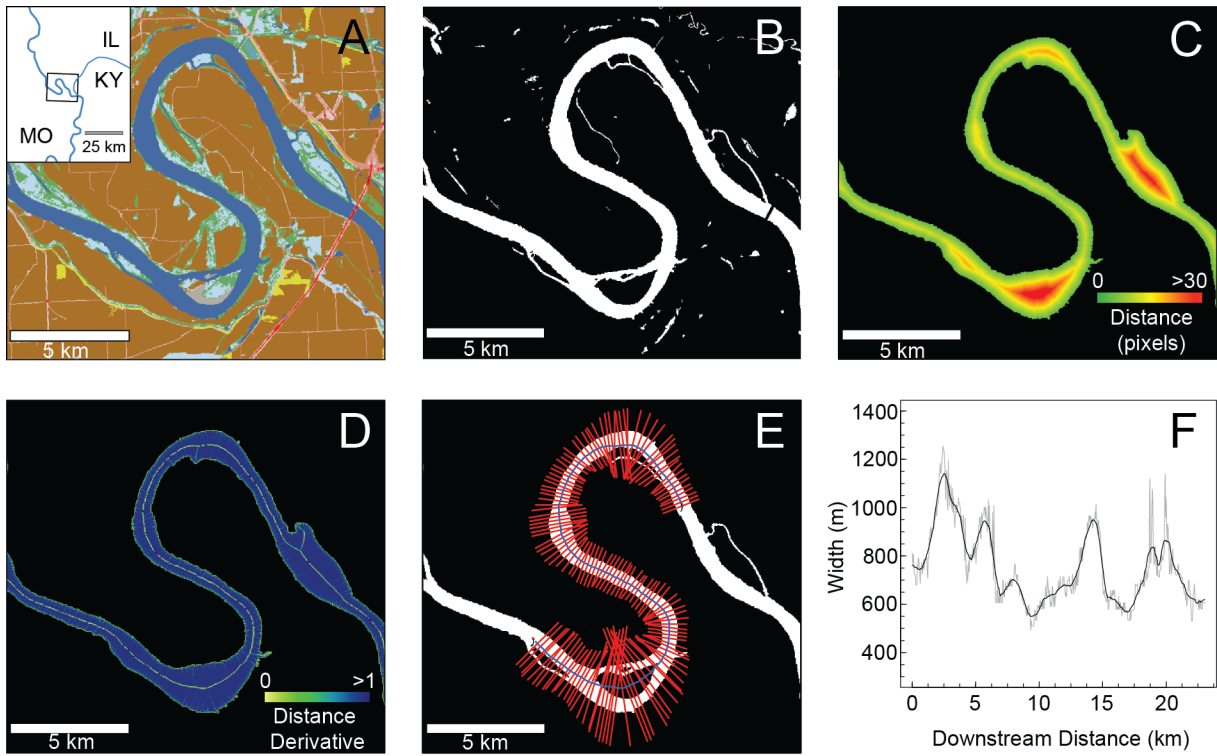
Sub-basin	Depth Only	Depth and Width	Moody-Troutman
Ohio	34%	35%	37%
Upper Mississippi	40%	33%	35%
Missouri	55%	33%	53%
<i>Total</i>	<i>43%</i>	<i>34%</i>	<i>42%</i>

