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Determination of cost coefficients of priority-based water allocation linear programming model – a network flow approach

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utilization of water resources. The means by which water is moved must also conform to the associated conveyance capacity.

Solving the above problem requires a clear identification and proper modeling of the allocating rules that account for every possible combination of supply and demand conditions (Ilich, 2008). A common approach is to utilize optimization methods (Yeh, 1985; Labadie, 2004; Rani and Moreira, 2010), among which the most widely applied is the linear programming (LP). This approach relies on LP to find the optimal feasible way of routing water in a regional system, given that the allocation objective, governing equations of physical water movement and operational constraints are appropriately linearly formulated. This formulating process requires sufficient knowledge of the optimization method as well as the under-analyzing problem to transform the physical and operational features into mathematical representation. Moreover, satisfying the allocating rules usually requires trial-and-error process to determine the most appropriate set of weighting factors or cost coefficients, which multiplying with respective allocated water constitutes the objective function. The lack of a systematic and precise way to establish and interpret the objective function may prevent the model from being entrusted or accepted by all involved stakeholders (Juízo and Lidén, 2010).

As a specialization of LP, network flow programming (NFP) only focuses on solving a specific subset of general LP problems that can be formulated in a more restrictive format. This loss of generality allows the resources allocation problem to be visually and precisely displayed by the network structure, and gains in return higher computational efficiency and easier comprehension of priority-based allocation mechanism. These characteristics has prompted model developers to incorporate NFP into many general models (Evenson and Moseley, 1970; Sigvaldason, 1976; Labadie et al., 1986; Martin, 1987; Kuczera and Diment, 1988; Brendecke et al., 1989; Chung et al., 1989; Andrews et al., 1992; Wurbs, 1993; Yerrameddy and Wurbs, 1996; Fredericks et al., 1998; Ilich et al., 2000; Dai and Labadie, 2001; Chou and Wu, 2010). The NFP represents the physical aspect of a water resources system as a directed network $G(N, L)$, where N is the set of n nodes and L is the set of m links. The formulation of a minimum cost

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NFP problem can be expressed as (Ahuja et al., 1993):

$$\text{Minimize } \sum_{(i,j) \in L} c_{ij} \cdot x_{ij} \quad (1)$$

Subject to

$$\sum_{\{j:(i,j) \in L\}} x_{ij} - \sum_{\{j:(j,i) \in L\}} x_{ji} = 0 \quad \text{for all } i \in N \quad (2)$$

$$l_{ij} \leq x_{ij} \leq u_{ij} \quad \text{for all } (i, j) \in L \quad (3)$$

where, i, j are the indices of node; (i, j) is the link from the tail node i to the head node j ; x_{ij} represents the amount of flow on link (i, j) ; c_{ij} is the unit shipping cost along link (i, j) ; l_{ij} and u_{ij} is the lower and upper limits on flow in link (i, j) .

In a NFP-based water allocation model, nodes can represent storage or non-storage points of confluence or divergence, and links represent reservoir outlet works, channels or pipes, water consumption, and carryover storage. Equation (2) indicates the continuity and availability of water at a node, for it states that the flow out of the node should equal to all incoming water. The upper and lower limits of a link represent its physical flow capacity, thus Eq. (3) states the transportability of water conveyance. The cost coefficient promotes flow routes that minimize net cost, thus determining the most preferable allocation of water supply with respect to a given allocating rule. Thus, correct assignment of link cost coefficients to reflect respective priorities is a necessary condition for any effective applications of not only NFP but LP-based water allocation models. Most common applications directly assign the cost coefficients related to the links of carryover storage or water consumption to represent the priorities of associated stakeholders. However, there are situations while internal links other than demand or storage have to be assigned with nonzero costs in order to achieve specific allocation requirements, such as water conveyance preference or surplus water diversion. This type of assignment is not straightforward for practitioners with little theoretical background, especially when forced to deal with a regional system of multiple

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reservoirs, water conveyance routes, instream flow requirements and trans-basin water diversions.

The present study demonstrates a method for establishing cost coefficients that adequately represent water supply allocation priorities. These cost coefficients allow one to simulate such water allocation priorities as rule curves of reservoir, storage allocation among multiple reservoirs, preferred water mains, and trans-basin diversion of surplus water. Path enumeration analysis is adopted to convert user-specified water supply allocation rules into a set of constraints; solving these constraints yields the cost coefficients that adhere to all specified rules. Further, an approach to prune the original system into a reduced network is finally proposed to establish the precise constraints of nonzero cost coefficients which can then be efficiently solved. This pruned procedure thus functions successfully to initialize an effective application of water allocation models.

2 Water allocation model

2.1 Alternative approaches: linear programming vs. network flow programming

The following presentation of methodology uses NFP framework to demonstrate the procedure of determining cost coefficients. This concept is helpful to interpret the establishment of objective function for more generalized LP-based models. The major difference between these alternative optimization approaches in modeling water resources allocations is how the non-NFP constraints, which cannot be represented by Eqs. (2) and (3), are incorporated. These constraints usually originate from the needs of simulating physical water movement process, such as return flows, flow losses, reservoir evaporation, and channel routing effects. In a pure NFP-based model, these features have been handled through the use of successive iterations (Ilich, 2008, 2009). These iterative processes are external to the algorithmic solving procedure. Usually the lower or upper limits of links are iteratively adjusted to meet non-NFP constraints,

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thus the priorities dictated by link costs are unchanged during iterations. By contrast, an LP solver can directly incorporate non-NFP constraints into the formulation and the algorithmic solving procedure. However, this flexibility may impair the characteristic of priority-based water allocation of NFP. One simple example is that water may be allocated to a junior-priority demand with less flow loss, rather than a senior demand with greater flow loss, if the objective function is not appropriately set up in the LP formulation. The discussions between Israel and Lund (1999) and Labadie and Baldo (2001) represent counterparts between these two approaches.

2.2 Framework of network flow programming–based allocation model

NFP-based water allocation models can be used to allocate water over single or multiple time steps. For models that allocate water across multiple time steps, links connect reservoir nodes in different time periods to represent carryover storage. These models have been applied in reservoir sizing (Kuzera, 1989; Khaliqzaman and Chandler, 1997), capacity expansion (Martin 1987; Gondolfi et al., 1997), the derivation of reservoir operating rules (Lund and Ferreira, 1996; Bessler et al., 2003), water transfer during droughts (Cheng et al., 2009), and the optimal real-time flood control operation of reservoirs (Braga and Barbosa, 2001). Single time step models allocate water only within an operational unit period, but the allocation is sequentially solved in every step during the simulation time horizon. Routing results produced in this manner are useful for quantifying the expected water supply situation and the risks of water shortage under the simulated conditions. This study discusses the assignment of cost coefficients for the single time step model.

Figure 1 illustrates a water resources system as a network during a unit operational period. Virtual links illustrated by dotted lines satisfy Eq. (2), which specifies continuity equations of nodes, by conveying water into and out of the system. These virtual links signify the inflow of system, initial and carryover storage of reservoir, water consumed by the stakeholders, and the water body that receives surplus flow.

2.3 Principle in assigning cost coefficients and the necessity of preprocessing analysis

The cost coefficients of links, generalized by Fig. 1, quantify the relative priority of each respective water user. These cost coefficients must reflect the flow priorities associated with demand or storage under predefined operating conditions. One straightforward way to achieve this is to assign decreasing unit costs for demand/storage links of higher priority to ensure that the highest priority stakeholder is satisfied first in the cost minimization problem (Israel and Lund, 1999). The costs of internal links other than demand or storage can be kept as zero, thus the allocation will be solely driven by the relative value of costs on the virtual links as shown in Fig. 1. Nevertheless, there are situations while only assigning cost coefficients on demand or storage links is not enough to achieve the allocation requirements. One simple example is that minor costs such as -1 or $+1$ are commonly assigned on links where flow is to be encouraged, such as hydropower plant, or discouraged such as routes with high transmission loss.

