A New Framework for Resolving Conflicts over Trans-boundary Rivers Using Bankruptcy Methods

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3 Abstract

4 A novel bankruptcy approach is proposed for resolving trans-boundary rivers conflicts in which 5 the total water demand or claim of the riparian parties is more than the available water. 6 Bankruptcy solution methods can allocate the available water to the conflicting parties with 7 respect to their claims. Four commonly used bankruptcy methods in the economic literature are 8 used here to develop new river bankruptcy solution methods for allocating water to the riparian 9 parties of river systems. Given the non-uniform spatial and temporal distribution of water across 10 river basins, bankruptcy the proposed solution methods are formulated as non-linear network 11 flow optimization models to allocate water with respect to time sensitivity of water deliveries at 12 different locations in a river network during the planning horizon. Once allocation optimization 13 solutions are developed, their acceptability and stability must be evaluated. Thus, a new 14 Bankruptcy Allocation Stability Index (BASI) is developed for evaluating the acceptability of 15 river bankruptcy solutions. To show how the proposed river bankruptcy framework can be 16 helpful in practice, the suggested methods are applied to a real-world tarns-boundary river 17 system with eight riparians under various hydrologic regimes. Stability analysis based on the proposed stability evaluation method (BASI) suggests that the acceptability of allocation rules is 18 19 sensitive to hydrologic conditions and demand values. This finding has an important policy 20 implication suggesting that fixed allocation rules and trans-boundary treaties may not be reliable 21 for securing cooperation over trans-boundary water resources as they are vulnerable to changing 22 socio-economic and climatic conditions as well as hydrologic non-stationarity.

Keywords: bankruptcy, conflict resolution, trans-boundary, water allocation, game theory, water
 resources management.

25 **1. Introduction**

26 Conflicts are integral to managing trans-boundary rivers due to the externalities 27 associated with growing demand and development in riparian states. There are 148 riparian 28 countries creating about 276 trans-boundary river basins in the world (De Stefano et al., 2012). 29 These basins cover over 45% of the earth's land surface and provide about 60% of the global 30 river flows (Wolf et al., 2006). To facilitate the cooperation over trans-boundary rivers over 400 31 international agreements were signed in the 20th century (De Stefano et al., 2012), reflecting a 32 great potential for cooperation over trans-boundary natural resources (Wolf et al., 2006). 33 However, stability of these agreements could be affected by the socio-economic and political 34 changes in the riparian states as well as the climatic and hydrologic changes. Dinar et al. (2010) 35 reported 112 complaints about water deficit in trans-boundary river systems during droughts and 36 floods in the 1950-2005 period, underlying the vulnerability of cooperation over trans-boundary 37 water systems to abnormal hydrologic conditions.

Game theory –the mathematical study of competition and cooperation— is a useful method for studying trans-boundary river conflicts. Both non-cooperative and cooperative game theory methods have been used in the past to study trans-boundary water conflicts (Parrachino et al., 2006; Madani, 2010).

Non-cooperative game theoretic methods are useful in studying the strategic behaviors of the riparian parties, feasibility of cooperative solutions, and providing strategic insights into the conflicts (Madani and Hipel, 2011; Madani, 2013). Example trans-boundary river conflicts analyzed by non-cooperative game theory concepts include the conflict over flooding of Ganges

46 and Brahmaputra rivers between India and Pakistan (Rogers, 1969), the Lower Mekong river 47 basin conflict between Cambodia, Laos, Thailand, and Vietnam (Dufournaud, 1982), the Jordan 48 river conflict between Jordan, Israel, Lebanon, Palestine, and Syria (Madani and Hipel, 2007), and the Nile river conflict between Burundi, Congo, Egypt, Eritrea, Ethiopia, Kenya, Rwanda, 49 50 Sudan, Tanzania, and Uganda (Elimam et al., 2008). These methods normally rely on qualitative 51 information to find the likely outcomes of conflicts based on various stability definitions, which incorporate a range of decision makers' (players') characteristics such as risk attitude, foresight 52 53 level, information quality (Madani and Hipel, 2011; Madani, 2013). While these methods 54 provide valuable insights into strategic conflicts and can help finding the possible resolutions of 55 the conflict, their results are not necessarily quantitative and in most cases are appropriate for 56 studying games with discrete solutions (strategies or actions).

57 Cooperative game theory solution methods normally seek allocating the incremental 58 benefits of cooperation (cost savings, added values, etc.) among the cooperating parties. In the 59 context of trans-boundary river management, cooperative game theory concepts can be used to 60 develop functional water allocation schemes. Example trans-boundary river conflicts analyzed 61 by cooperative game theory include the Ganges river conflict between Bangladesh and India 62 (Kilgoure and Dinar, 2001), the Euphrates and Tigris rivers conflict between Iraq, Syria, and 63 Turkey (Kucukmehmetoglu and Guldmen, 2004), and the Syr Darya river basin conflict between 64 Kyrgyzstan, Uzbekistan and Kazakhstan (Teasley and McKinney, 2011). Cooperative game 65 theory methods are appropriate for quantitative problems with a continuous solution domain.

66 Different resource allocation methods have been employed in the water resources 67 literature to increase system's efficiency and minimize conflicts. Social welfare maximization is 68 perhaps the mostly commonly used approach for water allocation in the literature. Based on this approach, a social (central) planner seeks maximizing the system-wide benefits, assuming there
is perfect cooperation among the water users. The social planner approach pays minimal
attention to individual gains and distribution of total benefits among the beneficiaries, making it
less practical.

73 Market mechanisms and cooperative game theory schemes are among the other water 74 allocation methods that are used to make the social planner's solution practical. These methods 75 focus on redistribution of the incremental benefits of cooperation and create win-win allocation 76 solutions that make cooperation attractive to individual rational beneficiaries. While these 77 methods are promising, their application is limited to problems in which utility information is 78 available for all parties and the incremental benefits of cooperation can be determined. Therefore, challenge remains in developing cooperative schemes for managing shared water 79 80 systems for which utility information might not be readily available, agreeable, or reliable 81 (common in trans-boundary river systems).

Operations research-based allocation methods (Madani et al., 2014a; Read et al., 2014) have also been employed in the water resource literature to allocate water. These methods are applicable are appropriate for problems with both discrete and continuous solutions and can be applied with and without utility information. However, as shown by Read et al. (2014), they seek distribution of dissatisfaction in an optimal way, disregarding the stability of allocation solutions. Therefore, their acceptability is questionable, making them less practical in real world.

Bankruptcy methods (O'Neil, 1982; Aumann and Maschler, 1985; Dagan and Volij, 1993) comprise another group of allocation methods used in the water resources literature for water allocation in presence and absence of utility information (Sheikhmohammady and Madani, 2008; Ansink and Ruijs, 2008; Ansink and Weikard, 2012; Madani and Zarezadeh, 2012;

Mianabadi et al., 2013; Madani and Dinar, 2013). These methods are promising due to their cooperative game theoretic nature and their attention to individual gains under different conditions (e.g. homogeneity of claims). However, as will be discussed in the section, the previous applications of bankruptcy methods do not set an appropriate basis for using these methods for solving transboundary river allocation problems with temporal and spatial flow variability.

The objective of this study is to bridge the gap of previous trans-boundary conflict resolution studies by developing a new bankruptcy-based water allocation mechanism that: 1) does not necessarily require the players' utility information (e.g., economic benefits of each beneficiary from the allocated water); 2) its application is not limited to problems in which cooperation must result in extra quantifiable benefit; 3) provides allocations solutions with respect to the temporal and spatial variability of water flows in trans-boundary river systems.

104 **2. River Bankruptcy Problem**

105 2.1. General description

106 Water conflicts can develop when the yield of a water system is not sufficient to fully 107 satisfy the demands of all beneficiaries. Such a situation is similar to a bankruptcy state in which 108 the total asset of an individual/entity is not enough to fully satisfy his/its debts. In other words, in 109 a bankruptcy problem the total value of the claims of the beneficiaries is more than the value of 110 the available resource. Such a similarity between a water allocation problem and a bankruptcy 111 problem has been the main motivation for using bankruptcy methods, rooted in the economics 112 and mathematics literature (O'Neil, 1982; Aumann and Maschler, 1985; Dagan and Volij, 1993), 113 to solve water resource bankruptcy problems (Sheikhmohammady and Madani, 2008; Ansink and Ruijs, 2008; Sheikhmohammady et al., 2010; Grundel et al., 2011; Ansink and Weikard,
2012; Madani and Zarezadeh, 2012; Mianabadi et al., 2013; Madani and Dinar, 2013).

