

1 **The Question of Sudan: A Hydroeconomic Optimization**

2 **Model for the Sudanese Blue Nile**

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13 **Key points:** Multi-objective optimization; Hydroeconomic modeling; Climate Change

14 effects on hydrology; Nile River

15 **Abstract:**

16 The effects of development and the uncertainty of a changing climate in East Africa pose

17 myriad challenges for water managers along the Blue Nile. Sudan's large irrigation

18 potential, hydroelectric dams, and prime location within the basin mean that Sudan's

19 water management decisions will have great social, economic and political implications

20 for the region. At the same time, Sudan's water use options are constrained by tradeoffs

21 between upstream irrigation developments and downstream hydropower facilities as well

22 as by the country's commitments under existing or future transboundary water sharing

23 agreements. Here, we present a model that can be applied to evaluate optimal allocation

24 of surface water resources to irrigation and hydropower in the Sudanese portion of the

25 Blue Nile. Hydrologic inputs are combined with agronomic and economic inputs to

26 formulate an optimization model within the General Algebraic Modeling System

27 (GAMS). A sensitivity analysis is performed by testing model response to a range of

28 economic conditions and to changes in the volume and timing of hydrologic flows.  
29 Results indicate that changing hydroclimate inputs have the capacity to greatly influence  
30 the productivity of Sudan's water resources infrastructure. Results also show that the  
31 economically optimal volume of water consumption, and thus the importance of existing  
32 treaty constraints, is sensitive to the perceived value of agriculture relative to electricity  
33 as well as to changing hydrological conditions.

34 **1. Introduction:**

35           The Nile Basin spans parts of 11 different countries in one of the most  
36 underdeveloped regions in the world. The transboundary nature of the Nile presents  
37 water-sharing challenges between upstream and downstream riparian nations (Waterbury  
38 et al. 1998). This is particularly true in the Eastern Nile basin, which is typically defined  
39 as the tributaries that arise in the Ethiopian Highlands—primarily the Blue Nile, Tekeze-  
40 Atbara, and Baro-Akobo-Sobat—together with the main stem Nile north of Khartoum  
41 (Figure 1). The Eastern Nile tributaries collectively contribute over 80% of flow in the  
42 main stem Nile. The Eastern Nile basin also exhibits strong hydrological connectivity, in  
43 that upstream climate variability and development directly impact downstream resources  
44 in a manner that is not observed in the White Nile system, where lakes and wetlands  
45 serve as a buffer between the Equatorial Lakes headwaters region and downstream water  
46 deficit areas in Sudan and Egypt (Blackmore & Whittington 2008). For this reason the  
47 utilization of Eastern Nile waters has long been a source of transboundary tension, most  
48 notably between Egypt, which claims historical rights to the majority of Nile River water,  
49 and Ethiopia, which has a strong interest in developing the Eastern Nile tributaries for  
50 hydropower and other uses.

51           While the diplomatic tensions between Egypt and Ethiopia have dominated the  
52 political and media discourse on Eastern Nile basin development (Cascao 2008, Igunza  
53 2014, Hussein 2014, Gebreluel 2014), Sudan has the greatest potential to influence  
54 transboundary distribution of water resources. The 1959 Nile Waters Agreement grants  
55 Sudan the right to use 18.5 billion cubic meters (bcm) of Nile water per year. At present,  
56 however, Sudan uses less than this allocation; its actual water demand has been estimated

57 to be approximately 16.1 bcm per year (Jeuland 2010). This value could change in the  
58 future, both through internal development decisions and through external influences such  
59 as climate change and upstream infrastructure in Ethiopia. Where climate change has the  
60 potential to alter the magnitude of Blue Nile inflow and local evaporative demand,  
61 upstream infrastructure would be expected to regularize the timing of flows and to reduce  
62 silt load entering Sudan. Silt accumulates over time in the reservoir and reduces the  
63 volume of reservoir. This affects hydropower production, reduces the available water for  
64 irrigation, imposes dredging costs, and reduces flood control capabilities.

65 In this context, there is a need for analytical tools focused on Sudan's hydro-  
66 development options. In particular, it is important to understand how impending changes  
67 affecting the Sudanese portion of the Eastern Nile basin, including climate change and  
68 upstream development in Ethiopia, are likely to affect Sudan's use of its Nile River  
69 resources for hydropower and irrigation. The objective of this paper is to present an  
70 optimization model that illustrates the sensitivities of Sudan's Blue Nile and main stem  
71 Nile water resources infrastructure to changes in climate and upstream development.

## 72 *1.1 The Blue Nile in Sudan*

73 Approximately 60 bcm of water flows annually from the Blue Nile basin in  
74 Ethiopia to Sudan. Inter-seasonal variability is large, with flows peaking in August and  
75 September, and inter-annual variability is also considerable—gauged flow at Roseries  
76 (Figure 1) has an inter-annual variability equal to 25% of the mean flow. The basin is  
77 also undergoing climate change that has had a significant impact on temperature but, as

78 of yet, no clear directional impact on total annual precipitation or river discharge. In  
79 coming decades, climate change impacts on basin hydrology are expected to become  
80 more significant.

81         The magnitude, seasonality, and even directionality of this change, however, are  
82 highly uncertain. Global Climate Models (GCM's) participating in the 5<sup>th</sup> Coupled Model  
83 Intercomparison Project (CMIP5; Taylor 2012) exhibit no consensus on projected  
84 change. A recent study of 10 CMIP5 models revealed projected precipitation change in  
85 the Blue Nile headwaters ranged from an increase of almost 40% by the mid 21<sup>st</sup> century  
86 relative to late 20<sup>th</sup> century to a decrease of approximately 40% at the same time period  
87 (Bhattacharjee and Zaitchik, 2015). Interestingly, some of the models with the most  
88 widely diverging projections demonstrate reasonably good representation of current  
89 climate patterns and variability for commonly used model evaluation metrics  
90 (Bhattacharjee and Zaitchik, 2015). This range of uncertainty is evident in previous  
91 multimodel comparison studies as well, as past analysis have found 21<sup>st</sup> century change  
92 in Upper Blue Nile basin flows ranging from 133% to -35% and precipitation ranging  
93 from 55% to -9% (Yates and Strzepek 1998). Other studies of selected GCM's have  
94 found a smaller range of uncertainty, but no consensus on direction of change: Elshamy  
95 et al. (2008) examined 17 selected GCM's for the period 2081-2098 and found flow  
96 changes ranging from -15% to 14%, while Nawaz et al. (2010), analyzed the output of  
97 three GCM's and deduced that the mean annual Blue Nile runoff would change by +15%,  
98 1% or -9% by the year 2025. Analysis conducted by Taye et al. (2010) projected future  
99 climate scenarios and ran them through two hydrologic models for two catchments  
100 representing source regions of the Blue and White Nile. Results illustrated a large range

101 in the projected flows from the baseline for both basins. Changes in projected mean  
102 annual flows from the Blue Nile catchment range from approximately -80% to 70%.

103 In addition to climate change, proposed infrastructure projects will drastically  
104 alter the nature of downstream flows. There are currently no large structures along the  
105 main stem of the Blue Nile in Ethiopia, but the western portion of Ethiopia holds  
106 tremendous hydro-electric potential (Guariso et al 1987). The Ethiopian government has  
107 had plans to increase utilization of this energy source since at least 50 years ago, when  
108 the concept of a cascade of hydroelectric dams on the Blue Nile was first proposed  
109 (Bureau of Reclamation 1964, and Guariso et al 1987). The concept of a cascade of dams  
110 is still of interest to Ethiopia, but at present the country's development energies are  
111 focused on construction of the Grand Ethiopian Renaissance dam (GERD), located at the  
112 border with Sudan (Figure 1). The GERD will be the Largest dam in Africa, holding back  
113 more than 60 billion cubic meters of water, and is expected to generate more than 5000  
114 MW of electricity (Hammond 2013). The construction of this dam will affect many  
115 aspects of water sharing in the region and raises numerous questions about its effects on  
116 downstream riparian nations.

117 Sudan has one large dam on the main stem Nile—the 1250 MW capacity, 67  
118 meter high Merowe dam, located 800 kilometers north of Khartoum near the fourth  
119 cataracts (Teodoru, 2006). In addition to Merowe, Sudan has two large dams along the  
120 Blue Nile reach, at Roseires and Sennar. Roseires was constructed in 1966 (Chesworth et  
121 al, 1990) with a capacity to generate 280 MW of electricity. Recent construction  
122 heightened the dam and increased the reservoir volume from 3.3 bcm to more than 7 bcm  
123 (McCartney et al. 2009). The Sennar dam was constructed in 1925 and holds back 900

124 million cubic meters of water (McCartney et al. 2009). Both dams were constructed to  
125 regulate flows that feed into multiple irrigation schemes, among them is the 800,000  
126 hectare (ha) Geziera scheme. The Geziera was constructed by the governing British  
127 magistrate in 1925 as the largest single irrigation scheme in the world at the time (Bernal  
128 1997). The dams also supply various schemes in Rahad and Suki as well as upstream and  
129 downstream of Sennar (McCartney et al. 2009). The Merowe dam (Figure 1) is located  
130 further downstream, in the cataracts of the main stem Nile in northern Sudan. This is a  
131 highly arid area and the dam's primary purpose is hydropower rather than irrigation. It  
132 was constructed in 2009 and now supplies the majority of Sudan's hydroelectric power.

133 All discussions of Nile flow and water resource development take place on the  
134 background of a complex and lengthy history of colonial and post-colonial era  
135 negotiations (Swain 1997). The most recent legally binding treaty involving Sudan is the  
136 1959 Nile Waters Agreement, under which Sudan and Egypt agreed to divide the average  
137 flow of 84 bcm at the old Aswan dam between the two countries: 55.5 bcm to Egypt, 10  
138 bcm to evaporation losses, and 18.5 bcm to Sudan. The treaty also granted Sudan  
139 permission to build a dam at Roseries. The agreement was limited to the two downstream  
140 nations and does not include any upstream riparian countries, and for this reason it is  
141 generally not recognized by the other countries on the Nile.

## 142 *1.2 Hydroeconomic Modeling in the Nile basin*

143 Hydro-economic models integrate natural hydrologic dynamics, infrastructure,  
144 and management options in a framework of economic costs and benefits. They are  
145 particularly valued in complex water management problems because they provide a

146 dynamic analysis of water resources and needs that guides basin managers and  
147 stakeholders towards an economically optimal management strategy in place of  
148 traditional, static systems based on water rights and fixed allocations (Harou et al., 2009).  
149 The core structure of most river basin hydroeconomic models is roughly similar: flows  
150 pass through a network of rivers and canals (or aquifers) and encounter nodes that  
151 represent resource infrastructure, such as reservoirs, abstraction sites, hydroelectric  
152 facilities, etc. But there is considerable diversity in the conceptual approach (simulation  
153 vs. optimization), representation of time (deterministic, stochastic, or dynamic), manner  
154 in which submodels are integrated to the hydroeconomic solution (modular vs. holistic),  
155 and, for optimization models, in the optimization objective function and algorithm  
156 (Harou et al., 2009).

