

June 17, 2015

Dr. Ross Woods
Editor
Hydrology and Earth System Sciences

Dear Dr. Woods,

We have completed the minor revisions to our *Hydrology and Earth System Sciences* manuscript “Exploring the impact of forcing error characteristics on physically based snow simulations within a global sensitivity analysis framework” (hess-2014-461) and are now resubmitting it.

In the pages below, we include our point-by-point response to the reviewer’s comments and a marked-up version of the manuscript to show all modifications made through the course of the review process. We appreciate your time and the reviewers’ time in the review process and look forward to hearing your decision. Thank you again for considering our manuscript for publication.

Sincerely,

A handwritten signature in black ink that reads "Mark S. Raleigh". The signature is written in a cursive style with a large, stylized 'M' and 'R'.

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Response to second review by F. Pianosi (Referee)

Note: reviewer comments are in italics and the authors' responses are in normal face.

Comment: The paper has been substantially revised after the first round of reviews and I think it is significantly improved. In particular, with respect to the comments raised in my review, the discussion of GSA results and their interpretation is much more solid and convincing.

The authors found some inadequacies in their code implementing the error models and after fixing them they were able to produce GSA results that look much more reliable. They also enriched their discussion of GSA results with more insights on their physical meaning and implications, and more interpretation of "surprising" or unexpected results.

In my opinion this revised manuscript is suitable for publication and could constitute an interesting contribution to the readership of HESS, and a nice demonstration of how GSA methods can be used to learn about the behavior of a hydrological model and its sources of uncertainty.

I have few minor suggestions (mainly again relating to methodological aspects and references of GSA), that the authors may consider in a final revision of their manuscript.

Response: We thank you for your time and thoughtful comments in this second review.

Comment: Lines 376-378: "Sensitivity analyses tend to focus more on the model parameter ... than on the forcing matrix". True, however recently there have been an increasing number of applications considering other input factors than parameters, for instance

Baroni, G., Tarantola, S., 2014. A general probabilistic framework for uncertainty and global sensitivity analysis of deterministic models: A hydrological case study. Environmental Modelling & Software 51, 26–34.

and references therein. It would be good to cite some of these works, also to stress that GSA does not need to focus on parameters only.

Response: Thank you for making us aware of this work. We have added a sentence here stating that other sensitivity analyses have considered other sources of model uncertainty (with citations).

Comment: Lines 387-389: "Sobol' sensitivity analysis uses variance decomposition to attribute output variance to input variance". I would say "to input variability" or "to input uncertainty" (see similar comment in my previous review)

Response: We changed the wording to "input uncertainty".

Comment: Lines 396-399: *“A key assumption to the Sobol' approach is that the factors are independent”*: I know the authors introduced this sentence to address one of my previous comments, however the sentence is not technically completely correct (I was a bit sloppy about this in my review too). There are some recent papers that show how to apply the Sobol' approach in the case of correlated/dependent inputs (Lilburne & Tarantola, 2009. Sensitivity analysis of spatial models.; Kucherenko et al, 2012. Estimation of global sensitivity indices for models with dependent variables; Castaing and Gratiet, 2015, ANOVA decomposition of conditional Gaussian processes for sensitivity analysis with dependent inputs), however they require a sampling and approximation strategy different from the one implemented in this paper and described in Sec. 3.3.3. So maybe better rephrase the sentence like:

“A key assumption to the implementation of the Sobol' approach used in this paper (see Sec. 3.3.3) is that the factors are independent”

Response: We agree that this is important to distinguish. We have changed the wording based on your recommendation. We also add a new sentence stating “Frameworks have been proposed for the case of correlated factors (e.g., forcing errors) in a sensitivity analysis (e.g., Kucherenko et al., 2012), but we leave those applications for future work.”

Comment: Line 436: *“Final S_{Ti} values”*: what does *“final”* mean here?

Response: By “final” we mean the S_{Ti} values computed using all samples. We have changed the wording to reflect this convention.

Comment: Line 442 and following (and Figure 2): *I think the term “Sobol' values” is a bit confusing, one could think it refers to values of the sensitivity indices rather than input samples, or suggest that there is a link between the quasi-random sampling strategy and the variance decomposition idea, while there is not (apart from the fact that Sobol' contributed to both). Maybe better use “input factor samples” or “parameter samples”?*

Response: Thank you for pointing out this potentially confusing issue. We have renamed “Sobol' values” as “input factor samples” in three cases in Section 3.3.5 and in Figure 2.

Comment: Lines 679-680: *“we calculated daily sensitivity indices of modeled SWE to forcing biases at each site and scenario (Fig. 8).”* I understand that here the output variable whose sensitivity is being assessed is the simulated SWE on given day (and sensitivity index is re-estimated at each day in the simulation horizon). If so, this is conceptually quite different from the output definitions used so far (aggregate indicators from the entire time series of simulated variables). Maybe good to add one sentence to further clarify the point? Readers not particularly familiar with GSA may struggle here.

Response: We added sentences to help clarify how this analysis is different: “This final analysis was conceptually different than the previous analyses (Fig 5-7) in terms of the model output considered. Whereas the previous analyses computed sensitivity indices for summative model

outputs (e.g., peak SWE, total sublimation), the final analysis re-calculated sensitivity indices for SWE each day. This approach allowed us to examine how SWE model sensitivity changed as a function of time within the snow season.”

Comment: *Table 4: I understand the number outside parenthesis is the number of “behavioural” samples in the initial Sobol’ matrix and the one in parenthesis is model simulations, the relation being the usual $N_{\text{sim}} = N_{\text{samp}} \times (k+2)$ where $k=8$ in your case study - but it took a while to figure out - maybe better just say it in the caption? Also, this seems to suggest that you checked output samples associated to the initial Sobol’ matrix only, while I suppose you should also check the feasibility after resampling - in other words, check the final matrix A_B ?*

Response: We can see how the relationship between number of samples and model simulations might not be obvious based on the table and caption, so clarification is warranted. The reported figures include all simulations from the initial matrices A, B, and A_B. Recall that A and B each require N simulations while A_B requires kN simulations, hence the total number of simulations is $N+N+kN = N \times (k+2)$. If a sample is rejected in one of these the matrices, the corresponding simulations in all three matrices (sampling and resampling matrices) are also rejected. So in effect we are checking the simulations from the final matrix A_B, as well as the A and B matrices.

We have revised the caption to read: “Number of samples (N) and model simulations (in parentheses) meeting the requirements for minimum peak SWE and snow duration and valid snow disappearance dates at each site in each scenario. The number of model simulations scaled as $N \times (k+2)$, where $k=12$ in scenario NB+RE and $k=6$ in all other scenarios. When a simulation was rejected, all related simulations (based on resampling) were also rejected.”

1 Exploring the impact of forcing error characteristics on physically based snow 2 simulations within a global sensitivity analysis framework

3

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8

9 Abstract

10 Physically based models provide insights into key hydrologic processes, but are associated with
11 uncertainties due to deficiencies in forcing data, model parameters, and model structure. Forcing
12 uncertainty is enhanced in snow-affected catchments, where weather stations are scarce and
13 prone to measurement errors, and meteorological variables exhibit high variability. Hence, there
14 is limited understanding of how forcing error characteristics affect simulations of cold region
15 hydrology [and which error characteristics are most important](#). Here we employ global sensitivity
16 analysis to explore how (1) different error types (i.e., bias, random errors), (2) different error
17 [probability](#) distributions, and (3) different error magnitudes influence physically based
18 simulations of four snow variables (snow water equivalent, ablation rates, snow disappearance,
19 and sublimation). We use Sobol' global sensitivity analysis, which is typically used for model
20 parameters, but adapted here for testing model sensitivity to co-existing errors in all forcings.
21 We quantify the Utah Energy Balance model's sensitivity to forcing errors with [1 840 000](#) Monte
22 Carlo simulations across four sites and [five](#) different scenarios. Model outputs were (1)
23 [consistently](#) more sensitive to forcing biases than random errors, (2) [generally](#) less sensitive to
24 forcing error distributions, and (3) [critically](#) sensitive to different forcings depending on the
25 relative magnitude of errors. For typical error magnitudes [found in areas with drifting snow](#),
26 precipitation bias was the most important factor for snow water equivalent, ablation rates, and
27 snow disappearance timing, but other forcings had a [more dominant](#) impact [when precipitation](#)
28 [uncertainty was due solely to gauge undercatch](#). Additionally, the relative importance of forcing
29 errors depended on the model output of interest. Sensitivity analysis can reveal which forcing
30 error characteristics matter most for hydrologic modeling.

31

32 **1. Introduction**

33 Physically based models allow researchers to test hypotheses about the role of specific processes
34 in hydrologic systems and how changes in environment (e.g., climate, land cover) may impact
35 key hydrologic fluxes and states (Barnett et al., 2008; Clark et al., 2011b; Deems et al., 2013;
36 Leavesley, 1994). Due to the complexity of processes represented, these models usually require
37 numerous meteorological forcing [inputs](#) and model parameters. Most inputs are not measured at
38 the locations of interest and require estimation; hence, large uncertainties may propagate from
39 hydrologic model inputs to outputs. Despite ongoing efforts to quantify forcing uncertainties
40 (e.g., Bohn et al., 2013; Clark and Slater, 2006; Flerchinger et al., 2009) and to develop
41 methodologies for incorporating uncertainty into modeling efforts (e.g., He et al., 2011b;
42 Kavetski et al., 2006a; Kuczera et al., 2010; Slater and Clark, 2006), many analyses continue to
43 ignore uncertainty. These often assume either that all forcings, parameters, and structure are
44 correct (Pappenberger and Beven, 2006) or that only parametric uncertainty is important (Vrugt
45 et al., 2008b). Neglecting uncertainty in hydrologic modeling reduces confidence in hypothesis
46 tests (Clark et al., 2011b), thereby limiting the usefulness of physically based models.

47

48 There are fewer detailed studies focusing on forcing uncertainty relative to the number of
49 parametric and structural uncertainty studies (Bastola et al., 2011; Benke et al., 2008; Beven and
50 Binley, 1992; Butts et al., 2004; Clark et al., 2008, 2011b, 2015a, 2015b; Essery et al., 2013;
51 Georgakakos et al., 2004; Jackson et al., 2003; Kelleher et al., 2015; Kuczera and Parent, 1998;
52 Liu and Gupta, 2007; Refsgaard et al., 2006; Slater et al., 2001; Smith et al., 2008; Vrugt et al.,
53 2003a, 2003b, 2005; Yilmaz et al., 2008). Di Baldassarre and Montanari (2009) suggest that
54 forcing uncertainty has attracted less attention because it is “often considered negligible” relative
55 to parametric and structural uncertainties. Nevertheless, forcing uncertainty merits more
56 attention in some cases, such as in snow-affected watersheds where meteorological and energy
57 balance measurements are scarce (Bales et al., 2006; Raleigh, 2013; Schmucki et al., 2014) and
58 prone to errors [due to environmental or instrumental factors](#) (Huwald et al., 2009; Lundquist et
59 al., 2015; Rasmussen et al., 2012). Forcing uncertainty is enhanced in complex terrain where
60 meteorological variables exhibit high spatial variability (Feld et al., 2013; Flint and Childs, 1987;

61 Herrero and Polo, 2012; Lundquist and Cayan, 2007). As a result, the choice of forcing data can
62 yield substantial differences in calibrated model parameters (Elsner et al., 2014) and in modeled
63 hydrologic processes, such as snowmelt and evapotranspiration (Mizukami et al., 2014; Wayand
64 et al., 2013). Thus, forcing uncertainty demands more attention in snow-affected watersheds.

65

66 Previous work on forcing uncertainty in snow-affected regions has yielded basic insights into
67 how forcing errors propagate to model outputs and which forcings introduce the most uncertainty
68 in specific outputs. However, these studies have typically been limited to: (1)
69 empirical/conceptual models (He et al., 2011a, 2011b; Raleigh and Lundquist, 2012; Shamir and
70 Georgakakos, 2006; Slater and Clark, 2006), (2) errors for a subset of forcings (e.g., precipitation
71 or temperature only) (Burles and Boon, 2011; Dadic et al., 2013; Durand and Margulis, 2008;
72 Lapo et al., 2015; Xia et al., 2005), (3) model sensitivity to choice of forcing parameterization
73 (e.g., longwave) without considering uncertainty in parameterization inputs (e.g., temperature
74 and humidity) (Guan et al., 2013), and (4) simple representations of forcing errors (e.g., Kavetski
75 et al., 2006a, 2006b). The last is evident in studies that only consider single types of forcing
76 errors (e.g., bias) and single distributions (e.g., uniform), and examines errors separately (Burles
77 and Boon, 2011; Koivusalo and Heikinheimo, 1999; Raleigh and Lundquist, 2012; Xia et al.,
78 2005). [Lapo et al. \(2015\) show that biases have a greater impact than random errors on modeled
79 snow water equivalent and surface temperature, but this analysis only considers longwave and
80 shortwave forcings and considers errors separately.](#) Examining uncertainty in one factor at a
81 time remains popular but fails to explore the uncertainty space adequately, ignoring potential
82 interactions between forcing errors (Saltelli and Annoni, 2010; Saltelli, 1999). [In contrast,](#)
83 [global sensitivity analysis explores the uncertainty space more comprehensively by considering](#)
84 [uncertainty in multiple factors at the same time.](#)

85

86 The purpose of this paper is to [use global sensitivity analysis to](#) assess how specific forcing error
87 characteristics influence outputs of a physically based snow model. To our knowledge, no
88 [previously published](#) study has investigated this topic in snow-affected regions. It is unclear how
89 (1) different error types (bias vs. random errors), (2) different error distributions, and (3)
90 different error magnitudes across all forcings affect model output. [The impact of forcing errors](#)

91 [on models can be tested by corrupting forcings with specified characteristics \(e.g., artificial](#)
92 [biases and random errors\) and quantifying the impact on model outputs \(e.g., Oudin et al., 2006;](#)
93 [Spank et al., 2013\), but we are unaware of any detailed studies that have done this type of](#)
94 [experiment for all meteorological forcings commonly required for physically based snow](#)
95 [models. We hypothesize that \(1\) model outputs are more sensitive to biases than random errors](#)
96 [in forcing variables, \(2\) the assumed probability distribution for biases will alter the relative](#)
97 [ranking of importance in forcing errors, and \(3\) the magnitude of forcing biases will have a](#)
98 [strong influence on which forcing errors are most important.](#)

99
100 [In our view, it is important to clarify the relative impact of specific error characteristics on](#)
101 [modeling applications, so as to prioritize future research directions, improve understanding of](#)
102 [model sensitivity, and to address questions related to network design. For example, given budget](#)
103 [constraints, is it better to invest in a heating apparatus for a radiometer \(to minimize bias due to](#)
104 [frost formation on the radiometer dome\) or in a higher quality radiometer \(to minimize random](#)
105 [errors associated with measurement precision\)? Additionally, it is important to contextualize](#)
106 [different meteorological data errors, as these errors are usually studied independently of each](#)
107 [other \(e.g., longwave radiation, Flerchinger et al., 2009; air temperature, Huwald et al., 2009\),](#)
108 [and it is unclear how they compare in terms of model sensitivity.](#)

109
110 The [overarching](#) research question is “how do assumptions regarding forcing error characteristics
111 impact our understanding of uncertainty in physically based model output?” Using the Sobol’
112 (1990) global sensitivity analysis framework, we investigate how artificial errors introduced into
113 high-quality observed forcings (temperature, precipitation, wind speed, humidity, shortwave
114 radiation, and longwave radiation) at four sites in contrasting snow climates propagate to four
115 snow model outputs (peak snow water equivalent, ablation rates, snow disappearance timing, and
116 sublimation) that are important to cold region hydrology. We select a single model structure and
117 set of parameters to clarify the impact of forcing uncertainty on model outputs. Specifically, we
118 use the physically based Utah Energy Balance (UEB) snow model (Mahat and Tarboton, 2012;
119 Tarboton and Luce, 1996) because it is computationally efficient. The presented framework
120 could be extended to other models.