116 Bankruptcy methods can be categorized as cooperative game theory solutions (Sheikhmohammady and Madani, 2008). Nevertheless, these methods are different in principle 117 118 from the commonly used cooperative game theory methods such as Nash-Harsanyi bargaining 119 solution (Harsanyi, 1959), Shapley Value (Shapley, 1953), and Nucleolus (Schmeidler, 1969), 120 among others. While the bankruptcy methods focus on allocation of the total deficit (the 121 difference between the total claim and the value of the available resource) between the parties, 122 commonly used cooperative game theoretic solution methods have been primarily developed for 123 allocation of the incremental benefits of cooperation among the cooperating parties. Therefore, 124 they are not readily applicable to the bankruptcy situations with no incremental benefit out of 125 cooperation or to cases in which the available information about the utilities of the parties from 126 their shares are missing or are not reliable.

127 In some river basins, developing agreeable utility functions to estimate the utility (e.g., 128 economic gain) of each riparian from its water use is very challenging due to the lack of trust and 129 information as well as the absence of cooperative tendencies in the region. Therefore, river 130 sharing games are often played as zero-sum games in which parties are mainly bargaining about 131 their volumetric shares from the river, while in reality, due to the difference in the non-linear 132 utility functions of the parties these games are not zero-sum (Madani, 2011; Madani and Lund, 133 2012). In fact, the zero-sum perception of the riparian parties is one of the main reasons for 134 competition rather than cooperation, which makes economically-efficient cooperative game 135 theoretic institutions (Madani and Dinar, 2012) or other mechanisms such as water trading and 136 markets impractical and unacceptable. To address these issues, bankruptcy methods can be 137 applied for developing water allocation solutions. Although bankruptcy methods provide 138 solutions, which are economically less efficient than those provided by common cooperative 139 game theory methods, they are potentially more publically acceptable and practical. Most 140 bankruptcy methods are based on common sense and are relatively easy to understand by the 141 general public, unfamiliar with the economic principles and fairness rationales of the 142 mathematically sophisticated cooperative game theory methods. This advantage has been the main reason for the success of some of the bankruptcy methods in practice since the ancient 143 144 times (Dagan and Volij, 1993) in different eras and locations. The proportional cutback principle 145 is an example of one of the oldest bankruptcy methods that has been widely used for water 146 resources management during droughts in different areas of the world (e.g., ganat water 147 allocation in the Persian Empire and groundwater allocation in California.)

148 2.2. Essential elements

149 The two essential elements of a bankruptcy problem include 1) the amount of resource 150 available; and 2) the values of beneficiaries' claims. In most water resources bankruptcy 151 problems, the first element simply equals the available water to be allocated to the beneficiaries 152 in a given location at a specific time. Also finding the claim values is straightforward in some 153 water systems (e.g., claims of groundwater users in case of groundwater bankruptcy are determined based on their groundwater rights in a regulated system). Therefore, bankruptcy 154 155 solutions have been already used in the literature for solving water allocation problems with 156 known (predetermined) claims and/or without temporal and spatial variability in resource 157 availability (Sheikhmohammady and Madani, 2008; Ansink and Ruijs, 2008; 158 Sheikhmohammady et al., 2010; Grundel et al., 2011; Ansink and Weikard, 2012; Mianabadi et 159 al., 2013; Madani and Dinar, 2013). Nevertheless, solving trans-boundary river bankruptcy

problems with original bankruptcy methods can be challenging for two reasons: 1) lack of an acceptable method by all parties to estimate the credible claims of the beneficiaries; and 2) the temporal and spatial change of the flow along the river basin.

163 2.3. Claims

Determination of the beneficiaries' claims in trans-boundary systems is challenging and highly controversial, due to a lack of information, unreliability of parties' claims and narratives, and a lack of globally acceptable framework for determining the credible claims of riparian parties. Thus, in Section 4 this paper suggests three different methods as possible claim estimation methods in trans-boundary river bankruptcy problems with potential applications in real-world trans-boundary water conflicts.

170 2.4. Physical constraints: Spatial and temporal variability

171 Classical bankruptcy methods assume homogenous resource accessibility and are 172 appropriate for one-shot allocation problems. Therefore, they are not necessarily applicable to 173 problems with temporal and spatial heterogeneity in resource availability. Due to the change of 174 the flow over time and space, especially in river systems with multiple tributaries, water 175 availability might be limited at a given location at a specific time. Therefore, original bankruptcy 176 methods may produce infeasible allocation solutions for river systems.

While temporal resource variability has not been considered in previous bankruptcy studies, few studies have tried to address the spatial variability of resource in bankruptcy problems. Ilkiliç and Kayı (2012) formulated a network (graph) model for bankruptcy allocation with respect to the possible geographical and infrastructural constraints in distributing the resource among beneficiaries. While their method satisfies the fairness principle, i.e. "equal treatment of the equals", it considers "no restrictions on the possible networks between sources

183 and agents" (Ilkilic and Kayi, 2012). Therefore, their model is not generally applicable to river 184 sharing problem, in which the physical characteristics of the river network impose restrictions on 185 networks between sources (river sections) and agents (riparian parties). In another study, Ansink 186 and Weikard (2012) proposed a sequential allocation approach for solving river bankruptcy 187 problems using classical bankruptcy methods. However, their method is only applicable to linear 188 river systems in which all riparians fall on the same line and are based on some assumptions 189 which might limit their applicability in complex multi-tributary transboundary river systems 190 involving equally powerful riarian (Mianabadi et al., 2013; Zarezadeh et al., 2014).

191 This paper proposes a new approach for solving trans-boundary river bankruptcy 192 problems with consideration of the constraints imposed by temporal and spatial variability of 193 water flows within river networks. The general characteristics of the proposed method are 194 discussed in the next section. While transboundary water allocation motivates this work, the 195 proposed method is applicable to other bankruptcy problems with temporal and spatial resource 196 availability constraints. Suggested examples of such problems by Ilkilic and Kayi (2012) include 197 aid relief during and after disasters, utility (gas, electricity, water) distribution in supply shocks, 198 and common property fisheries.

199

200 2.5. Acceptability

Given that the developed bankruptcy allocation solutions have no practical value unless they are acceptable and are considered to be fair by the beneficiaries, evaluating the acceptability of the developed solutions is essential. Ex-post analysis of the stability of allocation solutions is common in the water resources literature (e.g., Dinar and Howitt (1997), Teasley and McKinney (2011), Madani and Dinar (2012), Read et al. (2014)). Once different allocation

solutions are developed, stability of solutions is normally evaluated using quantitative measures to determine the solutions with higher potential acceptability. Alternatively, an axiomatic (exante) approach can be adopted for allocation stability evaluation. Based on this approach, which is more common in the economics literature, attractiveness of allocation rules is evaluated based on their properties such as monotonicity or independence properties, with respect to various possible perturbations of the problem at hand (Herrero and Villar, 2001; Thomson, 2003).

212 Ideally, the results of both approaches should coincide and this can be approved by future 213 research. Nevertheless, the water resources literature tends to commonly use the ex-post 214 approach, making it more attractive from the practical standpoint. In the ex-post approach, 215 multiple allocation solutions with transparent utility information (i.e., volumetric gains in case of 216 river bankruptcy) are proposed to the negotiators. This will expand the feasible solution set and 217 creates more opportunities for cooperation through providing 'substance' to negotiations (Bruce 218 and Madani, 2014). In addition, developing a compromise over an ex-ante approach, before 219 clarifying to the beneficiaries what their actual gains would be, seems more challenging 220 practically, unless decision is made by an authorized intervener (e.g., social planner, government, 221 or regulator), whose decision is enforceable and acceptable by all parties. What makes 222 application of an ex-ante approach even more complex in case of river bankruptcy problems is 223 the asymmetric accessibility of the resource (water) at a given time and location. Therefore, even 224 if the solution properties are reasonable, the actual solutions (volumetric allocations in this case) 225 will be affected by the physical limitations of the system. So, the same solution principles might 226 not yield similar results in two river bankruptcy problems with similar claims and total water 227 availability as the physical aspects of the system can make the actual allocations different, i.e. 228 water might not available at a given location at a given time, as desired based on the allocation rule. This might make the axiomatic approach less practical as it does not guarantee feasible allocation solutions based on a given allocation rule, failing to provide clear information to the parties about their actual gains. Therefore, an ex-post stability evaluation method is proposed and used in this study.

