

Large scale 3D-modeling by integration of resistivity models and borehole data through inversion

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ABSTRACT

We present an automatic method for parameterization of a 3D model of the subsurface, integrating lithological information from boreholes with resistivity models through an inverse optimization, with the objective of further detailing of geological models or as direct input to groundwater models. The parameter of interest is the clay fraction, expressed as the relative length of clay-units in a depth interval. The clay fraction is obtained from lithological logs and the clay fraction from the resistivity is obtained by establishing a simple petrophysical relationship, a translator function, between resistivity and the clay fraction. Through inversion we use the lithological data and the resistivity data to determine the optimum spatially distributed translator function. Applying the translator function we get a 3D clay fraction model, which holds information from the resistivity dataset and the borehole dataset in one variable. Finally, we use k-means clustering to generate a 3D model of the subsurface structures. We apply the procedure to the Norsminde survey in Denmark integrating approximately 700 boreholes and more than 100,000 resistivity models from an airborne survey in the parameterization of the 3D model covering 156 km². The final five-cluster 3D model differentiates between clay materials and different high resistive materials from information held in the resistivity model and borehole observations respectively.

25 **1 INTRODUCTION**

26 In a large-scale geological and hydrogeological modeling context, borehole data seldom provide an
27 adequate data base due to low spatial density in relation to the complexity of the subsurface to be mapped.
28 Contrary, dense areal coverage can be obtained from geophysical measurements, and particularly airborne
29 EM methods are suitable for 3D mapping, as they cover large areas in a short period of time. However,
30 the geological and hydrogeological parameters are only mapped indirectly, and an interpretation of the
31 airborne results is needed, often based on site-specific relationships. Linking electrical resistivity to
32 hydrological properties is thus an area of increased interest as reviewed by Slater (2007).

33 Integrating geophysical models and borehole information has proved to be a powerful combination for 3D
34 geological mapping (Jørgensen et al., 2012; Sandersen et al., 2009) and several modeling approaches
35 have been reported. One way of building 3D-models is through a knowledge-driven (cognitive), manual
36 approach (Jørgensen et al., 2013a). This can be carried out by making layer-cake models composed of
37 stacked layers or by making models composed of structured or unstructured 3D meshes where each voxel
38 is assigned a geological/hydrogeological property. The latter allows for a higher degree of model
39 complexity to be incorporated (Turner, 2006; Jørgensen et al., 2013a). The cognitive approach enables
40 various types of background knowledge such as the sedimentary processes, sequence stratigraphy, etc. to
41 be utilized. However, the cognitive modeling approach is difficult to document and to reproduce due to its
42 subjective nature. Moreover, any cognitive approach will be quite time-consuming, especially when
43 incorporating large airborne electromagnetic (AEM) surveys, easily exceeding 100,000 resistivity models.

44 Geostatistical modeling approaches such as multiple-point geostatistical methods (Daly and Caers, 2010;
45 Strebelle, 2002), transition probability indicator simulation (Carle and Fogg, 1996) or sequential indicator
46 simulation (Deutsch and Journel, 1998), provide models with a higher degree of objectivity in shorter
47 time compared to the cognitive, manual modeling approaches. An example of combining AEM and
48 borehole information in a transition probability indicator simulation approach is given by He et al. (2014).
49 Geostatistical modeling approaches based primarily on borehole data often face the problem that the data
50 are too sparse to represent the lateral heterogeneity at the desired spatial scale. Including geophysical data
51 enables a more accurate estimation of the geostatistical properties especially laterally. This could be
52 determination of the transition probabilities and the mean lengths of the different units. Though, the
53 geophysical data also opens the question of to what degree the different data types should be honored in
54 the model simulations and estimations. Combined use of geostatistical and cognitive approaches can be a
55 suitable solution in some cases (Jørgensen et al., 2013b; Raiber et al., 2012; Stafleu et al., 2011).
56 Integration of borehole information and geological knowledge as prior information directly in the
57 inversion of the geophysical data is another technique to combine the two types of information and

58 thereby achieve better geophysical models and subsequently better geological and hydrological models
59 (Høyer et al., 2014; Wisén et al., 2005).

60 Geological models are commonly used as the basis for hydrostratigraphical input to groundwater models.
61 However, even though groundwater model predictions are sensitive to variations in the hydrostratigraphy,
62 the groundwater model calibration is non-unique, and different hydrostratigraphic models may produce
63 similar results (Seifert et al., 2012).

64 Sequential, joint and coupled hydrogeophysical inversion techniques (Hinnell et al., 2010) have been used
65 to inform groundwater models with both geophysical and traditional hydrogeological observations. Such
66 techniques use petrophysical relationships to translate between geophysical and hydrogeological
67 parameter spaces. For applications in groundwater modeling using electromagnetic data see e.g Dam and
68 Christensen (2003) and Herckenrath et al. (2013). Also clustering analyses can be used to delineate
69 subsurface hydrogeological properties. Fuzzy c-means clustering has been used to delineate geological
70 features from measured EM34 signals with varying penetration depths (Triantafilis and Buchanan, 2009)
71 and to delineate the porosity field from tomography inverted radar attenuation and velocities and seismic
72 velocities (Paasche et al., 2006).

73 We present an automatic procedure for parameterization of a 3D model of the subsurface. The geological
74 parameter we map is the clay fraction (CF). In this paper we refer to *clay* as material described as clay in
75 a lithological well log regardless the type of clay; *clay till*, *mica clay*, *Palaeogene clay*, etc. This term is
76 robust in the sense that most geologists and drillers have a common conception on the description of *clay*
77 and it can easily be derived from the lithological logs. The clay fraction is then the cumulated thickness of
78 *clay* layers in a depth interval divided with the length of the depth interval. The CF-procedure integrates
79 lithological information from boreholes with resistivity information, typically from large-scale
80 geophysical AEM surveys. We obtain the CF from the resistivity data by establishing a petrophysical
81 relationship, a translator function, between resistivity and the CF. Through an inverse mathematical
82 formulation we use the lithological borehole data to determine the optimum parameters of the translator
83 function. Hence, the 3D CF-model holds information from the resistivity dataset and the borehole dataset
84 in one variable. As a last step we cluster our model space represented by the CF-model and geophysical
85 resistivity model using k-means clustering to form a structural 3D cluster model with the objective of
86 further detailing for geological models or as direct input to groundwater models.

87 Lithological interpretation of a resistivity model is not trivial since the resistivity of a geological media is
88 controlled by: porosity, pore water conductivity, degree of saturation, amount of clay minerals, etc.
89 Different, primarily empirical, models try to explain the different phenomena, where Archie's law
90 (Archie, 1942) is the most fundamental empirical model taking the porosity, pore water conductivity and,

91 the degree of saturation into account, but does not account for electrical conduction of currents taking
92 place on the surface of the clay minerals. The Waxman and Smits model (Waxman and Smits, 1968)
93 together with the Dual Water model of Clavier et al. (1984) provides a fundamental basis for widely and
94 repeatedly used empirical rules for shaly sands and material containing clay (e.g. Bussian, 1983; Sen,
95 1987; Revil and Glover, 1998). However, in a sedimentary depositional environment it can be assumed
96 in general that clay or clay rich sediments will exhibit lower resistivities than the non-clay sediments, silt,
97 sand, gravel, and chalk. As such, discrimination between clay and non-clay sediments based on resistivity
98 models is feasible and the CF-value is a suitable parameter to work with in the integration of resistivity
99 models and lithological logs. A 3D CF-model or clay/sand model will also contain key structural
100 information for a groundwater model, since it delineates the impermeable clay units and the permeable
101 sand/gravel units.

102 With the CF- procedure we use a two-parameter resistivity to CF translator function, which relies on the
103 lithological logs providing the local information for the optimum resistivity to CF translation. Hence, we
104 avoid describing the physical relationships underlying the resistivity images explicitly.

105 First, we give an overall introduction to the CF- procedure, and then we move to a more detailed
106 description of the different parts: observed data and uncertainty, forward modeling, inversion and
107 minimization, and clustering. Last we demonstrate the method in a field example with resistivity data
108 from an airborne SkyTEM survey combined with quality-rated borehole information.