157         Not surprisingly, the Nile River basin has been a common and important target for  
158 hydroeconomic analyses. One relatively early effort was reported in Guariso et al. (1987),  
159 in which a linear optimization model was implemented to evaluate the effect of the long-  
160 discussed cascade of hydroelectric dams on the Ethiopian Blue Nile on overall benefit  
161 and on water economics in Sudan and Egypt. The optimization objectives of this model  
162 were to maximize hydropower production in Egypt, Sudan and Ethiopia, as well as  
163 downstream agricultural water supply. Simulations indicated that there was minimal  
164 tradeoff between the two competing objectives. Thus, Ethiopia's increased hydropower  
165 output would have a minor adverse effect on downstream riparian nations, but upstream  
166 flow regulation also had benefits for downstream riparian nations, including the fact that  
167 an increase in upstream flow regulation would decrease water levels in the highly  
168 evaporative downstream reservoirs, thus increasing total water availability for



169 downstream riparian nations. This finding has been confirmed by subsequent modeling  
170 studies (e.g., Blackmore and Whittington 2008) and plays a role in studies that investigate  
171 the benefits of cooperation in the basin (Whittington 2004).

172 Another influential and relatively early optimization model for the Nile is the Nile  
173 Decision Support Tool (DST) which was developed by the Georgia Water Resources  
174 Institute. This model performs a basin wide hydrological and hydraulic simulation along  
175 with reservoir optimization capabilities and scenario assessment (Yao and Georgakakos,  
176 Georgakakos 2007). The optimization model in DST utilizes the extended linear  
177 quadratic Gaussian (ELQG) control method in order to perform a stochastic multi-criteria  
178 optimization that aims to find the optimal reservoir operation (Georgakakos 1987, 1989).  
179 A more recent basin-wide hydroeconomic optimization model, the Nile Economic  
180 Optimization Model (NEOM), was presented by Whittington et al. (2005) using GAMS  
181 software. This model was used to assess the economic implications of various  
182 infrastructural developments within the basin and aims to maximize for basin wide  
183 economic benefits due to irrigation and hydropower production. The authors quantify the  
184 economic benefit of cooperation by comparing the total benefits calculated from current  
185 allocation, with the total benefits derived from full communication and cooperation  
186 between various riparian nation states. They found that cumulative economic benefits for  
187 all players more than doubled the realized total benefit from \$4.1 billion in the status quo  
188 scenario to more than \$9 billion when all nations are fully cooperating.

189 Other recent modeling efforts have focused on a subset of the basin and  
190 investigated problems of dynamic and transient system management. In the Eastern Nile,  
191 Goor et al. (2010) present a dynamic reservoir optimization model that employs a

192 Stochastic Dual Dynamic Optimization Program (SDDP). The model identifies the most  
193 economically efficient policies for large scale reservoirs (Goor et al. 2010). Block and  
194 Strzepek (2010) focus on the Ethiopian Blue Nile, implementing an Investment Model  
195 for Planning Ethiopian Nile Development (IMPEND) that calculates the economic  
196 benefit of proposed development under changing climatic conditions. IMPEND has the  
197 ability to model the transient filling stages of the dams, as well as the stochastic nature of  
198 the climate variables, allowing for a focus on the transient nature of the development  
199 process, an aspect of water management that is absent from most other hydroeconomic  
200 models of the basin. Block and Strzepek (2010, 2012) apply the model to climate change  
201 analysis and find that the omission of this transient period in models result in the  
202 overestimation of total net benefits by more than \$6 billion, as well as a significant  
203 change in the benefit to cost ratio of the project. Block and Strzepek (2010) also highlight  
204 changes in the hydrology that are neglected in models with no filling process: reservoir  
205 filling scenarios require that up to 170% more water be retained in Ethiopia over 30 years  
206 compared to scenarios where the reservoirs are assumed to already be filled.

207 More recently Jeuland (2010) and Jeuland and Whittington (2014) present  
208 hydroeconomic simulations that analyze decision making within the Nile basin under a  
209 changing climate. Jeuland (2010) presents a basin-wide hydroeconomic framework that  
210 integrates a stochastic flow generator, a hydrological simulation model and an economic  
211 model for the Nile. His analysis shows that varying specific economic and physical  
212 parameters combine to have a substantial impact on net present value. Jeuland and  
213 Whittington (2014) present long term planning hydropower investment options within  
214 Ethiopia under varying hydrological conditions. By using simulations, the authors are

215 able to develop performance metrics for the different options, and show that results are  
216 dependent on the decision makers' risk preference.

217         The Sudan Hydro-economic Optimization Model (SHOM) presented in this paper  
218 is intended to provide a complementary perspective on optimal water resource decision-  
219 making in the Eastern Nile. In contrast to earlier modeling efforts, we focus specifically  
220 on the Sudanese portion of the Blue Nile and the main stem Nile north of Khartoum. We  
221 do this because Sudan is a relatively understudied and a pivotal player in Nile water  
222 resource management. In addition, we use a non-linear optimization model (see section 2)  
223 that maximizes economic benefits and assesses trade-offs between hydropower  
224 production and irrigation within Sudan.

## 225 **2. Methods:**

### 226 *2.1 The SHOM Optimization Model*

227         The General Algebraic Modeling System (GAMS) is front-end software that can  
228 be used to solve non-linear multi-objective optimization problems by calling various  
229 solvers. By using the reduced gradient method in the CONOPT solver, the model seeks a  
230 stationary point while reducing the number of variables by conducting a variable  
231 selection processes. By curtailing the number of variables and linearizing the non-linear  
232 constraints via a Taylor series approximation, the algorithm simplifies the problem and  
233 solves for the non-linear objective (Drud, 1992).

234         SHOM runs on monthly time steps. In this implementation the simulation network  
235 includes 2 dams located on the Blue Nile reach (Roseires and Sennar), 1 dam on the main  
236 stem Nile (Merowe), and agriculture is represented by 5 irrigation schemes corresponding

237 to existing developments along the Blue Nile (Figure 2). The combined storage volume  
238 of all dams is approximately 20 bcm, and the total irrigable area is 1.4 million ha. Tables  
239 1 and 2 define all the parameters and variables in SHOM.

#### 240 2.1.1 Objective Function:

241 The objective function of SHOM consists of two objectives which it seeks to  
242 maximize: agricultural and hydropower net benefits. Benefits refer to the total economic  
243 value attributed to each respective year summed over the twenty year run period. As  
244 noted by Whittington et al. (2005), the meaning of “value” takes more than one form. In  
245 this paper, the total net benefit attributed to the economic value of water is defined by the  
246 objective function and incorporates the benefits at each site location. Thus the total value  
247 of water is seen from the perspective of the producer (the State) and not from the  
248 perspective of the consumer. The objective function, illustrated below (Equation 1),  
249 represents the economic benefits from the agricultural and hydropower sectors. The total  
250 benefit attributed to hydropower production assumes infinite demand and is calculated as  
251 the total hydropower produced times the price per kilowatt hour. Initial dam  
252 infrastructural cost, cost of energy transmission and cost of dredging are not included in  
253 the objective function. Furthermore it is assumed in the sensitivity analysis presented in  
254 this paper that the price of electricity is fixed. Thus:

$$255 \quad \text{Objective} = \max \sum_{m,y} (D^y * bi_{m,y} + D^y * bh_{m,y}) \quad (1)$$

256 where,  $D^y$  = discount rate,  $bi_{m,y}$  is the total benefits from Irrigation,  $bh_{m,y}$  is the total  
257 benefits from hydropower, and all variables are dependent on month( $m$ ) and year( $y$ ).

#### 258 2.1.2 Hydropower Constraints:

259 Total hydropower generation ( $KWH_{l,m,y}$ ) is dependent on two variables (Equation  
 260 2), the amount of water passing through the turbines at any given time step ( $rhe_{l,m,y}$ ), and  
 261 the total height of water in the dam that forces water through the turbines ( $h_{l,m,y}$ ). (Cohon  
 262 2003, Loucks et. al 1981).

$$263 \quad \forall_{l,m,y}, KWH_{l,m,y} = c * effh * n * rhe_{l,m,y} h_{l,m,y} \quad (2)$$

264 Production of hydropower is constrained by the dam's generation capacity, thus any  
 265 additional release is categorized by the model as non-hydropower release.  $effh$  is the  
 266 efficiency of the dams, which was assumed to be 0.85 in the model. There is also a  
 267 conversion factor (c),  $c = 2.61 \times 10^{-3}$ .

268 As shown in Equation 3, total hydropower benefits for each month in each year is  
 269 dependent on the price of hydropower (P) and the sum of hydropower produced at all  
 270 dam locations ( $l$ ).

$$271 \quad bh_{m,y} = \sum_l (P * KWH_{l,m,y}) \quad (3)$$

### 272 2.1.3 Irrigation Constraints:

273 The water used for irrigation ( $i_{l,m,y}$ ) is dependent on the crop water requirement  
 274 (i.e. the volume of water needed per unit area of crop cultivated), and the area irrigated  
 275 during cropping season. Values of crop water requirement (Water) were drawn from a  
 276 World Bank report (Plusquellec 1990). The area irrigated ( $Area_{c,l,m,y}$ ) fluctuates  
 277 annually but remains constant during the cropping season (Equation 4). Therefore, the  
 278 volume of water allocated for irrigation:

$$279 \quad i_{l,m,y} = \sum_c (effi_c * Water_{c,l,m,y} * Area_{c,l,m,y}) \quad (4)$$

280 Efficiency of irrigation was assumed to be dependent on the crop type (Table 1) Elamin  
 281 et al. (2011). (NB: The agricultural output in the objective function is irrigation fed; rain-

282 fed agriculture was not considered). Therefore the total benefits due to irrigation for each  
283 m, at each y is:

$$284 \quad bi_{m,y} = \sum_{c,l}(effi_c * v_c * Water_{c,l,m,y} * Area_{c,l,m,y}) \quad (5)$$

285 where  $v_c$  is the marginal value of water for each crop (see section 2.2.1 for more details.)

286 Finally, per the 1959 Nile agreement Sudan's portion of withdrawals is limited to 18.5

287 bcm of water annually. Since our model is restricted to portions of the Blue Nile, we

288 assume the maximum bounds to be 14.5 bcm (Equation 6). This approximation is based

289 on the relative contribution of Blue Nile flows to the Nile system, and the recognition that

290 the largest irrigation schemes in Sudan are located along the Blue Nile. Thus for a

291 simulation of  $Y$  years the total water consumed by Sudan should be:

$$292 \quad \sum_{l,m,y}(i_{l,m,y}) + \sum_{l,m,y}(e_{l,m,y}) \leq Y * 14.5 \text{ bcm} \quad (6)$$

293 A second constraint is included in the model to ensure Egypt's share and to prevent a

294 large intake during drought years by ensuring Egypt's fractional share during those years

295 (Equation 7):

$$296 \quad \sum_{l,m}(i_{l,m,y}) + \sum_{l,m}(e_{l,m,y}) \leq 0.28 * \sum_m(R_y) \quad (7)$$

297

298 where  $R$  is the release at Merowe dam.