While various methods have been used in the literature to evaluate the stability and acceptability of water allocation solutions (Dinar and Howitt, 1997; Teasley and McKinney, 2011; Madani and Dinar, 2012; Read et al., 2014), these methods cannot be readily used to evaluate the acceptability of bankruptcy solutions. Therefore, a new quantitative stability evaluation method is developed in this study to evaluate the potential acceptability of the proposed bankruptcy solutions.

239 2.6. Robustness

240 Normally, in water allocation negotiations, the amount of available water in a given time-241 step (e.g. month) is determined based on the average historical flows in that time-step. Given that 242 the water flows are different in dry, wet, and normal years, water allocation agreements can vary 243 depending on the hydrologic conditions. Water allocation based on historical flows might make 244 allocation agreements vulnerable to hydrologic variability, uncertainty, and non-stationarity. 245 Therefore, instead of relying on fixed water shares, riparian parties can try to agree over a flexible allocation framework that adjusts allocation solutions considering the changing 246 247 conditions of the system. This study seeks to propose a robust bankruptcy solution framework 248 that can provide water allocation solutions that are not vulnerable to changing conditions and can 249 update allocation solutions accordingly. Therefore, stability of the allocation solution is 250 examined under different hydrological conditions to find if allocation rules and solutions must be changed under different hydrologies or a fixed allocation rule can provide acceptable allocationsthat are insensitive to hydrologic variability.

253 **3. River Bankruptcy Allocation Models**

254 Figure 1 shows a schematic of simple trans-boundary river system with a lake (sink) at the outlet and m riparians (i=1, 2, ..., m), each having different types of water demand (e.g., 255 256 domestic, agricultural, and environmental). Water bankruptcy occurs when the total demand of 257 the riparians exceeds the stock of water. Bankruptcy rules can be applied to allocate the available 258 water to the riparians with respect to their water demands (claims). In river systems, however, 259 the classic bankruptcy rules might produce infeasible allocation results due to spatial and 260 temporal flow variability and water access heterogeneity. Thus, bankruptcy rules must be 261 modified to account for the physical characteristics of the river network. We propose developing 262 non-linear network flow optimization models that facilitate application of four commonly used 263 bankruptcy methods, namely Proportional (P), Adjusted Proportional (AP), Constrained Equal 264 Award (CEA), and Constrained Equal Loss (CEL) rules, to river bankruptcy problems, with 265 respect to the physical water availability constraints. These models have the following general 266 characteristics:

1. Each bankruptcy optimization model is based on a specific bankruptcy rule.

268
2. An allocation solution developed by a river bankruptcy optimization model is
always unique.

3. The allocation solution set developed by a bankruptcy optimization model is
always feasible, considering the temporal and spatial flow variability in the
river network.

4. The allocation solutions developed by a river bankruptcy optimization model
are expected to satisfy the composition properties suggested by Ansink and
Weikard (2013) for river bankruptcy problems. Nonetheless, composition
properties have not been used in this study to derive the bankruptcy solutions.

2775.The bankruptcy optimization models seek "equal treatment of the equals" to the278extent possible. This means that the bankruptcy optimization models minimize279hydro-hegemony (Zeitoun and Warner, 2006) in the system by equal treatment280of all riparians regardless of their location in the system (upstream vs.281downstream) and level of contribution to the total flows. This characteristic282makes the proposed framework different in essence from the methods proposed283by Ansink and Weikard (2012) and Mianabadi et al. (2013).

6. In absence of water availability restrictions, a bankruptcy optimization model based on a given bankruptcy rule produces allocation results that are identical to allocation solutions based on that bankruptcy rule. In other words, when allocation based on a given bankruptcy rule is feasible, original bankruptcy solutions match the solutions produced by the corresponding bankruptcy optimization model.

290 7. In case of water availability restrictions (when application original bankruptcy
291 solutions produces infeasible allocation solutions), the bankruptcy optimization
292 model minimizes the difference between its allocation solutions and the
293 solutions based on the corresponding original bankruptcy rule.

- 8. Water allocations to riparians with equal claims are not necessarily equal in river bankruptcy problems, due to the uneven access to water along the river system.
- 297 9. A bankruptcy optimization model can be applied to any river network,
 298 irrespective of its physical characteristics (shape, number of tributaries, number
 299 of riparians, etc.).
- 300 10. Each river bankruptcy optimization model satisfies the following initial, mass
 301 balance (flow continuity) and non-negativity constraints:

302
$$T_{i,t} = I_{i,t} + O_{i-1,t} \quad \forall i$$
 (1)

$$O_{i,t} = T_{i,t} - S_{i,t} \qquad \forall i$$
(2)

$$O_{0,t} = 0$$
 (3)

$$305 O_{m,t} = D_t (4)$$

$$306 S_{i,t} \ge 0 \forall i (5)$$

$$307 S_{i,t} \le T_{i,t} \forall i (6)$$

$$\sum_{i=1}^{m} S_{i,t} \le E_t$$
(7)

309
$$E_t = \sum_{i=1}^m I_{i,t} - D_t$$
(8)

310 where for i=1, 2, ..., m in a given time step t:

311 $T_{i,t}$ is total available water in riparian *i*'s territory (decision variable); $I_{i,t}$ is 312 riparian *i*'s contribution to the river system through the tributaries originating 313 in its territory (known variable); $O_{i,t}$ is the total outflow from riparian *i* to the

314		downstream riparian state $(i+1)$ (decision variable); $S_{i,t}$ is the allocation	ated water
315		supply to riparian i in each month (decision variable); D_t is the sink	demand at
316		the system's outlet (known variable); and E_t is the total asset water	(available
317		water) to be shared in the bankruptcy problem.	
318		While the sink node at the system's outlet can be treated as a riparia	n, here we
319		assume that the environmental need of the sink has a high priority.	Therefore,
320		Equation (4) ensures that the lake's environmental demand is fully m	et.
321	11.	A bankruptcy optimization model is only appropriate for a bank	runt river
521	11.	A bankruptey optimization model is only appropriate for a bank	Supt liver
322		system in which the total demand exceeds the total available water. T	This makes
323		$E_t \le \sum_{i=1}^m C_{i,t}$ a necessary condition for validity of the optimization mo	del, where
324		$C_{i,t}$ is the claim (demand) of riparian <i>i</i> in time step <i>t</i> (known variable).	
325	12.	The amount of water allocated to a riparian party i (by a river b	oankruptcy
326		optimization model) never exceeds its claim/demand. So, all b	oankruptcy
327		optimization models satisfy the following constraint:	
328		$S_{i,t} \leq C_{i,t}$ $\forall i$	(9)
329		In case of downstream excess flow, i.e. when water availability is more	re than the
330		claim of the downstream riparian, this riparian must be excluded from	m the river
331		bankruptcy problem, as technically this riparian is not expected to be	subject to
332		any conflict of water allocation.	
333	Sections 2	3.1-3.4 present the mathematical formulations for each of the prop	osed river
334	network bankrup	tcy optimization models. All river bankruptcy optimization models a	are subject
335	to Equations (1)	-(9). One advantage of using a network bankruptcy model is that	it can be

applied to any river network, irrespective of its physical conditions. So, the river network should not necessarily match the natural river system and it can include water diversion/transfer infrastructure (already developed or under consideration during allocation negotiations). It must be noted that while the proposed models have been developed for river networks, they are generally applicable to any network bankruptcy problem in which the agents' accessibility to the resource can be determined based on the network structure.