109 **2 METHODOLOGY**

110 Conceptually, our approach sets up a function that best describes the petrophysical relationship between
111 clay fraction and resistivity. Through inversion we determine the optimum parameters of this translator
112 function, by minimizing the difference between the clay fraction calculated from the resistivity models
113 (Ψ_{res}) and the observed clay fraction in the lithological well logs (Ψ_{log}).

114 A key aspect in the CF-procedure is that the translator function can change horizontally and vertically
115 adapting to the local conditions and borehole data. The calculation is carried out in a number of elevation
116 intervals (calculation intervals) to cover an entire 3D model space. Having obtained the optimum and
117 spatially distributed translator function we can transform the resistivity models to form a 3D clay fraction
118 model, incorporating the key information from both the resistivity models and the lithological logs into
119 one parameter. The CF-procedure is a further development to three dimensions of the accumulated clay
120 thickness procedure by Christiansen et al., 2014, which is formulated in 2D.

121 The flowchart in Figure 1 provides an overview of the CF-procedure. The observed clay fraction (Ψ_{\log}) is
122 calculated from the lithological logs (box 1) in the calculation intervals. The translator function (box 2)
123 and the resistivity models (box 3) form the forward response, which produces a resistivity-based clay
124 fraction (box 4) in the different calculation intervals. The parameters of the translator function are
125 updated during the inversion to obtain the best consistency between Ψ_{res} and Ψ_{\log} . The output is the
126 optimum resistivity-to-clay fraction translator function (box 5), and when applying this to the resistivity
127 models (the forward response of the final iteration), we obtain the optimum Ψ_{res} and block kriging is used
128 to generate a regular 3D CF model (box 6).

129 The final step is a k-means clustering analysis (box 7). With the clustering we achieve a 3D model of the
130 subsurface delineating a predefined number of clusters that represent zones of similar physical properties,
131 which can be used as input in, for example, a detailed geological model or as structural delineation for a
132 groundwater model.

133 The subsequent paragraphs detail the description of the individual parts of the CF-procedure.

134 **2.1 Observed data - lithological logs and clay fraction**

135 The common parameter derived from the lithological logs and resistivity datasets is the clay fraction
136 (Figure 1, boxes 1-4). The *clay fraction*, of a given depth interval in a borehole (named Ψ_{\log}) is calculated
137 as the cumulative thickness of layers described as *clay* divided by the length of the interval. By using this
138 definition of clay and clay fraction we can easily calculate Ψ_{\log} in depth intervals for any lithological well
139 log as the example in Figure 2a shows. Having retrieved the Ψ_{\log} values we then need to estimate their
140 uncertainties since a variance estimate, σ_{\log}^2 is needed in the evaluation of the misfit to Ψ_{res} .

141 The drillings are conducted with a range of different methods. This has a large impact on the uncertainties
142 of the lithological well log data. The drilling methods span from core drilling resulting in a very good
143 base for the lithology classification, to direct circulation drillings (cuttings are flushed to the surface
144 between the drill rod and the formation) resulting in poorly determined layer boundaries and a very high
145 risk of getting the samples contaminated due to the travel time from the bottom to the surface. Other
146 parameters affecting the uncertainty of the Ψ_{\log} are sample intervals and sample density, accuracy of the
147 geographical positioning and elevation, and the credibility of the driller to mention a few important ones..

148 **2.2 Forward data – the translator function**

149 For calculating the clay fraction for a resistivity model, Ψ_{res} , we use the translator function as shown in
150 Figure 2b, which is defined by a m_{low} and a m_{up} parameter. With the CF-procedure we primarily want to
151 determine resistivity threshold values for a clay-sand interpretation of the resistivity models. Thin

152 geological layers are often not directly visible in the resistivity models, whereas they will most often
 153 appear in carefully described boreholes. The length of the calculation intervals reflects the resolution
 154 capability of the geophysical method of choice, which means that in some cases the calculation intervals
 155 contain both sand and clay layers when imposed on the lithological logs. The translator function must
 156 therefore be able to translate resistivity values as partly clay and partly sand to obtain consistency with the
 157 lithological logs. This is possible with the translator function in Figure 2b, where m_{low} and m_{up} represent
 158 the clay and sand cut-off values. So for resistivity values below m_{low} the layer is entirely clay (weight ≈ 1)
 159 and for resistivity values above m_{up} the layer is entirely sand or non-clay (weight ≈ 0).

160 Many functions fulfilling the above criteria could have been chosen, but we use the one shown because it
 161 is differentiable throughout while being flat at both ends and fully described by just two parameters. The
 162 translator function ($W(\rho)$) is mathematically a scaled complementary error function, defined as:

$$W(\rho) = 0.5 \cdot \operatorname{erfc}\left(\frac{K \cdot (2\rho - m_{up} - m_{low})}{(m_{up} - m_{low})}\right)$$

$$K = \operatorname{erfc}^{-1}(0.05)$$

163 (1)

164 where m_{low} and m_{up} are defined as the resistivity (ρ) at which the translator function, $W(\rho)$, returns a
 165 weight of 0.975 and 0.025 respectively (the K -value scales the erfc function accordingly). For a layered
 166 resistivity model the Ψ_{res} for a single resistivity model value in one calculation interval is then calculated
 167 as:

$$\Psi_{res} = \frac{1}{\sum t_i} \cdot \sum_{i=1}^N W(\rho_i) \cdot t_i$$

168 (2)

169 where N is the number of resistivity layers in the calculation interval, $W(\rho_i)$ is the clay weight for the
 170 resistivity in layer i , t_i is the thickness of the resistivity layer, and $\sum t_i$ is the length of the calculation
 171 interval. In other words, W weights the thickness a resistivity layer, so for a resistivity below m_{low} the
 172 layer thickness is counted as clay ($W \approx 1$) while for a resistivity above m_{up} the layer is counted as non-
 173 clay ($W \approx 0$). Figure 2a shows how a single resistivity model is translated into Ψ_{res} in numbers of
 174 calculation intervals.

175 The resistivity models are also associated with an uncertainty, and if the variance estimates of the
176 resistivities and thicknesses for the geophysical models are available we take these into account. The
177 propagation of the uncertainty from the resistivity models to the Ψ_{res} values is described in detail in
178 Christiansen et al. (2014).

179 To allow for variation, laterally and vertically, in the resistivity to Ψ_{res} translation, a regular 3D grid is
180 defined for the survey block (Figure 3). Each grid node holds one set of m_{up} and m_{low} parameters. The
181 vertical discretization follows the clay fraction calculation intervals, varying between 4-20 m increasing
182 with depth. The horizontal discretization is typically 0.5-2 km and a 2D bilinear horizontal interpolation
183 of the m_{up} and m_{low} is applied to define the translator function uniquely at the positions of the resistivity
184 models.

185 To migrate information of the translator function from regions with many boreholes to regions with few
186 or no boreholes, horizontal and vertical smoothness constraints are applied between the translator
187 functions at each node point as shown in Figure 3. Choosing appropriate constraints is based on the
188 balance between fitting the data while having a reasonable model. The balance is site and data specific,
189 but would typically be based on visual evaluations comparing the results against key boreholes. The
190 smoothness constraints furthermore act as regularization and stabilize the inversion scheme.

191 Finally, we need to estimate Ψ_{res} values at the Ψ_{log} positions (named Ψ_{res}^*) for evaluation. We estimate the
192 Ψ_{res}^* values by making a point kriging interpolation of the Ψ_{res} values and associated uncertainties within
193 a search radius of typically 500 m. The experimental semi-variogram is calculated from the Ψ_{res} values
194 for the given calculation interval and can normally be approximated well with an exponential function,
195 which then enters the kriging interpolation. The code Gstat (Pebesma and Wesseling, 1998) is used for
196 kriging, variogram calculation, and variogram fitting. Hence, for the output estimates of the Ψ_{res}^* both the
197 original variance of Ψ_{res} and the variance on the kriging interpolation itself is included to provide total
198 variance estimates of the Ψ_{res}^* values (σ_{res}^{2*}), which are needed for a meaningful evaluation of the data
199 misfit at the borehole positions.