121

122 **2. Study sites and data**

123 We selected four seasonally snow covered study sites (Table 1) in distinct snow climates (Sturm
124 et al., 1995; Trujillo and Molotch, 2014). The sites included (1) the tundra Innvait Creek (IC,
125 930 m) site (Euskirchen et al., 2012; Kane et al., 1991; Sturm and Wagner, 2010), located north
126 of the Brooks Range in Alaska, USA, (2) the maritime Col de Porte (CDP, 1330 m) site (Morin
127 et al., 2012) in the Chartreuse Range in the Rhône-Alpes of France, (3) the intermountain
128 Reynolds Mountain East (RME, 2060 m) sheltered site (Reba et al., 2011) in the Owyhee Range
129 in Idaho, USA, and (4) the continental Swamp Angel Study Plot (SASP, 3370 m) site (Landry et
130 al., 2014) in the San Juan Mountains of Colorado, USA. [We selected these sites because of the
131 quality and completeness of the forcing data, and because they spanned contrasting climates
132 \(Table 1\), allowing us to check for potential climate-dependencies in sensitivity to forcing errors.
133 Generalization of the results with climate was not possible due to the low sample size of sites.](#)

134

135 The sites had high-quality observations of model forcings at hourly time steps. Serially complete
136 published datasets are available at CDP, RME, and SASP (see citations above). At IC, data were
137 available from multiple co-located stations (Bret-Harte et al., 2010a, 2010b, 2011a, 2011b,
138 2011c; Griffin et al., 2010; Sturm and Wagner, 2010). These data were quality controlled, and
139 gaps in the data were filled as described in Raleigh (2013).

140

141 We considered only one year for analysis at each site (Table 1) due to the high computational
142 costs of the experiment. Measured evaluation data (e.g., snow water equivalent, SWE) at daily
143 resolution were used [only](#) for qualitative assessment of model output. SWE was observed at
144 snow pillows at IC and RME. [At CDP, a cosmic ray detector collected SWE data.](#) At SASP,
145 acoustic snow depth data were converted to daily SWE using density [inferred](#) from nearby
146 [SNOW TELemetry \(SNOTEL\) \(Serreze et al., 1999\) sites](#) and local snow pit measurements
147 (Raleigh, 2013).

148

149 We adjusted the available precipitation data at each site with a multiplicative factor to [correct for](#)
150 [potential undercatch errors](#) (e.g., Goodison et al., 1998; Rasmussen et al., 2012; Yang et al.,
151 2000) [and to](#) ensure the base model simulation with all observed forcings reasonably represented
152 observed SWE before conducting the sensitivity analysis. [Several studies have demonstrated the](#)
153 [necessity of](#) precipitation adjustments for realistic SWE simulations, even at well-instrumented
154 sites (e.g., Hiemstra et al., 2006; Reba et al., 2011; Schmucki et al., 2014). Precipitation
155 adjustments were most necessary at IC, where windy conditions preclude effective
156 measurements (Yang et al., 2000). In contrast, only modest adjustments were necessary at the
157 other three sites because they were located in sheltered clearings and because the data already
158 had some corrections applied in the published data. [We considered adjustment multipliers](#)
159 [ranging from 0.5 to 2.5 \(increments of 0.05\) and selected the multiplier that yielded the lowest](#)
160 [root mean squared error between observed and modeled SWE](#). Precipitation [multipliers were 1.6](#)
161 [at IC and 1.15 at SASP, and 0.9 at CDP and RME](#). [The undercatch errors at IC were consistent](#)
162 [with the 61-68% undercatch errors found by](#) Yang et al. (2000) [for Wyoming-type gauges in](#)
163 [wind-blown regions](#).

164

165 The initial discrepancies between modeled and observed SWE ([prior to applying the above](#)
166 [precipitation multipliers](#)) may have resulted from deficiencies in the measured forcings, model
167 parameters, model structure, and measured verification data, [and justification of our decision to](#)
168 [apply precipitation multipliers was warranted](#). [Manual observations of SWE \(e.g., snow surveys,](#)
169 [snow pits\) generally supported the automatically collected SWE observations \(no figures](#)
170 [shown\), and thus differences between observed and modeled SWE did not likely stem from](#)
171 [issues in the verification data](#). [Sites where we decreased the precipitation data \(CDP and RME\)](#)
172 [were also the warmer sites and experienced more mixed rain-snow events in the winter](#). Hence,
173 [we considered multiple hypotheses to explain the SWE differences at these sites: \(1\) the choice](#)
174 [of rain-snow parameterization, \(2\) the choice of parameters \(e.g., threshold temperatures\) for the](#)
175 [rain-snow parameterization, and \(3\) the quality of the forcing data \(e.g., precipitation\)](#). For these
176 [warmer sites, an exploratory analysis revealed that either \(1\) or \(3\) could explain the SWE](#)
177 [differences, but auxiliary data \(e.g., precipitation phase data\) were not available to discriminate](#)
178 [these hypotheses](#). [Choosing a different rain-snow parameterization might minimize the SWE](#)
179 [differences at the warmer sites but would not rectify the SWE differences at the colder sites \(IC](#)

180 [and SASP\) where most winter precipitation falls as snow. Therefore, the most straightforward](#)
181 [and consistent approach was to adjust the precipitation data and to leave the native UEB](#)
182 [parameterizations intact.](#) It was beyond the scope of this study to optimize model parameters and
183 unravel the relative contributions of uncertainty for factors other than the meteorological
184 forcings. [Nevertheless, we suggest these precipitation adjustments minimally affected the](#)
185 [sensitivity analysis, as we did not quantitatively compare the model outputs to the observed](#)
186 [response variables \(e.g., SWE\).](#)

187

188 3. Methods

189 3.1. Model and output metrics

190 The Utah Energy Balance (UEB) is a physically based, one-dimensional snow model (Mahat and
191 Tarboton, 2012; Tarboton and Luce, 1996; You et al., 2013). UEB represents processes such as
192 snow accumulation, snowmelt, albedo decay, surface temperature variation, liquid water
193 retention and refreezing, and sublimation. [Due to the one-dimensional structure of the model,](#)
194 [UEB does not account for lateral mass transfer of snow \(e.g., wind-induced snow drifting\), and](#)
195 [therefore these processes must be represented in other model components \(e.g., precipitation](#)
196 [uncertainty, see Sec. 3.2.3\).](#) UEB has a single bulk snow layer and an infinitesimally thin
197 surface layer for energy balance computations at the snow-atmosphere interface. UEB tracks
198 state variables for snowpack energy content, SWE, and a dimensionless snow surface age (for
199 albedo computations). We ran UEB at hourly time steps with six forcings: air temperature (T_{air}),
200 precipitation (P), wind speed (U), relative humidity (RH), incoming shortwave radiation (Q_{si}),
201 and incoming longwave radiation (Q_{li}). We used fixed parameters across all scenarios (Table 2).
202 We initialized UEB during the snow-free period; thus, model spin-up was unnecessary.

203

204 With each UEB simulation, we calculated four summary output metrics: (1) peak (i.e.,
205 maximum) SWE, (2) mean ablation rate, (3) snow disappearance date, and (4) total annual snow
206 sublimation. The first three metrics are important for the timing and magnitude of water
207 availability and identification of snowpack regime (Trujillo and Molotch, 2014), while the fourth
208 impacts the partitioning of annual P into runoff and evapotranspiration. We calculated the snow

209 disappearance date as the first date when 90% of peak SWE had ablated, similar to other studies
210 that use a minimum SWE threshold for defining snow disappearance (e.g., Schmucki et al.,
211 2014). The mean ablation rate was calculated in the period between peak SWE and snow
212 disappearance, and was taken as the absolute value of the mean of all SWE decreases.

213

214 3.2. Forcing error scenarios

215 To test how error characteristics in forcings affect model outputs, we [examined five](#) scenarios
216 (Fig. 1 and Table 3) with different assumptions regarding error types, distributions, and
217 magnitudes (i.e., error ranges). In the first scenario, only bias (normally [distributed for additive](#)
218 [errors](#) or lognormally distributed [for multiplicative precipitation errors](#)) was introduced into all
219 forcings at a level of high uncertainty (based on values observed in the field, see Sec. 3.2.3
220 below). This scenario was named “NB,” where N denotes normal (or lognormal) error
221 distributions and B denotes bias only. The remaining scenarios were identical to NB except one
222 aspect was changed: scenario NB+RE considered both bias and random errors (RE) [in all](#)
223 [forcings](#), scenario UB considered uniformly distributed biases [in all forcings](#), [scenario NB_gauge](#)
224 [considered precipitation error magnitudes associated with gauge undercatch](#), and scenario
225 NB_lab considered error magnitudes [for all forcings](#) at minimal values (i.e., specified instrument
226 accuracy as found in a laboratory). Constructed in this way (Fig. 1), we could test model
227 sensitivity to (1) bias vs. random errors by comparing NB and NB+RE, (2) error distributions by
228 comparing NB and UB, and (3) error magnitudes by comparing NB [\(high forcing uncertainty\) to](#)
229 [both NB_gauge \(moderate uncertainty in precipitation but high uncertainty for all other forcings\)](#)
230 and NB_lab [\(low forcing uncertainty\)](#).

231

232 3.2.1. Error types

233 Forcing data inevitably have some (unknown) combination of bias and random errors. However,
234 hydrologic sensitivity analyses have tended to focus more on bias with little or no attention to
235 random errors (Raleigh and Lundquist, 2012), [whereas data assimilation methods often focus on](#)
236 [random errors but assume bias does not exist](#) (e.g., Dee, 2005). [Rarely is there](#) any consideration
237 of interactions between [these](#) error types. [As a recent example](#), Lapo et al. (2015) tested biases

238 and random errors in Q_{si} and Q_{li} forcings, finding that biases generally introduced more variance
239 in modeled SWE than random errors. Their experiment considered biases and random errors
240 separately (i.e., no error interactions allowed), and examined only a subset of the required
241 forcings (i.e., radiation). Here, we examined co-existing biases in all forcings in NB, UB,
242 [NB_gauge](#), and NB_lab, and co-existing biases and random errors in all forcings in NB+RE.

243

244 Table 3 shows the assignment of error types for the [five](#) scenarios. We relied on studies that
245 assess errors in measurements or estimated forcings to identify typical characteristics of biases
246 and random errors. Published bias values were more straightforward to interpret than random
247 errors because common metrics, such as root mean squared error (RMSE) and mean absolute
248 error (MAE), encapsulate both systematic and random errors. Hence, when defining random
249 errors, published RMSE and MAE served as qualitative guidelines.

250

251 **3.2.2. Error distributions**

252 [In their recent review of global sensitivity analysis applications in hydrological modeling](#), Song
253 et al. (2015) [identified the selection of probability distributions \(this section\) and ranges \(Sec.](#)
254 [3.2.3\) as among the most important considerations. While it is common practice in sensitivity](#)
255 [analysis to assume a uniform distribution when sampling model parameters](#) (e.g., Campolongo et
256 al., 2011; Rosero et al., 2010), [this may fail to represent the real distribution of errors in](#)
257 [meteorological forcing data, as the uniform distribution implies that extreme and small biases are](#)
258 [equally probable. It is more likely that real error distributions more closely resemble non-](#)
259 [uniform distributions, with higher probability of smaller biases and lower probability of more](#)
260 [extreme biases \(e.g., normal distributions\). Investigators in other fields](#) (e.g., Foscarini et al.,
261 2010; Touhami et al., 2013) [have tested how distribution assumptions \(uniform vs. normal\)](#)
262 [change their computed measures of model sensitivity. These studies broadly suggest that the](#)
263 [grouping of most important factors may be similar under different distribution assumptions,](#)
264 [particularly in cases when interactions are minimal, but the relative ranking of factors within](#)
265 [those groups may vary depending on the distribution. Here we test how the assumed probability](#)
266 [distribution influences the sensitivity of a snow model to forcing errors.](#)

267
268 [We designed](#) the UB scenario [with the](#) naive hypothesis that the probability distribution of biases
269 was uniform [for all six meteorological variables](#). [In contrast](#), error distributions (Table 3) were
270 [assumed non-uniform \(described below\) in](#) scenarios NB, NB+RE, [NB_gauge](#), and NB_lab.
271 Unfortunately, error distributions are reported less frequently than error statistics (e.g., bias,
272 RMSE) in the literature. [We assumed that](#) T_{air} and RH errors follow normal distributions
273 (Mardikis et al., 2005; Phillips and Marks, 1996), as do Q_{si} and Q_{li} errors. Conflicting reports
274 over the distribution of U indicated that errors may be approximated with a normal (Phillips and
275 Marks, 1996), a lognormal (Mardikis et al., 2005), or a Weibull distribution (Jiménez et al.,
276 2011). For simplicity, we assumed that U errors were normally distributed. Finally, we assumed
277 P errors followed a lognormal distribution to account for snow redistribution due to wind
278 drift/scour (Liston, 2004) [or to account for precipitation gauge undercatch](#) (Durand and Margulis,
279 2007). Error distributions were truncated in cases when the introduced errors violated physical
280 limits (e.g., negative U ; see Sec. 3.3.5).

281

282 **3.2.3. Error magnitudes**

283 We considered [three](#) magnitudes of forcing uncertainty ([Table 3](#)): levels of uncertainty found (1)
284 [in the field for all forcings \(i.e., NB\)](#), (2) [in the field for all forcings except precipitation \(which](#)
285 [has uncertainty due to precipitation gauge undercatch, i.e., NB_gauge\)](#), and (3) [in](#) a controlled
286 laboratory setting [\(i.e., NB_lab\)](#). [These](#) cases were considered because they sampled realistic
287 errors [\(NB and NB_gauge\)](#) and minimum errors [\(NB_lab\)](#). We expected that the error ranges
288 exerted a major control on model uncertainty and sensitivity, [as demonstrated in several prior](#)
289 [sensitivity analyses \(see review of Song et al., 2015\)](#).

290

291 [Consideration of error magnitudes was achieved in each scenario by assigning a range to each](#)
292 [error probability distribution \(see Sec. 3.2.2 and Table 3\). While non-uniform distributions \(e.g.,](#)
293 [normal\) are typically described by measures other than the range \(e.g., mean and variance\), we](#)
294 [scaled these distributions \(see Sec. 3.3.5 for details\) such that they were bounded within a](#)
295 [specified range. This convention was necessary to ensure that differences between scenarios NB](#)

296 and UB were due solely to the shape of the error probability distributions, and not due to
297 differences in both distribution shape and the domain. Additionally, this followed the typical
298 practice of sensitivity analysis where the range specifies the domain of the distribution.

299

300 We considered field uncertainties in all forcings in NB, NB+RE, and UB, and in all forcings
301 except precipitation in NB_gauge. Field uncertainties depend on the source of forcing data and
302 on local conditions (e.g., Flerchinger et al., 2009; Lundquist et al., 2015). To generalize the
303 analysis, we chose error ranges for the field uncertainty that enveloped the reported uncertainty
304 of different methods for acquiring forcing data. T_{air} error ranges spanned errors in measurements
305 (Huwald et al., 2009) and commonly used models, such as lapse rates and statistical methods,
306 (Bolstad et al., 1998; Chuanyan et al., 2005; Fridley, 2009; Hasenauer et al., 2003; Phillips and
307 Marks, 1996). U error ranges spanned errors in topographic drift models (Liston and Elder,
308 2006; Winstral et al., 2009) and numerical weather prediction (NWP) models (Cheng and
309 Georgakakos, 2011). RH error ranges spanned errors in observations (Déry and Stieglitz, 2002)
310 and empirical methods (e.g., Bohn et al., 2013; Feld et al., 2013). Q_{si} error ranges spanned errors
311 in empirical methods (Bohn et al., 2013), radiative transfer models (Jing and Cess, 1998),
312 satellite-derived products (Jepsen et al., 2012), and NWP models (Niemelä et al., 2001b). Q_{li}
313 error ranges spanned errors in empirical methods (Bohn et al., 2013; Flerchinger et al., 2009;
314 Herrero and Polo, 2012) and NWP models (Niemelä et al., 2001a).