#### 299 2.1.4 Continuity Constraints:

300 Storage at each dam location can be calculated using simple water balance. The

301 storage at a particular time step is the total water contained in the reservoir in the

302 previous time step plus the water entering each dam minus what comes out of the

303 reservoir through upstream flow (Equation 8). The water entering is the upstream

304 boundary flow or upstream total dam release ( $q_{l,m,y}$  or  $r_{l,m,y}$  respectively), the water leaving

305 each dam node is the current dam release, the irrigated water and water loss due to  
306 evaporation.

$$307 \quad \forall_{l,m,y}, \quad s_{l,m,y} = q_{l,m,y} + r_{(l-1),m,y} + s_{l,(m-1),y} - r_{l,m,y} - i_{l,m,y} - e_{l,m,y} \quad (8)$$

308 NB:  $s_{l,(m-1),y}$  is the storage from the previous time step. When  $m = 1$ , the model uses the  
309 storage from  $s_{l,12,(y-1)}$ . Evaporation in  $\text{m}^3 / \text{m}^2$  (Ev) is estimated using the Thornthwaite  
310 equation (Thornthwaite, 1948), thus the total evaporated volume:  $e = Ev * \text{Dam Surface}$   
311 Area. The storage at each time step must also be less than each dam's respective  
312 maximum volume ( $V_{max}$ ) (Equation 9).

$$313 \quad s_{l,m,y} \leq V_{max} \quad (9)$$

314 Lastly, all the decision variables calculated by the optimization model must satisfy non-  
315 negativity constraints (Equation 10):

$$316 \quad s_{l,m,y}, r_{l,m,y}, i_{l,m,y} \geq 0. \quad (10)$$

## 317 *2.2 Model Parameters:*

### 318 *2.2.1 Marginal Value of Water for Irrigation*

319 Deriving the net benefits due to agriculture requires an intimate knowledge of  
320 both foreign and domestic agricultural economic markets. Calculating prices of output  
321 commodities relative to input production costs for future scenarios would require  
322 accurate price prediction of a non-linear, volatile market. Rather than attempt to analyze  
323 and project costs of agricultural inputs (e.g., water rates, fertilizer, land and labor) or to  
324 simplify tax rules and subsidies currently affecting agricultural prices in Sudan, we assign  
325 marginal water values for agriculture by assuming a horizontal demand curve for the  
326 marginal water values for each crop and that the average value of water equals the  
327 marginal value. The ratio of marginal water values for the crops was calculated using the

328 producer price of the crop ( $P_c$ , FAO 2009), the yield ( $Y_c$ , Ghezze, 1998), and the crop  
329 water requirement (*water*, Plasquelle 1990). To explore the sensitivities of the model we  
330 perform simulations using 6 different sets of marginal water values, with each crop  
331 assigned its own value (P1 – P6; Table 3). These values chosen are illustrative and are  
332 intended to assess the sensitivity of the model and are not meant to reflect the optimal  
333 estimate of current agricultural prices. Therefore the marginal crop values act as weights  
334 within the objective function to develop a tradeoff between the various objectives, as  
335 described in Section 3. For comparison, previous studies within the region have assumed  
336 a horizontal demand curve with an assigned marginal water value of  $0.05\$/\text{m}^3$  for  
337 agriculture (Whittington et al. 2005, Arjoon et al. 2014).

#### 338 2.2.2 Discount Rate ( $D^y$ )

339 Economic analyses of large-scale development projects need to discount  
340 anticipated future benefits relative to near-term costs and benefits forgone. Since the  
341 objective function and decision making in our model is solely based on economics, the  
342 discount rate can greatly influence the final value of the objective function of the model.  
343 To quantify this influence we performed simulations in which discount rate was varied  
344 from 3% to 7%, a range that has a considerable impact on the total value of the objective  
345 function, but not on the overall results. Discount rates may also affect the analysis of our  
346 deterministic hydroeconomic model by front-loading demands. In this model, this  
347 phenomenon is minimized by treaty constraints that limit water allocation for irrigation  
348 (Equations 6 and 7). The same discount rate was applied to both objectives within the  
349 objective function. The results presented in Section 3 used a discount rate of 5% for all  
350 analyses.



351 2.2.3 Simulations

352 We apply SHOM to a set of hydrological and development scenarios to test  
353 sensitivities to changes in flow volume and timing in the Blue Nile as well as to  
354 investigate the influence that changing agricultural practices, electricity markets, and  
355 international agreements might have on optimal water allocations. A list of these  
356 scenarios is provided in Table 4.

357 First, we examine sensitivity to changes in Blue Nile hydrology. As noted above,  
358 there is significant uncertainty in projections of future precipitation patterns—and hence  
359 future river flows—in the Blue Nile basin. For this reason we consider it important to test  
360 model sensitivity to substantial increases (+20%) “High flows” and decreases (-20%)  
361 “Low flows” in river flow, which is within the range of predictions of state of the art  
362 global climate models for the first half of the 21<sup>st</sup> century. These simulations are  
363 compared to an “Observed Flow” simulation based on historic flow rates.

364 In addition, we are interested in how the model responds to temporal smoothing  
365 of inflow from Ethiopia, which might result from the construction of one or more  
366 upstream dams. For this reason we include a third flow scenario, “Smoothed Flows,” in  
367 which the annual total flow is unchanged from present conditions but monthly flow  
368 values are averaged across three months, producing a smoothed hydrograph with less  
369 extreme wet season peaks and dry season troughs.

370 Changes in flows were restricted to the Blue Nile flows only; White Nile flows  
371 remained unchanged. This approach was adopted for multiple reasons. First, the White  
372 Nile originates in the Equatorial Lakes region, which is in a different climate zone. Thus  
373 it is unclear that an increase in Blue Nile flows would translate into an increase in White

374 Nile flows. Second, the White Nile passes through the Equatorial lakes and Sudd  
375 wetland, so that its annual flow is more buffered than the Blue Nile. Lastly, majority of  
376 the water in Egypt originates from the Blue Nile region, so changes in White Nile flow  
377 under climate change would not impact the main stem Nile as significantly as changes in  
378 the Blue Nile.

379         Next, we consider how changing agricultural management practices due to  
380 upstream development might alter optimal allocations under a smoothed flow regime.  
381 Expected upstream development will increase water availability during the dry months,  
382 which will incentivize farmers to change their agricultural practices. This has already  
383 been observed on the Atbara River, just north of the Blue Nile, where construction of a  
384 dam in Ethiopia has led Sudanese farmers to transition from a one cropping season to a  
385 multiple cropping season and to diversify crop types (Personal Communication, Professor  
386 Belay Simane, Addis Ababa University). For this reason we have included simulations to  
387 the smooth flows that add a second cropping season (Table 4 simulation “Smooth2crop”).

388         Third, we examine sensitivity to electricity prices. The construction of a large  
389 upstream structure like the GERD would produce a large amount of hydropower itself,  
390 and in a connected electricity market this would drive down the price of electricity. The  
391 GERD, for example, is expected to generate electricity that can be sold to Sudan at a  
392 reduced price, about 4 cents a KWh (Hai 2013). To account for this dynamic in general  
393 terms, we include a model simulation “SmoothPower” in which flow is smoothed and the  
394 price of electricity is cut by half from 8 cents per KWh to 4 cents per KWh (see Table 4).  
395 We also consider how this change in power price might interact with a change in  
396 cropping practices in simulation “SmoothPower2Crop.”

397 Finally, we introduce simulations in which there is upstream flow control, the  
398 opportunity for double cropping, and a relaxation of the downstream constraint. This  
399 relaxation, which we call “No Agreement” (NA), removes the requirement that Sudan  
400 provide adequate flow to Egypt in dry years—i.e., our second “treaty” constraint from  
401 section 2.1.3 (Equation 7). These simulations were performed for both high and low  
402 electricity prices: “Smooth2CropNA” and “SmoothPower2CropNA.” Removing the  
403 second constraint allows us to examine the impact that downstream delivery requirements  
404 have on Sudan’s optimal water allocations while keeping the total water use relatively  
405 similar to the baseline simulations, which facilitates comparisons between simulations.

406 All simulations in the sensitivity analysis were run for 20 years. To generate  
407 hydrological inputs for these simulations a 70 year record of monthly observed Blue Nile  
408 flows at Roseires was obtained from the Global Runoff Data Center ([www.grdc.org](http://www.grdc.org)).  
409 This record was randomly resampled to generate 1000 20-year timeseries of  
410 representative flow patterns. Interannual autocorrelation is insignificant (lag -1  
411 autocorrelation is 0.165) for this hydrological timeseries dataset, thus the distortive effect  
412 of resampling is minimal. The mean flow for all 1000 bootstrapped timeseries were  
413 assembled and ranked, thus defining the 5% and 95% confidence levels of flows for the  
414 20 year observed period. The model output was assessed using these confidence intervals.

415 **3. Results and Discussion:**

416 *3.1 Model Behavior*

417 To demonstrate general model behavior we first examine a 20-year demonstration  
418 simulation that uses bootstrapped historical flows and the P5 set of marginal water values  
419 (see Table 3). Hydrologic fluxes and storages at the three dams in the simulation  
420 (Roseires, Sennar, and Merowe) and for major irrigation areas are shown in Figures 3 and  
421 4.

422 Figure 3A shows the observed 20 year flows for the Blue Nile at the Sudan-  
423 Ethiopia border. Fluctuations of flows are illustrative of the wet and dry seasonal pattern,  
424 and annual flows also vary significantly, from -26% to 26% of the mean. This record  
425 shows two distinct periods of below average annual flows (months 70-120 and months  
426 190-240). The dam storage and release values reflect a response by the model to these  
427 periods of interseasonal dryness and wetness. The smaller dams (Roseires and Sennar)  
428 are emptied and filled annually (Figures 3B) with Merowe remaining relatively full year  
429 round in all years, with minor drops in its storage level during the dry months. Therefore  
430 there is no significant connection between the hydropower releases at Merowe and inter-  
431 annual variability. There is a significant connection between dry periods and hydropower  
432 release at Roseires. This is illustrated by lower hydropower releases during the periods of  
433 dry annual flows than during the wet periods (Figure 3C).

434 Figure 4 also shows results for the base case simulation, but as 20-year average  
435 seasonal cycles of storage, release, and withdrawals at each major dam and irrigation  
436 zone across the 1000 bootstrapped simulations. It is clear from Figure 4A that the large  
437 reservoir at Merowe is relatively insensitive to seasonal variability and to climatic

438 variability represented by bootstrapping. This offers a more robust view of the sensitivity  
439 of optimal reservoir operation and water withdrawals to season and to potential patterns  
440 of variability given historical conditions.

