



Modelling of snow
depth distribution

T. Grünewald et al.

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Statistical modelling of the snow depth distribution on the catchment scale

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Abstract

The spatial distribution of alpine snow covers is characterized by a large variability. Taking this variability into account is important for many tasks including hydrology, glaciology, ecology or natural hazards. Statistical modelling is frequently applied to assess the spatial variability of the snow cover. For this study, we assembled seven data sets of high-resolution snow-depth measurements from different mountain regions around the world. All data were obtained from airborne laser scanning near the time of maximum seasonal snow accumulation. Topographic parameters were used to model the snow depth distribution on the catchment-scale by applying multiple linear regressions. We found that by averaging out the substantial spatial heterogeneity at the metre scales, i.e. individual drifts and aggregating snow accumulation at the landscape or hydrological response unit scale, that 30 % to 91 % of the snow depth variability can be explained by models that are calibrated to local conditions at the single study areas. As all sites were sparsely vegetated, only a few topographic variables were included as explanatory variables, including elevation, slope, the deviation of the aspect from north (northing), and a wind sheltering parameter. In most cases, elevation, slope and northing are very good predictors of snow distribution. A comparison of the models showed that importance of parameters and their coefficients differed among the catchments. A “global” model, combining all the data from all areas investigated, could still explain 23 % of the variability. It appears that local statistical models cannot be transferred to different regions. However, there seem to be some temporal transferability, in which models developed on one peak snow season were good predictors for other peak snow seasons.

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1 Introduction

One of the most apparent characteristics of the mountain snow cover is its spatial heterogeneity (e.g. Seligman, 1936; McKay and Gray, 1981; Pomeroy and Gray, 1995). This spatial variability is present at a large range of scales, ranging from the sub-metre scale to hundreds of kilometres. The heterogeneity of the mountain snow cover has a significant influence on avalanche formation (Schweizer et al., 2003), local ecology (Litaor et al., 2008) and especially on hydrology (Balk and Elder, 2000; Lundquist and Dettinger, 2005; Bavay et al., 2013). The amount of water stored in the snow cover and its spatial distribution has an important impact on the timing, magnitude and duration of run-off related to melt of snow (Pomeroy et al., 1998; Lundquist and Dettinger, 2005; Lehning et al., 2006) and ice (Dadic et al., 2008). Many human activities, including agriculture (e.g. irrigation), hydropower water resources management, depend on information on the spatio-temporal variability of snow cover and melt. In order to capture the temporally varying run-off caused by snow melt, hydrological models need to account for the spatial distribution of snow.

Recent years have seen advances in modelling snow distributions by applying sophisticated physically based snow cover redistribution models (Pomeroy and Li, 2000; Lehning et al., 2006; Liston and Elder, 2006; Schneiderbauer and Prokop, 2011). Such models have been operated at grid resolutions of a few metres (e.g. Essery et al., 1999; Liston and Elder, 2006; Mott and Lehning, 2010; Mott et al., 2010; Schneiderbauer and Prokop, 2011) to hundreds of meters (e.g. Bernhardt et al., 2009; Bavay et al., 2009, 2013; MacDonald et al., 2010; Magnusson et al., 2010). These models require high level input, including meteorological data, sometimes detailed flow fields (Raderschall et al., 2008) and sometimes high-resolution digital elevation models. They are therefore very expensive in terms of required information and calculation resources, and have not been applied for larger areas or longer time frames. In general, there is a trade-off between model complexity and generality on the one hand and computation time on the other hand although reasonable compromises have been achieved using the

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hydrological response unit concept (MacDonald et al., 2009; Fang and Pomeroy, 2009) which derives from that of landscape units for stratified snow sampling (e.g. Steppuhn and Dyck, 1974).

5 Topography strongly influences but is not a causative factor itself in snow distribution (e.g. McKay and Gray, 1981; Pomeroy and Gray, 1995). The spatial heterogeneity of the snow cover is attributed to a number of different processes which act on different scales: local precipitation amounts are strongly affected by the interaction of the terrain with the local weather and climate (Daly et al., 1994; Beniston et al., 2003; Mott et al., 2013). Wind plays a major role for the deposition and redistribution of snow (e.g. McKay and Gray, 1981; Pomeroy and Gray, 1995; Essery et al., 1999; Trujillo et al., 2007; Lehning et al., 2008). Moreover, snow can be relocated by avalanches and sloughing (Blöschl and Kirnbauer, 1992; Gruber, 2007; Bernhardt and Schulz, 2010), and the local radiation and energy balance influence the spatially varying ablation processes (Cline et al., 1998; Pomeroy et al., 1998, 2004; Pohl et al., 2006; Mott et al., 2011).

10 Many studies have attempted to exploit the relationship between topography and snow in statistical models. Topographic parameters serve as explanatory variables for explaining the spatial heterogeneity of snow depth, snow water equivalent (SWE) or melt rates. Several studies have successfully developed binary regression tree models (e.g. Elder et al., 1998; Balk and Elder, 2000; Erxleben et al., 2002; Winstral et al., 2002; Anderton et al., 2004; Molotch et al., 2005; Lopez-Moreno and Nogues-Bravo, 2006; Litaor et al., 2008), where the response data (e.g. snow depth) are repeatedly split along a predictor (e.g. terrain parameter) into sub-groups by minimizing the sum of the residuals. Such regression tree models were capable of explaining 18 to 90 % of the snow-cover variability. The performance of the models depends on both the complexity of the tree (number of explanatory parameters and number of splits), and on the quality of the data that are analyzed.

25 A second very common statistical approach is multiple linear regression. As in the regression tree models, terrain parameters serve as explanatory variables. An early example is the multivariate regression model developed by Golding (1974) and applied

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to Marmot Creek Research Basin, Alberta. Golding found that elevation, topographic position, aspect, slope, and forest density were the most important variables for predicting snow accumulation but together these could only explain 48 % of the variation of SWE. Based on 106 snow poles Lopez-Moreno and Nogues-Bravo (2006) were able to explain more than 50 % of the large scale snow depth variability over the Pyrenees with elevation, elevation range, radiation and two location parameters. Chang and Li (2000) used monthly SWE data averaged from 13 to 36 snow courses in Idaho to build regression models with a combination of elevation, slope, aspect and a relative position. The models could explain 60 to 90 % of the monthly SWE variability for different regions and large catchments. Marchand and Killingtveit (2005) found that it was possible to model snow depth in open and forested areas of a large (849 km²) Norwegian catchment with different measures of elevation, aspect, curvature and slope ($R^2 = 0.05\text{--}0.48$). For their analysis, they aggregated a very large number of snow depth measurements, obtained by georadar and hand probing to a grid of 1000 m. Pomeroy et al. (2002) used a parametric model derived from a physically-based snow interception model to explain snow accumulation in the boreal forest of Saskatchewan and Yukon, Canada as a function of winter plant area index with an R^2 of 0.79; the parametric model had almost identical form to a regression model using canopy cover developed by Ku'zmin (1960) for snow accumulation in Russian boreal forests, suggesting commonality in the relationship of snow accumulation to forest structure in the circumpolar boreal forest.

Beside such applications for very large areas, several studies have applied linear regression for smaller catchments: for each of 19 topographic sub-units, Jost et al. (2007) averaged 60 manual snow depth and 12 density measurements of a 17 km² catchment in Canada. A linear regression model with elevation, aspect and forest cover could explain up to 89 % of the large scale variability in SWE. In order to apply universal kriging of SWE for a 8 km² glacier in Austria, Plattner et al. (2006) built a linear regression model with elevation, curvature, distance from ridge and a shelter index ($R^2 = 0.41$). The SWE measurements were obtained from the average of three snow depth measurements at 165 sample sites and snow densities from five snow pits.