1 **Figures and Captions**



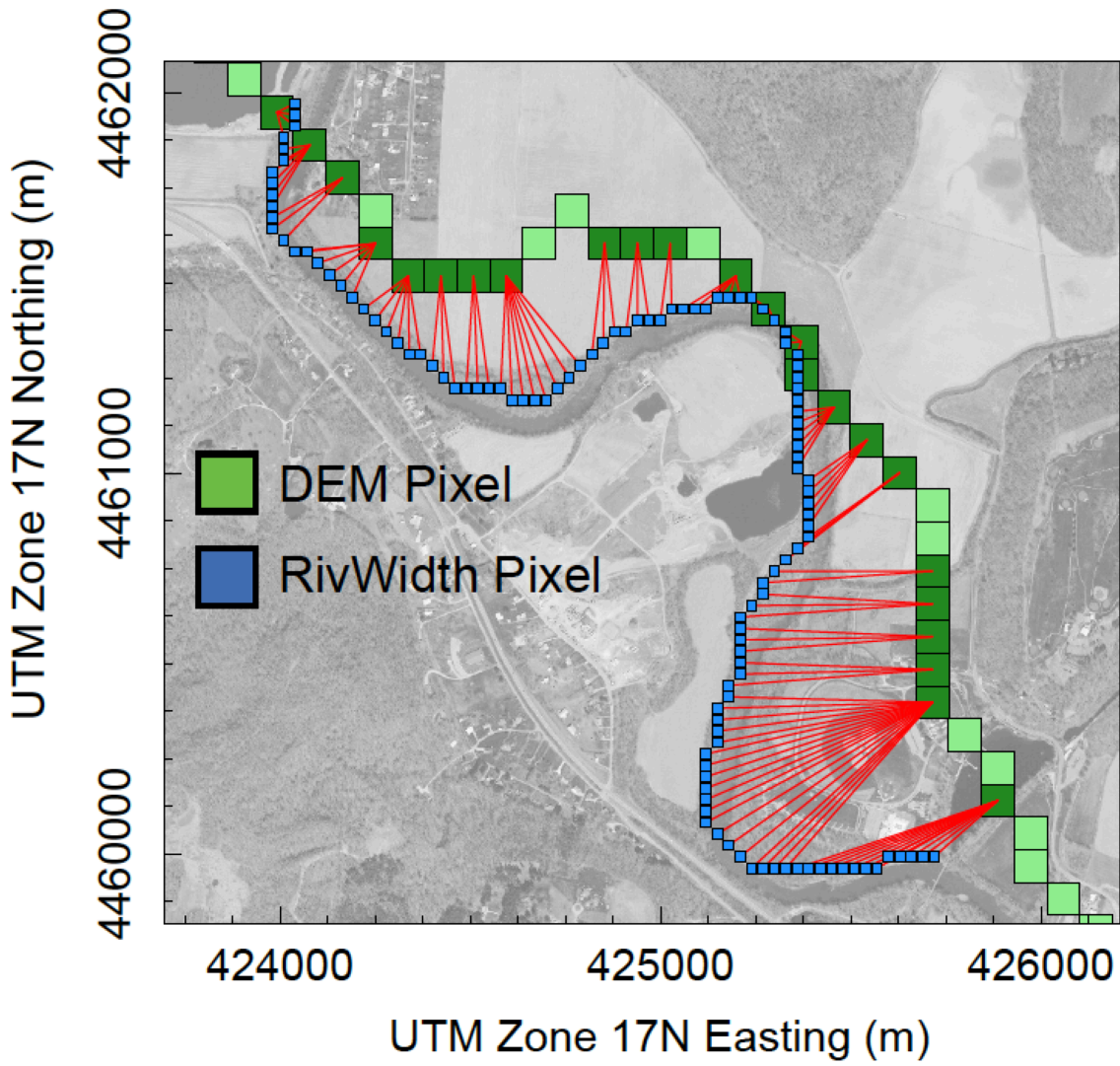
2

3 Figure 1. Major sub-basins of the Mississippi and USGS gauging stations used for width validation

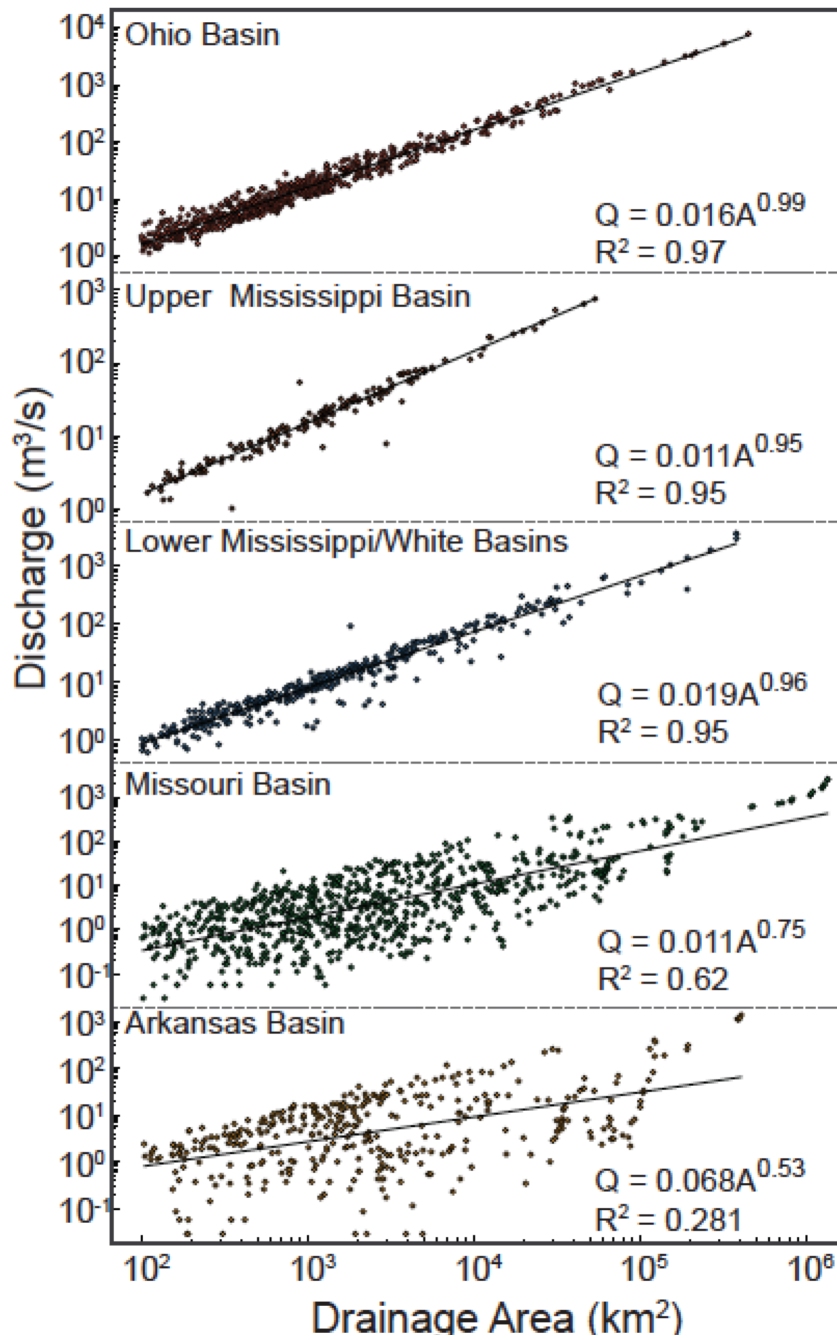


1
 2 Figure 2. Inputs, intermediate steps, and products for calculation of river width in this study: A) National
 3 Land Cover Dataset; B) binary water mask of the open water classification; C) distance image based on a filled
 4 channel mask; D) derivative of distance image used to calculate the centerline; E) flow width measurements
 5 along orthogonal line segments to each centerline pixel; F) plot of raw (grey) and smoothed (black) continuous
 6 widths.

