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Quantifying mesoscale soil moisture with the cosmic-ray rover

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Abstract

Soil moisture governs the surface fluxes of mass and energy and is a major influence on floods and drought. Existing techniques measure soil moisture either at a point or over a large area many kilometers across. To bridge these two scales we used the cosmic-ray rover, an instrument similar to the recently developed COSMOS probe, but bigger and mobile. This paper explores the challenges and opportunities for mapping soil moisture over large areas using the cosmic-ray rover. In 2012, soil moisture was mapped 22 times in a 25 km × 40 km survey area of the Tucson Basin at 1 km² resolution, i.e., a survey area extent comparable to that of a pixel for the Soil Moisture and Ocean Salinity (SMOS) satellite mission. The soil moisture distribution is dominated by climatic variations, notably by the North American monsoon, that results in a systematic increase in the standard deviation, observed up to 0.022 m³ m⁻³, as a function of the

- mean, between 0.06 and $0.14 \text{ m}^3 \text{ m}^{-3}$. Two techniques are explored to use the cosmicray rover data for hydrologic applications: (1) interpolation of the 22 surveys into a daily
- soil moisture product by defining an approach to utilize and quantify the observed temporal stability producing an average correlation coefficient of 0.82 for the soil moisture distributions that were surveyed and (2) estimation of soil moisture profiles by combining surface moisture from satellite microwave sensors with deeper measurements from the cosmic-ray rover. The interpolated soil moisture and soil moisture profile estimates
- allow for basin-wide mass balance calculation of evapotranspiration, totaling 241 mm for the year 2012. Generating soil moisture maps with cosmic-ray rover at this intermediate scale may help in the calibration and validation of satellite campaigns and may also aid in various large scale hydrologic studies.





1 Introduction

Quantifying area-average soil moisture at the mesoscale (2–1000 km) is difficult because of the footprint or support volume (Western and Bloschl, 1999; Robinson et al., 2008) of current measurement methods. Satellite microwave sensors have a large (3–

- ⁵ 50 km) footprint, which may be too coarse a resolution for atmospheric and hydrological applications (Kerr et al., 2010). Atthe other extreme, in-situ point measurements have very small support volumes that are likely not representative of the surrounding area (Zreda et al., 2012). Currently there is a gap in observational methods used to measure soil moisture at intermediate scales between point measurements and satellites pixels.
- ¹⁰ This has stimulated research into area-average soil moisture monitoring using GPS surface feedbacks (Larson et al., 2008), distributed sensor networks (Bogena et al., 2010), and cosmic-ray neutron monitoring (Zreda et al., 2008, 2012). GPS receivers and cosmic-ray neutron probes provide a significant improvement in measuring area-average soil moisture, but their support volumes are still small when compared with
- the vastness sampled by satellite instruments. Distributed sensor networks may also have a relatively small footprint if they are installed over a small area and, if they are widely spaced, they act as point measurements, not necessarily representative of a study area.

There remains a need for a practical method to measure soil moisture at the scale between the footprint of a stationary COSMOS probe (660 m diameter) and satellite imaging (3–50 km). We conducted the first systematic mapping of soil moisture with the use of a mobile cosmic-ray probe, called the cosmic-ray rover. The cosmic-ray rover uses the technology of the COSMOS probe and thus has the same horizontal footprint (660 m), when stationary, and the same range in measurement depth (12– 70 cm) (7m de et al. 0010). The cosmic ray rover allows for measurement depth (12–

²⁵ 76 cm) (Zreda et al., 2012). The cosmic-ray rover allows for mapping of soil moisture over an area commensurate with a satellite pixel, thereby filling a spatial gap in soil moisture observations.





In this study a cosmic-ray rover was used to make 22 one-day surveys inside the Tucson Basin over an area 25 km × 40 km in size and over a period approaching one year. We present results of neutron measurements and describe an exploratory approach to integrate these measurements with ancillary data to produce an enhanced soil moisture product. Section 2 introduces the geographic and hydrologic setting of the Tucson Basin. Section 3 outlines the cosmic-ray rover survey scheme and the conversion from neutron intensities to soil moisture. Section 4 describes the resulting cosmic-ray rover measurements with emphasis on the observed recurring spatial patterns and their predictability, and the paper concludes by estimating evapotranspiration in the Tucson Basin in 2012.

2 Geographic setting of the Tucson Basin

The city of Tucson sits in an extended basin within the Sonoran Desert in southern Arizona. The basin is at an altitude of ~ 800 m a.s.l. and is surrounded by five mountain ranges that reach up to 2800 m a.s.l. The Sonoran Desert climate has two wet seasons,
¹⁵ due to summer monsoon rainstorms and winter frontal precipitation (Serrat-Capdevila et al., 2007), separated by dry periods in spring and autumn. The summer monsoons are typically localized convection storms from the south that generate short but high-intensity rainfall. In contrast, the winter fronts are driven by Pacific winds and produce rains of longer duration and lower intensity (Jurwitz, 1953). Low atmospheric humidity
²⁰ and high temperatures create a water-limited environment where most of the precipi-

and high temperatures create a water-limited environment where most of the precipitation returns to the atmosphere as evapotranspiration. Consequently, recharge in this area is limited and occurs mainly in winter as mountain front, mountain block (Wilson and Guan, 2004), diffuse, and ephemeral wash recharge (Blasch et al., 2004), with diffuse infiltration being only a minor contributor (Walvoord et al., 2002). The survey area within the basin consists of three land classes: a Sonoran desert (72% of the survey area), urban development (27%) and agricultural land (1%).





