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Topographic controls on soil moisture scaling properties in polygonal ground using idealized high-resolution surface-subsurface simulations

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Abstract

Microtopographic features, such as polygonal ground, are characteristic sources of landscape heterogeneity in the Alaskan Arctic coastal plain. Here, we analyze the hypothesis that microtopography is a dominant controller of soil moisture in polygonal landscapes. We perform multi-year surface-subsurface isothermal flow simulations using the PFLOTRAN model for summer months at six spatial resolutions (0.25-8 m, in increments of a factor of 2). Simulations are performed for four study sites near Barrow, Alaska that are part of the NGEE-Arctic project. Results indicate a non-linear scaling relationship for statistical moments of soil moisture. Mean soil moisture for all study sites is accurately captured in coarser resolution simulations, but soil moisture variance is significantly under-estimated in coarser resolution simulations. The decrease in soil moisture variance in coarser resolution simulations is greater than the decrease in soil moisture variance obtained by coarsening out the fine resolution simulations. We also develop relationships to estimate the fine-resolution soil moisture probability dis-

- tribution function (PDF) using coarse resolution simulations and topography. Although 15 the estimated soil moisture PDF is underestimated during very wet conditions, the moments computed from the inferred soil moisture PDF had good agreement with the full model solutions (bias $< \pm 4$ % and correlation > 0.99) for all four sites. Lastly, we develop two spatially-explicit methods to downscale coarse-resolution simulations of soil
- moisture. The first downscaling method requires simulation of soil moisture at fine and coarse resolution, while the second downscaling approach uses only topographical information at the two resolutions. Both downscaling approaches are able to accurately estimate fine-resolution soil moisture spatial patterns when compared to fine-resolution simulations (mean error for all study sites are $< \pm 1$ %), but the first downscaling method
- more accurately estimates soil moisture variance. 25



1 Introduction

Northern permafrost soil currently contains approximately 1700 billion metric tons of frozen organic carbon (Tarnocai et al., 2009). Global climate is warming (Stocker et al., 2013), and "Arctic amplification" is predicted to cause disproportionately larger tem-

- ⁵ perature increases at high latitudes (Holland and Bitz, 2003). This warming will cause permafrost thaw and decomposition, leading to CO₂ and CH₄ emissions to the atmosphere. There is, however, a range of estimates regarding how rapidly permafrost thaw and decomposition will occur (Koven et al., 2011; Schaefer et al., 2011; Schuur and Abbott, 2011).
- ¹⁰ Soil moisture, θ , is one of the key environmental factors controlling the rate and products (i.e., CO₂ vs. CH₄) of microbial decomposition of thawed soil organic carbon (Schuur et al., 2008). Properties of the underlying permafrost in the Arctic have been shown to control changes in soil moisture. Observational studies have documented both increases and decreases of soil moisture in Alaska due to climate change. Based
- on analysis of remotely sensed data from 1950–2002, Riordan et al. (2006) found significant reduction in the number and area of shallow, closed-basin ponds in regions of discontinuous permafrost, but negligible change for ponds in continuous permafrost. Jorgenson et al. (2006) analyzed areal photographs from 1945, 1982, and 2001, and found large increases in degradation of ice-wedges in continuous permafrost of north-
- ²⁰ ern Alaska. Since CH₄ emissions are very sensitive to soil moisture status (Torn and Chapin lii, 1993) and have 25 times higher greenhouse warming potential on a century timescale than CO₂ (Bridgham et al., 1998), developing approaches to characterize soil moisture dynamics across a wide range of spatial scales is critical for predicting interactions between high-latitude terrestrial ecosystems and climate.
- Large portions of the Arctic are characterized by polygonal ground features, which are formed due to thermal expansion and contraction of ice wedges within the soil (Hinkel et al., 2005). Polygons are classified as "low-centered" or "high-centered" based on the relationship between their central and mean elevations. Polygonal ground fea-



tures are dynamic components of the Arctic landscape in which ice-wedge thaw under low-centered polygon rims leads to subsidence and eventually (\sim o(centuries)) to high-centered polygons (Seppala et al., 1991). Microtopography of polygonal ground influences soil hydrologic and thermal conditions (Engstrom et al., 2005). In addition to controlling CO_2 and CH_4 emissions, soil moisture impacts (1) partitioning of incoming radiation into latent, sensible, and ground heat fluxes (Hinzman and Kane, 1992; Mc-Fadden et al., 1998), (2) photosynthesis rates (Oberbauer et al., 1991; Oechel et al., 1993; McGuire et al., 2000; Zona et al., 2011), and (3) vegetation distributions (Wiggins, 1951). Non-vascular plants (mosses and lichens), which are abundant in Arctic ecosystems, contribute up to 75% of evaporative losses (Miller et al., 1976) and are strongly

10 influenced by near surface hydrologic conditions (Williams and Flanagan, 1996).