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Elevation, potential radiation and forest cover were good for representing 66 % of the spatial variability of SWE, obtained from 33 snow cores in a small Swiss catchment (Hosang and Dettwiler, 1991). In order to optimize a snow depth sampling scheme, Elder et al. (1991) applied regression models with elevation, slope and radiation, which explained 27 to 40 % of the SWE variability of a three year data set for the Emerald Lake basin (California). SWE was calculated from density measurements and 86 to 354 manual snow depths taken by manual probing.

Nonetheless, in evaluating such results the sample density, data quality, and scale of the investigation must be considered. All the studies listed up to now in this paper were limited by the small amount and spatial coverage of snow depth observations available for the analysis. Most are based on manual snow depth measurements and only tens to few hundreds of samples could be used for the regression modelling.

In the recent years, high-resolution and high quality snow depth data from terrestrial (e.g. Prokop et al., 2008; Grünewald et al., 2010) and airborne laser scanning (ALS) (Hopkinson et al., 2004; Deems et al., 2006; Grünewald and Lehning, 2011) have become available. Grünewald et al. (2010) used snow depth data obtained by terrestrial laser scanning and built linear regression models (elevation, slope, aspect, radiation/elevation, slope, maximum SWE, wind speed) which could explain 30 and 40 % of the spatial variability of daily ablation rates in the Wannangrat area (Davos, CH). In a recent study, Lehning et al. (2011) analyzed airborne Lidar measurements for two small catchments in Switzerland, and showed that a two-parameter model with elevation and a fractal roughness parameter can explain more than 70 % of the snow depth distribution when clustering data to sub-areas. Even though restricted to two small catchments, Lehning et al. (2011) speculate that it might be possible to transfer their findings to other mountain areas, and that a universal relationship of snow depth and accessible topography parameters might exist.

In this paper we would like to test this hypothesis using a much larger data set. We assembled high-resolution snow depth data from different mountain regions. For the first time, such high-resolution snow depth data from different areas are combined and

compared in a statistical analysis. This permits testing the hypothesis of whether the same or similar topographic parameters dominate the snow depth distribution on the catchment scale (100 to 10 000 m) in different areas. In Sect. 2, we describe the climatological and morphological characteristics of each data set and present the methods of data aggregation and linear regression in detail. In the Results section, the models developed for each region are compared with each other and results from model combinations are discussed.

2 Data and methods

2.1 Airborne laser scanning

Several studies have successfully applied snow depth data obtained by ALS in the recent years (e.g. Deems et al., 2006, 2008; Trujillo et al., 2007, 2009; Grünewald et al., 2010; Grünewald and Lehning, 2011). ALS enables area-wide data to be gathered in a very high spatial resolution and accuracy. Hopkinson et al. (2004) and Deems et al. (2006) showed that ALS was an appropriate and accurate method for gathering snow depth measurements, and since then, a rising number of data sets have become available (Deems et al., 2006; Moreno Banos et al., 2009; Dadic et al., 2010a; DeBeer and Pomeroy, 2010; Grünewald and Lehning, 2011; Schöber et al., 2011; Hopkinson et al., 2012). Detailed descriptions of the ALS measurement principle can be found in Geist et al. (2009), Baltsavias (1999) and Wehr and Lohr (1999).

From the point clouds obtained by ALS, we calculated digital surface models with a cell size of 1 m. Snow depth maps were then produced by subtracting a digital surface model, obtained by the same technology, in snow-free conditions from a digital surface model that was measured in the winter. Unrealistic data such as negative snow depths or extremely high values are rare but still need to be filtered. Such outliers mainly occur in very steep and rough terrain, which is attributed to larger measurement errors in such terrain (Grünewald et al., 2010; Grünewald and Lehning, 2011; Bollmann et al.,

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2011; Hopkinson et al., 2012). In this study, we set negative snow depths to zero and excluded extremely high snow depths from the data. The threshold for extreme high snow depth was set by visual inspection of the distribution separately for each data set, and was between 5 and 15 m. As ALS cannot measure snow depth on forested mountain slopes with reasonable accuracy and snow redistribution by interception and accumulation in forests were outside of the scope of this study, vegetated areas were masked. Most data sets currently available were measured near the peak of the local snow accumulation and represent the maximum of the seasonal snow amounts.

The accuracy of ALS-data depends mostly on the measurement platform. Most data sets mentioned above were gathered from airplanes, which are very effective in terms of the area that can be surveyed. The larger the flight height of the plane, which is typically several hundreds of metres above the surface, and the lower the impact angles of the laser beam in steep terrain, the lower is the accuracy. Nevertheless, the vertical error is usually below 30 cm for snow depth in alpine areas (Geist and Stötter, 2008; Moreno Banos et al., 2009; DeBeer and Pomeroy, 2010) but can be much larger in steep and rough areas. Alternatively ALS campaigns can be performed with helicopter-based systems (Vallet and Skaloud, 2005; Skaloud et al., 2006; Vallet, 2011). The reduced terrain following flying height and the potential of the system to be tilted in direction of the target (improved incident angle) results in a higher accuracy. Comparing helicopter based snow depth maps with terrestrial laser scanning and tachymeter surveys Grünewald et al. (2010) found that the error of the ALS data was below 10 cm. The typical area covered by ALS datasets obtained for this study is between 1 and 30 km² and they all have a spatial resolution close to one metre. Accuracy estimations and references to the data analyzed in this study are given in Table 1.

2.2 Site description

We assembled a large data set consisting of seven investigation areas located in six different regions, including the Swiss and the Austrian Alps, the Spanish Pyrenees, and the Canadian Rocky Mountains. Two catchments are dominated by glaciers whereas

the remaining areas are free of ice. The borders of the investigation areas analysed in this study have been defined manually. This study focuses on the snow depth distribution of alpine areas. Therefore, effects of vegetation, such as interception of snow by trees, were not considered and all parts of the investigation areas which are covered by significant vegetation were masked from the data. Furthermore, it has been shown that ALS snow depth measurements are more accurate over alpine areas than adjacent forest covered areas (Hopkinson et al., 2012). In the following, we give a brief overview of the study sites. For more details, the reader may refer to Table 1, Figs. 1 to 3 and to the references given in the text.

2.2.1 Wannengrat, CH

The Wannengrat (WAN) area (Fig. 1a) is a small alpine catchment that is located in the eastern part of the Swiss Alps. The site has been an intensive investigation area for snow studies in recent years (Grünewald et al., 2010; Grünewald and Lehning, 2011; Mott et al., 2010, 2011, 2013; Schirmer et al., 2011; Schirmer and Lehning, 2011; Wirz et al., 2011; Egli et al., 2012). Most of the area is above the local treeline and no tall vegetation is present. Elevations range from 1940 to 2650 m a.s.l. and the lower part is typically characterized by gentle slopes whereas the summit region is formed by talus and steep rock faces. Storms which dominate the snow accumulation in the area usually come from the north-west (Schirmer et al., 2011; Mott et al., 2010). Two helicopter based (Vallet and Skaloud, 2005; Skaloud et al., 2006; Vallet, 2011) winter ALS campaigns were obtained in the area on 26 April 2008 and 9 April 2009, which represent the maximum snow accumulation in the area for the two years. The area of the second flight covers 5 km², whereas the first flight only covers a small part of the domain (1.5 km², see Grünewald et al., 2010; Grünewald and Lehning, 2011).

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2.2.2 Piz Lagrev, CH

The Piz Lagrev (LAG) study area (Fig. 1b) includes the south face of the Piz Lagrev, which is part of the mountain range defining the northern rim of the Engadin valley in the south-east of the Swiss Alps. The site is above the local treeline, and elevations range from 1800 to 3080 m. The Piz Lagrev is characterized by steep talus slopes which are surrounded by steep rock faces. Two pronounced, sheltered bowls dominate the upper part of the area (Grünewald and Lehning, 2011). ALS measurements were obtained on 7 April 2009 using the same technology as for the Wannengrat, and cover an area of about 5 km². Analysis of a nearby weather station indicates that the prevailing wind direction is south-west.

