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| 2 | Assessing Hydrological Model Behaviors by Intercomparison of the |
| 3 | Simulated Stream Flow Compositions: Case Study in a Steep Forest |
| 4 | Watershed in Taiwan |
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28 Abstract

| 29 | The accuracy of streamflow composition simulated by different models has been rarely discussed. In |
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| 30 | this study, total 23 flood events covering full rainfall spectrum were simulated by using HBV and |
| 31 | TOPMODEL. Simulated streamflow compositions were compared with hydrograph decomposed by |
| 32 | independent geochemical data via end-member mixing analysis (EMMA). Results showed that both |
| 33 | models gave satisfactory streamflow simulation in terms of the Nash efficiency coefficient, correlation |
| 34 | coefficient, and discharge volume. However, the modeled interflow and base flow behaved differently |
| 35 | with the changing storm intensity and duration. The HBV simulated base flow considerably increased |
| 36 | as the storm duration prolonged; by contrast, the TOP-derived base flow remained stable. On the other |
| 37 | hand, HBV prefers generating less interflow to percolate more to the base flow for fitting the stream |
| 38 | flow. Accordingly, HBV is more suitable for thin soil layer. We suggested that a proper model |
| 39 | selection should take the implicit environmental background into account for simulating reliable |
| 40 | streamflow composition. Compared with the EMMA-derived flows, both models showed a significant |
| 41 | time lag (2-4 hr). If EMMA-derived hydrograph is real, the modeled base flow responses are required |
| 42 | to speed up. Our model's intercomparison against independent validation by geochemical data is a |
| 43 | good means of studying the model behaviors. The selection of a more appropriate hydrological model |
| 44 | should consider the characterization of the model structure and the watershed characteristics. |
| 45 | |
| 46 | |
| 47 | Keywords: stream flow composition, HBV, TOPMODEL, end-member mixing analysis (EMMA), |
| 48 | Taiwan |

註解 [R1]: For detailed comment #1

註解 [R2]: For technical comment #1

49

52 1. Introduction

53 Simulating the stream flow accurately is one of the main concerns of scientists and managers, 54 particularly in hydrology science and water resource assessment. For this goal, hydrological models 55 are implemented through different conceptualizations of simplified representations of the real world (Beven, 2001; Refsgaard and Henriksen, 2004). Therefore, a number of hydrological models with 56 57 different model structures were proposed and applied around the world. Undoubtedly, this significant 58 progress in hydrological modeling works has been facilitating many discharge-relevant applications. 59 Currently, the attentions have shifted to understanding more on the model structure and the 60 corresponding behaviors for advanced interpretations (Reed et al., 2004; Clark et al., 2008). For example, some previous studies applied different model structures (e.g., runoff generations or routings) 61 62 on the same catchment to determine the model suitability and applicability (Winchell et al., 1998; 63 Valeo et al., 2001; Johnson et al., 2003). These comparative studies revealed that models with 64 different structures could satisfactorily simulate the stream discharge for the same catchment. 65 However, the selection of the hydrological models and the model structure uncertainties are still not fully understood. Clark et al. (2008) have applied 79 unique model structures by combining the 66 67 components of four existing hydrological models into catchments. They concluded that the model 68 structure uncertainty is as important as the parameter uncertainty, indicating that intercomparison 69 among models can give insight into the understanding of hydrological models. In addition, Weiler et al. 70 (2003) integrated the instantaneous unit hydrograph and the temporal variability of rainfall isotopic 71 composition to interpret the runoff processes and pathways. The series of studies conducted by the 72 McDonnell's laboratory demonstrated that the transit time plays a crucial role in testing the 73 hydrological models and indicated the importance of geochemistry on hydrological modeling (Fenicia 74 et al., 2008; Sayama and McDonnell, 2009). 75 Although the abovementioned studies made a significant step forward on the choice and 76 suitability of hydrological models, the accuracy of the simulated stream flow composition controlled 77 by different model structures still needed further studies. Such result raises two interesting issues. 1. 78 Why does the model prefer to provide such streamflow composition? 2. What kind of streamflow

composition from the models is more realistic or reliable? Obviously, the model preference or model

80 behavior is dominated by the model structure, governing equations, and calibration. Therefore, this

81 study incorporated the same base-flow equation (linear reservoir concept) into different model

| 82 | structures (Hydrologiska Byrans Vattenbalans-avdelning (HBV) and TOPMODEL) to investigate the |
|----|---|
| 83 | influence of the model structure on the simulations (Wagener et al., 2010). Understanding the two |
| 84 | questions not only provide insight into hydrology but also water resource planning. |
| 85 | To investigate the two model behaviors, this study applied the hydrological models with the same |
| 86 | base-flow component to a steep mountainous watershed in Taiwan. Altogether, 23 events covering a |
| 87 | wide rainfall spectrum in hourly basis were used. The Nash efficiency coefficient (Nash_EC) and its |
| 88 | logarithmic form (<i>Nash_EC</i> _{log}) were used to calibrate parameters. The <i>Nash_EC</i> , volume bias ratio, |
| 89 | and correlation coefficient were used to evaluate the model applicability. The simulated streamflow |
| 90 | compositions were intercompared to investigate the model behaviors among the different events. |
| 91 | Finally, the two rainstorms, supplemented by an intensive geochemical dataset, were independently |
| 92 | introduced to assess and validate the simulated streamflow composition. This study improved our |
| 93 | understanding on model selection and the role of the parameters in streamflow composition, |
| 94 | |

95 2. Materials and Methods

96 **2-1 Study Area**

| 97 | This study chose the Chi-Chia-Wan watershed in central Taiwan as study area which is a typical |
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| 98 | forested, steep, and mountainous watershed with a drainage area of 105 km ² (Fig. 1). The elevation |
| 99 | varies from 1,131 m to 3,882 m above sea level, and the steep slope (average of approximately 33.3°) |
| 100 | represents a high runoff velocity and sediment transport (Kao <i>et al.</i> , 2011; Lee <i>et al.</i> , 2013). The Effective for detailed comment #1 |
| 101 | majority of soils are colluvial soils (including greyish yellow and dark greyish) and lithosols with high |
| 102 | permeability. The soil depth is various due to the frequent mass movements, but most soil depths vary |
| 103 | from 40 -120 cm (Soil and Water Conservation Bureau, 1985). The annual average air temperature is |
| 104 | 15.8 °C, and the monthly average air temperatures in January and July are 4 and 23 °C in 2000–2009 |
| 105 | (Huang et al., 2006). The original and secondary forests covering nearly 87% of the area are the |
| 106 | dominant land cover in this watershed. Most agricultural lands (e.g., orchard and vegetable farms) |
| 107 | locate along the road or the riparian zone. The annual precipitation is as high as 2,551 mm (based on É 解 [R6]: For technical comment #5 |
| 108 | 2000–2011 data) with distinct seasonality. Approximately 75% of the annual precipitation rains during |
| 109 | the wet season (May to October), and tropical cyclone (typhoon) is the main contributor. The annual |
| 110 | evapotranspiration here is estimated between 600-1200 mm and the daily evapotranspiration in |
| 111 | summer may be as high as 6-8 mm (Water Resources Agency, 2011). The annual discharge is 注册 [R7]: For detailed comment #3 |
| 112 | approximately 2,129 mm (from 2000–2011 data) with a mean daily discharge of 7.09 m ³ /s (equivalent |