200 **2.3 Inversion - objective function and minimization**

201 The inversion algorithm in its basic form consists of a nonlinear forward mapping of the model to the data
202 space:

$$\delta\Psi_{obs} = \mathbf{G}\delta\mathbf{m}_{true} + \mathbf{e}_{log}$$

203 (3)

204 where $\delta \Psi_{obs}$ denotes the difference between the observed data (Ψ_{log}) and the non-linear mapping of the
 205 model to the data space (Ψ_{res}). δm_{true} represents the difference between the model parameters (m_{up} , m_{low})
 206 of the true, but unknown, translator function and an arbitrary reference model (the initial starting model
 207 for the first iteration, then at later iterations the model from the previous iteration). e_{log} is the
 208 observational error, and G denotes the Jacobian matrix that contains the partial derivatives of the
 209 mapping. The general solution to the non-linear inversion problem of equation (3) is described by
 210 Christiansen et al. (2014) and is based on Auken and Christiansen (2004) and Auken et al. (2005).

211 The objective function, Q, to be minimized includes a data term, R_{dat} , and a regularization term from the
 212 horizontal and vertical constraints, R_{con} . R_{dat} is given as:

$$R_{dat} = \sqrt{\frac{1}{N_{dat}} \cdot \sum_{i=1}^{N_{dat}} \frac{(\Psi_{log,i} - \Psi_{res,i}^*)^2}{\sigma_i^2}}$$

213 (4)

214 where N_{dat} is the number of Ψ_{log} values and σ_i^2 is the combined variance of the i 'th Ψ_{log} (σ_{log}^2) and Ψ_{res}
 215 (σ_{res}^{2*}) given as:

$$\sigma_i^2 = \sigma_{log,i}^2 + \sigma_{res,i}^{2*}$$

216 (5)

217 The inversion is performed in logarithmic model space to prevent negative parameters, and R_{con} is
 218 therefore defined as:

$$R_{con} = \sqrt{\frac{1}{N_{con}} \cdot \sum_{i=1}^{N_{con}} \frac{(\ln(m_j) - \ln(m_k))^2}{(\ln(e_{r,i}))^2}}$$

219 (6)

220 Where e_r is the regularizing constraint between the two constrained parameters m_j and m_k of the translator
 221 function and N_{con} is the number constraint pairs. The e_r values in equation (6) are stated as constraint
 222 factors, meaning that an e_r factor of 1.2 corresponds approximately to a model change of +/- 20%.

223 In total the objective function Q becomes:

224

$$Q = \sqrt{\frac{N_{\text{dat}} \cdot R_{\text{dat}}^2 + N_{\text{con}} \cdot R_{\text{con}}^2}{(N_{\text{dat}} + N_{\text{con}})}}$$

225 (7)

226 Furthermore, is it possible to add prior information as a prior constraint on the parameters of the translator
227 function, which just adds a third component to Q in equation (7) similar to R_{con} in equation (6).

228 The minimization of the non-linear problem is performed in a least squares sense by using an iterative
229 Gauss-Newton minimization scheme with a Marquardt modification. The full set of inversion equations
230 and solutions are presented in Christiansen et al. (2014).

231 **2.4 Cluster analysis**

232 The delineation of the 3D model is obtained through a k-means clustering analysis, which distinguishes
233 groups of common properties within multivariate data. We have based the clustering analysis on the CF-
234 model and the resistivity model. Other data, which are informative for structural delineation of geological
235 or hydrological properties, can also be included in the cluster analysis. For example this could be
236 geological a priori information or groundwater quality data. The resistivity model is part of the CF-model,
237 but is reused for the clustering analysis because the representation of lithology used in the CF-model
238 inversion has simplified the geological heterogeneity captured in the resistivity model.

239 K-means clustering is a hard clustering algorithm used to group multivariate data. A k-means cluster
240 analysis is iterative optimization with the objective of minimizing a distance function between data points
241 and a predefined number of clusters (Wu, 2012). We have used Euclidean length as a measure of
242 distance. We use the k-means algorithm in MATLAB R2013a, which has implemented a two-phase
243 search, batch and sequential, to minimize the risk of reaching a local minimum (Wu, 2012). K-means
244 clustering can be performed on several variables, but for variables to impact the clustering equally, data
245 must be standardized and uncorrelated. The CF-model and resistivity model are by definition correlated.
246 We use Principal Component Analysis (PCA) to obtain uncorrelated variables.

247 Principal component analysis is a statistical analysis based on data variance formulated by Hotelling
248 (1933). The aim of a PCA is to find linear combinations of original data while obtaining maximum
249 variance of the linear combinations (Härdle and Simar, 2012). This results in an orthogonal
250 transformation of the original multi-dimensional variables into a space where dimension one has largest
251 variance, dimension two has second largest variance, etc. In this case the PCA is not used to reduce
252 variable space, but only to obtain an orthogonal representation of the original variable space to use in the
253 clustering analysis. Principal components are orthogonal and thus uncorrelated, which makes the

254 principal components useful in the subsequent clustering analysis. The PCA is scale sensitive and the
255 original variables must therefore be standardized prior to the analysis. Because the principal components
256 have no physical meaning, a weighting of the CF-model and the resistivity model cannot be included in
257 the k-means clustering. Instead the variables are weighed prior to the PCA.

258 **3 NORSMINDE CASE**

259 The Norsminde case model area is located in eastern Jutland, Denmark (Figure 4) around the town of
260 Odder (Figure 5) and covers 156 km², representing the Norsminde Fjord catchment. The catchment area
261 has been mapped and studied intensely in the NiCA research project in connection with nitrate reduction
262 in geologically heterogeneous catchments (Refsgaard et al., 2014). The modeling area has a high degree
263 of geological complexity in the upper part of the section. The area is characterized by Palaeogene and
264 Neogene sediments covered by glacial Pleistocene deposits. The Palaeogene is composed of fine-grained
265 marl and clay and the Neogene layers consist of marine Miocene clay interbedded with deltaic sand layers
266 (Rasmussen et al., 2010). The Neogene is not present in the southern and eastern part of the area where
267 the glacial sediments therefore directly overlie the Palaeogene clay. The Palaeogene and Neogene layers
268 in the region are frequently incised by Pleistocene buried tunnel valleys and one of these is present in the
269 southern part, where it crosses the model area to great depths with an overall E-W orientation (Jørgensen
270 and Sandersen, 2006). The Pleistocene deposits generally appear very heterogeneous and according to
271 boreholes they are composed of glacial meltwater sediments and till.

272 **3.1 Borehole data**

273 In Denmark, the borehole data are stored in the national database Jupiter (Møller et al., 2009) dating back
274 to 1926 as an archive for all data and information obtained by drilling. Today, the Jupiter database holds
275 information about more than 240,000 boreholes. All borehole layers in the database are assigned a
276 lithology code, which makes it easy to extract the different types of clay layers for the calculation of the
277 Ψ_{\log} values in the different calculation intervals.

278 For the model area, approximately 700 boreholes are stored in the database. Based on borehole meta-data
279 found in the database we use an automatic quality rating system, where each borehole is rated from 1-4
280 (He et al., 2014). The ratings are used to assign different uncertainty (weights) to the lithological logs/the
281 Ψ_{\log} values in the CF-procedure.

282 The meta-data used for the quality-rating are:

- 283 • Drill method: auger, direct circulation, air-lift drilling, etc.

- 284 • Vertical sample density
- 285 • Accuracy of the geographical position: GPS or manual map location
- 286 • Accuracy of the elevation: Differential GPS or other
- 287 • Drilling purpose: scientific, water abstraction, geophysical shot holes, etc.
- 288 • Credibility of drilling contractor

289 The boreholes are assigned points in the different categories and finally grouped into four quality groups
290 according to their total score. Boreholes in the lowest quality group (4) are primarily boreholes with low
291 sample frequencies (less than 1 sample per 10 m), low accuracy in geographical position, and/or drilled
292 as geophysical shot holes for seismic exploration.

293 The locations, quality ratings and drill depths of the boreholes are shown in Figure 5b. The drill depths
294 and quality ratings are summarized in Figure 6. As the top bar in Figure 6 shows that 4% of the boreholes
295 are categorized as quality 1, 46% as quality 2, 32% as quality 3, and 18% as quality 4. The uncertainties
296 of the Ψ_{\log} values for the quality groups 1-4 are based on a subjective evaluation and are defined as 10%,
297 20%, 30%, and 50%, respectively. The number of boreholes drastically decreases with depth as shown in
298 Figure 6. Thus, while about 100 boreholes are present in a depth of 60 m, only 25 boreholes reach a depth
299 greater than 90 m.