The recognition that soil moisture dynamics occur across a wide range of spatial scales (i.e., soil pore, Childs, 1940 to continental, Brocca et al., 2010; Li and Rodell, 2013) has motivated a large literature attempting to integrate relationships of soil moisture heterogeneity with topographic, biological, and forcing controls. Numerous studies have identified statistical self-similarity of soil moisture across a range of spatiotemporal scales via field observations and numerical experiments. A soil moisture field is self-similar if (Dubayah et al., 1997):

15

$$\mathbb{E}\left[\theta^{q}\left(A_{j}\right)\right] = \left(\frac{A_{j}}{A_{j}}\right)^{K(q)} \mathbb{E}\left[\theta^{q}\left(A_{j}\right)\right]$$

where q is the order of the moment, K(q) is a set of scaling exponents associated with 20 the moment, A_i and A_i represent fine and coarse scale areas or resolutions, respectively, and the ratio A_i/A_i is called the scale parameter λ . If K(q) is a linear function, then the *q*th moment of soil moisture is said to exhibit simple or linear scaling, otherwise soil moisture exhibits multi-scaling. By analyzing passive microwave remotely sensed soil moisture data from 30 m to 4.4 km, Rodriguez-Iturbe et al. (1995) and Hu 25 et al. (1997) found that soil moisture variance, σ_{A}^{2} , exhibited a simple scaling processes. In contrast, Nykanen and Foufoula-Georgiou (2001) demonstrated a non-linear scaling



(1)

relationship for variability in soil moisture using data from the 1997 Southern Great Plains Hydrology Experiments (SGP97). Many observational studies have also examined the relationship between the coefficient of variation of soil moisture, C_v , and mean soil moisture, $\overline{\theta}$, and found an inverse (Famiglietti et al., 1999, 2008; Kumar, 2004) or upward convex (Brocca et al., 2010, 2012; Choi and Jacobs, 2011) relationship. Ivanov et al. (2010) used an ecohydrologic model to demonstrate a hysteretic dependence between C_v and $\overline{\theta}$ that arises because of mean and variability in soil moisture initial conditions, and the initiation of lateral subsurface fluxes. Gebremichael et al. (2009) compared scaling characteristics of simulated and observed θ fields for SGP97 as

¹⁰ a metric for model validation and concluded that, although the model was successful in capturing total streamflow, the mechanism for runoff production was incorrectly modeled.

Numerical studies have investigated the importance of including spatial variability on model predictions. Sivapalan and Woods (1995) showed that subgrid variability

- of rainfall and soil moisture can have significant impact on land surface fluxes. Choi et al. (2007) demonstrated that subgrid variability impacts mean soil moisture predictions under relatively dry conditions. Jana and Mohanty (2012a) found that power-law scaling of soil hydraulic parameters allowed accurate prediction of subgrid topographic effects for four different hillslope configurations. However, there remains limited un derstanding of sub-meter scale soil moisture heterogeneity arising due to polygonal
- ground features in Arctic ecosystems (Chapin III et al., 2002).

Given the importance of soil moisture spatial heterogeneity on hydrological and biogechemical dynamics, watershed to global-scale models have integrated several approaches to account for the relevant processes, including: (1) using a non-spatially

explicit tiling approach (Oleson, 2013), (2) employing effective parameters at coarse resolution (Jana and Mohanty, 2012b), and (3) modifying the governing equations to explicitly include terms related to soil moisture variance (Choi et al., 2007; Kumar, 2004). We note that the third approach could also include terms related to higher-order moments, but we are not aware of such efforts in the literature.



We analyzed here another approach to represent subgrid hydrological heterogeneity in models; i.e., developing relationships (i.e., reduced order models (ROMs)) between the mean properties (which could be estimated with a coarser-resolution model) and either the statistical (Riley and Shen, 2014) or spatially explicit (Pau et al., 2014) prop- $_{5}$ erties of the field of interest (here θ). The ROMs could be made extensible if they could

be shown to be relatively invariant functions of the system properties, e.g., topographical indices, vegetation properties, or soil properties.

This study had three primary objectives: (1) characterize spatial scaling of soil moisture heterogeneity in the presence of polygonal ground features for an Arctic ecosys-

- tem, (2) develop reduced order models that allow prediction of higher-order statistical moments of soil moisture given coarse-resolution model simulations, and (3) identify controlling properties of the relationships between spatial heterogeneity and spatial resolution of predicted soil moisture fields as a first step toward representing spatial soil moisture heterogeneity in a coarser-resolution model. To address these objec-
- tives we performed multi-year surface–subsurface isothermal flow simulations using the PFLOTRAN model for summer months at multiple spatial resolutions. Descriptions of the study site, climate forcing, and model setup are presented in Sect. 2. Results of our spatial scaling analysis are presented in Sect. 3. We conclude with discussion, limitations of our approach, and observations and model structures required to overcome
 those shortcomings in the future.

2 Methodology

2.1 Study area

25

In order to reduce uncertainty regarding impacts of climate change in high-latitude ecosystems, a long term Department of Energy (DOE) Next-Generation Ecosystem Experiment (NGEE-Arctic) project was initiated with sites located near Barrow, Alaska (71.3° N, 156.5° W). Four primary NGEE-Arctic study sites (A, B, C, D; Fig. 1are located



within the Barrow Environmental Observatory (BEO), which is situated on the Alaskan Coastal Plain. Mean air temperature and precipitation for Barrow, AK during summer months (July–August) are 3.3 °C and 72 mm, respectively (Liljedahl et al., 2011). The BEO has continuous permafrost (Brown et al., 1980) with land surface characterized

- ⁵ by thaw lakes, drained thaw lake basins, and interstitial polygons (Hinkel et al., 2007). The seasonal thaw depth (active layer depth) ranges between 30–90 cm in thickness (Hinkel et al., 2003). The overall topographic relief for the BEO is low, but the four NGEE study sites have distinct microtopraphic features that include: low-centered (A), highcentered (B), and transitional polygons (C, D) (Table 1). Contrasting polygon types are
- indicative of different stages of permafrost degradation and were the primary motivation behind the choice of study sites for the NGEE-Arctic project. LIDAR Digital Elevation Model (DEM) data was available at 0.25 m resolution for the region encompassing all four NGEE sites.