3 Methods

3.1 Cosmic-ray rover

The cosmic-ray rover (Desilets et al., 2010) is a mobile neutron detector similar to the stationary COSMOS probe (Zreda et al., 2012). Our unit consists of two ³He-filled
⁵ proportional counters 7.94 cm in diameter and 99 cm in length with a gas pressure of 152 kPa. When combined, these counters have 8.5 times the count rate of the standard ³He stationary probe used in the COSMOS project (Zreda et al., 2012). The rover has three main components: a neutron detector tube, a neutron pulse module, and a data logger. When an incoming neutron collides with a ³He molecule an electric charge is deposited on the center wire that produces a distinct and detectable pulse (Krane, 1988). That pulse is processed by the pulse module and recorded as a neutron count in the data logger. The data logger also stores GPS locations and barometric pressure. The rover is typically placed inside or on top of a truck or car with external sensors located outside of the vehicle to monitor temperature and humidity separately. In this
¹⁵ study we used Maxim iButtons (model DS1923-F5). The stationary COSMOS probe in-

- tegrates neutron counts over sufficiently long time to produce a small uncertainty due to counting statistics. That time can be an hour or longer because soil moisture does not change quickly in time. In contrast, the integration time in the cosmic-ray rover must be short, typically one minute, to capture the average soil moisture with high spatial reso-
- ²⁰ lution along the path of the probe. That high resolution is achieved at the expense of the neutron measurement precision, which in our surveys is approximately 5 % uncertainty when counting for one minute. To achieve a 2 % counting uncertainty in the Tucson Basin a seven-minute moving average was applied to the data. This was determined to be the optimal balance between spatial resolution and measurement precision. The
- 25 seven-minute moving average window was chosen based on the absolute count rate in the Tucson Basin. (Note that the absolute count rate may be different elsewhere and other averaging windows may be more appropriate.)





The footprint of the cosmic-ray rover is a swath with its width equal to the footprint of a stationary probe and its length equal to the distance traveled during the averaging time (one minute for the raw data, and seven minutes for the moving average). The swath width varies only slightly with soil moisture and therefore can be considered constant

in our surveys. The measurement depth is sensitive to the hydrogen content of the soil, and ranges from 76 cm for completely dry soils to 12 cm for saturated soils (Zreda et al., 2008). Hydrogen in mineral grains (which we call lattice water) and in soil organic matter also decreases the penetration depth (Zreda et al., 2012), and because all soils contain that hydrogen, the practical upper limit of the measurement depth is reduced to 50 cm in the Tucson Basin.

3.2 Correction factors

The observed neutron intensity depends on the total hydrogen in the system, which we call "total surface moisture", and the intensity of the incident neutron radiation which depends on external factors, such as solar activity (Zreda et al., 2012). To extract the signal associated with pore water, the part of the overall signal that depends on hydrogen other than that in pore water must be assessed independently. These other factors controlling neutron intensity are solar activity, barometric pressure, atmospheric water vapor pressure, lattice water, soil organic matter, and vegetation.

The intensity of the incoming high-energy charged particles penetrating the top of ²⁰ Earth's atmosphere is inversely proportional to the solar activity (Zreda et al., 2012), and thus is variable in time. Because multiple surveys are used for comparison, the temporal variations in solar activity have been accounted for using the ratio (f_i) of neutron intensity at a reference time (I_0) to the neutron intensity at the time of the survey (I_i) in counts per unit time:

25 $f_i = \frac{I_0}{I}$

15



(1)

In this study, information needed to determine this correction was taken from the publicly available high-energy neutron-monitor data at http://www.nmdb.eu, station Jungfraujoch IGY.

Cosmic-ray particles travel from the top of the atmosphere and are attenuated by collisions with atmospheric nuclei. A fraction of these particles eventually reaches the Earth's surface, and their abundance is inversely proportional to the total mass of air traversed (Desilets and Zreda, 2003). The mass of air above the cosmic-ray probe varies in space and time, but this can be readily assessed by monitoring barometric pressure during the surveys. In a similar manner to the neutron intensity correction, the barometric pressure correction converts the measured neutron intensity to that at a reference pressure (P_0 , in g cm⁻²). The intensity decreases exponentially with increasing pressure at a rate dictated by the known (Desilets and Zreda, 2003) neutron attenuation length in air (λ , in g cm⁻²). The ratio (f_p) of the neutron intensity at pressure P (g cm⁻²) to the neutron intensity at the reference pressure P_0 (g cm⁻²) is (Desilets and Zreda, 2003):

$$f_p = e^{\frac{(P_0 - P)}{\lambda}}$$

The changing hydrogen in the atmospheric water vapor is removed by calculating the contribution to the measured neutron intensity as a liquid water equivalent (Rosolem et al., 2013). The correction adjusts the measured neutron intensity to that of the reference atmospheric water vapor content

$$f_{\rm CWV} = 1 + 0.0054 (\rho_v - \rho_v^0)$$

where f_{CWV} is the ratio of the measured neutron intensity at a specified absolute humidity (ρ_{ν} , in g m⁻³) to that the reference humidity (ρ_{ν}^{0} , in g m⁻³).

The corrected (normalized) surface moisture signal ($N_{\rm C}$, in counts min⁻¹) is then calculated by the product of the reference ratios and the raw neutron intensity (N, in counts min⁻¹):

 $N_{\rm C} = N \cdot f_i \cdot f_p \cdot f_{\rm CWV}$

(2)

(3)

(4)

In this way the effects of temporal variations in high energy neutron intensity, barometric pressure, and water vapor are all normalized to a reference condition in the value of the corrected neutron intensity term, $N_{\rm C}$. The variability of $N_{\rm C}$ is then just a function of the main surface hydrogen stocks, specifically pore water, lattice water, vegetation and soil organic carbon which is accounted for in the site calibration.

3.3 Calibration

5

10

A calibration curve developed by Desilets et al. (2010) relates the corrected neutron intensity (N_0) to the volumetric soil moisture $\theta(N_C)$ by the calibration parameter N_0 . N_0 will be the same everywhere if the measured neutron count rate is normalized for all factors. However, lattice water, vegetation and soil organic carbon are spatially variable. Therefore, N_0 becomes a site specific calibration parameter that implicitly includes the effects of lattice water, vegetation, and soil organic carbon inside the cosmic-ray footprint. Measuring N_C while independently and simultaneously measuring $\theta(N_C)$ allows for a computation of the calibration parameter, N_0 .