2.2.3 Haut Glacier d'Arolla, CH

The study domain Haut Glacier d'Arolla (ARO) is located on the main Alpine divide in the south-east of Switzerland (Fig. 2a). Elevations range from 2400 to 3500 m a.s.l. and the area of the domain is about 10 km². The region is dominated by the 4.4 km² Haut Glacier d'Arolla and by several smaller cirque glaciers. About 50 % of the area is glaciated and the rest of the domain is characterized by steep slopes and rock faces. Helicopter based Lidar measurements of the area were obtained in November 2006 and May 2007 (Dadic et al., 2010a,b). The resulting snow depth map represents the time of the maximum snow accumulation for at least the high regions of the catchment. According to Dadic et al. (2010a), at that point of time, elevations below 2700 m a.s.l. had already been affected by surface melt. Note that changes of the surface of the DEM due to glacier dynamics and the settling of firn in the accumulation area were not accounted for when calculating the snow depths. This resulted in a potential underestimation of the true snow depth in the accumulation area of the glacier, and in an overestimation in the ablation zone, whereas the overestimation in the ablation zone is countered by the previously mentioned surface melt. An analysis of weather stations in the surrounding area showed that wind directions are variable, but that the synoptic

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main flow is from the southwest. This is also confirmed by measurements in the catchment (Dadic et al., 2010a,b).

2.2.4 Hintereisferner, AT

The investigation area Hintereisferner (HEF) is situated in the upper Rofen valley, which is part of the Ötztal Alps at the Austrian–Italian border (Fig. 2b). The catchment, as defined for this study, covers an area of 25 km² and is characterized by glaciers, steep slopes and rock faces. Elevations range from 2300 to 3740 m a.s.l. and the largest glaciers are the valley glacier Hintereisferner (2002: ~ 6.5 km²) and the Kesselwandferner (2002: ~ 3.8 km²). On the local scale, wind directions are very variable, but the main direction is northwest. In this study, we analyze data obtained in three measurement campaigns in the beginning of May 2002, 2003 and 2009, and one data set acquired in June 2002 (Geist and Stötter, 2008, Table 1). The first three flights were near the end of the seasonal snow accumulation in the area, whereas snowmelt clearly had an effect on the lower parts of the catchment in June 2002. To calculate snow depth, each of the winter DSMs was subtracted from a summer DEM obtained in the previous autumn of the respective year. As for ARO, glacier dynamics were neglected in the calculations. More details on the investigation area and the ALS campaigns can be found in Geist and Stötter (2008) and Bollmann et al. (2011).

2.2.5 Vall de Núria, ES

Vall de Núria (NUR) (Fig. 3a) is located at the main divide in the Eastern part of the Spanish Pyrenees. An ALS campaign covering an area of 38 km² was performed on 9 March 2009, which is near the time of the peak of the seasonal accumulation for the area (Moreno Banos et al., 2009). 28 km² of the area remained after masking significant vegetation and human infrastructure. Elevations range from 2000 to 2900 m a.s.l. and the mean slope is 28°. The area is characterized by a mixture of gentle slopes and some steeper, rocky areas in the summit region. The most frequent synoptic wind

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direction in the area is from the northwest, even though a large variability of the wind direction is present on the local scale.

2.2.6 Marmot Creek, CA

Marmot Creek Research Basin in the Kananaskis Valley, Alberta is located within the Front Range of the Canadian Rocky Mountains. For our analysis we selected two small domains (Fig. 3b). The investigation area named Marmot Creek (MAR) in this study is the alpine zone surrounding Mount Allan and includes the Marmot Creek basin in the East. The 9 km² area is above the local treeline (about 2200 m) and covers elevations from 1760 to 2765 m a.s.l. MAR is characterized by a mixture of gentle and steep slopes (average slope 31°), covered by alpine tundra with some small bands of rock on the steepest slopes. The second study area is the summit region of Skogan Peak (SKO), which is 4 km to the east from Marmot Creek, above Skogan Pass and near Mount Lorette. The size of the domain is 8 km² and the elevation range is 1660 to 2660 m a.s.l. SKO is characterized by very rough topography with steep slopes and rock faces (average slope 40°). Only small areas have gentle terrain. Airborne Lidar surveys of the snow cover were obtained at 29 March 2008. The time of the flight did not coincide with the maximum of the seasonal snow accumulation in the area, which was reached in mid-May (DeBeer and Pomeroy, 2010; Hopkinson et al., 2012). The snow cover in the complete area is strongly affected by winds, which mainly come from the northwest to Fisera Ridge in MAR but generally come from the southwest (MacDonald et al., 2010). Further information on the area and the climatic conditions can be found in DeBeer and Pomeroy (2010), MacDonald et al. (2010), Marsh et al. (2012) and Pomeroy et al. (2012).

2.3 Aggregation of sub-areas

The aim of this study is to explain the spatial variability of snow depth on the catchment scale. With high-resolution snow depth measurements at hand, a statistical

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assessment considering snow depth and topography at the highest possible resolution is difficult. The difficulty becomes obvious if one thinks about cornices or other drift features. Maximum snow depth in a cornice is not the result of topographic features (e.g. slope) directly at this point but is shaped by the upwind topography interacting with the wind. Therefore, a systematic correlation between snow depth and terrain parameters will not be found at very small scales. Regression models of snow depth of the different investigation areas (not shown) confirmed that and showed that at the highest resolution (metre scale without aggregation), only 2 to 37 % of the variability could be explained by the terrain. Because of the large spatial variability at scales of metres (Shook and Gray, 1996; Watson et al., 2006), we define subareas in order to smooth this small-scale variability. We aggregated the data to spatially continuous subareas with length scales of some hundreds of metres. Such an aggregation follows the concept of hydrological response units (HRU), which has successfully been applied for semi-distributed hydrological models (Kite and Kouwen, 1992; Rinaldo et al., 2006; Pomeroy et al., 2007) and is consistent with the concept of stratified snow sampling (Steppuhn and Dyck, 1974) where landscape units were defined to minimise within-unit variance of SWE and maximise difference in SWE between units. The HRU concept has been successfully applied to snow redistribution modelling (Fang and Pomeroy, 2009; MacDonald et al., 2009, 2010) and ablation modelling (Pomeroy et al., 1998, 2007; Dornes et al., 2008; DeBeer and Pomeroy, 2010). The facets applied by Daly et al. (1994) for the calculation of precipitation gradients or to the concept of snow accumulation units outlined by Hopkinson et al. (2012) are also similar approaches. However, our approach is specifically aimed at smoothing very small-scale drift features and does not make any other homogeneity assumption.

Two different methods for the aggregation are applied. The first is the same as performed by Lehning et al. (2011), who manually defined sub-areas from a subjective impression of the terrain (Fig. 4). The length scale of these subareas was approximately 500 m. The second method is a simple automatic approach which divides the domain into quadratic subareas. This approach is very similar to a simple resample

of the data to larger cell sizes. We have tested different grid sizes ranging from 100 to 800 m. An example which illustrates the aggregation is shown in Fig. 4. The criteria which were applied to select the cell size appropriate for the study are: (i) the small scale variability should be smoothed out to an extent that the remaining variability can be reasonably explained by the topographic parameters, and (ii) the number of sub-areas must be large enough to be able to fit robust regression models ($N > 20$). In order to avoid small clusters which do not represent a significant footprint of the catchment, very small sub-areas ($< 10\,000\text{ m}^2$) were automatically excluded from the aggregated data.

As the second method is a straightforward and fully automated approach, it is possible to compose multiple statistical models by randomly shifting the origin of the grid. This approach helps to identify the range of model performance and if a selected grid results in a representative model. The impact of random effects, which might be caused by a single grid or by subjective classification of the sub-areas, can therefore be assessed.