Another example is the transbasin diversion of surplus water, which requires diverting the required surplus water of a system into the adjacent system to enhance the efficiency of water utilization. An intuitive way to achieve this requirement is to use the iterative approach suggested by Labadie and Baldo (2001). This approach recommends a conceptual “flow-through” demand to be placed in the transbasin tunnel. This demand is given a lower priority than all demands or storage in the system to be diverted, which guarantees that transbasin diversions only occur once all demands in the original system are satisfied. According to the water supplied to the flow-through demand, iterations are then performed to artificially inject this diverted water into the adjacent system. Thus transbasin diversion will work as long as the original system has surplus water, regardless of the hydrological condition of the other system. However, there is no need to perform diversion when both systems are in abundance of water, for the diverted flow will become surplus to the other system. Although the “flow-through” approach is capable of simulating physical water movement process such

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as non-consumptive water usage, it may not properly model the operational features, such as adequate timing of diversion in this situation. This is especially critical when the transbasin diversion is charged with money, thus unnecessary diversions should be avoided. Inevitably, satisfying the condition of surplus water diversion requires assigning a positive cost on the link of transbasin tunnel, without using the flow through demand approach.

The determination of cost becomes more complicate if a combination of various allocation rules is involved, such as different operating rule curves for individual reservoirs, preferences of water conveyances in multiple locations, the allocation of multi-reservoir storage, and trans-basin water diversions. When multiple links in the system have to be assigned with nonzero cost coefficients, the accumulation of costs along a flow path to a demand/reservoir might impair its priority which is originally dictated by the cost of virtual link. The connectivity between links of nonzero costs has to be identified to ensure that the sum of cost coefficients in paths to a water usage of higher priority is always less than the total costs of any path to a lower priority stakeholder. If the user can not ensure assigning nonzero costs on which links to achieve the allocation requirements, a general preprocessing analysis will have to assume that the cost coefficient of every link in the system is unknown.

This study develops a procedure to establish the objective function of NFP-based water allocation models, in which representative allocation rules encountered are all considered. The allocation associated with reservoir operating rule curves and multi-reservoir storage balancing was preliminarily addressed in Chou and Wu (2011). These two rules are more elaborated in this paper, with two additional rules, trans-basin surplus diversion and water conveyance preference, being proposed to constitute the comprehensive analyzing framework as shown in Fig. 2. Water allocation rules and cost-determining procedure is described in detail in the following section.

3 Water allocation rules

3.1 Rule 1: trans-basin diversion of surplus water

Generally, the development of a new trans-basin water diversion project must not impact existing users of the system. Figure 3 depicts a simple example, in which only surplus water in the system associated with reservoir B can be diverted for storage in reservoir A. Thus, the first rule allows users to specify a link in the network representing a way of distributing water with last priority. The priorities of all paths through this specific link are junior to any other paths to demands and storage in the system.

Let L be the set of all links, L_D be the set of virtual demand links, L_S be the set of virtual storage links in the network, and $(L_D + L_S)$ be the union of L_D and L_S . Define a path as a sequence of links without the repetition of head nodes, i.e., with no cycle in the path. Use \mathcal{R}_{LP} to represent the set of paths containing the specific link for the diversion of surplus water, and $\mathcal{R}_{L_D+L_S}$ to represent the set of paths with the final links belong to $(L_D + L_S)$. The mathematical formulation of priority requirement for surplus water diversion can be expressed as:

$$\max [\text{cost}(\mathcal{R}_{L_D+L_S} - \mathcal{R}_{LP})] < \min [\text{cost}(\mathcal{R}_{LP})] \quad (4)$$

where, $(\mathcal{R}_{L_D+L_S} - \mathcal{R}_{LP})$ is the same as $\mathcal{R}_{L_D+L_S}$ but excluding \mathcal{R}_{LP} , cost is a function used to calculate the sum of the cost coefficients of the links in a path, and $\text{cost}(\mathcal{R}_{LP})$ represents the set of total costs for all paths in \mathcal{R}_{LP} . Equation (4) states that the largest cost conducted by paths which do not pass from the trans-basin link is less than the least cost by passing from the trans-basin link. Because the lowest priority should correspond to the largest cost under the framework of NFP, a set of cost coefficients which satisfies this condition should guarantee that the trans-basin link will work only in case of surplus.

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For a total of np_{1a} paths in \mathcal{R}_{LP} where the k th path is represented as $P1a_k$, a Kronecker delta function can be used to represent if $P1a_k$ contains link (i, j) :

$$\forall (i, j) \in L, \delta 1a_k^{(i,j)} = \begin{cases} 1 & \text{if } (i, j) \in P1a_k \\ 0 & \text{otherwise} \end{cases} \quad (5)$$

5 Suppose that $(\mathcal{R}_{L_D+L_S} - \mathcal{R}_{LP})$ contains np_{1b} links and $P1b_k$ represents the k th path in $(\mathcal{R}_{L_D+L_S} - \mathcal{R}_{LP})$. Another Kronecker delta $\delta 1b_k^{(i,j)}$ can be used to represent if $P1b_k$ contains link (i, j) :

$$\forall (i, j) \in L, \delta 1b_k^{(i,j)} = \begin{cases} 1 & \text{if } (i, j) \in P1b_k \\ 0 & \text{otherwise} \end{cases} \quad (6)$$

10 Equation (4) can then be expressed by the following constraints:

$$\sum_{(i,j) \in L} \delta 1a_k^{(i,j)} c_{(i,j)} \geq C_{Min1} \quad k = 1, \dots, np_{1a} \quad (7)$$

$$\sum_{(i,j) \in L} \delta 1b_k^{(i,j)} c_{(i,j)} \leq C_{Max1} \quad k = 1, \dots, np_{1b} \quad (8)$$

$$C_{Max1} + \varepsilon \leq C_{Min1} \quad (9)$$

15 where, $c_{(i,j)}$ is the cost coefficient per unit flow of link (i, j) , C_{Min1} represents the lower bound of the total costs of paths in \mathcal{R}_{LP} , C_{Max1} represents the upper bound of the total costs of paths in $(\mathcal{R}_{L_D+L_S} - \mathcal{R}_{LP})$, and ε is an arbitrary positive integer specified by the user.

3.2 Rule 2: priorities between water usages and reservoir storage

20 The basic framework of water allocation in the water resources system is the priorities between water usages and reservoir storage. The priorities may be defined by water

rights, judicial or legislative actions to protect specific water usages, private agreements between stakeholders or the operating rule curves of reservoirs. Chou and Wu (2011) illustrated the setting of priorities between demands and storage for the operating rule curves commonly adopted in individual reservoir operating systems of Taiwan. The proposed mathematical formulation was as following:

Assume that $(L_D + L_S)$ is the set that consists of all virtual demand and storage links. $(L_D + L_S)(k)$ is the link prioritized k th among $(L_D + L_S)$. Equation (10) prioritizes all virtual demand and storage links that comprise a water supply network as follows:

$$\max\{\text{cost}[\mathcal{R}_{L_D+L_S(k)} - \mathcal{R}_{LP}]\} < \min\{\text{cost}[\mathcal{R}_{L_D+L_S(k+1)} - \mathcal{R}_{LP}]\}, k = 1 \sim m_d + m_s - 1 \quad (10)$$

In Eq. (10), the set $\mathcal{R}_{L_D+L_S(k)}$ consists of all potential flow routes with final link as $L_D + L_S(k)$, \mathcal{R}_{LP} is the same as defined in Eq. (4) of Sect. 3.1; and $m_d + m_s$ represents the number of links in $(L_D + L_S)$. Eq. (10) states that the largest cost among paths to a senior priority demand or storage is less than the least cost conducted by paths to a junior priority water usage. It thus guarantees finding coefficients which projects the defined priorities.