300 **3.2 EM data**

301 The major part of the model area is covered by SkyTEM data and adjoining ground based TEM
302 soundings are included in the resistivity dataset (Figure 5a).

303 The SkyTEM data were collected with the newly developed SkyTEM¹⁰¹ system (Schamper et al., 2014b).
304 The SkyTEM¹⁰¹ system has the ability to measure very early times, which improves the resolution of the
305 near surface geological layers, when careful system calibration and advanced processing and inversion
306 methodologies are applied (Schamper et al., 2014a). The recorded times span the interval from ~3 μ s to 1-
307 2 ms after end of the turn-off ramp, which gives a depth of investigation (Christiansen and Auken, 2012)
308 of approximately 100 m for an average ground resistivity of 50 Ω m. The SkyTEM survey was performed
309 with a dense line spacing of 50 m for the western part and 100 m line spacing for eastern part (Figure 5a).
310 Additional cross lines were made in a smaller area, which brings the total up to approximately 2000 line
311 km. The sounding spacing along the lines is approximately 15 m resulting in a total of 106,770 1D
312 resistivity models. The inversion was carried out in a spatially constrained inversion setup (Viezzoli et al.,
313 2008) with a smooth 1D-model formulation (29 layers, with fixed layer boundaries), using the AarhusInv
314 inversion code (Auken et al., 2014) and the Aarhus Workbench software package (Auken et al., 2009) .

315 The resistivity models have been terminated individually at their estimated depth of investigation (DOI)
316 calculated as described by Christiansen and Auken (2012).

317 The ground based TEM soundings originate from mapping campaigns in the mid-1990s. The TEM
318 soundings were all acquired with the Geonics TEM47/PROTEM system (Geonics Limited) in a central
319 loop configuration with a 40 by 40 m² transmitter loop. 1D layered resistivity models with 3 to 5 layers
320 were used in the interpretation of the TEM sounding data.

321 **3.3 Model setup**

322 The 3D translator function grid has a horizontal discretization of 1 km, with 16 nodes in the x-direction
323 and 18 nodes in the y-direction. Vertically the model spans from 100 m above sea level (asl) (highest
324 surface elevation) to 120 m below sea level (bsl). The vertical discretization is 4 m for layers asl and 8
325 m for layers bsl, which results in 40 calculation intervals. Hence, in total, the model grid holds
326 $16 \times 18 \times 40 = 11,520$ translator functions each holding two parameters. Translator functions in the 3D grid
327 situated above terrain, below DOI of the resistivity models, and outside geophysical coverage does not
328 contribute at all, and are only included to make the translator function grid regular for easier
329 computation/bookkeeping. The effective number of translator functions, is therefore close to 5,200.

330 The regularization constraints between neighboring translator functions nodes are set relatively loose to
331 promote a predominantly data driven inversion problem. In this case we use horizontal constraint factors
332 of 2 and vertical constraint factors of 3. This roughly allows the two parameters of the translator function
333 to vary with a factor of 2 (horizontal) and a factor of 3 (vertical) relative to adjacent translator function
334 parameters. The resulting variations in the translator model grid are a trade-off between data, data
335 uncertainties and the constraints (equation (7)). A spatially uniform initial translator function was used
336 with $m_{\text{low}} = 35 \Omega\text{m}$ and $m_{\text{up}} = 55 \Omega\text{m}$.

337 To create the final regular 3D CF-model the Ψ_{res} values from the geophysical models, the Ψ_{log} values
338 from the boreholes, and associated variances are used in a 2D-kriging interpolation for each calculation
339 interval. The 2D-grids are then stacked to form the 3D-CF-model. The Ψ_{log} values are primarily used to
340 close gaps in the resistivity dataset where boreholes are present, as seen for the large central hole in the
341 resistivity survey (Figure 8b), which is partly closed in the CF-model domain (Figure 8d) by borehole
342 information. In order to match the computational grid setup of a subsequent groundwater model, a
343 horizontal discretization of 100 m is used for the 3D-CF-model grid. In this case the dense EM-airborne
344 survey data could actually support a finer horizontal discretization (25-50 m) in the CF-model.

345 The k-means clustering is performed on two variables, the CT-model and resistivity model, in a 3D grid
346 with regular horizontal discretization of 100 m and vertical discretization of 4 m between 96 and 0 m asl

347 and 8 m between 0 and 120 m bsl. CF-model values range between 0 and 1 and have therefore not been
348 standardized. The resistivity values have been log transformed and standardized by first subtracting the
349 mean and then dividing by four times the standard deviation. The standardization of the resistivity was
350 performed in this way to balance the weight between the two variables in the clustering. A five cluster
351 delineation is presented for the Norsminde case in the result section.

352 **3.4 Results**

353 CF-modeling results from the Norsminde area are presented in cross sections in Figure 7 and as
354 horizontal slices in Figure 8. The total misfit of equation (7) is 0.37, but probably more interesting the
355 isolated data fit (equation (3)) is 1.26 meaning that we fit the data almost to the level of the assigned
356 noise. Figure 7a and b show the inversion results of the m_{low} and m_{up} parameters in section view. The
357 vertical variation in the translator is pronounced in the resistivity transition zones, because sharp layer
358 boundaries have a smoother representation in the resistivity domain.

359 For the deeper part of the model (deeper than 10 m bsl) the translator functions are less varying. This
360 corresponds well to the general geological setting of the area with relatively homogenous clay sequences
361 in the deeper part, but it is also a result of very limited borehole information for the deeper model parts.
362 The general geological setting of the area is also clearly reflected in the translator function in the
363 horizontal slices in Figure 8a and b. The eastern part of the area with lowest m_{low} values (dark blue in
364 Figure 8a) and lowest m_{up} values (light blue/green in Figure 8b) corresponds to the area where the
365 Palaeogene highly conductive clays are present. In the western part of the area the cross section intersects
366 the glacial complex, where the clays are mostly tills, and higher m_{low} and m_{up} values are needed to get the
367 optimum translation.

368 The resistivity cross section in Figure 7c and the slice section in Figure 8c reveal a detailed picture of the
369 effect of the geological structures seen in the resistivity data. Generally, a good correlation with the
370 boreholes is observed. Translating the resistivities we obtain the CF-model presented in Figure 7d and
371 Figure 8d. The majority of the voxels in the CF-model have values close to 0 or 1. This is expected since
372 the lithological logs are described binary clay/non clay, and Ψ_{log} values not equal to 0 or 1 can only occur
373 if both clay and non-clay lithologies are present in the same calculation interval in a particular borehole.

374 Evaluating the result in Figure 7d and Figure 8d, it is obvious that the very resistive zones are translated
375 to a CF-value close to 0 and the very conductive zones are translated to CF-value close to 1. Focusing on
376 the intermediate resistivities (20-60 Ω m) it is clear that the translation of resistivity to CF is not one-to-
377 one. For example, the buried valley structure (profile coordinate 6500-8500m, Figure 7d) has mostly
378 high-resistive fill with some intermediate resistivity zones. In the CF-section these intermediate resistivity

379 zones are translated to zones of high clay content, consistent with the lithological log at profile coordinate
380 7,000 m that contains a 25 m thick clay layer. The CF-section sharpens the layer boundaries compared to
381 the smooth layer transitions in the resistivity section. The integration of the resistivity data and
382 lithological logs in the CF-procedure results in a high degree of consistency between the CF-results and
383 the lithological logs, as seen in the CF-section in Figure 7d.

384 Horizontal slices of the 3D cluster model are shown in Figure 9. The near-surface part of the model
385 (Figure 9a-b) are dominated by clusters 2 and 4, while the deeper parts of the model (Figure 9c-d) are
386 dominated by clusters 3 and 5, with the east-west striking buried valley to the south, (Figure 9c), is
387 primarily represented by clusters 1 and 2.