2.4 Statistical models

We use multiple linear regression to model the spatial variability of snow depth. The dependent variable is the relative snow depth dHS (deviation from the catchment mean). Simple parameters that describe the surface topography and that can be derived from a summer digital elevation model serve as explanatory variables. Elevation reflects the effect of decreasing air temperatures with altitude and can therefore be used as a proxy for parameters such as freezing level or the amount of energy available for melt (Clark et al., 2011), and for orographic effects of precipitation (Frei and Schär, 1998; Grünewald and Lehning, 2011) though it is recognized that there are substantial differences in orographic effects between windward and leeward slopes (Pomeroy and Brun, 2001). In order to be able to combine data sets from different areas, elevation was changed to relative elevation (dE), which is the difference between the absolute and the minimum elevation of the area. This mapping respects the fact that all data sets are

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from the alpine zone at or above treeline but that this corresponds to different absolute elevation in the different areas. The slope (SL) represents gravitational processes such as sloughing and avalanching, which have a significant effect on the snow distribution (Blöschl and Kirnbauer, 1992; Gruber, 2007; Sovilla et al., 2010; Bernhardt and Schulz, 2010). In combination with northing (NO), the slope also describes the amount of solar energy which is available for the ablation and settling of snow. NO is also important for the deposition and redistribution of snow by wind (Seyfried and Wilcox, 1995; Lehning et al., 2008), as more snow is usually accumulated in the leeward sides of slopes and mountains. An additional parameter, which represents the effect of the wind, is the mean sheltering index SX (Winstral et al., 2002), which has been calculated for the direction of the main flow (see site descriptions) and for a maximum distance of 100 m. Several studies showed that SX is a good measure for sheltering and exposure of the local terrain, which gives a simple but reasonable representation of the local flow field and therefore of the redistribution of snow by wind (e.g. Winstral and Marks, 2002; Winstral et al., 2002; Anderton et al., 2004; Erickson et al., 2005; Molotch et al., 2005; Litaor et al., 2008; Schirmer et al., 2011). Finally, different measures for the surface roughness are applied. The standard deviation of the elevation ($\sigma(E)$) and slope ($\sigma(SL)$) represent classical morphometric roughness measures (Evans, 1972; Speight, 1974; Shepard et al., 2001). The surface roughness strongly affects the redistribution of snow by wind and gravitational processes (Jost et al., 2007), and can be seen as the capability of the surface to trap snow. As suggested by Lehning et al. (2011), we also tested the fractal dimension D and the ordinal intercept γ of the semi-variogram, which have been identified as good measures for the surface roughness (Goodchild and Mark, 1987; Power and Tullis, 1991; Klinkenberg, 1992; Klinkenberg and Goodchild, 1992; Xu et al., 1993; Sun et al., 2006; Taud and Parrot, 2006).

For each of the aggregated data sets, we separately calculated all possible two- and three-parameter regression models and selected the most significant models (p -value < 0.001). Further selection criteria are the explanatory power (R^2) of the model and – if the R^2 was similar – the number of parameters included in the model. For data

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sets with a two-parameter model, which had a similar performance as the best three-parameter-model, the two-parameter-model was selected. To account for possible interactions of the parameters included in the models, factor combinations (multiplication of parameters) have been tested and included where appropriate. The preconditions of linear regression (normal distribution and constant variance of residuals) were examined by analyzing the Quantil-Quantil-plots and the Tukey-Anscombe plots of the model residuals (not shown). Additionally, the physical meaningfulness of the models (e.g. sign of the coefficients) has been examined, and models have not been selected if the sign of the coefficient was counter-intuitive. As mentioned before, the automatic aggregation to quadratic sub-areas allows the calculation of multiple random grids. This in turn can be used to analyse whether the best models are consistent (same explanatory variables) and show a small standard deviation of the coefficients when calculated for different grid realizations. Note that the fractal parameters D and γ could not be included in the multiple model runs, as their computation is computationally very demanding. D and γ were therefore only applied for the models with manually defined sub-areas and for few selected quadratic models.

To assess the transferability of the results, we also built a “global” model by combining all data sets. In addition, sub-sets of the data were combined based on their morphological characteristics. The two morphological models discussed here are “Glacier”, which includes the two sites which are currently glaciated, and “No glacier”, which combines all remaining, non-glaciated data sets from alpine terrain.

The multiple-year data sets for HEF and WAN allow a leave-one-out cross-validation in order to investigate the inter-annual consistency of the models. For HEF, models calculated from data sets containing three of the snow depth surveys in the area are validated with the remaining years. We repeated this procedure for each combination. Scatter plots and the coefficients of determination (R_{det}^2) are used to assess the performance of the cross-validation. As the extent of the 2008 data set for WAN is very small it could not be used to compose an own regression model. Nonetheless it could be used to validate the model obtained from the 2009 data set.

3 Results and discussion

3.1 Aggregation of sub-areas

In order to find the appropriate level of aggregation for the automatic approach, we calculated models for different grid sizes and compared the results in terms of model performance. Figure 5 illustrates such a result for the Wannengrat area. The explanatory parameters of the model are dE , SL and NO. The figure illustrates a strong decrease in the snow depth variability with increasing grid size (Fig. 5a), which is negatively correlated to an increased model performance (Fig. 5b). This relationship is not surprising since an increasing portion of the variability is smoothed out by the aggregation. Nevertheless, at cell sizes of about 400 m the effect of additional smoothing appears very limited. Based on the analysis shown in Fig. 5, this level therefore appears to be a good choice. It can explain much of the remaining larger scale spatial, while the number of sub-areas still remains large enough to calculate robust statistical models. For the other investigation areas, similar results (not shown) were obtained. Cell sizes between 200 and 500 m showed to perform best. This is consistent with the length scale of > 100 m found by Shook and Gray (1996) for minimal autocorrelation in snow depth data. We therefore decided to apply a grid size of 400 m to all areas. Moreover, this is a similar level of aggregation as for the manually defined sub-areas. A comparison of models, calculated with sub-areas identified by the manual and the automatic (400 m) approach, showed that the results are very similar in terms of the best parameters selected for the final models, and in terms of model performance. As it is an objective and fully automatic method, we only show results from the automatic procedure in the following.

3.2 Statistical models

The model assumptions for linear regressions (see above) were fulfilled satisfactorily for all data. Nevertheless, small deviations from the normal distribution of residuals

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for very large and very small residuals have to be reported for ARO, HEF and SKO. Logarithmic transformation of the variables has been tested. As this did not yield improvements, the original, non-transformed variables were used.

3.2.1 Single catchment models

5 Table 2 summarizes the best models for each of the single investigation areas. The table indicates that similar parameter combinations dominate most areas. Such, dE , NO and SL are included in almost all models. SX is included for NUR and for MAR. A roughness index is only present in the model for NUR ($\sigma(SL)$) and SKO (γ). Nevertheless substituting γ by ($\sigma(SL)$) would result in a model with a similar performance.
10 For some areas, different parameter combinations than the ones presented have only a slightly lower performance (not shown). Factor combination significantly improved the model for NUR, MAR and ARO. Adding an additional parameter would further improve the models for some of the areas (NUR, MAR, SKO). In order to keep the models as simple as possible and to avoid an over-parameterization of the small areas, we do not include such additional variables.

15 As an example, we now focus on the Wannengrat area (first row in Table 2). The model represents a positive elevation gradient of the snow depth which is 15 cm per 100 m – a decrease of dHS with the slope angle ($2 \text{ cm} (\text{° SL})^{-1}$) and a decrease of dHS toward southerly aspects ($4 \text{ cm} (10\text{° NO})^{-1}$). Figure 6 compares a dHS map resulting from the model with measured dHS, aggregated to the model resolution. The upper image shows the snow depth distribution as aggregated from the ALS measurements, while the lower image presents the snow cover as calculated with the model. The figure illustrates that the statistical approach seems suitable to characterise the general spatial patterns of the snow depth distribution. Deviations occur especially in regions
20 of extreme dHS, for example, in single cells in the northwest, the southeast or the southwest. This indicates that the model does not properly capture the extremes of the distribution. Nevertheless, the deviations are only small.

