

**Interpolation of
extensive routine
water pollution
monitoring datasets**

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Interpolation of extensive routine water pollution monitoring datasets: methodology and discussion of implications for aquifer management

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Abstract

A large fraction of the fresh water available for human use is stored in groundwater aquifers. Since human activities such as mining, agriculture, industry and urbanization often result in incursion of various pollutants to groundwater, routine monitoring of water quality is an indispensable component of judicious aquifer management. Unfortunately, groundwater pollution monitoring is expensive and usually cannot cover an aquifer with the spatial resolution necessary for making adequate management decisions. Interpolation of monitoring data between points is thus an important tool for supplementing measured data. However, interpolating routine groundwater pollution data poses a special problem due to the nature of the observations. The data from a producing aquifer usually includes many zero pollution concentration values from the clean parts of the aquifer but may span a wide range (up to a few orders of magnitude) of values in the polluted areas. This manuscript presents a methodology that can cope with such datasets and use them to produce maps that present the pollution plumes but also delineates the clean areas that are fit for production. A method for assessing the quality of mapping in a way which is suitable to the data's dynamic range of values is also presented. Local variant of inverse distance weighting is employed to interpolate the data. Inclusion zones around the interpolation points ensure that only relevant observations contribute to each interpolated concentration. Using inclusion zones improves the accuracy of the mapping but results in interpolation grid points which are not assigned a value. That inherent trade-off between the interpolation accuracy and coverage is demonstrated using both circular and elliptical inclusion zones. A leave-one-out cross testing is used to assess and compare the performance of the interpolations. The methodology is demonstrated using groundwater pollution monitoring data from the Coastal aquifer along the Israeli shoreline.

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1 Introduction

Groundwater is an essential resource, especially in arid and semi-arid countries. In many cases, the groundwater aquifers are vulnerable to contamination from natural and anthropogenic sources. The vulnerability of the groundwater can be assessed using various means (e.g. Soutter and Must, 1998; Al-Hanbali et al., 2008; Baalousha, 2010; Javadi et al., 2011) however, the large uncertainty in these assessments and the operational requirements of water production call for more accurate estimations of the spatial distribution of pollutants. Probably the most important mechanism for detection of pollutants and protection of the groundwater is a pollution monitoring network (Baalousha, 2010). With the increasing demand for fresh water and the dwindling resources, the prevalence of comprehensive aquifer monitoring is rising. However, due to the cost of the monitoring operations, the networks cannot usually cover the aquifers at an adequate spatial resolution. Interpolation of monitoring data is thus used extensively to enhance the information that the raw monitoring data can provide (e.g. Reed et al., 2004; Kistemann et al., 2008; Morio et al., 2010). Beside enhancing the spatial coverage, the interpolation of pollution monitoring observations provides many additional benefits. It facilitates a visualisation of the spatial distribution of pollutants, avoiding bias due to variability in the spatial density of the monitoring. Interpolated pollution maps on a regular grid also enable quantification of the fraction of the aquifer area unfit for water production. In addition, using interpolated maps, the spatial distributions of different pollutants can be examined and compared at the same set of locations for the purpose of pollution source allocation and can be used as an input for statistical methods like Principle Component Analysis (Carroll et al., 2005; Güler et al., 2012; Melo et al., 2012), which require data on a regular grid.

Two types of interpolation cases are usually considered in the groundwater literature. One involves plumes of high pollution concentration, usually associated with a known point source (Varljen et al., 1999; Kistemann et al., 2008; Adhikary et al., 2011) and the other involves monitoring of major ions (Liu et al., 2005; Adhikary et al., 2010; Tutmez