342 Given the time-sensitivity of water deliveries, water solution must be done using an 343 appropriate time-step to prevent disruption in water deliveries to any riparian party. In systems 344 without enough storage capacity to regulate and carry over water, smaller time-steps (e.g., 345 month) can be used as the basis of allocations. In this case, allocations are time-specific and can 346 be done for each time-step independently, i.e. bankruptcy rule is applied to a given time-step 347 (e.g., month) during the planning horizon (e.g. year), based on the water availability and claims 348 in that month only, regardless of the allocations in other months. In regulated systems, operations 349 are more flexible. So, bankruptcy rule can be applied to the whole planning horizon (e.g., year), 350 considering the flow variability during the planning horizon. The benefit of using bankruptcy 351 optimization models in this case is that specific concerns of the riparian nations can be 352 incorporated as constraints into the model. Examples of such constraints would be minimum 353 acceptable water supply, minimum environmental flow, minimum reservoir storage/energy head 354 for hydroelectricity generation, maximum temperature minimum, minimum acceptable 355 reliability/resiliency of water supply, maximum acceptable vulnerability of water supply at 356 particular points within the river network in a given time (e.g., day, week, month) during the 357 planning horizon (e.g., year).

In this study, the proposed modeling framework is applied to an unregulated system for which bankruptcy (cutback) allocation decisions in each time-step are independent from other time-steps.

361 *3.1. Proportional (P) Rule*

The P rule satisfies an equal proportion of the creditors' claims. Based on this ancient bankruptcy method, the equal portion $(\lambda_{P_{i,i}})$ is calculated by dividing the total available resource by total demand. The P rule's water allocation optimization model for river systems is proposed in the following mathematical form:

366 Minimize
$$\lambda_{P_i} - \prod_{i=1}^m \lambda_{P_{i,i}}$$
 (10)

367 subject to:

$$368 \qquad \lambda_{P_{i,t}} = \frac{S_{i,t}}{C_{i,t}} \quad \forall i$$
(11)

$$369 \quad \lambda_{P_{i}} \le \lambda_{P_{i}} \quad \forall i \tag{12}$$

370 where for i=1, 2, ..., m in a given time step t:

371 λ_{p_i} is the riparian *i*'s proportional allocation coefficient (decision variable), and λ_{p_i} is the 372 maximum proportional allocation coefficient (decision variable). This optimization model tries 373 to minimize the latter variable. The second term in the objective function, ensures that the model 374 has a unique solution and the agents' allocation coefficients (λ_{p_i}) are close to each other to the 375 extent possible. The minimum objective value for a given problem is achieved when the agent's 376 allocation coefficients are equal. In that case, $\lambda_{p_i} = \lambda_{p_i}$ and the proportional allocation 377 coefficients match the proportional cutback rate under the original bankruptcy rule, which is 378 equal to $\frac{E_t}{\sum_{i=1}^{m} C_{i,t}}$ This case occurs when the flow variability does not make the original

379 bankruptcy rule infeasible.

380

381 3.2. Adjusted Proportional Rule (AP)

382 Based on this rule (Curiel et al., 1988) what remains for beneficiary *i* once all other 383 creditors are satisfied is the basis for allocation. To determine the initial amount of allocation to 384 creditor *i*, the summation of claims of all other beneficiaries is compared with the available stock 385 of water. In case of surplus, the initial allocation to stakeholder *i* is equal to the remaining water 386 stock once all others are satisfied. Otherwise, the initial allocation to *i* is set to 0. It is assumed 387 that the initial allocation calculated through this procedure is agreeable by all beneficiaries. Once 388 initial allocations are determined claims are revised. Claim of a given beneficiary is set equal to 389 the minimum of the remaining water and the difference between its initial claim and its initial 390 allocation. The P rule is then applied to the remaining water stock and the revised claims.

391 The mathematical formulation of the AP rule's river bankruptcy optimization model is392 proposed as follows:

393 Minimize
$$\lambda_{AP_i} - \prod_{i=1}^m \lambda_{AP_{i,i}}$$
 (13)

394 subject to:

$$395 \qquad R_{i,t} = \sum_{j \neq i} C_{j,t} \qquad \forall i \tag{14}$$

396
$$v_{i,t} = \frac{E_t - R_{i,t} + |E_t - R_{i,t}|}{2}$$
 $\forall i$ (15)

$$397 \qquad C_{i,t}^* = Min(C_{i,t}, E_t) \qquad \forall i \tag{16}$$

398
$$\lambda_{AP_{i,i}} = \frac{S_{i,i} - v_{i,i}}{C_{i,i}^* - v_{i,i}} \quad \forall i$$
 (17)

$$399 \quad \lambda_{AP_{i,i}} \le \lambda_{AP_i} \qquad \forall i \tag{18}$$

400
$$\lambda_{AP_{t}} \leq \frac{E_{t} - \sum_{i=1}^{m} v_{i,i}}{\sum_{j=1, j \neq i}^{m} (C_{j,t}^{*} - v_{j,i})} \quad \forall i$$
 (19)

401 where for i=1, 2, ..., m in a given time step *t*:

 $R_{i,t}$ is the summation of all riparian claims excluding riparian *i*; $v_{i,t}$ is the initial allocation to 402 riparian *i* (amount of water conceded to riparian *i* by all other riparians); $\lambda_{AP_{i,i}}$ is the riparian *i*'s 403 AP allocation coefficient (decision variable), and λ_{AP_t} is the maximum proportional (AP) 404 allocation coefficient (decision variable). Similar to the P rule's optimization model, the 405 406 minimum objective value is achieved when the original bankruptcy solution is feasible and the 407 optimized allocations match the allocations under application of the original bankruptcy rules. 408 The second term in the objective function ensures having a unique solution and minimizes the 409 differences between the allocation coefficients of the riparians.

410 *3.3. Constrained Equal Award Rule (CEA)*

This ancient rule, adopted by rabbinical legislators (Dagan and Volij, 1993) allocates the minimum of λ_{CEA_t} and $C_{i,t}$ to all beneficiaries, provided that the sum of allocations equals the total available resource. CEA tries satisfying the lower claims to the extent possible to minimize the number of unsatisfied creditors. This rule is supposed to favor the lower claims, normally belonging to weaker beneficiaries who can get more affected by losses (Madani and Dinar, 2012). Based on CEA, the initial allocation to all beneficiaries is equal to the lowest claim, 417 provided that the sum of initial allocations does not exceed the demand. The fully-satisfied 418 creditor is then excluded and the process continues with the remaining creditors after updating 419 their unsatisfied claims as well as the remaining resource value. At any stage (including the 420 initial stage) when allocating an amount equal to the lowest claim to all remaining creditors is 421 not feasible (due to unavailability of enough resource) the remaining resource is distributed 422 equally among all remaining creditors.

The mathematical formulation of the CEA rule's river bankruptcy optimization model is proposed as follows:

425 Minimize
$$\lambda_{CEA_t} - \frac{\prod_{i=1}^m \lambda_{CEA_{i,i}}}{(\lambda_{CEA_t})^{m-1}}$$
 (20)

426 subject to:

$$427 \quad \lambda_{CEA_{i,j}} = S_{i,t} \qquad \forall i \tag{21}$$

$$428 \qquad \lambda_{CEA_{i}} \le \lambda_{CEA_{i}} \qquad \forall i \tag{22}$$

429 where for i=1, 2, ..., m in a given time step t:

430 $\lambda_{CEA_{i,t}}$ is the feasible allocation to the riparian *i* (decision variable), and λ_{CEA_t} is the highest 431 feasible allocation to the creditors in time step *t* (decision variable). The second term in the 432 objective function is to enforce a unique solution and to minimize the difference between the 433 allocations which would be equal in absence of resource accessibility limitations. Given that 434 λ_{CEA_t} can be more than 1 (different from the λ_{P_t} and λ_{AP_t} which are always less than or equal 1) 435 the second term is divided by a positive number of comparable magnitude to ensure that the 436 second term is always smaller than or equal to the first term.