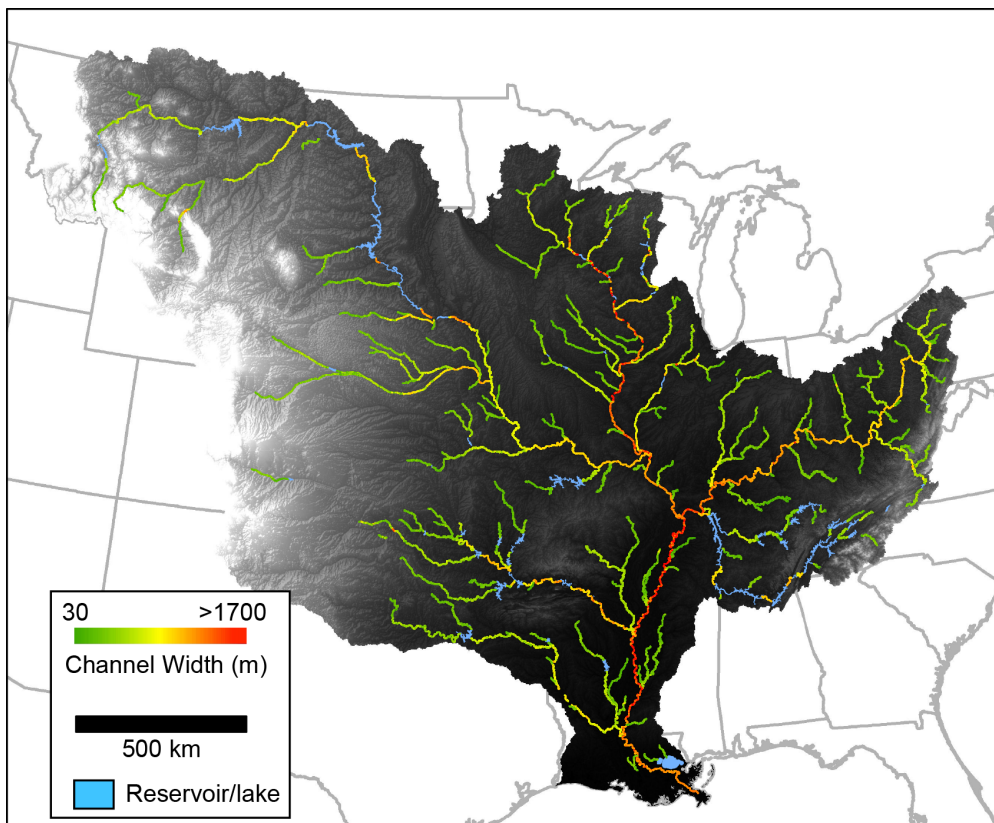
7



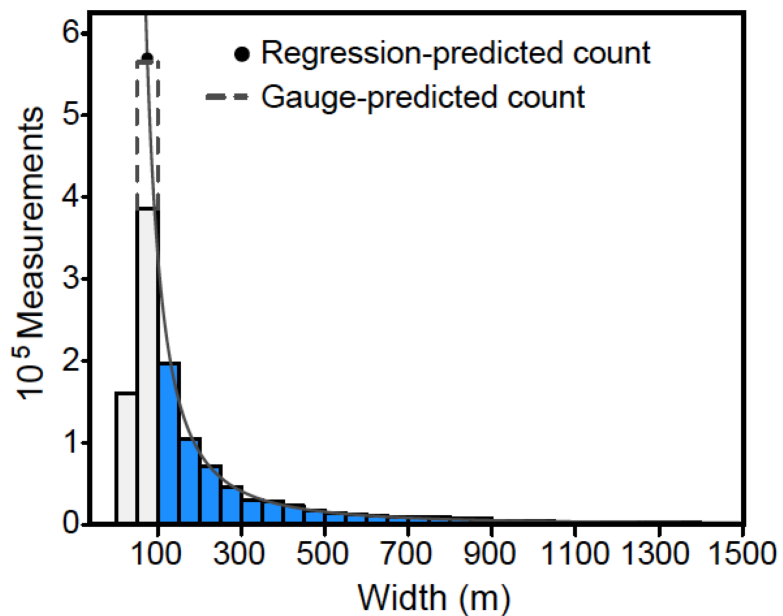
1
 2 Figure 3. Linking RivWidth and DEM measurements: RivWidth measurements for the Wallhonding River near
 3 Coshcocton, PA, matched to the nearest downstream DEM-derived channel pixels with drainage area values.



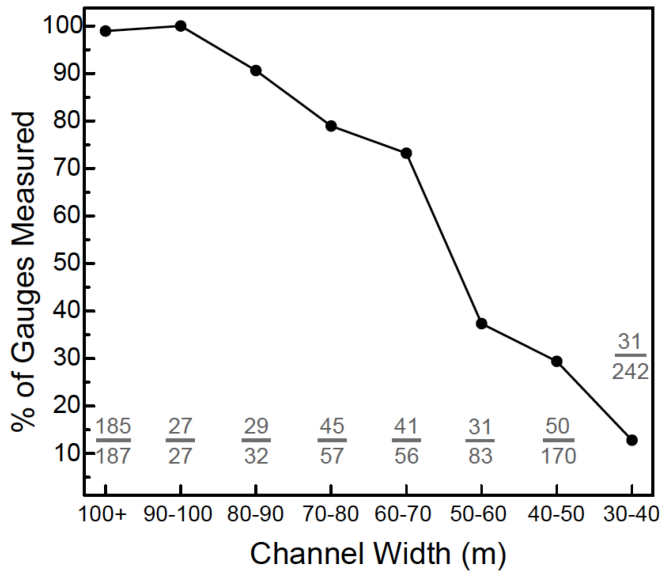
1
 2 Figure 4. Discharge-drainage area relationships for sub-basins of the Mississippi; exponents close to one indicate
 3 a nearly linear fit in the Ohio, Upper and Lower Mississippi sub-basins, but there is substantial deviation from
 4 unity in the Missouri and Arkansas sub-basins.