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and Hatipoglu, 2010). In both these cases the observed pollution concentration data follow well-behaved statistical distributions, and the geostatistical tools developed over the last decades provide good interpolation solutions. However, many anthropogenic pollutants are very rare in the natural environment and routine observations of their concentrations are expected to be, and in many cases are indeed, of zero concentration. In polluted locations though, the concentrations of anthropogenic pollutants can be very high, in some cases many orders of magnitude beyond the limits set by the standards. Interpolation of such data over a large water producing aquifer is problematic. It is very desirable to delineate the areas from which water production should be permitted, but to be able at the same time to indicate the extent of the polluted areas. Clearly, interpolation between high localized pollution values and zero, or very low values, results in an unrealistic smearing of the pollution beyond the true polluted area and leads to inefficient use of groundwater resources. This paper examines the possibility to achieve that goal using simple interpolation schemes which use for the estimation of the interpolated value at each grid point only selected observations within inclusion zones around it. In sparsely monitored areas, and most aquifer areas can be considered as such, this results in grid points at which interpolation is not carried out. The inherent trade-off between the interpolation coverage extent and the quality of the interpolations is discussed and demonstrated. The interpolation testing and comparisons are carried out using a comprehensive cross-testing scheme which is based on a quality measure suitable for the monitoring data's dynamic range of values and for water management purposes.

2 Data

2.1 Study area

Our work is demonstrated using data from Israel's coastal plain aquifer. The aquifer covers about 1800 km² along the coast between the Mt. Carmel ridge in the north to

used. Over the whole period, the concentration of the least monitored pollutant was observed in 423 wells while the concentration of the most monitored one was observed in 1882 wells (see details in Table 1).

The water samples were analyzed by several different laboratories over the years as part of the legal monitoring requirements. All the data are archived in a database of the Israel Water Authority. As part of this study, data quality assurance was carried out. The data were processed such that the different laboratory reporting limits for detection and quantification will not affect subsequent investigations using the data. This entailed setting observations below the quantification threshold to zero. Cases where the quantification threshold record was larger than 20 % of the standard environmental threshold were examined individually and processed according to instructions by experienced Israel Water Authority personnel. When in doubt, data were removed from the set. Descriptive statistics of the records of each pollutant were calculated and presented visually. Aberrant values were examined individually and a decision regarding their fate was taken following consultation with the relevant laboratory and Water Authority personnel.

2.2 Water head data

Water head gradients in the aquifer are used to construct the elliptical inclusion zones of the Inverse Distance Weighting (IDW) interpolation (see next section). Water level is routinely measured in the wells. For each well, the median of its water level observations during 2009–2010 was considered. These median values were projected to the regular grid used for the pollution data interpolation using linear Delaunay triangulation method implemented by the Matlab[®] griddata function (The MathWorks Inc., 2010). The water head gradient direction and magnitude were then calculated for each point on that regular grid using a finite differences scheme.

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3 Methods

3.1 Interpolation methodology

The IDW estimator at a desired interpolation point (x, y) is given by the weighted sum of the data points z_i observed at locations (x_i, y_i)

$$z(x, y) = \sum_{i=1}^N \frac{w_i(x_i, y_i) z_i(x_i, y_i)}{\sum_{j=1}^N w_j(x_i, y_i)}. \quad (1)$$

The weights $w_i(x_i, y_i)$ are given by

$$w_i(x_i, y_i) = \frac{1}{d_i^p}, \quad (2)$$

where d_i is the Euclidean distance between (x, y) and (x_i, y_i) and p is a positive real number. The optimal value of p can be determined by cross-validation using a line search of a range of values. For simplicity this study assumes $p = 2$, which is a very common practice (Isaaks and Srivastava, 1989). In a large aquifer, especially whose flow pattern is interrupted by impermeable barriers, the N observations used for the interpolation at a given point should be a small subset of the complete dataset (Isaaks and Srivastava, 1989). This subset should include only observations at locations which given the advection and dispersion time scales may be associated with the concentration at the interpolation grid point. These locations can be defined as those residing in an inclusion zone around it.

We considered the two types of inclusion zones shown in Fig. 2. The first is a circle with radius ρ , including only data points at a distance shorter than ρ from the interpolation point. The second type of inclusion zone is an ellipse with minor and major semi-axes a and b , respectively. The major axis of the ellipse should be directed along the water advection direction, dictated by the local water head gradient. The ratio between the ellipse axes should manifest the advection and transverse dispersion ratio

and was set as a value reciprocally proportional to the logarithm of the magnitude of the head gradient at the interpolation point. This ratio is in the range $[1, R]$, where R is the maximal ratio between the axes, encountered at the interpolation location where the head gradient is the largest. As R approaches unity, at locations where the head gradient is the smallest, the ellipse approaches a circle with radius a . Figure 3a shows a graph of the ratio between the ellipse axes as a function of the head gradient magnitude. The value of R is set a-priori based on the transverse dispersion expected in the aquifer. For example, in the coastal aquifer the transverse dispersion is assumed usually to be around 2. Thus in the example in Fig. 3a, $R = 4$ for points with the largest (and very rare, see Fig. 3b) head gradient but $R = 2$ for points where the head gradient is 0.001 mm^{-1} , close to the statistical mode of the gradient magnitude values.