437 *3.4. Constrained Equal Loss Rule (CEL)*

438 This rule can be viewed as the opposite of CEA, as it gives priority to satisfying the 439 highest claims (more powerful creditors) first. Once the highest claim is satisfied, the process is 440 repeated with the remaining resource and creditors. The process stops at any stage (including the first stage) if the available resource is not sufficient to satisfy the highest claim of the remaining 441 442 creditors. At this stage, the remaining resource is split equally among the remaining creditors. By doing this, CEL allocates $C_i - \lambda_{CEL_i}$ to all beneficiaries whose claims are bigger than λ_{CEL_i} , 443 allocating 0 to those who do not fall in this category. So, the final allocation to each beneficiary 444 is equal to $max \{0, C_i - \lambda_{CEL_i}\}$. 445



The CEL rule's river bankruptcy optimization model is proposed as follows:

447 Minimize
$$\lambda_{CEL_{t}} - \frac{\prod_{i=1}^{m} \lambda_{CEL_{i,i}}}{(\lambda_{CEL_{t}})^{m-1}}$$
 (23)

448 subject to:

449
$$\lambda_{CEL_{i,t}} = C_{i,t} - S_{i,t} \qquad \forall i$$
(24)

$$450 \quad \lambda_{CEL_{i,i}} \le \lambda_{CEL_i} \qquad \forall i \tag{25}$$

451 where for i=1, 2, ..., m in a given time step *t*:

452 $\lambda_{CEL_{i,i}}$ is the unmet claim of the riparian *i* (decision variable), and λ_{CEL_i} is the maximum unmet

453 claim of all riparians (decision variable).

454 **4. Example: The Qezelozan- Sefidrood River Bankruptcy Problem**

The proposed framework is applied to develop bankruptcy-based water allocation schemes for resolving a real-world trans-boundary river conflict in Iran. The Qezelozan-Sefidrood river basin (Figure 2) is located in the intersection of the Iran's Alborz and Zagros 458 mountain ranges, with an area about 59,400 km², making it the largest basin of the nation. The 459 basin overlaps with eight provinces (Kurdistan, Hamadan, Zanjan, Eastern Azerbaijan, Ardebil, 460 Tehran, Qazvin and Gilan) and the river provides the basis for important economic activities in 461 these provinces. The river eventually flows into the Caspian Sea in north of Iran, which is the 462 largest enclosed body of water in the world and the source of more than 90% of the world's 463 caviar supply (Madani et al., 2014b). Supplying the required environmental flows of the Caspian 464 Sea is essential to health of the sea and its valuable ecosystem.

465 While the study basin is not international, interprovincial or interstate basins are 466 effectively equivalent to international basins as long as their boundaries do not match the 467 political boundaries and they are managed by more than one authority. The Qezelozan-Sefidrood 468 river basin is an example of a trans-boundary river basin, in which serious conflict has arisen as a 469 result of recent socio-economic (i.e., population increase and development), political (i.e., 470 changes in the water resources management structure), and hydrologic and climatic (i.e., frequent 471 droughts) changes. As a result of political changes in the country, the Qezelozan-Sefidrood river, 472 which was historically shared by six Iranian provinces and managed by only one water resources 473 authority, is now shared by eight provinces and managed by eight water authorities. As a result 474 of population increase and development in the region, each province is trying to increase its 475 share from the river and minimize the outgoing flow, resulting in significant reduction of water 476 flowing into downstream provinces. To increase their water uses from the river, the upstream 477 provinces have aggressive water resources development plans. These development plans include 478 construction of multiple new reservoirs, which are currently under construction or in the study 479 phase. Complete implementation of these plans will negatively impact the downstream 480 provinces, that historically have had more access to the Qezelozan-Sefidrood river due to their 481 stronger political and economic power as well as higher populations. Therefore, the political 482 tension has increased in the basin, making Qezelozan-Sefidrood river the subject of one of the 483 most intractable conflicts over water resources in Iran. To show the utility of the proposed model 484 in solving trans-boundary water allocation conflicts, the proposed framework is applied to derive 485 new water allocation schemes for the Qezelozan-Sefidrood river system.

To first step in solving river bankruptcy problems is determining the legitimate claims of the riparian parties. This step is challenging in unregulated systems without established water rights. In case of Qezelozan-Sefidrood river, we propose three alternatives for determining the claims of the riparian parties. These alternatives, which help setting the upper and lower boundaries of the claims include:

491 1) Historical uses: Based on this alternative, historical uses of Qezelozan-Sefidrood river,
492 revealed by the historical water use data are set as the claims of the riparians. The water
493 use values are calculated based on the difference between the recorded inflows and
494 outflows of each province at the hydrometric satiations. This alternative sets the lower
495 claim boundary for each riparian.

Planned uses: Iran is one of the countries with a high number of under-construction dams.
Currently, several water storage projects are under development at different locations in
the riparian states of Qezelozan-Sefidrood river. These projects have received approval
from the central government, receiving financial support from the central and provincial
governments. Each project has an associated estimation of sectorial water demands (i.e.
domestic, agricultural, industrial, and environmental) used for calculation of the required
storage capacity. Based on this alternative, total claim of each riparian is set equal to the

503total documented water demands of different Qezelozan-Sefidrood river-related504reservoirs within its boundaries, which are already in operation or under development.

505 3) Future uses: Beside under-construction projects, each riparian state has plans for getting
506 approval for constructing additional water storage infrastructure to meet its increasing
507 water demand as a result of development. Based on this claim estimation alternative,
508 water demands of these additional facilities will be added to the water claims calculated
509 based on alternative 2, only if plans for construction of these facilities have been publicly
510 announced. This alternative sets the upper claim boundary for each riparian.

511 Figure 3 indicates the estimated monthly water claims of the riparian states of the 512 Qezelozan-Sefidrood river based on the three proposed methods. Detailed calculations of water 513 claims based on the proposed claim determination alternatives can be found in Zarezadeh (2011). 514 Given that allocation solutions can be sensitive to climatic/hydrologic conditions, three different 515 water availability scenarios, representing three distinct hydrologic conditions, normal (average), 516 dry, wet, were initially considered for solving the Qezelozan-Sefidrood river bankruptcy 517 problem. In the normal scenario river flows are based on the average monthly river discharges 518 during the 1956-2006 period. Dry scenario flows match the average monthly river discharges 519 during the major drought of 1998-2001 in the region. The wet scenario flows are based on the 520 monthly flows during the 1968-1969 period. The annual river discharge under the wet scenario 521 will be sufficient to meet the historical, planned, and future claims of the riparian states and the 522 Caspian Sea's (sink) water demand (Figure 4). Therefore, river bankruptcy problem is solved 523 only for the normal and dry cases.

524 Due to the unclear status of water rights/claims and the future status of reservoir networks 525 in the Qezelozan-Sefidrood river system, the system is considered as an unregulated system here,

disregarding the possible benefits resulting from coordination of reservoir operation strategies in the basin. The problem is solved using a monthly time-step and allocations are determined in each time-step separately. Under this approach the total allocation to each riparian over the whole planning horizon (e.g. year) is the summation of bankruptcy allocations in the existing time-steps within the planning horizon (e.g. twelve months).

Figure 5 indicates the monthly water yield of the Qezelozan-Sefidrood river system under the normal and dry conditions as well as the total monthly claims of the riparian parties (including Caspian Sea's water demand). This figure clearly shows the water bankruptcy situation in the Qezelozan-Sefidrood river system in almost half of the year, especially in warmer months with higher agricultural water demands.

The four proposed bankruptcy optimization models in section 3 were run under two hydrologic scenarios to calculate bankruptcy allocations under normal and dry conditions. The models were first run on a monthly basis to calculate the monthly allocations. Summation of 12 monthly allocations based on each model with a given set of claims under a given hydrology determines the corresponding annual allocation of each province. The annual bankruptcy allocations based on different bankruptcy models, claims, and hydrologies are presented in Figure 6.

As expected based on definition, the CEL method favors the creditor with the highest claim (in this the downstream Province of Gilan). The opposite is true for the CEA method which gives priority to satisfy the claims of the creditors with lower claims (in this the provinces upstream of Gilan). The AP and P methods can be considered as moderate allocation methods which result in allocations that are between the high and low allocations estimated by the other two methods. In comparison with P, the AP method allocates a higher share to the parties with

549 lower claims and a lower share to the parties with higher claims, trying to address the bias 550 toward higher claims in the P method. The difference between the allocation values for different 551 claims and hydrologies underline the sensitivity of bankruptcy allocation schemes to the 552 difference in claim values and hydrologic conditions in bankruptcy problems.