2.2 Model

In this study we used the PFLOTRAN model, an open-source subsurface flow and reactive transport model (Hammond et al., 2012), which we modified to include surface flow. Subsurface reactive flows and transport processes in PFLOTRAN are solved using implicit time integration and finite volume spatial discretization. PFLOTRAN uses the Portable Extensible Toolkit for Scientific Computation (PETSc) libraries (Balay et al., 2013) for parallelization and domain decomposition.

We sequentially coupled a 2-D diffusion-wave overland flow model with PFLOTRAN:

$$\frac{\partial h}{\partial t} + \frac{\partial (hu)}{\partial x} + \frac{\partial (hv)}{\partial y} = S$$

where *h* is depth of surface water [m]; *u* and *v* are velocities $[ms^{-1}]$ in *x* and *y* directions, respectively; and *S* is the source term $[ms^{-1}]$. The water velocity in *x* direction is com-



(2)

puted using Manning's formula (Manning, 1891):

$$u = -\operatorname{sgn}\left(H_{i+1,j} - H_{i,j}\right) \frac{h_{i+1/2,j}^{\frac{2}{3}}}{n_{\mathrm{m}}} \left|\frac{H_{i+1,j} - H_{i,j}}{x_{i+1,j} - x_{i,j}}\right|^{\frac{1}{2}}$$

where H(= h + z) is total water head [m], *z* is surface elevation [m], and n_m is the Manning's coefficient. The velocity in the *y* direction can be computed similarly. The overland flow model uses a finite volume spatial discretization and a forward Euler time integration scheme and transports surface water laterally within the domain until the surface–subsurface coupling time is reached. Then, using continuity of pressure at the surface–subsurface interface, infiltration or exfiltration is calculated. In this study, we choose 15 min as the coupling time between surface–subsurface based on a sensitivity study that minimized computational expense while maintaining accuracy of the numerical solution.

2.3 System characterization and climate forcing

Polygonal ground regions in Arctic ecosystems are also characterized by fine-scale variation in soil texture across the polygon centers, rims, and troughs (Quinton and Marsh, 1998). Troughs and centers of low-center polygons allow for preferential infiltration during the thaw season, which in turn leads to zonation of vegetation types across polygonal features (Minke et al., 2009). Apart from horizontal variability in soils due to surface features, cryoturbation leads to vertical heterogeneity in Arctic soils. Cryoturbation is a physical process of mixing soil material due to freeze-thaw cycles of ice wedges, which causes near surface soil to move downwards and deeper soil to move

- 20 wedges, which causes near surface soil to move downwards and deeper soil to move upwards with a time scale of hundreds of years (Bockheim, 2007). Koven et al. (2009) have shown inclusion of cryoturbative mixing within a terrestrial carbon cycle model leads to a better agreement between model predictions and observations of bulk soil organic matter and ¹⁴C. Due to a lack of data to represent horizontal heterogeneity in soils at our study sites, we assumed horizontally homogeneous soil properties. Vertical
- ²⁵ soils at our study sites, we assumed horizontally homogeneous soil properties. Vertical



(3)

soil heterogeneity is accounted for within our simulations using data reported at three depths (0-5, 5-10, and 20-25 cm) (Hinzman et al., 1991). Since our focus is on thaw period soil moisture heterogeneity over a decade, we did not account for heterogeneity arising from cryoturbation in this study.

⁵ The following van Genuchten (1980) relationship was used to approximate observations reported in Hinzman et al. (1991) of capillary pressure and hydraulic conductivity as a function of water saturation given by,

$$\theta(\psi) = \begin{cases} \theta_{r} + \frac{\theta_{s} - \theta_{r}}{\left[1 + (\alpha |\psi|)^{n}\right]^{1 - \frac{1}{n}}}, \ \psi < 0\\ \theta_{s}, \ \psi \ge 0 \end{cases}$$

$$\kappa(\psi) = \kappa_{r} e^{2} \int_{0}^{1} \left[1 - e^{\frac{1}{m}}\right]^{m} \end{cases}$$

$$K_{\rm r}(\psi) = K_{\rm sat} s_{\theta}^2 \left\{ 1 - \left[1 - s_{\theta}^{\overline{m}} \right] \right\}$$

$$s_{\theta} = \frac{\theta - \theta_{\rm r}}{\theta_{\rm s} - \theta_{\rm r}}$$

15

where θ , θ_s , and θ_r are soil moisture, saturated soil moisture (or porosity) and residual soil moisture, respectively; ψ is capillary pressure [m]; α is a parameter related to air entry pressure [m⁻¹]; K_{sat} is saturated hydraulic conductivity (cmmin⁻¹), and m(= 1 - 1/n) and n are empirical constants. Table 2 summarizes the values of van Genuchten parameters used in this study, while Fig. 2 shows comparison of data reported in Hinzman et al. (1991) and the fitted van Genuchten model.

Boundary conditions (BCs) for the surface domain included precipitation and snowmelt while evapotranspiration (ET) was applied as a sink term for the subsurface domain. BCs for PFLOTRAN were obtained by running an offline Community Land

²⁰ Model (CLM4.5) simulation using meteorological data (1998–2002) from the Ameriflux station in Barrow, AK (shown in Fig. 3). A 3000 years CLM4.5 simulation was performed to allow for subsurface biogeochemistry in the model to reach equilibrium and then hourly output was saved for PFLOTRAN simulations. The ET sink was distributed



(4)

(5)

(6)

vertically within the PFLOTRAN subsurface domain using the same exponential rooting profile applied in CLM4.5 for Arctic shrubs (Oleson, 2013). Because of a lack of observations, no horizontal heterogeneity in vegetation type was accounted for in this study.

5 2.4 Simulation setup

We performed 5 year multi-resolution PFLOTRAN surface–subsurface simulations to characterize soil moisture scaling for our four NGEE-Arctic study sites. The finest resolution PFLOTRAN meshes for all four sites were created starting with 0.25 m LI-DAR DEM data and comprised of prismatic grid cells with planar surface area of $3.12 \times 10^{-2} \,[\text{m}^2]$ (= $1/2 \times 0.25 \,\text{m} \times 0.25 \,\text{m}$). The horizontal extent of the finest scale meshes was 104 m with 346 122 cells and we used 10 equally-spaced vertical layers reaching a depth of 50 cm. Additional experiments were performed at each of the

four NGEE-Arctic study sites using meshes created from coarsened DEM data at 0.5, 1, 2, 4, and 8 m and an example of coarse resolution DEM for site B and D are shown

¹⁵ in Fig. 4. The first two near-surface soil layers were assigned van Genuchten parameters corresponding to the 0–5 and 5–10 cm data, respectively, and the remaining eight layers were assigned soil parameters corresponding to data from 20–25 cm (Hinzman et al., 1991).

3 Results and discussion

We perform several analyses of the simulation outputs: (1) characterize the relationships between soil moisture moments and spatial resolution of the simulations, (2) investigate how these relationships changed when coarser-resolution simulations are used instead of spatially averaging the finest-resolution simulation (3) develop analytical approximations to relate 2nd, 3rd, and 4th statistical moments with the mean moisture, (4) investigate the topographic controls on the soil moisture probability den-



sity function, and (5) develop a method to combine the coarse-resolution simulation predictions and the fine-resolution topographic information to dynamically estimate the fine-resolution soil moisture probability distribution function.

3.1 Time series analysis

Across the four sites and five years of simulation, the coarse-resolution PFLOTRAN simulations show that soil moisture in sites A and B are comparable and relatively drier, site C is intermediate, and site D is the wettest (Fig. 5. Time series of simulated mean soil moisture for the four NGEE-Arctic study sites.) Predicted soil moisture decreased in the first half of each year except 2000, corresponding to a net loss associated with
 evapotranspiration. All sites became wetter starting in mid July (2001) and mid August (1998, 1999, 2000, and 2002) corresponding to increasing precipitation inputs (Fig. 3). The relatively smaller drydown period in 2000 following initial saturation occurred because of much higher precipitation in the beginning of the summer season.

The coarse-resolution simulations are able to capture the mean of the fine-resolution

- ¹⁵ soil moisture ($\overline{\theta}$) accurately, with average differences of < 1 % across all four sites and years. For brevity, we present this first analysis of simulation results at Site A for 1999, but our conclusions are applicable to all sites and for the entire simulation period. Soil moisture variance (σ_{θ}^2) decreased during dry-down periods and increased immediately after rainfall events (Fig. 6 shows predictions with mesh resolutions of 0.25, 2, and
- 8 m). The lower variance in coarser-resolution simulations compared to finer-resolution simulations is attributed to decreases in slope and curvature of the underlying DEM and is consistent with the findings of other studies (Kuo, 1999; Niedda, 2004).

We analyzed the loss of variance due to coarsening of the DEM using information theory (Shannon and Weaver, 1949). The information content, *I*, a measure of the variability of a parameter, is defined as

 $I = -\sum_{i=1}^{n} p_i \ln(p_i)$



(7)

where *N* is the number of bins into which the parameter range is divided and p_j is the proportion of the parameter in the *j*th bin. The information content for slope and curvature decreased with coarser grids for all four study sites (Fig. 7). Similar to results reported by Kuo (1999), our study site had a larger decrease in *I* with increasing grid resolution for curvature than slope. Both, slope and curvature of the terrain contribute to prediction of mean soil moisture via governing equations of subsurface flow, thus a loss in *I* with increasing grid size implies that the hydrologic response of the model will be less spatially variable at coarser resolution.

We aggregated the simulated θ at 0.25, 2, and 8 m resolutions (Fig. 6) and then computed variance for the coarsened soil moisture predictions. Each successive coarsening of the soil moisture field led to a decrease in variance, but these decreases are not as large as those calculated from the model simulations at the coarser resolutions. This result shows non-linear impacts of DEM resolution on simulated soil moisture. As in many observational (Teuling and Troch, 2005; Brocca et al., 2010) and modeling (Albertson and Montaldo, 2003) studies of temperate watersheds, our model predictions

- ¹⁵ bertson and Montaldo, 2003) studies of temperate watersheds, our model predictions for the four polygonal tundra sites resulted in a concave-up relationship between variance and mean soil moisture (Fig. 8). At low (high) $\overline{\theta}$, soil moisture variance is expected to be low since the entire domain is expected to be relatively dry (wet). At an intermediate mean moisture value, soil moisture variance reached a peak value, $\sigma_{\theta, \text{ peak}}^2$, that
- ²⁰ differed between sites. The framework presented by Yeh and Eltahir (1998) to describe the relationship between topography and spatial distribution of soil moisture explains the variation of simulated σ_{θ}^2 across our study sites. Yeh and Eltahir (1998) showed that for a steady state assumption and when only accounting for variability in surface topography, σ_{θ}^2 is a linear function of the variance in elevation, σ_z^2 (Eq. 20 of Yeh and Eltahir,
- ²⁵ 1998). In order to investigate the $\sigma_{\theta}^2 \sigma_z^2$ relationship at our Barrow sites, we created seven mean soil moisture bins between 0.52–0.58; for each study site, the mean σ_{θ}^2 for each soil moisture bin is computed (Fig. 11). Simulated soil moisture variance is largest for sites B and C, which have the highest σ_z^2 ; followed by sites A and D, respectively, which agrees with results presented in Yeh and Eltahir (1998). The slope of the linear



 $\sigma_{\theta}^2 - \sigma_z^2$ relationship exhibits a non-linear relationship with $\overline{\theta}$ (Fig. 10), which similar to the $\sigma_{\theta}^2 - \overline{\theta}$ relationship. This analysis shows that the steady state linear relationship between soil moisture variance and topography as suggested by Yeh and Eltahir (1998) is applicable in the transient case with the modification that slope of $\sigma_{\theta}^2 - \sigma_z^2$ is dependent on transient mean soil moisture.

Ivanov et al. (2010) reported hysteresis between C_v and $\overline{\theta}$ for a steep zero-order basin in a semiarid climate. The design of numerical experiments by Ivanov et al. (2010) ensured an absence of infiltration excess runoff generation and topography induced subsurface soil moisture redistribution was attributed as the chief cause of the nonunique relationship between C_v and $\overline{\theta}$. In our study sites, the presence of polygonal surface features created preferential flow and infiltration pathways for surface flows, which resulted in an overall increase in σ_{θ}^2 after rainfall events and resulted in an absence of hysteretic relationships between C_v and $\overline{\theta}$.

- Next we examine relationships between simulated soil moisture variance and spatial ¹⁵ resolution at all sites for the entire simulation period. To illustrate the patterns that emerged, we discuss these relationships at Site A for the driest (t = 71 day) and wettest (t = 84 day) conditions (Fig. 11). Also shown are soil moisture variance estimated by aggregating the finest-resolution simulation across spatial resolutions for the same two days. It is evident from Fig. 11 that soil moisture variance exhibits non-linear scaling, as ²⁰ has been observed in many previous studies (Nykanen and Foufoula-Georgiou, 2001;
 - Lawrence and Hornberger, 2007; Brocca et al., 2012).

3.2 Estimation of fine-resolution soil moisture PDF

In this polygonal tundra system the soil moisture distribution is strongly controlled by topography, exhibiting a strong inverse relationship between saturation and elevation

⁵ (Fig. 12). We therefore investigated an approach to estimate both the full probability distribution function (PDF) of fine-resolution soil moisture (with $f_{\Theta}(\theta)$ representing the PDF from the fine-resolution simulations) and its moments using coarse-resolution



simulations and site-level topography. We developed an estimated soil moisture PDF $(f_{\Theta}(\theta))$ by rotating the probability distribution function of the DEM, $f_Z(z)$, about its mean and scaling the rotated $f_Z(z)$ by the predicted coarse-resolution maximum (θ_{max}^{fine}) and minimum (θ_{min}^{fine}) soil moisture at the finest resolution for each day. θ_{max}^{fine} and θ_{min}^{fine} are obtained from coarse-resolution mean soil moisture $(\overline{\theta})$ simulations using a best-fit cubic polynomial curve:

$$\theta_{\text{max/min}}^{\text{fine}} = \gamma_3 \overline{\theta}^3 + \gamma_2 \overline{\theta}^2 + \gamma_1 \overline{\theta} + \gamma_0$$

where γ_i are best-fit coefficients. The estimated (from Eq. (10) and the coarseresolution simulations) and fine-resolution simulated $f_{\Theta}(\theta)$ showed very good correspondence (e.g., Fig. 13 for Site A). The agreement between estimated and simulated fine-resolution PDF is better for drier conditions than wetter conditions, and the estimated PDF underestimates soil moisture at higher $\overline{\theta}$ conditions. The ability to predict the soil moisture PDF from the inverted and scaled DEM PDF is consistent with the idea that, in polygonal tundra, the relatively lower elevations (troughs) are more likely

to be saturated, the relatively higher elevations (rims) are less likely to be saturated, and there is a dominant PDF peak at an intermediate soil moisture corresponding to the polygon centers (which have the largest fractional cover in the polygons). The close correspondence between simulated and inferred soil moisture PDFs using the transformed elevation PDF in each site provides a quantitative method to estimate moisture over time that qualitatively matches this intuitively reasonable distribution.