The choices of ρ and a have an important impact on the interpolations. Small ρ and a increase the chances that only relevant observations will be included in the computation of an interpolated value. However, the smaller the number of observations used to produce an interpolation value, the larger is its statistical uncertainty. When just very few values are used, an aberrant error in any of them will have a large impact on the result. In the limit where ρ or a are so small that no observations are included, the uncertainty is infinite i.e. we know nothing on the value there. The trade-off in the choice of ρ and a is demonstrated in the next subsection. For comparison we applied also an IDW interpolation where all observations in the aquifer are used in the calculation of each interpolated point. We will refer to this interpolation as infinite inclusion zone interpolation. In the comparison between the circular and elliptical inclusion zone interpolations we always made sure that the total area covered by the inclusion zones around the interpolation points is equal i.e. following the example demonstrated in Fig. 2 at all the interpolation points.

3.2 Assessment of the quality of the interpolation

Any interpolation scheme must be tested in an objective way to assess its performance at producing unobserved values. Given a reasonably large and representative data

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for points which have no data observations in their inclusion zone.) We consider and present SR calculations using the latter, thus providing a performance measure of the interpolations that did take place. The issue of locations for which interpolations are not carried out due to lack of observations in their vicinity will be discussed in the context of the areal coverage that the interpolation can provide.

The computational work required for implementing the processes described in this section was carried out using computer codes written in-house by the authors in the Matlab[®] programming language (The MathWorks Inc., 2010).

4 Results

Figure 5 demonstrates the mapping properties of three types of interpolation schemes for the sample of maximal observed chromium values in each well during the five year period 2006–2010. The three maps were prepared using the same input data and the same 500 m × 500 m interpolation grid, extending over the parts of the aquifer area covered by wells. Figure 5a was produced using all the data for each interpolation point (infinite inclusion zone). Figure 5b was produced using circular inclusion zones with a radius such that the total area which they cover around the interpolation grid points equals the area covered by the corresponding ellipses with minor semi-axes of 1000 m used to produce Fig. 5c. The map in Fig. 5a shows a smooth pattern, with no zero values at all, that covers the full interpolation grid. It is very different from the patterns in Fig. 5b and c which are composed of clusters of very high and very low (including zero) concentration values and which do not cover the full grid area. The differences between Fig. 5b and c are hardly noticeable. Figure 6 shows the fractions of the aquifer area covered by chromium concentrations within percentile brackets of the Israeli chromium concentration drinking water standard of 50 ppb. Using an infinite inclusion zone results in full coverage of the interpolation grid. However, none of the grid points was assigned zero concentration. The fractions of the area which were assigned concentrations in between 0–25, 25–50, 50–75 and 75–100 % of the standard brackets are 0.52, 0.23,

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0.08 and 0.05, respectively. Most important of all, in 0.11 of the interpolation grid points, the concentrations exceed the standard. The fractions of interpolation points yielded by the two interpolations using inclusion zones are very similar to each other. The fractions of the grid points that were not assigned an interpolation value in the circular and elliptical inclusion zones maps were 0.38 and 0.36, respectively. In both cases, fractions of 0.12, 0.46, 0.15 and 0.006 of the grid points have values in the 0–25, 25–50, 50–75 and 75–100 % ranges of the standard brackets, respectively. The fraction of grid points where the drinking water standard is exceeded is 0.021.