553 **5. Stability Evaluation**

554 The suggested bankruptcy optimization models provide different allocation solutions, 555 based on different notions of fairness. Therefore, their acceptability is always questionable, given 556 that there is always at least one beneficiary who finds one of the given alternatives unfair 557 because she can gain more under another rule (Madani and Lund, 2011). As one of the most 558 commonly used social choice (voting) methods (Sheikhmohammady and Madani, 2008; Madani 559 et al., 2014c), Plurality Index can be considered as an indicator of potential acceptability of a 560 decision rule in multi-participant decision-making problems. Based on this index, the number of 561 stakeholders who prefer one method to the others is simply an indicator of the degree of 562 acceptance of that method (Dinar and Howitt, 1997).

563 The higher the allocation to a riparian state, the more preferred the allocation rule 564 (bankruptcy method) by that state. Table 1 shows the Plurality Index (number of votes received) 565 of each bankruptcy solution method for different claim values under different hydrologies. The 566 assumption is that each party selects the allocation scheme that gives it the highest share. Given 567 that the Hamadan Province has no historical or planned claim, its vote is only counted when 568 future claims are considered. Based on Plurality Index, the CEA method, which highly satisfies 569 the riparians with lower claims (majority in this case) in both normal and dry conditions, is the 570 winner. However, given the absolute objection of the most powerful province, i.e. Gilan, to this

method, which allocates low shares to this province, this solution is not practical without strongintervention of the central government or providing strong cooperation incentives to Gilan.

573 Majority does not necessarily win in multi-participant decision-making problems with 574 asymmetric decision-makers' powers, especially when the minority group is powerful. 575 Therefore, the Plurality Index might is not very appropriate for identifying the feasible solution 576 when there is power imbalance among the beneficiaries. Other methods can be used to quantify 577 the potential acceptability of allocation solutions (Read et al., 2014). Loehman et al. (1979) used 578 the following Power Index (α_i), originally developed by Shapley and Shubik, 1954, to evaluate 579 the power of players in cooperative game theory problems in which players are trying to find the 580 best method for allocating the incremental benefits of cooperation to coalition members:

581
$$\alpha_i = \frac{x_i - x_i}{\sum_{j \in N} (x_j - x_j')}, \quad i \in N, \quad \sum_{i \in N} \alpha_i = 1$$
 (26)

where x_i is the allocated cooperative benefit share to player *i*, x'_i is the status-quo (noncooperative) gain of player *i*, and *N* is the set of all players.

584 A high Power Index value reflects less power or a higher willingness to cooperate. A 585 stable allocation solution can be achieved when the power is distributed more or less equally 586 among the players (Dinar and Howitt, 1997). Therefore, the coefficient of variation of powers, 587 also known as Stability Index (S_{α}) is used as an indicator of the stability of allocation solutions:

$$588 \qquad S_{\alpha} = \frac{\sigma_{\alpha}}{\overline{\alpha}} \tag{27}$$

589 where σ_{α} is the standard deviation of powers and $\overline{\alpha}$ is the mean power. The lower the index, 590 the more stable the allocation solution. 591 Given that cooperation in bankruptcy problems does not have incremental benefits and 592 parties' gains are zero in the status-quo, the Power Index is not readily quantifiable in bankruptcy 593 problems. Therefore, we propose modification of Power Index (BPI) for bankruptcy problems as 594 follows:

595
$$BPI_i = \frac{S_i - v_i}{\sum_{j \in \mathbb{N}} (S_j - v_j)}, \quad i \in \mathbb{N}, \quad \sum_{i \in \mathbb{N}} BPI_i = 1$$
(28)

596 where:

597
$$S_i = \sum_{t=1}^n S_{i,t}$$
 (29)

$$598 \qquad \upsilon_i = \sum_{t=1}^n \upsilon_{i,t} \tag{30}$$

599 BPI_i is the Bankruptcy Power Index (BPI) of riparian *i*, v_i is the sum of the conceded water to 600 riparian *i* by all other riparians in all time-steps in the overall planning horizon, *N* is the set of 601 riparians, and *n* is the number of time-steps in the planning horizon (*n*=12 months in the study 602 example).

603 Bankruptcy Allocation Stability Index (BASI) is then equal to the coefficient of variation 604 of BPIs, which can be used to evaluate the potential acceptability of a bankruptcy solution:

$$605 \qquad BASI = \frac{\sigma_{BPI}}{BPI} \tag{31}$$

606 where σ_{BPI} is the standard deviation of riparian powers and \overline{BPI} is mean power. The higher the 607 index, the less stable the allocation solution.

Table 2 shows the BASI value for each bankruptcy solution under a given hydrology for a unique claim set. Based on this table, the CEL method is the most stable method under the

610 normal hydrology even though this method is not the most popular method (based on the 611 Popularity Index). Given that stability (feasibility) is more important than popularity (social 612 optimality) in conflict resolution (Read et al., 2014) we can conclude that CEL is the best 613 mechanism for water allocation in this bankruptcy study case. Nevertheless, the stability of this 614 method is sensitive to the hydrological conditions and this method becomes the least stable 615 allocation method under dry conditions. Under the dry conditions, the P rule is the most stable 616 with lower demands. As the demands increase, the CEA method (the most popular method) 617 becomes more stable. The changes in stablility of allocation rules with changes in demand and 618 hydrology, shows that not only stability of allocation mechanism is sensitive to both the 619 hydrologic conditions (water availability) and the claim set characteristics. Future studies can 620 focus on understanding the correlations between the claim set characteristics (magnitude of 621 claims, heterogeneity of claims, etc.), resource availability, and BASI of allocation rules.

622 6. Conclusions

Using an example of real-world river bankruptcy problem, this work formed the basis and 623 624 set practical guidelines for developing allocation schemes for resolving trans-boundary water 625 allocation conflicts based on bankruptcy methods. Although the suggested approach does not 626 necessarily maximize the total welfare in the basin and might result in sub-optimal allocations 627 from the economic standpoint, it can be used to develop practical solutions when side-payments 628 are not feasible, parties are not highly cooperative (or not interested in implementing solutions 629 based on conventional cooperative game theory solutions), and utility information is not 630 available.

631 Considering the non-uniform spatial and temporal variability of water flows, resulting in
 632 unequal access to water in river systems, the work proposed solving river bankruptcy problems

using non-linear optimization models. Four river bankruptcy network flow optimization models
were proposed based on four conventional bankruptcy rules, i.e. Proportional (P), Adjusted
Proportional (AP), Constrained Equal Award (CEA), and Constrained Equal Loss (CEL), for
trans-boundary water allocation. The models can be applied to any river network (or bankruptcy
network) problem, irrespective of its shape and resource variability/accessibility conditions.

638 Acknowledging the difference in the notion of fairness and the possibility of rejection of 639 suggested allocations by the beneficiaries, who find certain allocation rules unfair, there is need 640 for evaluating the acceptability of different bankruptcy solutions. While popularity of each 641 solution is a simple indicator of the potential acceptability of a solution, it was argued that in 642 case of asymmetric powers, majority cannot necessary determine the feasible solution, especially 643 when the powerful parties do not support the most popular solution. Therefore, a new index 644 (Bankruptcy Allocation Stability Index) was formulated for evaluating the potential 645 acceptability/stability of allocation solutions with respect to distribution of claims and 646 dissatisfaction among the beneficiaries.

Evaluation of the stability of different bankruptcy allocation solutions for different water demand and hydrologic scenarios suggested that acceptability is sensitive to both water demand (claim) and water availability. This finding has a significant policy implication for transboundary water management, suggesting that inflexible water allocation agreements and treaties that have been developed based on stationary assumptions are not resilient, especially in face of the expected socio-economic and climatic changes.