The following constraints can be established from the concept of Eq. (10), derived by a similar process of converting Eq. (4) into Eqs. (7)–(9) as shown in Sect. 3.1.

$$C_{\text{Min}2_k} \leq \sum_{(i,j) \in \mathcal{L}} \delta 2_{k,l}^{(i,j)} c_{(i,j)} \leq C_{\text{Max}2_k} \quad l = 1, \dots, np_{2,k}; k = 1, \dots, m_d + m_s \quad (11)$$

$$C_{\text{Max}2_k} + \varepsilon \leq C_{\text{Min}2_{k+1}} \quad k = 1, \dots, m_d + m_s - 1 \quad (12)$$

where $C_{\text{Max}2_k}$ and $C_{\text{Min}2_k}$ define the feasible range of net conveyance costs for flow paths in $\mathcal{R}_{L_D+L_S(k)} - \mathcal{R}_{LP}$; the Kronecker delta function $\delta 2_{k,l}^{(i,j)}$ indicates whether the l th flow path of $\mathcal{R}_{L_D+L_S(k)} - \mathcal{R}_{LP}$ includes the link (i, j) ; $np_{2,k}$ is the number of paths exist in $\mathcal{R}_{L_D+L_S(k)} - \mathcal{R}_{LP}$, and ε is the same as in Eq. (9), which is used to maintain an interval of costs between consecutive priorities.

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3.3 Rule 3: preferences in water conveyance

Although there are multiple ways to meet a demand, for water the routes with less transmission loss, lower operating costs, and the potential for additional hydro-electric generation are generally preferred. This rule allows users to specify the priorities of water conveyance through paths between two specific nodes. For example, possible paths between the reservoir and demand nodes in Fig. 4 are listed in the sequence of their priorities as follows: (1) A–B–D–E–F–H, (2) A–B–D–G–H, (3) C–D–E–F–H and (4) C–D–G–H.

Suppose that there are np_3 possible paths between the specified source and target nodes. We assume that these paths are arranged in sequence according to their conveyance priorities, i.e., if $P3_k$ represents the k th path, then water conveyance through $P3_k$ should be prior to $P3_{k+1}$. The function $\delta 3_k^{(i,j)}$ indicates whether $P3_k$ includes the link (i, j) . The following constraints can then be established:

$$C_{\text{Min}3_k} \leq \sum_{(i,j) \in L} \delta 3_k^{(i,j)} c_{(i,j)} \leq C_{\text{Max}3_k} \quad k = 1, \dots, np_3 \quad (13)$$

$$C_{\text{Max}3_k} + 1 \leq C_{\text{Min}3_{k+1}} \quad k = 1, \dots, np_3 - 1 \quad (14)$$

where $C_{\text{Max}3_k}$ and $C_{\text{Min}3_k}$ represent the upper and lower bounds of costs associated with the paths between the specified source and target nodes.

3.4 Rule 4: priorities in multi-reservoir storage allocation

The operation of a multi-reservoir system involves allocating water from multiple reservoirs to satisfy the joint demand. The respective priority rankings for carryover storage of each reservoir determine which reservoir should be used first to satisfy demand throughout a multi-reservoir system. For example, Fig. 5 depicts a system with two parallel reservoirs, Reservoirs A and B, which both can provide water to the joint demand. Operating rules of this two-reservoir system dictate that joint demand be supplied by

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allocating water from available sources in the following order: (1) first from Weir C until it has been emptied; (2) then from Reservoir A, provided that its water level is over its lower limit of rule curve; (3) finally, from Reservoir B. Accordingly, the storage components can be listed in the sequence of their associated priorities as: (1) the storage under the lower limit of Reservoir A, (2) the storage of Reservoir B, (3) the storage over the lower limit of Reservoir A and (4) the storage of Weir C.

Assume that $L_S(k)$ represents the k th-priority link in the set of storage links, L_S . The priority constraint for allocating storage in a multi-reservoir system can be expressed as follows:

$$\begin{aligned} & \max[\text{cost}(\mathcal{R}_{L_S(k+1) \rightarrow \text{JD}} - \mathcal{R}_{\text{LP}})] + \max[\text{cost}(\mathcal{R}_{L_S(k)} - \mathcal{R}_{\text{LP}})] < \\ & \min[\text{cost}(\mathcal{R}_{L_S(k) \rightarrow \text{JD}} - \mathcal{R}_{\text{LP}})] + \min[\text{cost}(\mathcal{R}_{L_S(k+1)} - \mathcal{R}_{\text{LP}})] \quad k = 1, \dots, m_s - 1 \end{aligned} \quad (15)$$

where $\mathcal{R}_{L_S(k)}$ is the set of all routes with final link as $L_S(k)$. $\mathcal{R}_{L_S(k) \rightarrow \text{JD}}$ consists of all flow paths that begin at the reservoir, where the link $L_S(k)$ originates, and culminate by supplying joint demand. $(\mathcal{R}_{L_S(k) \rightarrow \text{JD}} - \mathcal{R}_{\text{LP}})$ is the same set after excluding \mathcal{R}_{LP} ; m_s represents the net total of links in L_S . The concept of Eq. (15) is explained as following: suppose that there is one unit of water initially stored in the reservoir for each of the storage links. The water can either be released to satisfy the joint demand or retained in the reservoir to contribute to the associated carryover storage. The left hand side of Eq. (15) represents the largest cost induced by storing water in the senior storage link (index k) and releasing water from the junior storage (index $k + 1$) to supply joint demand. On the other hand, the right hand side represents the least cost induced by storing and releasing water in the converse way. The inequality ensures that a junior storage will release water in a higher priority to supply joint demand.

According to similar process as shown from Eq. (4) to Eqs. (7)–(9), the following constraints can be established:

$$C_{\text{Min}4a_k} \leq \sum_{(i,j) \in L} \delta 4a_{k,l}^{(i,j)} c_{(i,j)} \leq C_{\text{Max}4a_k} \quad l = 1, \dots, \text{np}_{4a,k}; k = 1, \dots, m_s \quad (16)$$

$$C_{\text{Min}4b_k} \leq \sum_{(i,j) \in L} \delta 4b_{k,l}^{(i,j)} c_{(i,j)} \leq C_{\text{Max}4b_k} \quad l = 1, \dots, \text{np}_{4b,k}; k = 1, \dots, m_s \quad (17)$$

$$C_{\text{Max}4a_{k+1}} + C_{\text{Max}4b_k} + \varepsilon \leq C_{\text{Min}4a_k} + C_{\text{Min}4b_{k+1}} \quad k = 1, \dots, m_s - 1 \quad (18)$$

where $C_{\text{Max}4a_k}$ and $C_{\text{Min}4a_k}$ define the feasible range of net conveyance costs for flow paths represented by $(\mathcal{R}_{L_S(k) \rightarrow \text{JD}} - \mathcal{R}_{\text{LP}})$; $C_{\text{Max}4b_k}$ and $C_{\text{Min}4b_k}$ define the feasible range of net conveyance costs for flow paths represented by $(\mathcal{R}_{L_S(k)} - \mathcal{R}_{\text{LP}})$; the functions $\delta 4a_{k,l}^{(i,j)}$ and $\delta 4b_{k,l}^{(i,j)}$ indicate whether the l th flow path of $(\mathcal{R}_{L_S(k) \rightarrow \text{JD}} - \mathcal{R}_{\text{LP}})$ and $(\mathcal{R}_{L_S(k)} - \mathcal{R}_{\text{LP}})$ include the link (i, j) respectively; $\text{np}_{4a,k}$ and $\text{np}_{4b,k}$ is the numbers of paths in $(\mathcal{R}_{L_S(k) \rightarrow \text{JD}} - \mathcal{R}_{\text{LP}})$ and $(\mathcal{R}_{L_S(k)} - \mathcal{R}_{\text{LP}})$ respectively, and ε is the same as in Eqs. (9) and (12).