15
$$\theta(N_{\rm C}) = \frac{a_0}{\frac{N_{\rm C}}{N_0} - a_1} - a_2$$

where $a_0 = 0.0808$, $a_1 = 0.372$, $a_2 = 0.115$ (Desilets et al., 2010). For calibration, $\theta(N_C)$ may be measured by many methods, but comprehensive gravimetric sampling followed by oven drying is the common practice (Zreda et al., 2012). The calibration parameter N_0 remains constant in time unless there is significant vegetation change throughout the year. In space, the parameter can be determined at different locations via multiple

the year. In space, the parameter can be determined at different locations via multiple gravimetric calibrations; alternatively, the spatially varying amount of hydrogen in lattice water, vegetation and soil organic carbon can be independently analyzed and then normalized to a constant calibration parameter.

The variability of lattice water, vegetation, and soil organic carbon was investigated in Tucson Basin. The vegetation density is low and nearly constant in the Sonoran Desert

(5)



environment, and thus does not affect the neutron intensity in a significant way. For a lattice water estimate, 16 soil samples collected within the basin were analyzed. Each sample was a composite of a subset of ~ 50 samples within the cosmic-ray probe footprint. The average lattice water content in the basin is 0.88 ± 0.77 wt. %. This value is 5 comparable to the value of 0.70 wt. % obtained at the Santa Rita COSMOS probe site

- at the southern end of the basin (Fig. 1). In the urban area, lattice water is also found in roads, buildings and other infrastructure. We measured hydrogen content in 4 brick, 7 cement, and 6 asphalt samples. Brick contained an upper bound of 0.68 wt. % lattice water, asphalt samples had an upper bound of 5.10 wt. %, and cement samples had
- and upper bound of 1.52 wt. %. The exact amount of hydrogen was not captured since 10 a fraction left bound in hydrocarbons which were not directly measured; therefore we have a constraining upper bound by the known mass that was burned off gas. Brick, cement and asphalt occupy a small percentage of the support volume (horizontal extent and depth thickness) of the urban areas except for the densely built downtown;
- therefore we assume their lattice water signal is negligibly small. The effect of dense 15 urbanization is unknown and needs to be investigated further, but for this study the downtown is less than one percent of the survey area and is therefore negligible. The soil organic carbon was not analyzed throughout the basin, but assumed to be negligible because of the arid environment; at the Santa Rita site soil organic carbon is

0.3 wt. % (Zreda et al., 2012). 20

The Santa Rita COSMOS probe served as the sole calibration site for the cosmicray rover used for measurements across the basin, and it is important to recognize that the results derived later depend on assuming the cosmic-ray rover calibration does not change with location and land cover. The assumption is based on the homogeneity

found by the independent analysis of lattice water, vegetation, and soil organic carbon. 25 The cosmic-ray rover was cross-calibrated against the stationary probe which had been previously calibrated against gravimetric samples. To cross-calibrate, N_0 was calculated for the cosmic-ray rover by using soil moisture derived from the stationary probe $(\theta(N_{\rm C}))$ and the neutron intensity measured and corrected with the rover $(N_{\rm C})$. This





cross-calibration was made twice in 2012, in each case over 3 h to reduce the counting uncertainty to less than 1%. The calibration result was also checked during each survey by stopping the rover inside the stationary Santa Rita footprint for \sim 10–30 min.

4 Results

- From the 22 cosmic-ray rover surveys we produced exploratory soil moisture maps of 5 the Tucson Basin as snap shots in time on a 700 m by 700 m grid between latitude 31.95° N and 32.31° N and longitude 110.76° W and 110.03° W. The large total number of neutron counts for each survey $(2 \times 10^5 - 3 \times 10^5 \text{ total counts})$ gave a high degree of confidence for the basin-average soil moisture value. Ancillary data was integrated with these maps to produce a daily soil moisture product as a depth-integrated value and as a depth-profile. The time-interpolation between daily average values and the calculations of soil moisture profiles involve additional assumptions thus increasing the level of uncertainty of these results beyond errors implicit in the data. However, we think it worthwhile to provide these exploratory results for the purpose of demonstrating potential applications of the cosmic-ray rover; they are likely to improve when using 15 alternative techniques to quantify the evolution of the daily soil moisture distribution with time. The derived soil moisture profiles were used along with independent precipitation and stream flow data to estimate the change in the moisture storage term in a mass balance calculation for the Tucson Basin. Details of these analyses are given in the
- ²⁰ following sections.

4.1 Tucson Basin Survey

The swath footprint is calculated by convoluting the stationary (circular) support volume with the length traveled within a specified time interval, i.e. the length traveled multiplied by 660 m plus the stationary support volume. The average driving speed of the cosmic-ray rover was 55 km h^{-1} giving a mean footprint length of 1 km², but speeds varied from





near stationary when in stop-and-go city traffic to 100 km h^{-1} on highways. Each survey comprised ~ 900 data points (gathered over ~ 900 min), with a higher point density in developed areas reflecting the higher road density and lower speeds (Fig. 1). The surveys were conducted each month throughout the year, but once a week during the monsoon season (July–September) in order to capture the increased soil moisture dynamics associated with the increased precipitation in this season.

As previously mentioned, tradeoff between spatial resolution and measurement precision resulted in a one-minute counting interval. The measurement uncertainty decreases with the number of counts (N) by Poisson statistics and is computed as $N^{-0.5}$

- (Zreda et al., 2012). In the Tucson Basin, one-minute data produced ~ 5% counting uncertainty and ~ 2% uncertainty when the seven-minute moving average was applied. The moving average reduces the counting uncertainty so the soil moisture signal dominates. However, this smoothing has two negative effects: it reduces local maxima and minima in soil moisture data and it produces correlated data points. The raw
 one-minute and seven-minute data are shown in Fig. 1, together with the geographic
- location of the survey area.