388 The histograms in Figure 10 show how the original variables, the CF-model, and the resistivity model are
389 represented in the five clusters. Clusters 3 and 5 have resistivity values almost exclusively below 10 Ωm
390 and CF values above 0.7, but mostly close to 1. In the resistivity model space clusters 2 and 4 represent
391 high and intermediate resistivity values respectively with some overlap, while cluster 1 overlap both
392 clusters 2 and 4. Figure 10 also clearly shows that both the resistivity values and the CF-values contribute
393 to the final clusters. The clusters 1, 2, and 4 span only part of the resistivity space with significant
394 overlaps (Figure 10a), while they are clearly separated in the CF-model space and span the entire interval
395 (Figure 10b). The opposite is observed for clusters 3, 4, and 5, which are clearly separated in the
396 resistivity space (Figure 10a), but strongly overlap in the CF-model space (Figure 10b).

397 The CF-model does not differentiate between clay types, contrary the EM-resistivity data that have a
398 good resolution in the low resistivity range and therefore, to some degree, are able to distinguish between
399 clay types. This results in the two-part clustering of the low resistivity ($>20 \Omega\text{m}$) values as seen in Figure
400 10a.

401 **4 DISCUSSION**

402 **4.1 Translator function, grid and discretization**

403 The spatially varying resistivity to CF translator function is the key to achieve consistency between the
404 borehole information and the resistivity models, and the spatial variations of the translator model accounts
405 for, at least, two main phenomena: 1) Changes in the resistivity-lithology petrophysical relationship, 2)
406 The resolution capability in the geophysical results.

407 The first issue includes spatial changes in the pore water resistivity, the degree of water saturation, and/or
408 contents of clay minerals for the sediments described lithologically as clay. The spatial variation in the

409 pore water resistivity on this modeling scale is probably relatively smooth and small and will therefore
410 only have a minor impact on the resistivity to lithology/clay fraction translation. Even in the case with
411 larger fluctuations in the pore water resistivity (e.g. present of saline pore water) the translator function
412 will automatic adapt to this as long as we have borehole information available that resembles the changes
413 and the basic assumption that the clay rich formations are more conductive than coarse-grained sediments
414 is fulfilled.

415 In the Norsminde area used in the case history the groundwater table is generally located a few meters
416 below the surface and the groundwater is fresh. This means that the neither pore water resistivity nor the
417 water saturation plays a major role for the resistivity-clay fraction relationship and thus the translator
418 function. Though, in the case with a thicker unsaturated zone like for the pore water resistivity, the
419 translator function will automatically adapt to this situation as long as borehole information is available.

420 The varying content of clay minerals in the lithologies described as *clay* will effect the translator model.
421 The correlation between the clay mineral content and resistivity is quite strong and could be the key
422 parameter instead of the simple clay fraction of this procedure, but it would require clay mineral content
423 values available in boreholes on a large modeling scale, which is why we disregard this approach and use
424 the intentionally simple definition of clay and clay fraction.

425 The second issue concerns the resolution of the true formation resistivity in the resistivity models.
426 Lithological logs contain point information with a good and uniform vertical resolution. Contrary, AEM
427 data provide a good spatial coverage, but the vertical resolution is relatively poor and decreasing with
428 depth. Detailed geological layer sequences might only be represented by an average conductivity or only
429 have a weak signature in the resistivity models. By allowing spatial variation in the translation we can, to
430 some degree, resolve weak layer indications in the resistivity models by utilizing the vertically detailed
431 structural information from the lithological logs via the translator function.

432 The resolution in the final CF-model is strongly correlated to the resolution in the resistivity model, since
433 the resistivity dataset contribute with the majority of the information. In general EM-methods are
434 sensitive to absolute changes in the electric conductivity, which makes the resolution in the low resistivity
435 end superior to the resolution of high-resistivity contrasts. The diffusive behavior of EM-methods results
436 in a decreasing horizontal and vertical resolution capability with depth, and the vertical resolution
437 capability furthermore strongly depends on the layer sequence. A sequence of thin lithological layering
438 may therefore be represented as a single resistivity layer with an average conductivity, which is obviously
439 challenging for the geological interpretation. The horizontal resolution strongly depends on the
440 sample/line density of the geophysical measurements, but the footprint of a single measurement sets the
441 lower limit for the horizontal resolution. The Norsminde airborne SkyTEM survey is conducted with a

442 very dense line spacing giving a very high lateral resolution, which could actually support a finer
443 horizontal discretization (25-50 m) in the CF-model. The 100 m horizontal discretization of the CF-model
444 and cluster-model was selected to match the computational grid setup of a subsequent groundwater
445 model. A detailed overview of resolution capabilities of the Norsminde SkyTEM survey is given by
446 Schamper et al. (2014b) including an extensive comparison to borehole data

447 The horizontal sampling of the translator function should in principle be able to reproduce the true (but
448 unknown) variations in the resistivity to CF translation. Though it is primarily the borehole density and
449 secondarily the complexity of the petrophysical relationship between clay and resistivity that dictates the
450 needed horizontal sampling of the translator function. To our experience a horizontal discretization of the
451 translator function grid of 1-2 km (linearly interpolated between nodes) is sufficient to obtain an
452 acceptable consistency between the lithological logs and the translated resistivities. For the deeper part of
453 the model domain where the borehole information is sparse, a coarser translator function grid would be
454 sufficient.

455 Starting model values for the translator function in the inversion scheme become important in areas with
456 very low borehole density, primarily the deeper part of the model domain. The starting model values are
457 selected based on experience and by a visual comparison of the resistivity models to key lithological logs.
458 The horizontal and vertical constraints to migrate some information from regions with many boreholes to
459 regions with few boreholes or with no boreholes. As in most inversion tasks a few initial inversions are
460 performed to fine-tune and to evaluate the effect of different starting models and constraints setup.

461 The CF-procedure supports both uncertainty estimates on the input data, on the output translator
462 functions, and on the final CF-model. Generally, the uncertainties in the CF-model are closely related to
463 the borehole density and quality, as well as resolution and density of the resistivity models. The
464 calculation and estimation of input and output uncertainties is described in detail in Christiansen et al.
465 (2014).

466 **4.2 Clustering and validation**

467 For the clustered 3D-model each cluster represents some unit with fairly uniform characteristics. It could
468 be hydrostratigraphic units where the hydraulic conductivity of the cluster units is determined through a
469 subsequent groundwater model calibration, typically constrained by hydrological head and discharge data.
470 Groundwater model calibration of the Norsminde 3D-cluster model has been performed with a
471 preliminary positive outcome, but more experiments are needed before drawing final conclusions. In this
472 process one needs to evaluate the cluster validity, i.e. how many clusters the data can support. Cluster
473 validity can be assessed with various statistical measures (e.g. Halkidi et al., 2002). The number of

474 clusters resulting in the best hydrological performance might also be used as a measure of cluster validity.
475 The validity of the clusters and the resulting groundwater model is still to be explored in more detail.

476 **5 CONCLUSION**

477 We have presented a procedure to produce 3D clay-fraction models, integrating the key sources of
478 information in a well-documented and objective way.

479 The CF-procedure combines lithological borehole information with geophysical resistivity models in
480 producing large scale 3D clay fraction models. The integration of the lithological borehole data and the
481 resistivity models is accomplished through inversion, where the optimum resistivity to clay fraction
482 function minimizes the difference between the observed clay fraction from boreholes and the clay fraction
483 found through the geophysical resistivity models. The CF-procedure allows for horizontal and lateral
484 variation in the resistivity to clay fraction translation with smoothness constraints as regularization. The
485 spatially varying translator function is the key to achieve consistency between the borehole information
486 and the resistivity models. The CF-procedure furthermore handles uncertainties on both input and output
487 data.

488 The CF-procedure was applied to a 156 km² survey with more than 700 boreholes and 100,000 resistivity
489 models from an airborne survey. The output was a detailed 3D clay fraction model combining resistivity
490 models and lithological borehole information into one parameter.

491 Finally a cluster analysis was applied to achieve a predefined number of geological/hydrostratigraphic
492 clusters in the 3D-model and enabled us to integrate various sources of information, geological as well as
493 geophysical. The final five-cluster model differentiates between clay materials and different high resistive
494 materials from information held in resistivity model and borehole observations respectively.

495 With the CF-procedure and clustering we aim at building 3D models suitable as structural input for
496 groundwater models. Each cluster will then represent a hydrostratigraphic unit and the hydraulic
497 conductivity of the units will be determined through the groundwater model calibration constrained by
498 hydrological head and discharge data.