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Returning to Table 2 and focussing on the different areas, it appears that both the parameters and the model coefficients are varying between the data sets. It is also obvious that the performance of the models (R^2) is quite different. While the model for LAG can explain more than 90 % of the snow depth variability, only 30 % could be explained for MAR and 41 % for SKO. For most areas, the R^2 is between 0.5 and 0.7, which is a very good score in comparison to published results obtained at similar scales. The large range in the model performance might be attributed to the topographic diversity within the single catchments. Smaller, less complex catchments, such as LAG or WAN perform much better than the very large (HEF, ARO, NUR) or very complex (MAR, SKO) areas. Reasons for the relatively low R^2 for MAR and SKO can be found in the characteristics of the data sets, where the topography in the summit region of the two areas is dominated by extremely steep rock-faces (Fig. 3b), which are exposed to wind and avalanches. In the period before the snow depth data had been acquired, several heavy storms occurred in the area. The heavy winds eroded and sublimated much of the snow cover in the summit region and, as a result, the major portion of the summit region was nearly free of snow. This is a common characteristic of alpine snow in the relatively windy Canadian Rockies (MacDonald et al., 2010). A further possible reason for the lower performance of some of the models could be the accuracy of some parts of the ALS data. As mentioned before, it must be expected that biases are larger in steep and rough terrain, especially for the data obtained from airplanes. Such terrain-based errors will also influence the models on resolutions as presented here and must be considered when interpreting results from such areas, especially when slope serves as an explanatory variable.

In general, the results confirm that topography dominates the snow depth distribution at that scale. The deviations between the models indicate that the influences on the snow depth distribution are variable in the different areas. For example, the magnitude of the elevation gradient is between 6 and 25 cm/100 m, and the coefficient for slope varies by a factor of four (ARO not included because of factor combinations). For NUR

and MAR, dE seems not to be important at all. Instead, the sheltering effect of the terrain (SX) is more important.

The representativeness of the results obtained from the selected grid (Table 2, Fig. 4) was assessed by calculating multiple model runs, for which the origins of the grid were shifted randomly. Results are summarized in Table 3. Fifty runs were performed for the best model, as identified in Table 2 (but without factor combinations), for each investigation area. The table shows the sample space (25 to 75 % quantiles) for all model parameters and for the model performance. The last column indicates the R^2 of the model-run that is based on the same grid as the models presented in Table 2. Taken as a whole, Table 3 shows that most of the models represent the total average well.

An additional important finding from these ensemble calculations is that the scatter between the single runs is only moderate. For R^2 , interquantile ranges between 0.01 and 0.12 (Table 3) were calculated. Nevertheless, it is still necessary to note that for a few data sets outliers with much larger or much smaller R^2 values were observed.

3.2.2 Combined models

For practical applications on a large scale, it would be very beneficial if it were possible to find a “global” model, which would be able to predict a large portion of the spatial variability for all data sets. We therefore combined all data to one large data set and built a new model, following the same procedure described above. However, the resulting model (Table 4), which selected dE and SL as explanatory variables, was only able to explain 23 % of the total snow depth variability of the aggregated data. Additional model parameters or factor combinations could not significantly improve the model. A model that only includes data from the alpine areas, which are presently not glaciated, is capable of explaining 30 % of the variability. This is clearly worse than the models for most of the single data sets (Table 2). It appears that as suggested by Pomeroy and Gray (1995), the interaction between topography and snow depth is not the same at different sites, and that a statistical relationship, developed for one area,

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cannot directly be transferred to a different site. In contrast, the “glacier” model features a similar performance to the models for the single glaciers (ARO and HEF). This could indicate that similar characteristics are important for the snow cover on glaciated catchments or that the sample size is too small to show substantial variability in glaciated sites. However, since the model consists of the same data as the HEF model presented in Table 2, only supplemented by the comparably small ARO data, the ARO data will therefore only have a minor effect on the model and its R^2 value.

Finally, when combining data sets from different sources, one needs to be aware of possible differences in the platforms and sensors applied for the data acquisition. Sensors of different manufacturers can be very diverse in their design, operational envelope and laser pulse specifications which might result in different levels of performance and error propagation.

3.2.3 Inter-annual consistency

Results of the cross-validation, as described in Sect. 3.2.1, are shown in Table 5. Figure 7 illustrates the scatter-plots for the validation, as shown in lines two (a) and five (b) of Table 5. The table emphasizes that the R_{det}^2 values are around 0.5, which is similar to the R^2 values of the full models. Only WAN and the fourth HEF model have a lower R_{det}^2 . Nevertheless, Fig. 7b shows that for the WAN data the model is appropriate for both years for most sub-areas, even if R_{det}^2 is low.

From these findings, we conclude that the models can be transferred between various years, at least for the points of time at which maximum snow accumulation occurred. This confirms a finding of Schirmer et al. (2011), who detected a large consistency in the snow depth distribution at the Wannengrat between two years. A high inter-annual correlation was also reported by Deems et al. (2008) for two mountain sites in Colorado. However, at Wolf Creek Research Basin in Yukon, Canada, Pomeroy et al. (2004) and MacDonald et al. (2009) found substantially different snow accumulation distributions from year to year as primary wind directions of the major storms

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shifted between southerly and westerly. From our data, we cannot verify if the models can also be applied for earlier periods in the season. As the snow cover present at the end of the winter is the result of many individual snow fall events which are all affected by the topography, we speculate that the models, at least at a scale as presented in this paper, might also have explanatory power if applied to the accumulation season. The study of Schirmer et al. (2011), who concluded that few major storms shape the snow depth distribution at the end of the winter, supports that hypothesis.

4 Conclusions

In this paper, we have applied linear multiple-regression modelling of snow depth distributions with topographic parameters for several small and medium size catchments in different mountain regions of the world. We showed that statistical modelling is capable of explaining large parts of the spatial distribution of snow depth on the catchment scale. This is only achieved if the data is aggregated to length scales of some hundreds of metres, in order to smooth out the very large heterogeneity caused by drifting snow at small scales. After arbitrary clustering of the data to quadratic cells with a grid size of 400 m, 30 to 90 % of the variability could be explained by including only three explanatory parameters. For the first time, a systematic investigation of the explanatory power as a function of scale has been made. The parameters which are most frequent in the models are the elevation gradient (dE), the slope (SL), a substitute for the aspect (NO), and a wind-sheltering index (SX). These results are typically better than those obtained by other studies because of the systematic aggregation. It is important to notice that owing to the high resolution of the original data applied in our study, the full small-scale variability of the snow cover is captured. This is not the case for most earlier studies, which had to rely on a limited number of point observations, such as snow stakes or SNOTEL sites. This means that not only is it likely that the full variability is not represented in these data sets, but also that there is a potential bias in the data, e.g. if only flatter portions of a catchment are sampled (Wirz et al., 2011).

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Studies which compare data from different regions are also rare. Our analysis showed that there are clear differences between the models for the specific regions, but that a global model still explains a significant fraction of the variability (23 % or 30 % without glaciers). This indicates that the relationship between snow and topography is less universal than hypothesized by Lehning et al. (2011) and the application of a “global” model is limited. On the contrary, it could be shown that statistical models, developed for one year, can sometimes be well applied to other years, at least for the points of time of the maximum seasonal accumulation. This is an important finding for applications in hydrology or glaciology. A method, as presented here, can serve as a straightforward approach to characterise the spatial distribution of the snow cover. Applications from year to year should be applied with caution in some areas which have been reported to show high inter-annual changes in wind regimes that transport blowing snow.