< 註解 [R3]: For technical comment #1

| 113 | to 5.83mm/day). | 註解 [R8]: For detailed comment #2 |
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| 114 | For the rainstorm selection, a total of 23 rainstorms with significant water level rise (over 2 m) were | |
| 115 | selected to evaluate the model applicability (Table 1). In general, the average cumulative rainfall was | |
| 116 | approximately 430 mm within 102 h. The total rainfalls varied from 184.5 mm to 836.4 mm and the | |
| 117 | maximum rainfall intensity ranged from 10.7 mm/h to 39.5 mm/h. The total runoff depth ranged from | 註解 [R9]: For technical comment #1 |
| 118 | 37.8 mm to 672.6 mm and was significantly positively correlated with the total rainfall and rainfall | |
| 119 | duration. The peak discharges ranged from $\frac{66.5 \text{ m}^3}{\text{s}}$ to $\frac{510.4 \text{ m}^3}{\text{s}}$ (equivalent to 2.28 mm/h to $\frac{17.5}{2}$ | 註解 [R10]: For technical comment |
| 120 | mm/h) and were positively correlated with the total rainfall, average rainfall intensity, and maximum | #6 |
| 121 | rainfall intensity (Table 1). The streamflow responding to the rainfall within a short time lag (generally | |
| 122 | less than 2 h) indicates that the watershed has a steep slope and short traveling time. These events, | |
| 123 | which crossed a wide spectrum in terms of the total rainfall and duration, are the critical factors to | |
| 124 | detect the limit of model applicability. | |

126 2-2 Hydrological Modeling: TOPMODEL and HBV

127 The two hydrological models [HBV (Hydrologiska Byråns Vattenbalans-avdelning) and
128 TOPMODEL (hereafter, TOP)] were used in this study. Both models are regarded as conceptual
129 distributed model and have been widely applied in many studies. Here, the two models were briefly
130 introduced.

131

132 **2-2.1 HBV Model**

133 The HBV model was originally developed by the water balance section of the Swedish 134 Meteorological and Hydrological Institute and has been modified into several versions (e.g., 135 Bergström and Forsman, 1973; Bergström, 1992; Lindström et al., 1997; Krysanova et al., 1999; 136 Haberlandt et al., 2001; Blöschl et al., 2008). Aghakouchak and Habib (2010) modified this model into 137 a distributed-based model, and we used this version in the current study. The HBV model consists of 138 four modules: (1) snowmelt and snow accumulation, (2) soil moisture and effective precipitation, (3) 139 evapotranspiration, and (4) runoff response. For rainstorm (short-term) simulation, the hourly time 140 step was used. In this study, the snow accumulation, snowmelt, and evapotranspiration modules were 141 turned off. Although the elevation in the study site is high (> 3,000m), very little or no snow appears in 142 subtropical summer. The amount of evapotranspiration during rainstorms (~3 days) should be less than

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143 24mm which is much smaller compared to the average of rainstorm precipitation (\sim 430mm).

Therefore, the two modules can be neglected to reduce the parameters involved in calibration.
In the HBV model, precipitation is usually divided into two components: the first part contributes
to the soil root zone, and the second one contributes to the interflow storage. The second component is
usually known as effective precipitation. This component is estimated by an exponential coefficient
and the saturation level in the soil root zone. In the soil root zone, saturation level is defined as the soil
moisture over the field capacity (*FC*), the parameter that describes the maximum water storage.
Adopting this concept, the higher the saturation is, the larger is the precipitation proportion recharged

into the inter flow storage. Equation (1) describes the calculation of the effective precipitation, whichis a function of the current soil moisture content.

153 $P_{eff} = P \cdot \left(\frac{SM}{FC}\right)^{\beta}$ (1)

154

155 where P_{eff} is the effective precipitation [L], SM is the current soil moisture [L], FC is the maximum soil 156 storage capacity [L], P is the hourly precipitation [L], and β is a model parameter (shape coefficient) [-]. The soil moisture status temporally evolves by receiving the rest of rainfall in each time step until 157 reaching FC. An initial value of the soil moisture is required to start the calculations. 158 159 The interflow and baseflow estimations at the watershed outlet are based on the linear reservoir 160 concept (Fig. 2a). The reservoirs are directly connected to each other by a constant percolation rate (P_r) . Two outlets (Q_s and Q_i) are in the upper reservoir and one outlet (Q_b) is in the lower reservoir. When 161 the water level in the upper reservoir exceeds the threshold value (L), surface runoff (Q_s) occurs. For 162 163 the surface flow routing, the unit response function implemented by the diffusive transport approach is 164 used (Liu et al., 2003; Huang et al., 2009). The water level in the upper reservoir is used to generate the 165 interflow (Q_i) . The base-flow response in the lower reservoir is relatively slower and controlled by the 166 water level in that reservoir. The recession coefficients K_s , K_i , and K_b , control the response functions of 167 the three flows. The three recession coefficients and the percolation rates are all model parameters, 168 which are estimated via calibration. Equations (2) and (3) illustrate the calculation of the three flows in the outlet: 169 $Q_s = \begin{cases} K_s(S_i - L)A_c & if S_i > L \\ 0 & if S_i < L \end{cases}$ 170 (2)

171

172 $Q_i = A \cdot K_i \cdot S_i$

173 $\boldsymbol{Q}_{\boldsymbol{b}} = \boldsymbol{A} \cdot \boldsymbol{K}_{\boldsymbol{b}} \cdot \boldsymbol{S}_{\boldsymbol{b}} \quad (3)$

5

註解 [R13]: For detailed comment #4

註解 [R12]: For detailed comment #3

註解 [R14]: For technical comment

175 where Q_s , Q_i , and Q_b represent the surface flow, interflow, and base flow $[L^3/T]$, respectively. The parameters K_s , K_i , and K_b are the recession coefficients of the surface flow, interflow, and base flow 176 177 $[T^{-1}]$, respectively. S_i is the upper reservoir water level [L], S_b is the lower reservoir water level [L], and L is the threshold of water level [L]. A and A_c are the watershed and cell area [L²], respectively (Fig. 178 179 2a).