315

316 P error ranges spanned both undercatch (e.g., Rasmussen et al., 2012) and wind drift/scour errors
317 in NB, NB+RE, and UB, but only undercatch errors in NB_gauge. We assumed that P biases
318 due to gauge undercatch in NB_gauge ranged from -10% to +10% because Meyer et al. (2012)
319 found 95% of SNOTEL sites (often in forest clearings) had observations of accumulated P
320 within 20% of peak SWE. Results of NB, NB+RE, and UB were thus most relevant to areas
321 with prominent snow redistribution (e.g., alpine zone), whereas NB_gauge results were more
322 relevant to areas with minimal wind drift errors. It could be argued that uncertainty due to snow
323 drift processes is a structural issue and not a source of forcing error; however, this distinction
324 depends strongly on what type of model is considered. This process is clearly a structural
325 component for snow models with explicit (e.g., three dimensional models with dynamic wind

326 [transport](#), Lehning et al., 2006) [or implicit \(one dimensional models with probabilistic subgrid](#)
327 [snow variability routines, e.g., Clark et al., 2011a\) treatment of snow redistribution. However,](#)
328 [when a one dimensional snow model is applied at length scales shorter than drift process length](#)
329 [scales \(as assumed here with UEB\), then it is not possible to account for snow drift in a structural](#)
330 [sense. Therefore, we treat drifting snow as a form of precipitation error in NB, NB+RE, and UB.](#)
331 [Because UEB lacks dynamic wind redistribution, accumulation uncertainty was not linked to \$U\$](#)
332 [errors but instead to \$P\$ errors \(e.g., drift factor, Luce et al., 1998\).](#)

333

334 In contrast, scenario NB_lab assumed laboratory levels of uncertainty ([i.e., measurement](#)
335 [accuracy](#)) for each forcing. [Skiles et al. \(2012\) considered a similar scenario in their sensitivity](#)
336 [analysis of the SNOBAL model \(Marks and Dozier, 1992; Marks et al., 1992\) to instrument](#)
337 [accuracy at SASP, finding a 5 day range in uncertainty in modeled snow disappearance, with](#)
338 [longwave uncertainty having the greatest impact. An emerging sensitivity analysis \(Sauter and](#)
339 [Obleitner, 2015\) with the CROCUS model \(Brun et al., 1992\) applied on the Kongsvegen](#)
340 [Glacier \(Svalbard\) indicates that longwave measurement uncertainty has an approximately](#)
341 [comparable effect on modeled snow depth as \$\pm 25\%\$ precipitation uncertainty, but is the most](#)
342 [dominant influence on the modeled energy balance and turbulent heat flux \(relative to the](#)
343 [measurement uncertainty of other forcings\). Here we build on these efforts to examine how](#)
344 [instrument accuracy impacts modeled snow variables in a variety of seasonal snow climates. In](#)
345 [general, laboratory](#) uncertainty levels vary with the type and quality of sensors, as well as related
346 accessories (e.g., [radiation shield for the temperature sensor](#)), which we did not explicitly
347 consider. [Because the actual sensors available varied between sites \(Table 1\) and we needed](#)
348 [consistent errors across sites within scenario NB lab, we](#) assumed that the manufacturers'
349 specified accuracy of meteorological sensors at a typical SNOTEL site were representative of
350 minimum uncertainties in forcings because of the widespread use of SNOTEL data in snow
351 studies. While we used the specified accuracy for [idealized](#) P measurements in NB_lab, we note
352 that the instrument uncertainty of $\pm 3\%$ was likely unrepresentative of errors likely to be
353 encountered. For example, corrections applied to the P data (see Sec. 2) exceeded this
354 uncertainty by factors of 3 to 20.

355

3.3. Sensitivity analysis

Numerous approaches that explore uncertainty in numerical models have been developed in the literature of statistics (Christopher Frey and Patil, 2002), environmental modeling (Matott et al., 2009), and optimization/calibration [of hydrology and earth systems models](#) (Beven and Binley, 1992; Duan et al., 1992; Kavetski et al., 2002, 2006a, 2006b; Kuczera et al., 2010; Razavi and Gupta, 2015; Song et al., 2015; Vrugt et al., 2008a, 2008b). Among these, global sensitivity analysis is an elegant platform for testing the impact of input uncertainty on model outputs and for ranking the relative importance of inputs while considering co-existing sources of uncertainty. Global methods are ideal for non-linear models (e.g., snow models). The Sobol' (1990, hereafter Sobol') method is a robust global method based on the decomposition of variance (see below). We investigate Sobol', as it is often the baseline for testing sensitivity analysis methods (Herman et al., 2013; Li et al., 2013; Rakovec et al., 2014; Tang et al., 2007).

368

3.3.1. Overview: [model conceptualization and sensitivity](#)

One can visualize any hydrology or snow model (e.g., UEB) as:

$$\mathbf{Y} = M(\mathbf{F}, \boldsymbol{\theta}) \quad (1)$$

where \mathbf{Y} is a matrix of model outputs (e.g., SWE), $M(\)$ is the model operator, \mathbf{F} is a matrix of forcings (e.g., T_{air} , P , U , etc.), and $\boldsymbol{\theta}$ is an array of model parameters (e.g., [Table 2](#)). The goal of sensitivity analysis is to [determine which input factors](#) (\mathbf{F} and $\boldsymbol{\theta}$) [are most important to](#) specific outputs (\mathbf{Y}) (Matott et al., 2009). Sensitivity analyses [often](#) focus more on the model parameter array ($\boldsymbol{\theta}$) than on the forcing matrix (Foglia et al., 2009; Herman et al., 2013; Li et al., 2013; Nossent et al., 2011; Rakovec et al., 2014; Rosero et al., 2010; Rosolem et al., 2012; Tang et al., 2007; van Werkhoven et al., 2008). [However, recent analyses have considered other input factors and sources of uncertainty](#) (e.g., Baroni and Tarantola, 2014; Schoups and Hopmans, 2006). Here, we extend the sensitivity analysis framework to forcing uncertainty by creating k new parameters ($\phi_1, \phi_2, \dots, \phi_k$) that specify forcing uncertainty characteristics (Vrugt et al., 2008b) [and reformulate equation 1 as:](#)

$$\mathbf{Y} = M(\mathbf{F}, \boldsymbol{\theta}, \boldsymbol{\phi}) \quad (2)$$

384 By fixing the original model parameters (Table 2), we focus solely on the influence of forcing
 385 errors on model output (Y). Note it is possible to consider uncertainty in both forcings and
 386 parameters in this framework.

387

388 3.3.2. Sobol' sensitivity analysis

389 Sobol' sensitivity analysis uses variance decomposition to attribute output variance to input
 390 [uncertainty](#). First-order and higher-order sensitivities can be resolved; here, only the total-order
 391 sensitivities [were](#) examined (see below) [for clarity and because the resulting first-order](#)
 392 [sensitivity indices were typically comparable to the total-order sensitivity indices \(e.g., 83% of](#)
 393 [all cases had total-order and first-order indices within 10% of each other\), suggesting minimal](#)
 394 [error interactions](#). The Sobol' method is advantageous in that it is model independent, can
 395 handle non-linear systems, and is among the most robust sensitivity methods (Saltelli and
 396 Annoni, 2010; Saltelli, 1999). The primary limitation of Sobol' is that it is computationally
 397 intensive, requiring a large number of samples to account for variance across the full parameter
 398 space. [A key assumption to the Sobol' approach used in this paper \(see Sec. 3.3.3\) is that the](#)
 399 [factors are independent; hence, our analysis does not consider cases of correlated errors \(e.g., a](#)
 400 [positive measurement bias in \$T_{\text{air}}\$ that causes a negative \$RH\$ bias\). Frameworks have been](#)
 401 [proposed for the case of correlated factors \(e.g., forcing errors\) in a sensitivity analysis \(e.g.,](#)
 402 [Kucherenko et al., 2012\), but we leave those applications for future work. Below, we provide a](#)
 403 [brief summary of the Sobol' sensitivity analysis methodology implemented here but note that](#)
 404 [further details can be found in](#) Saltelli et al. (2010).

405

406 3.3.3. Sensitivity indices and sampling

407 Within the Sobol' global sensitivity analysis framework, the total-order sensitivity index (S_{Ti})
 408 describes the variance in model outputs (Y) due to a specific [forcing error](#) (ϕ_i), including both
 409 unique (i.e., first-order) effects and all interactions with all other parameters:

$$410 \quad S_{Ti} = \frac{E[V(Y | \phi_{-i})]}{V(Y)} = 1 - \frac{V[E(Y | \phi_{-i})]}{V(Y)} \quad (3)$$

411 where E is the expectation (i.e., average) operator, V is the variance operator, and ϕ_{-i} signifies all
 412 parameters except ϕ_i . The latter expression defines S_{Ti} as the variance remaining in Y after
 413 accounting for variance due to all other parameters (ϕ_{-i}). S_{Ti} values have a range of [0, 1].
 414 Interpretation of S_{Ti} values was straightforward because they explicitly quantified the variance
 415 introduced to model output by each parameter (i.e., forcing errors). As an example, an S_{Ti} value
 416 of 0.7 for bias parameter ϕ_i on output Y_j indicates 70% of the output variance was due to bias in
 417 forcing i (including unique effects and interactions).

418

419 A number of numerical methods are available for evaluating sensitivity indices, [and most adopt a](#)
 420 [Monte-Carlo approach](#) (Saltelli et al., 2010). Evaluation of Eq. (3) requires two sampling
 421 matrices, which we refer to as matrices \mathbf{A} and \mathbf{B} (Fig. 2a). To construct \mathbf{A} and \mathbf{B} , we first
 422 specified the number of samples (N) in the parameter space and the number of parameters (k),
 423 depending on the error scenario (Table 3). Selecting [input factor samples](#) for these two matrices
 424 was achieved using the quasi-random Sobol' sequence (Saltelli and Annoni, 2010). The
 425 sequence [can be approximated as](#) a uniform distribution in the range [0, 1]. Figure 2a shows
 426 [input factor samples from](#) an example Sobol' sequence in two dimensions. For each scenario
 427 and site, we generated a ($N \times 2k$) Sobol' sequence matrix with quasi-random numbers in the [0,
 428 1] range, and then divided it in two parts such that matrices \mathbf{A} and \mathbf{B} were each distinct ($N \times k$)
 429 matrices. Calculation of S_{Ti} required perturbing [factors](#); therefore, a third Sobol' matrix (\mathbf{A}_B) was
 430 constructed from \mathbf{A} and \mathbf{B} . In matrix \mathbf{A}_B , all columns were from \mathbf{A} , except the i th column, which
 431 was from the i th column of \mathbf{B} , resulting in a ($kN \times k$) matrix (Fig. 2a). Sec. 3.3.5 provides
 432 specific examples of this implementation. From Eq. (3), we compute S_{Ti} as (Jansen, 1999;
 433 Saltelli et al., 2010):

$$434 \quad S_{Ti} = \frac{\frac{1}{2N} \sum_{j=1}^N (f(\mathbf{A})_j - f(\mathbf{A}_B^{(i)})_j)^2}{V(Y)} \quad (4)$$

435 where $f(\mathbf{A})$ is the model output evaluated on the \mathbf{A} matrix, $f(\mathbf{A}_B^{(i)})$ is the model output evaluated
 436 on the \mathbf{A}_B matrix where the i th column is from the \mathbf{B} matrix, and i designates the parameter of
 437 interest. Evaluation of S_{Ti} required $N(k+2)$ simulations at each site and scenario.

438

439 **3.3.4. Bootstrapping of sensitivity indices**

440 To test the reliability of S_{Ti} , we used bootstrapping with replacement across the $N(k+2)$ outputs,
441 similar to Nossent et al. (2011). The mean and 95% confidence interval were calculated using
442 the Archer et al. (1997) percentile method and 10 000 samples. For all cases, final S_{Ti} values
443 [\(i.e., computed sensitivity indices with all samples considered\)](#) were close to the mean
444 bootstrapped values [\(i.e., 99% had a difference less than 0.001 and no difference was greater](#)
445 [than 0.003\)](#), suggesting convergence. Thus, we report only the mean and 95% confidence
446 intervals of the bootstrapped S_{Ti} values.

447

448 **3.3.5. Workflow and error introduction**

449 Figure 2 shows the workflow for creating the Sobol' A , B , and A_B matrices, [mapping input factor](#)
450 [samples](#) to errors, applying errors to the original forcing data, executing the model and saving
451 outputs, and calculating S_{Ti} values. The workflow was repeated at all sites and scenarios. Each
452 step is described in more detail below:

453

454 Step 1) Generate an initial ($N \times 2k$) Sobol' matrix (with N and k values for each scenario, Table
455 3), separate into A and B , and construct A_B (Fig. 2a). NB+RE had $k=12$ (six bias and six random
456 error parameters). All other scenarios had $k=6$ (all bias parameters).

457

458 Step 2) In each simulation, map the [input factor sample](#) of each forcing error parameter (ϕ) to the
459 specified error distribution and range (Fig. 2b, Table 3). [Here we treat the input factor samples](#)
460 [as quantiles, which allows us to map these to errors via different probability distributions. For a](#)
461 [uniform distribution, the quantile value scales linearly between the specified lower and upper](#)
462 [error ranges \(Fig. 2b\). This linear scaling is not possible for normal \(or lognormal\) distributions](#)
463 [\(due to differences in distribution shape\) and we therefore map the quantile values to normal \(or](#)
464 [lognormal\) distributions scaled within the specified range. We begin by generating a probability](#)
465 [distribution of random numbers with specified mean=0 and standard deviation of 1 for the case](#)
466 [of a normal distribution, and with specified mean=20 and standard deviation of 0.5 for the case](#)
467 [of a lognormal distribution. The random numbers of the distribution are normalized in the \[0, 1\]](#)

468 [range by subtracting the minimum value and dividing by the maximum value, and then quantiles](#)
 469 [of these normalized values are computed. The final step of the mapping is to multiply the](#)
 470 [normalized quantile by the specified range of uncertainty and adding the lower bound value.](#) For
 471 example, a Q_{si} bias parameter of $\phi=0.75$ (quantile value) in the $[-100 \text{ W m}^{-2}, +100 \text{ W m}^{-2}]$ range
 472 would map to a Q_{si} bias of $+50 \text{ W m}^{-2}$ [when assuming a uniform probability distribution but only](#)
 473 [+14 \$\text{W m}^{-2}\$ when assuming a normal distribution.](#) For context, a bias parameter of $+50 \text{ W m}^{-2}$ or
 474 [higher has about a 25% probability of occurring in the uniform distribution but only 2% in the](#)
 475 [normal distribution.](#)

476

477 Step 3) In each simulation, perturb (i.e., introduce artificial errors) the observed time series of the
 478 i th forcing (F_i) with bias (all scenarios), or both bias and random errors (NB+RE only) (Fig. 2c):

$$479 \quad F'_i = F_i \phi_{B,i} b_i + (F_i + \phi_{B,i})(1 - b_i) + \phi_{RE,i} R c_i \quad (5)$$

480 where F'_i is the perturbed forcing time series, $\phi_{B,i}$ is the bias parameter for forcing i , b_i is a binary
 481 switch indicating multiplicative bias ($b_i=1$) or additive bias ($b_i=0$), $\phi_{RE,i}$ is the random error
 482 parameter for forcing i , R is a time series of randomly distributed noise (normal distribution,
 483 mean=0) scaled in the $[-1, 1]$ range, and c_i is a binary switch indicating whether random errors
 484 are introduced ($c_i=1$ in scenario NB+RE and $c_i=0$ in all other scenarios). For T_{air} , U , RH , Q_{si} , and
 485 Q_{li} , $b_i=0$; for P , $b_i=1$. [The decision to treat biases as multiplicative for \$P\$ but additive for all](#)
 486 [other forcings was made based on practical considerations \(e.g., multiplicative bias in \$T_{air}\$ are](#)
 487 [difficult to interpret\) and on convention of past studies that report forcing errors. However, we](#)
 488 [note this is somewhat subjective, as errors in some forcings \(e.g. radiation\) have been reported in](#)
 489 [both conventions.](#) For P , U , and Q_{si} , we restricted random errors to periods with positive values.
 490 [Similar to other sensitivity analyses \(e.g., Baroni and Tarantola, 2014\), we checked \$F'_i\$ for non-](#)
 491 [physical values \(e.g., negative \$Q_{si}\$ \) and set these to physical limits. This was most common when](#)
 492 [perturbing \$U\$, \$RH\$, and \$Q_{si}\$; negative values of perturbed \$P\$ only occurred when random errors](#)
 493 [were considered \(Eq. 5\). Due to this resetting of non-physical errors, the error distribution was](#)
 494 [truncated \(i.e., it was not always possible to impose extreme errors\). Additional tests \(not](#)
 495 [shown\) suggested that distribution truncation changed sensitivity indices minimally \(i.e., \$<5\%\$ \),](#)
 496 [and thus we assumed this truncation](#) did not alter the relative ranking of forcing errors.

497

498 Step 4) Input the $N(k+2)$ perturbed forcing datasets into UEB (Fig. 2d). At each site, NB+RE
499 required 140 000 simulations, whereas the other [four](#) scenarios each required 80 000 simulations,
500 for a total of [1 840 000](#) simulations in the analysis. The doubling of k in NB+RE did not result
501 in twice as many simulations because the number of simulations scaled as $N(k+2)$.

502

503 Step 5) Save the model outputs for each simulation (Fig. 2e). [The outputs included daily time](#)
504 [series of SWE, and four summary outputs including peak SWE, mean ablation rate, snow](#)
505 [disappearance date, and total snow sublimation.](#)

506

507 Step 6) Calculate S_{Ti} for each forcing error parameter and model output (Fig. 2f) based on Sect.
508 3.3.3-3.3.4. Prior to calculating S_{Ti} , we screened the model outputs for cases where UEB
509 simulated too little or too much snow (which can occur with perturbed forcings); [this was an](#)
510 [essential step to ensure meaningful results.](#) [Other studies](#) (e.g., Pappenberger et al., 2008) [have](#)
511 [also applied screening methods to model output prior to calculating sensitivity indices.](#) For a
512 valid simulation, we required a minimum peak SWE of 50 mm, a minimum continuous snow
513 duration of 15 days, and identifiable snow disappearance. We rejected samples that did not meet
514 these criteria to avoid meaningless or undefined metrics (e.g., peak SWE in ephemeral snow or
515 snow disappearance for a simulation that did not melt out). The number of rejected samples
516 varied with site and scenario (Table 4). On average, [94%](#) passed the requirements. All cases had
517 at least 86% satisfactory samples, except in UB at SASP, where only ~34% met the
518 requirements. [In this case, the most common reason for rejecting a simulation was that too much](#)
519 [snow was simulated, such that it never disappeared by the end of the model run. The rejected](#)
520 [runs were characterized by high \(positive\) precipitation biases and low \(negative\) biases in \$T_{air}\$,](#)
521 [and \$Q_{sj}\$ and \$Q_{lj}\$.](#) Despite this attrition, S_{Ti} values still converged in all cases.

522

523 4. Results

524 4.1. [Propagation of forcing uncertainty](#) to model outputs

525 Figure 3 shows density plots of daily SWE from UEB at the four sites and [five](#) forcing error
526 scenarios (Fig. 1, Table 3), while Fig. 4 summarizes the model outputs. As a reminder, NB
527 assumed normal (or lognormal) biases at field level uncertainty. The other scenarios were the
528 same as NB, except NB+RE considered both biases and random errors, UB considered uniform
529 distributions, [NB_gauge considered gauge undercatch biases in precipitation](#), and NB_lab
530 considered lower error magnitudes [in all forcings](#) (i.e., laboratory level uncertainty).

531
532 Large uncertainties in SWE were evident, particularly in NB, NB+RE, and UB (Fig 3.a-l). The
533 large range in modeled SWE within these three scenarios often translated to large ranges in mean
534 ablation rates (Fig 4.e-h), snow disappearance dates (Fig 4.i-l) and total sublimation (Fig 4.m-p).
535 In contrast, SWE and output [uncertainties](#) in [NB_gauge and NB_lab](#) [were](#) comparatively small
536 (Fig. 3m-t and Fig. 4). [Model output ranges were generally larger in NB_gauge than NB_lab.](#)
537 The envelope of SWE simulations in NB_lab [more tightly](#) encompassed observed SWE at all
538 sites, except during early winter at IC (Fig. 3m), which was possibly due to initial *P* data quality
539 and redistribution of snow to the snow pillow site.

540
541 NB and NB+RE generally yielded similar SWE density plots (Fig. 3a-h), but NB+RE yielded a
542 [slightly](#) higher frequency of extreme SWE simulations. NB and NB+RE also had very similar
543 (but not equivalent) mean outputs values and ensemble spreads at all sites except IC (Fig. 4).
544 This initial observation suggested that random errors [in the forcings had minimal impact on](#)
545 [model behavior](#) at CDP, RME, and SASP. [NB+RE and NB model outputs were slightly](#)
546 [different at IC \(particularly for the ablation rates\), indicating that random errors had some](#)
547 [influence there, and this was possibly due to](#) the low snow accumulation ([~200 mm peak SWE](#)
548 [observed](#)) at that site and brief snowmelt season (less than 10 days [in the observations](#)).

549
550 NB and UB yielded generally very different model outputs (Fig. 3 and Fig. 4). The only
551 difference in these two scenarios was the assumption regarding error distribution (Table 3).
552 Uniformly distributed forcing biases (scenario UB) yielded a [relatively](#) uniform ensemble of
553 SWE simulations (Fig. 3i-l), larger mean values of peak SWE and ablation rates, and later snow

554 disappearance, as well as larger uncertainty ranges in all outputs. At some sites, UB also had a
555 higher frequency of simulations where seasonal sublimation was negative (i.e., condensation).

556

557 Contrasting NB and NB_gauge, NB_gauge had a lower uncertainty range in SWE and slightly
558 higher mean peak SWE at all sites (Fig. 3 and Fig. 4). With the exception of RME, the ranges in
559 ablation rates in NB_gauge were at least 50% smaller than in NB (Fig. 4 e-h). Snow
560 disappearance ranges were marginally smaller in NB_gauge relative to NB (Fig. 4i-l). Finally,
561 sublimation ranges were very similar between NB and NB_gauge (Fig. 4m-p).

562

563 Relative to NB, NB_lab had smaller uncertainty ranges in all model outputs (Fig. 3 and Fig. 4),
564 an expected result given the lower magnitudes in forcing errors in NB_lab (Table 3). Likewise,
565 NB_lab SWE simulations were generally less biased than NB, relative to observations (Fig. 3).
566 NB_lab generally had higher mean peak SWE and ablation rates, and later mean snow
567 disappearance timing than NB (Fig 4).

568

569 **4.2. Model sensitivity to forcing error characteristics**

570 Total-order sensitivity indices (S_{Ti}) were calculated for four summary variables of model output
571 (peak SWE, mean ablation rates, snow disappearance dates, and total sublimation) and for daily
572 SWE output at all sites and error scenarios. Examination of the total-order indices with sample
573 size indicated that most indices stabilized after evaluating the model at 3 000 to 5 000 samples
574 (no figures shown). Below we sequentially compare sensitivity indices from different scenarios
575 to scenario NB to test the impact of differences in error characteristics (type, probability
576 distribution, and magnitudes).

577

578 **4.2.1. Impact of error types**

579 We first focus on sensitivity to forcing bias, as this error type was common to scenarios NB and
580 NB+RE. Figure 5 shows the computed total-order sensitivity indices from the two scenarios
581 (with sensitivities to biases and random errors shown separately in NB+RE). Both NB and

582 [NB+RE](#) showed that UEB peak SWE was most sensitive to P bias at all sites (Fig.5a-d). [In both](#)
583 [scenarios](#), P bias was also the most important factor for ablation rates and snow disappearance at
584 all sites (Fig. 5e-l). For ablation rates in NB, T_{air} bias was the next most important factor [\(after \$P\$](#)
585 [bias\)](#) at CDP, while biases in Q_{si} and Q_{li} were secondarily important at RME (Fig.5f-g). [For](#)
586 [ablation rates at IC in NB+RE, most types of errors had some baseline influence \(i.e., \$S_{T_i} > 0.5\$ \) on](#)
587 [model sensitivity \(Fig. 5e\). In both NB and NB+RE, biases in the radiation terms were of](#)
588 [secondary importance to snow disappearance timing \(Fig. 5i-k\). In contrast to the other three](#)
589 [model outputs](#), sublimation in NB and NB+RE was insensitive to P bias and the most important
590 [factors varied somewhat between sites and scenarios \(Fig. 5m-p\). In both scenarios, sublimation](#)
591 [was most sensitive to \$RH\$ bias at IC and \$U\$ bias at SASP. At CDP and RME, sublimation was](#)
592 [most sensitive to \$RH\$ bias in NB; however, in NB+RE, sublimation was most sensitive to \$Q_{li}\$ bias](#)
593 [at CDP and to \$T_{air}\$ bias at RME \(Fig. 5n-o\). In both scenarios, biases in \$T_{air}\$, \$Q_{si}\$, or \$Q_{li}\$ were](#)
594 [generally of secondary importance for sublimation.](#)

595

596 [We hypothesized that the snow model outputs would have higher sensitivity to biases than to](#)
597 [random errors in the forcings. The results of our analysis generally supported this hypothesis.](#)
598 [Across all outputs and sites, \$S_{T_i}\$ values for random errors were always less than or comparable to](#)
599 [the smallest \$S_{T_i}\$ bias values, and the most important factor was always a bias term \(Figure 5\).](#)
600 [Furthermore, there was typically high correspondence between NB and NB+RE \(bias terms](#)
601 [only\) in terms of identifying the most important forcing error \(e.g., \$P\$ bias in peak SWE and](#)
602 [ablation rates at all sites, Fig. 5a-h\). The main exceptions were snow disappearance at IC \(Fig.](#)
603 [5i\), and sublimation at CDP and RME \(Fig. 5n-o\), where the two scenarios identified different](#)
604 [errors as the most important factor. However, even in these exceptional cases, the two scenarios](#)
605 [yielded similar groupings of more important vs. least important errors. For example, biases in](#)
606 [\$T_{air}\$ and \$RH\$ were important to sublimation at RME in both scenarios \(Fig. 5o\), though they](#)
607 [distinguished these sensitivities differently \(i.e., NB found \$RH\$ bias was more important whereas](#)
608 [NB+RE found \$T_{air}\$ bias was more important\).](#)

609

610 [While there was general correspondence between NB and NB+RE \(bias terms\), sensitivity](#)
611 [indices were not identical across cases, due to interactions between biases and random errors in](#)

612 NB+RE. Random errors changed model sensitivity to biases, and the change in sensitivity was
613 more notable (i.e., absolute change exceeding 0.10) for ablation rates and snow disappearance at
614 IC (Fig. 5e,i) and sublimation at all sites (Fig. 5m-p). Random errors amplified model sensitivity
615 to biases in some cases (e.g., U bias in all sublimation scenarios) but diminished model
616 sensitivity to biases in other cases (e.g., RH bias in all sublimation scenarios). Because
617 consideration of second-order sensitivity indices was beyond the scope of the study, we were
618 unable to determine which specific interactions were important in terms of error types, and leave
619 this topic for future work.

620

621 **4.2.2. Impact of probability distribution of errors**

622 We hypothesized that the assumed probability distribution of errors would alter the relative
623 hierarchy of forcing biases. However, the results did not consistently support this hypothesis
624 (Fig. 6). In all cases, scenarios NB and UB identified the same factor as the most important and
625 similar factors as the least important at all sites. Specifically, P bias was most important for peak
626 SWE, ablation rates, and snow disappearance at all sites in both scenarios (Fig. 6a-l). The only
627 exception was in scenario UB at IC, where ablation rates had similar sensitivity to P bias and U
628 bias. In both scenarios, T_{air} bias was the second most important factor for peak SWE and
629 ablation rates at the warmest site, CDP. Both scenarios showed that RH bias was the least
630 important factor to snow disappearance at all four sites (Fig. 6i-l). Finally, both NB and UB
631 showed that P bias was least important for sublimation (in contrast to the other model outputs)
632 and that RH and U biases were among the most sensitive factors for sublimation (Fig. 6m-p).
633 More specifically, sublimation was most sensitive to RH bias at IC, CDP, and RME, and U bias
634 as SASP (Fig. 6m-p).

635

636 For a few specific forcings and outputs, the selected probability distribution played a role in
637 model sensitivity to that type of forcing bias. For example, assumption of a uniform probability
638 distribution (UB) for forcing errors enhanced the sensitivity of sublimation to U and RH biases
639 but reduced sublimation sensitivity to Q_{si} and Q_{li} biases at all sites (Fig. 6m-p). In contrast,
640 assuming a normal distribution (NB) of biases yielded the opposite results. Additionally,

641 modeled ablation rates at IC were notably more sensitive to forcing biases (precipitation
642 excluded) in scenario UB than in NB.

643

644 **4.2.3. Impact of error magnitude**

645 We hypothesized that the relative magnitude of forcing errors would exert a strong control on
646 model sensitivity. Comparing NB to NB_gauge and to NB_lab generally supported this
647 hypothesis (Fig. 7). The contrast in S_{T_j} values between scenarios NB, NB_gauge, and NB_lab
648 implied that the specified ranges of forcing errors was a critical determinant of model sensitivity.

649

650 While P bias was the most important factor at all sites in NB for peak SWE, ablation rates, and
651 snow disappearance, P bias was never the most important factor for these model outputs in
652 NB_gauge, and in many cases was among the least important errors (Fig. 7a-l). In NB_gauge,
653 peak SWE was most sensitive to RH bias at IC, T_{air} bias at CDP and RME, and Q_{li} bias at SASP
654 (Fig. 7a-d). Ablation rates in NB_gauge were most sensitive to T_{air} bias at CDP and to Q_{li} bias at
655 IC, RME, and SASP (Fig. 7e-h). Snow disappearance was also most sensitive to Q_{li} bias at all
656 four sites in NB_gauge (Fig. 7i-l). However, for sublimation at all sites, NB and NB_gauge
657 yielded very similar sensitivities to forcing biases (Fig. 7m-p). Specifically, in both NB and
658 NB_gauge, modeled sublimation was most sensitive to RH bias at IC, CDP, and RME and to U
659 bias at SASP (Fig. 7m-p). The similarity in sublimation sensitivity indices between NB and
660 NB_gauge emerged because these scenarios only differed in terms of P uncertainty (Table 3) and
661 because P bias was not important to modeled sublimation. The contrast between sensitivity
662 indices in these two scenarios and for these four outputs illustrated that model sensitivity may
663 depend on both the magnitudes of uncertainty for specific forcings and on the output of interest.

664

665 Whereas NB_gauge demonstrated that reducing the magnitude of forcing uncertainty in one
666 factor (i.e., precipitation) was sufficient to change which factors were most and least important,
667 NB_lab showed that changing the magnitude of forcing uncertainty in all terms could yield a
668 substantially different pattern of model sensitivity (Fig. 7). As a primary example, scenarios NB
669 and NB_lab did not agree whether P bias or Q_{li} bias was the most important factor for peak

670 SWE, ablation rates, and snow disappearance dates at all four sites (Fig. 7a-l). For sublimation,
671 NB_lab sensitivity indices indicated that Q_{li} bias was most important, whereas RH bias (IC,
672 CDP, and RME) and U bias (SASP) were most important in NB (Fig. 7m-p). Across all sites
673 and outputs in NB_lab, Q_{li} bias was consistently the most important factor (Fig. 7). In one sense,
674 this was surprising, given that the bias magnitudes were lower for Q_{li} than for Q_{si} (Table 3).
675 However, the albedo of snow minimizes the amount of energy transmitted to the snowpack from
676 Q_{si} , thereby rendering Q_{si} errors less important than Q_{li} errors. Additionally, the non-linear
677 nature of the model may enhance the role of Q_{li} through interactions with other factors. The
678 general lack of importance in P bias in NB_lab (main exception was peak SWE at IC, Fig. 7a)
679 was due to the discrepancy between the laboratory specified accuracy for P gauges and typical
680 errors encountered in the field.

681

682 **4.2.4. Relative controls of forcing error characteristics on SWE sensitivity**

683 The above results sequentially compared sensitivity indices from different error scenarios to NB
684 in order to ascertain how different assumptions regarding error types, distributions, and
685 magnitudes translated to changes in model sensitivity. To summarize the relative controls of
686 these three forcing error characteristics on model sensitivity, we calculated daily sensitivity
687 indices of modeled SWE to forcing biases at each site and scenario (Fig. 8). This final analysis
688 was conceptually different than the previous analyses (Fig 5-7) in terms of the model output
689 considered. Whereas the previous analyses computed sensitivity indices for summative model
690 outputs (e.g., peak SWE, total sublimation), the final analysis re-calculated sensitivity indices for
691 SWE each day. This approach allowed us to examine how SWE model sensitivity changed as a
692 function of time within the snow season.

693

694 Comparing the broad patterns in the time varying S_{Ti} values across the five scenarios, it was
695 evident that error magnitudes were the greatest determinant in model sensitivity to forcing errors
696 through the snow season (compare Fig. 8a-l with Fig. 8m-t). NB, NB+RE, and UB exhibited
697 similar patterns, with high S_{Ti} in P bias throughout the year and with the other forcing biases
698 yielding low S_{Ti} values in the winter and increasing S_{Ti} values in the spring and early summer for
699 some forcings (Fig. 8a-l). In contrast, NB_gauge and NB_lab (Fig. 8m-t) had lower S_{Ti} values

700 for P bias, and more coherent changes in S_{Ti} values that were more synchronized with the
701 specific part of the snow season.

702
703 After error magnitudes, the next most important determinant to model sensitivity was the
704 probabilistic distribution of forcing errors (compare Fig. 8a-d and Fig. 8i-l). Relative to NB, UB
705 tended to yield lower S_{Ti} values for P bias. UB also had higher S_{Ti} values for biases in T_{air} , Q_{li} ,
706 and Q_{si} as time progressed at IC, CDP, and RME (Fig. 8i-k). Finally, the addition of random
707 errors was least important to model sensitivity, as the evolution of S_{Ti} bias values was very
708 similar between NB and NB+RE at most sites (compare Fig. 8a-d and Fig. 8e-h). Random errors
709 mattered the most to modeled SWE at IC, but random errors only changed S_{Ti} values (on
710 average) by less than 10%.

711

712 **5. Discussion**

713 Here we examined the sensitivity of physically-based snow simulations to forcing error
714 characteristics (i.e., types, probability distributions, and magnitudes) using Sobol' global
715 sensitivity analysis. A key result is that among these three characteristics, the magnitude of
716 biases had the most significant impact on UEB simulations (Figs. 3-4) and on model sensitivity
717 (Figs. 7-8). The assumed probability distribution of biases was important in that it increased the
718 range of model outputs (compare NB and UB in Fig. 4), but surprisingly, this usually translated
719 to only modest changes in model sensitivity to forcing errors (Figs. 6 and 8). Random errors
720 were usually less important than biases. Although random errors changed model sensitivity to
721 biases through error interactions, this effect was only large in specific conditions (e.g., ablation
722 rates at IC, Fig. 5e), and the snow model was never more sensitive to random errors than to
723 biases (Fig. 5). Below we discuss these three error characteristics (in order of importance, as
724 suggested by the results), place forcing errors in the context of structural uncertainty, and
725 identify limitations of the analysis and future research directions.

726

727 **5.1. Ranges of error magnitudes**

728 [The results supported our hypothesis that the magnitude of biases strongly influences the relative](#)
729 [importance of forcing errors. The three magnitudes of uncertainty considered \(NB, NB_gauge,](#)
730 [and NB_lab\) all resulted in different patterns in model sensitivity to forcing biases, and these](#)
731 [patterns also varied with the output of interest \(Fig. 7\). Modeled peak SWE, ablation rates, and](#)
732 [snow disappearance were consistently sensitive to \$P\$ bias in scenario NB and to \$Q_{li}\$ bias in](#)
733 [scenario NB_lab, but there was less consistency in the dominant forcing errors across these three](#)
734 [outputs in scenario NB_gauge.](#) While peak SWE, ablation rates, and snow disappearance dates
735 had similar sensitivities to forcing errors (particularly to P biases), sublimation exhibited notably
736 different sensitivity to forcing errors. P bias was frequently the least important factor for
737 sublimation, in contrast to the other model outputs. Biases in RH , U , and T_{air} were often the
738 major controls on modeled sublimation in NB, NB+RE, UB, and NB_gauge, while Q_{li} bias
739 controlled modeled sublimation in NB_lab. These [field](#) results partially agree with the
740 sensitivity analysis of Lapp et al. (2005), who showed the most important forcings for
741 sublimation in the Canadian Rockies were U and Q_{si} . [However, they did not consider \$Q_{li}\$ in their](#)
742 [sensitivity analysis and so the experiments are not exactly comparable.](#) These results suggest
743 that no single forcing is important across all modeled variables, and model sensitivity strongly
744 depends on the output of interest.

745

746 [The dominant effect of \$P\$ bias on modeled peak SWE, ablation rates, and snow disappearance in](#)
747 [the field scenarios \(e.g., NB\) confirmed previous reports that \$P\$ uncertainty is a major control on](#)
748 [snowpack dynamics \(Durand and Margulis, 2008; He et al., 2011b; Schmucki et al., 2014\). It](#)
749 [was surprising that \$P\$ bias was often the most critical forcing error for ablation rates in these](#)
750 [scenarios \(Fig. 5-6\). Prior investigations into the relative importance of forcings to ablation were](#)
751 [typically framed for a snowpack at the end of winter, such that \$P\$ uncertainty was not considered](#)
752 [\(e.g., Zuzel and Cox, 1975\). The results here showed that ablation rates were highly sensitive to](#)
753 [\$P\$ bias and this is likely](#) because it controlled the timing and length of the ablation season.
754 Positive P bias extends the fraction of the ablation season in the warmest summer months when
755 ablation rates and radiative energy approach maximum values, [whereas negative \$P\$ bias truncates](#)
756 [the fraction of ablation in the warm season.](#) Trujillo and Molotch (2014) reported a similar result
757 based on SNOTEL observations.

758
759 The contrast between scenarios NB, NB_gauge, and NB_lab highlights that selection of the error
760 ranges is a critical step in sensitivity analysis. However, we recognize that there is some
761 subjectivity in the specification of these ranges. Quantification of errors in forcing estimation
762 methods is best achieved through comparisons with surface observations (e.g., Bohn et al., 2013;
763 Flerchinger et al., 2009), but it remains challenging to specify error ranges with confidence
764 (Song et al., 2015). Key considerations controlling the ranges and impacts of forcing errors
765 include the representativeness of the forcing data (e.g., reanalysis, numerical weather model
766 output, extrapolated surface measurements, etc.) in the study area, the length scale of dominant
767 processes (e.g., snow drifting), and the configuration of the snow model (e.g., spatial scale,
768 complexity). Here we selected ranges in the field scenarios to encompass errors encountered
769 across a variety of possible forcing data sources (Table 3), but ultimately the appropriate ranges
770 must be tailored to the specific application. This supports the need for continual evaluation of
771 forcing datasets across a variety of climates and environmental conditions.

772

773 **5.2. Probability distribution of errors**

774 The results did not universally support our hypothesis that the assumed probability distribution
775 of biases was important to the relative ranking of forcing errors. The relative consistency in the
776 dominant forcing errors between NB and UB may have emerged because the probability
777 distributions of all six forcing biases varied together between these two scenarios (i.e., all forcing
778 biases were uniform in UB and either normal or lognormal in NB). While we did not conduct
779 additional tests, we suspect that changing the probability distribution of just a single forcing error
780 (e.g., T_{air} bias) from normal to uniform would have uniquely enhanced model sensitivity to that
781 particular forcing error (Touhami et al., 2013).

782

783 The similarity of results between scenarios NB and UB conform to findings in previous studies
784 (e.g., Foscarini et al., 2010; Touhami et al., 2013) where uniform and normal distributions
785 identified similar factors as the most important. These previous studies imply that greater
786 differences in sensitivity indices (as a function of distribution) will emerge when factor

787 interactions are more prominent. The case with the strongest error interactions here (i.e.,
788 ablation rates at IC) also yielded the largest differences in sensitivity indices between scenarios
789 NB and UB, which is consistent with the prevailing logic.

790

791 **5.3. Error types**

792 The results were consistent with our hypothesis that the snow model is more sensitive to biases
793 than to random errors in the forcings. While previous investigations supported this idea for
794 shortwave and longwave forcings in physically based snow models (i.e., Lapo et al., 2015), the
795 current study showed that biases are more important than random errors for all commonly
796 required meteorological forcings (and not just irradiances). The model was more sensitive to
797 biases and less sensitive to random errors due to the systematic nature of biases. In contrast, the
798 effect of random errors tended to cancel out when integrating model outputs over long periods.
799 Our selected model outputs were generally a function of several months of mass and energy
800 exchange in the snowpack, thereby ensuring minimization of effects from random errors.
801 Random errors only had a greater impact on ablation rates at IC (Fig. 5e), and this was because
802 the relatively brief snowmelt period presented an opportunity for the random errors to not cancel
803 out. Hence, the model may have greater sensitivity to random errors for other model outputs not
804 considered here that integrate over relatively short time scales (e.g., snowmelt over a single day).

805

806 **5.4. Contextualizing forcing and structural uncertainties**

807 Our central argument at the onset was that forcing uncertainty may be comparable to parametric
808 and structural uncertainty in snow-affected catchments. To support our argument and to place
809 our results in context, we compare our results at CDP in 2005-2006 to Essery et al. (2013), who
810 assessed the impact of structural uncertainty in a suite of local snowpack processes (i.e., snow
811 compaction, fresh snow density, snow albedo evolution, surface heat and moisture fluxes, snow
812 cover fraction, snow hydrology, and thermal conductivity) on SWE simulations from 1701
813 physically based snow models at the same site/year. Figure 9 compares the 95% uncertainty
814 ranges in peak SWE, ablation rates, and snow disappearance in NB, NB gauge, and NB lab to
815 the ranges found across the 1701 snow models of Essery et al. (2013). From the comparisons at

816 [this site](#), it is clear that the uncertainty [associated with drifting snow \(i.e., scenario NB\)](#)
817 [overwhelms the structural uncertainty in local snowpack processes for all three model outputs.](#)
818 [As discussed previously](#), it could be argued that [the uncertainty due to drifting snow is a](#)
819 [structural issue \(not a forcing issue\) and that this does not represent the uncertainty of sheltered](#)
820 [areas where drifting snow less important. Hence, NB gauge may be a better determinant of the](#)
821 [level of uncertainty that can be attributed unambiguously to errors in forcing data. In that case,](#)
822 [the output uncertainty range due to model forcing is still larger than that due to the structural](#)
823 [uncertainty \(as considered by Essery et al., 2013\) in the cases of peak SWE and snow](#)
824 [disappearance but is smaller for ablation rates \(Fig. 9\). As expected, the case of forcing](#)
825 [uncertainty in NB lab yields the lowest range in model outputs at CDP \(Fig. 9\), though it is](#)
826 [interesting to note that the uncertainty in peak SWE due to structural uncertainty \(90 mm\) is only](#)
827 [marginally larger than that due to the specified instrument accuracy \(60 mm\). These](#)
828 [comparisons illustrate that](#) forcing uncertainty cannot be discounted, and the magnitude of
829 forcing uncertainty is a critical factor in how forcing uncertainty compares to [other sources of](#)
830 [uncertainty \(e.g., structural\). This resonates with the recent work of Magnusson et al. \(2015\)](#)
831 [who found that uncertainty in the P forcing was a greater determinant of model performance than](#)
832 [structural considerations.](#)

833

834 **5.5. Caveats and future research**

835 Limitations of the analysis are [that the impact of forcing error characteristics on model behavior](#)
836 [is evaluated through the lens of a single sensitivity analysis method and a single snow model. It](#)
837 [is possible that alternative sensitivity analysis methods might yield different results than the](#)
838 [Sobol' method, as suggested in previous studies \(e.g., Pappenberger et al., 2008\). Likewise, we](#)
839 [recognize it is possible that](#) different snow models may yield different sensitivities to forcing
840 uncertainty. [As one](#) example, both Koivusalo and Heikinheimo (1999) and Lapo et al. (2015)
841 found UEB (Tarboton and Luce, 1996) and the SNTHERM model (Jordan, 1991) exhibited
842 significant differences in radiative and turbulent heat exchange. [As another example, the role of](#)
843 [U bias on snowpack formation may vary strongly depending on the snow model configuration.](#)
844 [Because of the lack of wind transport in UEB, we lumped snow drift uncertainty into P](#)
845 [uncertainty via a “drift factor” formulation \(Luce et al., 1998\) and this could not account for the](#)

846 [role of wind in snow drift/scour processes \(Mott and Lehning, 2010; Winstral et al., 2013\). This](#)
847 [convention would be unnecessary for a model that explicitly models this process \(e.g., the](#)
848 [SNOWPACK model, Lehning et al., 2006\), and for this type of model we would expect the role](#)
849 [of \$U\$ bias to be enhanced \(relative to UEB\) for outputs such as peak SWE and snow](#)
850 [disappearance timing. While sensitivity may vary with model selection in these examples, there](#)
851 [is also evidence suggesting that similar results may emerge when using different snow models](#)
852 [for a similar type of error scenario. Despite using different models, a somewhat different suite of](#)
853 [forcing variables, and slightly different error ranges, our NB_lab experiment corroborated](#)
854 [independent reports that \$Q_{lj}\$ measurement uncertainty was most important to both modeled snow](#)
855 [disappearance \(Skiles et al., 2012\) and sublimation/latent heat exchange \(Sauter and Obleitner,](#)
856 [2015\). Our analysis demonstrated this result was consistent across four snow climates and this](#)
857 [result was apparent in four different model outputs \(Fig. 7\). The implication here is that more](#)
858 [work is needed to better understand how different snow models respond to forcing uncertainty.](#)

859

860 [Generalizing the relationship between model sensitivity and site climate is a research topic of](#)
861 [high interest. Although we found similarities in model sensitivity to specific forcing errors](#)
862 [across sites \(e.g., high sensitivity to \$P\$ bias in peak SWE, ablation rates, and snow disappearance](#)
863 [in NB, NB+RE, and UB, Fig. 8a-l\), we note that the sites exhibited some differences in](#)
864 [sensitivity when \$P\$ uncertainty was reduced to gauge levels \(Fig. 8m-p\). Additionally, the sites](#)
865 [exhibited differences in the relative importance of secondary forcing errors \(Fig. 6-7\). There](#)
866 [may be interesting linkages between climate and model sensitivity, but we were unable to](#)
867 [generalize relationships between site geo-characteristics and sensitivity indices because of the](#)
868 [relatively low number of sites represented here \(n=4 sites, 1 year each\) and the confounding](#)
869 [number of differences between sites. A much larger population of snow measurement sites is](#)
870 [required in order to test relationships between sensitivity indices and site characteristics, and this](#)
871 [is an important avenue of future research. A successful example of relating climate](#)
872 [characteristics to sensitivity indices when many study sites and years are available can be found](#)
873 [in van Werkhoven et al. \(2008\).](#)

874

875 [While](#) the Sobol' method is often considered the "baseline" method in global sensitivity analysis,
876 we note [the limitation is](#) that it comes at a relatively high computation cost (1 [840](#) 000
877 simulations [across](#) four sites [and five](#) error scenarios) and [it](#) may be prohibitive for many
878 modeling applications ([e.g., for models of higher complexity and dimensionality](#)). [For context,](#)
879 [the typical time required for a single simulation was 1.4 seconds, resulting in a total](#)
880 [computational expense of 720 hours \(30 days\) across all scenarios. Examination of the](#)
881 [convergence rates indicated that most sensitivity indices stabilized after one-third of the](#)
882 [simulations completed, and hence the same results could have been found using significantly](#)
883 [fewer simulations \(no figures shown\)](#). Ongoing research is developing new sensitivity analysis
884 methods that compare well to Sobol' but with reduced computational demands (e.g., FAST,
885 Cukier, 1973; method of Morris, 1991; DELSA, Rakovec et al., 2014), [and is comparing how](#)
886 [different methods classify sensitive factors differently](#) (Pappenberger et al., 2008; Tang et al.,
887 2007). We expect that detailed sensitivity analyses that concurrently consider uncertainty in
888 forcings, parameters, and structure in a hydrologic model will be more feasible in the future with
889 better computing resources and advances in sensitivity analysis methods.

890

891 The question remains: "what can be done about forcing errors in hydrologic modeling?" First,
892 the results suggest model-based hypothesis testing must account for uncertainties in forcing data.
893 The results also [highlight](#) the need for continued research in constraining P uncertainty in snow-
894 affected catchments. [Progress is being](#) achieved [with](#) advanced pathways for quantifying
895 snowfall precipitation, such as NWP models (Rasmussen et al., 2011, 2014) [and through](#)
896 [systematic intercomparisons of precipitation and snow gauges \(e.g., Solid Precipitation](#)
897 [Intercomparison Experiment, <http://www.rap.ucar.edu/projects/SPICE/>\)](#). However, in a broader
898 sense, the hydrologic community should [also](#) consider whether deterministic forcings (i.e., single
899 time series for each forcing) are a reasonable practice for physically-based models, given the
900 large uncertainties in both future (e.g., climate change) and historical data (especially in poorly
901 monitored catchments) and the complexities of hydrologic systems (Gupta et al., 2008). We
902 suggest that probabilistic model forcings (e.g., Clark and Slater, 2006), [which have a legacy in](#)
903 [data assimilation methods](#) (e.g., precipitation uncertainty, Durand and Margulis, 2007), present
904 one potential path forward where measures of forcing uncertainty can be explicitly included in
905 the forcing datasets. The challenges are (1) to ensure statistical reliability in our understanding

906 of forcing errors and (2) to assess how best to input probabilistic forcings into current model
907 architectures.

908

909 **6. Conclusions**

910 Application of the Sobol' sensitivity analysis framework across sites in contrasting snow
911 climates reveals that forcing uncertainty can significantly impact model behavior in snow-
912 affected catchments. Model output uncertainty due to forcings can be comparable to or larger
913 than model uncertainty due to model structure. [Furthermore, this work demonstrates that](#)
914 [sensitivity analysis can be applied to understand the role of specific error characteristics in model](#)
915 [behavior.](#) Key considerations in model sensitivity to forcing errors are the magnitudes of forcing
916 errors and the outputs of interest. For the [physically-based snow](#) model tested, random errors in
917 forcings are generally less important than biases, and the [probability](#) distribution of biases is
918 relatively less important [to model sensitivity](#) than the magnitude of biases.

919

920 The analysis shows how forcing uncertainty might be included in a formal sensitivity analysis
921 framework through the introduction of new parameters that specify the characteristics of forcing
922 uncertainty. The framework could be extended to other physically based models and sensitivity
923 analysis methodologies, and could be used to quantify how uncertainties in model forcings and
924 parameters interact. [Based on this framework, it](#) would be interesting to assess the interplay
925 between co-existing uncertainties in forcing errors, model parameters, and model structure, and
926 to test how model sensitivity changes relative to all three sources of uncertainty.

927

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941

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1406

1407 **7. Tables**1408 **Table 1** Basic characteristics of the snow study sites, ordered from left-to-right by increasing elevation.

<u>Site Name</u>	<u>Innavait Creek</u>	<u>Col de Porte</u>	<u>Reynolds Mountain East (sheltered site)</u>	<u>Swamp Angel Study Plot</u>
<u>Site ID</u>	<u>IC</u>	<u>CDP</u>	<u>RME</u>	<u>SASP</u>
<u>Location</u>	<u>Alaska, USA</u>	<u>Rhône-Alpes, France</u>	<u>Idaho, USA</u>	<u>Colorado, USA</u>
<u>Latitude (N)</u>	<u>68.62</u>	<u>45.30</u>	<u>43.07</u>	<u>37.91</u>
<u>Longitude (E)</u>	<u>-149.30</u>	<u>5.77</u>	<u>-116.75</u>	<u>-107.71</u>
<u>Elevation (m)</u>	<u>930</u>	<u>1330</u>	<u>2060</u>	<u>3370</u>
<u>Study Period (WY)</u>	<u>2011</u>	<u>2006</u>	<u>2007</u>	<u>2008</u>
<u>Snow Climate</u>	<u>Tundra</u>	<u>Mountain (maritime)</u>	<u>Mountain (intermountain)</u>	<u>Mountain (continental)</u>
<u>Sensors</u>	<u>T_{air}: Vaisala HMP45C P: Campbell Scientific TE 525 U: Met One 014A RH: Vaisala HMP45C Q_{si}: Kipp & Zonen CMA 6 Q_{lj}: none (taken as residual from measurements of all other radiation components^A)</u>	<u>T_{air}: PT 100/4 wires P: PG2000, GEONOR U: Chauvin Arnoux Tavid 87 – non-heated RH: Vaisala HMP 45D Q_{si}: Kipp & Zonen CM14 Q_{lj}: Eppley PIR</u>	<u>T_{air}: Vaisala HMP 45 P: Belfort Universal Gages U: Met One 013/023 RH: Vaisala HMP 45 Q_{si}: Eppley Precision Spectral Pyranometer Q_{lj}: Eppley PIR</u>	<u>T_{air}: Vaisala CS500 P: ETI Noah II U: RM Young Wind Monitor 05103-5 RH: Vaisala CS500 Q_{si}: Kipp & Zonen CM21 Q_{lj}: Kipp & Zonen CG-4</u>
<u>Operators</u>	<u>NRCS, CRREL, Ameriflux</u>	<u>Météo-France</u>	<u>Northwest Watershed Research Center, Agricultural Research Service</u>	<u>Center for Snow and Avalanche Studies</u>
<u>Oct-Dec T_{air} (°C)</u>	<u>-16.1</u>	<u>2.0</u>	<u>0.2</u>	<u>-3.7</u>
<u>Jan-Mar T_{air} (°C)</u>	<u>-14.7</u>	<u>-1.6</u>	<u>-2.0</u>	<u>-8.7</u>
<u>Apr-Jun T_{air} (°C)</u>	<u>-1.4</u>	<u>8.9</u>	<u>8.4</u>	<u>2.7</u>
<u>Oct-Mar P^B (mm)</u>	<u>200</u>	<u>690</u>	<u>480</u>	<u>1000</u>
<u>Mean annual U (m s⁻¹)</u>	<u>2.2</u>	<u>1.0</u>	<u>1.6</u>	<u>1.1</u>

1409 ^A At IC, Q_{lj} was taken as $Q_{lj} = Q_{net} - (Q_{si} - Q_{so}) + (5.67 \times 10^{-8}) T_{surf}^4$, where Q_{net} is measured net radiation ($W m^{-2}$), Q_{si} is measured incoming shortwave radiation
1410 ($W m^{-2}$), Q_{so} is measured reflected shortwave radiation ($W m^{-2}$), and T_{surf} is measured snow surface temperature (°C).

1411 ^B Note that precipitation data were adjusted with a multiplier (see Section 2) prior to conducting the sensitivity analysis.

1412

1413 **Table 2** UEB model parameters used across all simulations and sites

Description of parameter	Units	Value
Rain threshold temperature	°C	+3.0
Snow threshold temperature	°C	-1.0
Snow emissivity	--	0.99
Bulk snow density	kg m ⁻³	300
Liquid water holding capacity	fraction	0.05
Snow saturated hydraulic conductivity	m hr ⁻¹	20
Visual new snow albedo	--	0.85
Near infrared new snow albedo	--	0.65
New snow threshold depth to reset albedo	m	0.01
Snow surface roughness	m	0.005
Forest canopy fraction	fraction	0
Ground heat flux	W m ⁻²	0

1414 **Table 3** Details of error types, distributions, and uncertainty ranges for the [five](#) scenarios. Bold
 1415 face in the error type, distribution, and uncertainty range indicates defining characteristics,
 1416 relative to scenario NB.

Forcing	Error Type ^A	Distribution ^B	Range	Units	Citations and Notes
Scenario NB (k=6, N=10000)					
T_{air}	B	Normal	[-3.0, +3.0]	°C	Bolstad et al. (1998); Chuanyan et al. (2005); Fridley (2009); Hasenauer et al. (2003)
P	B	Lognormal	[-75, +300] ^C	%	Goodison et al. (1998); Luce et al. (1998); Rasmussen et al. (2012); Winstral and Marks (2002)
U	B	Normal	[-3.0, +3.0]	m s ⁻¹	Winstral et al. (2009)
RH	B	Normal	[-25, +25]	%	Bohn et al. (2013); Déry and Stieglitz (2002); Feld et al. (2013)
Q_{si}	B	Normal	[-100, +100]	W m ⁻²	Bohn et al. (2013); Jepsen et al. (2012); Jing and Cess (1998); Niemelä et al. (2001b)
Q_{li}	B	Normal	[-25, +25]	W m ⁻²	Bohn et al. (2013); Flerchinger et al. (2009); Herrero and Polo (2012); Niemelä et al. (2001a)
Scenario NB+RE (k=12, N=10000)					
This scenario has six bias parameters (identical to NB above), plus the following six random error parameters					
T_{air}	RE	Normal	[0.0, 7.5]	°C	Chuanyan et al. (2005); Fridley (2009); Hasenauer et al. (2003); Huwald et al. (2009); Phillips and Marks (1996)
P	RE	Lognormal	[0.0, 25]	%	Guan et al. (2005); Hasenauer et al. (2003); Hutchinson et al. (2009)
U	RE	Normal	[0.0, 5]	m s ⁻¹	Cheng and Georgakakos (2011); Liston and Elder (2006); Luo et al. (2008); Winstral et al. (2009)
RH	RE	Normal	[0.0, 15]	%	Bohn et al. (2013); Liston and Elder (2006); Phillips and Marks (1996)
Q_{si}	RE	Normal	[0.0, 160]	W m ⁻²	Hasenauer et al. (2003); Jepsen et al. (2012); Liston and Elder (2006); Thornton et al. (2000)
Q_{li}	RE	Normal	[0.0, 80]	W m ⁻²	Bohn et al. (2013); Flerchinger et al. (2009); Liston and Elder (2006)
Scenario UB (k=6, N=10000)					
Identical to NB, except all probability distributions are uniform					
Scenario NB_gauge (k=6, N=10000)					
Identical to NB, except P uncertainty mimics documented differences between P and SWE at SNOTEL sites					
P	B	Lognormal	[-10, +10]	%	Meyer et al. (2012)
Scenario NB_lab^D (k=6, N=10000)					
T_{air}	B	Normal	[-0.30, +0.30]	°C	Vaisala HMP45 specified accuracy
P	B	Lognormal	[-3.0, +3.0]^E	%	RM Young 52202 specified accuracy
U	B	Normal	[-0.30, +0.30]	m s ⁻¹	RM Young 05103 specified accuracy
RH	B	Normal	[-3.0, +3.0]	%	Vaisala HMP45 specified accuracy
Q_{si}	B	Normal	[-25, +25]	W m ⁻²	Li-Cor 200X specified accuracy of ~5%
Q_{li}	B	Normal	[-15, +15]	W m ⁻²	Assumed ~5% of mean intersite values

1417 ^A B=bias, RE=random errors. Biases are additive ($b_i=0$, Eq. 5) for all forcings except P , which has multiplicative
 1418 bias ($b_i=1$).

1419 ^B Probability distributions were truncated in instances when introduction of errors caused non-physical forcing
 1420 values (see Sec. 3.3.5).

1421 ^C [The high upper \$P\$ bias \(300%\) mimics cases where snowfall data collected in an area of drift deposition are
 1422 assumed \(incorrectly\) to represent other basin locations.](#)

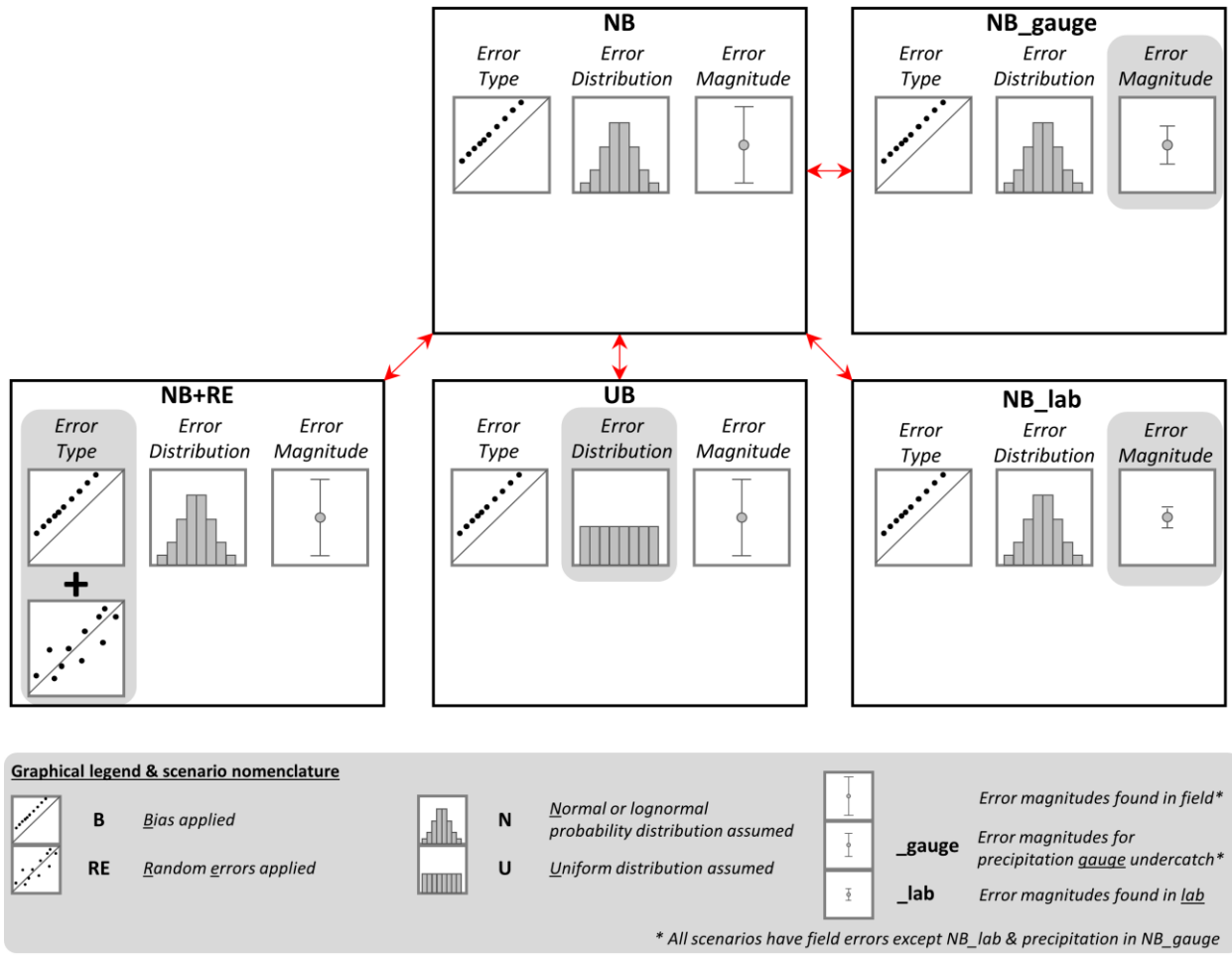
1423 ^D Uncertainty ranges in this scenario are based primarily on manufacturer's specified accuracy for typical sensors
 1424 deployed at SNOTEL sites (*NRCS Staff, personal communication, 2013*). We assume the P storage gauge has the
 1425 same accuracy as a typical tipping bucket gauge.

1426 ^E We neglect P undercatch errors in the lab uncertainty scenario.

1427 **Table 4** Number of samples (N) and model simulations (in parentheses) meeting the
 1428 requirements for minimum peak SWE and snow duration and valid snow disappearance dates at
 1429 each site in each scenario. The number of model simulations scaled as $N \times (k+2)$, where $k=12$ in
 1430 scenario NB+RE and $k=6$ in all other scenarios. When a simulation was rejected, all related
 1431 simulations (based on resampling) were also rejected.

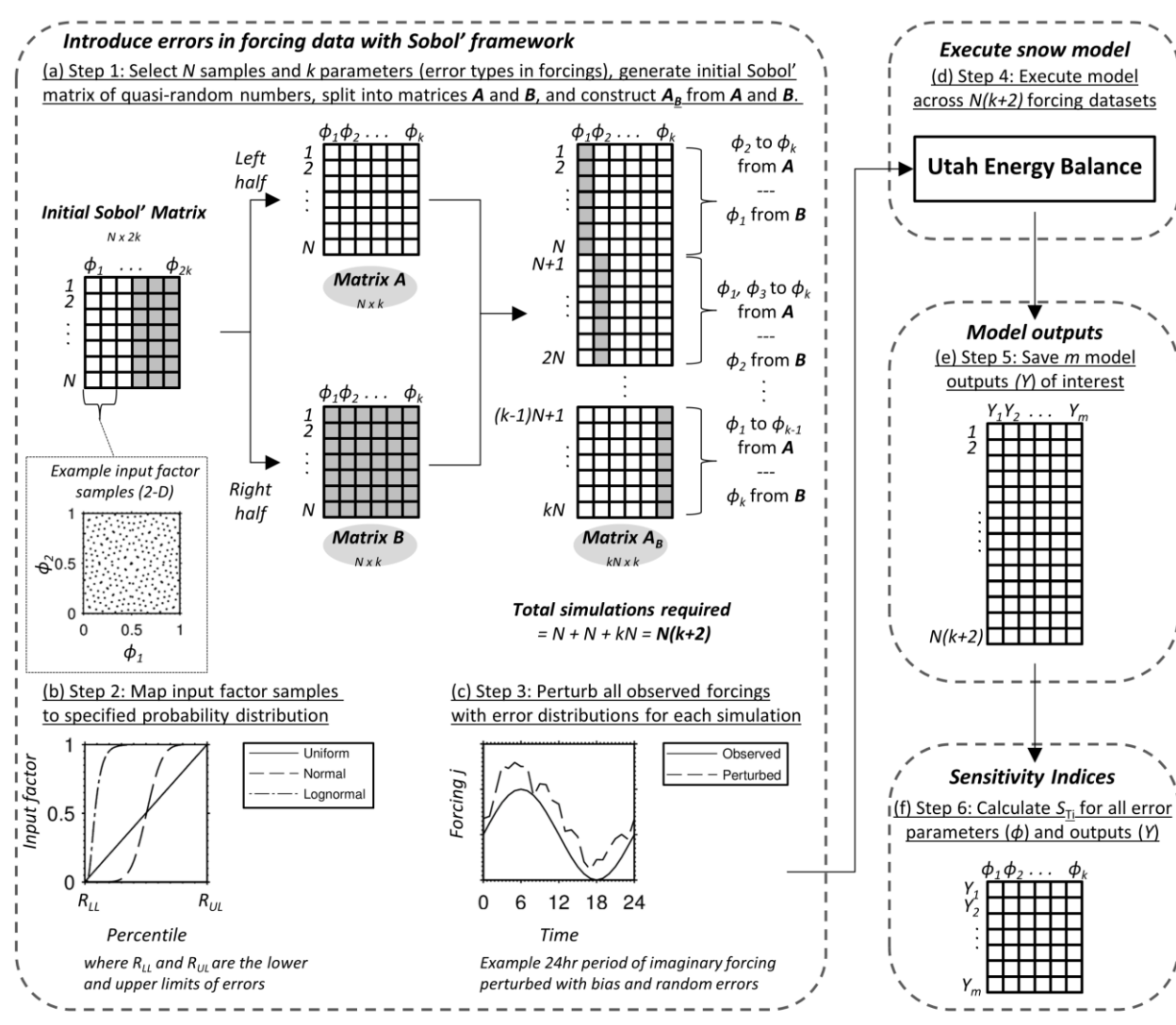
	Scenario NB	Scenario NB+RE	Scenario UB	Scenario NB gauge	Scenario NB lab
IC	9898 (79 184)	<u>10 000</u> <u>(140 000)</u>	8608 (68 864)	<u>10 000</u> <u>(80 000)</u>	10 000 (80 000)
CDP	9792 (78 336)	<u>9869</u> <u>(138 166)</u>	8925 (71 400)	<u>9999</u> <u>(79 992)</u>	10 000 (80 000)
RME	8799 (70 392)	<u>9233</u> <u>(129 262)</u>	9102 (72 816)	<u>10 000</u> <u>(80 000)</u>	10 000 (80 000)
SASP	9984 (79 872)	<u>9984</u> <u>(139 776)</u>	3399 (27 192)	<u>10 000</u> <u>(80 000)</u>	10 000 (80 000)

1432 **7.8.Figures**



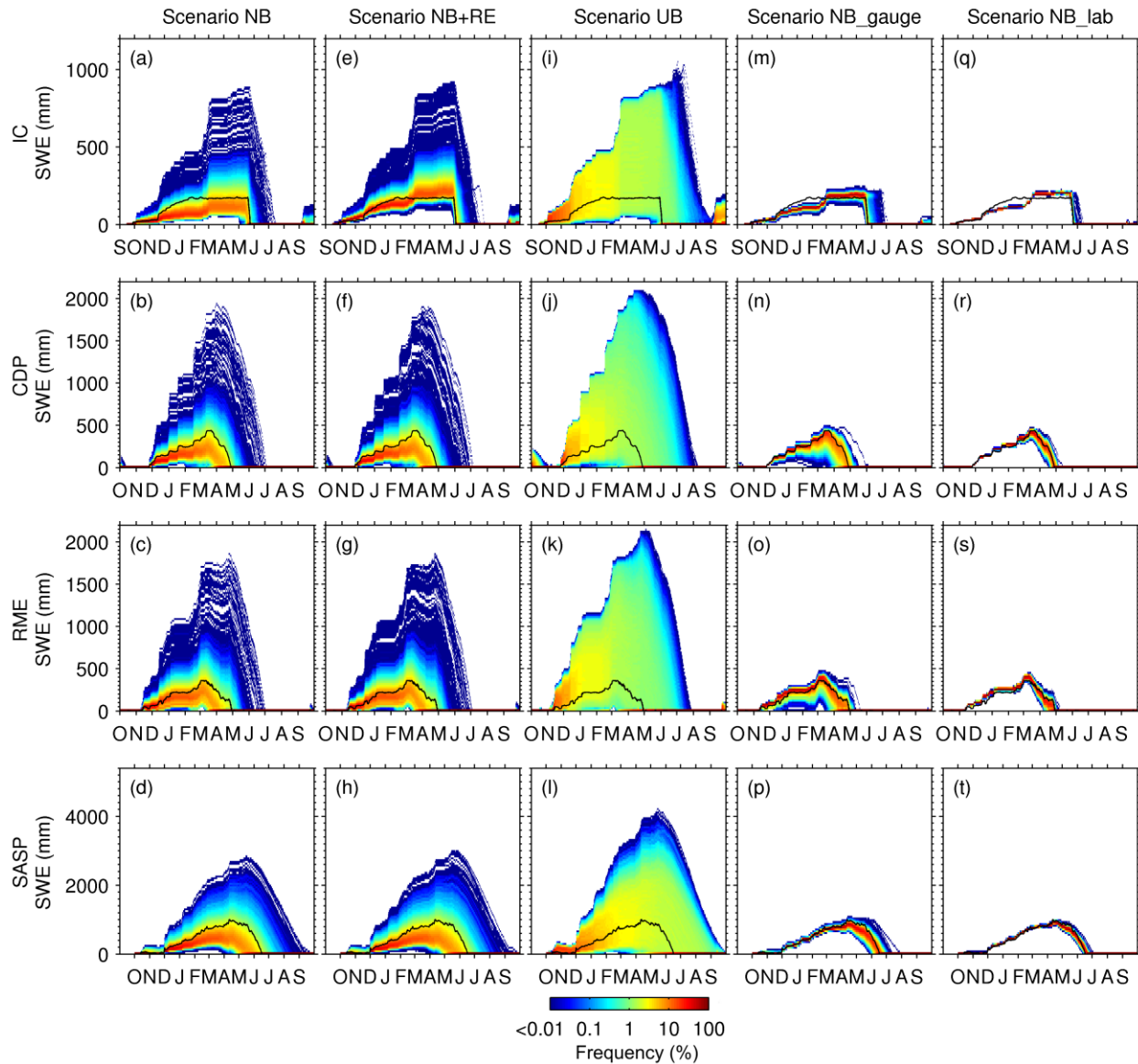
1433

1434 **Figure 1** Scenarios of interest and the type, distribution, and magnitude of errors considered in
 1435 each. NB considers normally (or lognormally) distributed biases with error magnitudes found in
 1436 the field. NB+RE is the same as NB but also considers random errors. UB is the same as NB
 1437 but considers uniformly distributed errors instead. [NB_gauge is the same as NB with](#)
 1438 [reduced precipitation uncertainty \(typical difference between precipitation gauge and snow](#)
 1439 [pillow\).](#) NB_lab is the same as NB but considers laboratory error magnitudes.



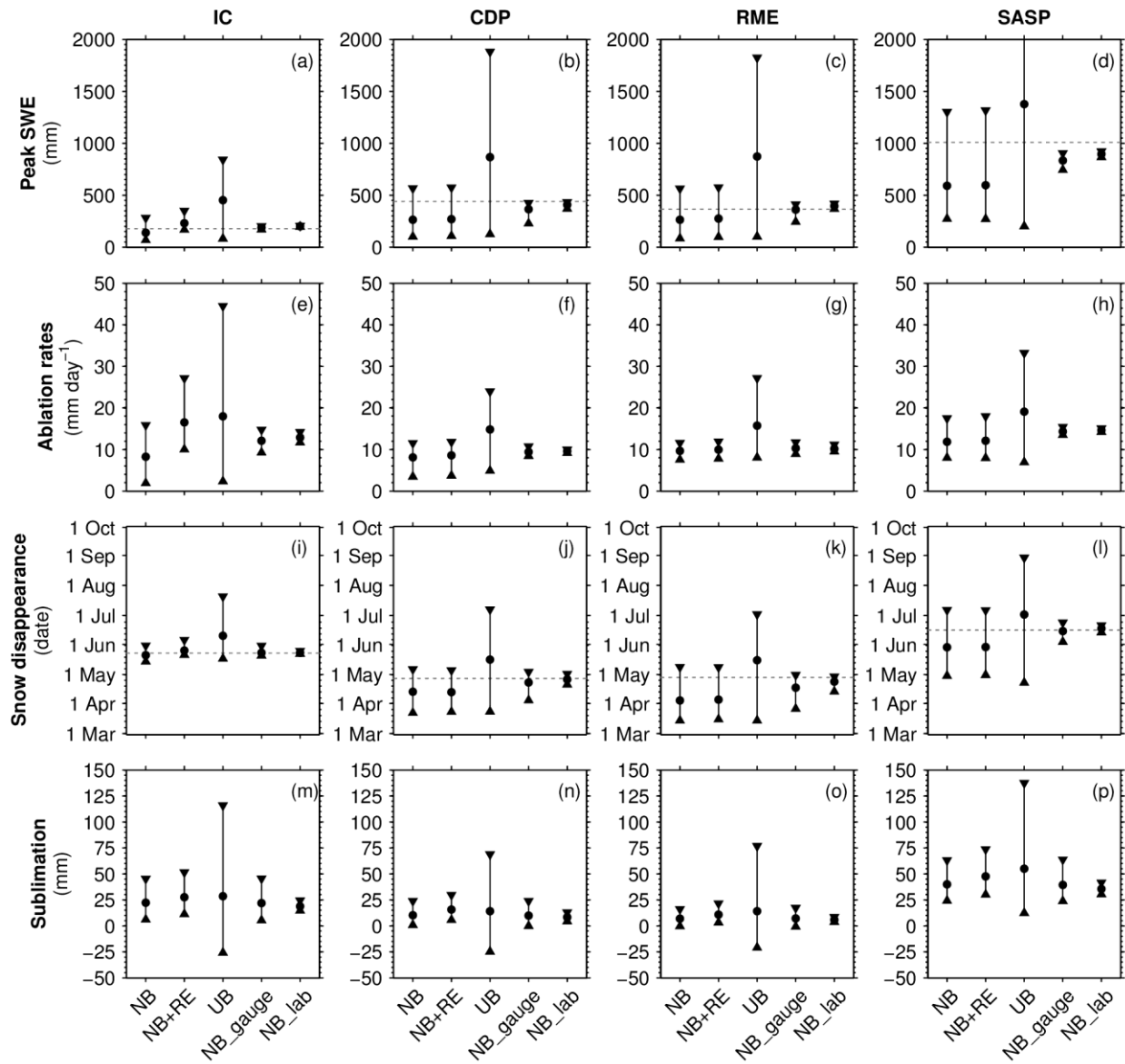
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1441 **Figure 2** Conceptual diagram showing methodology for imposing errors on the forcings with
 1442 error parameters (ϕ) within the Sobol' sensitivity analysis framework, and workflow for model
 1443 execution and calculation of sensitivity indices on model outputs (Y).



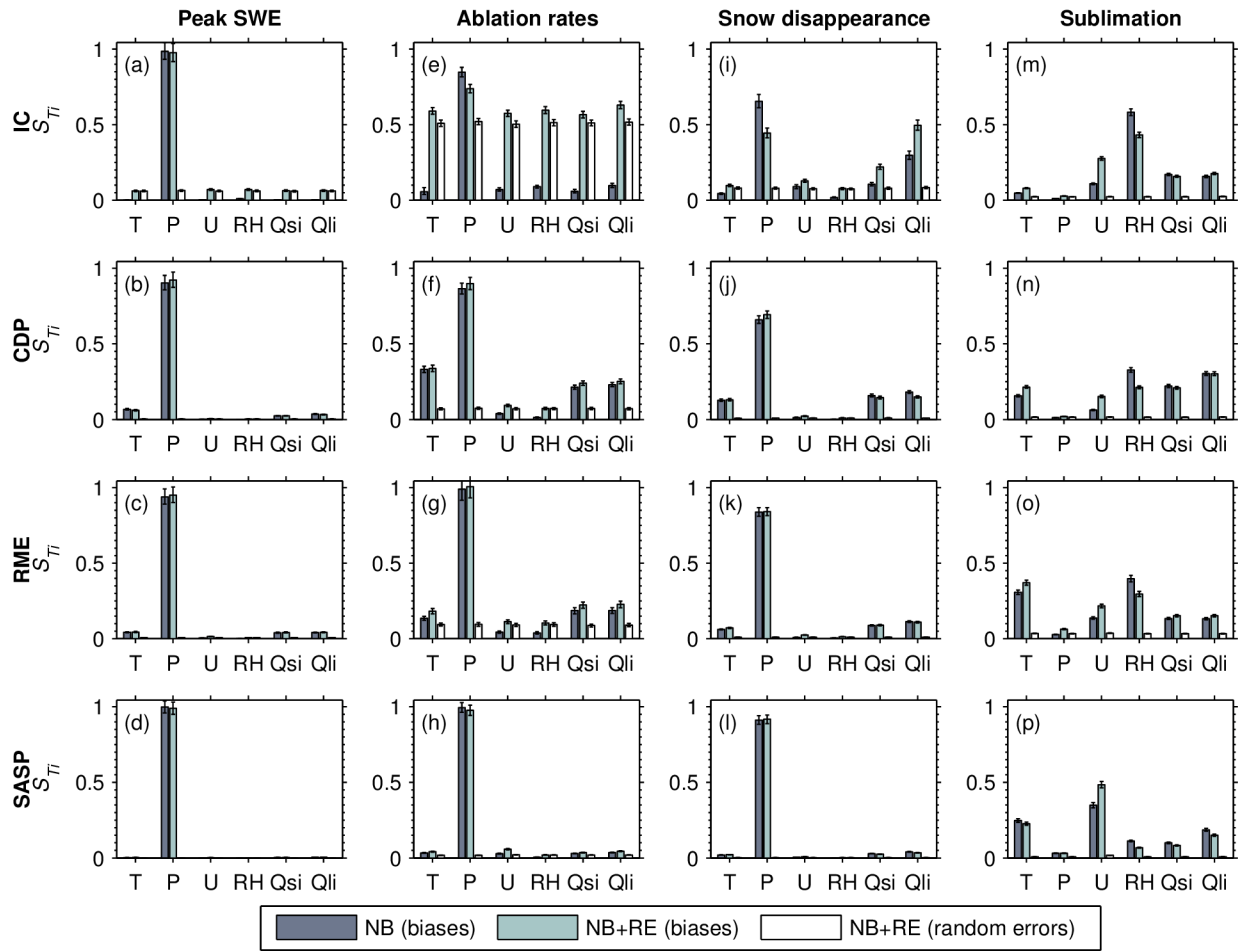
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1445 **Figure 3** Observed (black line) and modeled SWE (color density plot) at the four sites across the
 1446 [five](#) uncertainty scenarios (see Figure 1 and Table 3). The number of model simulations in the
 1447 density plots varies with the site and scenario (see Table 4). The density plots were constructed
 1448 using 100 bins in the SWE dimension with relative frequency tabulated in each bin each day.
 1449 Note the frequency colorbar is on a logarithmic scale. Sites are arranged from top to bottom in
 1450 order of increasing elevation and decreasing latitude. Scenarios are defined as normally
 1451 distributed bias (NB), normally distributed bias and random errors (NB+RE), uniformly
 1452 distributed bias (UB), [normally distributed bias with precipitation gauge uncertainty NB_gauge](#),
 1453 and normally distributed bias at laboratory error magnitudes (NB_lab).