499 The 3D clay fraction model can also be seen as a binomial geological sand-clay model by interpreting the
500 high and low CF-values as clay and sand respectively, as the color scale for the CF-model example in
501 Figure 7 and Figure 8 indicated. Integration and further development of the CF-model into more complex
502 geological models have been carried out with success (Jørgensen et al., 2013b).

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511 emeritus Niels Bøje Christensen for insightful comments on the uncertainty migration.

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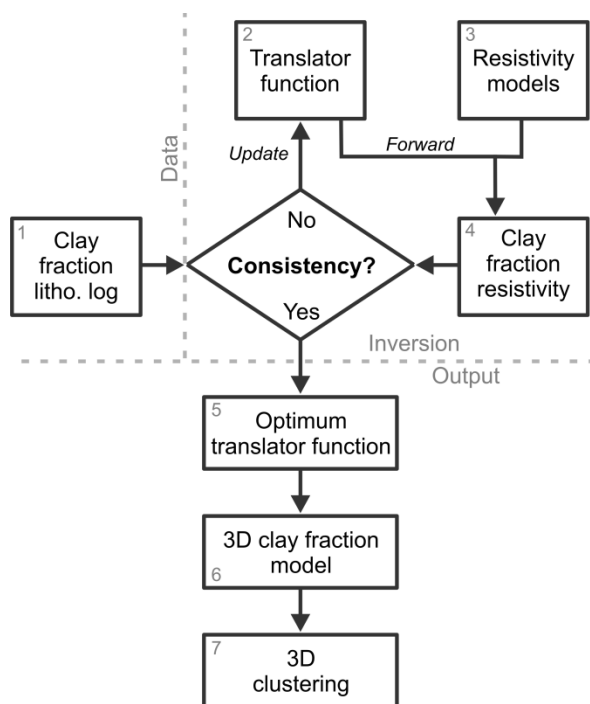
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627

628 **FIGURES AND FIGURE CAPTIONS**

629 **Figure 1**

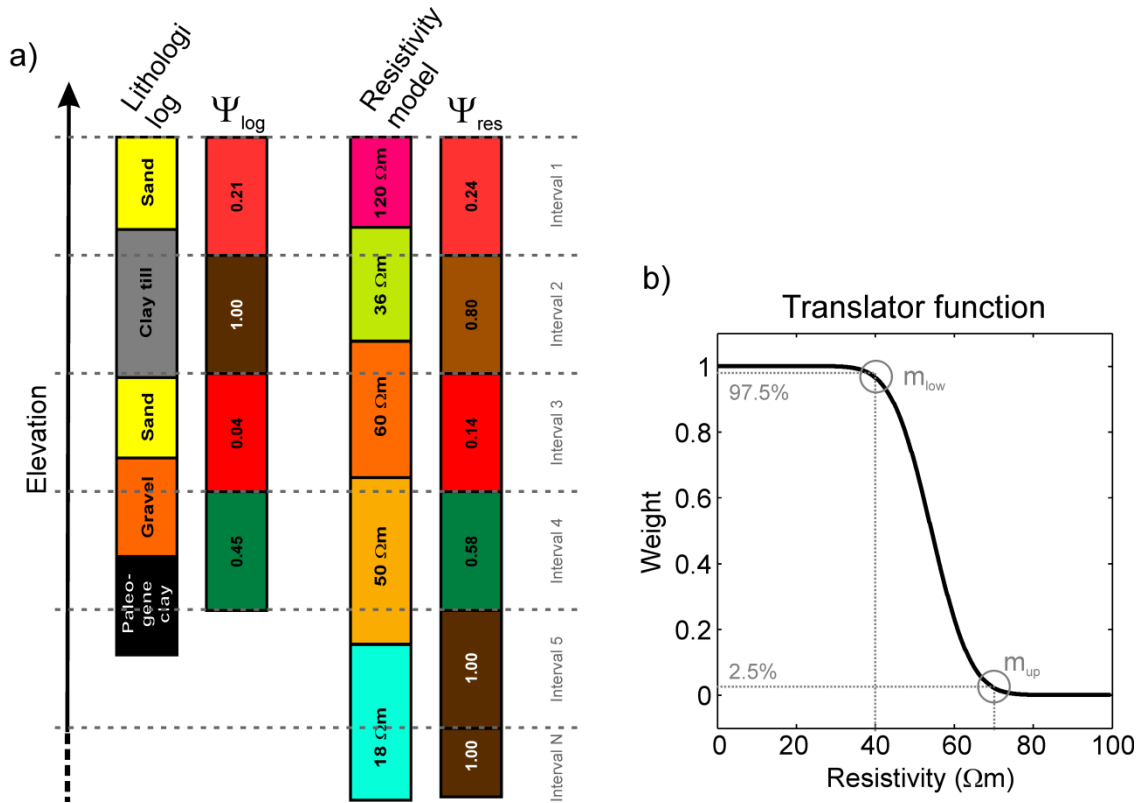
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632 Figure 1. Conceptual flowchart for the CF-procedure and clustering

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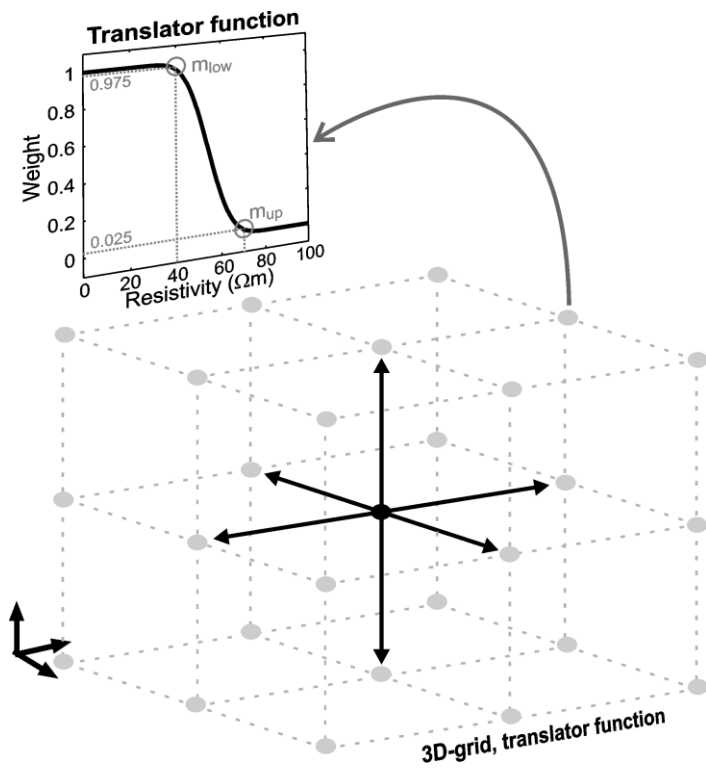


635

636 Figure 2. a) Example of how a lithological log translates into a Ψ_{log} and how a resistivity model translates
 637 into Ψ_{res} , for a numbers of calculation intervals. The resistivity values and the resulting clay fraction
 638 values are stated on the bars, but also indicated with colors with reference to the color scales of Figure 7.
 639 b) The translator function returns a weight, W, between 0 and 1 for a given resistivity value. The
 640 translator function is defined by the two parameters m_{low} , and m_{up} . In this example the m_{low} , and m_{up}
 641 parameters are 40 Ωm and 70 Ωm respectively.

643 **Figure 3**

644



645

646 Figure 3. The translator function and 3D translator function grid. Each node in the 3D translator function

647 grid holds a set of m_{up} and m_{low} . The m_{up} and m_{low} parameters are constrained to all neighboring

648 parameters as indicated with the black arrows for the black center node.