The process and analysis described above for chromium was carried out for all 31 pollutants using three inclusion zone sizes (ellipses with minor semi-axes of 500, 1000 and 1500 m, and the corresponding circular zones). It should be noted that a 1000 m distance scale is quite conservative and that most pollution plumes in the Costal aquifer are not expected to have advanced much farther than 1 km from their source. Figure 7 summarizes some interesting results noted in the maps of pollutants 11–31 (the non-major ions). The figure provides the fractions of interpolation points for which the two types of inclusion zone interpolations could not provide a result due to lack of observations in the inclusion zones (Fig. 7a–c). It also provides the fractions of the interpolation points which were assigned concentrations exceeding the health standards (Fig. 7d–f). The most notable point that Fig. 7 shows is that as the inclusion zones increase, the fraction of interpolation points not assigned a concentration decreases, but the fraction of points assigned concentrations exceeding the health standard increases. An additional interesting point is that the fractions of the interpolation points not assigned a concentration is smaller using the elliptical inclusion zones. This is hardly noticeable in Fig. 7a (500 m minor ellipse semi-axes and the corresponding circle radii) but is clear in the other two plots with the differences between them at the $\alpha = 0.078$ and $\alpha = 0.0025$ statistical significance levels for the 1000 and 1500 m minor ellipse semi-axes, respectively (Mann–Whitney test). The differences in the fractions of points exceeding the standard between the two methods are very small and inconsistent. It must be emphasized that by design the total area around the interpolation points cov-

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5 Discussion and conclusions

Interpolation of groundwater pollution data over a large aquifer is a difficult task given the extreme pollution data distributions demonstrated in Fig. 4, and the fact that in most cases there are many pollution sources scattered over the aquifer area. The applicability of using local inclusion zones around the interpolation points was studied in this paper. The quality of the results was assessed using the SR, a simple measure suitable to both the dynamic range of the observations and to management decisions regarding the aquifer. The interpolations using limited inclusion zones proved clearly superior to using an unlimited one (i.e. using all the data to produce each interpolation point). By using limited inclusion zones, the achieved SRs are in the range 0.5–1.0. An aquifer management team can direct a monitoring program based on these results by, for example, enhancing the monitoring of pollutants for which the SR is low. The SRs achieved by the interpolations using circular and elliptical inclusion zones were very similar, with an increase in SR as the inclusion zones decrease.

This study emphasizes the clear trade-off that practitioners must keep in mind when producing interpolation maps using limited inclusion zones. The SRs indeed improve as the zones become smaller. However, that advantage is achieved at the expense of the total fraction of covered area.

Using limited inclusion zones leaves a fraction of the aquifer uncovered i.e. with complete uncertainty regarding the pollutant concentration there. We believe this is a realistic approach which enables an efficient management of the water resources both in terms of water production and pollution remediation. Identifying areas where interpolation cannot be carried out with sufficient confidence helps in directing future monitoring programs. Delineating polluted areas with high level of accuracy focuses the remediation efforts. We noted a modest advantage of using elliptical inclusion zones, which benefits from the water head information. Maps produced using elliptical inclusion zones managed to provide similar information regarding the pollution extent but at a smaller price in terms of areal coverage.

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Table 1. A list of the pollutants monitored in the coastal aquifer whose data were used in this study. The table provides for each pollutant its group affiliation, the number of wells at which it was monitored during the study period and the number of wells at which all the records are of zero concentration. The pollutant groups are: 1 – major ions, 2 – volatile organic compounds, 3 – heavy metals, 4 – fuels, 5 – pesticides/herbicides.