1
2 Figure 5. Mississippi River width map (shown with USGS HydroSHEDS DEM) of $\sim 1.2 \times 10^6$ observations at 30
3 m resolution based on the NLCD open water classification

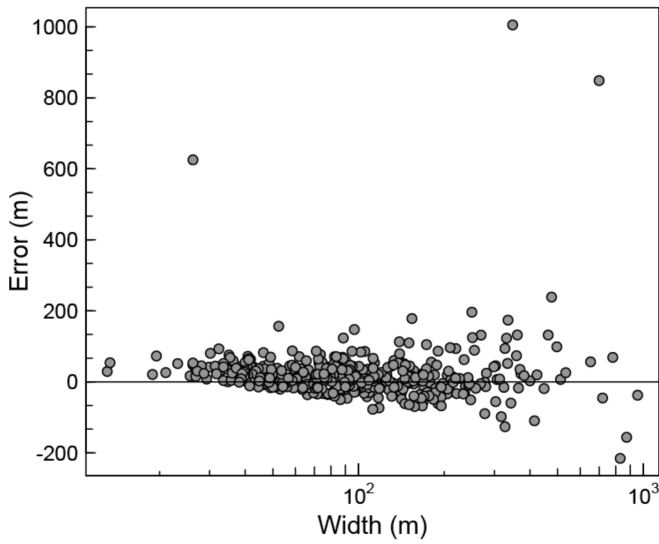


4
5 Figure 6. Width distributions for all rivers >100 m (blue bars) and many rivers < 100 m (grey bars); black circle
6 represents measurements predicted by the 100-1500 m distribution regression (n=570,000, black line); dashed
7 gray lines show estimated number of 50-100m rivers from the frequency distribution of USGS river gauges
8 (n=565,000).