We next compared the first four central moments from the estimated (Eq. 10) and simulated PDFs (e.g., Fig. 14 for Site A). The bias and correlation of the first four central moments across all four sites are $< \pm 4\%$ and > 0.99, respectively (Table 4). Although these estimated moments are of comparable accuracy to those developed by

²⁵ relating the moments to the mean moisture field (Sect. 3.2), the ability to predict the full PDF provides a potentially more accurate representation of the dynamically varying soil moisture field.



(8)

Estimation of fine scale soil moisture field 3.3

The approach presented in the previous section estimated statistical properties of the soil moisture distribution at finer spatial resolution from coarse resolution simulations without explicitly retrieving θ at fine resolution. In this section, we present two approaches to downscale simulated coarse-resolution soil moisture fields to estimate fine-resolution soil moisture. The first downscaling approach uses soil moisture simulations results at both fine and coarse resolution to develop spatially-explicit, timevarying downscaling factors. The second downscaling approach estimates spatiallyexplicit time-invariant factors based on elevation at fine and coarse resolutions. In the first downscaling approach, for a given fine-grid cell (i, j), daily downscaling factors, d_{θ} , to map soil moisture from 8 to 0.25 m is computed as:

$$d_{\theta}(i,j,t) = \frac{\theta_{0.25\,\mathrm{m}}(i,j,t)}{\theta_{8\,\mathrm{m}}(i^*,j^*,t)}$$

where $\theta_{0.25m}$ and θ_{8m} are simulated soil moisture at 0.25 and 8m, respectively, and (i^*, j^*) is the corresponding coarse resolution grid cell that encompasses the fine grid cell. The temporally averaged downscaling factor, $\overline{d_{\theta}}$, is less than 1.0 for rims of high centered-polygons (in Site A and C) and centers of high-centered polygons (in Site B and C); while centers and troughs of low-centered polygons had values of d_{θ} , > 1. (Fig. 15). The downscaling factor for Site D had an overall value greater than 1.0 without a dominant spatial pattern of $\overline{d_{\theta}}$ in comparison to the other three sites because of an absence of troughs at Site D (Table 1). The estimated d_{ρ} map showed imprints of 20 a coarse grid cell for certain portions of the domain (Fig. 15a). In order to capture the temporal variation in the downscaling factor, we fitted the following linear regression to relate the downscaling factor for each fine grid cell with the simulated coarse resolution soil moisture:

²⁵
$$d_{\theta}(i, j, t) = \lambda_1 \theta_{8m}(i^*, j^*, t) + \lambda_0$$

Discussion Paper

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Discussion Paper

(9)

(10)

where λ_0 and λ_1 are best-fit coefficients. Daily absolute relative error in soil moisture, $\varepsilon(d_{\theta})$, is computed between the estimated, $\theta_{0.25 \text{ m}}^{d_{\theta}}$, and simulated, $\theta_{0.25 \text{ m}}$, values at the fine-resolution as:

$$\varepsilon(d_{\theta}) = \left| \frac{\theta_{0.25\,\mathrm{m}}^{d_{\theta}} - \theta_{0.25\,\mathrm{m}}}{\theta_{0.25\,\mathrm{m}}} \right| \times 100 \tag{11}$$

⁵ The maximum and mean $\varepsilon(d_{\theta})$ for all study sites are < ±0.34 and < ±0.03%, respectively (Table 5). Additionally, we used a temporally averaged downscaling factor to estimate daily fine-scale soil moisture fields; maximum and mean $\varepsilon(\overline{d_{\theta}})$ are < ±3.78 and < ±0.16%, respectively.

With the demonstrated success of $\overline{d_{\theta}}$ in estimating fine-scale soil moisture from coarse resolution simulations, we developed a second downscaling approach by relating the mean soil moisture downscaling factor with the DEM. Downscaling factors are computed using the same approach as for d_{θ} for three DEM characteristics: elevation (d_{e}), slope (d_{s}), and curvature (d_{c}) for each study site. A pair-wise linear regression analysis between d_{θ} and the three DEM characteristics showed an existence of a strong linear relationship between d_{θ} and d_{e} (Fig. 16), while a linear relationship is not found between d_{θ} - d_{s} and d_{θ} - d_{c} . We next estimated daily snapshots of fine-resolution soil moisture based on d_{θ} obtained from linear relationship of d_{e} (Fig. 17). The maxi-

- mum and mean error in estimated soil moisture using d_{θ} based on DEM characteristics for all study sites are < ± 5.24 and < $\pm 0.88\%$, respectively (Table 5).
- ²⁰ Even though both downscaling approaches can accurately capture spatial distributions of soil moisture at the finest resolution (with mean error < ±1%), the first downscaling method is able to accurately preserve fine-scale soil moisture variance for all study sites, while second downscale method significantly underestimates σ_{θ}^2 (Fig. 18). Additionally, the first downscaling method is able to reproduce scaling behavior of soil
- ²⁵ moisture variance as obtained by fine-scale simulation, while the second method underestimates this relationship. The reason for the failure of the second downscaling



approach can be explained on the basis of the $\overline{\theta} - \sigma_{\theta}^2$ relationships. It is evident from Fig. 8 that mean and variance of soil moisture exhibit a non-monotonic relationship and use of time-invariant downscaling factors is unable to capture the non-monotonicity of the $\overline{\theta} - \sigma_{\theta}^2$ relationship. Additionally, the first downscaling approach is able to more accurately estimate soil moisture variance as a function of resolution (Fig. 19). While the second downscaling method has the advantage of relying solely on fine- and coarse-resolution. Future studies will attempt to develop the $\overline{\theta} - \sigma_{\theta}^2$ solely based on DEM characteristics at the two resolutions.

