

**Alternative in-stream  
denitrification  
equation for the  
INCA-N model**

J. R. Etheridge et al.

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# Technical Note: Alternative in-stream denitrification equation for the INCA-N model

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[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)

## Abstract

The Integrated Catchment model for Nitrogen (INCA-N) is a semi-distributed, process based model that has been used to model the impacts of land use, climate, and land management changes on hydrology and nitrogen loading. An observed problem with the INCA-N model is reproducing low nitrate-nitrogen concentrations during the summer growing season in some catchments. In this study, the current equation used to simulate the rate of in-stream denitrification was replaced with an alternate equation that uses a mass transfer coefficient and the stream bottom area. The results of simulating in-stream denitrification using the two different methods were compared for a 9 month simulation period of the Yläneenjoki catchment in Finland. The alternate equation (Nash–Sutcliffe efficiency = 0.59) simulated concentrations during the growing season that were closer to the observed concentrations than the current equation (Nash–Sutcliffe efficiency = 0.47). The results of this work promote the incorporation of the alternate equation into the model for further testing.

## 1 Introduction

Catchment scale nutrient models can be used to predict the effect of changing land use and climate on nutrient export. The Integrated Catchment model for Nitrogen (INCA-N) is a catchment scale model that simulates both hydrology and mineral nitrogen processes (Wade et al., 2002; Whitehead et al., 1998). INCA-N has been applied to many European catchments, but one problem has been the overestimation of nitrate-nitrogen ( $\text{NO}_3\text{-N}$ ) concentrations during the summer growing season (Jarvie et al., 2002; Rankinen et al., 2006). It is assumed that the current equations used in INCA-N to model in-stream denitrification also take into account other retention mechanisms (O’Shea and Wade, 2009), but other results show that a retention process such as macrophyte uptake is not accurately represented by the current equations for in-stream denitrification (Jarvie et al., 2002; Rankinen et al., 2006, 2013). There is also the potential for the

HESSD

10, 14557–14569, 2013

### Alternative in-stream denitrification equation for the INCA-N model

J. R. Etheridge et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

overestimation of NO<sub>3</sub>-N concentrations by the model caused by inaccuracies in the mass of nitrogen added to the stream through groundwater flow (Wade et al., 2006, 2008).

Birgand et al. (2007) proposed the use of a mass transfer coefficient ( $\rho$ ) to quantify the in-stream NO<sub>3</sub>-N retention in their extensive review of in-stream denitrification in agricultural catchments. The mass transfer coefficient multiplied by the NO<sub>3</sub>-N concentration corresponds to the mass of nitrogen that would be removed from the water above a certain area of stream bed during a defined period of time. Birgand et al. (2007) recommended that the mass transfer coefficient be used in streams with NO<sub>3</sub>-N concentrations above 1 mgL<sup>-1</sup> based on the premise that above this threshold, the concentration gradient would be in a downward direction in accordance with the mass transfer coefficient theoretical application. The goal of this work was to test the equations proposed by Birgand et al. (2007) to determine their effectiveness in improving the INCA-N simulation of in-stream NO<sub>3</sub>-N concentrations in the growing season of temperate and boreal climates.

## 2 Methods

### 2.1 In-stream mass balance of NO<sub>3</sub>-N as implemented in the INCA-N model

The INCA-N model is a dynamic model that uses a mass balance approach to track the movement of mineral nitrogen in a catchment (Wade et al., 2002; Whitehead et al., 1998). Wade et al. (2002) described the equations for in-stream denitrification that have been used in the model since version 1.6. INCA-N model version 1.11.10 was used in this study.

Equation (1) shows how the mass of nitrogen removed through in-stream denitrification is calculated in the INCA-N model:

$$m_{\text{INCA}} = \frac{R_n C_{1,t-1} V}{1000} \quad (1)$$

# HESSD

10, 14557–14569, 2013

## Alternative in-stream denitrification equation for the INCA-N model

J. R. Etheridge et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion







**Alternative in-stream denitrification equation for the INCA-N model**

J. R. Etheridge et al.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

of the model was calibrated such that the in-stream nutrient concentrations followed the dynamics of the observed concentrations and were of similar magnitude. This was done by adjusting the nutrient process rates in the model. Data available related to nitrogen process rates ranging from fertilizer application data to rates of denitrification measured experimentally were used to reduce uncertainty in model results. More details about the Yläneenjoki Catchment and the model calibration can be found in Etheridge et al. (2013).