Ordinary kriging was used as the interpolation technique to produce the soil moisture maps shown in Fig. 2 from the seven-minute average data for the 22 Tucson Basin surveys. There are three main soil moisture features apparent in the data: (1) the distinct seasonality of soil wetness, (2) the enhanced urban soil wetness, and (3) the enhanced soil wetness of large scale agriculture. These three features are discussed sequentially in greater detail below.

The seasonality of wetness is due to the seasonality of precipitation and air temperature. The monsoons (July–September) account for more than half of the annual precipitation in Tucson (Jurwitz, 1953). During this period, the regional variance (variogram sill) of the soil moisture distribution increases from a background of 0.02–0.04 (m³ m⁻³)² to 0.08–0.12 (m³ m⁻³)², except for the anomalously high variance in March. This anomaly is attributed to the recent winter rain event. In general, the degree of regional variance across the basin diminishes as the mean soil moisture increases which





is observed in a variogram analysis in time. The correlation length scale, which ranges between 1.5 km and 5.5 km, does not show the same pattern and does not seem to be related to precipitation nor the mean soil moisture. During the monsoon season, the soil moisture enters into a more dynamic state due to fast wetting from monsoon precipitation and then fast drying due mainly to evaporation. This seasonal moisture

5 precipitation and then fast drying due mainly to evaporation. This seasonal moistur effect is seen in the survey maps as a relative shift in soil moisture (Fig. 2).

The urban wetness is clearly visible in all maps (Fig. 2). The northern part of the Tucson Basin is predominantly a developed urban area. This urbanization is observed to create a moisture oasis in the drier surrounding Sonoran Desert. Adding urban land-

scaping (parks, gardens, lawns, etc...) causes more moisture to be added to the environment by irrigation. The soil moisture in the urban landscape is consistently wetter than the natural landscape, regardless of the season.

Agricultural wetness is apparent in two areas of irrigated agriculture in the Tucson Basin, both along the Santa Cruz Wash that runs north to south on the west side of

¹⁵ the basin. The first is the San Xavier Indian Reservation in the west-central side of the basin and the more prominent region is the Green Valley pecan farms at the southern end of the survey area. The pecan farm is a large flood irrigated plot that remains wetter than the surrounding desert landscape by ~ 0.03–0.07 m³ m⁻³ and up to 0.10 m³ m⁻³ when surface ponding was present.

In comparison with previous soil moisture distribution studies, the standard deviation was plotted against the mean soil moisture (Fig. 3). Famiglietti et al. (2008) expressed this relationship with the following function

$$\sigma = k_1 \cdot \theta_{\text{mean}} \cdot e^{(k_2 \cdot \theta_{\text{mean}})}$$

where σ is the standard deviation (m³ m³), θ_{mean} is the spatial mean soil moisture (m³ m⁻³), and k_1 and k_2 are the fitting parameters. The magnitude of the variability was shown to increase with spatial extent; up to 0.07 m³ m⁻³ for the 50 km scale. In our data, we observe the one-minute data reaching a maximum standard deviation of 0.03 m³ m⁻³ and the seven minute data reaching 0.02 m³ m⁻³. The mean soil moisture



(6)



in the Tucson Basin was only captured between $0.07 \text{ m}^3 \text{ m}^{-3}$ and $0.16 \text{ m}^3 \text{ m}^{-3}$; therefore it does not display the full convex upward behavior, but does fit the function in this range. The seven-minute smoothing decreases the overall variability by averaging out anomalous small scale features along with inherent noise, shown as a downward translation in Fig. 3 and described in further detail in the following section. The discrepancy in the magnitude between our results and point observations of Famiglietti et al. (2008) is likely due to a similar phenomenon, the small meter-scale heterogeneity seen in point measurements is averaged out in larger support volume of the cosmic-ray rover.

- ¹⁰ When evaluating the soil moisture maps it is important to recognize systematic shortcomings in the rover survey data that are associated with driving with variable speed. As previously mentioned, when the velocity is constant at 55 km h⁻¹ the seven-minute smoothing interval corresponds to a 6.4 km long swath, but the swath can be as long as 12 km when the speed is 100 km h⁻¹ on the highway, or as short as a stationary circu-
- ¹⁵ Iar footprint with a diameter of 660 m if the vehicle stops for more than seven minutes. This gives a range of swath lengths and it can also produce points that have anomalous count rates when traffic stops that are otherwise averaged out and not apparent when driving past the same point at constant speed. To illustrate this effect, Fig. 4 shows the neutron intensity measured while moving along an east-west transect across the
- ²⁰ Tucson Basin as one-minute raw counts and seven-minute averages, and also when the cosmic-ray rover stopped at five specific locations. The soil moisture offset from the seven-minute moving average of the mobile survey when cosmic-ray rover is stationary can be up to 0.10 m³ m⁻³ (e.g., at stop 1). This effect is reflected in the derived Tucson Basin maps in which anomalous small-scale values are consistently included in the intermelation at leastings where the appreciate many reverse reverses the seven there.
- interpolation at locations where the cosmic-ray rover routinely stopped for longer than about seven minutes and, in particular, for stops near the University of Arizona where the soil is wetter, and Sentinel Hill where the soil is drier (see Fig. 1 for these locations). The soil moisture values recorded when stopped are of course accurate but they are only representative of the local 660 m diameter footprint. Other small scale anomalies





presumably also exist within the region surveyed but these are not apparent because their influence is averaged out in transit.

Other biases also exist in the maps of soil moisture for the Tucson Basin that are associated with areas with low road density and bias in the direction of travel, such as in

- the southern part of the study region where there are few roads and where those roads that exist have are a dominant bias towards running in the north-south direction. In such regions error is introduced by interpolation when using the simple kriging method adopted for this study because the data is sparse. For example, the pecan farms in the south of the study region fall in a narrow strip of land but, because there are no adjacent accessible roads that allow sampling of the drier soils nearby their wet soil
- ¹⁰ adjacent accessible roads that allow sampling of the drier soils nearby, their wet soil signal is propagated beyond the irrigated area by the kriging algorithm.