649 **Figure 4**

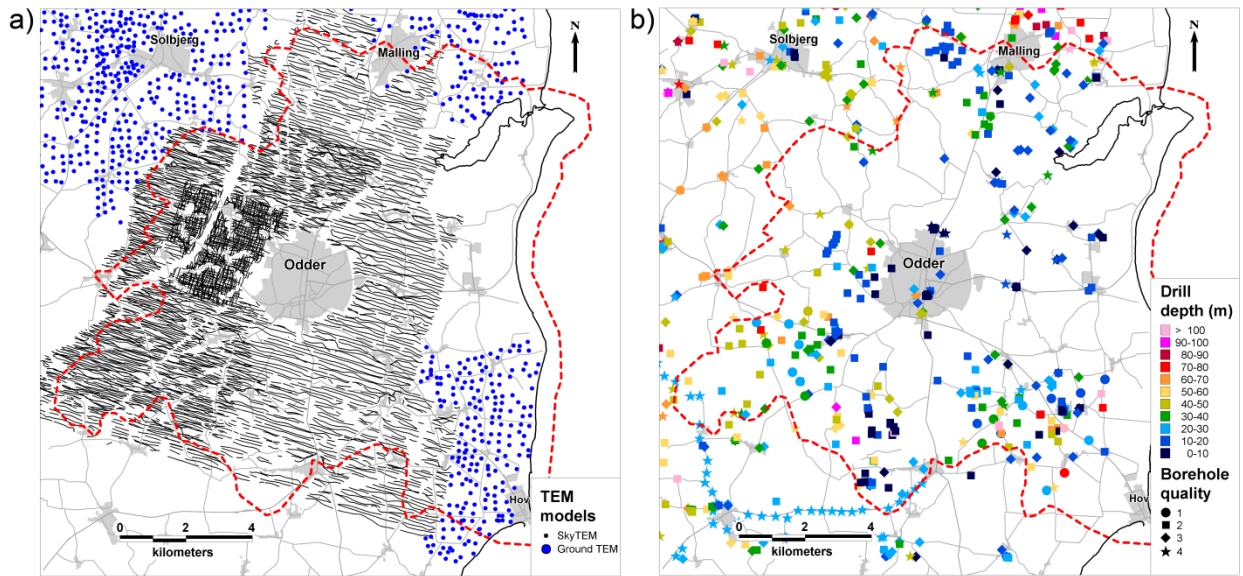
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652 Figure 4. The black square marks the Norsminde survey area.

653 **Figure 5**

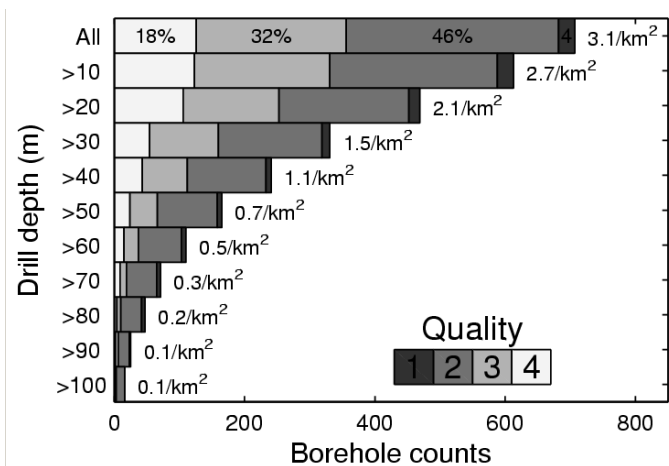


654
 655 Figure 5. a) Resistivity model positions for the SkyTEM survey and the ground-based TEM soundings. b)
 656 Borehole locations, quality (shape), and drill depth (color). Quality 1 corresponds to the highest quality
 657 and 4 to the lowest quality. The red dashed line outlines the catchment area (156 km²).

658

659 **Figure 6**

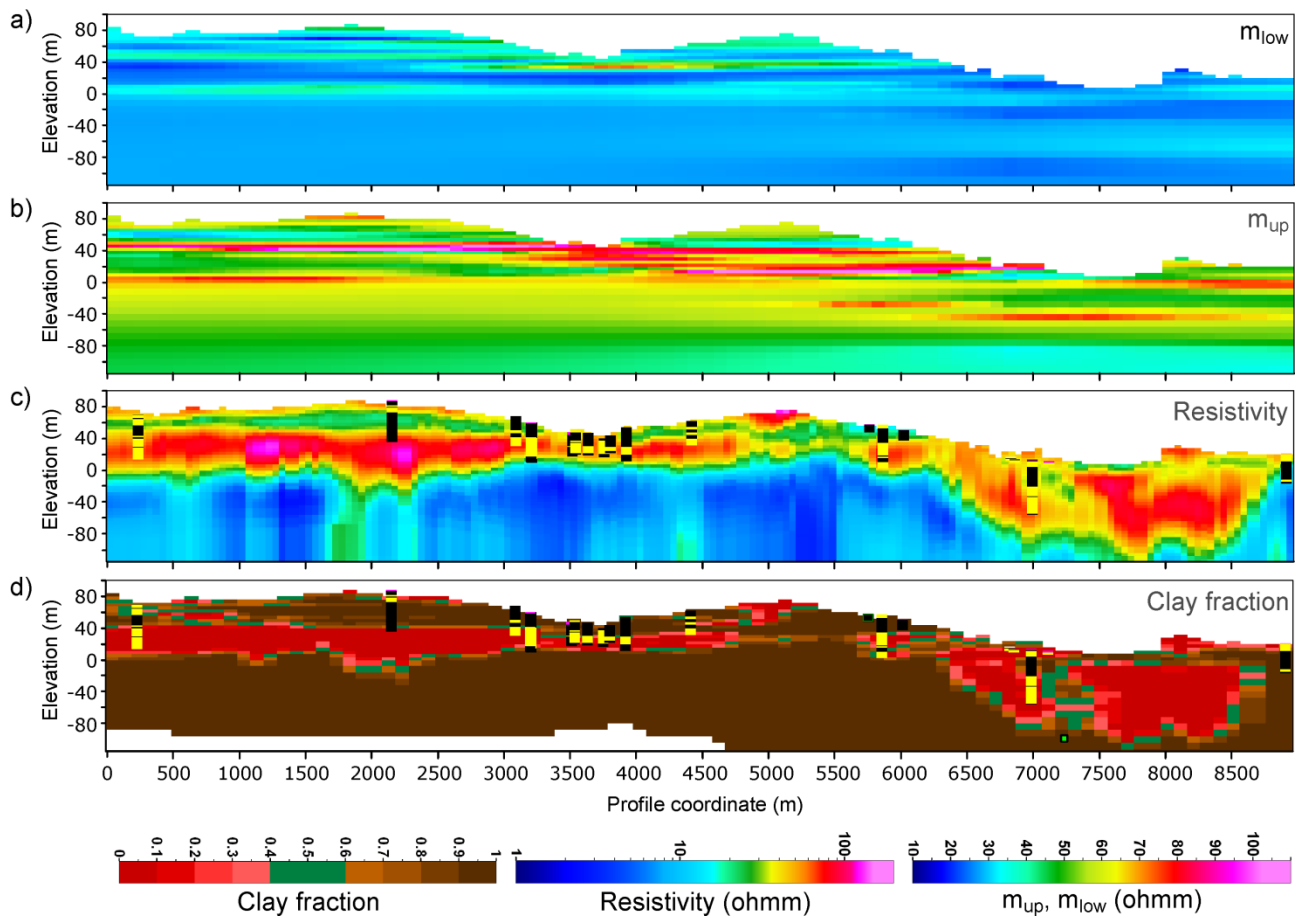
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661
 662 Figure 6. Number of boreholes vs. drill depth for the Norsminde survey area. The bars show how many
 663 boreholes reach a certain depth. The value to the right of the bars specifies the number of boreholes per
 664 km² at the different depths. The color coding of the bars marks the borehole quality grouping.