We expect that more area-wide snow depth data sets will become available in the coming years. It might soon be possible to cover a larger spectrum of mountain regions for all over the world. It will be interesting to see if the results presented can be confirmed for different areas and if a true “global” model can be developed. Combining statistical with parametric or physically based methods might also yield more robust, yet still simple, models of snow accumulation. Another question which needs to be addressed is if such statistical relations are also valid for different points of time during the snow season, and how the statistical relationships change with time. This would require area-wide snow depth data for a larger area from different points of time during a season.

It should also be possible to extend similar models to vegetated areas. This would lead to the introduction of additional explanatory parameters which represent the influence of trees and vegetation, for example, a measure of winter plant-area index as used by Pomeroy et al. (2002).

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Table 1. Data sets. “Date” is the date of the winter survey, “Area” the area of the data set, “Mean acc.” the mean accuracy in vertical direction and “Platform” the Measurement platform.

Name	Date	Area [km ²]	Mean acc. [m]	Platform	Reference
Wannengrat (WAN)	26 Apr 08	4	0.1	Riegl LMS Q240i-60	Grünwald et al. (2010); Lehning et al. (2011); Grünwald and Lehning (2011)
	9 Apr 09	1.5			
Piz Lagrev (LAG)	7 Apr 09	3	0.1	Riegl LMS Q240i-60	Grünwald and Lehning (2011); Lehning et al. (2011)
Haut Glacier d’Arolla (ARO)	1 May 07	10	0.15	Riegl LMS Q240i-60	Dadic et al. (2010a,b)
	7 May 02				
Hintereisferner (HEF)	15 Jun 02	25	0.3	Optech ALTM1225	Geist and Stötter (2008); Bollmann et al. (2011)
	4 May 03			Optech ALTM1225	
	4 May 03			Optech ALTM2050	
	7 May 09			Optech ALTM3100	
Val de Nuria (NUR)	9 Mar 09	28	0.3	Optech ALTM3025	Moreno Banos et al. (2009)
Marmot Creek (MAR) Skogan Peak (SKO)	29 Mar 08	9	0.2	Optech ALTM3100C	DeBeer and Pomeroy (2010); Hopkinson et al. (2011)
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Table 2. Best two- to three-parameter model for each single investigation area, where dHS and dE are in metres and SL and NO in degree. Column 3 to 5 show the R^2 , the adjusted R^2 (R_{Adj}^2) and the number of sub-areas for each model. For HEF all data (four points of time) were combined to one single model.

Area	Model					R^2	R_{Adj}^2	N	
WAN	dHS = 0.00153 · dE	−0.0240 · SL	−0.0043 · NO			+0.60	0.76	0.73	35
LAG	dHS = 0.00202 · dE	−0.0574 · SL				+1.39	0.91	0.90	29
NUR	dHS =	−0.0005 · NO	+0.56 · SX	+0.1715 · σ (SL)	−0.0012 · NO · σ (SL)	−0.49	0.50	0.49	222
MAR	dHS =	−0.0115 · SL	−0.0025 · NO	+0.77 · SX	−0.0049 · NO · SX	+0.61	0.30	0.27	66
SKO	dHS =	−0.0363 · SL	−0.0074 · NO	+0.59 · γ		+1.84	0.41	0.38	66
ARO	dHS = 0.00246 · dE	−0.0009 · SL	−0.0032 · NO		−4.054 × 10 ^{−5} · dE · SL	−0.26	0.53	0.50	82
HEF*	dHS = 0.00182 · dE	−0.0385 · SL	−0.0024 · NO			+0.05	0.51	0.50	720

* includes HEF(05-2002), HEF(06-2002), HEF(05-2003), HEF(05-2009)

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Table 3. Comparison of the model performance of the multiple random runs and the single selected model as presented in Table 2 (R_{sel}^2). α_i are the factors of the respective model parameters as listed in column 2. The 50 model runs obtained for each data set resulted in a distribution for each of the factors (α_i , β) and R^2 . Column 3 to 7 show the 25, 50 and 75% quantiles of these distributions.

Area	Model	Quantiles α_1			Quantiles α_2			Quantiles α_3			Quantiles β			Quantiles R^2			R_{sel}^2
		0.25	0.5	0.75	0.25	0.5	0.75	0.25	0.5	0.75	0.25	0.5	0.75	0.25	0.5	0.75	
WAN	$\alpha_1 \cdot dE + \alpha_2 \cdot SL + \alpha_3 \cdot NO + \beta$	0.00131	0.00140	0.00151	-0.0046	-0.0042	-0.0039	-0.0260	-0.0240	-0.0224	0.58	0.62	0.68	0.67	0.73	0.77	0.76
LAG	$\alpha_1 \cdot dE + \alpha_2 \cdot SL + \beta$	0.00218	0.00226	0.00232	-0.04764	-0.04579	-0.04317				0.74	0.86	1.02	0.90	0.91	0.92	0.91
NUR	$\alpha_1 \cdot NO + \alpha_2 \cdot SX + \alpha_3 \cdot \sigma(SL) + \beta$	-0.0101	-0.0099	-0.0096	0.52	0.58	0.61	0.0691	0.0726	0.0752	0.21	0.28	0.31	0.47	0.49	0.50	0.46
MAR	$\alpha_1 \cdot SL + \alpha_2 \cdot NO + \alpha_3 \cdot SX + \beta$	-0.0129	-0.0124	-0.0118	-0.0038	-0.0037	-0.0035	0.32	0.38	0.43	0.69	0.71	0.72	0.28	0.30	0.32	0.28
SKO	$\alpha_1 \cdot SL + \alpha_2 \cdot NO + \alpha_3 \cdot \sigma(SL) + \beta$	-0.0114	-0.0074	-0.0052	-0.0061	-0.0059	-0.0057	0.0009	0.0165	0.0221	0.68	0.73	0.85	0.31	0.33	0.35	0.37
ARO	$\alpha_1 \cdot dE + \alpha_2 \cdot SL + \alpha_3 \cdot NO + \beta$	0.00119	0.00128	0.00136	-0.01981	-0.01902	-0.01813	-0.0040	-0.0030	-0.0027	0.16	0.23	0.26	0.50	0.56	0.61	0.49
HEF*	$\alpha_1 \cdot dE + \alpha_2 \cdot SL + \beta$	0.00126	0.00127	0.00130	-0.03934	-0.03863	-0.03801				0.14	0.18	0.21	0.41	0.42	0.42	0.43

* includes only HEF(05-2002)

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Table 4. Best models, R^2 , R^2_{Adj} and number of subareas (N) for different combinations of the investigation areas.

Area	Model				R^2	R^2_{Adj}	N	
All ^a	dHS =	$0.00079 \cdot dE$	$-0.0145 \cdot SL$	$-0.0028 \cdot NO$	+0.28	0.23	0.22	682
No Glacier ^b	dHS =	$-0.0133 \cdot SL$	$-0.00528 \cdot NO$	$+0.0454 \cdot \sigma(SL)$	+0.53	0.30	0.29	423
Glacier ^c	dHS =	$0.00021 \cdot dE$	$-0.0686 \cdot SL$	$+5.329 \times 10^{-5} \cdot dE \cdot SL$	+0.79	0.48	0.48	802

Included data sets:

^a WAN, LAG, NUR, MAR, SKO, ARO, HEF(05-2001);^b WAN, LAG, NUR, MAR, SKO;^c ARO, HEF(05-2002), HEF(06-2002), HEF(05-2003), HEF(05-2009)[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[I ◀](#)[▶ I](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

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Table 5. Cross-validation for HEF and WAN. The first column lists the data which were used to fit the model (model parameters dE , SL , NO). The second column shows the data set used for the validation. R_{Model}^2 is the R^2 of the model, and R_{det}^2 the coefficient of determination.