180

2-2.2 TOPMODEL 181

182 TOPMODEL proposed by Beven and Kirkby (1979) has been applied widely around the world 183 (Beven, 1996). The kernel feature of this model is to use the topographic index (defined as the 184 contributing area over the gradient, see Equation 4) to estimate the variable source area and then 185 simulate the discharge.

 $\gamma_i = \ln\left(\frac{a_i}{T_i \cdot tan\beta_i}\right)$ 186

(4) 187 where \mathbf{y}_i is the local topographic index. Parameter T_i is the lateral transmissivity as the soil is saturated $[L^2/T]$. *a* is the specific contributing area defined as the drainage area per unit contour length 188 [L], and tan β is the local gradient [-]. Because of its concise structure, numerous modifications have 189 190 been introduced in the past three decades. We used the three-layer TOPMODEL (Huang et al., 2009) 191 in this study. This modification has been widely used in Taiwan for relevant hydrological applications 192 either for hourly or for daily time step input (Huang et al., 2011; Huang et al., 2012). The conceptual 193 scheme is shown in Fig 2(b). This model divides the soil column into three layers: upper, middle, and 194 bottom layers, to simulate the surface flow, interflow and base flow, respectively (composing the stream discharge). In this model, the following 9 parameters need calibration: maximum root zone 195 196 storage S_{rmax} [L], initial root zone storage, $S_{r\theta}$ [L], Mannings' surface roughness, n [-], maximum draining capacity in the middle layer, T_d [L/T], lateral transmissivity, T_i [L²/T], interflow recession 197 coefficient, m_i [L], base-flow recession coefficient, K_b [T⁻¹], groundwater recharge or percolation, K_{per} 198 199 [L/T] and bypass flow rate, Q_{by} [L/T]. 200 For the upper layer, there are two ways to reduce the storage. One way is the evapotranspiration, 201 which is turned off as mentioned before. The other way is the quick bypass flow (Q_{by}) from the upper

- 202 layer to the bottom layer when the saturation exceeds 0.6. When the storage is fully filled by
- 203 precipitation, the surplus rainfall infiltrates into the middle layer. However, the infiltrating water
- 204 depends on the remaining space in the middle layer or on the maximum draining capacity T_d . Therefore,
 - 6

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205 the saturation excess runoff can be described as the following:

206
$$\boldsymbol{\delta}_{i} = \begin{cases} P_{i} - D_{i} & \text{if } T_{d} > D_{i} \\ P_{i} - T_{d} & \text{if } T_{d} \le D_{i} \end{cases}$$
(5)

207

where P_i and D_i are the rainfall on ith cell [L] and the local soil moisture deficit [L], respectively. δ_i is

- 209 the surplus rainfall [L], which transforms to the surface runoff. In this equation, D_i is only the condition 210 to determine the rainfall converted to surface runoff. For the second equation in equation (5), the
- 211 maximum drainage capacity, T_{d} , is the upper limit to avoid too much rainfall infiltrating into dryer or
- 212 near-ridge cell so rapidly. The observational study in New Zealand revealed the larger contribution
- 213 from new water in ridge top sites, indicating the possible generation of infiltration excess runoff
- 214 (Sklash et al., 1986). Although the second equation is somehow similar to infiltration capacity based
- 215 runoff, this equation mainly followed the concept of saturation excess runoff in most cases.
- For the middle layer, the local soil moisture deficit D_i can be estimated by

217
$$D_i = \overline{D} + m_i (\gamma - \ln \left(\frac{u_i}{\tau_i \cdot tan \beta_i} \right))$$
(6)

where \overline{D} is the mean value of the soil moisture deficit over the catchment area. This equation uses the difference between the local topographic index and the average topographic index to estimate the possible local soil moisture deficit everywhere. Meanwhile, the subsurface flow for each time step can be estimated by the following recession curve function:

222
$$Q_i = Q_0 \cdot \exp\left(-\frac{\overline{D}}{m_i}\right)$$
 (7)

where Q_i is the interflow $[L^3/T]$ and $Q_0 = A \cdot \exp(-\gamma)$ is the discharge when the average soil moisture deficit is zero.

225 For the base flow, the same linear reservoir concept is applied to simulate the base flow as follows:

$$226 \quad \boldsymbol{Q_b} = \boldsymbol{S_b} \boldsymbol{K_b} \quad (8)$$

- where Q_b is the base flows [L³/T]. S_b [L] and K_b [L²/T] are water level and the recession coefficient, respectively. The initial S_b can be derived from the initial observed discharge at time t = 0. The above three flows compose the stream discharge at the catchment outlet.
- The two models show different model structures, particularly in the surface flow generation. The TOPMODEL generates the surface flow depending on the variable source area. The saturation in the middle layer is the key factor in generating surface flow. However, the HBV model separates the rainfall into root zone and inter-flow storage through the effective precipitation calculation, which is proportional to the soil moisture content and shape factor. In other words, the effective precipitation is
 - 7

註解 [R16]: For detailed comment #5

235 the valve that controls the recharge into interflow storage before reaching full saturation in the root 236 zone. In addition, the surface flow occurs only when the water level in the interflow storage is higher 237 than the threshold L, which means that the surface flow in HBV is controlled by threshold L. Hence, 238 the maximum interflow is somewhat limited. To set the common ground for the two models, we 239 introduced the same base-flow governing equation to investigate the different model behaviors. The 240 experiment design can aid us in understanding more about the model behaviors. Further, the 241 sensitivities of the parameters were also evaluated to clarify the role of the allocation of the three flows. 242 Hydrograph shapes, runoff volumes, and correlation coefficient were three measures used to discuss 243 the model performance. Finally, the two rainstorms, supplemented by the intensive geochemical 244 dataset for the stream flow compositions, were used to validate the simulated compositions. 245