4.2 Time interpolation

Previous studies have shown temporal stability in soil moisture (Cosh et al., 2004; Martinez-Fernandez and Ceballos, 2003; Vachaud et al., 1985) and have reported that
the spatial variance may be related to the mean soil moisture (Martinez-Fernandez and Ceballos, 2003; Western et al., 2004). Temporal stability in the spatial patterns indicate that the soil moisture distribution acts in a systematic way dominated by persistent surface and atmospheric characteristics and processes. In the Tucson Basin, we observe stability in that the high soil moisture regions remain consistently high and the low soil moisture regions remain consistently high and the low soil temporal stability and incorporate it into the modeling of the daily soil moisture distributions. To do this, we calculated the offset of each cell (700 × 700 m) from the mean soil

moisture (θ_{mean}) as a fraction (f) of the basin-wide standard deviation (σ)

 $\theta_{\mathsf{cell}} = \theta_{\mathsf{mean}} + f \cdot \sigma$

where θ_{mean} and σ are in units of m³ m⁻³. The standard deviation is derived from the exponential form outlined in Eq. (6) which was fitted to our seven-minute data (Fig. 3).





(7)

The *f* parameter remains relatively constant in time as indicated by the temporal standard deviation, validating the statement of temporal stability. The mean of the spatially varying parameter and its standard deviation from the 22 maps surveys is shown in Fig. 5. The standard deviation of the *f* parameter is fairly low except for the pecan farms due to irregular irrigation, and for the anomalously wet University of Arizona and anomalously dry Sentinel Hill. Equation (7) relies on two conditions, that the soil moisture distribution displays temporal stability in the spatial patterns and that the exponential relationship between the mean soil moisture and the standard deviation is defined correctly; both seem to be satisfied for our data set. In Fig. 6 we show the reproduced soil moisture distributions of the 22 survey days from the *f* parameter and mean soil moisture from surveyed data. The maps are very similar to the cosmic-ray rover surveys (Fig. 2) because of a high degree of temporal stability indicated by an average correlation coefficient of 0.82; however, we conclude that this approach is ac-

curate only if the basin-wide mean soil moisture is defined correctly. Note that in these reproduced maps the spatial pattern does not change since the mean of the *f* parameters data was used.

The challenge in modeling this distribution at the daily time-step is having an accurate representation of the mean soil moisture from an independent measurement. The Santa Rita COSMOS point measurement served as our reference data as it is highly paralleleted with the basis wide mean. Daily asil mainture means were produced from the

- ²⁰ correlated with the basin-wide mean. Daily soil moisture maps were produced from the year 2012 based on Eqs. (6)–(7) and the correlation between the basin mean and the Santa Rita COSMOS probe shown in Fig. 7. Figure 7 displays two linear regressions, one assigned for the winter months (January–April) and another for the dry-summer and monsoonal months (May–December). The regression functions have an r^2 of 0.84
- ²⁵ and 0.91 giving a reliable fit, suggesting that the relationship between the Santa Rita probe and the basin-wide mean soil moisture changes with season and when different atmospheric and surface processes dominate. In the dataset, it is seen as abrupt shift in the estimated mean soil moisture (Fig. 9, top panel). This transition is not well





25 $C = \frac{1}{2}Z^*$

7142

captured with the current method and is considered a processing artifact; however the rest of the dataset matches the survey results within 0.02 m³ m⁻³ uncertainty.

4.3 Basin-wide hydrologic application

4.3.1 Soil moisture profile

- Soil moisture profiles are not necessarily uniform and a single sample value of a por-5 tion of the profile (which is the case for the cosmic-ray rover) may not accurately represent the soil water storage in a near-surface water balance. To improve the storage estimate, we developed an integrated approach using the cosmic-ray rover and satellite measurements to estimate an area-average soil-moisture profile. This approach is
- similar to that used in remote sensing, where satellite retrievals have utilized different 10 wavelengths that penetrate to different depths (Jackson, 1980; Reutov, 1990), although all have been limited to the top 5 cm (Laymon et al., 2001). Our approach uses information from three depths in the soil column to generate soil moisture profiles: (1) a surface measurement (from satellite-based microwave instrument, 0-5 cm), (2) a deeper mea-
- surement (from cosmic-ray rover, 12–76 cm), and (3) a constraining value at depth. In 15 our analysis the cosmic-ray rover measurements are averaged in space to the size of the Soil Moisture and Ocean Salinity (SMOS) level 3 products which we take as the surface measurement (http://catds.ifremer.fr/).

The cosmic-ray probe's penetration depth was recently derived by Franz et al. (2012a) where the soil moisture, bulk density, and lattice water determine the depth 20 from which 86% of the neutrons are sourced. Franz et al. (2012a) also approximated how much each layer contributes to the overall signal by a linear weighting function. This integrated measurement is converted to a point on the soil moisture profile by assigning it the centroid of the weighting function (C, cm)





(8)

where *z*^{*} is the penetration depth in cm. The centroid is computed as 1/3 of *z*^{*} because the linear weighting function creates a right triangle with the weight of the surface layer as the horizontal leg and the depth of penetration as the vertical leg. The centroid depth is the most representative point of the soil column to assign the cosmic-ray measure-⁵ ment.

Data from 190 TDT probes installed at the Santa Rita stationary COSMOS site (Franz et al., 2012b) show no significant change in soil moisture below the depth of 40 cm, which is consistent with previous observations that diffuse recharge at the basin floor is minimal (Walvoord et al., 2002). Because the daily dynamics of soil moisture at

- ¹⁰ 40 cm depth is so slow, when synthesizing the area average profile we assume the soil moisture at this depth is constant and assigned the value 0.06 m³ m⁻³, consistent with the TDT data. This exploratory exercise may not be applicable everywhere. In wetter areas where soil infiltration and deep leakage are significant, the soil moisture value at depth may not be so easily constrained.
- In common with other satellite microwave sensors, the SMOS signal has substantial noise due to the influence on the measurement of variables other than moisture (Entekhabi et al., 2004; Kerr et al., 2010). Nevertheless, it still captures the same trend seen with the cosmic-ray measurement defined by a linear function (Fig. 8). In order to limit noise propagating through the storage terms and also to fill the time gaps, the
- ²⁰ level 3 product was correlated with the interpolated cosmic-ray soil moisture and adjusted based on the fitted linear function. The adjusted level 3 product was used as the surface measurement in the profile calculation. The computed soil moisture profiles are shown in Fig. 9 as the bottom panel. As mentioned in the previous section, the top panel shows the modeled basin-wide mean with precipitation and the cosmic-ray rover survey means.