3.5 Rule 5 (default): minimization of surplus water

The proposed method penalizes any water into the final receiving body by the following requirements:

$$\min[\text{cost}(\mathcal{R}_{L_T})] > 0 \quad (19)$$

$$\max[\text{cost}(\mathcal{R}_{L_D+L_S})] < 0 \quad (20)$$

where, L_T is a set that includes all terminal links originated from the node representing water receiving body; \mathcal{R}_{L_T} is a set that consists of all possible flow paths, each of which has a final link belongs to L_T . Equation (19) states that the least cost by paths which include the virtual terminal link is greater than zero, and Eq. (20) states the largest cost to a virtual demand or storage link is less than zero. In this manner, the NFP algorithm

will then try to allocate unregulated flows to water users, and release spill flows from reservoir only if absolutely necessary to prevent inducing positive cost. The following inequalities can then be established:

$$\sum_{(i,j) \in L} \delta 5_k^{(i,j)} c_{(i,j)} \leq -\varepsilon \quad k = 1, \dots, np_5 \quad (21)$$

$$\sum_{(i,j) \in L} \delta 6_k^{(i,j)} c_{(i,j)} \geq \varepsilon \quad k = 1, \dots, np_6 \quad (22)$$

where, $\delta 5_k^{(i,j)}$ and $\delta 6_k^{(i,j)}$ are Kronecker delta functions to represent whether link (i, j) is in the k th path in $\mathcal{R}_{L_D+L_S}$ and \mathcal{R}_{L_T} , respectively; np_5 is the number of paths in $\mathcal{R}_{L_D+L_S}$ and np_6 denote the number of paths in \mathcal{R}_{L_T} .

Furthermore, we assume that the cost coefficients of all links other than demand, storage and terminal are greater than 0:

$$c_{(i,j)} \geq 0 \text{ for all } (i, j) \in (L - L_D - L_S - L_T) \quad (23)$$

3.6 Linear programming for determining cost coefficients

The constraints Eqs. (7)–(9), (11)–(14), (16)–(18) and (21)–(23) define the feasible region for cost coefficients. Linear programming (LP) can be employed to solve the problem, by coupling the constraints with the following objective function:

$$\text{Minimize} \quad \sum_{(i,j) \in (L - L_D - L_S - L_T)} c_{(i,j)} \quad (24)$$

Equation (24) will keep the costs of links other than storages, demands and terminals to be zero as long as feasible. Only a few links will be assigned with nonzero costs when absolutely necessary. For example, rule 3 may require assignment of nonzero costs on particular links to discourage flow through routes with high loss rates. The assigned cost will then be minimized to be +1 based on the objective function and Eqs. (13) and

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(14). Under this setting, the allocation of water will be primarily dictated by the costs of virtual links, while the minor costs on particular non-virtual links guide local flow conveyance.

3.7 Determination of values of the Kronecker delta functions

5 The Kronecker delta functions for each link as described in Sects. 3.1–3.5, can be established using the path enumeration algorithm of Kroft (1967). Here a path refers to a sequence of nodes such that from each node there is a link to the next node in the sequence. Furthermore, there should be no cycle, i.e., repetition of nodes, in the path. Repeated identifying possible paths between different associate nodes can help determining the values of the above Kronecker delta functions. The computing
10 procedure of Kroft's algorithm is provided in Appendix A.

4 Case study

The proposed method was applied to determine cost coefficients of NFP model for simulating the joint water allocation of the Hsintein and Tahan Rivers water resources system of northern Taiwan. This case study simulates projected conditions of the
15 given system in 2021. The Feitsui Reservoir, with an effective storage capacity of $336 \times 10^6 \text{ m}^3$, is located on the Peishih Creek, one of the two major upstream tributaries of Hsintein River. It serves mainly to supply the demand for domestic water in Taipei (TP) district. Downstream from the confluence of Peishih and Nanshih Creeks are the Cihukeng, Chihtan, and Chintan Weirs, which serve to regulate upstream flow and raise the water level for the diversion of water into three treatment plants. Cihukeng
20 Weir also serves to raise the water level to divert flow into the off-channel Cihukeng hydropower plant through a man-made canal. The tail-water from the hydropower plant is then diverted to the downstream Chintan Weir.

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The other river in the joint operating system, the Tahan River, has its own reservoir, the Shihmen Reservoir. The capacity of Shihmen Reservoir is $215 \times 10^6 \text{ m}^3$ according to the survey in 2011. It was designed for irrigation, hydropower generation, public water supply, and flood moderation. Downstream from the Shihmen Reservoir are its afterbay and the Yuanshan Weirs, which serve to regulate the reservoir release. The Shanshia Pumping Station on the Shanshia River, which is a tributary of the Tahan River, can also support public water supply in this region.

The primary demands for water in the Shihmen Reservoir system are irrigational and the public demand of southern, northern Taoyuan (TY) and Pan-Hsin (PH) districts. Pingcheng, Longtang, and Shihmen Treatment Plants withdraw raw water from the Shihmen Reservoir and supply the southern TY district. The northern TY district is supplied by Danan Treatment Plant, which withdraws raw water from the Yuanshan Weir.

The Tahan River and Hsintien River systems jointly supply the public demand from PH district. The Panhsin Treatment Plant receives raw water from both the Yuanshan Weir and Shanshia Pumping Station. The Hsintien River system will provide a maximum of $1.01 \text{ million m}^3 \text{ day}^{-1}$ of treated water to the PH district after year 2016 through the under constructed trans-basin pipeline of the “Pan-Hsin Water Supply Improvement Plan, Phase II” (PH-Phase II).

There is also a trans-basin raw water diversion project being planned in Nanshih Creek in the upstream of Hsintien River, which will focus on building a diversion weir, called Limogan Weir, and a trans-basin tunnel upstream of Nanshih Creek. It aims to divert surplus water from Nanshih Creek to an upper section of Shanshia River, thereby increasing the water utilization efficiency through joint operations. The network of this water resources system is depicted in Fig. 6.

4.1 Priority requirement for trans-basin water diversion

The diversion link of Limogan Weir is specified as the last priority link of rule 1, because it should only divert surplus water from Nanshih Creek. This setting ensures that the

trans-basin tunnel will not withdraw water originally intended to meet the demands of the Hsintein River system.

4.2 Priority requirement for reservoir operating rule curves

The rule curves of Feitsui Reservoir include the severe limit (SL), lower limit (LL), middle limit (ML) and upper limit (UL). The Feitsui Reservoir Administration specifies the following conditions for operation in 2021 (Chou and Wu, 2011):

1. While reservoir water level is below the SL, it only has to provide 80% of TP demand.
2. While reservoir level is above the SL but below the LL, it only has to provide 80% of TP and PH demands.
3. 100% of TP and PH demands should be satisfied while the reservoir level is above the LL.
4. While the reservoir level is raised to range between the ML and UL, extra water may be released for peak-hours hydropower generation.
5. Sufficient water should be released to support full-capacity hydropower generation while reservoir level exceeds the UL.

Figure 7, which identifies a variable for each virtual link, illustrates the determination of storage and demand links with respect to the five operating rules delineated above. The codes of virtual links associated with the operating rule curves of Feitsui Reservoir are listed in the sequence of their associated priorities as following: (1) $D_{80\%}^{TP}$, (2) S_{SL}^F , (3) $D_{80\%}^{PH}$, (4) S_{LL}^F , (5) $D_{100\%}^{TP}$ and $D_{100\%}^{PH}$, (6) S_{ML}^F , (7) D_P^{F-HP} , (8) S_{UL}^F , (9) D_F^{F-HP} , (10) S_{FC}^F , and (11) S^{F-W} .