Data in model	Validation data	R_{Model}^2	R_{det}^2
HEF 5/2002, 6/2002, 5/2003	HEF 5/2009	0.51	0.48
HEF 5/2002, 6/2002, 5/2009	HEF 5/2003	0.50	0.53
HEF 5/2002, 5/2003, 5/2009	HEF 6/2002	0.48	0.59
HEF 6/2002, 5/2003, 5/2009	HEF 5/2002	0.54	0.35
WAN 2009	WAN 2008	0.76	0.40

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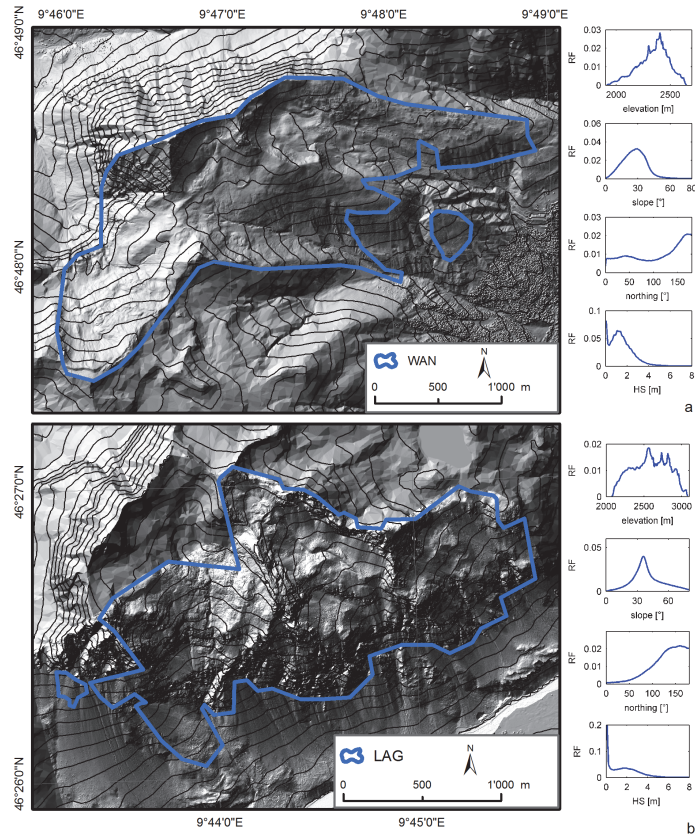


Fig. 1. Hillshade map of (a) the Wannengrat (WAN) and (b) the Piz Lagrev (LAG) study areas. The contour lines have an equidistance of 50 m. The right panels show histograms for elevation, slope, northing and the area-wide absolute snow depth obtained from ALS. Data source basemap: (a, b): DOM-AV ©2012 swisstopo (5704 000 000).

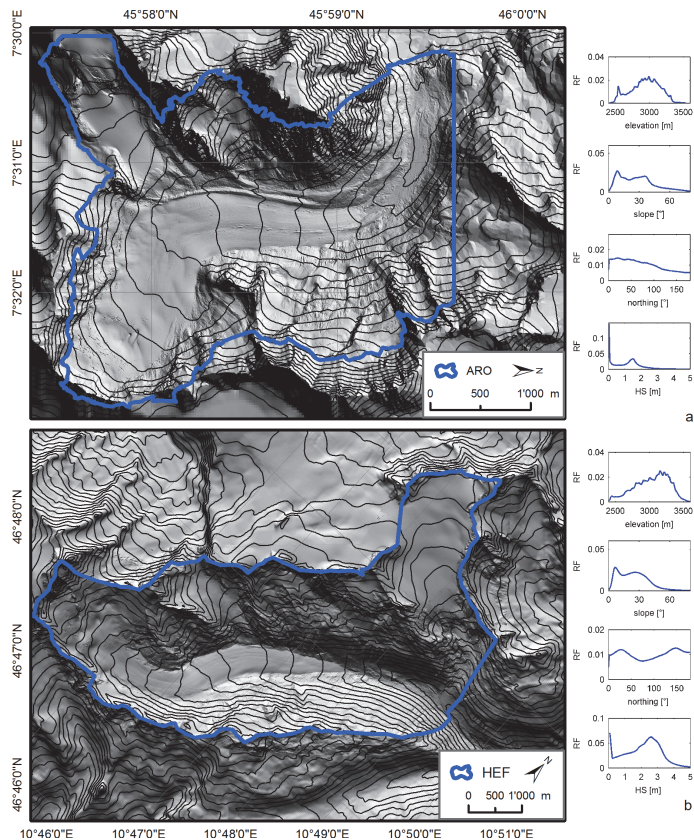


Fig. 2. Hillshade map of **(a)** Haut Glacier d'Arolla (ARO) and **(b)** the Hintereisferner (HEF) study areas. The contour lines have an equidistance of 50 m. The right panels show histograms for elevation, slope, northing and the area-wide absolute snow depth obtained from ALS (for HEF: Mai 2002). Data source basemap: **(a)** DOM-AV ©2012 swisstopo (5704 000 000); **(b)** Land Tirol – <http://data.tirol.gv.at>.

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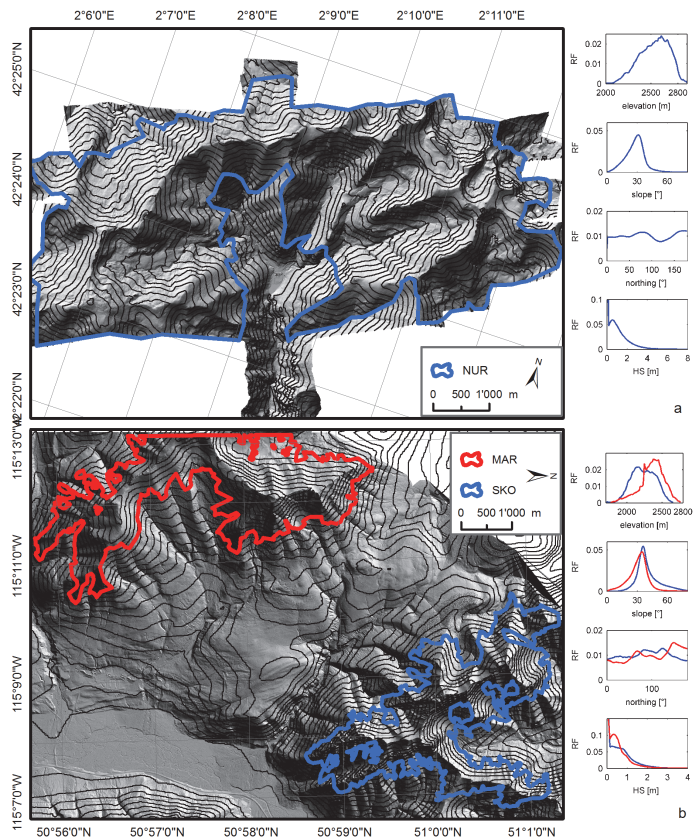


Fig. 3. Hillshade map of (a) the Val de Nuria (NUR) and (b) Marmot Creek Research Basin area with the study areas Marmot Creek (MAR) and Skogan Peak (SKO). The contour lines have an equidistance of 50 m. The right panels show histograms for elevation, slope, northing and the area-wide absolute snow depth obtained from ALS.