As a check for internal consistency, the generated profile is circulated back to a cosmic-ray "equivalent" soil moisture value. The depth of penetration, soil moisture profile, and weighting function are all known, so the cosmic-ray equivalent value can be calculated by multiplying the weighting function by the profile. The equivalent values





match the interpolated cosmic-ray measurements within $0.01 \text{ m}^3 \text{ m}^{-3}$ uncertainty except during the rain events for which a deviation up to $0.02 \text{ m}^3 \text{ m}^{-3}$ is observed.

4.3.2 Mass balance

A mass balance is computed to provide estimates of evapotranspiration loss and to ex-⁵ plore the possible use of the cosmic-ray rover as a tool in adding closure to a basin-wide mass balance. The mass balance outlined here serves as the survey area average including all land cover types. The mass balance calculation is defined (see, for example, Freeze and Cherry, 1979, by the equation).

 $\mathsf{ET}(t) = P(t) - R(t) - \Delta S_{\mathsf{surface}}(t) - \Delta S_{\mathsf{ground}}(t)$

¹⁰ Where ET is evapotranspiration at time *t*, *P* is precipitation, *R* is runoff, $\Delta S_{surface}$ is the change in surface storage as soil moisture, and ΔS_{ground} is the change in groundwater storage; all terms are in mm day⁻¹ per unit area. As discussed in Sect. 2, there is minimal diffuse recharge, and wash recharge is orders of magnitude less than evapotranspiration. The regional groundwater flow is also negligible compared to the evapotranspiration flux (Kalin, 1994). Therefore, ΔS_{ground} is negligible and the equation reduces to:

$$\mathsf{ET}(t) = P(t) - R(t) - \Delta S_{\mathsf{surface}}(t)$$

Runoff was calculated from the inlet and outlet gauges using the publicly available United States Geological Survey's (USGS) stream gauge network (http://waterdata. ²⁰ usgs.gov/nwis/rt) and the Pima County Flood Control's (PCFC) Alert system (http:// alert.rfcd.pima.gov) (The PCFC inlet gauges used were: 2203, 2093, 2073; the USGS inlet gauges used were: 09482000, 09484000, 09485000, 09484600, 09486350; the USGS outlet gauge used was 09486500; the numbers are the station IDs).

 $R(t) = Q_{\rm out} - Q_{\rm in}$

(9)

(10)

(11)

CC ①

where Q_{in} is flow into the area and Q_{out} is flow out of the area per day. The annual runoff from the Tucson Basin in 2012 calculated in this way was -3.17 mm which is negative because inflow is greater than the outflow due to evaporation from the area, and which is in any case negligible compared to other terms in the water balance.

The soil moisture profiles are used to calculate change in storage. The integral is calculated at each time step to calculate the soil moisture storage (S(t), in mm day⁻¹).

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$$\Delta S(t) = \int_{0}^{z_{d}} \theta(z) \mathrm{d}z - S_{t-1}$$
(12)

Where $\Delta S(t)$ is the change in storage (mm day⁻¹), $\theta(z)$ is the soil moisture in m³ m⁻³ at depth *z* (mm) at time *t*, and *z_d* (mm) is the base of the estimated profile, set to 400 mm. Precipitation is gridded for the basin using 104 rain gauges from the publicly available Rainlog Network (http://rainlog.org) and the PCFC's Alert system with a linear interpolation. The basin-wide average precipitation events in 2012 had magnitudes between 3 mm day^{-1} and 15 mm day^{-1} , with a yearly total of 224 mm. The rain gauge network is denser in the developed areas of Tucson than in the less developed areas in the south side of the Tucson Basin, and consequently has greater confidence. The uncertainty is expressed in the cumulative distribution plot in Fig. 10; the gray shaded region represents the difference between the basin-wide precipitation based on the Rainlog network and the ALERT network; the average precipitation is shown as the black line.

- ET is calculated daily from Eqs. (9)–(11) from a uniform profile down to 70 cm and the derived soil moisture profiles from the previous section to investigate if the soil moisture profiles improve the mass flux calculation. These are shown in Fig. 10 where the ET from the estimated profile behaves much more reasonably than the uniform profile which tends to overestimate the near surface mass flux. The ET curves show a decrease after a rain event, because of the coarse time resolution. The average daily
- soil moisture shows the increase in precipitation typically the day after the event since the soil moisture during the event is averaged out with the soil moisture on the previous





day. Also, the uniform case shows large decreases in ET that is unrealistic since the soil moisture increases are much greater than the precipitation event itself. The abrupt change in the ET curves is again due to the change in regression from the Santa Rita probe when attempting to estimate the basin-wide mean soil moisture. In summary, the
⁵ mass balance gives insight into how the interpolation and profile estimate techniques are performing. The value of ET derived from the profile seems to constrain the soil moisture change to values more realistic of system and the cosmic-ray rover provides a new observation technique to measure it.

5 Conclusions

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- ¹⁰ This paper outlines a new approach which shows new potential to generate soil moisture maps at the mesoscale between the satellite products and point measurements with the cosmic-ray rover. The following list summarizes the main points of the paper:
 - Measurements of cosmic-ray neutrons with the cosmic-ray rover yielded soil moisture maps in the Tucson Basin (25 km × 40 km) at an interpolated resolution of ~1 km.
 - Temporal stability in the spatial patterns is observed; this is hypothesized to be a result of reoccurring processes and fixed surface characteristics.
 - If temporal stability exists, an estimate of the soil moisture distribution may be more accurately modeled by upscaling or downscaling by quantifying the temporal stability as a function of the spatial mean and spatial standard deviation.
 - Integrating cosmic-ray rover measurements with satellite products may allow for an improved estimate of the soil moisture profile, and therefore an improvement in catchment scale mass balance.