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658 8. References

Ansink, E. and Ruijs, A.: Climate change and the stability of water allocation agreements,

660 Environmental and Resource Economics, 41(2), 249–266, 2008.

- Ansink, E. and Weikard, H.P.: Sequential sharing rules for river sharing problems, Social
 Choice and Welfare, 38, 187-210, 2012.
- Ansink, E. and Weikard, H.P.: Composition properties in the river claims problem.
- 664 MPRA Working Paper 51618, 2013.
- Aumann, R. J. and Maschler, M.: Game theoretic analysis of a bankruptcy problem from
 the Talmud. J. Economic Theory, 36(2), 195-213, 1985.
- Bruce, C. J. and Madani, K.: Successful Collaborative Negotiation over Water Policy:
 Substance versus Process", Department of Economics, University of Calgary, Working Paper
 2014-36, 2014.
- 670 Curiel, I. J., Maschler, M. and Tijs, S. H.: Bankruptcy game, Zeitschrift für Operations
 671 Research, 31(5), A143-A159, 1987.
- Dagan, N. and Volji, O.: The bankruptcy problem: a cooperative bargaining approach,
 Mathematical Social Sciences, 26(3), 287-297, 1993.
- 674 De Stefano, L., Duncan, J., Dinar, S., Stahl, K., Strzepek, K.M. and Wolf, A.T.: Climate
- change and the institutional resilience of international river basins. Journal of Peace Research,
 49, 193–209, 2012.

Dinar, A. and Howitt, R. E.: (1997), Mechanisms for allocation of environmental control
cost: empirical tests of acceptability and stability, J. Environmental Management, 49(2), 183–
203, 1997.

Dinar, S., Odom, O., McNally, A., Blankespoor, B. and Kurukulasuriya, P.: Climate
Change and state grievances: the resiliency of international river treaties to increased water
variability, Institute of Advanced Study Insights Working Paper Series, Durham University,
3(22), 2010.

Dufournaud, C.: On the Mutually Beneficial Cooperative Scheme: Dynamic Change in
the Payoff Matrix of International River Basin Schemes, Water Resources Research, 18(4), 764772, 1982.

Elimam, L., Rheinheimer, D., Connell, C. and Madani, K.: An ancient struggle: a game
theory approach to resolving the Nile conflict, In: Babcock, R.W., Walton, R. (Eds.), Proceeding
of the 2008 World Environmental and Water Resources Congress, Honolulu, Hawaii. American
Society of Civil Engineers, pp. 1–10, 2008.

Grundel, S., Borm, P. and Hamers, H.: A Compromise Stable Extension of Bankruptcy
Games: Multipurpose Resource Allocation, CentER Discussion Paper, 2011-029. 17p, 2011.

Giordano, M. and Wolf, A.: Sharing waters: Post-Rio international water management,
Natural Resources Forum, 27(2), 163-171, 2003.

695 Harsanyi, J. C.: A bargaining model for the cooperative n-person game, In Contributions

to the Theory of Games, 4 (A. W. Tucker and D. R. Luce, eds): 324–356. Princeton, NJ:

697 Princeton University Press, 1959.

Herrero, C. and Villar, A.: The three musketeers: Four classical solutions to bankruptcy
problems. Mathematical Social Sciences 42(3), 307–328, 2001.

700 Ilkılıç, R. and Kayı, C.: Allocation rules on networks, Working Paper 118, Universidad701 del Rosario, 2012.

- Kilgour, D. M. and Dinar, A.: Flexible water sharing within an international river basin,
 Environmental and Resource Economics. 18(1), 43–60, 2001.
- 704 Kucukmehmetoglu, M. and Guldmen, J.: International water resources allocation and
- conflicts: the case of the Euphrates and Tigris, Environment and Planning, 36(5), 783-801, 2004.
- Loehman, E., Orlando, J., Tschirhart, J. and Winstion, A.: Cost allocation for a regional
 wastewater treatment system, Water Resources Research, 15(2), 193–202, 1979.

708 Madani, K.: Game theory and water resources, J. Hydrology, 381(3-4), 225-238, 2010.

Madani, K.: Hydropower Licensing and Climate Change: Insights from Game Theory,
Advances in Water Resources, 34 (2), 174-183, 2011.

Madani, K.: Modeling International Climate Change Negotiations More Responsibly:
Can Highly Simplified Game Theory Models Provide Reliable Policy Insights?, Ecological
Economics, 90, 68-76, 2013.

Madani, K. and Dinar, A.: Policy implications of institutional arrangements for sustainable management of common pool resources: The case of groundwater, Proceeding of the 2011 World Environmental and Water Resources Congress, pp. 981-989, ASCE, Palm Springs, California, Edited by: Beighley II R. E. and Kilgore M. W., ASCE, 2011.

Madani K. and Dinar, A.: Cooperative Institutions for Sustainable Common Pool
Resource Management: Application to Groundwater, Water Resources Research, 48(9),
W09553, 2012.

Madani, K. and Dinar, A.: Exogenous Regulatory Institutions for Sustainable Common
Pool Resource Management: Application to Groundwater, Water Resources and Economics, 2-3,
57-76, 2014.

Madani, K. and Hipel, K. W.: Strategic insights into the Jordan river conflict, Proceeding
of the 2007 World Environmental and Water Resources Congress, Tampa, Florida, Edited by:
Kabbes K. C., ASCE, 2007.

Madani, K. and Hipel, K. W.: Non-cooperative stability definitions for strategic analysis
of generic water resources conflicts, Water Resources Management, 25, 1949–1977, 2011.

Madani K. and Lund, J. R.: A Monte-Carlo game theoretic approach for Multi-Criteria
Decision Making under uncertainty, Advances in Water Resources, 35(5), 607-616, 2011.

Madani, K. and Lund, J. R.: California's Sacramento-San Joaquin Delta conflict: from
cooperation to chicken, Water Resources Planning and Management, 138(2), 90-99, 2012.

Madani, K., Sheikhmohammady, M., Mokhtari, S., Moradi M. and Xanthopoulos, P.:
Social Planner's Solution for the Caspian Sea Conflict, Group Decision and Negotiation, 23(3),
579-596, 2014a.

Madani, K., Rouhani, O. M., Mirchi, A. and Gholizadeh, S.: A Negotiation Support
System for Resolving an International Trans-boundary Natural Resource Conflict",
Environmental Modeling and Software, 51: 240–249, 2014b.

Madani K., Read L. and Shalikarian L.: Voting Under Uncertainty: A Stochastic
Framework for Analyzing Group Decision Making Problems, Water Resources Management,
28(7),1839-1856, 2014c.

Madani, K. and Zarezadeh, M.: Bankruptcy Methods for Resolving Water Resources
Conflicts, 2012 World Environmental and Water Resources Congress, pp. 2247-2252, ASCE,
Albuquerque, New Mexico, Edited by: Loucks E. D, 2012.

Mianabadi, H., Mostert, E., Zarghami, M. and Giesen, N. van de.: Transboundary water
resources allocation using bankruptcy theory; Case study of Euphrates and Tigris Rivers,
Proceedings of the Transboundary water management across borders and interfaces: present and
future challenges International Conference & Workshops (TWAM,2013). 16- 20 March, Aveiro,
Portugal, 2013.

O'Neill, B.: A problem of rights arbitration from the Talmud, Mathematical Social
Sciences, 2(4), 345–371, 1982.

Parrachino, I., Dinar, A. and Patrone, F.: Cooperative game theory and its application to
natural, environmental, and water resource issues: 3. Application to Water Resources. World
Bank Policy Research Working Paper No. 4074, WPS4072, 2006.

Read, L., Madani, K. and Inanloo, B.: Optimality versus Stability in Water Resource
Allocation Negotiations, Journal of Environmental Management, 133, 343-354, 2014.

Rogers, P.: A game theory approach to the problems of international river basins, Water
Resources Research, 5(4), 749-760, 1969.

759 Shapley, L. S.: A value for n-person games, Annals of Mathematics Studies, 28, 307–

760 318, and in Contributions to the Theory of Games, Vol. 2 (H. W. Kuhn and A. W. Tucker, eds).

761 Princeton: Princeton University Press, 1953.

Shapley, L. S. and Shubik, M.: A method for evaluating the distribution of power in a
committee system. American Political Science Review 48:787–792, 1954.

Sheikhmohammady, M., Kilgour, D.M., and Hipel, K.W.: Modeling the Caspian Sea
Negotiations, Group Decision and Negotiation, 19(2), 149-168, 2010.