No.	Name	Symbol	Pollutant group	No. of wells	No. of zeros
1	Boron	B	1	1089	10
2	Calcium	Ca	1	1068	0
3	Chloride	Cl	1	1882	0
4	Fluoride	F	1	464	52
5	Bicarbonate	HCO ₃	1	948	0
6	Potassium	K	1	1067	0
7	Magnesium	Mg	1	989	0
8	Sodium	Na	1	1060	0
9	Nitrate	NO ₃	1	1780	13
10	Sulphate	SO ₄	1	1029	2
11	1,1-Dichloroethene	1,1-DCE	2	862	733
12	1,2-Dichloroethane	1,2-DCA	2	865	732
13	Alachlor	Alachlor	5	618	600
14	Aldicarb	Aldicarb	5	423	423
15	Arsenic	As	3	777	457
16	Atrazine	Atrazine	5	641	403
17	Benzene	BNZ	2, 4	1097	784
18	Carbon Tetrachloride	CCl ₄	2	845	758
19	Cadmium	Cd	3	784	672
20	Chloroform	CHCl ₃	2	816	672
21	cis-1,2-Dichloroethene	c-1,1-DCE	2	838	735
22	Chromium	Cr	3	827	139
13	1,2-Dibromo-3-chloropropane	DBCP	3, 4	705	691
24	Ethylene dibromide	EDB	2, 3, 4	814	729
25	Lindane	Lindane	5	602	563
26	Methyl tert-butyl ether	MTBE	2, 4	566	303
27	Nickel	Ni	3	803	514
28	Lead	Pb	3	977	599
29	Simazine	Simazine	5	600	410
30	1,1,1-Trichloroethene	TCE	2	883	616
31	Tetrachloroethene	PCE	2	876	681

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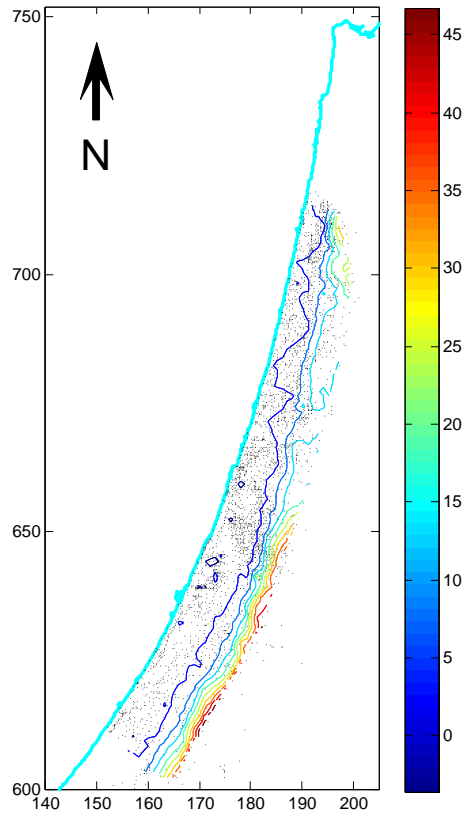


Fig. 1. A map showing the locations of the wells in the aquifer (black dots), and the water head levels (colored thin continuous lines). The colorbar on the right provides the head levels color-key in m. The thick cyan line marks the Mediterranean coast. The coordinates are in the New Israeli Grid in km.

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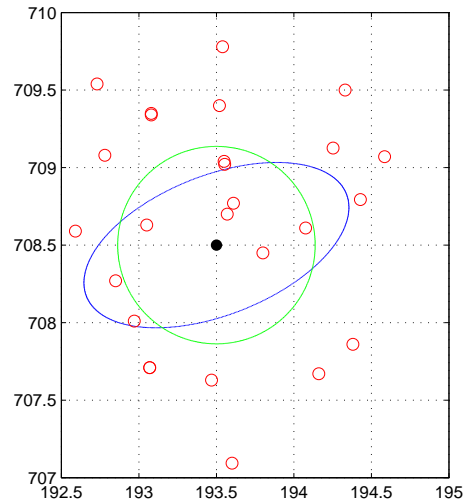


Fig. 2. A diagram showing the two types of inclusion zones (large circle and ellipse) and the well locations (small circles) in the vicinity of grid point (193.5° E, 708.5° N). The coordinates are in the New Israel Grid in km. The head gradient is in direction 68.5° from the north. The head magnitude is 0.0016 mm⁻¹ and R was set at 4, resulting in ellipse axes ratio of 2.0023 (see text and Fig. 3). The minor ellipse semi-axis was set at $a = 450$ m. To have a circular zone with area equal to that of the ellipse, the circle's radius is thus $\rho = (a \cdot a \cdot 2.0023)^{0.5} = 636.76$ m.