441 Figure 4A shows that the dams along the Blue Nile (Sennar and Roseires), in  
442 contrast, are significantly sensitive to seasonal and interannual variability: in the months  
443 preceding the wet season both Sennar and Roseires are emptied and then refilled during  
444 the rainy season, while Merowe is able to remain relatively full year round maximizing  
445 hydropower generation. This is in small part a product of the fact that Blue Nile flows are  
446 more strongly seasonal than main stem flows, which are slightly moderated by inflow  
447 from the White Nile. But the primary reason for the difference is the model's objective to  
448 maximize total benefit through the system. Maximizing hydropower output requires large  
449 hydropower release (Figure 4B), and adequate head through the turbines (see hydropower  
450 constraints section). Since Merowe is the largest hydroelectric facility, it is critical to  
451 hydropower optimization that it is active and that its reservoir is relatively full for as  
452 much of the year as possible. The model maximizes hydropower by maintaining Merowe  
453 at full capacity for most of the dry months at the expense of storage at Roseires and  
454 Sennar. Thus Roseires is emptied between January to May and a relatively full dam is  
455 maintained at Merowe for most of the dry season, maximizing total hydropower  
456 production. Since the Blue Nile has highly seasonal flows and Roseires and Sennar are  
457 relatively small dams, this comes at the cost of seasonally reduced reservoir storage and  
458 hydropower potential at those dams. In Figures 4A and B, the largest variability between  
459 simulations (biggest +/- bars) is observed during the months of emptying and filling (Feb-  
460 Aug), reflecting sensitivity to inter-annual climate variability.

461 Figure 4C shows total water withdrawal amounts during the cropping season  
462 upstream of Sennar dam, which would include the Rahad, Suki and Upstream Sennar  
463 irrigation schemes, and upstream of Merowe dam, which includes the Geziera and  
464 Downstream Sennar irrigation schemes. Since the larger schemes are situated upstream of  
465 Merowe and downstream of Sennar, the largest withdrawals are downstream of Sennar.  
466 There were four crops modeled with different cropping cycles that overlapped during the  
467 season (Table 1), so the total agricultural water requirement varied on a monthly basis.  
468 Withdrawals, however, were maintained at between 1-2.5 bcm on average from July to  
469 October and drop to zero during the non-cropping period.  
470 Currently, the influence of agriculture on dam management is limited due to two factors.  
471 First, though the crop calendar is somewhat different for each of the four crops, there is  
472 only one cropping season, which approximately coincides with the wet months, so  
473 agricultural productivity peaks when the water supply via Blue Nile peak flows is  
474 plentiful (Figure 4C) and the total annual withdrawals are limited by prevailing  
475 agricultural practices. Second, as shown in the tradeoff analysis below (Section 3.2), the  
476 1959 Nile Waters Agreement constraints serves as a cap on water demands for scenarios  
477 with high marginal values of water for agriculture.

### 478 *3.2 Tradeoff Analysis*

479 Understanding the tradeoff between hydropower and irrigation is central to  
480 understanding how the model allocates water to the different objectives. Figure 5 shows

481 results of simulations for three of the marginal values (P2, P4 and P5) represented in  
482 Table 3. The agricultural benefit is removed from the objective function and phrased as a  
483 constraint, and thus a tradeoff curve can be constructed that illustrates the hydropower-  
484 agriculture relationship for each set of agricultural marginal water values. For the case  
485 with higher marginal value of water for agriculture (P2), the gradient of the tradeoff  
486 curve is low. Thus the loss of one unit benefit of hydropower would result in a gain of  
487 more than one unit benefit of irrigation. In order to maximize total benefits, then, the  
488 model would allocate more and more water to agricultural production until it hits a  
489 constraint. For the case with a low marginal value of water for agriculture (P5) the  
490 opposite is true: the model prioritizes moving water through the turbines at the expense of  
491 agriculture. For intermediate marginal water values (P4) there is an inflection point at  
492 which the gradient is equal to 1.0 (circled point in Figure 5). To the left of the point the  
493 gradient is less than 1.0, which would cause the model to shift towards agriculture, and to  
494 the right it is greater than 1.0, pushing the model back towards hydropower. Thus the  
495 inflection point is the optimum balance between agriculture and hydropower for that  
496 marginal value of water under given simulation conditions.

497         The implications of the optimal inflection point for total benefits are illustrated  
498 schematically in Figure 6. The blue line in Figure 6 represents a base case scenario with  
499 an optimum division between irrigation and hydropower indicated by the inflection point  
500 at gradient equal to one. The other lines are representative of scenarios in which changing  
501 conditions—altered flow regime, market modifications, policy decisions, or other  
502 external factors—shift the optimum in a manner that can change both the total value  
503 realized from the system and the division between irrigation and hydropower. A

504 movement up and to the right on the chart is a win-win condition for Sudan in which both  
505 irrigation and hydropower benefits increase, while a move down and to the left is a lose-  
506 lose scenario. Movement up and to the left and down and to the right are trade-off  
507 scenarios in which hydropower benefit increases to the detriment of irrigation and vice  
508 versa. The interpretation of these “wins” and “losses” would, of course, differ for other  
509 stakeholders. Egypt might view movement to the right on the chart—increasing irrigation  
510 withdrawals—as a potential threat to water resources in the absence of increased Nile  
511 river flow or the counterbalancing shared benefits.

512         With this framework in mind, we next consider simulations for one set of  
513 marginal water values (P4). These simulations allow us to ascertain the changing nature  
514 of the tradeoff curves for changes in mean flow consistent with the range of predicted  
515 climate change and for changes in flow timing representative of flow regulation from  
516 upstream development. P4 is used because it represents an intermediate set of  
517 profitability values; P3-P1 have high irrigation profitability and are limited by the 1959  
518 constraints, while P5 and P6 push simulations strongly towards hydropower. Figure 7  
519 shows the results of these simulations, with inflection points indicated as circles around  
520 the point at which the gradient crosses through 1.0. These circled data points are the  
521 optimal values for each scenario at which the model would converge for the given  
522 hydrologic inputs and parameter values.

523         The relative position of these inflection points lies at the core of optimization-  
524 based hydro-economic analysis. When a change in hydrology (e.g., “high flow” versus  
525 “observed flow”) causes the inflection point to move to the right on the chart it suggests  
526 that this hydrologic change will push Sudan towards more irrigation. Similarly, if the



527 inflection point moves up on the chart it suggests that the hydrologic change is pushing  
528 Sudan towards hydropower. These dynamics matter enormously for studies of how  
529 climate change or upstream development is likely to impact Sudan's water resource  
530 decision-making. Movement that is up and to the left or down and to the right is  
531 particularly interesting, as it suggests that Sudan's optimal development strategy involves  
532 a shift between hydropower and irrigation. In more general terms, a hydrologic shift that  
533 moves the optimal point up and to the left on Figure 6 could be thought of as a change  
534 that pushes Sudan towards a hydropower development pathway, while a shift that moves  
535 the point down and to the right pushes Sudan towards an irrigation development pathway  
536 relative to baseline simulation conditions.

537         Model sensitivity to reduced flow (-20%) is consistent with expectation. For the  
538 P4 water value set this low flow scenario results in a decrease in benefits from both  
539 irrigation and hydropower production (triangles and dashed line in Figure 7). Conversely,  
540 an increased flow (+20%) increases both agricultural production and hydropower  
541 production (squares and dotted line in Figure 7). Lastly, the smoothed flows show an  
542 increase in hydropower and almost no change in irrigation benefits. Stabilized flows  
543 increase water availability during the dry season and at the tail ends of the wet season,  
544 and thus there is more water available throughout the year for hydropower, increasing its  
545 benefits (x's and solid line in Figure 7).

546         Next, the sensitivity to agricultural value was analyzed by varying marginal value  
547 of water in agriculture (P1 – P6). Figure 8 shows the trade-off curve of Pareto optimal  
548 values of hydropower and irrigation benefits for P1 – P6 (See Table 3). A solution point  
549 is Pareto optimal if there is no other feasible point that improves at least one objective

550 function without exacerbating another objective function. As described above, a higher  
551 marginal value for agriculture assigns greater weight to agricultural production, which  
552 could be interpreted as a higher agricultural profit margin. First, we note that for all  
553 scenarios in Figure 8 the tradeoff curves flatten out at very high values of irrigation  
554 benefit. This flattening reflects the fact that at high marginal values the agricultural  
555 benefits are limited by the 1959 Nile Waters Agreement constraints. The trade-off curve  
556 approaches horizontal because the same amount of water is allowed to pass downstream  
557 through the turbines at Merowe while the calculated irrigation benefit per unit water  
558 continues to increase when marginal value is set to higher values.

559         Perhaps more interesting, Figure 8 can also be used to study how the marginal  
560 value of agricultural water affects the impact that a change in flow regime has on optimal  
561 water allocation. For the smoothed flow (upstream development) all marginal water value  
562 sets (P1-P6) show no significant increase/decrease in agriculture benefits, due in part to  
563 withdrawal restrictions imposed by the 1959 treaty and, perhaps, in part to the absence of  
564 a second cropping season in these simulations. All the P1-P6 marginal values, however,  
565 provide a win for Sudan: greater hydropower benefits. In other words, smoothed flows  
566 allow for more effective use of existing hydropower infrastructure.

567         The smoothPower simulation (smoothed flow with a drop in the price of power)  
568 shows a policy shift from a hydropower-centric solution to a policy that increases  
569 agricultural production. Interestingly, this shift is relatively modest in all cases and is  
570 extremely small for simulations with high agricultural marginal water values (P1-P3).  
571 This is in large part reflects the limitation on Sudan's annual water withdrawals imposed  
572 by the model's downstream constraints, which guarantee flow to Egypt. For P1-P3 the

573 Smooth Flow simulation already runs up against these constraints, preventing larger  
574 shifts to irrigation in SmoothPower.

575         We note that all of these results, including the shift to agriculture in  
576 SmoothPower, are for existing cropping practices. Figure 9 considers a shift in  
577 management practices and introduces a second cropping season to the smoothed flow. An  
578 additional cropping season shows increases in irrigation benefits particularly if  
579 agricultural marginal water values are high (P1 – P3). Smooth2crop in Figure 9  
580 introduces a second crop season to the smoothed flow, and SmoothPower2crop includes  
581 this double cropping and an estimate of less expensive power due to upstream production  
582 sold to Sudan. The modest increases in irrigation benefits for these flows, particularly in  
583 scenarios of high irrigation profitability, illustrate Sudan’s limitation due to the  
584 constraints in the model representative of the 1959 agreement. The second constraint  
585 guarantees at least three times more water passing Merowe downstream into Egypt that it  
586 does allow for irrigation at upstream schemes, thereby forcing Sudan toward a  
587 hydropower path and limiting its irrigation potential (see Irrigation constraints Section  
588 2.1.3, Equation 7).

589         To test for the restrictive nature of the 1959 agreement in our simulations, we  
590 have included two additional runs that remove the second constraint of the 1959  
591 agreement (Smooth2cropNA and SmoothPower2cropNA) but maintain Sudan’s long  
592 term average water use at 14.5 bcm. SmoothPower2cropNA includes the reduction in  
593 power price due to upstream control and the removal of the second 1959 constraint. Both  
594 runs show a significant increase in irrigation benefits for cases P1 – P3 (Figure 9).