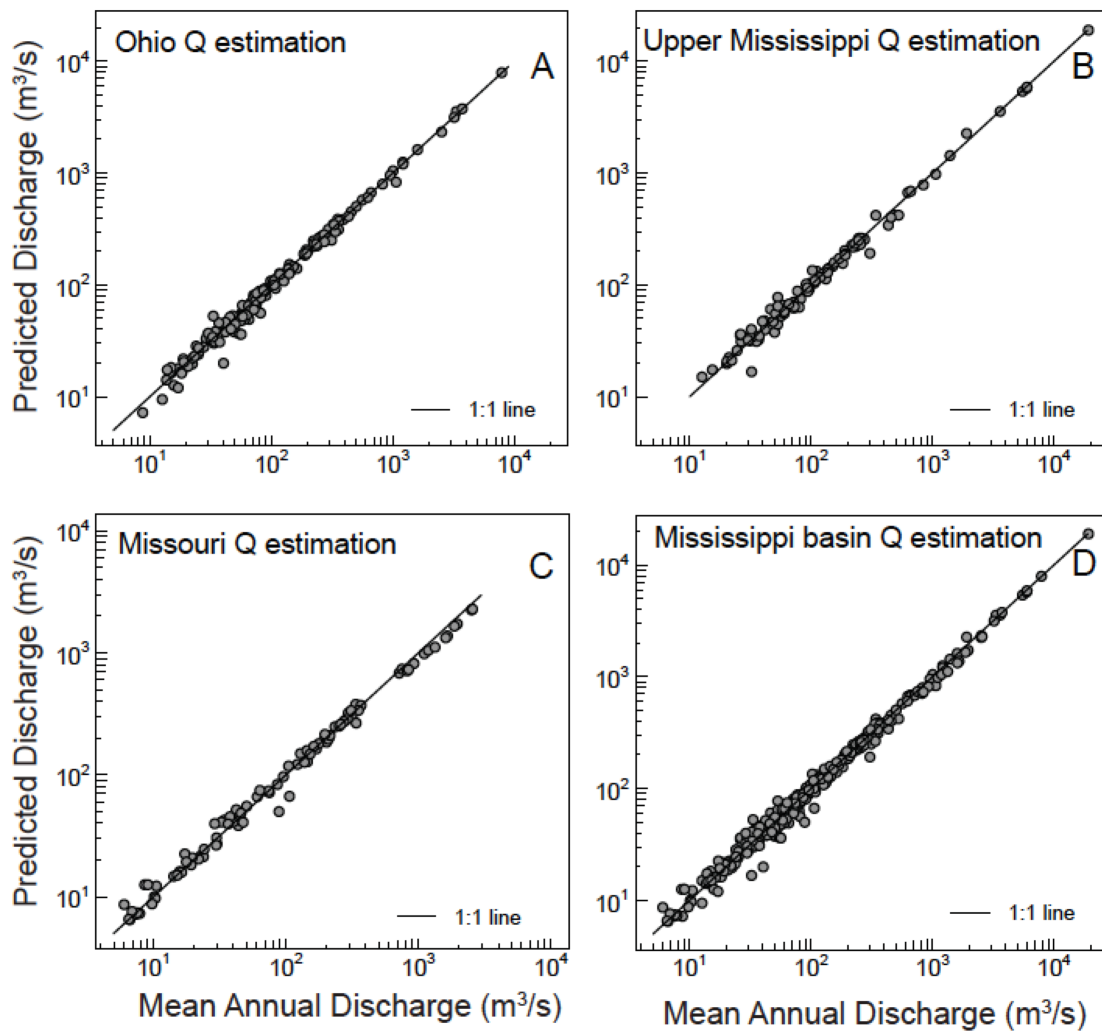
1

2 Figure 7. Percentage of USGS gauging stations measured in this study, binned by *in situ* channel width; grey
 3 fractions indicate number measured out of total gauges per 10-m width range.