Shihmen Reservoir operating rule curves must comply with the following criteria:

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The first condition in the above rules essentially means that the weirs are at the last priority to store water, because their storage is always consumed first. The logic of whether supplying water to the joint demand can be used to compare and determine the priorities of different storage components in Feitsui and Shihmen Reservoirs. For instance, water stored in the Feitsui Reservoir under the SL should be senior to all Shihmen Reservoir storage, because the third condition prevents Feitsui from supplying PH when its storage falls below the SL. Aside from the SL, the priorities of other storage of Feitsui should be junior to the storage of Shihmen Reservoir, because the Feitsui Reservoir should be the default water source for PH demand during normal conditions. According to these characteristics, the codes of virtual storage links are listed in the order of their associated priorities as following: (4) S_{SL}^F , (2) S_{SL}^S , (3) S_{LL}^S , (4) S_{UL}^S , (5) S_{FC}^S , (6) S_{LL}^F , (7) S_{ML}^F , (8) S_{UL}^F , (9) S_{FC}^F , (10) S^{F-W} and S^{S-W} .

4.4 Result and discussion

Figure 8, which applies a value of 10 to the variable ε , quantifies the cost coefficients that follow from the priorities specified in the previous sections. Figure 8 shows a cost-coefficient value of -370 for the SL link in Feitsui Reservoir. This value is lower than the coefficient for satisfying PH demand. Operating rules thus require that Feitsui water supplies only 80 % of TP demand while its water level is unable to attain the SL. Under these conditions, the alternate supply source, the Shihmen Reservoir, will supply 80 % of the PH district demand. The cost of supplying the remaining PH demand would be -190 ($= -270 + 80$), which is larger than the cost of simply storing that water in the storage facilities in the Tahan River system.

Assume that both the Feitsui and Shihmen Reservoirs each have one unit of water and that the Feitsui water level is higher than its SL. If the water from Shihmen Reservoir is allocated to supply 80 % of the joint demand, the other one unit of water can be stored in Feitsui Reservoir to achieve the minimum unit cost of -280 . On the other hand, the unit cost of supplying joint demand with Feitsui Reservoir water (and thus

retaining Shihmen Reservoir storage) is only -290 . Hence, minimum-cost NFP-based water allocation ensures that the joint demand will be satisfied by the Feitsui storage in a higher priority, provided that its water level exceeds the SL.

The trans-basin diversion link in Fig. 8 has a positive cost coefficient of $+180$. The minimum total cost of paths through this link is -180 , which is the sum of the costs of the diversion link and the highest priority demand in the Tahan River system. The lowest priority in the Hsintein River system is storage in weirs, each of which has a cost of -210 . Thus the model will not allocate water from Nanshih Creek unless all of the weirs of Hsintein River are full. In other words, the trans-basin tunnel will only divert surplus water from Nanshih Creek.

In the joint operation of Fig. 8, Feitsui Reservoir is the primary regular source and Shihmen Reservoir provides the backup source for PH district. Another operating strategy is to maintain the storage of these two reservoirs at the same intervals as their individual rule curves. For instance, the storage zones between the LL and SL of both reservoirs would share the same priority. Based on this concept of storage balancing joint operation, the virtual storage links are listed in the order of their associated priorities as following: (1) S_{SL}^F , (2) S_{SL}^S , (3) S_{LL}^F and S_{LL}^S , (4) S_{ML}^F and S_{UL}^S , (5) S_{UL}^F , (6) S_{FC}^F and S_{FC}^S , (7) S^{F-W} and S^{S-W} . Under this setting, the reservoir with the higher storage is charged with supplying the joint demand to maintain the storage of the two reservoirs in the same interval. The analyzed cost coefficients based on the storage balancing joint operation are illustrated in Fig. 9.

Based on Fig. 9, possible joint operating scenarios include the following:

1. Any water over the UL in the Shihmen Reservoir will be allocated to the PH district to meet 80 % of its full demand, provided that Feitsui level does not exceed its UL.
2. When the level of Shihmen Reservoir is between its UL and LL, the Feitsui Reservoir will satisfy the joint demand as long as its level exceeds the ML. However, if Feitsui storage is unable to attain the LL, then water from the Shihmen Reservoir will be allocated to meet 80 % of PH district demand in a higher priority.

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3. Provided that the Shihmen Reservoir water level ranges between the SL and LL and the water level in the Feitsui Reservoir exceeds the LL, water from Feitsui Reservoir will be allocated to PH district demand. Shihmen Reservoir water will be released to independently satisfy 80 % of joint demand only when the Feitsui water level drops below its SL.

4. When the Shihmen Reservoir water level drops below the SL, the Feitsui Reservoir will independently fulfill PH district demand provided that its own water level exceeds the SL. If the Feitsui Reservoir water level is below the SL, then Shihmen Reservoir water will be allocated to ensure that 80 % of PH demand is satisfied.

In addition to the allocation priorities defined by operating rule curves and joint operating rules, preference for flow through hydropower plant can be simulated by directly assigning a negative unit cost to the links connecting to the run-of-river or reservoir hydro plants to encourage associated flows. Because the interval of costs between consecutive priorities of demands or storage is set as 10, this unit cost will not impair the priority requirements by the above rules, as long as the accumulations of minor costs to demands or reservoirs are within the range between -10 to 10 .

5 A pruned analyzing procedure

In the aforementioned analyzing procedure, the bulk of the computational load is expended on network path enumeration analysis. For a complete network, in which every pair of distinct nodes is connected by a unique link (as an extreme example), if there are n nodes in the network, then the number of links will be $2 \times C_2^n$, resulting in $\sum_{i=1}^{n-2} C_i^{n-2}$ paths between any two distinct nodes. This means that the number of paths would grow exponentially with an increase in the number of nodes for such a dense network. The enormous number of resulting paths would not only require considerable time for enumeration, but would also expand the size of the subsequent LP problem.

Path enumeration is required because the cost coefficient of every link is assumed to be unknown in the default condition. If additional conditions could be included, such as the assignment of only a few links with nonzero costs and the costs of other links set at 0, then a simpler analyzing procedure could be employed to reduce the required computational load.

Using $G(N, L)$ to present the under analyzing network, which is defined by a set N of n nodes and a set L of m links. Suppose that there are m_P non-virtual links within L which are assigned with nonzero costs and $m_P < m$. Defining L_P as the set containing these specified links, N_{PT} and N_{PH} as the sets of tail and head nodes of links in L_P , respectively. Defining $(N_D + N_S + N_T)$ as the set which contains all nodes which represent demands, reservoirs or final water receiving bodies in N , and $(L_D + L_S + L_T)$ as the set of demand, storage or terminal links. Then the cost determining procedure can be simplified as below:

1. From each of the nodes which convey inflow into the system, using the depth first search (DFS) algorithm to identify the downstream reachable nodes in $G(N, L - L_P)$. The detail of DFS algorithm can be found in Ahuja et al. (1993).
2. A fictitious node, denoted as node f , is created. If node $i \in (N_D + N_S + N_T)$ is identified to be reachable from inflow nodes in the previous step, then a fictitious link (f, i) is created. This fictitious link serves to replace all paths to node i which consist of only links with zero cost in $G(N, L)$. Define L_F as the set which contains these fictitious links.
3. Using DFS to identify the downstream reachable nodes in $G(N, L - L_P)$ from the head node of each link in L_P .
4. Suppose that link (i, j) belongs to L_P and node k belongs to either N_{PT} or $(N_D + N_S + N_T)$. If k can be reached from j in $G(N, L - L_P)$, then a fictitious link (j, k) is created and added into L_F . These fictitious links represent the connectivity between links with nonzero costs.

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5. Establish a reduced network $G'(N', L')$, in which N' is the union of N_{PT} , N_{PH} , $(N_D + N_S + N_T)$ and node f , and L' is the union of L_P , L_F and $(L_D + L_S + L_T)$.
6. The same procedure described in Sect. 3 can be followed to determine the cost coefficients of links in L_P and $(L_D + L_S + L_T)$, except that $G(N, L)$ is replaced by $G'(N', L')$.