The observed temporal stability of soil moisture in the Tucson Basin may or may not be present elsewhere. This deserves further investigation. Future work should determine

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how to calibrate the cosmic-ray rover for vegetation, lattice water, and soil organic carbon. Interpolation techniques can also be improved to constrain the observations to land cover information, such as the outline of the pecan farm or other increased areas of wetness. In terms of spatial structure and the predictability, the functional form in
⁵ Eq. (6) (Famiglietti et al., 2008) and the *f* parameter in Eq. (7) should be investigated to find out how universal or variable these relationships are at this scale. For hydrologic applications, the ET estimates and soil moisture profiles need to be validated with robust datasets, such as distributed eddy covariance towers within the survey area. The mass balance study in Sect. (4) is an example of the potential use of the cosmic-ray rover but is currently only an exploratory method to investigate the catchment scale hydrology. The main objective of this paper was to provide a methodological approach for the cosmic-ray rover and an example dataset of mesoscale soil moisture maps.

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References

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- Blasch, K., Ferré, T. P. A., Hoffmann, J., Pool, D., Bailey, M., and Cordova, J.: Processes Controlling Recharge Beneath Ephemeral Streams in Southern Arizona, in: Groundwater Recharge in a Desert Environment: The Southwestern United States, Am. Geophys. Un., Vol. 9, 69–76, 2004.
- Bogena, H. R., Herbst, M., Huisman, J. A., Rosenbaum, U., Weuthen, A., and Vereecken, H.: Potential of Wireless Sensor Networks for Measuring Soil Water Content Variability, Vadose Zone J., 9, 1002–1013, doi:10.2136/vzj2009.0173, 2010.
- Cosh, M. H., Jackson, T. J., Bindlish, R., and Prueger, J. H.: Watershed scale temporal and
 spatial stability of soil moisture and its role in validating satellite estimates, Remote Sens.
 Environ., 92, 427–435, doi:10.1016/j.rse.2004.02.016, 2004.
 - Desilets, D. and Zreda, M.: Spatial and temporal distribution of secondary cosmic-ray nucleon intensities and applications to in situ cosmogenic dating, Earth Planet. Sc. Lett., 206, 21–42, doi:10.1016/s0012-821x(02)01088-9, 2003.
- ¹⁵ Desilets, D., Zreda, M., and Ferre, T. P. A.: Nature's neutron probe: Land surface hydrology at an elusive scale with cosmic rays, Water Resour. Res., 46, W11505, doi:10.1029/2009wr008726, 2010.
 - Entekhabi, D., Njoku, E. G., Houser, P., Spencer, M., Doiron, T., Kim, Y. J., Smith, J., Girard, R., Belair, S., Crow, W., Jackson, T. J., Kerr, Y. H., Kimball, J. S., Koster, R., McDonald,
- K. C., O'Neill, P. E., Pultz, T., Running, S. W., Shi, J. C., Wood, E., and van Zyl, J.: The hydrosphere state (Hydros) satellite mission: An earth system pathfinder for global mapping of soil moisture and land freeze/thaw, IEEE T. Geosci. Remote Sens., 42, 2184–2195, doi:10.1109/tgrs.2004.834631, 2004.

Famiglietti, J. S., Ryu, D. R., Berg, A. A., Rodell, M., and Jackson, T. J.: Field ob-

- 25 servations of soil moisture variability across scales, Water Resour. Res., 44, W01423, doi:10.1029/2006wr005804, 2008.
 - Franz, T. E., Zreda, M., Ferre, T. P. A., Rosolem, R., Zweck, C., Stillman, S., Zeng, X., and Shuttleworth, W. J.: Measurement depth of the cosmic ray soil moisture probe affected by hydrogen from various sources, Water Resour. Res., 48, W08515, doi:10.1029/2012wr011871, 2012a.





Franz, T. E., Zreda, M., Rosolem, R., and Ferre, T. P. A.: Field Validation of a Cosmic-Ray Neutron Sensor Using a Distributed Sensor Network, Vadose Zone J., 11, 4, doi:10.2136/vzj2012.0046, 2012b.

Freeze, R. A. and Cherry, J. A.: Groundwater, Prentice Hall, Englewood Cliffs, NJ, 1979.

- Jackson, T. J.: Profile soil-moisture from surface measurements, J. Irrig. Drain. Div.-Asce, 106, 81–92, 1980.
 - Jurwitz, L. R.: Arizona's Two-Season Rainfall Pattern, Weatherwise, 6, 96–99, doi:10.1080/00431672.1953.9932951, 1953.
 - Kalin, R. M.: The hydrogeochemical evolution of the groundwater of the Tucson basin with appli-
- cation to 3 dimensional groundwater flow modelling, Department of Geosciences, University of Arizona, 1994.
 - Kerr, Y. H., Waldteufel, P., Wigneron, J. P., Delwart, S., Cabot, F., Boutin, J., Escorihuela, M. J., Font, J., Reul, N., Gruhier, C., Juglea, S. E., Drinkwater, M. R., Hahne, A., Martin-Neira, M., and Mecklenburg, S.: The SMOS Mission: New Tool for Monitoring Key Elements of the
- Global Water Cycle, P. IEEE, 98, 666–687, doi:10.1109/jproc.2010.2043032, 2010.
 Krane, K. S.: Introductory nuclear physics, Wiley, New York, 845 pp., 1988.
 Larson, K. M., Small, E. E., Gutmann, E. D., Bilich, A. L., Braun, J. J., and Zavorotny, V. U.: Use of GPS receivers as a soil moisture network for water cycle studies, Geophys. Res. Lett., 35, L24405, doi:10.1029/2008gl036013, 2008.
- Laymon, C. A., Crosson, W. L., Jackson, T. J., Manu, A., and Tsegaye, T. D.: Ground-based passive microwave remote sensing observations of soil moisture at S-band and L-band with insight into measurement accuracy, IEEE T. Geosci. Remote Sens., 39, 1844–1858, doi:10.1109/36.951075, 2001.
- Martinez-Fernandez, J. and Ceballos, A.: Temporal stability of soil moisture in a large-field experiment in Spain, Soil Sci. Soc. Am. J., 67, 1647–1656, 2003.
 - Reutov, E. A. and Shutko, A. M.: Microwave spectroradiometry of water content of nonuniformly moistened soil with a surface transition layer, Sov. J. Remot. Sens., 6, 72–79, 1990.
 - Robinson, D. A., Campbell, C. S., Hopmans, J. W., Hornbuckle, B. K., Jones, S. B., Knight, R., Ogden, F., Selker, J., and Wendroth, O.: Soil moisture measurement for ecological
- and hydrological watershed-scale observatories: A review, Vadose Zone J., 7, 358–389, doi:10.2136/vzj2007.0143, 2008.
 - Rosolem, R., Zreda, M., Franz, T. E., and Zeng, X.: The effect of atmospheric water vapor on the cosmic-ray soil moisture signal, J. Hydrometeorol., in press, 2013.