246 2-3 Calibration and Performance Evaluation

247 In hydrological modeling, calibration is intensively used to determine the unknown and/or 248 non-measurable parameters by ranking the performance measure between simulations and 249 observations. However, many previous studies showed that no unique performance measure is better 250 suited than another for the calibration of a model (Gupta et al., 1998; Yapo et al., 1998; Madsen, 2000; 251 Vrugt et al., 2003); therefore, multi-objective calibration has been proposed and applied widely. For 252 the multi-objective calibration, the simulations laid on the Pareto front can be regarded as the best 253 simulations, and the corresponding parameters are good candidates for further applications (e.g., 254 parameter uncertainty estimation). Here, we use two performance measures for calibration. One 255 measure is Nash efficiency coefficient, Nash EC (proposed by Nash and Sutcliffe, 1970). This 256 coefficient (Equation 9) varies from negative infinity to unity, where unity represents a perfect match 257 and zero indicates that the simulation performance is identical to the expected value (mean) of the 258 observations. However, this coefficient using the squared difference between simulation and 259 observation leads to high sensitivity in the high flow. To consider the low-flow properly, a variant 260 Nash EC_{log} , which transfers the simulated and observed discharges into a logarithmic scale, is applied 261 as the other performance measure. In this study, over 80,000 parameter sets were generated by the 262 uniform or log-uniform distribution for the two models. The detailed description of parameter range 263 and used distribution was illustrated in Table 2. The best simulations and the corresponding parameter 264 sets, defined by the highest values of the Nash EC and Nash EClog, are selected for further discussion.

265
$$Nash_EC = 1 - \frac{\sum_{i=1}^{T} (Q_{sim,i} - Q_{obs,i})^2}{\sum_{i=1}^{T} (Q_{obs,i} - \overline{Q_{obs}})^2}$$
 (9)

where Q_{sim} and Q_{obs} are the simulated and observed discharges, respectively, and *T* is the total of time step during the evaluation period.

269 In addition to the two performance measures for calibration, we also used the following three 270 indexes, namely, Nash EC, EQV, and CC, to show the extent of the agreement between simulations 271 and observations. EOV defines as the ratio of the total simulated volume over the total observed 272 volume. This index is useful in investigating the volume bias which is important for irrigation, 273 reservoir operation, and flood control. CC is the correlation coefficient between simulations and 274 observations. Notably, a high CC with poor EQV indicates that the simulation has a highly similar 275 shape with the observations but biases in the runoff volume. Based on the three indexes, the 276 simulations in terms of hydrograph shape, volume, and correlation can be assessed comprehensively.

277

266

278 **3. Results**

279 After intensive simulations and calibration, the performances of Nash EC and Nash EClog for the 280 HBV- and TOP-derived simulations are shown in Fig. 3. The overall Nash_EC and Nash_EClog values 281 were scattered in an awl shape, and the maximum values met at approximately 0.65 in both axes for the 282 two models. In general, both models could simulate the rainstorm fairly well showing a good 283 agreement between the two model-derived simulations and observations. Notably, the pareto front 284 may not exist when the performance measures are inherently similar or the simulation has the similar 285 tradeoff weight between the performance measures. In this circumstance, all the simulations approach 286 to a specific point. Therefore, we selected the best 15 simulations (the highest values of the sum of the 287 two measures) as the representative simulations, and their corresponding parameter sets were regarded 288 as the well-performed sets for each model (discussed later). The detailed simulation results are 289 tabulated in Table 3. 290 In the HBV-derived simulations, the Nash EC values varied from 0.16 to 0.91 with a mean of 0.70. 291 For the TOPMODEL, the Nash EC values ranged from 0.10 to 0.89 with a mean of 0.64. The

HBV-derived simulations were slightly better than the TOP-derived simulations. The standard

deviations for the HBV- and TOP-derived models were 0.22 and 0.19, respectively, showing a similar

level of variations among events. For *EQV*, the average performance of the two models was similar

295 (0.92 and 0.93 for HBV and TOP, respectively). However, the range varied from 0.56 to 1.52 for HBV

and from 0.68 to 1.20 for TOP, respectively, showing that TOPMODEL could make the simulated

297 volume more consistent (less variation) with observations. For the correlation coefficient, the average
9

註解 [R17]: For detailed comment #7

CC for HBV and TOP was 0.94 and 0.88, respectively, which indicated that the HBV simulations
 might give a higher correlation than the TOP simulations. The standard deviation of the TOP-derived

300 *CC* was larger than that of the HBV-derived *CC*.

301 In summary, both model could simulated the streamflow in the similar performance level in

302 terms of the hydrograph shape. TOP-derived simulation has the more consistent discharge volume

- 303 than the HBV-derived simulation. However, HBV gave higher correlation coefficient than
- 304 TOPMODEL. However, the outperformed parameter sets do not guarantee applicability for the all
- 305 events (Huang et al., 2009). Although the pursuit of higher performance measures (e.g., average
- 306 *Nash_EC* and *Nash_EC*_{log} in this study) is the main consideration of calibration, pursuing the smaller
- 307 variation in order to increase the applicability for all events (e.g., different hydrological conditions)
- 308 should be emphasized as well.
- 309

310 4. Discussions

311 4-1 Well-performed simulation and corresponding parameter sets

312 The well-performed simulations and the performance in terms of Nash EC, EQV, and CC are 313 illustrated to reveal the variation in the simulations among the rainstorms (Fig. 4). In Fig. (4a.1) and 4(b.1), we found that the Nash EC values of the 15 well-performed simulations for each event were 314 315 quite diverse for the models, particularly in the small events. For the correlation coefficient, the HBV 316 model presented good and consistent simulations for all events (Fig. 4a.2). The higher correlation 317 coefficient values indicated that the simulations and observations all agreed well in terms of 318 hydrograph shape. In contrast, the TOP-derived simulations for small events were highly divergent 319 (Fig. 4b.2). For the runoff volume estimations, the HBV-derived simulations for small events were 320 distinctly overestimated but were underestimated for large events (Fig. 4a.3). However, the TOP-derived simulations estimated the runoff volume better and remained more consistent compared 321 322 to the HBV model (Fig. 4b.3). 323 This comparison showed the both models could not simulate the small events very well. It may 324 be due to the fact that the spatial rainfall distributions of the small rainstorm are usually more 325 heterogeneous than that of large events (Huang et al., 2012). Nevertheless, HBV could outperform in 326 correlation coefficient, but it significantly overestimated the discharge. In contrast, TOPMODEL 327 showed a promising and consistent result in runoff volume, but failed in correlation coefficient. The

328 diverse values for some small events in TOPMODEL may result from the surface runoff mechanism. 10 **註解 [R19]:** For detailed comment #10