665 **Figure 7**

666



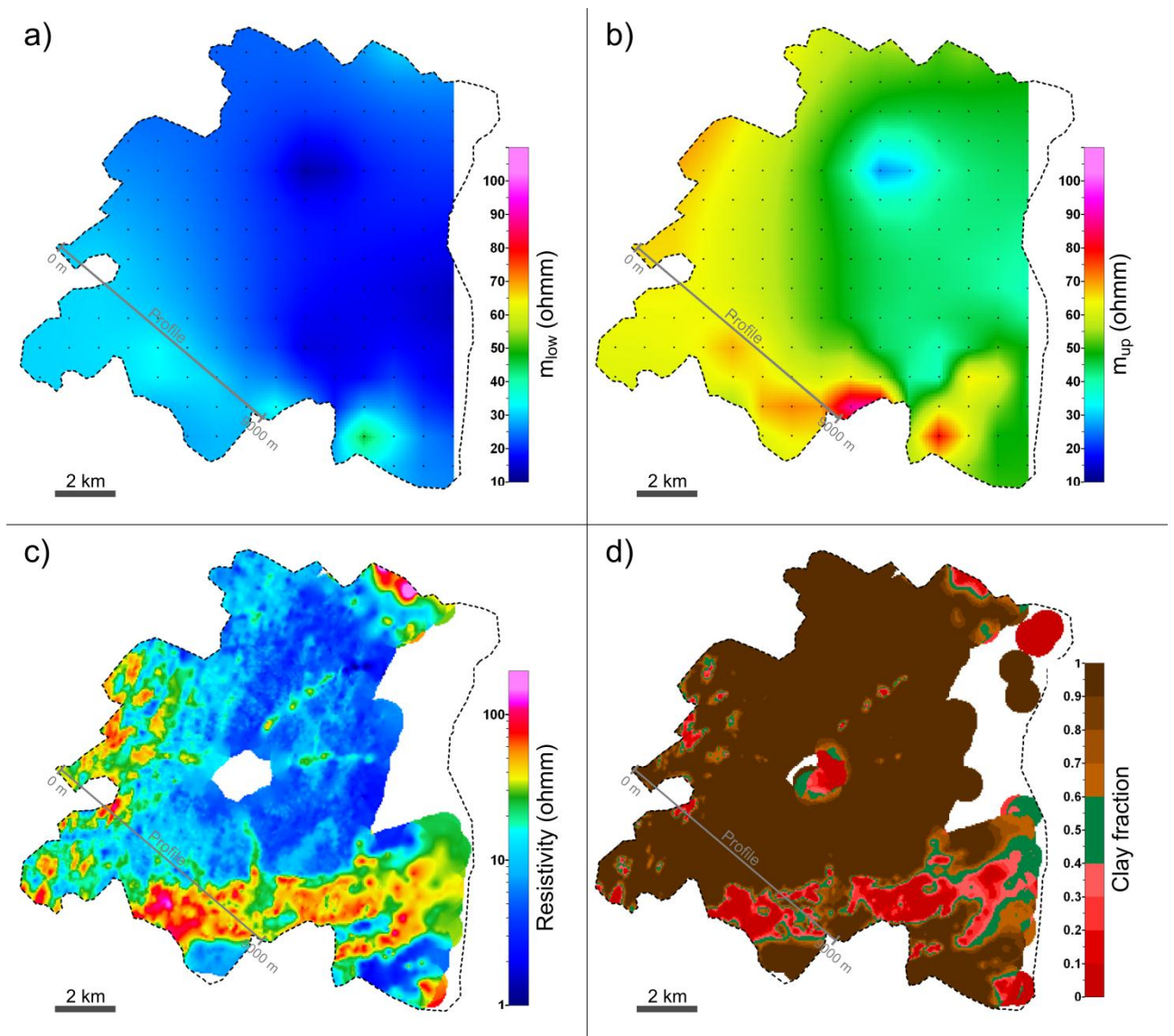
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668 Figure 7. Northwest-southeast cross sections (vertical exaggeration x6). Location and orientation of the
669 cross sections are marked in Figure 8. a) The m_{low} parameters of the translator function. b) The m_{up}
670 parameters of the translator function. c) The resistivity section with boreholes within 200 m of the profile
671 superimposed. Black and yellow vertical bars show the position of boreholes: Black blocks mark the clay
672 layers, and yellow blocks mark sand and gravel layers. d) Clay fraction section and boreholes (same
673 boreholes as plotted in the resistivity section).

674

675 **Figure 8**

676

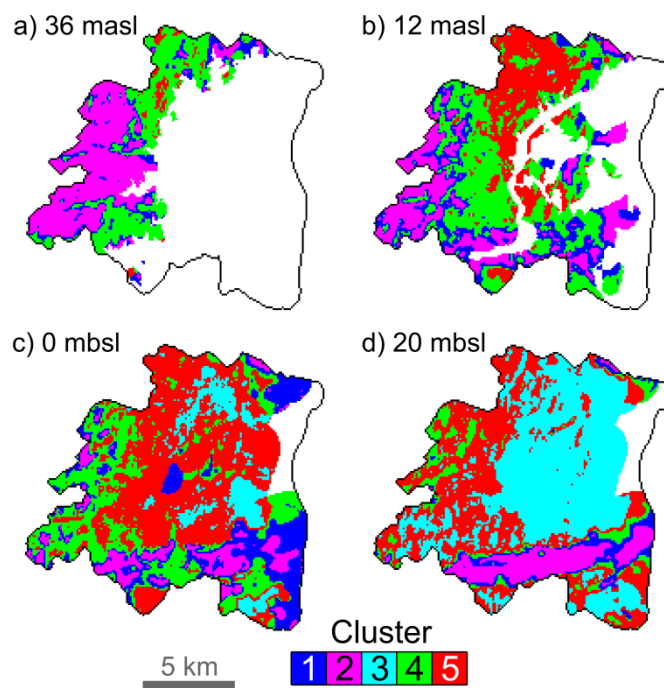


677

678 Figure 8. Horizontal slices at 2 m bsl cropped to the catchment area (dashed line). a) The m_{low} parameters
679 of the translator function superimposed with the 1 km translator function grid (black dots). b) The m_{up}
680 parameters of the translator function superimposed with the 1 km translator function grid (black dots). c)
681 Resistivity slice (interpolated). Note that no EM-data is available around the town of Odder (see Figure
682 5a) resulting in a "hole" in the resistivity map. d) Resulting CF-model. The hole in the resistivity map is
683 here partly closed because CF-values from boreholes are available in this area.

684 **Figure 9**

685

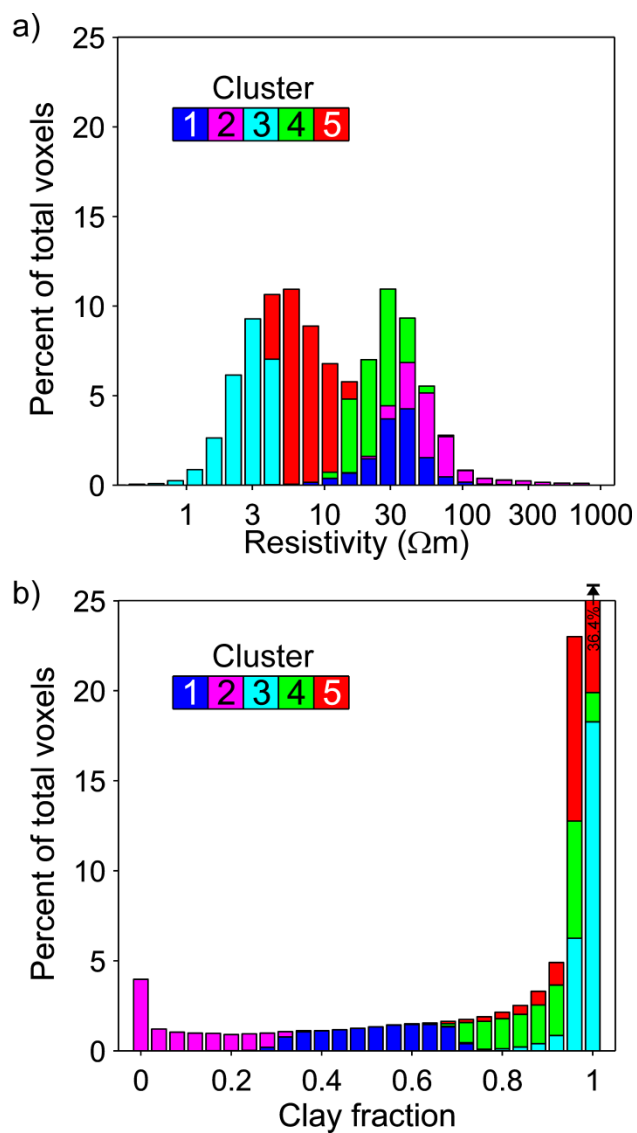


686

687 Figure 9. Horizontal slices in four depths of the 3D cluster model.

688 **Figure 10**

689



690

691 Figure 10. Cluster statistics. The histograms show which data from the original variables make up the five
692 clusters. a) The distribution of the resistivity data in the five clusters. b) The distribution of the CF data in
693 the five clusters.

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