The above procedure takes advantage of the fact that total costs of a path are determined only by the links with nonzero cost coefficients in the path. Thus the enumeration of paths containing all links in L can be reduced to only enumerating feasible combinations of links in L_P and $(L_D + L_S + L_T)$. Because DFS is a basic algorithm with worst case complexity as only $O(m)$, the reduced network G' can be efficiently established from the original network G . The scale of G' should be much less than G because typically $m_P \ll m$. Thus enumerating paths in G' will require much less computational time and the size of the consequent LP problem can be greatly reduced.

This pruned procedure was employed to finally evaluate the two illustrative problems of Sect. 4. In these final evaluations, only the transbasin diversion link and the links connecting to 20 % joint demand are specified with nonzero costs. The original system was pruned into a reduced network similar to the schematic shown in Fig. 8. For each problem, the number of constraints in the LP formulation was reduced from the original 3227 to only 486. The analyzing results using the pruned procedure were identical to those as illustrated in Figs. 8 and 9.

6 Conclusions

This paper presents a methodology for determining the cost coefficients of the objective function of an NFP-based model for simulating river/reservoir system operations and associated water allocation. This issue is of great importance because adequate simulation of water allocation rules is the key to successful implementations of any water allocation models. Among the many studies on water allocation within reservoir/river

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systems in the literature, this paper is one of the very few which explicitly study how to appropriately set up the objective function for a NFP-based simulation model. The assignment of cost coefficients was usually performed intuitively, as practices of art by researchers. This issue is treated by a scientific manner in this paper, with systematic presentations of representative allocation rules encountered in real world applications. A general procedure is proposed to solve the problem. Although additional analyzing efforts are required, the obtained coefficients guarantee that the allocation requirements are satisfied. Thus the possibly time-consuming trial and error process to check the validity of assigned costs can be avoided.

For an experienced analyst, the adequate assignment of cost coefficients may be done without any preprocessing procedure. But this is not necessarily true for practitioners with less theoretical background, especially when they are dealing with systems of complex networks and allocation rules. For a system consists of multiple reservoirs and trans-basin diverting tunnel or pipe as shown in the case study, achieving surplus water diversion and storage allocation inevitably requires assigning nonzero costs on internal links other than demands or storage. This practice is not as straightforward as for systems with simple allocation priorities on demands or reservoir storage. Even for an experienced practitioner, there is always a chance of wrong assignment of costs due to the variety and complexity of water resources systems. The proposed procedure can also serve to validate the effectiveness of the intuitively assigned costs.

Furthermore, if the links to be assigned with nonzero costs can be specified in advance, a simpler procedure can be employed to reduce the computing effort of preprocessing analysis. This procedure prunes the original system into a reduced network. Thus the time required to establish and solve the constraints of cost coefficients can be greatly shortened, which further increases the merit of the proposed method.

Appendix A

Kroft's path enumeration algorithm

Kroft's algorithm aims to find all paths that connect a source node s and a target node t . It uses a stack (a data structure that stores elements in a last in first out manner) to store the path that has been built by the algorithm thus far. The recursive procedure is as follows:

1. Upon entering the procedure, the element at the top of the stack, say node i , is selected. The procedure searches for the first outgoing link of node i , say link (i, j) of which the head node (node j) is not already on the stack.
2. If a node j is found, then it is added to the stack.
 - (a) If $j = t$, then the elements in the stack represent a new path from s to t . The path is output and j is deleted from the stack.
 - (b) If $j \neq t$, then the above steps are repeated recursively.
3. If the algorithm is unable to find a link (i, j) for which node j is not already on the stack, node i is deleted from the stack. The above steps are then repeated recursively.

When the above procedure is called for the first time, only source node s is initially contained within the stack in the algorithm. The algorithm terminates when the stack is empty.

While implementing Kroft's algorithm, a number of programming techniques similar to a common DFS algorithm are also used. For instance, an adjacency list may be used to store the network structure. The adjacency list for node i , denoted as $A(i)$, is defined as the set of links emanating from node i . A data structure comprising a singly linked list is used to establish an adjacency list for every node in the network. An array of pointer variables, known as $\text{first}(i)$, is used to point to the first link of $A(i)$ for each

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i that belongs to \mathbf{N} . Another pointer array, $\text{currentarc}(i)$, is also used to store the next candidate link that the algorithm is going to examine from node i . More details related to these skills and their implementation for a DFS algorithm can be found in Ahuja et al. (1993).

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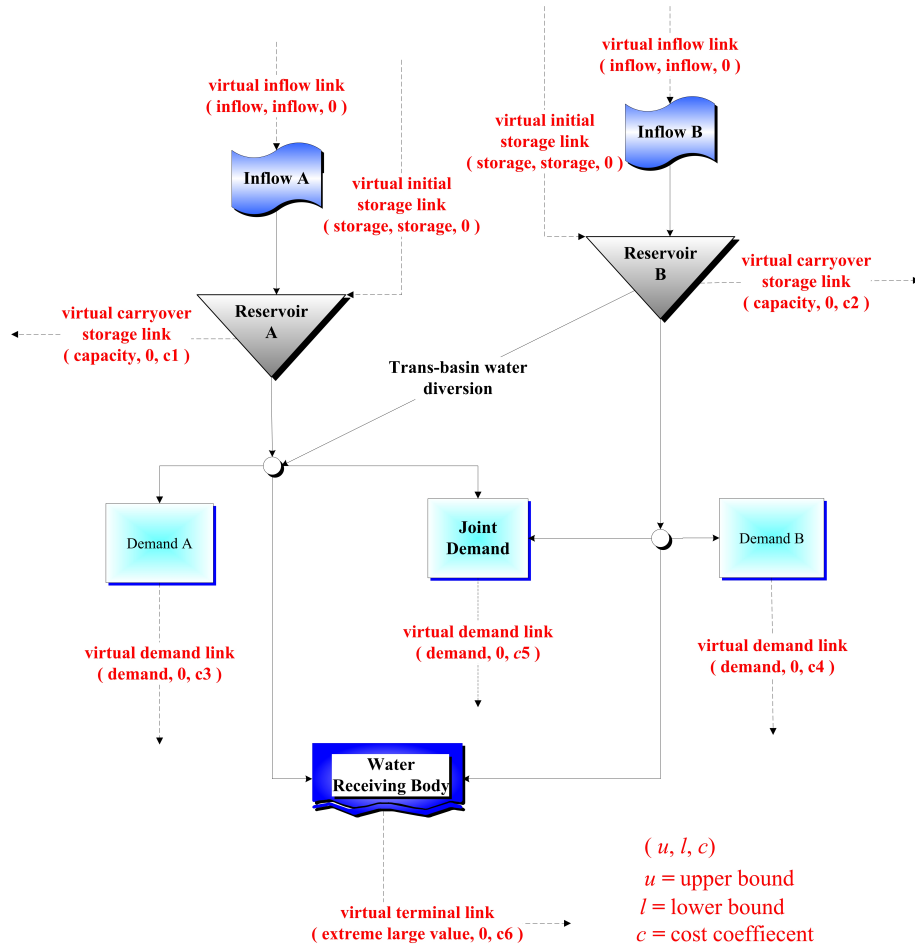


Fig. 1. Network structure of water resources system.