- Serrat-Capdevila, A., Valdes, J. B., Perez, J. G., Baird, K., Mata, L. J., and Maddock, T.: Modeling climate change impacts and uncertainty on the hydrology of a riparian system: The San Pedro Basin (Arizona/Sonora), J. Hydrol., 347, 48-66, doi:10.1016/j.jhydrol.2007.08.028, 2007.
- 5 Vachaud, G., Desilans, A. P., Balabanis, P., and Vauclin, M.: Temporal stability of spatially measured soil-water probability density-function, Soil Sci. Soc. Am. J., 49, 822-828, 1985.
 - Walvoord, M. A., Plummer, M. A., Phillips, F. M., and Wolfsberg, A. V.: Deep arid system hydrodynamics - 1. Equilibrium states and response times in thick desert vadose zones, Water Resour. Res., 38, doi:10.1029/2001wr000824, 2002.
- Western, A. W. and Bloschl, G.: On the spatial scaling of soil moisture, J. Hydrol., 217, 203-10 224. doi:10.1016/s0022-1694(98)00232-7. 1999.
 - Western, A. W., Zhou, S. L., Grayson, R. B., McMahon, T. A., Bloschl, G., and Wilson, D. J.: Spatial correlation of soil moisture in small catchments and its relationship to dominant spatial hydrological processes, J. Hydrol., 286, 113-134, doi:10.1016/j.jhydrol.2003.09.014, 2004.
- 15 Wilson, J. L. and Guan, H.: Mountain-Block Hydrology and Mountain-Front Recharge, in: Groundwater Recharge in a Desert Environment: The Southwestern United States, Am. Geophys. Un., Vol. 9, 113-137, 2004.

Zreda, M., Desilets, D., Ferre, T. P. A., and Scott, R. L.: Measuring soil moisture content non-

- invasively at intermediate spatial scale using cosmic-ray neutrons, Geophys. Res. Lett., 35, 20 L21402, doi:10.1029/2008gl035655, 2008.
 - Zreda, M., Shuttleworth, W. J., Zeng, X., Zweck, C., Desilets, D., Franz, T., and Rosolem, R.: COSMOS: the COsmic-ray Soil Moisture Observing System, Hydrol. Earth Syst. Sci., 16, 4079-4099, doi:10.5194/hess-16-4079-2012, 2012.

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Fig. 1. Left: geographic location of the Tucson Basin survey area outlined in black, an example driving route shown in red with the footprint in grey and the points of interest: COSMOS probe (stationary reference), University of Arizona (wet), Sentinel Hill (dry), and agriculture (wet). Top right: one-minute soil moisture data from the 27 July 2012 survey in $m^3 m^{-3}$. Bottom right: seven-minute smoothed soil moisture data. The smoothing reduces the uncertainty due to counting statistics to 2%, but increases the length of the footprint by a factor of 7.



















Fig. 4. Raw (one-minute), smoothed (seven-minute running averages) and stationary neutron intensity from an east-west trending transect in the Tucson Basin. The stationary points are locations where the rover was stopped; the neutron intensity was recorded for at least 7 min at these stops. Stops 1, 3, and 5 are small-scale features with anomalously high soil-moisture values (low neutron count rate). Stop 1 is near a golf course, stop 3 is on the University of Arizona irrigated campus, and stop 5 is at a wet spot in the foothills of the Santa Catalina Mountains.





Fig. 5. Left: the spatial structure map in the 25×40 km survey area of the mean parameter *f* from the 22 cosmic-ray rover surveys. Right: the standard deviation map of the parameter *f* values.



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Fig. 6. The modeled soil moisture maps from 2012 using the relationship in Eq. (7). The same overall trend is preserved when the mean soil moisture is constrained. The pattern is consistent because the mean f parameter was used to reproduce each map result.







Fig. 7. The correlation between the mean soil moisture from the 22 cosmic-ray rover surveys with the corresponding soil moisture from the Santa Rita COSMOS point measurement. The correlation changes with season and is approximated by separating the winter months (January–April) from the dry season and monsoon (May–December) surveys.













Fig. 9. Top: time-interpolated soil moisture (blue line) generated from the modeled results where the mean soil moisture was estimated from the Santa Rita COSMOS point measurement. Precipitation amounts are shown as black bars and rover surveys as gray boxes. Bottom: soil moisture profiles generated from three depth points. The abrupt shift in the mean soil moisture is due to the change in the linear regression relationship from winter to summer and is an artifact in the result.







Fig. 10. Left: the change in soil moisture storage in mm per day. Right: cumulative distribution in time of precipitation (Precip), ET estimated from the soil moisture profiles $(ET_{profile})$ and uniform profile $ET_{uniform}$. The abrupt decreases in cumulative ET is due to a time discrepancy between precipitation events and daily average soil moisture values.