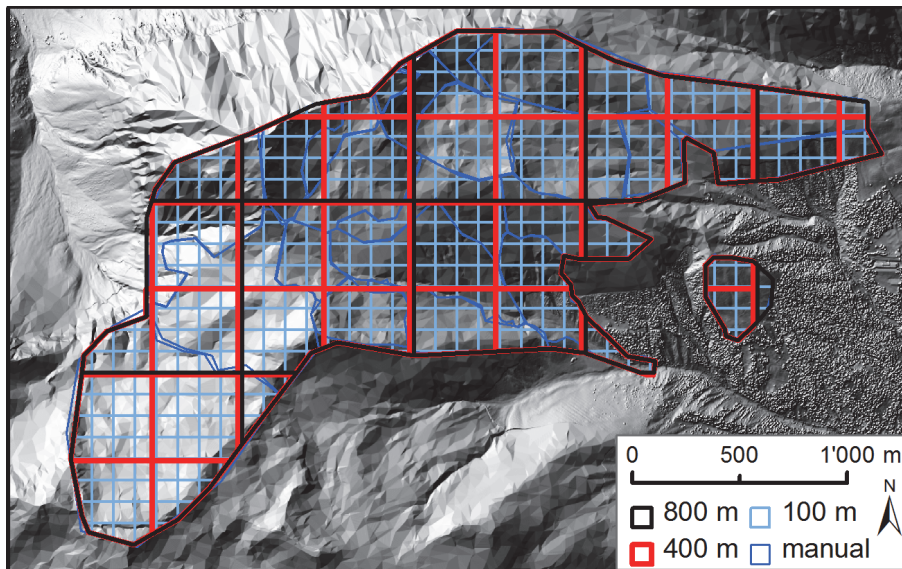


Fig. 4. Aggregation of sub-areas for the Wannengrat area by the manual and the automatic method (grids of different cellsize)

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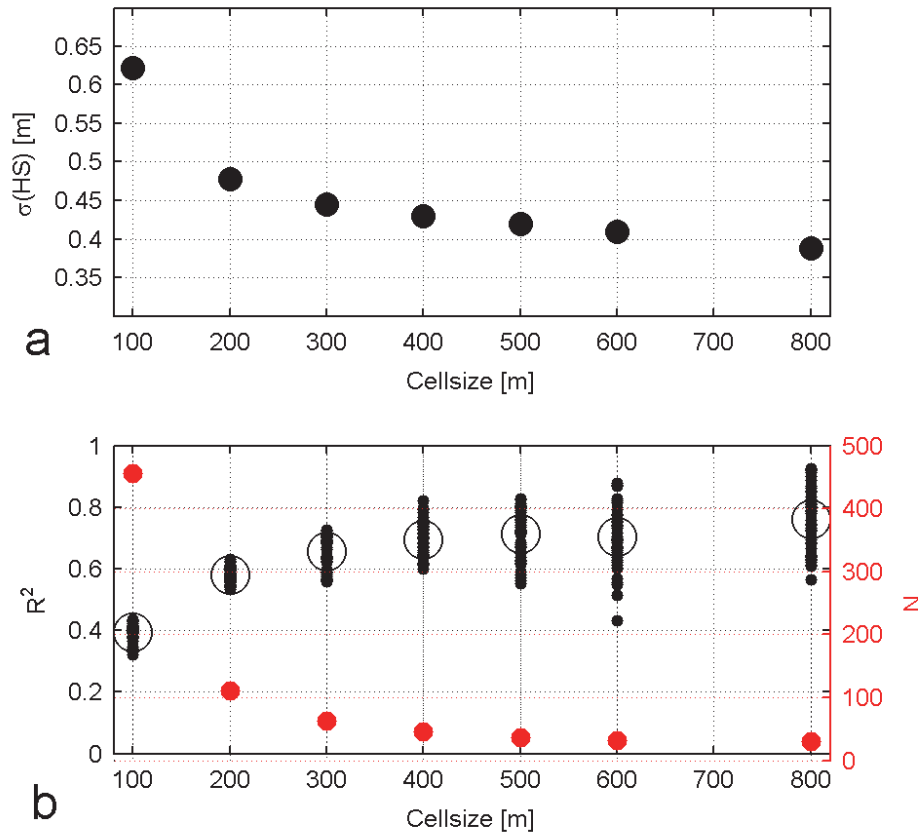


Fig. 5. Relationship between the level of aggregation (cell size) and snow depth variability expressed by (a) the standard deviation $\sigma(\text{HS})$, and (b) model performance (R^2) for the Wannengrat area (model with dE, SL, NO). The black circles indicate the mean of 50 random model runs. The red dots show the average number of sub-areas (N) at each aggregation level.

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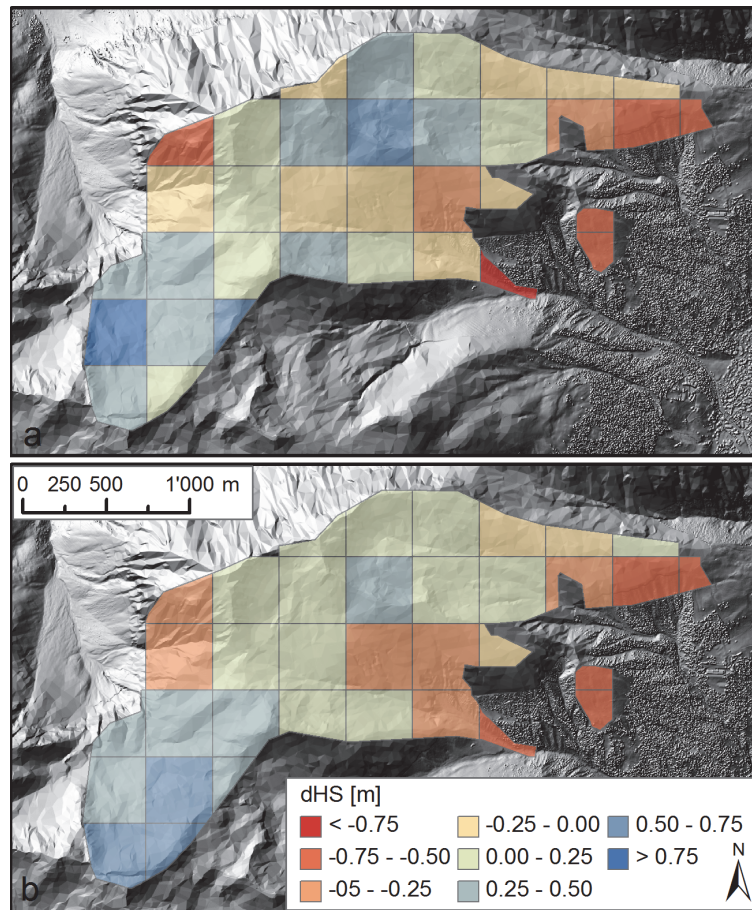


Fig. 6. Comparison of dHS for the Wannengrat in April 2009, aggregated to **(a)** a 400 m grid from ALS-measurements, and **(b)** modelled with a regression model with dE , SL and NO .

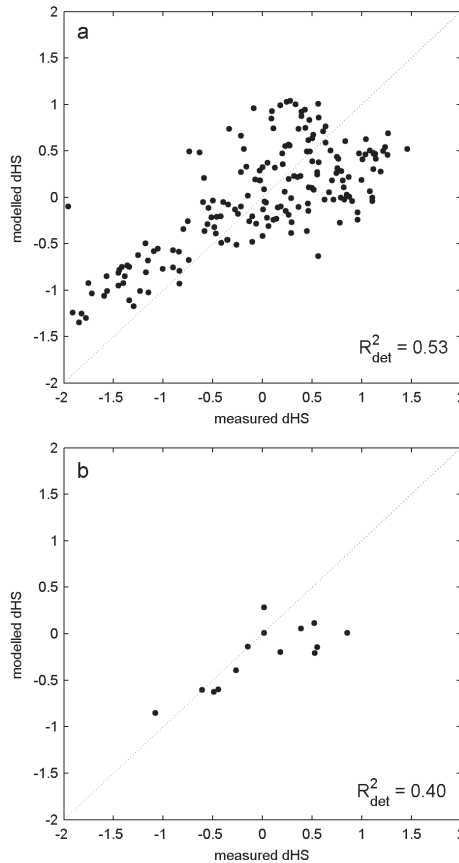


Fig. 7. Measured vs. modeled (parameters: dE, SL and NO) dHS for **(a)** HEF and **(b)** WAN. For HEF, the snow depth data obtained in May 2003 are validated in a model calculated with the data from May 2002, June 2002 and May 2009. For WAN, the model from 2009 is validated with data from 2008.

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