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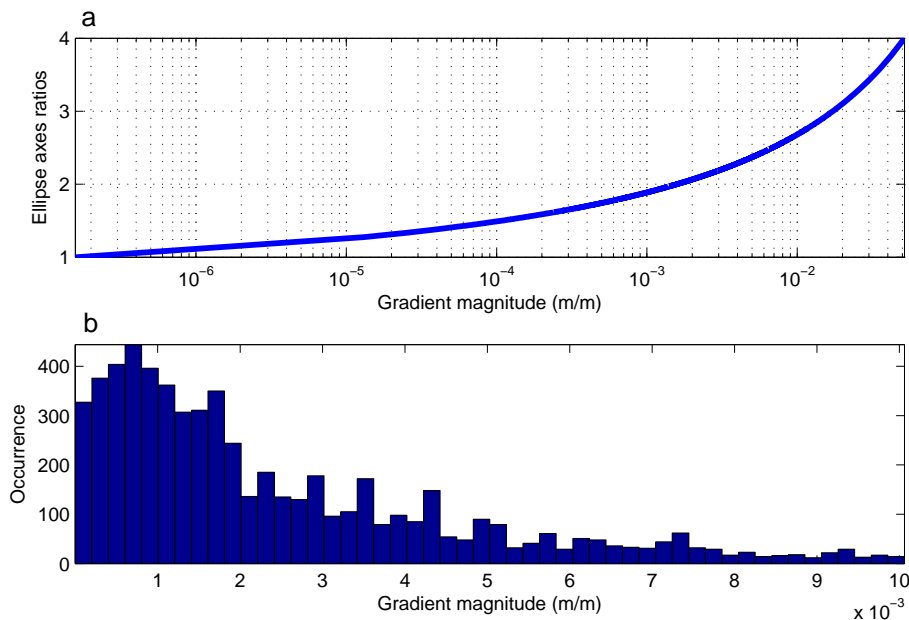


Fig. 3. (a) The ratio between the axes of an elliptical inclusion zone as a function of the head gradient magnitude. (b) A histogram of the head gradient magnitudes at the well locations in the coastal aquifer.

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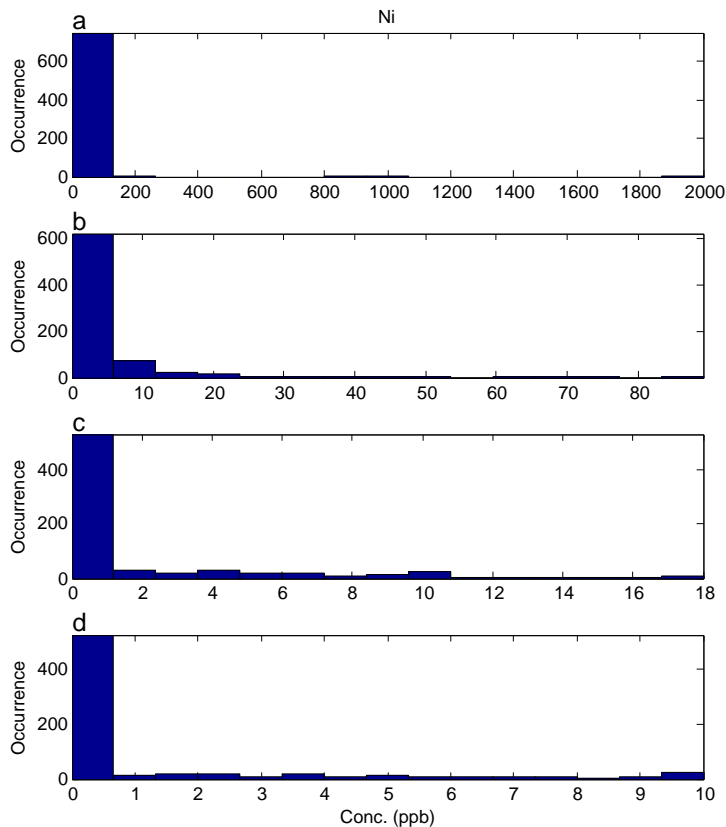


Fig. 4. Histograms of the monitoring nickel concentrations. The maximal value observed in each well in 2000–2010 was considered. At any data value range presented in the figure the great majority of the data are very small with a few very large ones. **(a)** Using all the values. **(b)** Using only values below the 99 % percentile. **(c)** Using only values below the 95 % percentile. **(d)** Using only values below the 90 % percentile.