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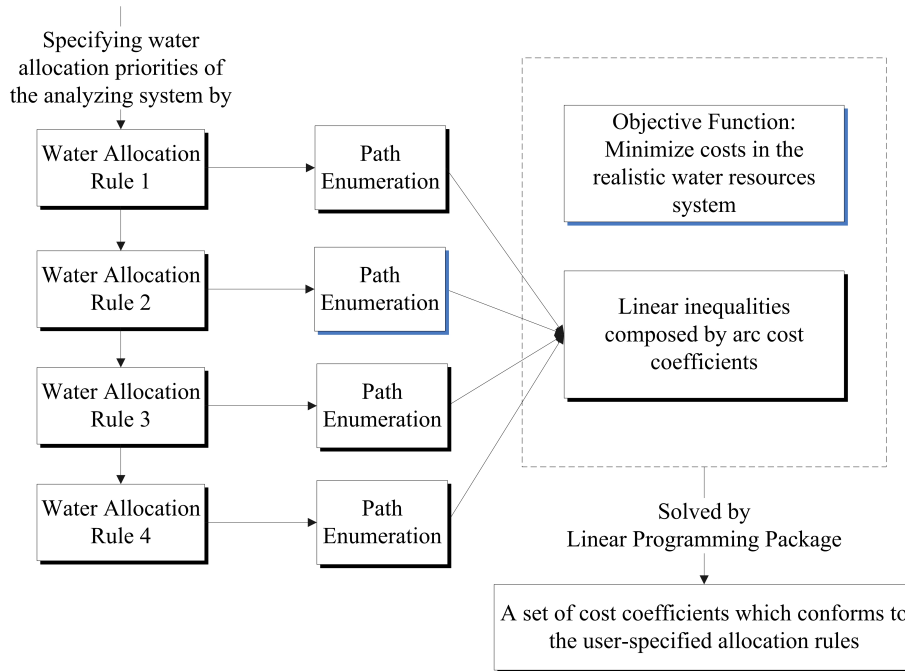


Fig. 2. Cost determining procedure proposed in this study.

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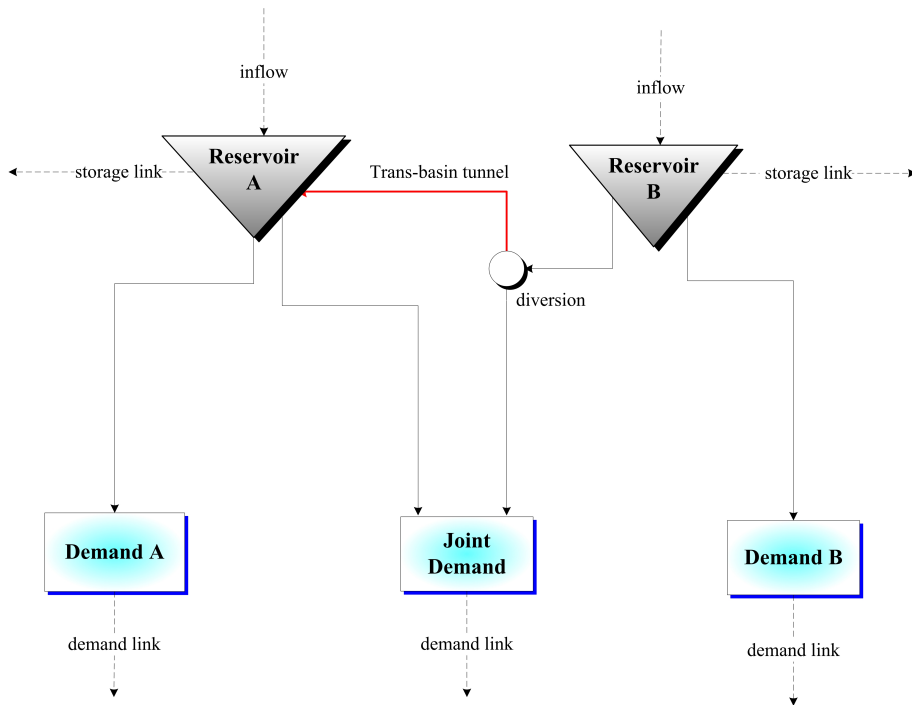


Fig. 3. Example of trans-basin water diversion.

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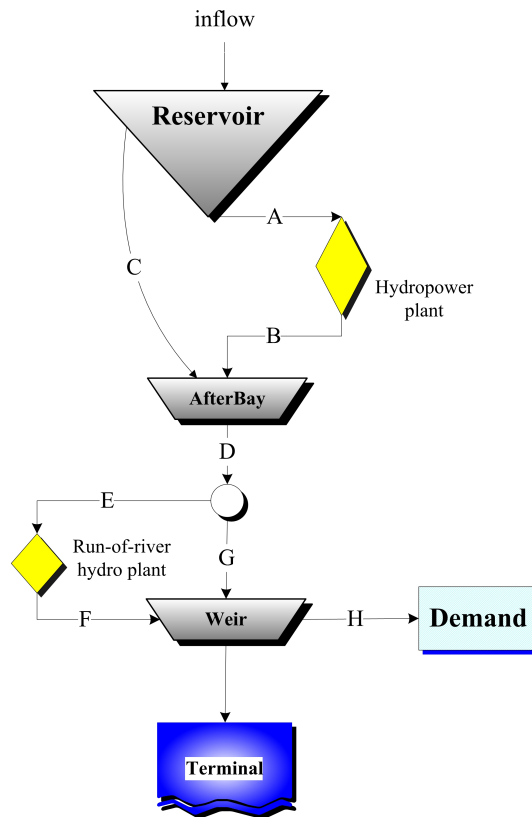


Fig. 4. Water supply routes.

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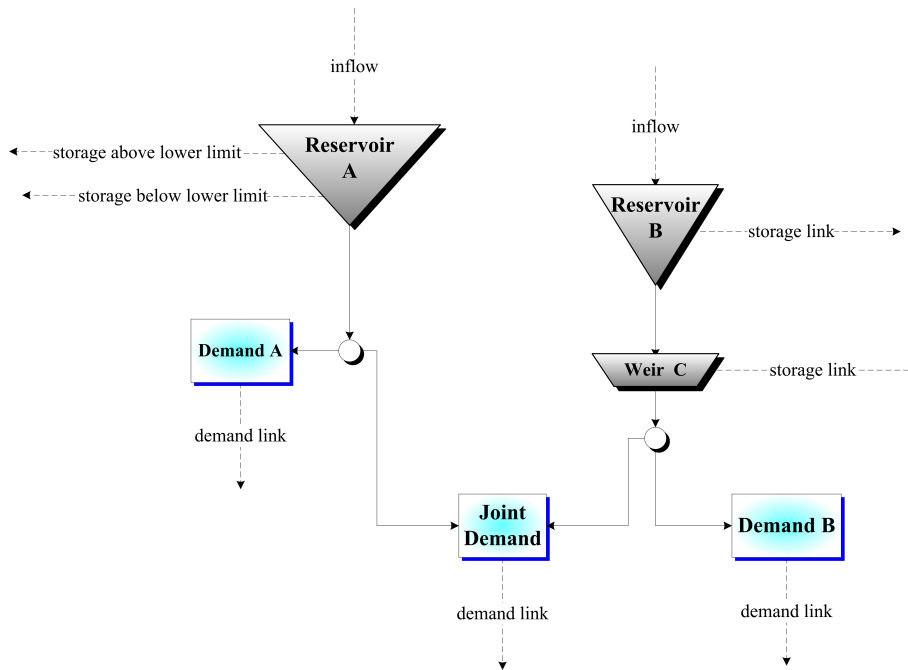


Fig. 5. Example of a multi-reservoir system.