1 註解 [R18]: For detailed comment #9

| 329 | The surface runoff mostly generates in source area. Given a biased precipitation pattern on source |
|-----|---|
| 330 | area it would lead to a significant over- or underestimation in surface runoff rather than infiltration |
| 331 | excess runoff (Huang et al., 2011). We cannot expect that the hydrological models can simulate such |
| 332 | events well only based on the limited data. As for runoff volume estimation, the TOP-derived |
| 333 | simulations maintained the water balance better than that derived by HBV. Taking a closer look at the |
| 334 | model structures we found that the runoff estimation by HBV strongly depends on the storage status |
| 335 | and the yield parameters (e.g., K_s , K_i , and K_b); therefore, it may not keep the water mass balance. In |
| 336 | other words, HBV is more flexible in adjusting the simulated streamflow. In reality, many watersheds |
| 337 | may not follow the mass balance, but it has been the basic assumption in many hydrological models. |
| 338 | Therefore, the water mass balance assumption may need other environmental backgrounds to support. |
| 339 | For the corresponding parameter sets, the retrieved parameter values were normalized to the upper |
| 340 | and lower limits and linked to one another for showing the connectivity (Fig. 5). This figure shows that |
| 341 | different parameter combinations could produce virtually equal model simulations. However, some |
| 342 | parameters are constrained within a limited range indicating the parameters are more sensitive and |
| 343 | dominant in simulation (Madsen, 2000; Madsen et al., 2003). The pattern of parameter combination |
| 344 | also represents the model behavior. For HBV, once the parameters, S_{ramx} , K_s , L , and K_b are fixed or |
| 345 | determined; the similar simulations can be expected. Meanwhile, the similar parameter combinations |
| 346 | show a similar model behavior in simulation. In contrast, only the parameter DE_i and K_{per} are sensitive |
| 347 | and other parameters are diverse in TOPMODEL simulations. It seems that more than one type of |
| 348 | parameter combinations can achieve similar performance which indicates that more than one type of |
| 349 | streamflow compositions can be obtained. In this regard, a model which gives the more types of |
| 350 | parameter combinations with similar performance has high flexibility. |
| 251 | |

352 4-2 Comparison of HBV- and TOP-derived Stream Composition

The simulated three flows for all rainstorms are listed in Table 4. The proportions of the 353 354 HBV-derived flows are 0.22, 0.29, and 0.49 for the surface flow, interflow, and base flow, respectively. 355 By contrast, the TOP-derived flows for the surface flow, interflow, and base flow are 0.27, 0.50, and 356 0.23, respectively. Obviously, the base flow in HBV model plays a dominant role in simulating the streamflow; however, in TOPMODEL interflow is the major component for streamflow. Furthermore, 357 358 the three flow proportion against average rainfall intensity and storm duration are shown in Figs. 6-8. 359 Figure 6 shows that both simulated surface flow proportions increase from 0.1 to 0.5 with the increase 360 in the average rainfall intensity from 2.0 mm/h to 11.0 mm/h. Meanwhile, both simulated surface flow 11

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註解 [R21]: For detailed comment #12

註解 [R22]: For technical comment #1

proportions decrease from 0.5 to 0.1 with the increase in the storm duration from 40 h to 160 h.
However, the HBV-derived surface flows among events show larger variation than those derived from
TOPMODEL. Nevertheless, the consistent results in surface flow derived from the two model
structures, even for extreme events, reveal that the surface flow proportions which, as expected,

increase and decrease with the average rainfall intensities and storm durations, are fairly reliable andrealistic.

367For the interflow, the models showed discrepant relationships with the average rainfall intensity368and storm duration (Fig. 7). The HBV model showed lesser interflow (~0.3) than TOPMODEL (~0.5).

369 Notably, the two model behaviors had opposite responses to the storm duration. As the storm duration

increased, the TOP-derived interflow increased from ~0.3 to 0.6. However, the HBV-derived

interflow decreased from \sim 0.4 to 0.15. The opposite behaviors were due to the model structure.

372 Theoretically, TOPMODEL simulates a larger interflow as using the decrease in the average soil

deficit, which is also used to determine the variable source area. In our case, the maximum variable
source area was approximately 30% to 65%. Therefore, TOPMODEL can be expected to give even
larger interflow for more torrential rainstorms. By contrast, the HBV model simulates the interflow
using the limited depth of *L*. When heavy rainfall exceeds *L*, surface runoff occurs and the inter-flow

storage is reduced rapidly. Therefore, the inter flow proportion is relatively limited even when thestorm duration increases.

379 For the base flow, the two models showed similar patterns with average rainfall intensity (Fig. 8). 380 However, the HBV ranges from 0.7 to 0.1, which is much wider than that derived from TOP (from 0.4 381 to 0.1). It is an indication that for small events, the base flow is dominant in HBV, but the inter flow 382 is important in TOPMODEL. Meanwhile, the HBV-derived base flow increases with the increase in 383 the storm duration; however. TOP-derived base flow (avg = 0.23; std. = 0.098) is stable for all events. 384 In the TOPMODEL structure, the middle layer yields interflow efficiently and thus the base flow 385 remains unchanged. By contrast, the HBV model recharges more to the lower reservoir in order to fit 386 the streamflow. Therefore, the base flow is compelled to increase, particularly during extreme 387 rainstorms, which indicates that HBV may be more suitable for watersheds with thin soil layer. 388 Likewise, TOPMODEL is expected to be preferable for watersheds with thick soil layer. In this regard, 389 we could expect that the proper model choice should be based on the extensive spectrum of rainstorms 390 and the extra environmental background, instead of intensive calibration. Meanwhile, such 391 intercomparison between models also increased our understanding of the model structure and 392 behavior.

4-3 Comparison with Chem-hydrograph

395 Furthermore, geochemical dataset was introduced to derive the streamflow composition through 396 the end-member mixing analysis (EMMA). Lee et al. (2010; 2011; 2013) collected water samples in 397 wells and soil columns for the end member of the base flow and interflow. Besides, we sampled the 398 stream and rainwater at high frequency (~3 h interval) during event no. 15 and 17. The 399 chem-hydrographs of the three components after the EMMA are shown in Figs. 9(a) and (b) for event nos. 15 and 17, respectively. It shows that the base flow was quite stable and only changed during the 400 401 flood peak time. In general, the base flow occupied approximately 25% of the total runoff. The 402 response of interflow surged and diminished rapidly. The interflow proportion was similar to the base 403 flow. The remaining discharge was attributed to the surface flow. From the geochemical perspective, 404 the surface flow is the most important component during the rainstorm period, which occupies 405 approximately 40% to 50% of the total runoff volume.

406 EMMA is recognized as a useful analysis tool for hydrograph separation, although the number and 407 selection of geochemical tracers are sometimes questionable (Barthold et al., 2011; Carrera et al., 408 2004). Despite the uncertain proportion of discharge components and the objective identification of the 409 end members, the result of the stream composition, in terms of relative proportion, is relatively reliable. 410 It substantially provides another perspective for stream flow composition. More importantly, the 411 time-series changes of the flows should be realistic. In this regard, the EMMA-derived stream 412 composition could be a good reference for comparison with the model-derived ones. 413 The EMMA- and the model-derived results are listed in Table 4. The HBV model simulation 414 shows that the interflow and base flow are dominant components for event nos. 15 and 17, respectively. 415 By contrast, TOPMODEL considers the interflow as the superior component; the surface flow is only 416 secondary. No model yields the same EMMA-derived composition with regard to the proportion.

417 From the quantity perspective, the TOP-derived surface flow shows a good agreement with that

418 derived by EMMA. By contrast, the HBV-derived interflow is close to the EMMA-derived results,

419 although the surface flow is underestimated.

The quantity and the response-time results are shown in Figs. 10 and 11 for event nos. 15 and 17, respectively. These two figures show that the HBV-simulated discharge is slightly underestimated, and TOPMODEL overestimated in the streamflow. However, TOPMODEL exhibits a good agreement in the recession segment for the two events. For the interflow, the two models produce fair results. HBV model simulates the base flow as a gentle dome. By contrast, the TOP-derived base flow shows a quick-response steep-bell shape. In the shape comparison, the TOPMODEL outperforms the HBV

- 426 Model. However, a significant time lag of approximately 2 h to 4 h is observed. In our case, the base
- 427 flow responds with the streamflow simultaneously. The base flow could thus be considered a type of
- 428 piston flow. In this regard, incorporating the piston flow theory into the hydrological models can
- 429 improve the time lag, which aids in the interpretation of the base flow.

432 **5. Summary**

Many hydrological models can simulate the stream flow satisfactorily and plausibly. However,
different runoff compositions can result in the similar streamflow. Therefore, recent attention has
shifted to model structures to ensure the accuracy of inferences derived from modeling. In our study,
HBV presented consistent parameter combinations; however, TOPMODEL achieved more parameter
combinations, which implied that HBV preferred to give only one composition for simulated
streamflow, but TOPMODEL could yield more. Rethinking is thus necessary to identify which model
structure is better.

440 In the comparison of the simulated components, both simulated surface flows realistically reflect 441 the nature. The simulated surface flows increased with the increasing the rainfall intensity and 442 decreased with the increasing storm duration. Both base flows also showed the same patterns, although 443 HBV-derived base flow was the dominant. However, the two modeled interflows exhibited a 444 contrasting relationship with the storm duration. The HBV interflow decreased with the increase of 445 duration. Because of the limited interflow storage, this model compelled to percolate much water to the 446 base flow storage in order to fit the observed streamflow, which indicated that HBV could be more suitable for the thin-soil environment. On the other hand, TOPMODEL could be a better choice for 447 448 catchments with thick soil. Compared with the EMMA-derived flows, a significant 2 h to 4 h time lag 449 was observed, which indicated that the real base flow responses are faster than the models have 450 presented. Possibly, an explicit consideration of the piston-flow characteristics in the base flow should 451 be incorporated to improve the time lag and aid in the interpretation of the base flow.

452 Obviously, intercomparison between models under a wide spectrum of rainstorms is a good way to 453 better understand the model behaviors. Besides, the independent geochemical data (e.g. 454 EMMA-derived components) provides another perspective in examining the model behaviors. 455 Undoubtedly, rejecting a model completely is difficult. Alternatively, it is very likely that more than 456 one model structure is essential to capture the streamflow and tracer dynamics simultaneously when 457 the rainstorm cases and environment background are insufficient. In this regard, we need to revisit the 458 model behavior and the model structure again independently validation for testing hydrological 459 models.

462

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| Event | Date | Duration | Rainfall | Max. | Runoff | Peak | RC* ³ |
|-----------|---------------------------------------|----------|----------|------------------|--------|---------|------------------|
| no. | | (hr) | (mm) | RI* ² | volume | flow | |
| | | | | (mm/hr) | (mm) | (mm/hr) | |
| 1 | 1986/09/18 | 108 | 316.0 | 26.5 | 140.3 | 5.4 | 0.44 |
| 2 | 1986/08/22 | 95 | 247.2 | 15.6 | 69.9 | 2.9 | 0.28 |
| 3 | 1989/09/10 | 120 | 595.3 | 38.4 | 330.7 | 13.4 | 0.56 |
| 4 | 1990/09/07 | 96 | 454.9 | 28.6 | 237.6 | 7.9 | 0.52 |
| 5 | 1990/08/18 | 121 | 425.6 | 24.9 | 245.5 | 6.9 | 0.58 |
| 6 | 1990/06/22 | 105 | 359.7 | 28.8 | 132.2 | 3.7 | 0.37 |
| 7 | 1996/07/30 | 110 | 451.1 | 27.3 | 363.8 | 13.5 | 0.81 |
| 8 | 1997/08/28 | 90 | 228.5 | 17.5 | 120.8 | 5.2 | 0.53 |
| 9 | 1998/10/15 | 120 | 273.6 | 23.3 | 128.6 | 2.8 | 0.47 |
| 10 | 2000/08/22 | 94 | 398.8 | 25.7 | 107.3 | 3.5 | 0.27 |
| 11 | 2004/08/23 | 80 | 452.9 | 25.9 | 351.1 | 17.5 | 0.78 |
| 12 | 2004/07/02 | 96 | 431.3 | 35.3 | 112.3 | 4.5 | 0.26 |
| 13 | 2005/08/31 | 40 | 426.9 | 39.5 | 198.3 | 17.4 | 0.46 |
| 14 | 2006/06/08 | 144 | 409.4 | 20.3 | 247.9 | 5.5 | 0.61 |
| 15^{*1} | 2007/08/17 | 87 | 490.2 | 38.5 | 334.3 | 13.9 | 0.68 |
| 16 | 2007/09/17 | 97 | 184.5 | 15.0 | 75.8 | 2.3 | 0.41 |
| 17^{*1} | 2007/10/05 | 120 | 629.7 | 35.4 | 403.2 | 15.4 | 0.64 |
| 18 | 2008/07/17 | 90 | 200.0 | 21.7 | 93.0 | 2.6 | 0.47 |
| 19 | 2008/09/12 | 144 | 836.4 | 10.7 | 672.6 | 11.6 | 0.80 |
| 20 | 2008/09/27 | 91 | 672.9 | 33.3 | 483.4 | 16.5 | 0.72 |
| 21 | 2009/08/06 | 154 | 829.4 | 22.0 | 622.6 | 11.6 | 0.75 |
| 22 | 2009/10/05 | 72 | 220.5 | 14.9 | 37.8 | 2.0 | 0.17 |
| 23 | 2010/9/19 | 72 | 253.1 | 28.9 | 103.7 | 4.9 | 0.41 |
| | Average 102 430.0 26.1 245.1 8.4 0.52 | | | | | | |

