



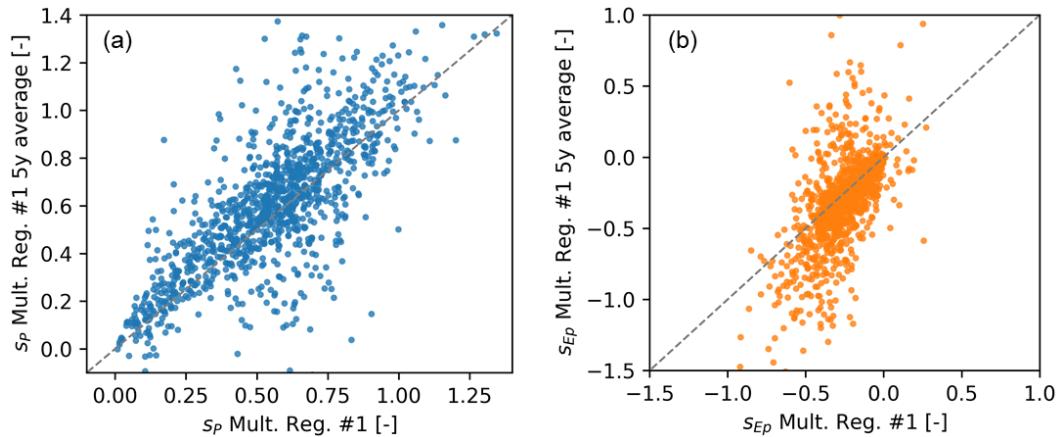
*Supplement of*

## **Uncertainty, temporal variability, and influencing factors of empirical streamflow sensitivities**

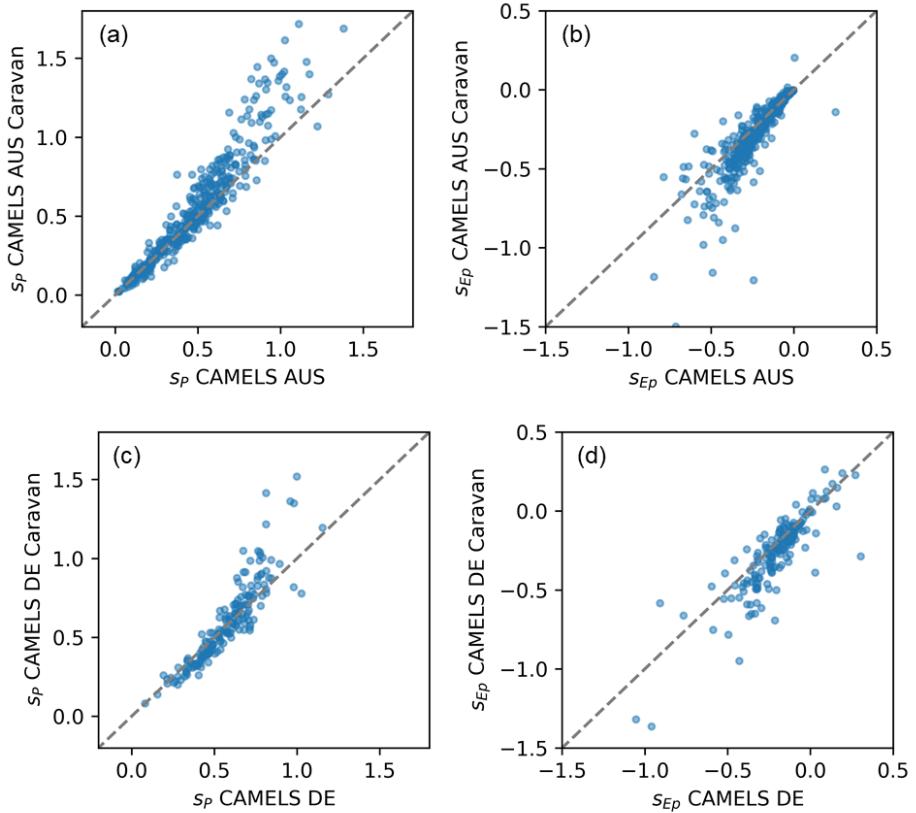
**Sebastian Gnann et al.**

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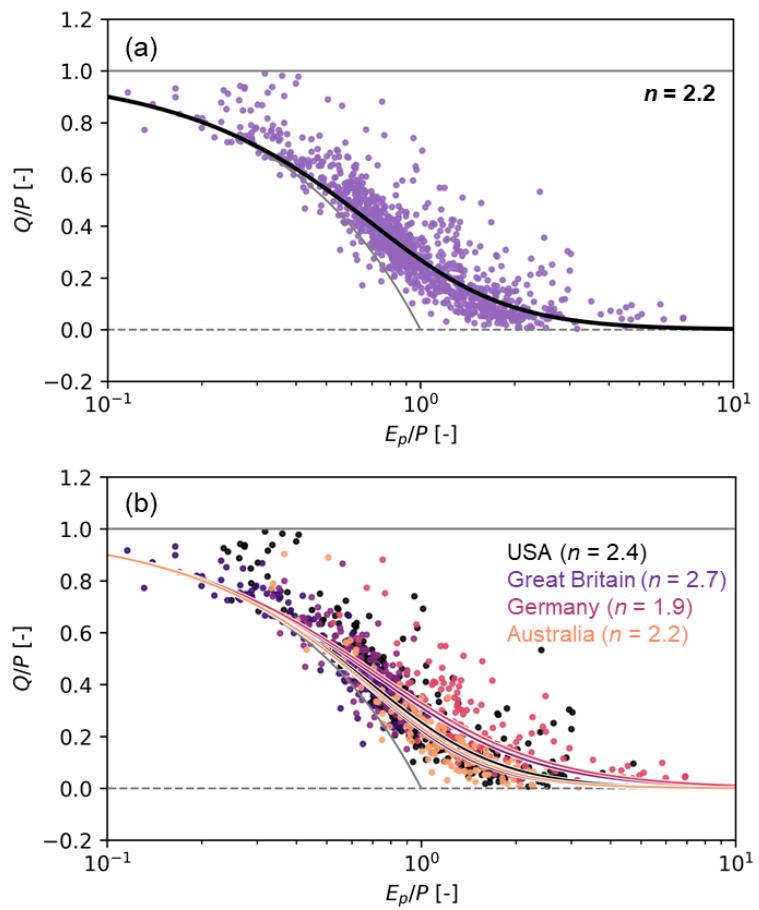
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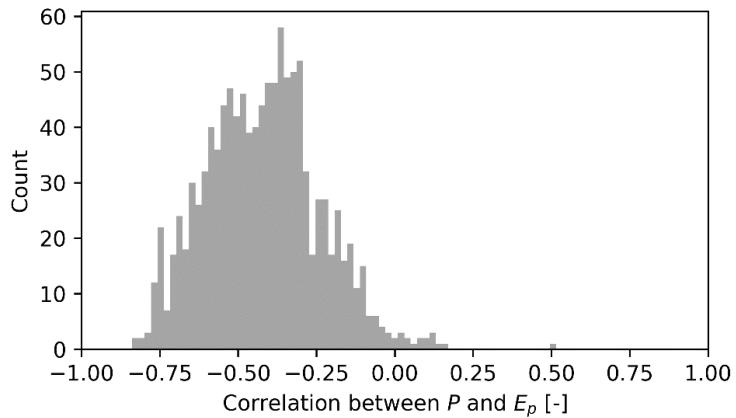
**Figure S1:** Comparison between estimated sensitivities using annual averages of  $P$  and  $E_p$  and estimated sensitivities using averages over non-overlapping 5-year blocks, both estimated using Multiple Regression #1. Panel (a) shows streamflow sensitivity to precipitation (Spearman correlation  $\rho_s = 0.74$ ) and panel (b) shows streamflow sensitivity to potential evaporation ( $\rho_s = 0.65$ ). The results broadly agree, though the sensitivities estimated using 5-year averages fall more often outside the theoretical range (e.g.,  $s_P > 1$  or  $s_{E_p} > 0$ ).



**Figure S2:** Comparison between sensitivities derived from national forcing products and Caravan forcing for (a) streamflow sensitivity to precipitation for CAMELS-AUS v2 ( $\rho_s = 0.97$ ), (b) streamflow sensitivity to potential evaporation for CAMELS-AUS v2 ( $\rho_s = 0.94$ ), (c) streamflow sensitivity to precipitation for CAMELS-DE ( $\rho_s = 0.94$ ), and (d) streamflow sensitivity to potential evaporation for CAMELS-DE ( $\rho_s = 0.86$ ).

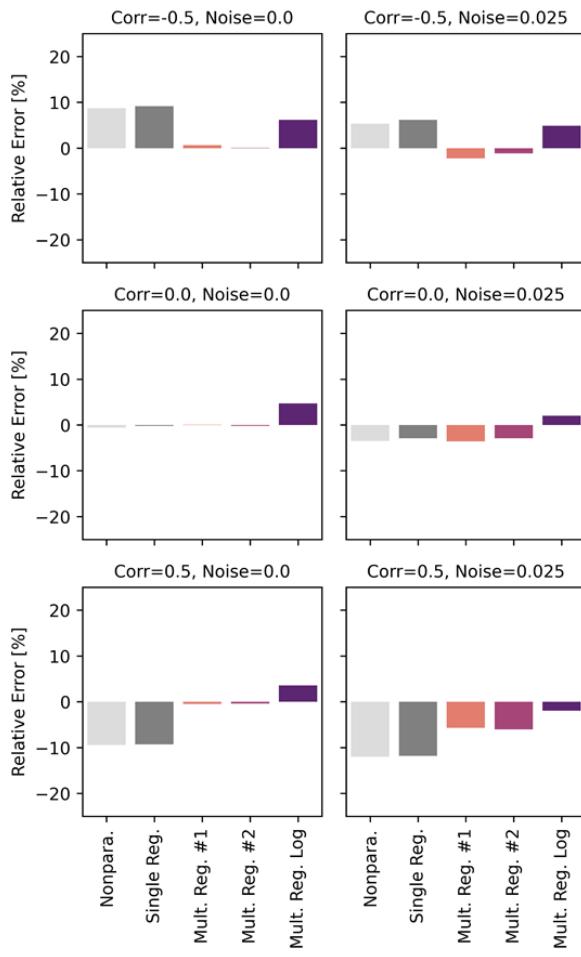


**Figure S3:** Budyko plots showing the Turc-Mezentsev model alongside the 1121 catchments analysed in the corresponding manuscript, with (a) the parameter  $n$  being calibrated to the entire dataset and (b) the parameter  $n$  being calibrated to each national dataset individually.

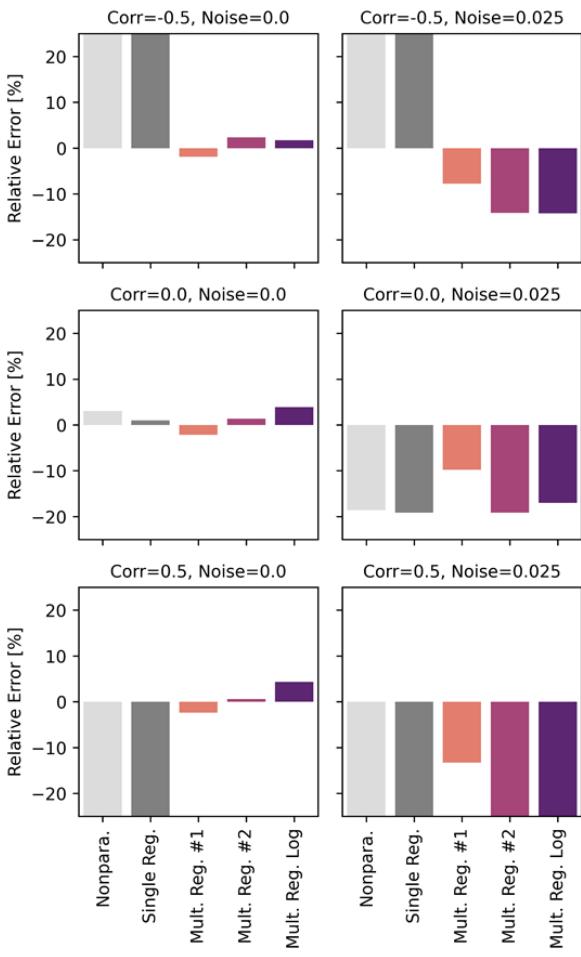


**Figure S4:** Pearson correlation  $\rho_p$  between precipitation and potential evaporation for the entire dataset (average = -0.42). Overall, 16 catchments (located in the US, Great Britain, and Germany) show a positive correlation between precipitation and potential evaporation.

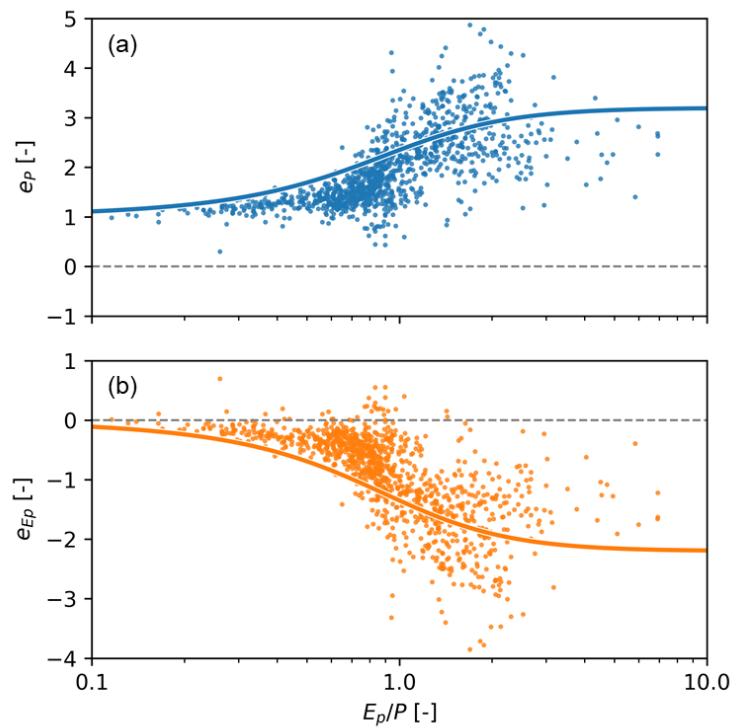
(a) Streamflow sensitivity to precipitation



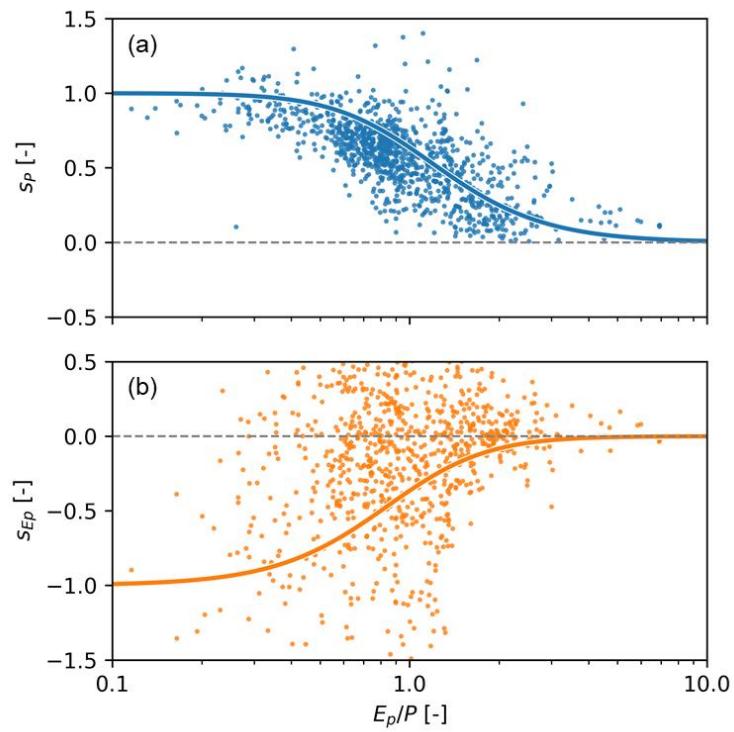
(b) Streamflow sensitivity to potential evaporation



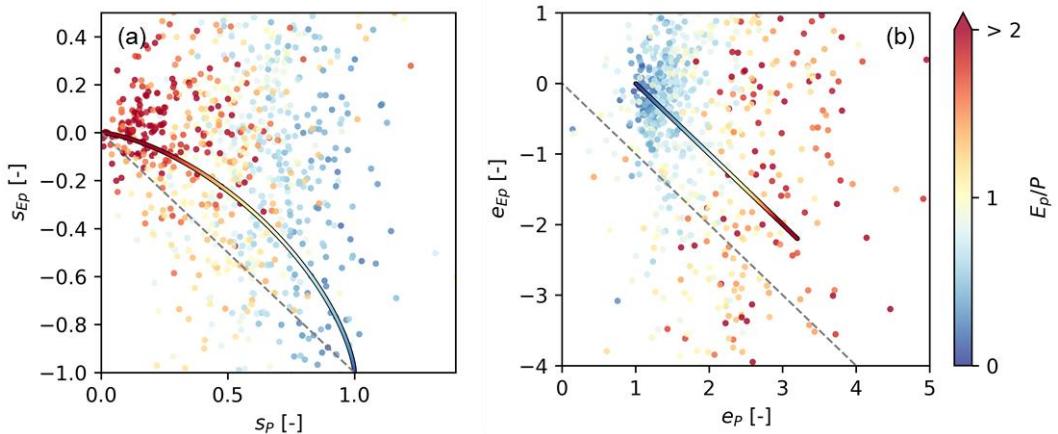
**Figure S5:** Average relative errors for the different estimation methods when applied to synthetic data with different degrees of correlation and noise. (a) Streamflow sensitivity to precipitation. (b) Streamflow sensitivity to potential evaporation. Note that the y-axes are capped for better visibility.



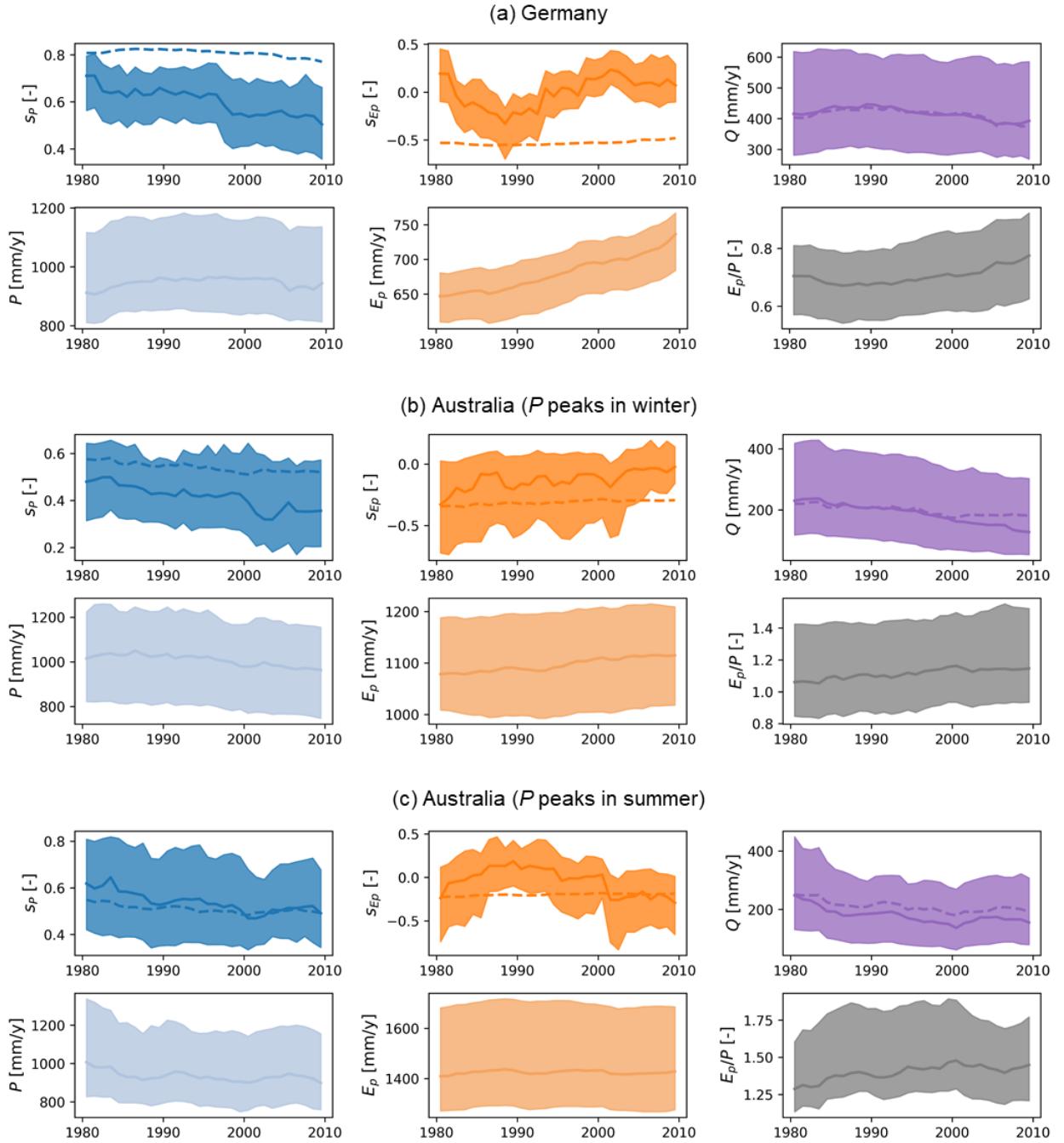
**Figure S6:** Streamflow elasticity to (a) precipitation and (b) potential evaporation, calculated using multiple regression #1 with observations from 1121 catchments. Both panels show empirically calculated values (dots) and theoretical values based on the Turc-Mezentsev model with  $n = 2.2$  (solid lines). Note that the y-axes are capped for better visibility.



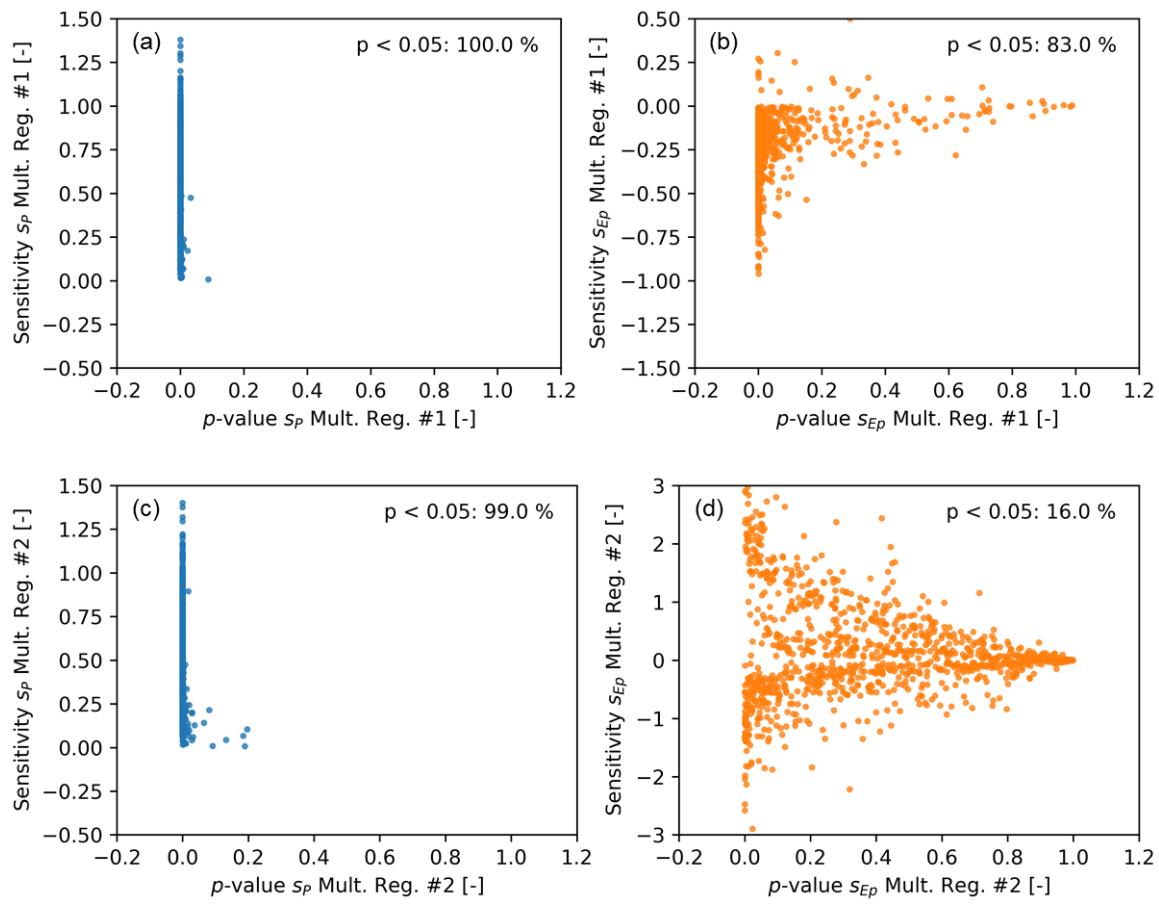
**Figure S7:** Streamflow sensitivity to (a) precipitation and (b) potential evaporation, calculated using multiple regression #2 with observations from 1121 catchments. Both panels show empirically calculated values (dots) and theoretical values based on the Turc-Mezentsev model with  $n = 2.2$  (solid lines). Note that the y-axes are capped for better visibility and thus not all catchments are shown.



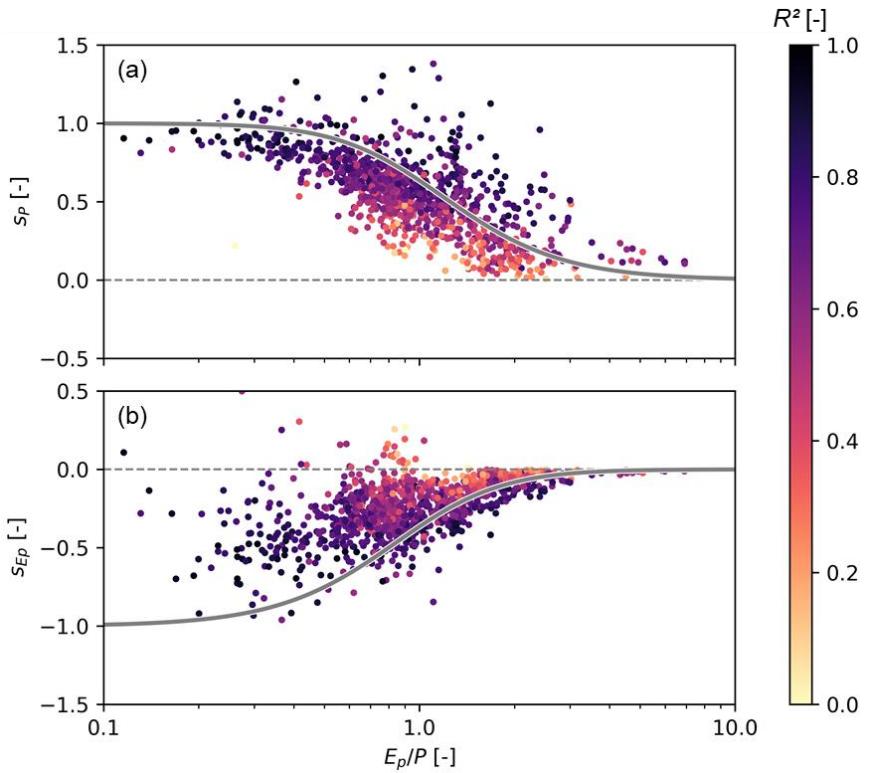
**Figure S8:** (a) Streamflow sensitivity to precipitation plotted against streamflow sensitivity to potential evaporation. (b) Streamflow elasticity to precipitation plotted against streamflow elasticity to potential evaporation. Both panels show empirically calculated values using multiple regression #2 (dots in the back) and theoretical values based on the Turc-Mezentsev model (line in front), coloured according to the aridity index. The grey dashed line starts at the origin and has a slope of -1, so that values plotting above it imply that  $s_P > s_{EP}$  (a) and  $e_P > e_{EP}$  (b).



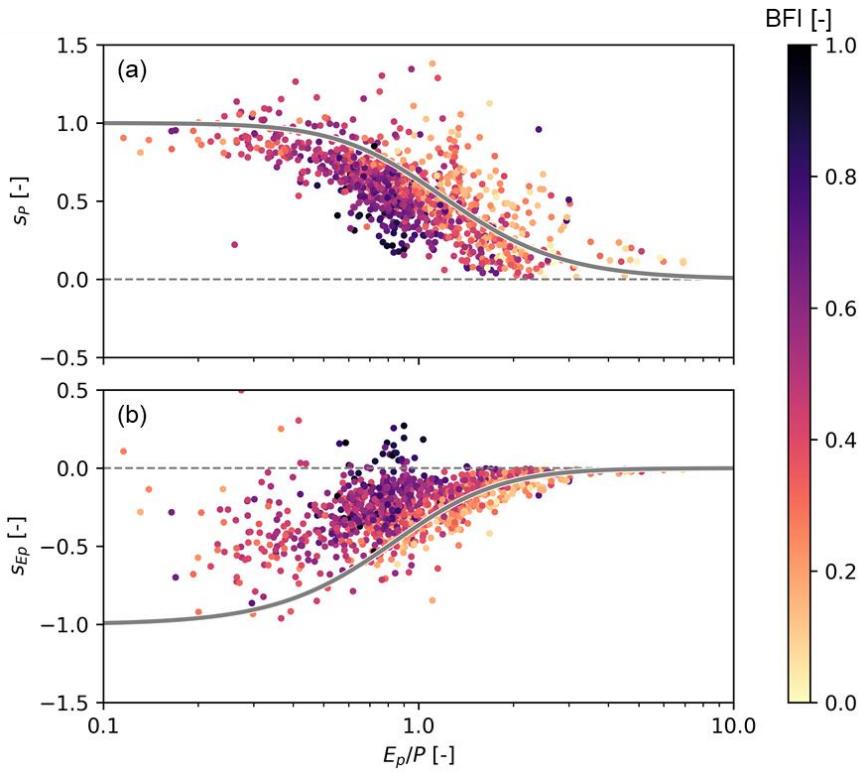
**Figure 9:** Change of streamflow sensitivities and other variables over time for (a) 144 catchments in Germany, (b) 100 catchments in Australia with most precipitation falling in winter ( $P_S < 0$ ), and (c) 109 catchments in Australia with most precipitation falling in summer ( $P_S > 0$ ). Shaded areas indicate the 25<sup>th</sup> and 75<sup>th</sup> percentiles and thick lines indicate the median of all catchments. Dashed lines indicate the trends calculated with the Turc-Mezentsev model for the sensitivities and  $Q$  based on observed  $P$  and  $E_P$  data and using a calibrated value of  $n = 1.9$  for (a),  $n = 1.7$  for (b) and  $n = 2.6$  for (c). Sensitivities are calculated using method #1 over 20-year blocks with the middle year shown (e.g., 1980 indicates a block from 1970 to 1990).



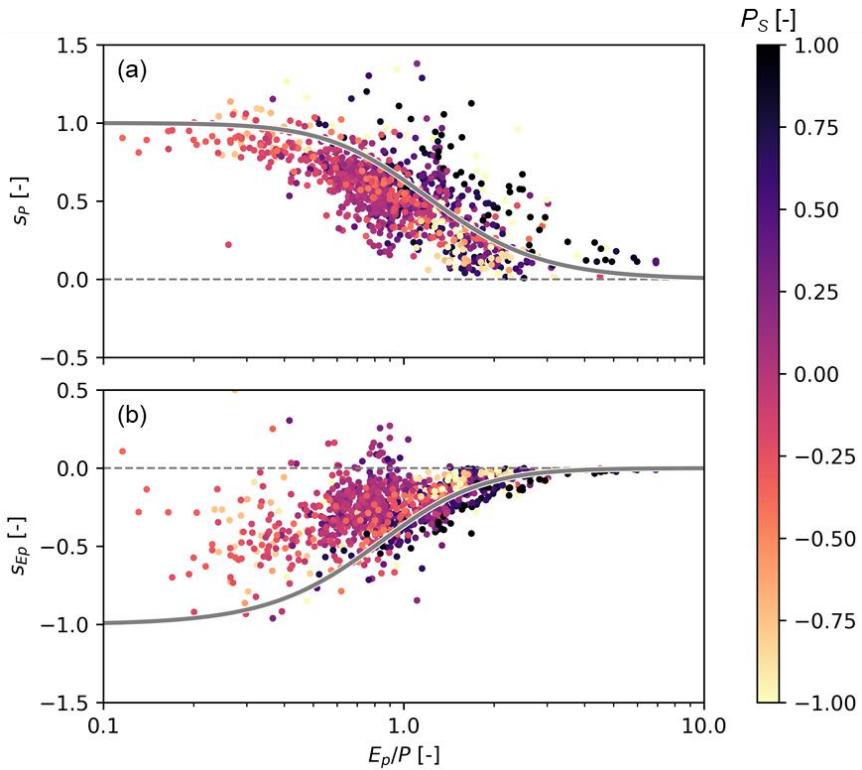
**Figure S10:** Scatter plot showing  $p$ -values against their regression coefficients (i.e., sensitivities) for multiple regression methods #1 (a, b) and #2 (c, d).



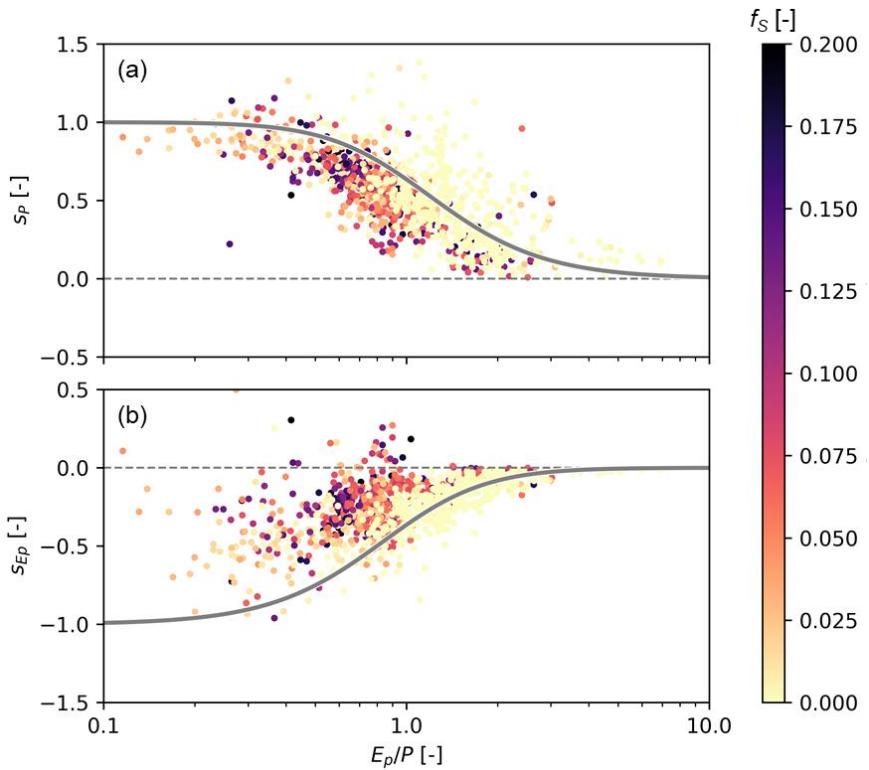
**Figure S11:** Streamflow sensitivity to precipitation (a) and potential evaporation (b) calculated using multiple regression method #1 with observations from 1121 catchments, coloured according to  $R^2$ . Both panels show empirically calculated values (dots) and theoretical values based on the Turc-Mezentsev model (dashed lines). Note that the y-axes are capped for better visibility. Spearman rank correlation  $\rho_S$  between  $R^2$  and relative deviation from the Turc-Mezentsev curve is 0.60 for  $s_P$  and 0.25 for  $s_{E_p}$ .



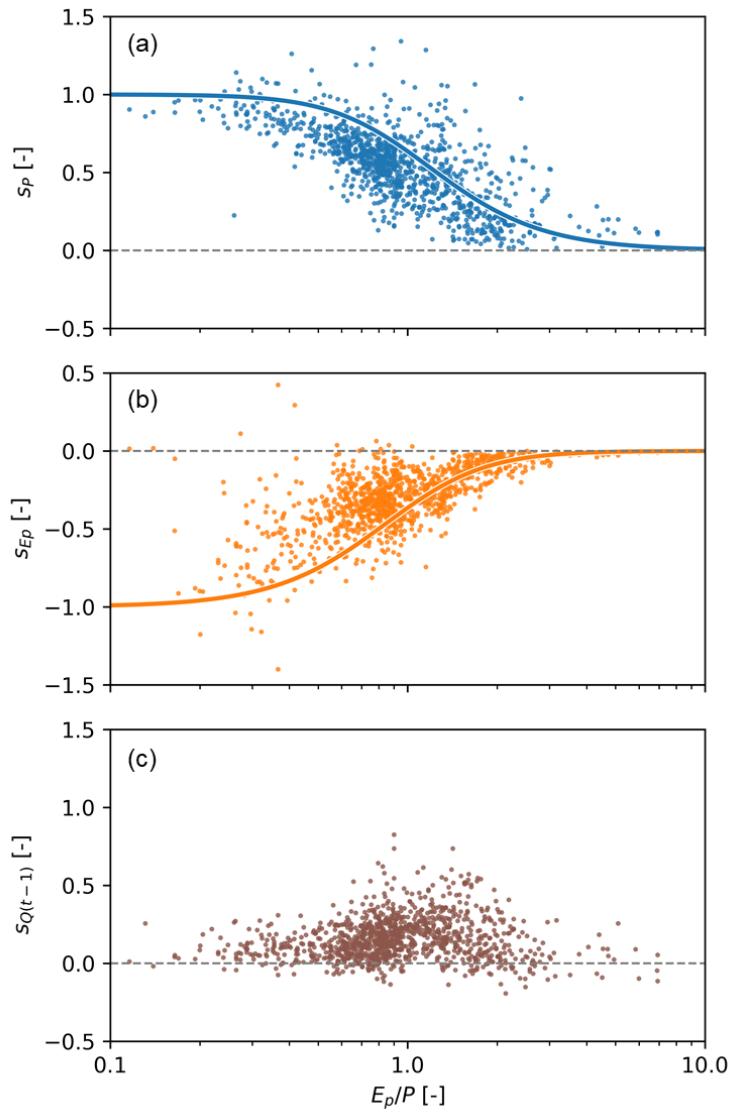
**Figure S12:** Streamflow sensitivity to precipitation (a) and potential evaporation (b) calculated using multiple regression method #1 with observations from 1121 catchments, coloured according to the baseflow index (BFI). Both panels show empirically calculated values (dots) and theoretical values based on the Turc-Mezentsev model (dashed lines). Note that the y-axes are capped for better visibility. Spearman rank correlation  $\rho_S$  between BFI and relative deviation from the Turc-Mezentsev curve is -0.41 for  $s_p$  and -0.44 for  $s_{E_p}$ .



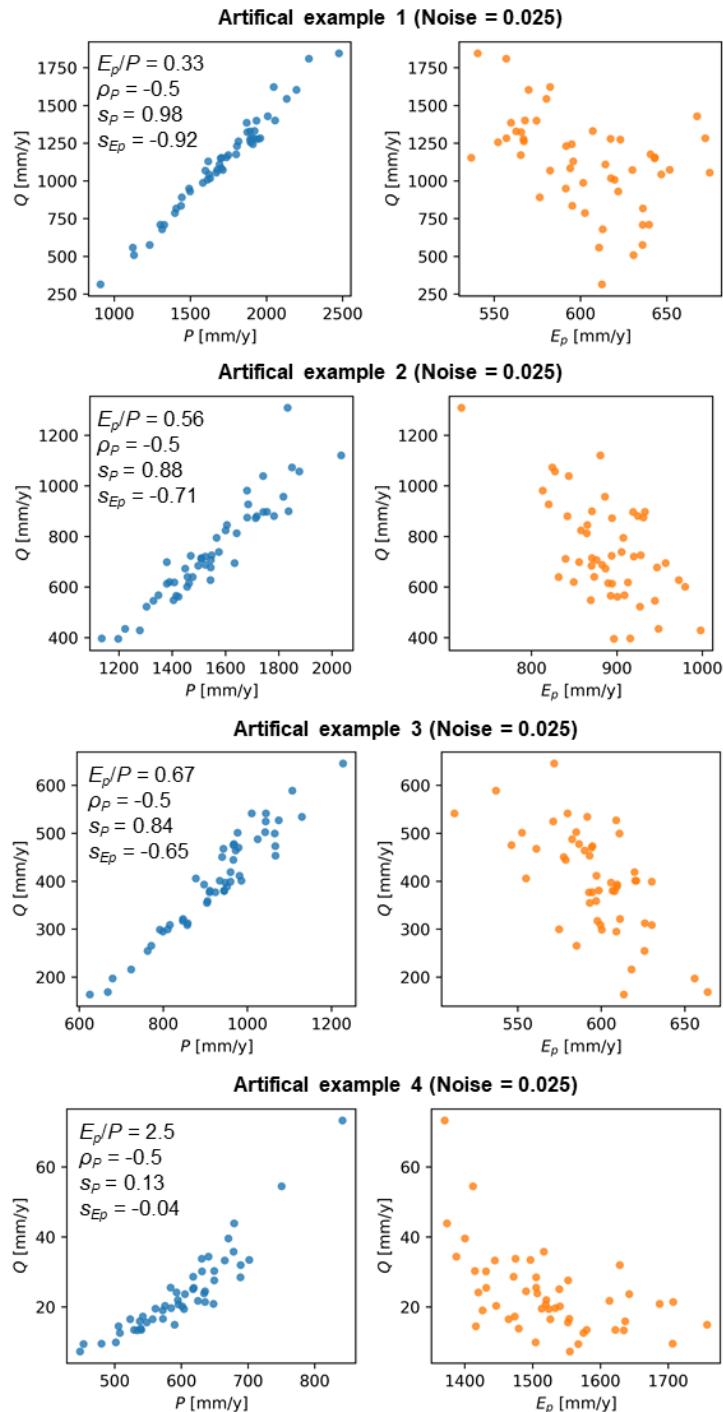
**Figure S13:** Streamflow sensitivity to precipitation (a) and potential evaporation (b) calculated using multiple regression method #1 with observations from 1121 catchments, coloured according to precipitation seasonality  $P_s$ . Both panels show empirically calculated values (dots) and theoretical values based on the Turc-Mezentsev model (dashed lines). Note that the y-axes and the colour scale are capped for better visibility. Spearman rank correlation  $\rho_s$  between  $P_s$  and relative deviation from the Turc-Mezentsev curve is 0.09 for  $s_P$  and 0.20 for  $s_{E_p}$ .



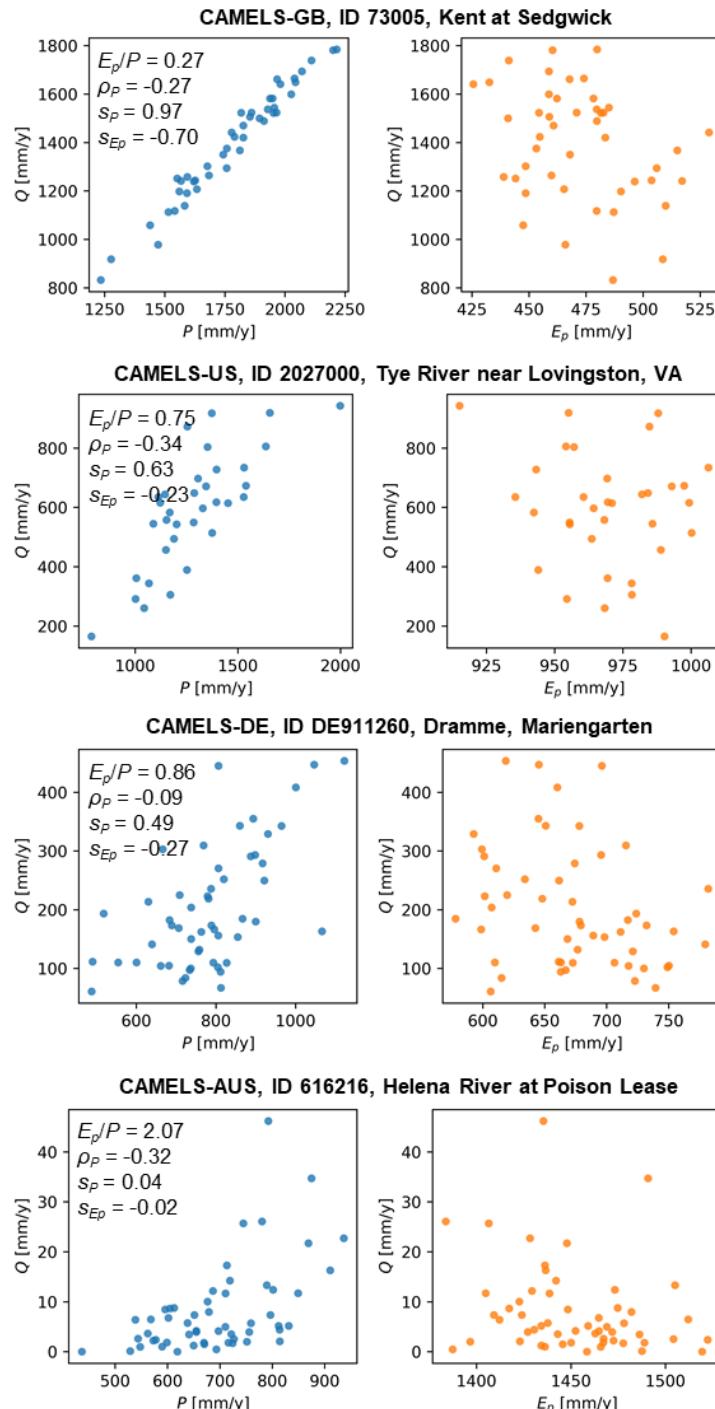
**Figure S14:** Streamflow sensitivity to precipitation (a) and potential evaporation (b) calculated using multiple regression method #1 with observations from 1121 catchments, coloured according to snow fraction  $f_s$ . Both panels show empirically calculated values (dots) and theoretical values based on the Turc-Mezentsev model (dashed lines). Note that the y-axes are capped for better visibility. Spearman rank correlation  $f_s$  between  $P_s$  and relative deviation from the Turc-Mezentsev curve is -0.31 for  $s_P$  and -0.46 for  $s_{Ep}$ .



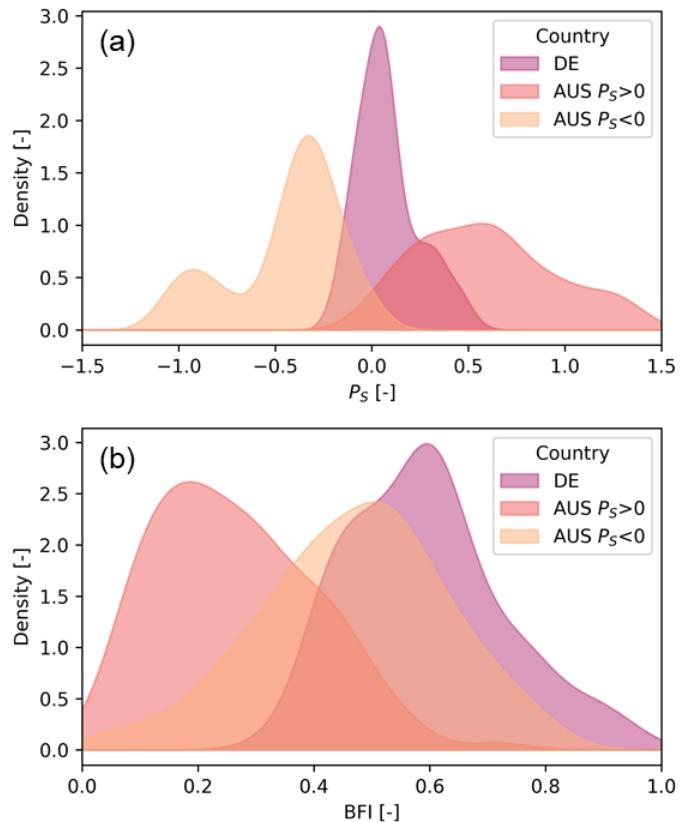
**Figure S15:** Streamflow sensitivity to precipitation  $s_P$  (a), potential evaporation  $s_{Ep}$  (b), and (c) storage  $s_{Q(t-1)}$  (using previous year's streamflow  $Q(t-1)$  as a proxy), calculated using multiple regression method #1 with observations from 1121 catchments, but now with an additional storage predictor. Both panels show empirically calculated values (dots) and theoretical values based on the Turc-Mezentsev model (dashed lines). Note that the y-axes are capped for better visibility. The median  $R^2$  for the storage model leads to a slight improvement from 0.65 to 0.69, suggesting that it can explain a larger proportion of the variation in the data, while the values for  $s_P$  and  $s_{Ep}$  remain relatively stable.



**Figure S16:** Scatter plots showing  $P$  vs.  $Q$  and  $E_p$  versus  $Q$  of 4 artificial catchments created using the Turc-Mezentsev model (with noise and a correlation between  $P$  and  $E_p$  of -0.5), as well as the corresponding sensitivities. The catchments are ordered based on the aridity index.



**Figure S17:** Scatter plots showing  $P$  versus  $Q$  and  $E_p$  versus  $Q$  of 4 catchments, as well as the corresponding correlation between  $P$  and  $E_p$  and the sensitivities, estimated using Multiple Regression #1. The catchments are ordered based on the aridity index.



**Figure S18:** Distributions of precipitation seasonality (a) and baseflow index (b) based on a Gaussian kernel density (KDE) estimation for the German catchments and the two Australian subsets used for the trend analysis.  $P_S < 0$  indicates catchments where most precipitation falls in winter and  $P_S > 0$  indicates catchments where most precipitation falls in summer. Note that there is some overlap for the two Australian  $P_S$  distributions due to the use of KDE.

**Table S1:** Absolute and relative trends of streamflow sensitivities. Relative trends are normalised with the value from the first year. Note that all relative trends indicate a decrease in magnitude, but are reported as positive numbers for the sake of simplicity.

	Empirical [-/50y]	Analytical [-/50y]	Empirical [%/50y]	Analytical [%/50y]
<b>Germany</b>				
$s_P$	-0.16	-0.04	26	5
$s_{Ep}$	+0.16	+0.06	70	11
<b>Australia (most <math>P</math> in winter)</b>				
$s_P$	-0.18	-0.09	40	18
$s_{Ep}$	+0.11	+0.08	49	26
<b>Australia (most <math>P</math> in summer)</b>				
$s_P$	-0.11	-0.03	15	8
$s_{Ep}$	+0.04	+0.03	15	15