Sheikhmohammady, M. and Madani, K.: Sharing a multi-national resource through
bankruptcy procedures, Proceeding of the 2008 World Environmental and Water Resources
Congress, Honolulu, Hawaii, Edited by Babcock R. W. and Walton R., pp. 1-9, American
Society of Civil Engineers, 2008.

Schmeidler, D.: The nucleolus of a characteristic function game, SIAM Journal of
Applied Mathematics, 17(6), 1163–1170, 1969.

Teasley, R. L. and McKinney, D. C.: Calculating the benefits of trans-boundary river
basin cooperation: the Syr Darya basin, Water Resources Planning and Management, 137(6),
481-490, 2011.

Thomson, W.: Axiomatic and game-theoretic analysis of bankruptcy and taxation
problems: A survey. Mathematical Social Sciences 45(3), 249–297, 2003.

Wolf, A. T., Kramer, A., Carius, A., and Dabelko, G. D.: Water Can Be a Pathway to
Peace, Not War. Woodrow Wilson International Center for Scholar. No. 1., 2006.
www.wilsoncenter.org/topics/pubs/NavigatingPeaceIssue1.pdf

Zarezadeh, M.: Water Allocation in the Qezelozan- Sefidrood Basin under Climate
Change, using Bankruptcy Approach for Conflict Resolution, M. S. thesis, Dep. Of Water
Resources Engineering, Tarbiat Modares University, Tehran, Iran, 2011.

Zarezadeh M., Madani K., and Morid S.: Interactive comment on Resolving conflicts
 over trans-boundary rivers using bankruptcy methods, Hydrol. Earth Syst. Sci. Discuss., 10,
 C8199–C8199, 2014, <u>http://www.hydrol-earth-syst-sci-discuss.net/10/C8199/2014/hessd-10-</u>
 <u>C8199-2014.pdf</u>

- 787 Zeitoun M., Warner J.: Hydro-hegemony a framework for analysis of trans-boundary
- 788 water conflicts, Water Policy 8(5), 435–460, 2006.

	Hydrology										
Claim	Normal					Dry					
	Р	AP	CEL	CEA	Winner	Р	AP	CEL	CEA	Winner	
Historical	0	0	1	<u>6</u>	CEA	0	0	1	<u>6</u>	CEA	
Planned	0	0	1	<u>6</u>	CEA	0	1	1	<u>5</u>	CEA	
Future	0	1	1	<u>6</u>	CEA	0	2	1	<u>5</u>	CEA	

Table 1. Plurality Index of different bankruptcy solutions for different claims and hydrologies

	Bankruptcy Stability Index								
Scenario		Nor	mal		Dry				
-	Р	AP	CEL	CEA	Р	AP	CEL	CEA	
Historical	0.11	0.10	<u>0.07</u>	0.15	<u>0.90</u>	1.00	1.33	1.27	
Planned	0.31	0.31	0.21	0.43	1.11	1.01	1.68	0.77	
Future	6.57	6.49	<u>3.48</u>	9.65	1.01	0.95	1.54	0.73	

 Table 2. Bankruptcy Index Values of different bankruptcy solutions for

 different claims and hydrologies

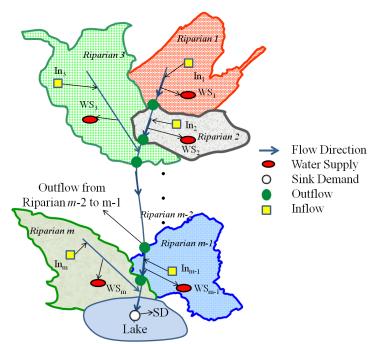


Figure 1. Schematic map of a trans-boundary river network



Figure 2. Qezelozan-Sefidrood river basin and its eight riparian provinces

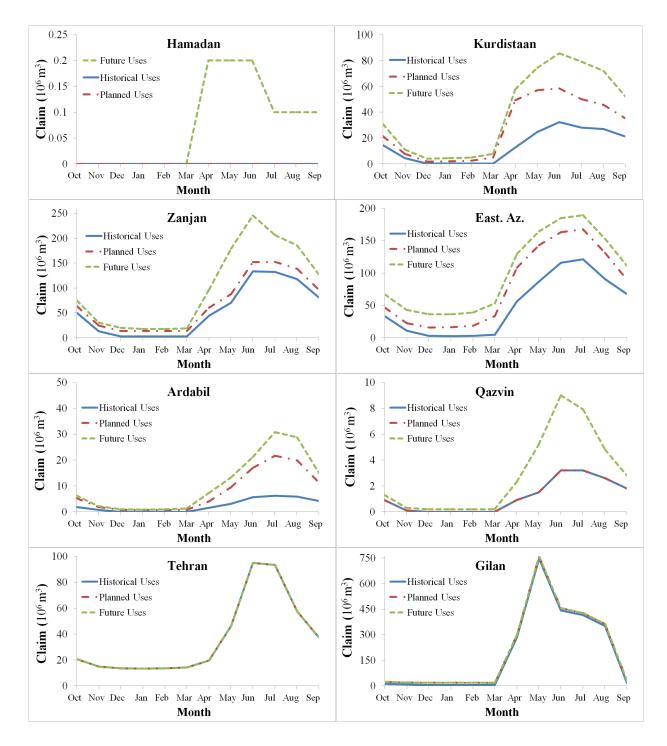


Figure 3. Estimated monthly claims of the riparian provinces based on the three proposed claim calculation method

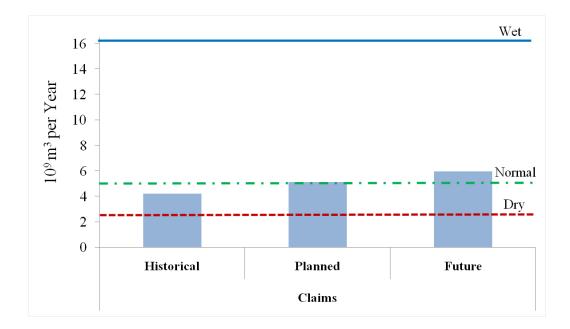


Figure 4. Total annual claims (including Caspian Sea's water demand) based on three different claim estimation methods and total annual water yield under three different hydrologic scenarios

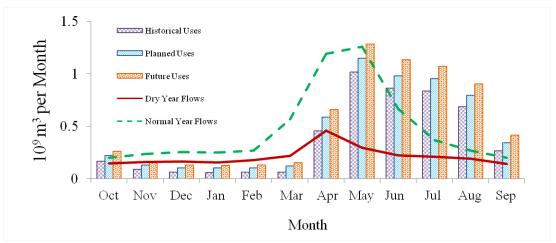


Figure 5. Total monthly claims (including Caspian Sea's water demand) based on three different claim estimation methods and total annual water yield under normal and dry hydrologies

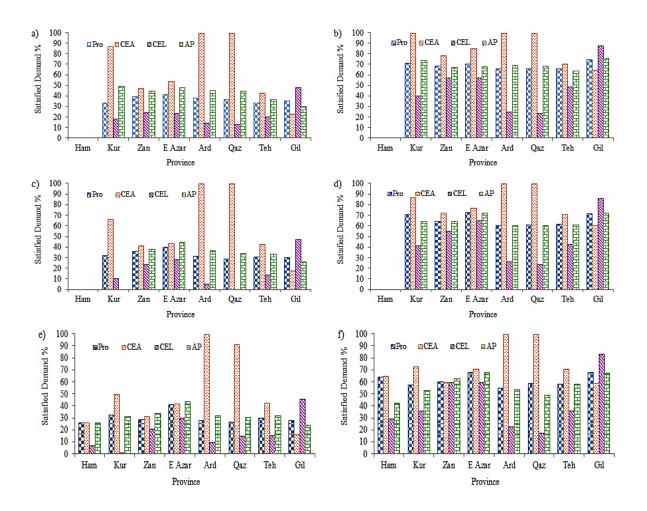


Figure 6. Satisfied annual water claim (%) of the riparian provinces based on different bankruptcy solution methods for different claims and hydrologies (a: historical claim in normal year, b: historical claim in dry year, c: planned claim in normal year, d: planned claim in dry year, e: future claim in normal year, and f: future claim in dry year)