3.4 Impact of vegetation heterogeneity of fine scale soil moisture simulation

The results presented in previous Sects. 3.1–3.4 assumed no heterogeneity in vegetation cover and applied a horizontally homogenous evapotranspiration sink within the subsurface domain of PFLOTRAN model. As reported by Gangodagamage et al. (2014), our study site has varying vegetation types that are associated polyg-¹⁵ onal landscape features: mosses and sedges are mostly present in wetter parts of the domain (troughs and centers of low-centered polygons); while lichen and shrubs mainly cover drier areas (rims of low-centered polygons and centers of high-centered polygons). As a first step to account for vegetation heterogeneity, we spatially varied the evapotranspiration sink based on the vegetation distribution. Based on the scal-

- ²⁰ ing factor (Sect. 3.3; Fig. 15), the evapotranspiration sink was increased (decreased) by 50% for regions with d_{θ} greater (less) than 1. A set of additional PFLOTRAN simulations was performed with modified ET for all four sites at 0.25 [m]. Soil moisture variance with and without vegetation heterogeneity did not show any appreciable differences across all four sites (Fig. 20). The lack of contrast within the simulation results
- when heterogeneous vegetation cover was accounted for may be attributed to several reasons: (1) evapotranspiration sinks in the high Arctic are low, (2) the imposed simple



vegetation cover (50 % higher or lower ET) oversimplified the natural system, and (3) soil moisture-vegetation feedbacks were not accounted for.

4 Summary and conclusions

In this study, we analyzed multi-year surface–subsurface isothermal flow simulations during summer months for four polygonal ground study sites near Barrow, AK. PFLO-TRAN simulations are performed at six different spatial resolutions for each of the four study sites. We analyzed simulation results to characterize spatial scaling of statistical moments for soil moisture and developed relationships to predict those statistical moments at fine-resolution from coarse-resolution simulations. Although coarse-resolution

simulations are able to accurately represent mean soil moisture, soil moisture variance is significantly under estimated in coarser-resolution simulations. Soil moisture variance decreased at coarser resolution due to loss of information content of slope and curvature of the underlying DEM. However, the observed decrease in soil moisture variance in coarser-resolution simulations is greater than the decrease in soil moisture to variance obtained by coarsening out the fine-resolution simulation.

A concave relationship between soil moisture mean and variance without a hysteresis effect is predicted. The PDF of topography and soil moisture are strongly inversely correlated and a method to obtain the fine-resolution soil moisture PDF from coarseresolution simulations is developed and tested. The inferred soil moisture PDF accurately represented the fine-resolution simulated PDF. The moments computed from the

rately represented the fine-resolution simulated PDF. The moments computed from the inferred soil moisture PDF were in very good agreement when compared to moments derived from fine-resolution simulations.

Several important caveats need to be acknowledged regarding our results. Our simulations assumed a static active layer depth corresponding approximately to the maximum seasonal value seen at the NGEE-Arctic sites. Although we included a first-order estimate of vertical heterogeneity in soil types, horizontal heterogeneity and vertical heterogeneity associated with cryoturbative mixing were neglected. The evapotranspi-



ration flux is prescribed from an offline CLM simulation, implying that we were unable to account for soil moisture-ET feedbacks and horizontal heterogeneity in vegetation type. Although we believe that our basic conclusions regarding polygonal tundra soil moisture spatial structure and topographic controls are valid, future work should char-⁵ acterize the impacts of these simplifications on our conclusions.

Finally, though the method to estimate the soil moisture probability density function from coarse-resolution simulations is accurate, that method is unable to retrieve the spatially explicit dynamic fine-resolution soil moisture field. We therefore presented two methods to map simulated coarse resolution soil moisture data onto fine resolution

- ¹⁰ grid using downscaling factors. The first downscaling approach, based on fine- and coarse-resolution simulations, is able to capture mean and variance of soil moisture at fine resolution. The second downscaling approach, which relied only on DEMs at the two resolutions, is able to capture spatial pattern θ , but underestimates soil moisture variance. We are presently exploring additional methods to infer the spatial structure
- of soil moisture at fine resolution from coarse-resolution simulations using a Principal Orthogonal Decomposition method (Pau et al., 2014). The ultimate goal of using fine-resolution simulations to improve prediction of coarse-resolution hydrological and biogeochemical exchanges with the atmosphere requires further work to develop fineresolution models of representative landscapes, develop ROMs from these models,
- and integrate those ROMs into a coarser-resolution land model. We believe such an approach is a viable method to represent fine-resolution heterogeneity in climate-scale land models.

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Table 1. Characteristics of NGEE-Arctic study sites	.
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Site	Polygonal characteristics	Mean elevation [m]	Standard deviation of elevation [m]
Α	Low centered polygons with troughs	4.66	0.10
В	High centered polygons	4.68	0.12
С	Transitional polygons	4.44	0.12
D	Low centered polygons without troughs	4.27	0.07



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Table 2. van Genuchten model parameters used to fit data reported in Hinzman et al. (1991).