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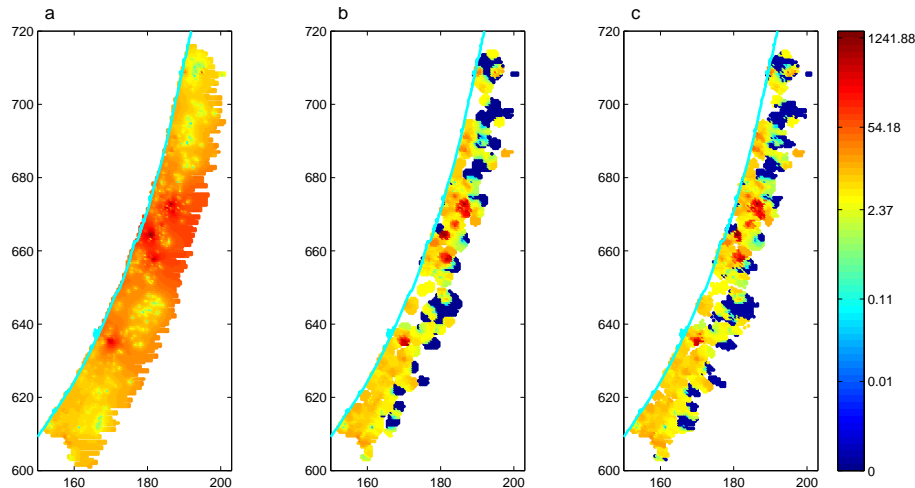


Fig. 5. Interpolation maps of chromium concentrations. The continuous cyan line marks the coast line. The coordinates are of the New Israeli Grid in km. The concentrations are color coded. Identical color coding was used for the three maps and is given in the color bar in ppb units. **(a)** Using an infinite inclusion zone (all data points are used to produce each grid value). **(b)** Using a circular inclusion zone. **(c)** Using an elliptical inclusion zone. The radius of the circular inclusion zones was set such that the total area covered by the circular zones is equal to the area covered by ellipses with minor semi-axis of 1000 m. Note the gaps in the areal coverage of maps **(b)** and **(c)** compared to that of map **(a)**.

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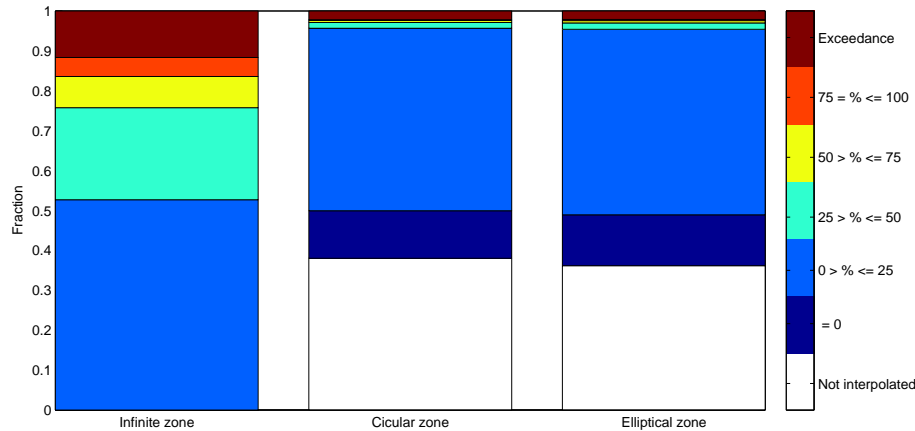


Fig. 6. The fractions of the aquifer area covered by chromium concentration at different brackets. The brackets are between percentages of 50 ppb, the Israeli Standard for chromium.