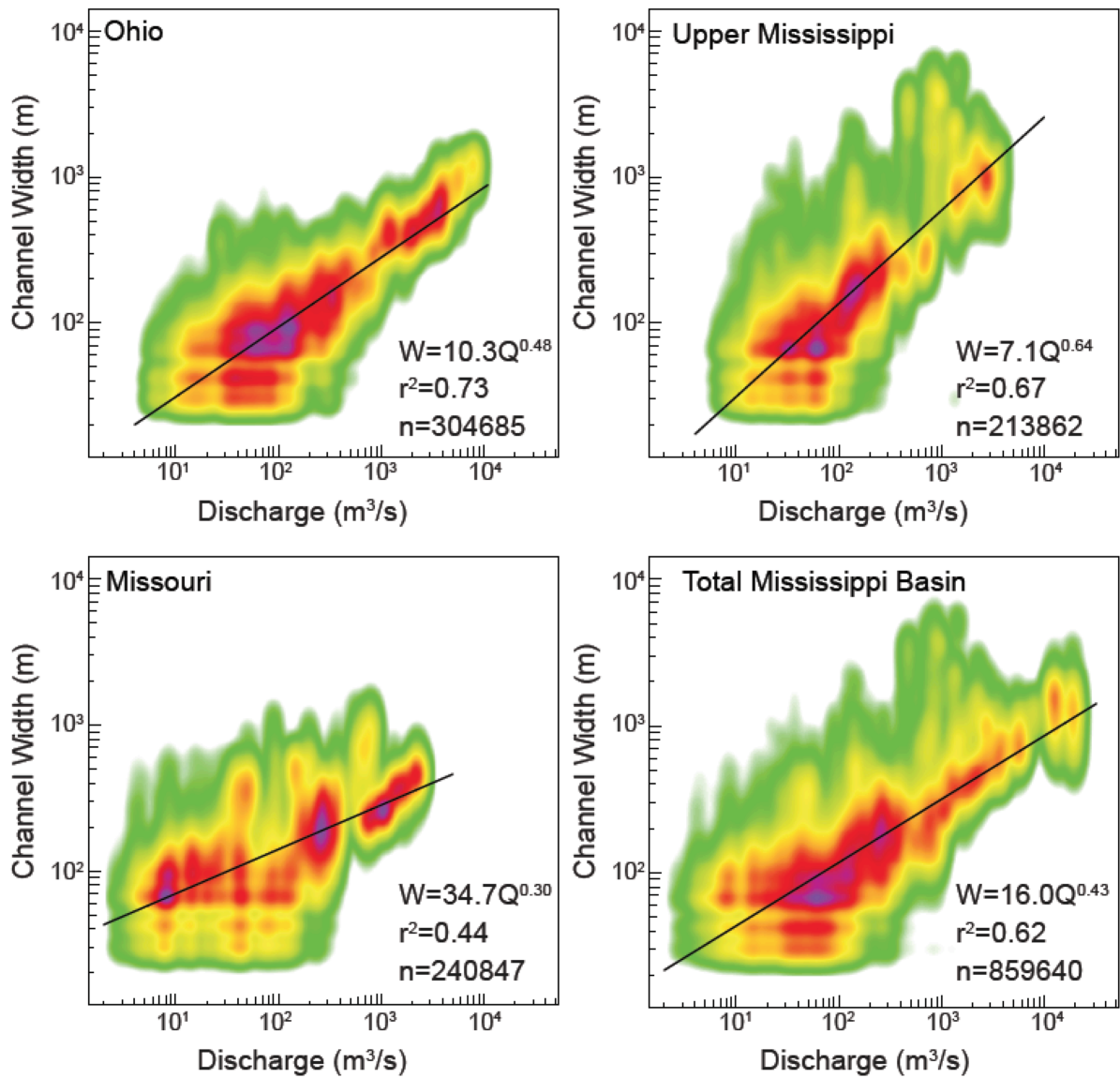
4

5 Figure 8. Width measurement error based on *in situ* channel measurements from 456 USGS streamflow gauging
 6 stations

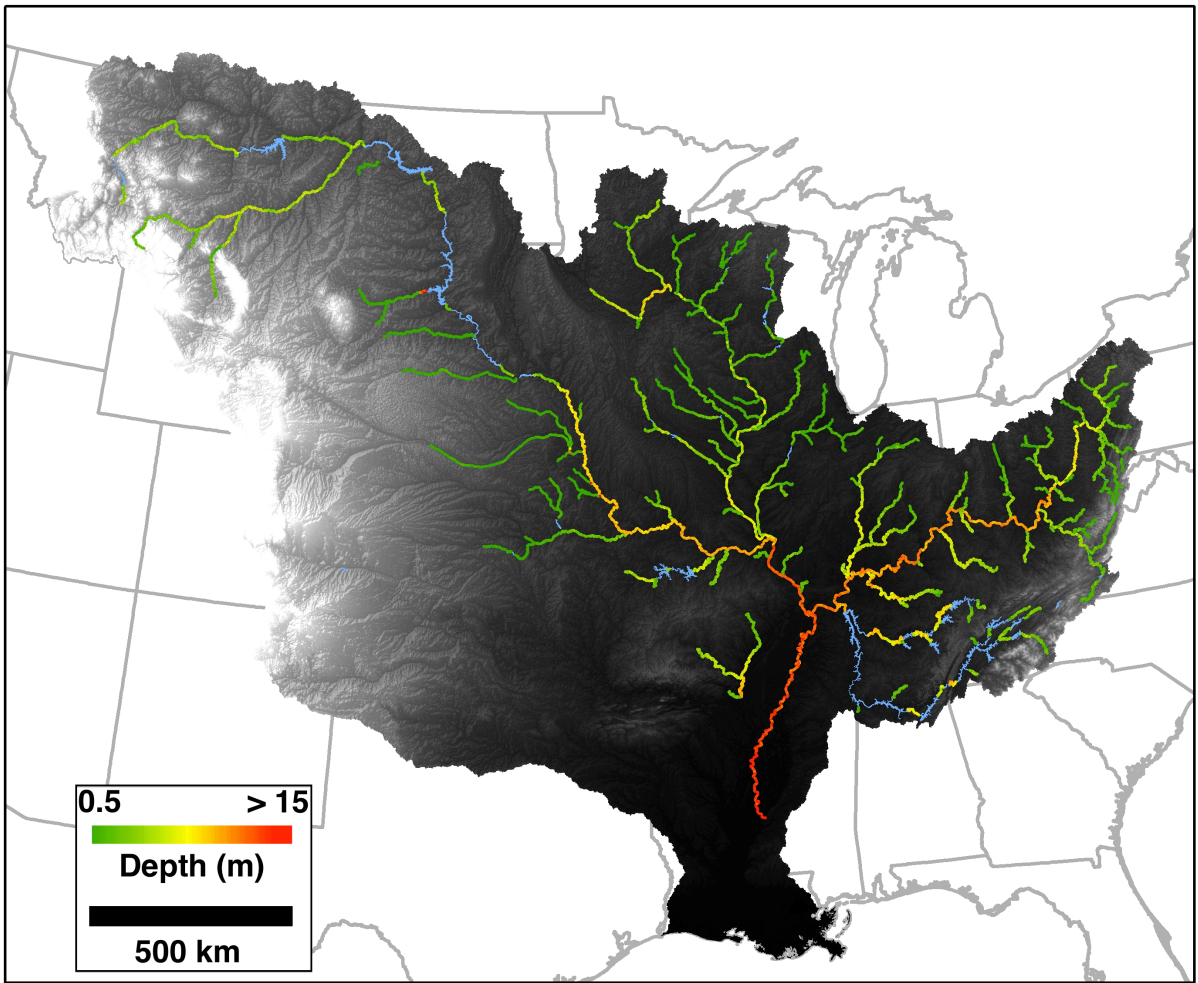


1

2 Figure 9. Estimated and USGS measured mean discharges for 346 gauging stations in the Mississippi basin.



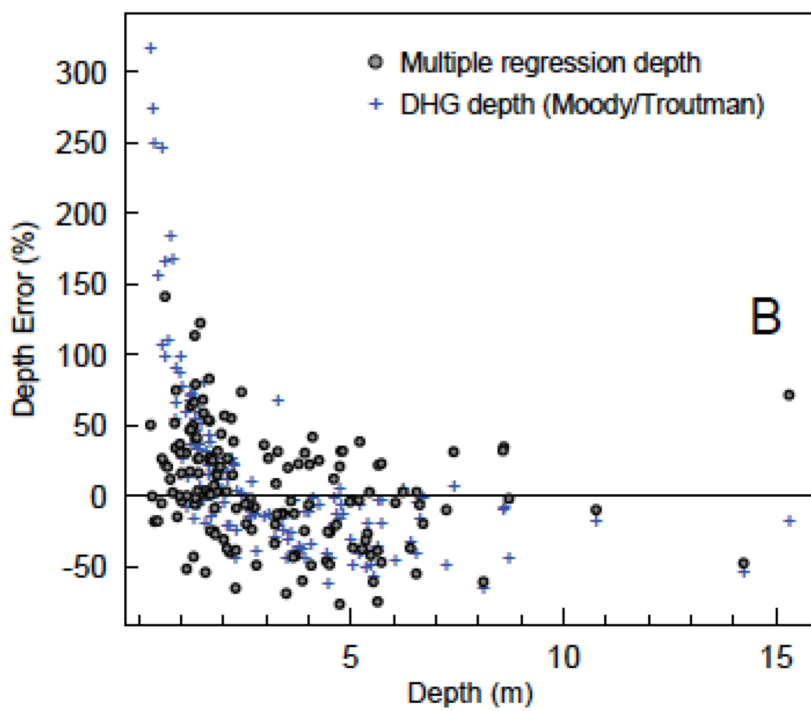
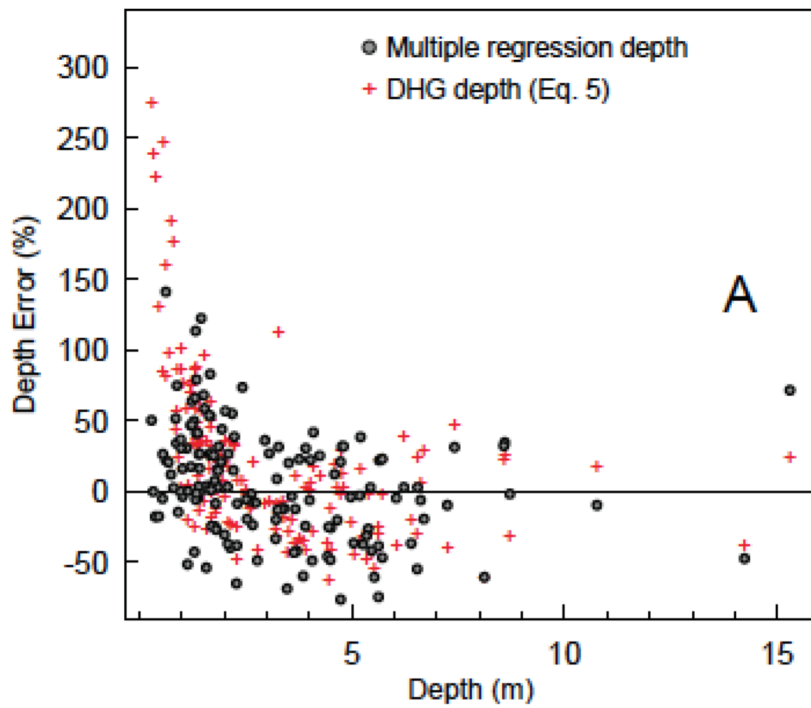
1
 2 Figure 10. Density plots of width versus discharge for the Ohio, Upper Mississippi, Missouri, and entire
 3 Mississippi basin. Linear fits represent downstream hydraulic geometry relationships analogous to Equation 1a.



1

2 Figure 11. 8×10^5 mean depths in the Mississippi basin estimated using multiple regression of d against Q and w ;

3 lakes shown in blue



1
 2 Figure 12. Relative depth error for multiple regression method (circles) and A) DHG estimate (this study); B)
 3 DHG estimate (Moody and Troutman, 2002)

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