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1455 **Figure 4** Distributions of model outputs (rows) at the four study sites (columns) arranged by
 1456 scenario. For each scenario, the circle is the mean and the whiskers show the range
 1457 encompassing 95% of the simulations (see Table 4 for number of simulations for each site and
 1458 scenario). The dashed lines in (a-d) and (i-l) are the observed values. Axes are matched between
 1459 sites for a given model output; note that the range in scenario UB in (d) is truncated by the axes
 1460 limits (upper value = 3030 mm). Scenarios are defined as normally distributed bias (NB),
 1461 normally distributed bias and random errors (NB+RE), uniformly distributed bias (UB),
 1462 [normally distributed bias with precipitation gauge uncertainty NB_gauge](#), and normally
 1463 distributed bias at laboratory error magnitudes (NB_lab).



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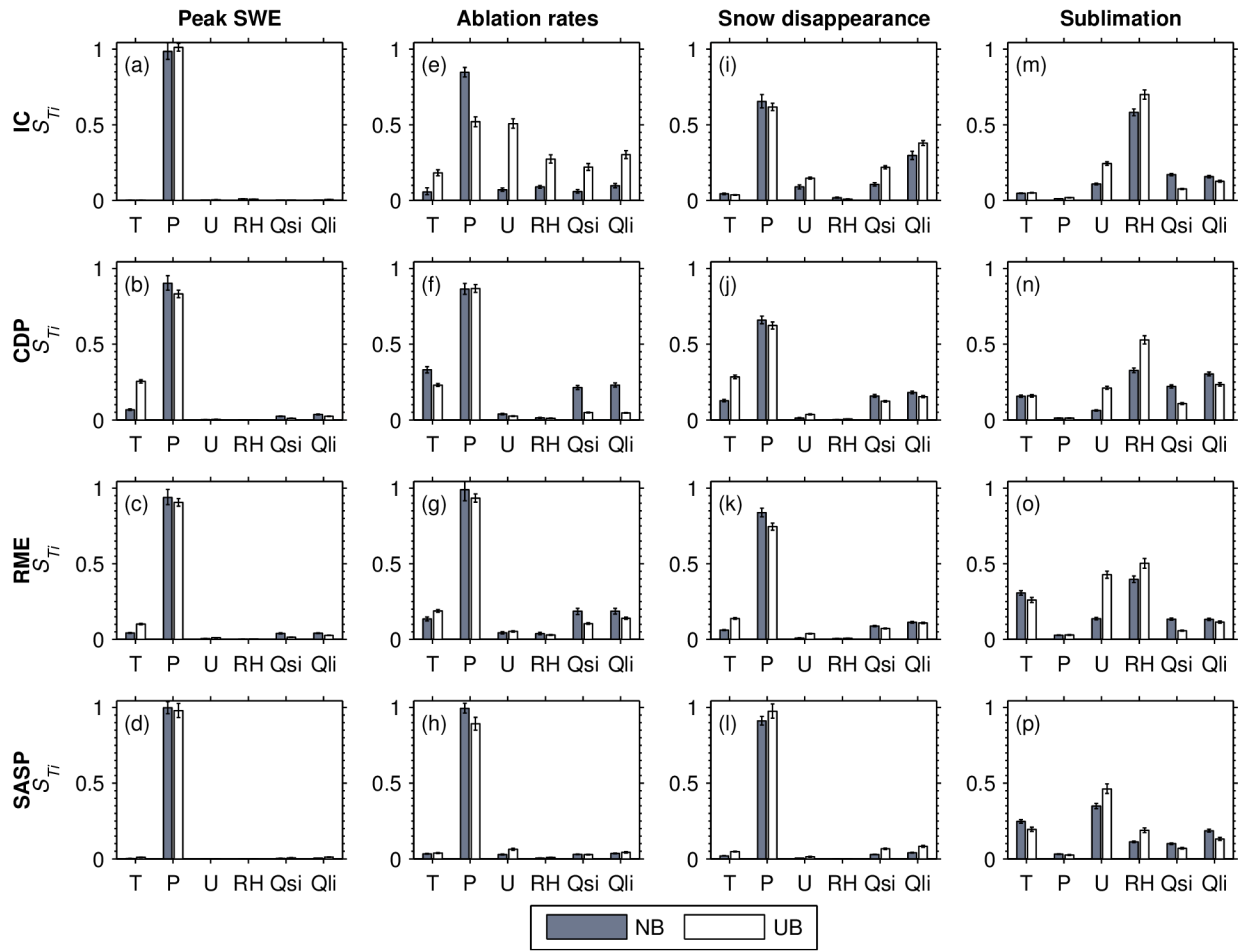
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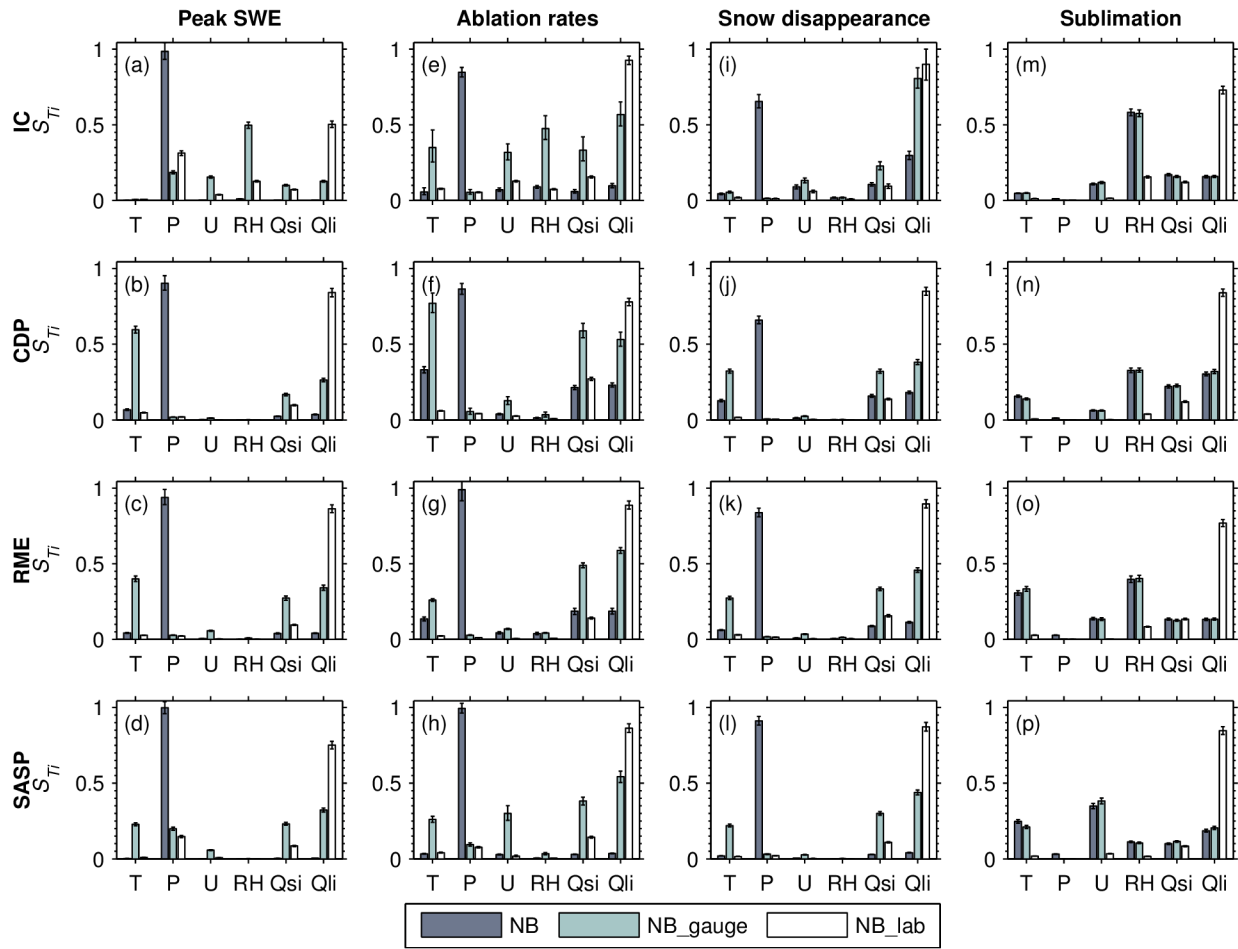
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Figure 5 Model sensitivity as a function of forcing error type. Shown are the total-order sensitivity indices (S_{Ti}) of four model response variables (columns) at the four sites (rows) from scenarios NB and NB+RE. In NB+RE, bias and random error parameters are shown separately. NB+RE considers normally distributed bias and random errors, while NB considers normally distributed bias only. The bar indicates the mean (bootstrapped) sensitivity indices and associated 95% confidence intervals.



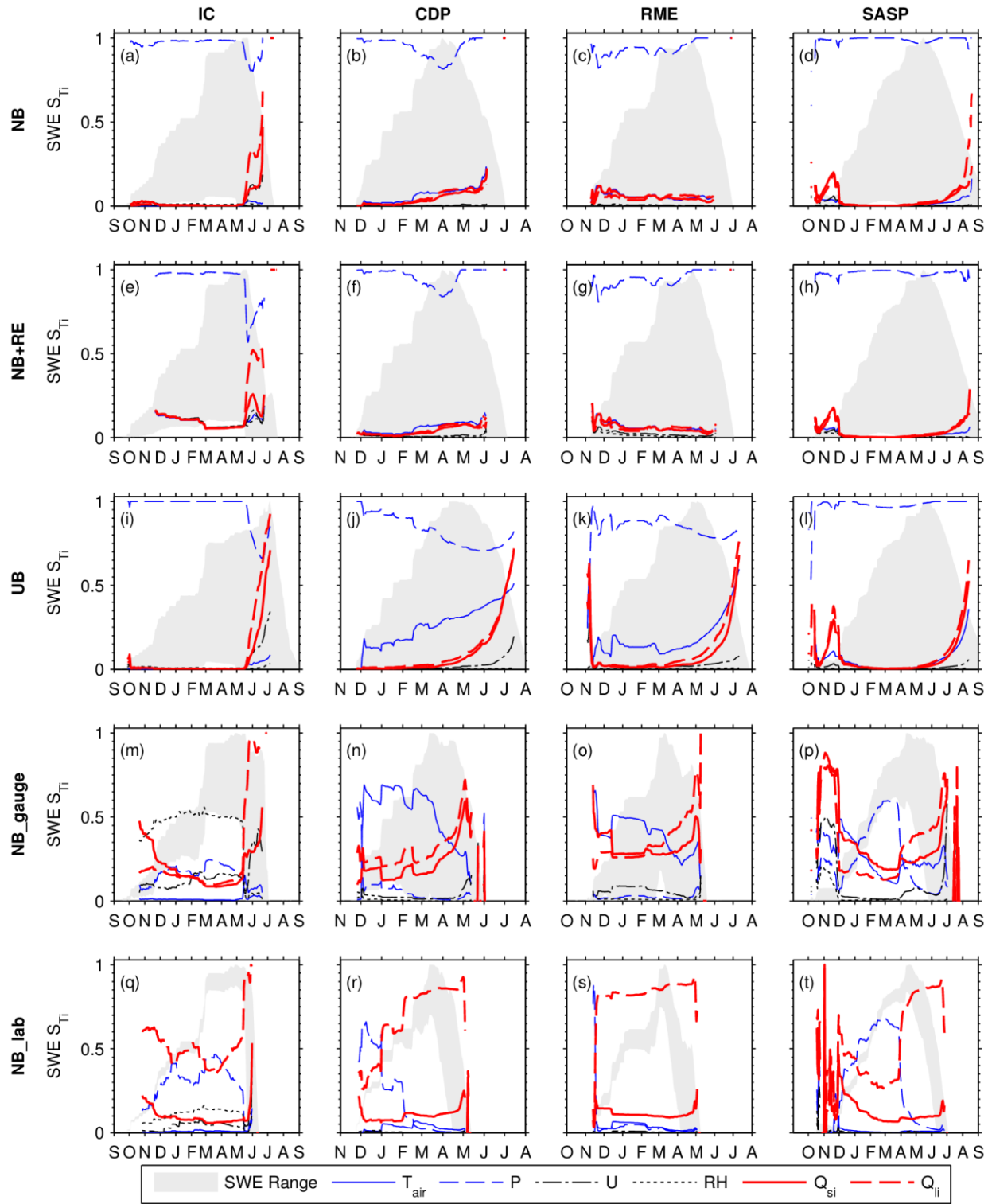
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Figure 6 Same as Fig. 5, but comparing S_{Ti} values from scenarios NB and UB to test model sensitivity as a function of error distribution. UB considers uniformly distributed bias, while NB considers normally distributed bias.



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Figure 7 Same as Fig. 5, but comparing S_{Ti} values from scenarios NB, NB_gauge, and NB_lab to test model sensitivity as a function of error magnitudes. NB considers normally distributed bias at error magnitudes found in the field. NB_gauge has lower precipitation uncertainty (gauge undercatch) than NB but is otherwise identical. NB_lab considers normally distributed bias at error magnitudes found in the laboratory.



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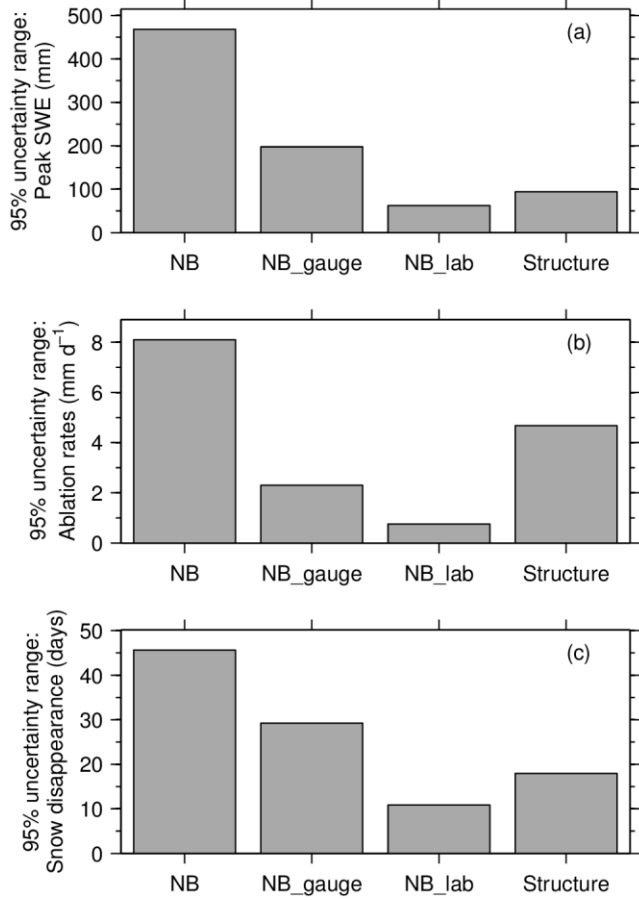
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Figure 8 Variation of daily SWE sensitivity to forcing bias based on site (columns) and error scenario (rows). The normalized range (where 1 = maximum SWE) in modeled SWE is shown (gray area) for context. Sensitivity indices in the early and late part of the snow season were screened out, as a high number of simulations with SWE=0 yielded invalid sensitivity indices.



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1487 **Figure 9** [Uncertainty ranges \(95% intervals\) in \(a\) peak SWE, \(b\) ablation rates, and \(c\) snow](#)
 1488 [disappearances date at CDP in WY2006 for three forcing uncertainty scenarios and the](#) Essery et
 1489 [al. \(2013\) structural uncertainty.](#)