Table 1 the rainstorm characteristics in Chi-Chia-Wan catchment since 1986

608 *¹ meant the events had the chem-hydrographs for validation

609 *² Max RI was the maximum rainfall intensity during the event

 *3 RC, runoff coefficient indicated the total runoff over the total rainfall

Table 2 the descriptions, ranges, and distributions of parameters for HBV and TOPMODEL ______ 主任 [R23]: For detailed comment #6

| 6 | 1 | 5 |
|---|---|---|
| 0 | I | э |

| HBV | | | | TOPMODEL | | | |
|------------------|------------|------------|--------------|-----------|------------|------------|--------------|
| Parameter | Unit | Range | Distribution | Parameter | Unit | Range | Distribution |
| n | [-] | 0.0 - 1.0 | Uniform | n | [-] | 0.0 - 1.0 | Uniform |
| Srmax | [L] | 0.0 - 35.0 | Uniform | Srmax | [L] | 0.0 - 35.0 | Uniform |
| S_{r0} | [L] | 0.0 - 35.0 | Uniform | S_{r0} | [L] | 0.0 - 35.0 | Uniform |
| Beta | [-] | 1.0 - 10.0 | Uniform | T_d | [L/T] | 10.0 - | Uniform |
| L | [L] | -3.01.0 | Log uniform | m_i | [L] | 0.0 - 2.0 | Log uniform |
| Ks | $[T^{-1}]$ | 0.0 - 1.0 | Uniform | T_i | $[L^2/T]$ | 1.0 - 10.0 | Uniform |
| K_i | $[T^{-1}]$ | -3.01.0 | Log uniform | K_b | $[T^{-1}]$ | -3.01.0 | Log uniform |
| K _b | $[T^{-1}]$ | -3.01.0 | Log uniform | Kper | [L/T] | -3.01.0 | Log uniform |
| K _{per} | [L/T] | -2.0 - 1.0 | Log uniform | Q_{by} | [L/T] | -3.01.0 | Log uniform |
| Q_{by} | [L/T] | 0.0 - 13.0 | Uniform | | | | |

| Event | HBV Model | | | TOP Model | | |
|---------|-----------|------|------|-----------|------|------|
| no. | Nash EC | EQV | CC | Nash EC | EQV | CC |
| 1 | 0.87 | 0.91 | 0.96 | 0.86 | 0.91 | 0.94 |
| 2 | 0.72 | 1.37 | 0.97 | 0.68 | 0.81 | 0.86 |
| 3 | 0.80 | 0.72 | 0.97 | 0.89 | 0.84 | 0.95 |
| 4 | 0.16 | 0.56 | 0.96 | 0.79 | 0.85 | 0.93 |
| 5 | 0.25 | 0.56 | 0.97 | 0.78 | 0.76 | 0.97 |
| 6 | 0.84 | 1.07 | 0.97 | 0.67 | 1.11 | 0.93 |
| 7 | 0.81 | 0.73 | 0.95 | 0.75 | 0.78 | 0.92 |
| 8 | 0.77 | 0.86 | 0.92 | 0.47 | 0.87 | 0.74 |
| 9 | 0.86 | 0.92 | 0.96 | 0.43 | 0.83 | 0.73 |
| 10 | 0.91 | 0.97 | 0.97 | 0.61 | 0.84 | 0.82 |
| 11 | 0.84 | 0.89 | 0.95 | 0.88 | 1.05 | 0.97 |
| 12 | 0.66 | 1.11 | 0.87 | 0.54 | 1.06 | 0.89 |
| 13 | 0.69 | 0.98 | 0.84 | 0.70 | 1.17 | 0.89 |
| 14 | 0.56 | 0.79 | 0.92 | 0.78 | 1.00 | 0.92 |
| 15* | 0.82 | 0.78 | 0.96 | 0.61 | 1.00 | 0.94 |
| 16 | 0.75 | 1.14 | 0.93 | 0.60 | 0.94 | 0.83 |
| 17* | 0.83 | 0.82 | 0.97 | 0.81 | 1.15 | 0.98 |
| 18 | 0.85 | 1.06 | 0.95 | 0.10 | 0.68 | 0.63 |
| 19 | 0.43 | 0.64 | 0.92 | 0.59 | 0.95 | 0.90 |
| 20 | 0.89 | 0.86 | 0.96 | 0.40 | 1.20 | 0.94 |
| 21 | 0.60 | 0.70 | 0.92 | 0.69 | 0.88 | 0.86 |
| 22 | 0.30 | 1.52 | 0.95 | 0.62 | 0.82 | 0.85 |
| 23 | 0.78 | 1.14 | 0.97 | 0.38 | 0.80 | 0.75 |
| Average | 0.70 | 0.92 | 0.94 | 0.64 | 0.93 | 0.88 |
| Std. | 0.22 | 0.24 | 0.03 | 0.19 | 0.14 | 0.09 |

| 620 Table 3 the HBV- and TOP-derived simulations evaluated by | y Nash_EC, EQV, and CC |
|--|------------------------|
|--|------------------------|

621 *Note that the value for each event is the average of the representative simulations.