	0–5 cm	5–10 cm	20–25 cm
$\theta_{\rm s} [{\rm m}^3 {\rm m}^{-3}]$	0.9	0.86	0.55
$\theta_{\rm r} [{\rm m}^3 {\rm m}^{-3}]$	0.05	0.05	0.05
$\alpha [{\rm m}^{-1}]$	2.0	1.0	1.5
$K_{\rm sat}$ [cm min ⁻¹]	1.1640	0.6240	0.0564
n [–]	1.35	1.35	1.25

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Table 3. Bias and correlation (R^2) for soil moisture moments computed from PFLTORAN simulations at multiple resolutions and cubic polynomial curve relationship (described in Sect. 3.2).

	2nd Central Moment		3rdCentral Moment		4th Central Moment	
	Bias	R^2	Bias	R^2	Bias	R^2
А	-0.03%	0.999	0.52%	0.999	-0.14%	0.997
В	-0.08 %	0.997	-3.04 %	0.998	-0.35 %	0.996
С	-0.08 %	0.993	-0.94 %	0.994	-0.33 %	0.989
D	-0.26 %	0.982	-0.55 %	0.976	0.07 %	0.974

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Table 4. Bias and correlation (R^2) for moments computed from the soil moisture probability density function based on fine-resolution simulations and estimated PDF from coarse-resolution simulations (described in Sect. 3.2).

	1st Moment		2nd Central Moment		3rd Central Moment		4th Central Moment	
	Bias	R^2	Bias	R^2	Bias	R^2	Bias	R^2
Α	1.43%	0.996	1.80%	0.996	2.19%	0.995	2.58%	0.994
В	1.73%	0.996	2.42%	0.996	3.12%	0.995	3.82 %	0.994
С	0.31 %	0.994	-0.44 %	0.993	-1.18%	0.993	-1.93 %	0.992
D	0.72%	0.999	0.42%	0.999	0.12%	0.999	-0.17%	0.998

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Table 5. Maximum and mean absolute error between simulated soil moisture field at 0.25 m and estimated soil moisture based on three types of downscaling factors.

Dow	nscaling factor		А	В	С	D
Based on	Temporal resolution					
Simulation	Varying in time	Maximum error	0.23 %	0.34 %	0.28 %	0.16%
		Mean error	0.02 %	0.02 %	0.03%	0.01 %
Simulation	Constant in time	Maximum error	2.40 %	2.19%	3.78 %	2.57 %
		Mean error	0.12%	0.16%	0.12%	0.08%
DEM	Constant in time	Maximum error	3.23 %	5.24 %	4.50 %	3.30 %
		Mean error	0.65 %	0.88%	0.61 %	0.28 %



Figure 1. LIDAR DEM for the four NGEE-Arctic study sites.







Figure 2. Fitted van Genuchten model (in red) to data (in blue) reported in Hinzman et al. (1991).



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Figure 3. Time series of meteorological forcing dataset for summer months (June–September) of 1998–2002 used for PFLOTRAN simulations: (a) daily evapotranspiration flux; (b) daily rain rate; and (c) cumulative daily rainfall.





Figure 4. DEM for Site B (top row) and Site C (bottom row) at 0.25, 1, and 8 m resolutions.





Figure 5. Time series of simulated mean soil moisture for the four NGEE-Arctic study sites.













Figure 8. Soil moisture mean vs. variance at all four sites using finest resolution simulation for entire study period.



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Figure 9. Simulated soil moisture variance vs. elevation variance at different mean soil moisture levels.





Figure 10. Slope of linear relationship between soil moisture variance – topography variance (computed from data presented in Fig. 9) vs. mean soil moisture bin.





Figure 11. Soil moisture variance vs. scale factor for simulated soil moisture at Site-A for driest (blue) and wettest (red) day in 1999. A dashed line shows results obtained by performing PFLO-TRAN at different spatial resolutions, while a solid line shows results obtained by aggregating 0.25 m PFLORAN simulation to coarser resolutions.





Figure 12. (a) DEM; and **(b)** simulated soil moisture distribution for driest day (t = 74 d) in 1999 at Site A.





Figure 13. PDF for soil moisture at Site A for 1999 based on 0.25 m simulation (solid line) and inferred PDF using 8 m simulation (circle symbol).





Figure 14. Comparison of soil moisture moments computed from estimated PDF and fine-scale simulations for Site A.





Figure 15. Mean downscaling factor for the four NGEE-Arctic sites.





Figure 16. Linear relationship between downscaling factors for elevation (d_e) and soil moisture (d_{θ}) for all four NGEE-Arctic sites.





Interactive Discussion



0.44

0.45



Figure 18. Comparison of simulated soil moisture variance obtained for DEM at 0.25 [m] with estimated soil moisture fields at finest resolution via two downscaling approaches.





Figure 19. Soil moisture variance vs. scale factor for simulated soil moisture at Site A for the driest in 1999. Results are shown for (i) PFLOTRAN simulation at different spatial resolutions, (ii) aggregation of 0.25 m PFLORAN simulation to coarser resolutions, and aggregation of estimated fine-scale simulation obtained by (iii) first downscaling method and (iv) second downscaling method.





Figure 20. Comparison of simulated soil variance with and without vegetation heterogeneity for simulations performed at 0.25 [m].



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