595 **4. Conclusions:**

596 This paper introduces a hydroeconomic model for Sudan (SHOM) that considers  
597 hydropower and irrigation benefits under conditions of existing infrastructure and  
598 practices. SHOM includes a nonlinear multiobjective optimization routine that allows us  
599 to study interactions between component objectives under a range of flow scenarios and  
600 valuation of agricultural returns. A number of our modeling results confirm or  
601 complement previous hydro-economic analyses—for example, the fact that upstream  
602 regulation can provide benefits to downstream riparians. Ajoon et al. (2014), for example,  
603 shows that including the GERD in a SDDP hydroeconomic model resulted in an increase  
604 in hydropower generation in Sudan and Egypt. Other results are intuitive, such as the fact  
605 that under reduced flows there is a decline in hydropower and irrigation benefits.  
606 However, even in this simple sensitivity test the model returns some non-obvious results.  
607 While one might expect that smoothing the Blue Nile hydrograph through upstream  
608 regulation would inevitably lead to increased irrigation withdrawals, we find that doing  
609 so is only beneficial under select combinations of marginal values of water and if the  
610 upstream facility results in a drop in the price of electricity in Sudan. Otherwise the  
611 optimal development path is to increase hydropower production.

612 Another interesting result is the restrictive nature of the downstream flow  
613 constraint. The more that economic considerations (lowering of power prices and changes  
614 in agricultural practices) push Sudan towards irrigation, the more expensive these  
615 constraints—i.e., the restrictions imposed by a water sharing agreement—become to the  
616 country. The current requirement to deliver adequate flows to Egypt is not a severe  
617 constraint as long as agriculture is economically inefficient, irrigation is hampered by

618 siltation and seasonal flow variability, and hydropower is an economic driver to send  
619 water downstream. But if these realities are shifted by an upstream facility that regulates  
620 flow, reduces sediment load, and provides inexpensive electricity, the treaty-enforced cap  
621 on water use will quickly become a constraint on Sudan's optimal hydro-development  
622 options.

623         The modeling results presented in this study contribute to current understanding  
624 of Nile hydroeconomics by presenting a focused analysis of Sudanese options, performed  
625 with a multiobjective optimization model capable of capturing nonlinear interactions.  
626 There are, however, a number of important limitations that need to be addressed in future  
627 model development. First, the model does not include knowledge of current dam  
628 operating procedures or of stage-volume relationships for proposed dams (GERD) or for  
629 existing dams in recent years. Second, the model does not include the effects of siltation.  
630 A dam that controls siltation would affect the objective function by easing dam operation  
631 and significantly reducing dredging costs for canals that feed irrigation schemes. At the  
632 same time, reduced silt load would increase the need for fertilizer in downstream  
633 agricultural lands that currently benefit from natural nutrient input from silt-laden waters.  
634 Third, limitations in current agricultural and economic data make it difficult to estimate  
635 total agricultural benefits, so the marginal value of agricultural water essentially functions  
636 as a tuning parameter in SHOM that allows us to study general sensitivity to the value of  
637 agriculture. This could certainly be improved with access to more reliable and recent  
638 agricultural data, though the perceived value of agriculture and the support of this value  
639 through land and economic policies are always difficult to quantify.

640           The scope of SHOM is also a matter of ongoing evaluation. In focusing on  
641 hydropower and irrigation we adopt the framework of many earlier hydro-economic  
642 optimization models in the Nile and elsewhere. We recognize, however, that climate  
643 change and river development can have a broad range of impacts, many of which are  
644 difficult to quantify. These include ecological impacts, effects on fisheries, and burden  
645 placed on particular populations living within the basin. These important considerations  
646 must be accounted for in any application of hydroeconomic analysis to development  
647 decision making, and it would be valuable to find ways to broaden Nile basin  
648 hydroeconomic models to include a more diverse array of processes and outcome  
649 variables. Lastly, we recognize that our use of a deterministic model presents a highly  
650 idealized scenario of a decision maker with perfect foresight. Deterministic models do  
651 not account for the uncertainties in some of the input parameters, therefore the results and  
652 decisions presented in this paper will produce benefits that are higher than any real world  
653 scenario.

654           Future operation of SHOM may be within a value of information framework that  
655 aims to assess operational seasonal forecasts. A more in-depth study of the value of  
656 information of seasonal forecasts will require the conversion of SHOM from a  
657 deterministic model to a stochastic model in order to adjust to the stochastic nature of  
658 forecasts. In addition, we would add that our analysis was performed for a portion of the  
659 Blue Nile as well as the downstream main Nile stem within Sudan. Future development  
660 of the model should incorporate other major tributaries such as the White Nile and the  
661 Atbara. Inclusion of other Nile tributaries and their infrastructure in the model will  
662 present a more holistic approach to analyzing Sudan's water resources decision making.

663           The Nile River is a finite water resource shared by a number of emerging  
664 economies, and the long-standing tensions regarding its equitable use are only increasing  
665 as demand for food, water, and electricity rise across the region. On account of both  
666 history (i.e., the 1959 Nile Waters Agreement) and geography, the Republic of Sudan is a  
667 particularly critical player in determining the future of Nile development and related  
668 hydroeconomic development decisions in neighboring countries. The effect of climate  
669 change and upstream development, in turn, will be critically important in determining  
670 Sudan's long term optimal development path and associated policy decisions. Here we  
671 present a first analysis targeted specifically at Sudan's optimal irrigation and hydropower  
672 development options under scenarios of changing Nile flows and upstream development.  
673 Results reinforce the understanding that Sudan has the potential to weigh in heavily on  
674 matters of regional water and food security depending on how it chooses to make use of  
675 the Blue Nile and main stem Nile as it flows through its territory. Further research is  
676 required to understand how these choices are affected by additional development, trade,  
677 and policy decisions within the basin, and how Sudan's own infrastructure and  
678 agricultural practices might evolve to optimize returns under evolving climatic and  
679 economic conditions.

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686 Network-Monthly (GHCN-M) temperature dataset station Wad Medina nr62751 in  
687 ghcnm.tavg.v3.qcu v3.2.2.20140804, WMO Station code 62751.  
688 (<http://climexp.knmi.nl>), as well as the Food and Agricultural (FAO) dataset  
689 (FAOSTAT). (<http://faostat.fao.org/>).



690 **Appendix:**

691 **SHOM MODEL:**

692 *Objective Function:*

$$\text{Objective} = \max \sum_{m,y} (D^y * bi_{m,y} + D^y * P_{m,y} bh_{m,y}) \quad (1)$$

693 **Constraints:**

694 *Hydropower:*

$$\forall_{l,m,y}, KWH_{l,m,y} = c * n * effh * rhe_{l,m,y} * h_{l,m,y} \quad (2)$$

$$bh_{m,y} = \sum_l (P * KWH_{l,m,y}) \quad (3)$$

$$\forall_{l,m,y}, r_{l,m,y} = rhe_{l,m,y} + nhe_{l,m,y} \quad (9)$$

$r_{l,m,y}$  = total release,  $rhe_{l,m,y}$  = hydropower release,  $nhe_{l,m,y}$  = non-hydropower release

$$\forall_{l,m,y}, rhe_{l,m,y} \leq Q_{dc} \quad (11)$$

where  $Q_{dc}$  is the flow capacity through the turbines.

*Irrigation:*

$$i_{l,m,y} = \sum_c (effi_c * Water_{c,l,m,y} * Area_{c,l,m,y}) \quad (4)$$

$$bi_{m,y} = \sum_{c,l} (effi_c * v_c * Water_{c,l,m,y} * Area_{c,l,m,y}) \quad (5)$$

$$\sum_{l,m,y} (i_{l,m,y}) + \sum_{l,m,y} (e_{l,m,y}) \leq Y * 14.5 \text{ bcm} \quad (6)$$

$$\sum_{l,m} (i_{l,m,y}) + \sum_{l,m} (e_{l,m,y}) \leq 0.28 * \sum_m (R_y) \quad (7)$$

$$\sum_{c,l} Area_{c,l,m,y} \leq 1.4 \text{ million ha} \quad (12)$$

695 *Continuity:*

$$\forall_{l,m,y}, s_{l,m,y} = q_{l,m,y} + r_{(l-1),m,y} + s_{l,(m-1),y} - r_{l,m,y} - i_{l,m,y} - e_{l,m,y} \quad (8)$$

$$s_{l,m,y} \leq Vmax \quad (9)$$

$$\text{Non Negativity Constraints: } s_{l,m,y}, rhe_{l,m,y}, nhe_{l,m,y}, r_{l,m,y}, i_{l,m,y}, Area_{c,l,m,y} \geq 0 \quad (10)$$

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839 **Tables :**

Parameters	Value Range	Units	Notes
Discount Rate (D)	3% - 7%	-	5% used in the simulation analysis
Flows(q)			
High	20%		
Low	-20%	Million m <sup>3</sup>	CI = Confidence Intervals
Smooth	3-month Average		
Bootstrapped Flows	5%, 50%, 95% CI		
Water Requirement(Water)			
Wheat	0.23 - 0.48		Value depends on Month
Cotton	0.48 - 0.73	m <sup>3</sup> / m <sup>2</sup>	(Plusquellec 1990,
Sorghum	0.69 - 0.94		Ghezze 1998)
Groundnuts	0.89 - 1.14		
Efficiency			
Effh	0.85	-	Hydropower Efficiency
Irrigation			Irrigation Efficiency
Wheat	0.233	-	
Cotton	0.065	-	
Sorghum	0.333	-	
Groundnuts	0.312	-	
Power (P)	0.08	cents/KWh	
Evaporation <sup>a</sup>	0.08 - 0.3	m <sup>3</sup> / m <sup>2</sup>	Evaporation is derived from the Thornthwaite equation (Thornthwaite, 1948). Range Depends on Month and location.
e	1.9 - 76.5	Million m <sup>3</sup>	e = Ev*Dam Surface Area

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Table 1: SHOM Parameters

Variables	Definition	Units	Notes
s <sup>b</sup>	Storage	Million m <sup>3</sup>	Storage volume is assumed to be cylindrical in the model
r	Release (r = rhe + nhe)	Million m <sup>3</sup>	Release has two components, rhe = Hydropower release, nhe = non-hydropower release
i	Irrigation Volume	Million m <sup>3</sup>	
Area	Area Irrigated	Million m <sup>3</sup>	
bi	Irrigation Benefits	\$	
KWH	Power Generated	KWh	Calculated from the hydropower equation. Function of hydropower release and head
bh	Hydropower Benefits	\$	

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Table 2: SHOM Variable definitions

	Marginal value of water (\$/m3)					
	P1	P2	P3	P4	P5	P6
Cotton	0.287	0.118	0.036	0.008	0.001	0.00001
Wheat	0.062	0.025	0.008	0.002	0.000	0.000
Groundnut	0.083	0.034	0.011	0.002	0.000	0.000
Sorghum	0.017	0.007	0.002	0.000	0.000	0.000