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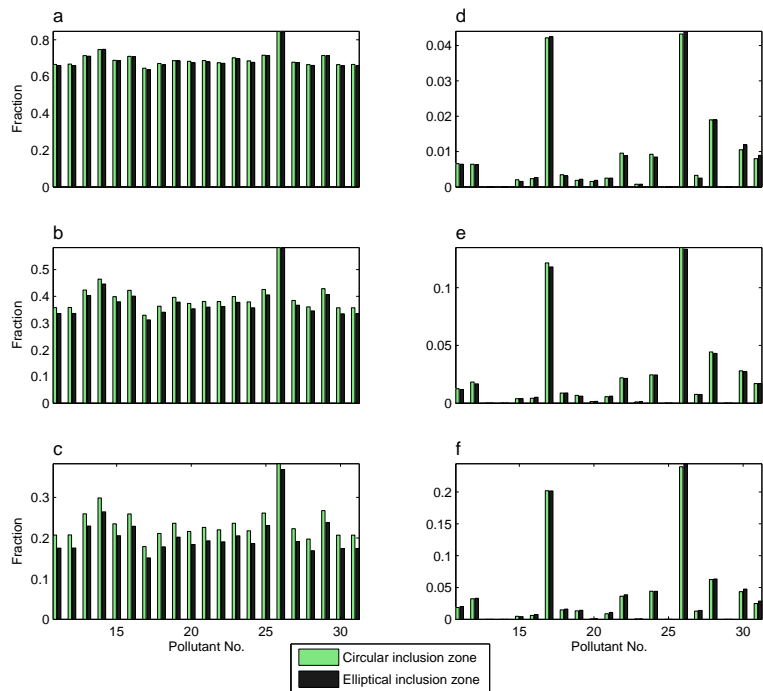


Fig. 7. (a) The fractions of the interpolation points that were not assigned a concentration value for pollutants 11–31 (non-major ions, see Table 1) using interpolation elliptical inclusion zones with minor semi-axes of 500 m and the corresponding circular zones. **(b)** Like **(a)** but for minor ellipse semi-axis of 1000 m. **(c)** Like **(a)** but for minor ellipse semi-axis of 1500 m. **(d)** The fractions of the interpolation points that were assigned a concentration value exceeding the health standard of pollutants 11–31 (non-major ions, see Table 1) using interpolation elliptical inclusion zones with minor semi-axes of 500 m and the corresponding circular zones. **(e)** Like **(d)** but for minor ellipse semi-axis of 1000 m. **(f)** Like **(d)** but for minor ellipse semi-axis of 1500 m.

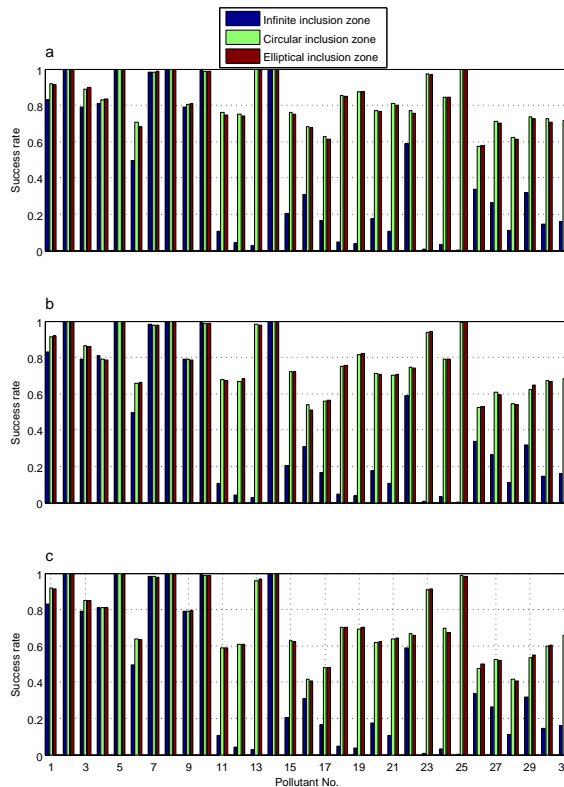


Fig. 8. The cross-tested success rate values achieved for each pollutant by interpolations using elliptical, circular and infinite inclusion zone. The interpolation was carried out for the whole aquifer area. **(a)** The radius of the circular inclusion zones was set such that the total area covered by the circular zones around the interpolation points is equal to the area covered by ellipses with minor semi-axis of 500 m. **(b)** The same as **(a)** but using ellipse minor semi-axes of 1000 m. **(c)** The same as **(a)** but using ellipse minor semi-axes of 1500 m.