The in-stream denitrification and nitrification are the final two processes that alter nitrogen in the INCA-N model, so it was possible to change the in-stream denitrification calculations without changing the results from any other portion of the model. The order of calculations in INCA-N allowed the alternate equation calculations to be completed using a spreadsheet instead of altering the model code. Simulations with the alternate in-stream denitrification equation were done using Excel 2007 (Microsoft, Redmond, WA, USA). Equation 3 is the in-stream mass balance equation for  $\text{NO}_3\text{-N}$  in the model. The input mass of  $\text{NO}_3\text{-N}$  ( $m_{\text{in}}$ ), the reach discharge ( $Q$ ), the reach volume ( $V$ ), and the mass of nitrogen that is nitrified in the reach are all outputs of the model. These model outputs were taken directly from the calibrated model and were not altered in this work. The primary change that was made was replacing  $m_{\text{INCA}}$  with  $m_{\text{alt}}$  in Eq. (3), which changes the concentration of  $\text{NO}_3\text{-N}$  in the stream.

To make the calculations using the alternate equation, the stream bottom area ( $A$ ) of the modeled reach was estimated using ArcGIS (ESRI, Redlands, CA, USA). The main sources of data were a raster map (1 m resolution) of all of the water areas in Finland and a map showing the streamline of the modeled reach. A buffer was created around the modeled streamline using the analysis tools in ArcGIS. All of the water area from the raster map located within this buffer was considered the stream bottom area input to the model. The stream bottom area used in this simulation is  $20\,000\text{ m}^2$ . This method may overestimate the stream bottom area of the primary reach as it includes both the stream bottom and the banks in the projected area. This error was considered reasonable because the entire stream bottom in the catchment was not included, but







# HESSD

10, 14557–14569, 2013

## Alternative in-stream denitrification equation for the INCA-N model

J. R. Etheridge et al.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Using the alternate equation improved the goodness-of-fit of the modeled results when compared to the observed concentrations. The original INCA-N equation produced a  $R^2$  value of 0.52 and a NS of 0.47 when comparing the observed  $\text{NO}_3\text{-N}$  concentrations to the simulated concentrations. The alternate equation using the mass transfer coefficient produced 0.59 for both the  $R^2$  and NS values. The improved goodness-of-fit values show the improved estimation of  $\text{NO}_3\text{-N}$  concentrations during the summer growing season by the alternate equation.

The rate of in-stream denitrification in the INCA-N model was  $0.145 \text{ day}^{-1}$ . This resulted in a total nitrogen removal due to in-stream denitrification of 2600 kg for the 9 month modeling period. This was equivalent to 17 % of the N that entered the stream being retained by in-stream processes. A mass transfer coefficient of  $0.4 \text{ m day}^{-1}$  was used in the alternate equation as it produced the best results through calibration. The 9 month nitrogen removal via in-stream denitrification was 2100 kg or 14 % of the total N that entered the stream for the alternate equation. The mass of nitrogen removed through denitrification was lower using the alternate equation because it did not simulate as much nitrogen removal during periods of high flow as can be seen by the higher  $\text{NO}_3\text{-N}$  concentrations at the end of the simulation period. The lower in-stream retention simulated by the alternate equation was closer to values of between 5 and 15 % that have been estimated in Finnish catchments (Lepistö et al., 2006; Martikainen et al., unpublished). The mass transfer coefficient of  $0.4 \text{ m day}^{-1}$  used in this model application was within the range of plausible values based on the review by Birgand et al. (2007), though most of the values in the review were below  $0.3 \text{ m day}^{-1}$ . One potential reason the mass transfer coefficient was higher in the model application than in field experiments was an underestimate of the stream bottom area. Recall, the stream bottom area was estimated only for the main reach modeled in INCA-N. It did not include the entire stream bottom area in the whole catchment. In-stream denitrification was occurring throughout the catchment in the many streams and drainage ditches that feed the main river channel. An increased stream bottom area would have reduced the mass transfer coefficient and produced similar results in the model. The assumption of a constant

stream bottom area did not cause extreme peaks in  $\text{NO}_3\text{-N}$  concentrations during periods of high flow or extremely low  $\text{NO}_3\text{-N}$  concentrations during periods of low flow in the model calibration (Fig. 1), so this assumption appeared to be acceptable.