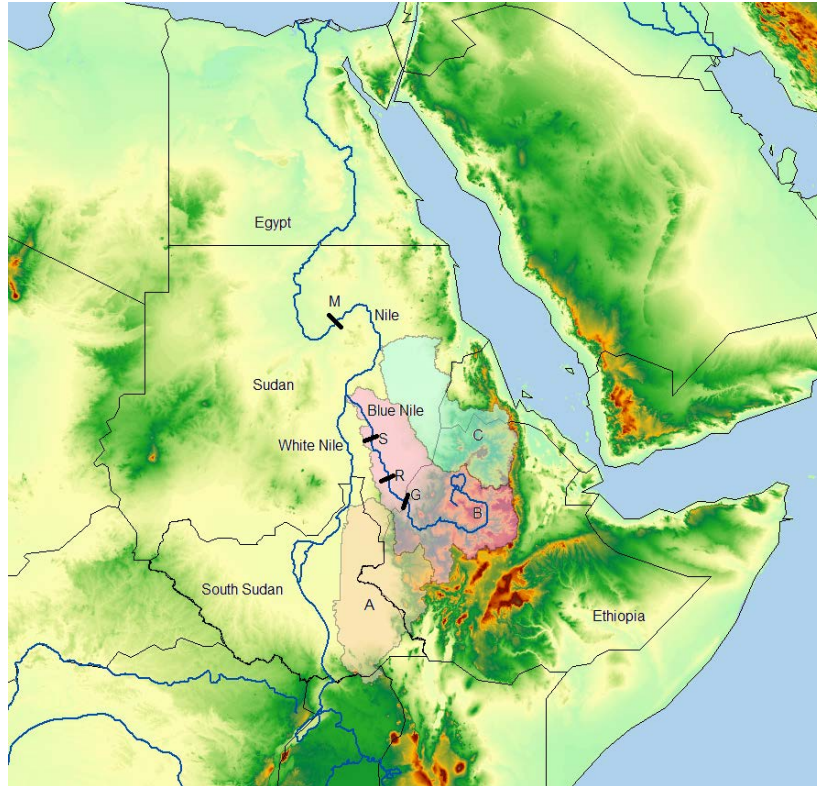
Table 3: Marginal Values of Water for each Crop

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Simulations	Description
High Flows	+20% Observed
Low Flows	-20% Observed
Smoothed Flows	3 month averaged
Smooth2crop	Smooth flow + 2 cropping season
SmoothPower	Smooth flow + 0.04 cents/KWh power price
Smooth2cropNA	Smooth flow + 2 cropping season + Removal of second 1959 agreement constraint
SmoothPower2crop	Smooth flow + 0.04 cents/KWh power price + 2 cropping season
SmoothPower2cropNA	Smooth flow + 0.04 cents/KWh power price+ 2 cropping season + Removal of second 1959 agreement constraint

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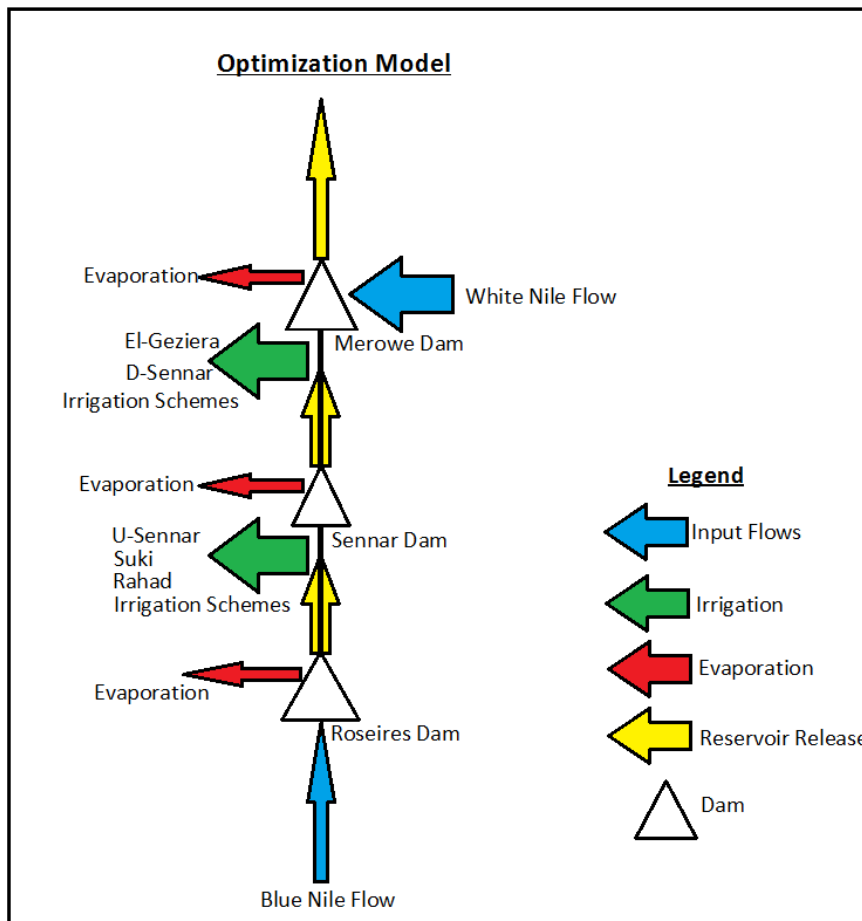
Table 4: Description of the simulations used in SHOM



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847 Figure 1: Map of the Nile and its tributaries A = Baro-Akobo-Sobat, B= Blue Nile, C =  
848 Tekese-Atbara Basins, S = Sennar Dam, R = Roseries Dam, M = Merowe Dam and G =  
849 GERD

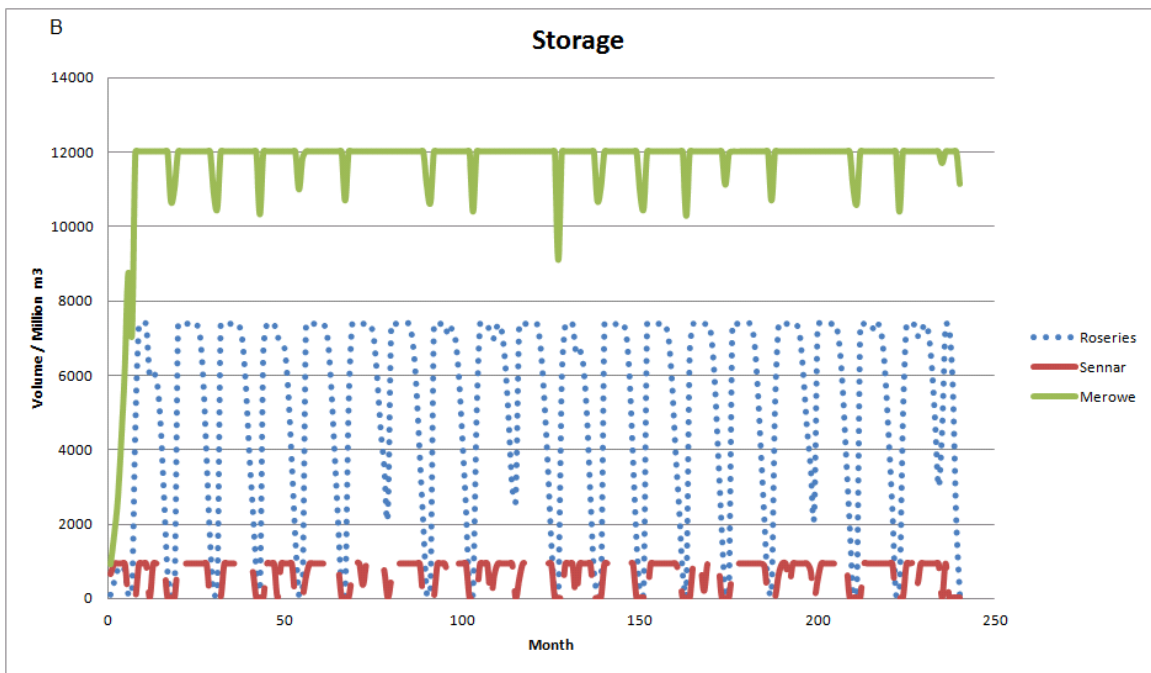
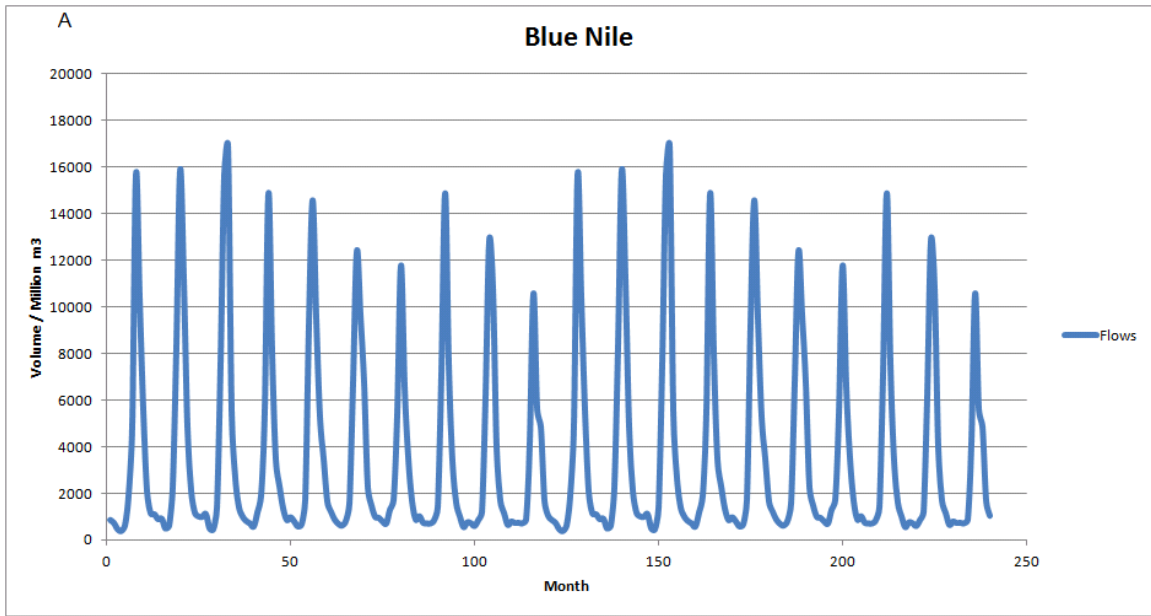


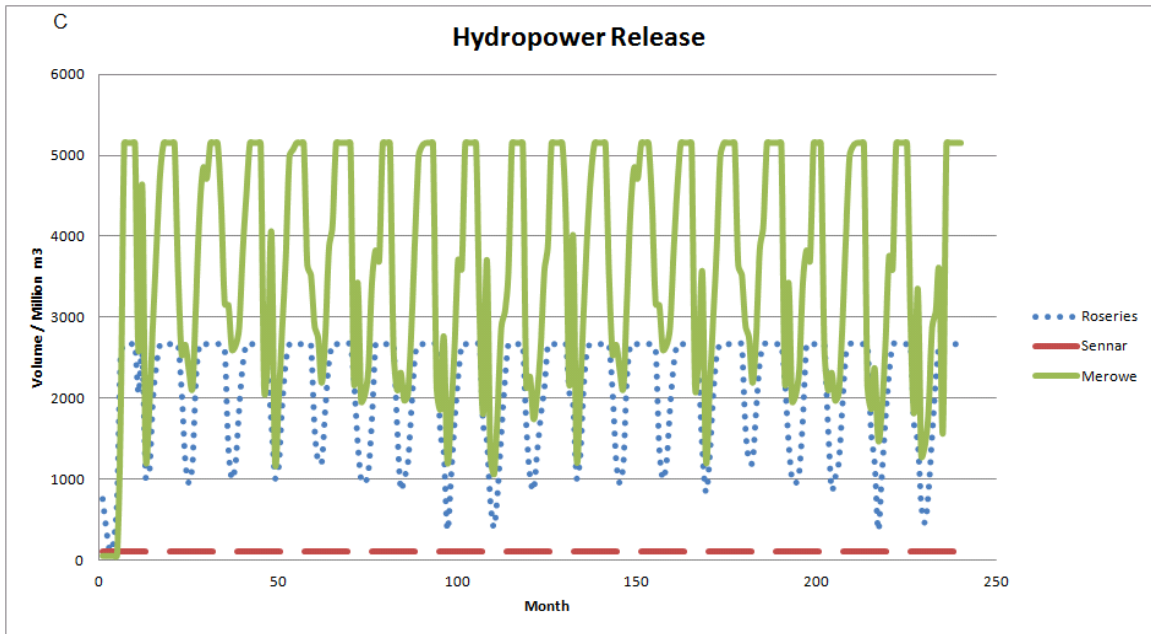


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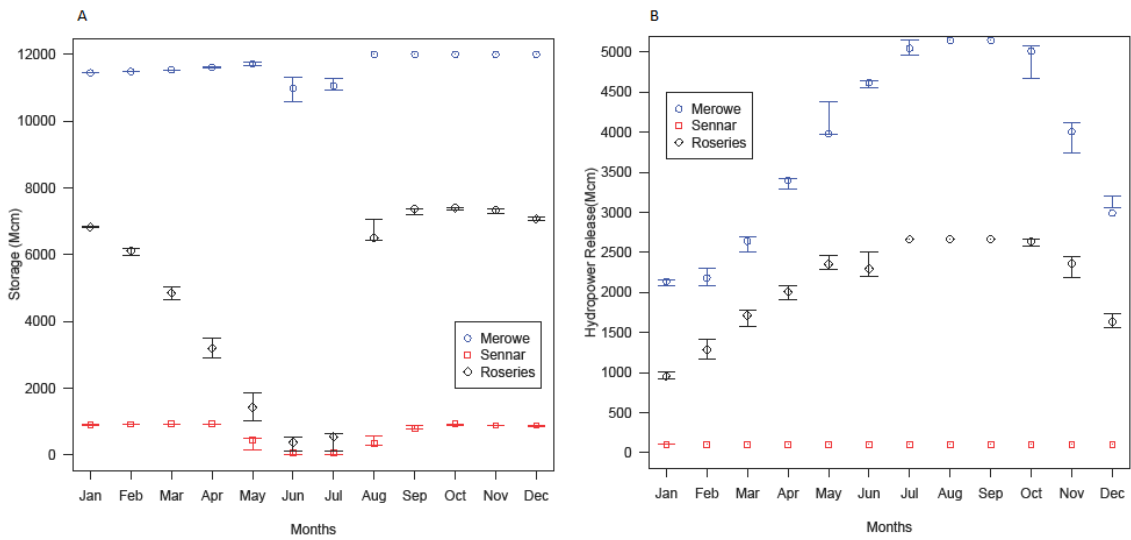
Figure 2: Schematic of the Optimization Model

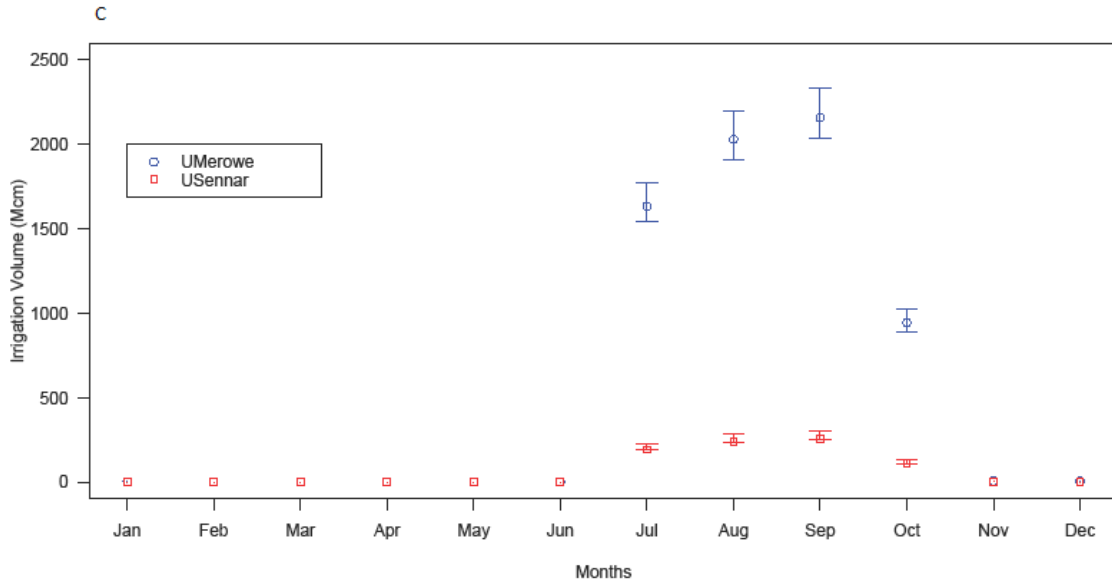




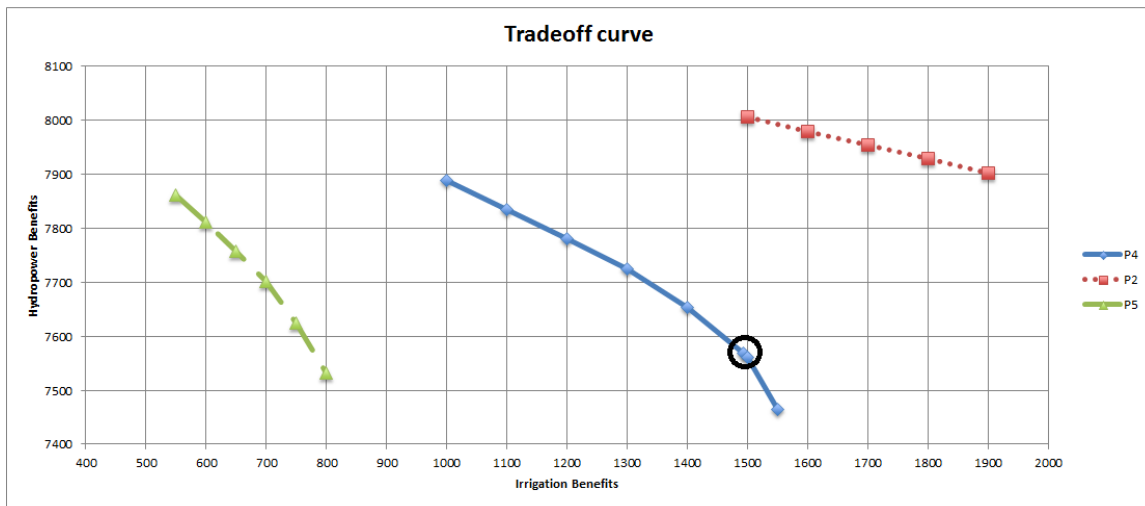
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Figure 3: Annual cycle of (A) observed flow, (B) storage and (C) hydropower release at the three dams over the 20 year demonstration simulation



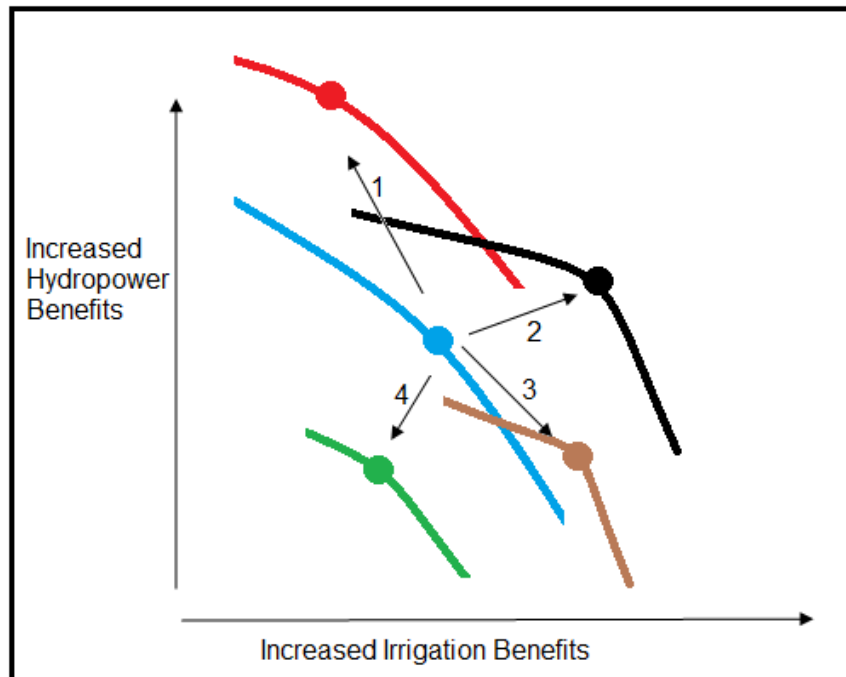


854 Figure 4: Annual cycle of (A) reservoir storage and (B) hydropower release at the three  
 855 dams, and (C) irrigation withdrawals upstream of Sennar and upstream of Merowe in the  
 856 base case simulation of bootstrapped historical flows and marginal values P4. Data points  
 857 are the mean average value over the 20 year simulation and error bars represent the  
 858 difference in output between the 5% and 95% confidence interval bootstrapped flow.