| Event no. | HBV Model derived | | | TOP Model derived | | | |
|-----------|-------------------|------------|-----------|-------------------|------------|-----------|--|
| | Surface flow | Inter flow | Base flow | Surface flow | Inter flow | Base flow | |
| 1 | 0.26 | 0.31 | 0.43 | 0.30 | 0.51 | 0.19 | |
| 2 | 0.17 | 0.32 | 0.51 | 0.26 | 0.46 | 0.28 | |
| 3 | 0.27 | 0.31 | 0.41 | 0.33 | 0.50 | 0.16 | |
| 4 | 0.17 | 0.23 | 0.60 | 0.21 | 0.56 | 0.23 | |
| 5 | 0.15 | 0.22 | 0.63 | 0.16 | 0.57 | 0.27 | |
| 6 | 0.18 | 0.27 | 0.55 | 0.18 | 0.56 | 0.26 | |
| 7 | 0.34 | 0.35 | 0.31 | 0.44 | 0.44 | 0.13 | |
| 8 | 0.14 | 0.26 | 0.60 | 0.10 | 0.58 | 0.32 | |
| 9 | 0.11 | 0.23 | 0.66 | 0.10 | 0.55 | 0.35 | |
| 10 | 0.26 | 0.32 | 0.42 | 0.32 | 0.49 | 0.18 | |
| 11 | 0.41 | 0.39 | 0.20 | 0.51 | 0.41 | 0.07 | |
| 12 | 0.18 | 0.30 | 0.52 | 0.24 | 0.56 | 0.20 | |
| 13 | 0.43 | 0.40 | 0.17 | 0.53 | 0.39 | 0.08 | |
| 14 | 0.07 | 0.16 | 0.77 | 0.09 | 0.54 | 0.37 | |
| 15* | 0.31 | 0.42 | 0.27 | 0.39 | 0.46 | 0.16 | |
| 16 | 0.09 | 0.24 | 0.67 | 0.09 | 0.52 | 0.40 | |
| 17* | 0.29 | 0.31 | 0.40 | 0.30 | 0.55 | 0.15 | |
| 18 | 0.11 | 0.25 | 0.64 | 0.16 | 0.46 | 0.38 | |
| 19 | 0.25 | 0.27 | 0.48 | 0.27 | 0.58 | 0.15 | |
| 20 | 0.36 | 0.34 | 0.31 | 0.40 | 0.44 | 0.16 | |
| 21 | 0.20 | 0.25 | 0.55 | 0.22 | 0.61 | 0.17 | |
| 22 | 0.13 | 0.29 | 0.58 | 0.27 | 0.38 | 0.36 | |
| 23 | 0.26 | 0.35 | 0.39 | 0.45 | 0.30 | 0.24 | |
| Average | 0.22 | 0.29 | 0.49 | 0.27 | 0.50 | 0.23 | |
| Std. | 0.10 | 0.06 | 0.16 | 0.13 | 0.08 | 0.10 | |

Table 4 The proportion of the simulated surface-, inter-, and base-flows derived from the two models HBV Model derived TOP Model derived

| at | | Chem-hydrograph | | HBV Model | | TOP Model | |
|-------|--------------|-----------------|------------|-------------|------------|-------------|------------|
| Event | Flow type | Amount | Proportion | Amount | Proportion | Amount | Proportion |
| Щ | | (m^3/sec) | (%) | (m^3/sec) | (%) | (m^3/sec) | (%) |
| 15 | Surface-flow | 3949 | 40.5 | 2428 | 31.1 | 3711 | 38.5 |
| | Inter-flow | 2905 | 29.8 | 3305 | 42.3 | 1689 | 45.5 |
| No. | Base-flow | 2896 | 29.7 | 2076 | 26.6 | 1537 | 16.0 |
| 17 | Surface-flow | 5562 | 47.3 | 2690 | 29.2 | 4116 | 30.4 |
| No.] | Inter-flow | 2928 | 24.9 | 2837 | 30.8 | 7460 | 55.1 |
| Z | Base-flow | 3269 | 27.8 | 3685 | 40.0 | 1963 | 14.5 |

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 Table 5 Stream discharge composition derived from two models and EMMA



Figure 1. The landscape, stream network and topographic index pattern within the Chi-Chia-Wancatchment. The raingages and flow stations are labeled by red square and black dot.





643 symbols mean the flow is modeled by linear reservoir





Figure. 3 The Nash_EC and Nash_EC_{log} values corresponding to the generated parameter sets in

calibration process. The HBV-derived and TOP-derived results are shown in left and right panel,

respectively. The x-axis and y-axis represent the Nash_EC_{log}, and Nash_EC, respectively. The gray

circles represent the simulations partly and the black ones are the best 15 simulations sorted out by the

- equally weighted ranking.
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Figure 5. Normalized range of parameter values of the 15 best simulations (gray lines) for HBV Model
(a) and TOP Model (b). The vertical dashed lines represent the parameter in logarithmic scale. The
black lines indicate the best one for the two models.



Figure 6. The variation of HBV-derived surface flow against averaged rainfall intensity (a) and storm duration (b). The variation of TOP-derived surface flow against averaged rainfall intensity (c) and storm duration (d). The black dot and gray line represent the mean and the standard deviation among the best simulations.



Figure 7. The variation of HBV-derived inter-flow against averaged rainfall intensity (a) and storm duration (b). The variation of TOP-derived inter-flow against averaged rainfall intensity (c) and storm duration (d). The black dot and gray line represent the mean and the standard deviation among the best simulations.



Figure 8. The variation of HBV-derived base-flow against averaged rainfall intensity (a) and storm duration (b). The variation of TOP-derived base-flow against averaged rainfall intensity (c) and storm duration (d). The black dot and gray line represent the mean and the standard deviation among the best simulations.





Figure 9. The EMMA-estimated three discharge components of event no. 15 and no. 17 are shown in
(a) and (b), respectively. The black lines represented the observed stream discharge. The green and red
lines indicate the estimated inter- and base-flow derived from EMMA. (seeing text in section 4-3 for
details)



Figure 10. Comparison between the measured stream discharges (event no. 15) and the best 15 simulations derived from HBV model (a.1) and TOP model (b.1). The comparison of interflow derived from mixing analysis (green dots) with the simulated inter-flows (sky blue zone) derived from HBV model (a.2) and TOP model (b.2), respectively. The comparison of base flow derived from mixing analysis (red dots) with the simulated inter-flows (blue zone) derived from HBV model (a.3) and TOP model (b.3), respectively.

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Figure 11. Comparison between the measured stream discharges (event no. 17) and the best 15 simulations derived from HBV model (a.1) and TOP model (b.1). The comparison of interflow derived from mixing analysis (green dots) with the simulated inter-flows (sky blue zone) derived from HBV model (a.2) and TOP model (b.2), respectively. The comparison of baseflow derived from mixing analysis (red dots) with the simulated inter-flows (blue zone) derived from HBV model (a.3) and TOP model (b.3), respectively.