Using the alternate equation in INCA-N may improve the modeling results, but may not be the best representation of the natural processes that are occurring. It was possible that the overestimation of  $\text{NO}_3\text{-N}$  concentrations during the low flow summer period was also influenced by the groundwater storage of  $\text{NO}_3\text{-N}$  being modeled incorrectly (Wade et al., 2006, 2008). Further investigation is required into the influence of groundwater flow on in-stream  $\text{NO}_3\text{-N}$  concentrations and how this is modeled.

## 4 Conclusions

Although Birgand et al. (2007) recommended using the mass transfer coefficient when the  $\text{NO}_3\text{-N}$  concentrations were greater than  $1 \text{ mgL}^{-1}$ , it appears that the alternate equation, using the mass transfer coefficient, simulates in-stream denitrification during low flow and low  $\text{NO}_3\text{-N}$  concentration conditions better than the current equations used in the INCA-N model. It was possible that a downward flux of  $\text{NO}_3\text{-N}$  continued to occur at concentrations below  $0.5 \text{ mgL}^{-1}$  and the alternate equation was still valid in this catchment. The impact of using the alternate equation during periods of higher flow and concentrations above  $1 \text{ mgL}^{-1}$  needs further evaluation in catchments that have more observation points.

An added input that is not easily defined, is not generally thought of as a model improvement. One drawback of using the mass transfer coefficient alternate equation in the INCA-N model is it requires an added input of stream bottom area. An improved simulation of in-stream  $\text{NO}_3\text{-N}$  retention during the summer growing season should promote the addition of model complexity. Using such a short period of time to test the use of the proposed in-stream denitrification equation is not as accurate as doing a multiple year calibration in the model, but this work provides evidence that the mass

# HESSD

10, 14557–14569, 2013

## Alternative in-stream denitrification equation for the INCA-N model

J. R. Etheridge et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

transfer coefficient equations should be considered as an alternate method of modeling the in-stream denitrification in the INCA-N model.

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## Alternative in-stream denitrification equation for the INCA-N model

J. R. Etheridge et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



**Alternative in-stream denitrification equation for the INCA-N model**

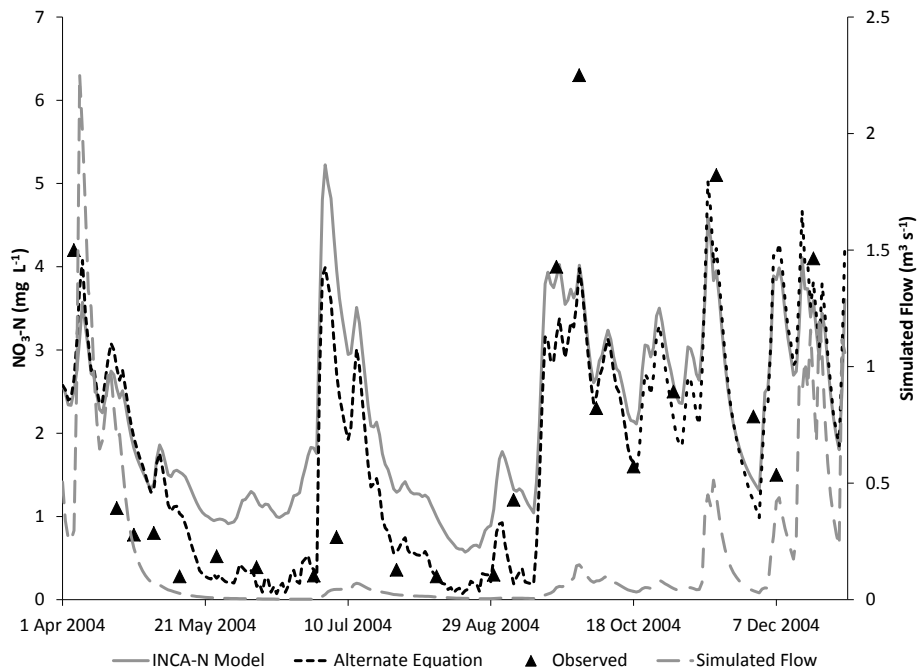
J. R. Etheridge et al.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

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## Alternative in-stream denitrification equation for the INCA-N model

J. R. Etheridge et al.



**Fig. 1.** Graph comparing the INCA-N model results to the results with the alternate equation.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion