

This discussion paper is/has been under review for the journal Hydrology and Earth System Sciences (HESS). Please refer to the corresponding final paper in HESS if available.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk^{1,2}, H. H. G. Savenije¹, C. C. J. M. Tiberius¹, and W. M. J. Luxemburg¹

¹Delft University of Technology, Delft, the Netherlands

²Seaway Heavy Lifting Engineering, Zoetermeer, the Netherlands

Received: 14 September 2013 – Accepted: 7 October 2013 – Published: 14 November 2013

Correspondence to: M. Valk (mvalk@shl.nl)

Published by Copernicus Publications on behalf of the European Geosciences Union.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)

Abstract

In this paper we present a novel method to determine the time of occurrence of tidal slack with a GPS receiver mounted on an anchored buoy commonly used to delineate shipping lanes in estuaries and tidal channels. Slack tide occurs when the tide changes direction from ebb to flood flow, or from flood to ebb. The determination of this point in time is not only useful for shipping and salvaging, it is also important information for calibrating tidal models, for determining the maximum salt intrusion and for the further refinement of the theory on tidal propagation. The accuracy of the timing is well within 10 min and the method – able to operate in real-time – is relatively cheap and easy to implement on a permanent basis or in short field campaigns.

1 Introduction

In tidal hydraulics, the most frequent and easiest to observe state variable is the water level. Unfortunately, the calibration of tidal hydraulic models on water levels alone is not very accurate. If the channel geometry is accurately known, then the fundamental calibration parameter is the roughness coefficient, which then reflects all the uncertainty inherent in the observational errors in the geometry, the tidal boundary conditions, and the water levels. Reasonable fits between observed and modelled water levels can be obtained with a range of values of calibration parameters, whereby it is uncertain whether the model performs well for the right reason. In hydrology this problem is commonly termed equifinality (Beven, 1993, 1996, 2001), meaning that different parameter combinations can provide equally good (or poor) model fits. This implies that an adequate model performance may give reasonable results for the wrong reasons. In short, tidal water levels alone are not sufficient to impose a strong constraint on the calibration parameters. However, if we add information on the tidal velocity, the additional constraint will allow a more accurate calibration of the hydraulic model and, as a result, a lower predictive uncertainty.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



with an error margin smaller than 10 min. The method has big potential, and further improvements and refinements are still possible.

The core of the paper consists of a detailed description of the method, including the statistical procedure, which derives an estimate of the time of slack from GPS observations of position. We present a case study of a successful field test using buoy 18 in the Scheldt estuary, see Fig. 1, which subsequently we validated by means of ADCP-measurements taken one day later at nearly the same spot.

The Scheldt Estuary is the area between Breskens/Vlissingen and Gent. The estuary is 50 m wide near Gent and this increases to 5 km at Vlissingen (see Fig. 1). Furthermore, it is the only connection between the ports of Terneuzen, Gent and Antwerp and the North Sea. The port of Antwerp is the second largest port of Europe, ranked by the total freight shipping. The shipping lanes of the estuary are permanently dredged and monitored to ensure a safe entrance for vessels with a deep draft. About 2.2 billion m³ of water flows in and out of the estuary during a tidal period. The river discharges about 5.5 million m³ per tidal cycle, which is small compared to the tidal volume. This implies that the Scheldt Estuary is tide dominated.

2 Measuring moment of slack tide

There is a wide variety of instruments designed for the measurement of water currents. Propeller based water current measurement instrument are relatively cheap but provide solely information on the exact location of the instrument and it has moving parts. An ADCP (Acoustic Doppler Current Profiler) provides detailed current information throughout the entire water column, but has to be installed at a fixed platform, which may be not at hand at the desired location.

By installing a system on an Anchored Aid TO Navigation (ATON) buoy, solves the requirement for a fixed location. A first attempt to estimate slack tide using a GPS receiver on an anchored ATON buoy is described in Lievens (2010). Hereby, the potential of a GPS-buoy to observe the moment of slack tide in estuaries is shown.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

We will observe the motion of an anchored buoy, due to water current (and wind and waves), with GPS, in order to determine the very moment the water flow in the estuary changes its direction due to tide (slack tide). Advantages of using a GPS receiver for this purpose are that the receiver (which is fairly lightweight equipment) can be fit easily onto an existing buoy, and the sensor has no parts in or under water. The measurements can be done autonomously and remotely by the receiver (no infrastructure needed on shore). The receiver operates with moderate power consumption (just a solar panel and battery would be sufficient for power supply). With the measurements, the moment of slack tide – as we outline in the following sections – can be determined in (near) real-time. The better than 10 min accuracy can be achieved with an equipment cost on the order of 1 kEuro (hence affordable), namely a middle-class single frequency, SBAS-enabled, GPS receiver.

3 GPS for hydrology

So far, GPS measurements have hardly been used for water-flow information. The use of GPS on buoys for hydrology concerns water level and water circulation. The concept of deriving hydrological information from GPS observations on anchored and drifting buoys is developed in the last two decades. It is applied to the measurement of the vertical tide and water level, tsunami detection, wave-height, and the measurement of the incident angle of tidal waves, and near shore current.

The observation of the vertical tide with GPS-buoys is described by Nagai et al. (2004); DeLoach (1995). These methods involve a specially designed measurement buoy and an accurate GPS position solution, derived via relative positioning. The observed height of the buoy is then (frequency) filtered and related to the relevant datum. This results in an observed tidal elevation in a difficult accessible environment. Water level measurements with GPS in a river and a lake are reported about for instance by Moore et al. (2000); Cheng (2006); Apel et al. (2011).

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)

Another application is the detection of approaching tsunamis. The method of an experimental system is presented by Kato et al. (2001) which relies on one measurement buoy. An alternative implementation is presented by Kato et al. (2000) which makes use of two buoys: a support and a sensor buoy. The latter is insensitive for wind-waves.

A complete implementation is described by Nagai et al. (2006), the system consists of a GPS-buoy, fixed GPS base station and a tsunami detection algorithm.

An example of measuring wave-height and direction is presented in Harigae et al. (2004). The measurement of the wave direction of a gravity wave with GPS-buoys is described by Yoo et al. (2004). The wave direction is measured with an arrayed GPS-buoy configuration. The principle relies on the measured phase difference of the tidal wave between the different GPS-buoys.

Near-shore currents are measured with a drifting GPS-buoy by Schmidt et al. (2003). The methodology is based on deriving the current information from the trajectory of the buoy. The information is then applied in an analysis of sediment transport and distribution of pollutants. A similar application, as to study the circulation in a lake or a bay due to wind for instance, is described in Pous et al. (2004).

4 GPS positioning

The basic principle of positioning with GPS consists of observing distances to satellites. The distance from a satellite to a receiver on, or near the Earth's surface, is obtained by measuring the travel-time of a radio-signal, transmitted by a satellite, and multiplying this by the speed of light. The position of the receiver can be determined in three-dimensional geometry from three observed distances. The satellite positions are known from the navigation-messages broadcast by the satellites. The fact that the clock in the receiver is generally not synchronized with the time of the GPS system (as maintained by atomic clocks, as on board of the satellites) complicates the process of measuring the travel-times (and hence distances). When the receiver clock lags behind, or runs ahead, all distances will be measured systematically too short, or too long.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

By observing simultaneously also a fourth satellite, the receiver can determine the offset of its clock, and account for this. This mode of positioning is known as single point, or standalone positioning with pseudorange measurements. For an instantaneous position solution, at least four satellites need to be observed simultaneously. The position accuracy lies, under favorable circumstances, in the order of 5–10 m.

The major error sources with GPS single point positioning are the satellite clock and the satellite position (the information on these given in the navigation message is accurate at the few meter level), delays of the radio-signal in the Earth's atmosphere (these delays in the ionosphere and troposphere can range from several meters to tens of meters), multipath (reception of signals which have been reflected against objects as buildings and cars, and hence have travelled a longer distance) and finally receiver (thermal) noise. For further details we refer to textbooks, as Misra and Enge (2006).

With single point positioning, errors in the broadcast satellite position and clock, and delays of the radio-signals in the Earth's atmosphere propagate directly into the position solution. For two receivers on Earth relatively close together however, these errors are largely similar. One could exploit this in order to position GPS receivers – not too far apart – with respect to each other. This is the basic concept of relative positioning (or Differential positioning). The position accuracy can thereby be improved to the meter-level, and ultimately to the centimeter-level (depending on the distance between the receivers, and also on the type of measurements by the receivers, see below). The above mentioned multipath-effects can be reduced by careful antenna-site selection, antenna design, and receiver signal processing. With regard to receiver noise, two types of range-measurements can be made by a receiver: pseudorange code measurements, with an accuracy ranging from several meters to decimeters (low and high-end equipment respectively), and carrier phase measurements, with an accuracy at centimeters or millimeters even (generally with middle-class and high-end equipment).

In the sequel we will use Satellite Based Augmentation System (SBAS)-positioning. This is differential positioning with respect to a network of so-called reference stations across Europe, the European Geo-stationary Navigation Overlay Service (EGNOS).

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

The network of GPS receivers provides corrective information (relayed in real-time through a geo-stationary satellite) with regard to satellite position, clock and ionospheric delay. The primary measurement at the user is the pseudorange (observed on a single frequency, L1, obtained with a middle-class GPS receiver). The resulting position accuracy is at the submeter to one meter level. The measurements in our study have been processed in EGNOS-mode using the Pegasus software (Butzmuehlen et al., 2001), after the fact, but this can also be done in real-time by the receiver.

As a ground-truth we employ carrier-phase based Differential GPS in this experiment: the (high-end) receiver on the buoy is positioned – using the cm-accurate (dual-frequency) carrier phase measurements – with respect to a stationary GPS receiver, nearby on the shore (just 1.5 km away). The resulting position accuracy is at the few centimeter level. The measurements have been processed in carrier-phase based Differential GPS mode with in-house developed software, see Buist (2013).

5 GPS measuring campaign on buoy

As outlined in the introduction, the measurement campaign took place on a buoy in the Westerscheldt estuary, from 1–5 July 2011. The receiver and antenna were installed on the buoy, see Fig. 2, and recollected after one week. The (high-end) Trimble R7 receiver on the buoy measured and logged for 100 h (at a 1 s interval) before the (28 Ah) battery was completely drained, covering 8 full tidal cycles, while the base station on shore (for the ground-truth) logged for the complete time interval.

A high-end dual-frequency GPS receiver was used in this experiment in order to allow also for a reconstruction of the ground-truth trajectory of the buoy with centimeter accuracy. For the (operational) results presented here, only the single frequency measurements were used. It has been verified that similar performance can be obtained with a middle-class (single frequency) GPS receiver with an equipment cost in the order of 1 kEuro, see Appendix.

The measurement campaign took place under rather favourable weather conditions; fairly typical Summer weather in the Netherlands. The wind varied between 2 and 10 ms^{-1} , and gradually moved from North-North-West to East-South-East over the 5 days of the campaign.

The three-dimensional (cm-accurate ground-truth) position solutions for the buoy are presented in terms of a local North, East and Up system, and shown in the East-North plane in Fig. 3, with the height color-coded, to see the tidal elevation, which changes – peak-to-peak – by about 4 m. In Fig. 3 the motion is shown only for one full tidal cycle; the path of the buoy is similar for the eight observed tidal cycles.

The track of the buoy is a result of various forces. The motion in Fig. 3 appears to be influenced by one dominant current direction. The buoy is located – close to the town of Terneuzen – in a so-called ebb channel, and separated from a short-circuit channel which connects the ebb and flood channel and other disturbing factors.

6 New method to determine slack tide

In this section a sequence of measured GPS positions of the buoy are converted into an estimate for the time moment of slack tide. The approach taken is a purely geometric one; it does not require any modeling of the buoy dynamics. Basically we map the three-dimensional motion into a single dimension along the dominant water current direction; the coordinate in this single dimension is referred to as the extension. Next – in its simplest form – a mechanism is proposed which decides, each time on the basis of a single position solution (extension), whether the buoy is already beyond its “slack moment” – position or not. The first occurrence of passing through the “slack moment” – extension delivers the epoch of slack tide moment.

The first subsection describes the necessary assumptions. Principle component analysis is applied in Sect. 6.2 to simplify the buoy’s motion from a (local horizontal) two-dimensional position to a one-dimensional extension in the dominant current direction. The third subsection describes a method to determine the centre position,

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



i.e. the point of zero extension. Then we show how the “slack tide” position is set. Finally we outline the decision strategy to determine the moment of slack tide, based on observed GPS positions.

6.1 Assumptions with regard to reduction of dimension

5 The buoy is subject to different forces. Not only the tidal current, in which the interest lies, is responsible for the motion of the buoy. Forces are also delivered by wind induced waves, creating a high frequency oscillating motion in all three directions. The influence of the wind on the path of the buoy can be neglected according to Lievens (2010). A low frequency oscillating motion in the (local) upward direction is caused by the tidal elevation. Finally, the chain produces a counter-force to keep the buoy in its position. 10 The track of the buoy as a result of these forces is indicated in Fig. 3.

First, the motion in the local vertical direction is neglected. Although it contains information about the tidal elevation, and the (significant) wave height, it is not of interest for the tidal current. Besides, due to the (relatively) small amplitude (± 2 m), it cannot be 15 measured with sufficient accuracy using a non high-end GPS receiver. The proposed equipment and mode of positioning (SBAS) delivers an accuracy at the submeter level at best.

Secondly, it is assumed that there is one dominant direction in the motion of the buoy. This can be verified and determined for instance during a calibration campaign of a few tidal cycles. Deviations could be caused by an opposite Coriolis force on the 20 ebb and flood current, morphological interaction, inertial and gradient effects (Stive and Bosboom, 2011). In the area of interest “de Pas van Terneuzen”, the assumptions turned out to be well valid. The direction of both the ebb and flood stream varies with a maximum of only 5° (Rijkswaterstaat, 2011). This was also confirmed in our measurement campaign on buoy 18 (see Fig. 3). The largest motion (± 80 m) is observed 25 in one direction. This is the dominant current direction.

In perpendicular direction only a small motion can be observed. This motion is caused by a complex system of forces and is not of interest for the tidal current.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Therefore, it is possible to simplify the buoy motion from two to one dimension without losing “information” with regard to the tidal current. The methodology is described in the next subsections.

6.2 Principle component analysis: estimation of the dominant current direction

The central idea of principal component analysis (PCA) is to reduce the dimensionality of a data set of interrelated (random) variables, while retaining as much as possible of the variation present in the data set. The dataset is transformed into a new set of variables, referred to as the principle components. The principle components are uncorrelated and ordered so that the first few retain most of the variation present in all of the original variables (Jolliffe, 2002).

This principle is used to transform a two-dimensional horizontal position of the buoy into a one-dimensional extension. It is assumed that the first principle component describes the extension of the buoy due to the dominant current direction. Given a set of points in Euclidean space, the first principal component corresponds to a line that passes through the multi-dimensional mean and minimizes the sum of squares of the distances of the points to the line (Pearson, 1901).

Matrix \mathbf{X} is an $n \times p$ matrix of n centralized observations of p attributes (Teunissen et al., 2005). In this particular case there are two attributes ($p = 2$): the East and North coordinates of the buoy. Matrix \mathbf{X} consists of a vector of East coordinates \mathbf{e} , and a vector of North coordinates \mathbf{n} , which are both subtracted with their mean value.

$$\mathbf{X} = [\mathbf{e} \ \mathbf{n}] \quad (1)$$

Now we determine the eigenvalue decomposition of the 2-by-2 empirical variance matrix of the horizontal positions, $\mathbf{Q}_{\mathbf{xx}} = \mathbf{U}\mathbf{\Lambda}\mathbf{U}^T$. $\mathbf{\Lambda}$ is the diagonal eigenvalue matrix (with eigenvalues $\mathbf{\Lambda}_1, \dots, \mathbf{\Lambda}_n$ along the diagonal), and \mathbf{U} the matrix of unit eigenvectors (Teunissen et al., 2005).

The eigenvectors point in the principal axes directions of the ellipse associated with variance matrix $\mathbf{Q}_{\mathbf{xx}}$ (and an assumed two-dimensional normal distribution), and the

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



eigenvalues give the lengths of the principal axes (Teunissen et al., 2005). The principal components \mathbf{Y} of the dataset in matrix \mathbf{X} are now defined as:

$$\mathbf{Y} = \mathbf{X} \cdot \mathbf{U} \quad (2)$$

5 The first column of $n \times p$ matrix \mathbf{Y} consists of the variation in the direction of the first principle component, that is, the extension, with regard to the empirical mean, in the dominant current direction. The second column can be seen as the residuals after the (coordinate) transformation (it is the motion in the direction perpendicular to the dominant current direction). In the experiment, the residuals (over the full campaign)
10 had zero mean, and a standard deviation of about 2.5 m.

6.3 Determination of the centre point

The anchor position of the buoy is an important parameter for the estimation of the moment of slack tide. It defines the centre point, i.e. the point of zero extension. Anchor positions may be available in a database, but the accuracy is often insufficient
15 (Lievens, 2010). Also in this case it appears that the given anchor position is biased. Therefore, an alternative for the estimation of the centre point is proposed, by means of a calibration.

The previous section results in an extension of the buoy with regard to the estimated dominant current direction. However, as indicated, this extension is related to the empirical mean. This empirical mean (over time) does however not represent the point of zero extension. Due to asymmetry of the tidal current, the buoy remains (time-wise)
20 longer in the ebb stream than in the flood stream, see also Fig. 3, where the mean is at (0,0). Therefore the ordinary time average (empirical mean) of the extensions results in a centre position that is shifted in the direction of this ebb stream. This problem is
25 also described by Lievens (2010).

The following method holds under the assumption that the position data are previously screened and outliers – if any – are removed from the dataset. The extension is observed during a number of tidal cycles n , for instance in a calibration campaign. For

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



each complete tidal cycle, denoted by the subscript i , the maximum extension e_i^{\max} and the minimum extension e_i^{\min} are determined. Since multiple tidal cycles are observed, creating redundancy, the average centre point \bar{c} is given by:

$$\bar{c} = \frac{1}{n} \sum_{i=1}^n \frac{e_i^{\min} + e_i^{\max}}{2} \quad (3)$$

In the experiment with buoy 18, the shift was found to be slightly over 7 m. The centre-point \bar{c} was found to lie – along the principle axis – about 7 m to the high-water side, with respect to the empirical mean.

This method, with redundancy present, also enables quality control of the estimated centre point. The variation in the centre point, obtained from different (individual) tidal cycles, can be analysed.

The tidal elevation does influence the maximum extension in the local horizontal direction. Figure 4 shows a schematic representation of the situation. With the application of Pythagoras' theorem the maximum amount of extension for high and low water can be calculated following a purely geometric reasoning. The following dimensions for buoy 18 are used: the length of the chain l_{chain} is 40 m (J. van Espen, personal communication, 2011), the draft of the buoy equals approximately 1 m, the water depth with respect to national datum NAP z equals 16 m, and a tidal amplitude t equals approximately 2 m (Rijkswaterstaat, 2011). This results in a maximum extension for low water e_{lw} of 38.5 m and for high water e_{hw} 37.0 m. The difference in maximum extension, due to the difference in tidal elevation equals 1.5 m in case of a progressive tidal wave. The tidal elevation effect can be largely neglected in the determination of the centre point using Eq. (3) in our case, as the tidal wave in the Westerscheldt estuary is of a mixed type. There is a serious offset between the moment of maximum current and maximum elevation. In our case there is only little tidal elevation at maximum current.

From now on, we will use the measured extension (see Fig. 5) of the buoy with respect to the centre-point found in this subsection, which is an estimate for the actual anchor position.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



6.4 Slack tide position

With reference to Fig. 4 we determine, in a purely geometric way, the extension at the moment of slack tide. The idea is that the chain extends – over the seafloor – from the anchor to the position of the buoy (position 2 in the sketch). In this situation there is no net force, and the water current is reversing its direction.

Now the following holds:

$$e_{st} = l_{chain} + d_{buoy} - z - t \quad (4)$$

with e_{st} the extension at the moment of slack tide (related to high or low water slack), l_{chain} the length of the chain, d_{buoy} the draft of the buoy, z is the depth with respect to datum (NAP), and t the elevation during HW slack or LW slack.

The above Eq. (4) results in two different values of e_{st} , one for the extension at the moment of slack tide for high water, and one for low water, because of the difference in tidal elevation at those moments.

Now we supply figures specifically for the measurement campaign at the Westerscheldt. As stated in the first subsection the length of the chain l_{chain} is set to 40 m for buoy 18. The water depth related to NAP z is obtained from a hydrographic chart and is 16 m. The draft of the buoy d_{buoy} is derived by a simple displacement calculation and is set to 1 m.

The tidal elevation at the expected moment of slack tide, which is approximately 60 min after high or low water, is respectively +2.3 m and –1.8 m. Now the extension for the moment of high water slack is: $e_{st}^{hw} = 40 + 1 - 16 - 2.3 = 22.7$ m, and for low water slack: $e_{st}^{lw} = 40 + 1 - 16 + 1.8 = 26.8$ m (actually $e_{st}^{lw} = -26.8$ m, as the extension with high water is set positive).

It is noted that the dimensions given above carry some uncertainty, and this uncertainty is taken into account as well, in the next subsection.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

6.5 Variance of extension observable

In the next subsection the observed extension of the buoy is compared to the slack-tide extension, and a decision is taken on whether one is larger or smaller than the other. The variables involved carry uncertainty, and this uncertainty is modeled through a variance of the extension in this subsection.

The variance σ^2 of the extension consists of three components: the variance of the GPS position observable σ_{gps}^2 , the (short term) buoy motion that is *not* related to the current σ_{bd}^2 , the buoy-dynamics to say, and the uncertainty of the extension that is related to the (definition of the) moment of slack tide σ_{est}^2 ; this extension was determined in the previous subsection. Under the assumption that these effects are independent, straightforward error propagation can be applied

$$\sigma^2 = \sigma_{\text{gps}}^2 + \sigma_{\text{bd}}^2 + \sigma_{\text{est}}^2 \quad (5)$$

The standard deviation for the extension as observed with GPS follows directly from the GPS equipment and the mode of operation. They can be determined for instance by occupying a station on shore with known position for 24 h, as for instance done in the Appendix. With a middle-class to high-end receiver and a decent antenna we found values in the order of several decimeters, when we use the SBAS/EGNOS mode of operation. In this case we used $\sigma_{\text{gps}} = 0.34$ m, for the extension based on a single position solution.

The cm-accurate ground-truth positions for the buoy in the experiment allow us to analyse the short term (random) buoy motion, as the buoy motion will be much bigger than the centimeter uncertainty in the GPS position solution. Figure 6 shows the extension of the buoy during a period of zero net movement. The buoy is in the ebb extreme extension, and slightly hovering around due to wind and wind induced waves, and in particular tilting due to these effects (and the GPS antenna is attached to the top of the buoy for good signal reception). From these measurements the standard deviation about the (unknown) mean is determined $\sigma_{\text{bd}} = 0.35$ m.

13758

HESSD

10, 13743–13782, 2013

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

The standard deviation of the extension that is related to the moment of slack tide e_{st} relies on the standard deviations of the chain length, the draft of the buoy, the charted depth and the tidal elevation. No a-priori information is available on these, and therefore we have to come up with reasonable estimates ourselves. The standard deviation of the chain length is assumed to be 0.2 m, which is approximately the length of one shackle. The draft of the buoy is calculated using the shape and weight of the buoy, and is estimated at $\sigma_{d_{buoy}} = 0.2$ m. The average tidal elevation for an a-priori defined moment of slack tide is known with a precision of $\sigma_t = 0.1$ m. The precision of the charted water depth at the location of the buoy is influenced by many parameters. The most important are the accuracy of the anchor position in combination with the morphology, the dynamics of the morphology in combination with the acquisition time and the measurement technique. The standard deviation of the charted depth σ_z is assumed to be 0.3 m.

Assuming these effects to be independent, application of error propagation yields

$$\sigma_{e_{st}}^2 = \sigma_{l_{chain}}^2 + \sigma_{d_{buoy}}^2 + \sigma_z^2 + \sigma_t^2 \quad (6)$$

resulting in $\sigma_{e_{st}} \approx 0.42$ m.

Now the values for $\sigma_{e_{st}}$, σ_{bd} and σ_{gps} have been determined, they are combined, according to Eq. (5), in a total standard deviation $\sigma = 0.62$ m, necessary for hypothesis testing in the next subsection. The uncertainty in the determined centre point (at or below 0.1 m) can be neglected – this determination is based on multiple observations, cf. Eq. (3).

6.6 Hypothesis testing

The estimation of the slack tide moment is based on GPS measurements of the position of the buoy. The observed position is not perfect, due to (GPS) measurement noise, oscillating behavior due to wind and waves, and uncertainty in the (defined) slack tide extension. The decision whether the buoy is, when in transition from flood to

6.7 Significance level α

Uncertainty in the variable on the basis of which we take the decision, inevitably leads to non-zero probabilities of incorrect decision, as already suggested in Fig. 7. There is the probability that in reality the buoy has not yet passed the slack-tide position, but that nevertheless it is decided that it has; this is a false alarm indicated by α . And there is the probability that in reality the buoy has passed already the slack-tide position, but that the decision reads that it has not; this is a missed detection indicated by β . Both occurrences are undesirable, and a trade-off has to be found through the critical value/decision threshold. In the example of Fig. 7 the threshold can be moved to the left, thereby reducing the probability of false alarm, but it comes at the cost of a larger missed detection probability, and a larger detection delay.

In Fig. 8 the detection delay is shown as a function of the level of significance α (false alarm probability) for various GPS receivers and operating modes. Different GPS receivers (and operating modes) lead to different values of σ_{gps} in Eq. (5). The analysis of Fig. 8 is based on the motion of the buoy (extension) as a function of time, which we obtained from averaging the cm-accurate ground-truth trajectories over several tidal cycles, and assuming a normal distribution for the extension as in Eq. (7).

Figure 8 clearly shows the relation between the significance level and the detection delay for different GPS-equipment and operating modes. The high-end Trimble R7 in RTK-mode shows the best results, that is, the smallest detection delay for all significance levels α . For the Garmin GPS 76C(S)x handheld receiver in SBAS-mode the detection delay is almost four times longer compared to the results obtained with the Trimble. The difference in detection delay between the Trimble R7 in RTK-mode and the single frequency Septentrio AsteRx1 receiver in SBAS mode is small, for both antennas. This can be explained by the fact that the contribution to the uncertainty due to the GPS-measurements can be neglected compared to the other sources, see Eq. (5). Therefore the optimum of performance and economy, seems to be reached

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

by the middle-class receiver, capable of delivering decimeter accurate pseudorange measurements, operating in SBAS/EGNOS mode.

To conclude the analysis of the detection performance Fig. 9 shows the probability of (correct) detection γ as a function of the detection delay. This graph is based on a significance level of $\alpha = 0.05$ (corresponding to a probability of (correct) detection of 0.05 at a zero detection delay, where the observed extension equals the defined slack-tide extension), and the averaged buoy extension as a function of time (from the ground-truth) as input. The probability of detection γ increases from approximately zero to one in approximately 400 s.

6.8 Determination of phase lag

The main goal of this research is the estimation of the moment of slack tide. When the moment of slack tide is related to tidal elevation, we can determine the phase lag. The previous subsections relate positions to the moment of slack tide. The time tag associated with the first position which is found to be beyond the slack-tide position gives the slack-tide moment in time, denoted respectively by m_{hws} and m_{lws} . The phase lag for high water is defined as follows:

$$\epsilon_{hw} = m_{hws} - m_{hw} \quad (9)$$

And for low water:

$$\epsilon_{lw} = m_{lws} - m_{lw} \quad (10)$$

In this study tidal elevation data from a nearby on-shore measurement station in Terneuzen is used to determine the moment of high and low water, under the assumption that the tidal elevation of buoy 18 is equal to that of Terneuzen. With application of Eqs. (9) and (10) the high and low water phase lags are determined.

HESSD

10, 13743–13782, 2013

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

7 Results and discussion

Figure 10 shows the estimated phase lags for high and low water at water surface at the location of buoy 18 on 1–5 July 2011. The results are based on the Trimble R7 measurements obtained on buoy 18 which are processed in EGNOS-mode using the Pegasus software (Butzmuehlen et al., 2001), after the fact. This implies that the accuracy of the processed results are equivalent to that of the proposed medium-range receiver i.e. the Septentrio AsteRx1 in combination with a survey antenna operating in EGNOS-mode and a significance level α of 0.05.

The average of the 8 observed high water phase lag e_{hw} is 71 min. This is slightly longer than the average low water phase lag e_{lw} of 67 min. A slight difference in phase lag for high- and low water is expected, which is caused by the complex tidal propagation in estuaries. This difference is also described by Haas (2007).

The observed phase lags in the 1–5 July period show a standard deviation σ about the mean of 4.7 min for the high water phase lag based and 7.5 min for the low water phase lag, both are based on 8 observations. This holds under the assumption that the duration of the phase lag, for the five measurement days, is constant.

A significant part of this standard deviation is caused by the determination of the moment of high or low water and not by the moment of slack tide. The standard deviation of the estimated moment of slack tide is likely to be better than this.

Finally we provide argumentation why the proposed method works in terms of position, rather than velocity. In Fig. 11 the extension, smoothed velocity and acceleration of the buoy during the observed tidal cycles are plot as a function of time. The figure shows also the smoothed mean average for the position, velocity and acceleration (red line). For the velocity the individual tracks are smoothed with a moving average filter (blue lines) in order to reveal a trend in the velocity. The observed velocity is much noisier, and shows velocities up to 3 m s^{-1} . This is due to the three-dimensional oscillatory motion of the buoy. The maximum smoothed velocity is in the order of $1\text{--}3 \text{ cm s}^{-1}$, and is observed during the transition of the buoy. This low average velocity causes the

HESSD

10, 13743–13782, 2013

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

tidal current being buried in the noise by the oscillating motion of the buoy, and measurement noise in case of a low or medium performance GPS receiver. This makes a detection based on velocity extremely difficult, therefore our method is based on position.

8 Validation

The validation is based on a comparison of the phase lag estimated with the proposed GPS method on 1–5 July 2011, against a ADCP measurement campaign performed by a survey vessel operated by Rijkswaterstaat on 6 July 2012. During the measurement campaign of Rijkswaterstaat the survey vessel sailed for 12 h survey lines across the channel (“Pas van Terneuzen”). The interval between the subsequent passes through the channel was around 10 min, due to the small channel width. The result is a detailed current observation through the entire water column of the channel with a time resolution of approximately 10 min, see Fig. 12. This cross section was 1 km to the east of buoy 18.

We have chosen a point in the cross section similar to that of buoy 18, i.e. same depth and equal distance to the channel bank, and assumed that the results are similar. In addition the channel width is similar at the the location of buoy 18 and the location of the ADCP measurements. Using a linear interpolation technique we obtained a continuous current velocity for this point.

Based on this data and the observed water level we obtained a phase lag for high water e_{hw} of 68 min and for low water e_{lw} of 65 min. The average estimated phase lags from buoy 18 are in close agreement with the ADCP results. The difference is 3 min for high water, and 2 min for low water.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

9 Conclusions

The goal of this study was to investigate opportunities for the measurement of slack moments in tidal estuaries with affordable GPS equipment on an anchored buoy. Satellite Based Augmentation System (SBAS) GPS positioning was found to deliver a sufficient position accuracy, while at the same time allowing a simple implementation. A middle-class GPS receiver with SBAS-capability and a good antenna can deliver positions at the sub-meter level.

A measurement campaign was carried out, using a buoy in the Westerscheldt estuary. The buoy showed – in horizontal direction – primarily a one dimensional motion, along the dominant water current direction. Next, using a purely geometric approach, the high tide and low tide slack positions of the buoy were set. The uncertainty in these slack positions is less than half a meter.

In operational mode, possibly in real-time, based on the GPS measurements, and employing statistical hypothesis testing, the moment of slack is determined. Taking all uncertainties into account, analysis showed that the moment of slack is detected within 300 s, in over 99.9% of the cases. On average the detection delay is about 2 min. Together with the moments of high and low water, the phase lag was analyzed over 8 consecutive tidal cycles, and the variation of the phase lag was 4.7 min for high water, and 7.5 min for low water, expressed in terms of standard deviation about the mean. Part of this variation is caused by uncertainty in the moments of high and low water, and therefore the moment of slack is expected to have an even better accuracy, also it is not sure if the phase lag should be constant.

The obtained phase lags were externally verified, by comparison against Acoustic Doppler Current Profiler (ADCP) measurements. The average phase lags from GPS were in close agreement with the ones from ADCP; differences were at the few minutes only.

In this contribution, it has been demonstrated that deriving the moment of slack tide from GPS measurements on an anchored buoy is feasible, with an accuracy of better

HESSD

10, 13743–13782, 2013

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



than 10 min, using affordable equipment. In the implementation presented here the high and low water levels – at the dm-level – are needed as additional information. For determination of phase lags, additionally the moments (in time) of high and low water are required at the location of the buoy.

10 Outlook

The proposed system is designed to be easily implemented in estuaries around the globe, since the system only relies on the availability of ATON buoys, which are widely available. This creates opportunities for the study and monitoring of the tidal propagation in estuaries

In an estuary of interest this system should be installed on buoys across the longitude cross-section. The number of equipped buoys determines the spatial resolution of the observed slack tide. For each individual buoy the following information should be acquired: the length of the anchor chain, the draft of the buoy, the vertical tidal amplitude during the measurements at the location of the buoy, and the water depth at the approximate location. Before the system is fully operational, the dominant current direction should be found by an analysis of the buoy's motion during several tidal cycles.

The system could be implemented for a short time period, for example to measure the phase lag throughout the longitudinal cross-section of the estuary. However, a permanent system is more suitable for the observation of long time varying effects and enhances the situational awareness of mariners navigating through the estuary, which improves the safety and efficiency of maritime commerce and coastal resource management.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Appendix

Accuracy of a middle-class GPS receiver

The positioning performance of the proposed middle-class single frequency GPS receiver in SBAS/EGNOS mode, is demonstrated in Fig. A1, using an accurately known location. Also the impact of the antenna choice is shown, a survey antenna at top and a simple patch antenna at bottom. In Sect. 6.5 the standard deviation of the extension of the buoy observed with GPS was set to $\sigma = 0.34$ m.

Acknowledgements. The company Multraship based in Terneuzen is acknowledged for their support with the pilot on the Westerscheldt. Also the support of the national Rijkswaterstaat (RWS) agency, part of the Ministry of Infrastructure and the Environment, through its regional service Zeeland, based in Middelburg, is much appreciated. In addition colleagues Peter Buist and Peter de Bakker, as well as students Wouter Berghuijs and Bart van Osnabrugge are acknowledged. Financial support for publication of this paper by the TU Delft Library – under grant Open Access 78354 – is also acknowledged. Finally, The company Seaway Heavy Lifting Engineering is acknowledged for providing the opportunity to finish this paper.

References

- Apel, H., Hung, N., Thoss, H., and Schöne, T.: GPS buoys for stage monitoring of large rivers, *J. Hydrol.*, 412–413, 182–192, 2011. 13748
- Beven, K.: Prophecy, reality and uncertainty in distributed hydrological modelling, *Adv. Water Resour.*, 16, 41–51, 1993. 13744
- Beven, K.: Equifinality and uncertainty in geomorphological modelling, in: *The Scientific Nature of Geomorphology: Proceedings of the 27th Binghamton Symposium in Geomorphology*, 27–29 September 1996, Vol. 27, John Wiley & Sons, 289 pp., 1996. 13744
- Beven, K.: How far can we go in distributed hydrological modelling?, *Hydrol. Earth Syst. Sci.*, 5, 1–12, doi:10.5194/hess-5-1-2001, 2001. 13744
- Buist, P.: Multi-platform integrated positioning and attitude determination using GNSS, Ph. D. thesis, Delft University of Technology, 2013. 13751

13767

HESSD

10, 13743–13782, 2013

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)

- Butzmuehlen, C., Stolz, R., Farnworth, R., and Breeuwer, E.: PEGASUS-prototype development for EGNOS data evaluation-first user experiences with the EGNOS system test-bed, in: Proceedings of the 2001 National Technical Meeting of the Institute of Navigation, 628–637, 2001. 13751, 13763, 13779
- 5 Cheng, K.: Analysis of water level measurements using GPS, Ph. D. thesis, the Ohio State University, 2006. 13748
- DeLoach, S.: GPS Tides: A Project to Determine Tidal Datums with the Global Positioning System, Army Topographic Engineering Center Alexandria VA, 1995. 13748
- Haas, J.: Phase lags in alluvial estuaries, Master's thesis, TU Delft, 2007. 13763
- 10 Harigae, M., Yamaguchi, I., Kasai, T., Igawa, H., Nakanishi, H., Murayama, T., Iwanaka, Y., and Suko, H.: A low-cost GPS-based wave height and direction sensor for marine safety, in: Proceedings of the 17th International Technical Meeting of the Satellite Division of The Institute of Navigation (ION GNSS 2004), 1234–1245, 2004. 13749
- Jolliffe, I.: Principal Component Analysis, Vol. 2, Wiley Online Library, 2002. 13754
- 15 Kato, T., Terada, Y., Kinoshita, M., and Kakimoto: Real-time observation of tsunami by RTK-GPS, Earth Planets Space, 52, 841–846, 2000. 13749
- Kato, T., Terada, Y., Kinoshita, M., Kakimoto, H., Isshiki, H., Moriguchi, T., Takada, M., Tanno, T., Kanzaki, M., and Johnson, J.: A new tsunami monitoring system using RTK-GPS, in: US National Tsunami Hazard Mitigation Program Review and International Tsunami Symposium, 7–10, 2001. 13749
- 20 Lievens, M.: Observing tidal slack in the Scheldt estuary, Master's thesis, TU Delft, 2010. 13747, 13753, 13755
- Misra, P. and Enge, P.: Global Positioning System: Signals, Measurements and Performance, 2nd Edn., Ganga-Jamuna Press, Lincoln, MA, 2006. 13750
- 25 Moore, T., Zhang, K., Close, G., and Moore, R.: Real-time river level monitoring using GPS heighting, GPS Solut., 4, 63–67, 2000. 13748
- Nagai, T., Ogawa, H., Terada, Y., Kato, T., and Kudaka, M.: GPS buoy application to offshore wave, tsunami and tide observation, in: Coastal Engineering Conference, Vol. 29, 1093 pp., 2004. 13748
- 30 Nagai, T., Kato, T., Moritani, N., Izumi, H., Terada, Y., and Mitsui, M.: Offshore tsunami monitoring network design using GPS buoys and coastal on-site sensors, in: Coastal Engineering Conference, Vol. 30, 1529 pp., 2006. 13749

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[◀](#)

[▶](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



- Pearson, K.: LIII. on lines and planes of closest fit to systems of points in space, *Philos. Mag.*, 6, 559–572, 1901. 13754
- Pous, S., Carton, X., and Lazure, P.: Hydrology and circulation in the Strait of Hormuz and the Gulf of Oman – results from the GOGP99 experiment: 1. Strait of Hormuz-art. no. C12037, *J. Geophys. Res.-Oceans*, 109, 42–56, 2004. 13749
- Rijkswaterstaat: Presentatie Meetresultaten: debiet – sediment – OSM meting, Tech. rep., 2011. 13753, 13756
- Savenije, H.: Lagrangian solution of St. Venant's equations for alluvial estuary, *J. Hydraul. Eng.*, 118, 1153–1163, 1992. 13745
- Savenije, H.: *Salinity and Tides in Alluvial Estuaries*, Elsevier LTD., 2005. 13745
- Savenije, H., Toffolon, M., Haas, J., and Veling, E.: Analytical description of tidal dynamics in convergent estuaries, *J. Geophys. Res.*, 113, C10025, doi:10.1029/2007JC004408, 2008. 13745
- Schmidt, W., Woodward, B., Millikan, K., Guza, R., Raubenheimer, B., and Elgar, S.: A GPS-tracked surf zone drifter, *J. Atmosph. Ocean. Tech.*, 20, 1069–1075, 2003. 13749
- Stive, M. and Bosboom, J.: *Coastal Dynamics*, VSSD, 2011. 13753
- Teunissen, P., Simons, D., and Tiberius, C.: *Probability and Observation Theory*, Department of Earth Observation and Space systems, Faculty of Aerospace Engineering, Delft University of Technology, 2005. 13754, 13755
- Toffolon, M. and Savenije, H.: Revisiting linearized one-dimensional tidal propagation, *J. Geophys. Res.*, 116, C07007, doi:10.1029/2010JC006616, 2011. 13745
- Van Veen, J.: Ebb and flood channel systems in the Netherlands tidal waters, *Koninkl. Ned. Aardrijkskundig Genootschap*, 67, 303–325, 1950. 13745
- Yoo, Y., Hou, D., Kouguchi, N., Ishida, H., Shiotani, S., Fujii, H., and Deguchi, I.: Arrayed GPS-buoys wave observation system, in: *OCEANS'04. MTS/IEEE TECHNO-OCEAN'04*, IEEE, 3, 1370–1375, 2004. 13749

HESSD

10, 13743–13782, 2013

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.



Fig. 1. Overview of the Westerscheldt estuary, the small map in the left corner indicates the location of Westerscheldt estuary in Western Europe with a red rectangle. The complexity of this alluvial estuary is shown with this aerial photograph. The position of buoy 18 is indicated by a red arrow, near the town of Terneuzen. The area shown measures 60 by 40 km. Image is taken from Google Maps.

[Title Page](#)

[Abstract](#)

[Introduction](#)

[Conclusions](#)

[References](#)

[Tables](#)

[Figures](#)

[⏪](#)

[⏩](#)

[⏴](#)

[⏵](#)

[Back](#)

[Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Fig. 2. Buoy 18 in the Westerscheldt is located near the town of Terneuzen. On this buoy a Trimble R7 GPS receiver is mounted inside the cage. The Trimble Zephyr (survey) antenna is installed on a range pole on top of the buoy. Note the eddies induced by the tidal current around the buoy.

13771

HESSD

10, 13743–13782, 2013

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



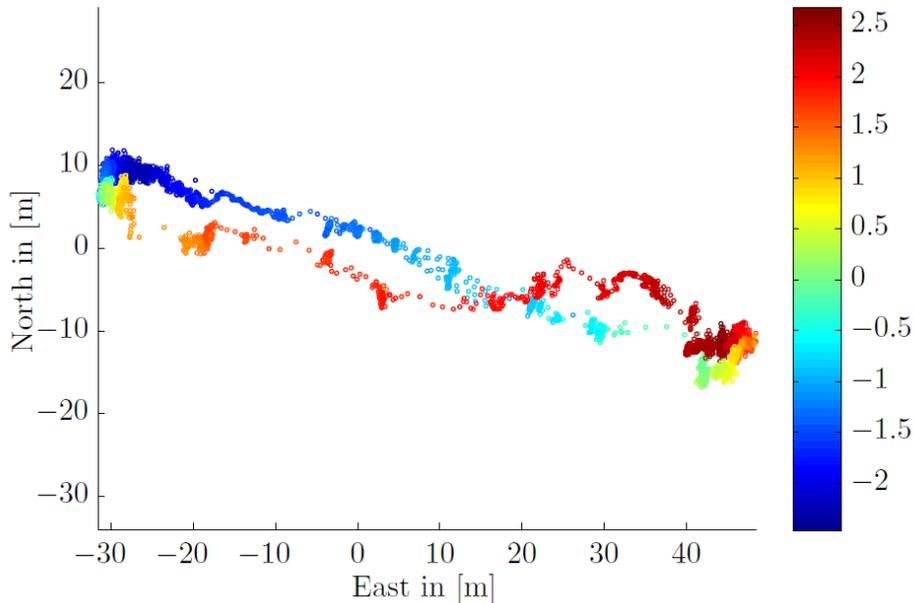


Fig. 3. Three-dimensional position estimates of buoy 18, during one complete tidal cycle from high water to high water on 2 July 2011, plot at a 60 s interval. The marker is color-coded after the elevation of the buoy in meters. The elevation is shown here with respect to the time-wise mean value. Note that the buoy only moves significantly in one direction. This is the dominant current direction, perpendicular to that only a small scale movement is observed. The origin represents the empirical mean of the position.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

[Title Page](#)

[Abstract](#) | [Introduction](#)

[Conclusions](#) | [References](#)

[Tables](#) | [Figures](#)

[⏪](#) | [⏩](#)

[◀](#) | [▶](#)

[Back](#) | [Close](#)

[Full Screen / Esc](#)

[Printer-friendly Version](#)

[Interactive Discussion](#)



Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

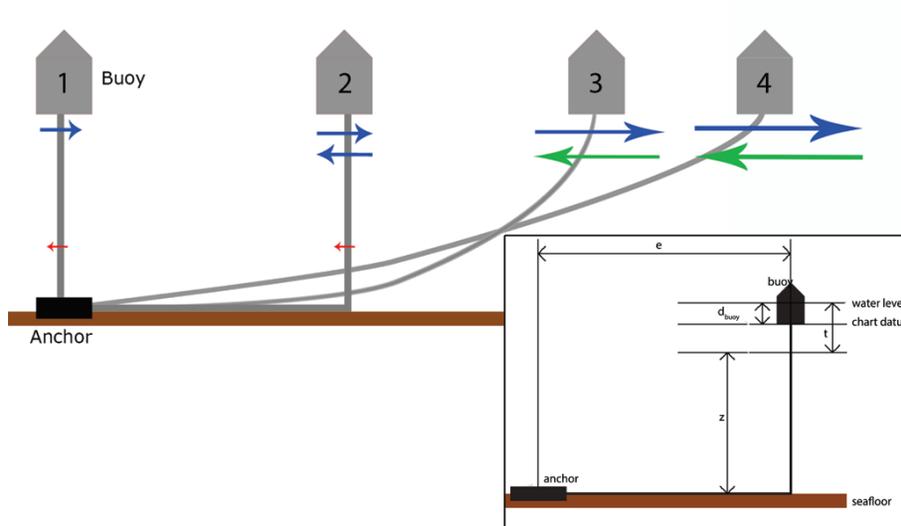


Fig. 4. Schematic representation of the maximum extension e during high water hw and low water lw; l_{chain} indicates the length of the anchor chain, z denotes the depth with regard to the chart datum, and t denotes the tidal elevation related to the chart datum. The buoy is shown in four critical positions. Blue arrows indicate the force created by the friction of the current on the buoy, this is the drag force. Red arrows indicate a drag force between the chain and the sea floor. Green arrows indicate an active spring force, created by the chain. The two blue arrows in position 2 indicate that during this position the current is changing its direction. Position 2 is the extension related to the the moment of slack tide.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

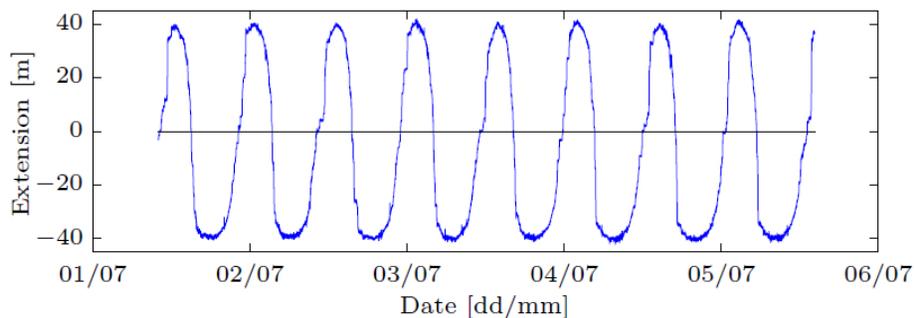


Fig. 5. This graph shows the extension of buoy 18 in the dominant current direction (main principle component) related to the centre point. The maximal extension during ebb and flood are approximately the same.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

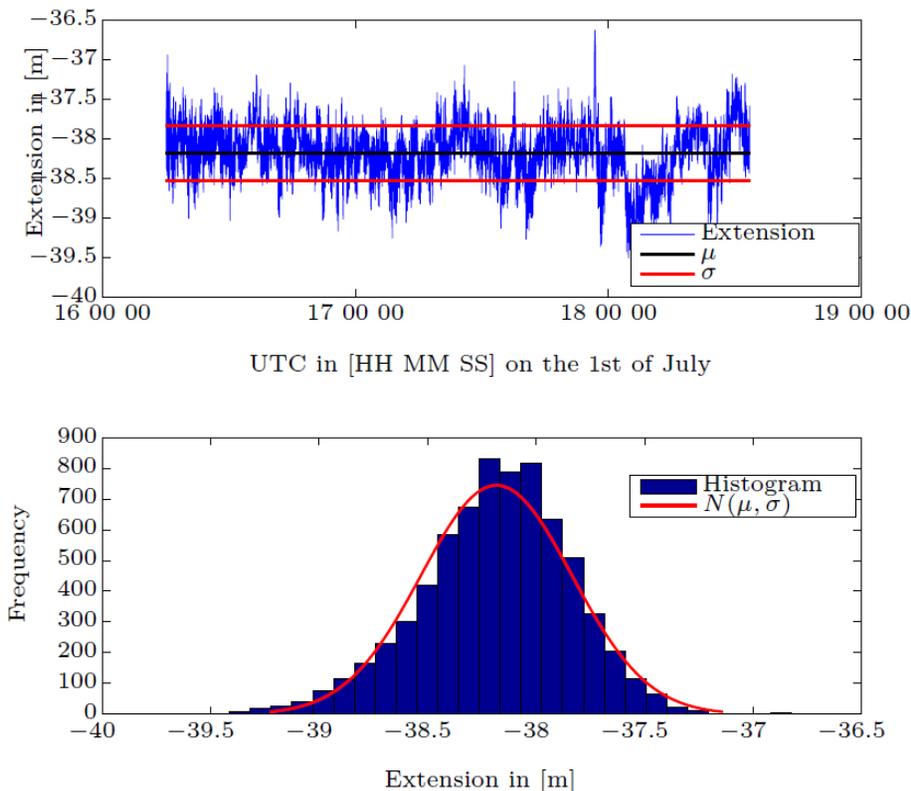


Fig. 6. Top: This graph shows the dynamics of buoy 18 on the 1 July 2011 during a period of zero net movement. The cm accurate GPS position estimates are projected onto the dominant current direction and plot against time. The mean and standard deviation about the mean have been determined ($\mu = -38.2$ m and $\sigma = 0.35$ m). The graph at bottom shows the histogram of the extension and a best fitting normal distribution.

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

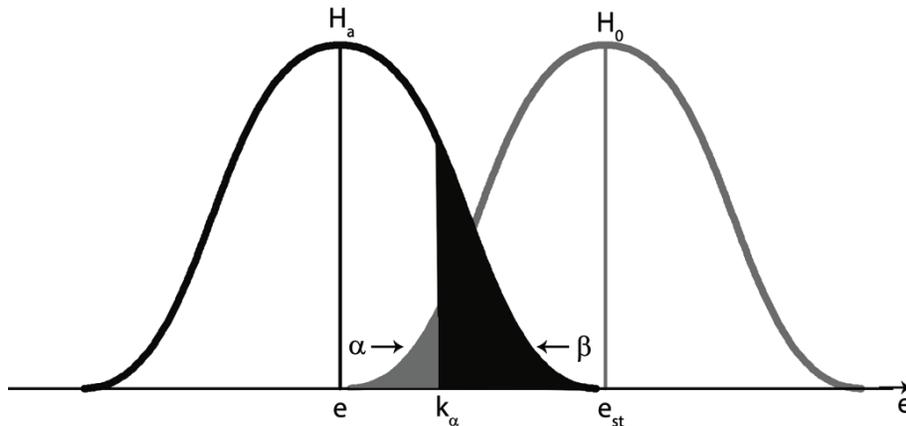


Fig. 7. Statistical hypothesis testing. The buoy is moving primarily in one direction, between two maximum extensions (by the anchor-chain). The slack-tide positions have been determined using Fig. 4. The uncertainty in the observed extension of the buoy is modeled through a distribution. Shown here is the situation for high water slack. The moment of slack tide is announced once the observed extension goes beyond the critical value/threshold k_α .

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

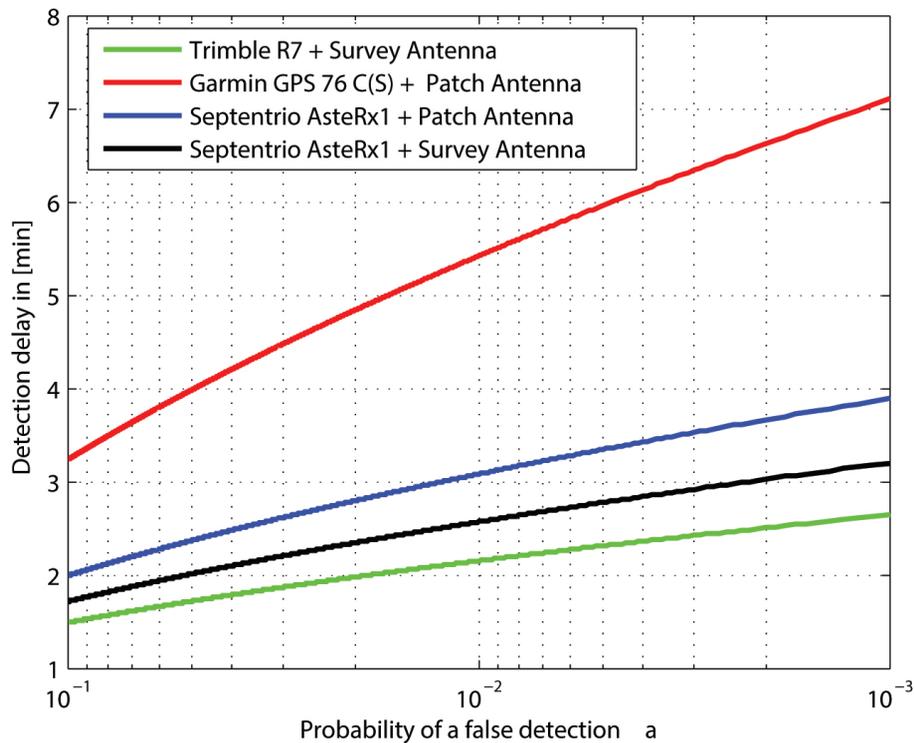


Fig. 8. This graph shows the detection delay as a function of the significance level, for various GPS receivers and operation modes. A small value for α indicates a higher significance and a smaller chance on a false alarm. However, a smaller value for α results in a larger detection delay.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[◀](#)
[▶](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)

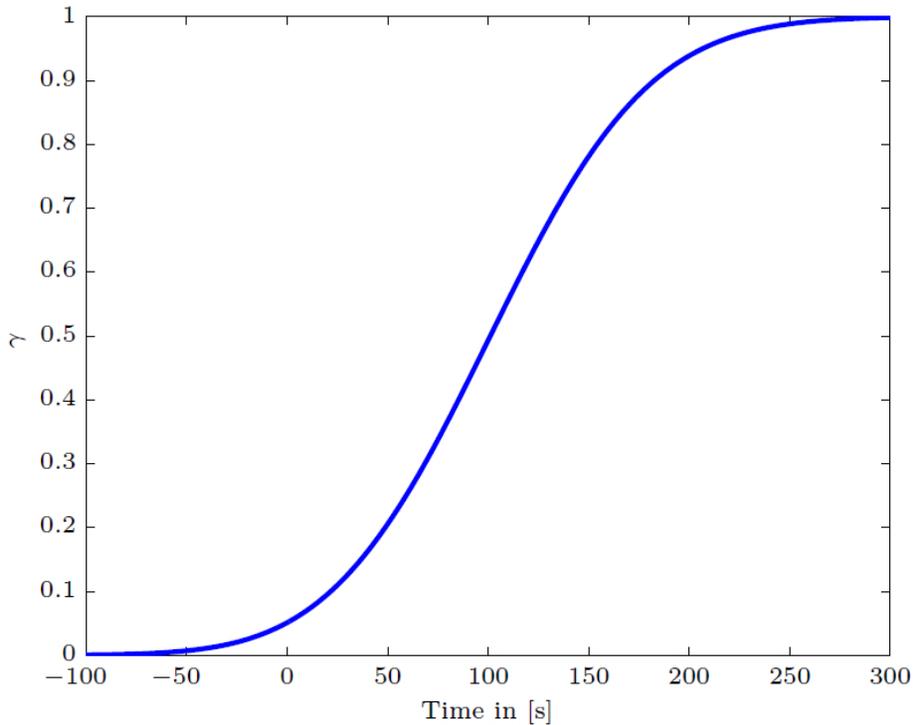


Fig. 9. This graph shows the probability of detection γ as a function of the detection delay in time. The level of significance is set at $\alpha = 0.05$. Zero detection delay corresponds to the very moment the observed extension e is equal to the extension related to slack tide e_{st} . At this particular moment $\alpha = \gamma$. As time progresses the probability of detection γ increases until $\gamma = 1$.

HESSD

10, 13743–13782, 2013

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

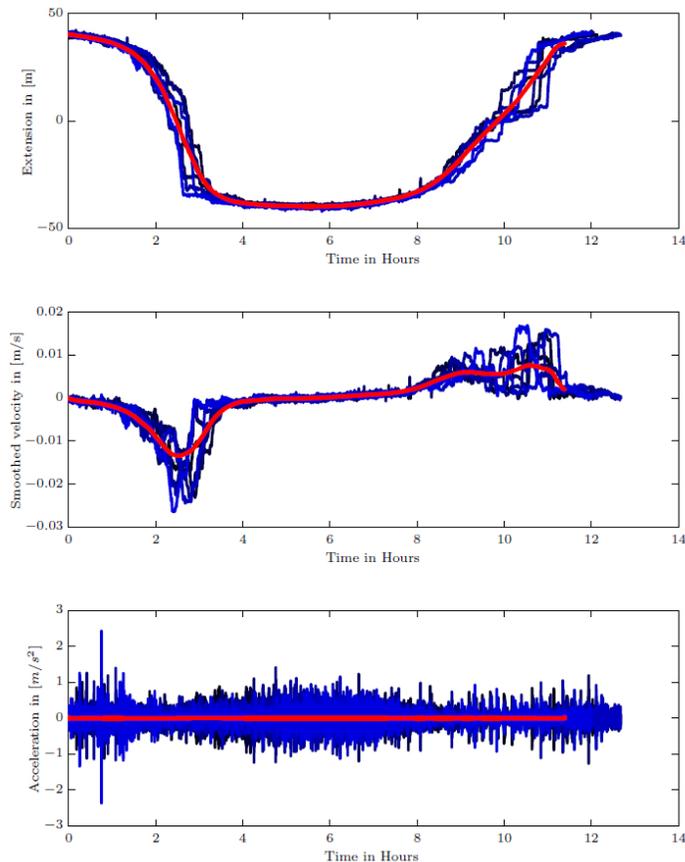


Fig. 11. The three graphs show the position, smoothed velocity and acceleration of the buoy during six complete tidal cycles. The blue lines, varying from light to dark blue, indicate the succeeding tidal cycles. The redline is obtained by taking the smoothed average of all observed tracks. Position estimates are obtained here with the ground-truth solution of the Trimble R7 receiver (at 1 Hz).

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

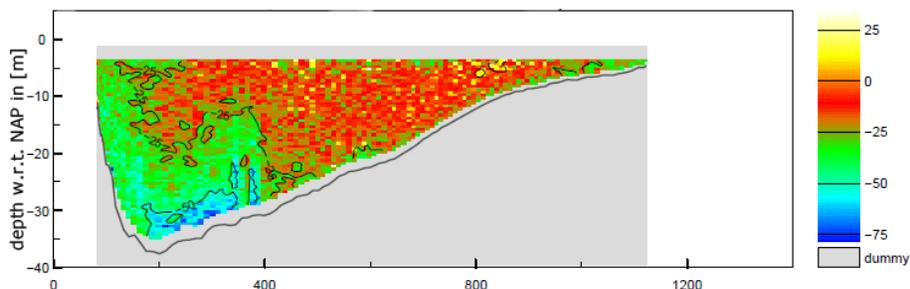


Fig. 12. Observed current velocity in cm s^{-1} in a cross-section of “De pas van Terneuzen” near buoy 18 on 6 July 2011 at 16:04 LT. Positive velocity values indicate an ebb current, and negative values indicate a flood current. At the bottom the flow is recently reversed, while on the surface the tide is still slacking. This illustrates the variability of the water current within a cross-section of the estuary (courtesy of RWS).

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Determining slack tide with a GPS receiver on an anchored buoy

M. Valk et al.

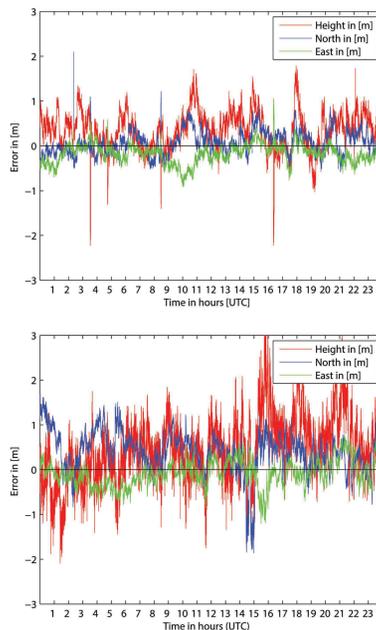


Fig. A1. Top: Position error plot of middle-class single frequency Septentrio AsteRx1 receiver with the PolaNt survey antenna in SBAS/EGNOS mode of operation, 24 h static test in Delft, on 3 May 2011. The North, East and Up position error components are plot against time. The mean values are 0.07, -0.18 and 0.35 m for North, East and Up; the standard deviations are 0.26 , 0.21 and 0.44 m, and the 95 % values 0.55 , 0.14 and 1.05 m. Bottom: Position error plot of Septentrio AsteRx1 receiver with the patch antenna in SBAS/EGNOS mode of operation, 24 h static test in Delft, on 8 August 2011. The North, East and Up position error components are plot against time. The mean values are 0.00 , -0.06 and 0.30 m for North, East and Up; the standard deviations are 0.77 , 0.49 and 1.16 m, and the 95 % values 1.08 , 0.52 and 1.69 m.

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[⏪](#)
[⏩](#)
[◀](#)
[▶](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)