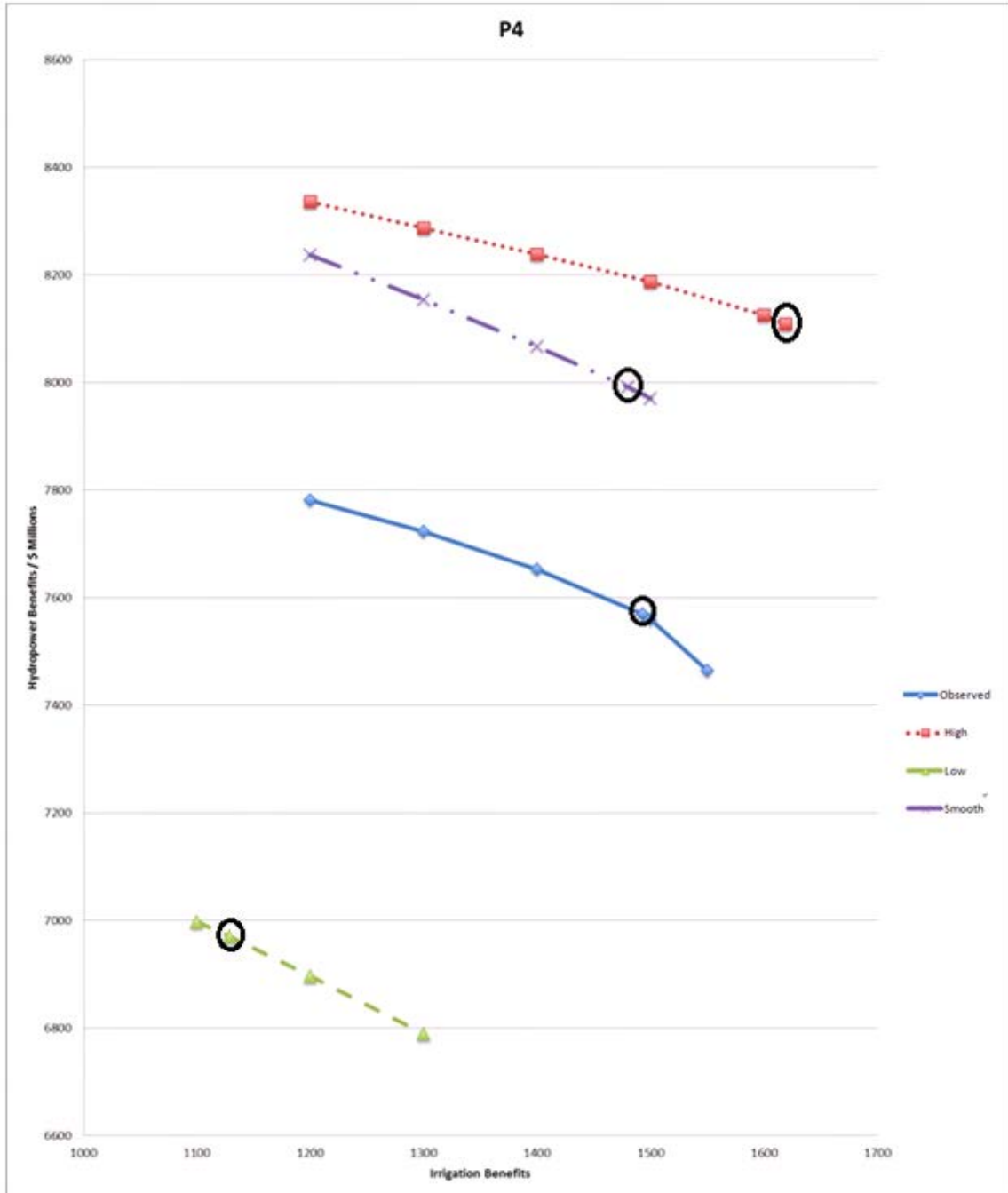
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860 Figure 5: SHOM hydropower vs. irrigation benefit trade off curves for three different  
 861 water values (P2, P4 and P5).



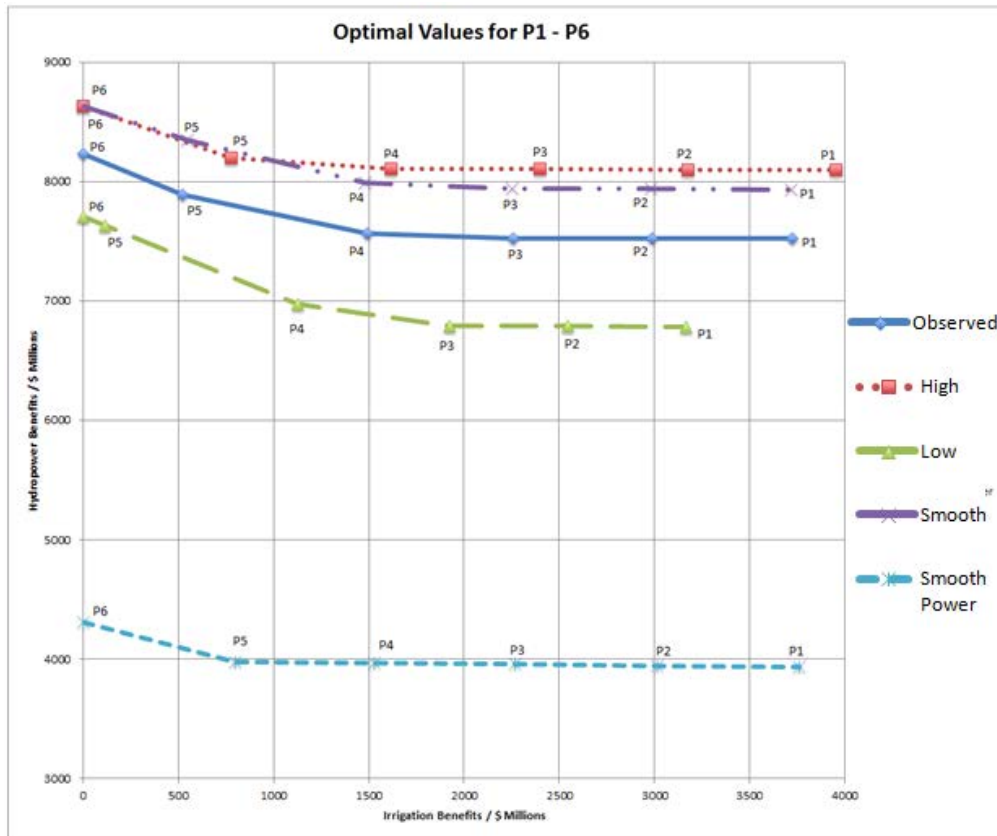
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Figure 6: Schematic of the four possible ways in which changing conditions can shift the optimum model solution from a baseline set of solutions represented by the blue curve. Arrow 1 (shift to red curve) depicts a win-loss tradeoff where a loss in irrigation benefits is offset by an increased in hydropower benefits. Arrow 2 (shift to black curve) depicts a win-win outcome, with a gain in both hydropower and irrigation. Similarly, arrows 3 and 4 can be characterized as loss-win and loss-loss, respectively.



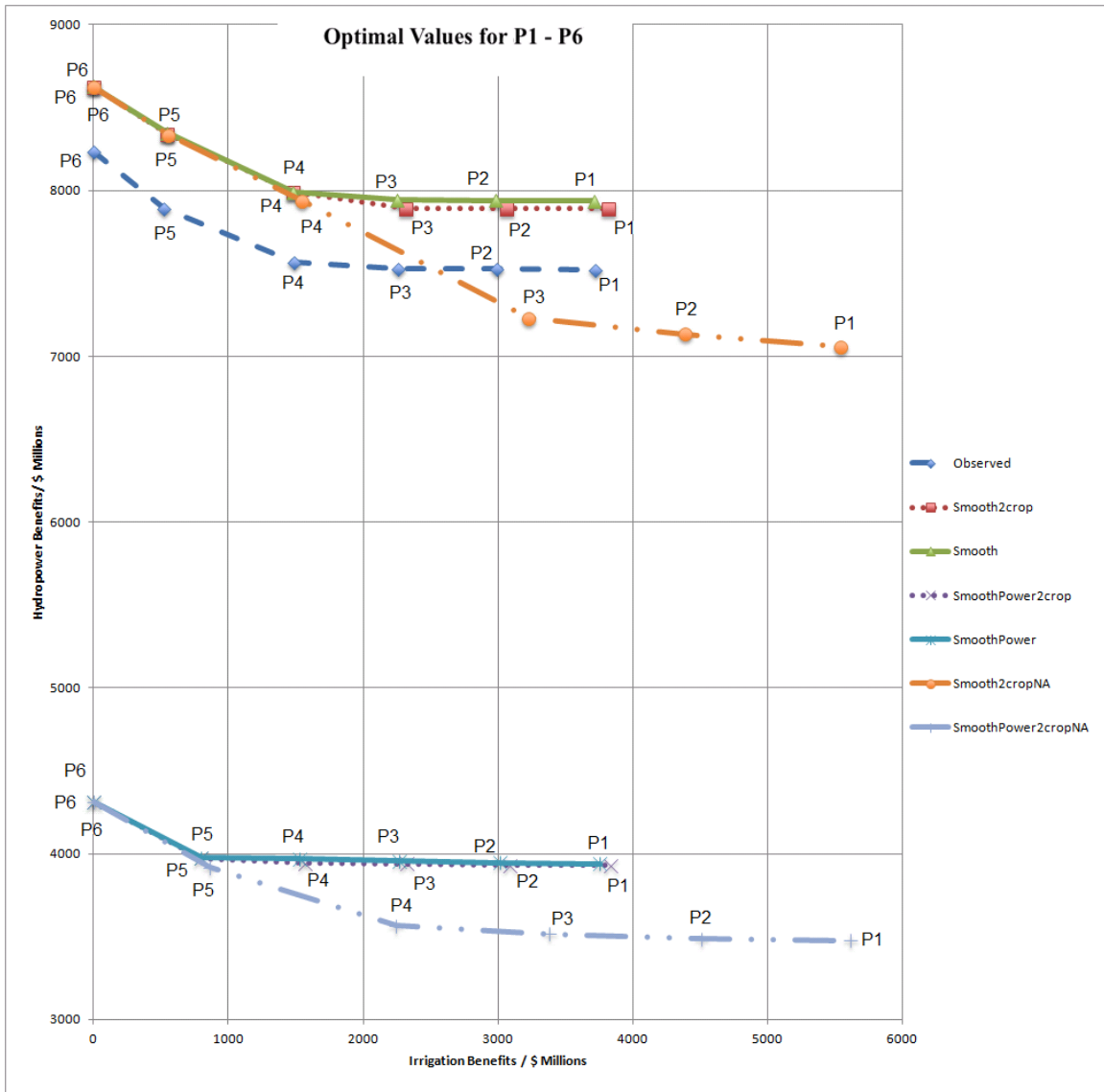
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Figure 7: Results of SHOM simulations in which the agricultural benefits are phrased as constraints, and the hydropower benefits are calculated for a specific agricultural benefit. The circles highlight the optimal values for each scenario.



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Figure 8: Hydropower vs. irrigation benefits in SHOM simulations. Points represent Pareto optima values for water value sets P1-P6.



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Figure 9: Hydropower vs. irrigation benefits illustrating adaptive management practices. Points represent Pareto optima values for water value sets P1-P6.