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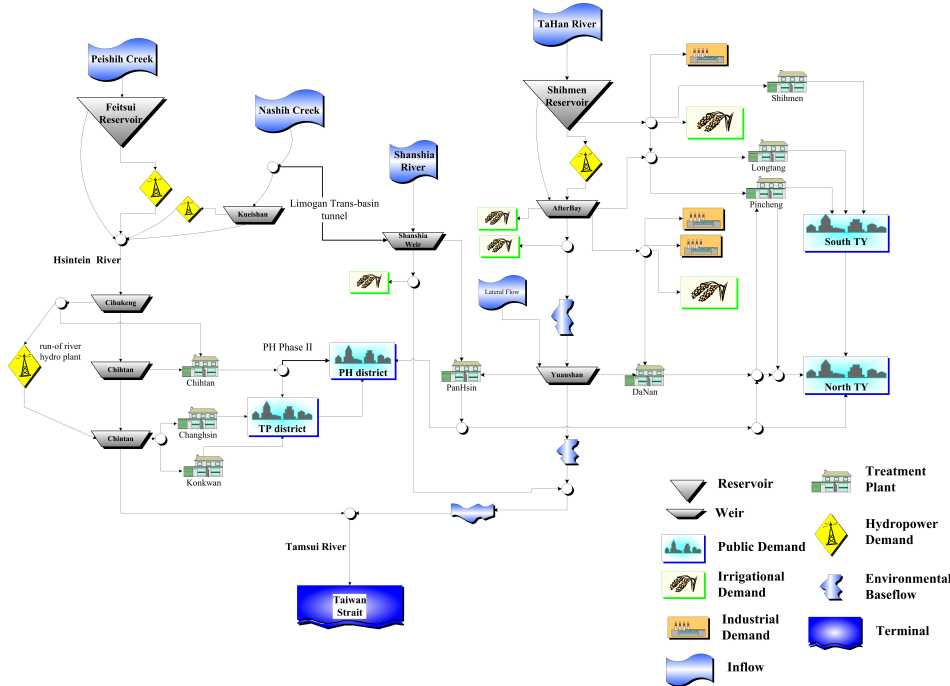


Fig. 6. Joint operation system of Feitsui and Shihmen Reservoirs.

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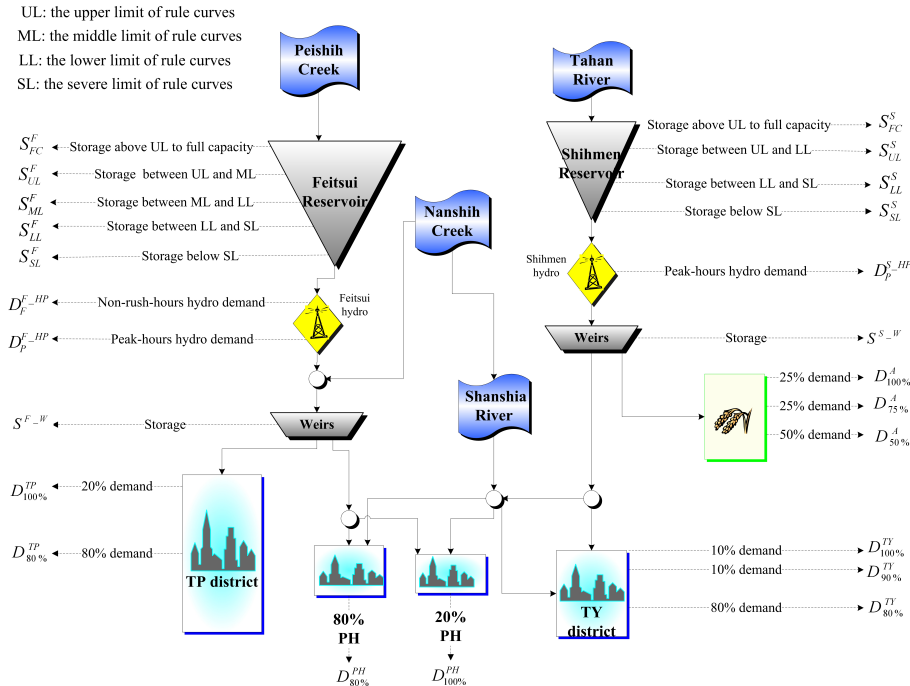


Fig. 7. Virtual demand and storage links of the joint operation system of Feitsui and Shihmen Reservoirs.

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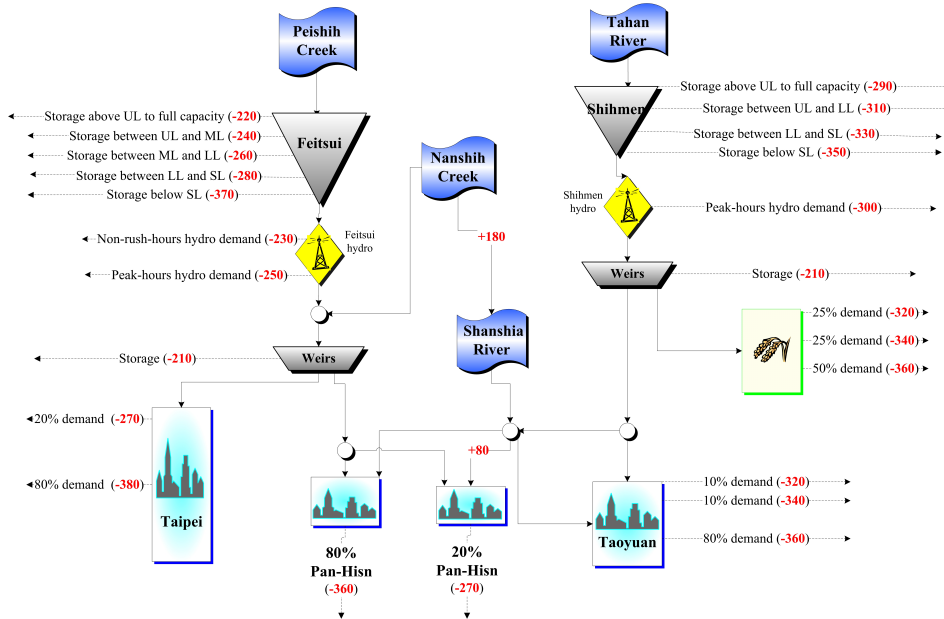


Fig. 8. Assigned coefficients based on conditions specified in Sects. 4.1–4.3.

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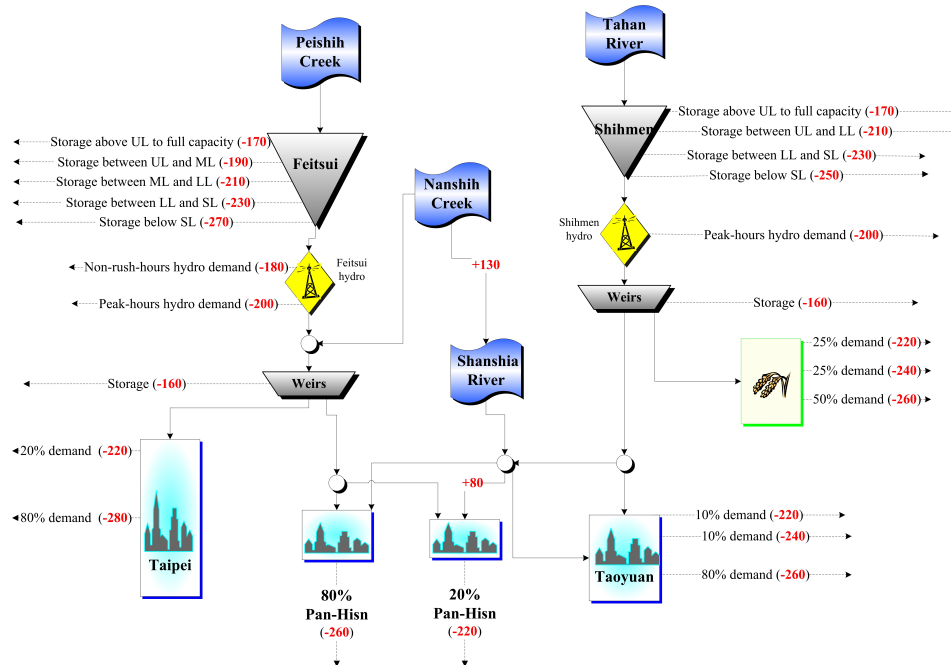


Fig. 9. Cost coefficients for storage balancing of two reservoirs.